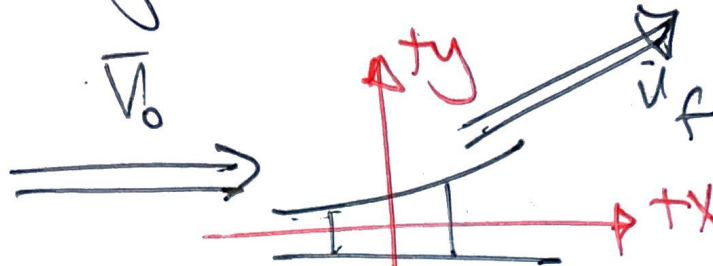


Given

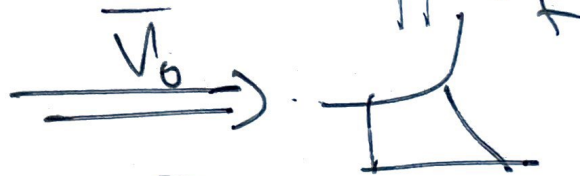
(a)



$$V_0 = V_f = 40 \text{ m/s}$$

$$\frac{dm}{dt} = 30 \text{ kg/s}$$

(b)

Req'd: \vec{F}_{blade} (c)

Assump speed/flow
are both constant

Strategy

$$\vec{F} = - \frac{dm}{dt} \vec{V}_{\text{flow}}$$

Estimate = (a) should give most "forward" force

all will be in range of $30 \frac{\text{kg}}{\text{s}} \cdot 40 \frac{\text{m}}{\text{s}} = \underline{1200 \text{ N}}$

Soln (a) tracking the signs is the challenge here!

$$\vec{V}_f = +40 \text{ m/s} \hat{i}$$

$$\frac{dm}{dt} = -\frac{30 \text{ kg}}{\text{s}}$$

$$\vec{V}_{\text{flow}} = 40 \cos 45^\circ \hat{i} + 40 \sin 45^\circ \hat{j}$$

28.28

$$\frac{dm}{dt} = \frac{30 \text{ kg}}{\text{s}}$$

Centering!!

$$\vec{F}_{\text{in}} = -\left(-\frac{30 \text{ kg}}{\text{s}}\right)(40 \text{ m/s} \hat{i}) = 1200 \text{ N} \hat{i}$$

$$\vec{F}_{\text{out}} = -\left(\frac{30 \text{ kg}}{\text{s}}\right)(28.3 \text{ m/s} \hat{i} + 28.3 \text{ m/s} \hat{j}) = -849 \hat{i} - 849 \hat{j} \text{ N}$$

$$\vec{F}_{\text{net}} = \vec{F}_{\text{in}} + \vec{F}_{\text{out}} = 1200 \text{ N} \hat{i} + (-849 \hat{i} - 849 \hat{j}) \text{ N}$$

$$\boxed{\vec{F}_{\text{net}} = 351 \hat{i} - 849 \hat{j}}$$

Soln: cont (b)(c)

(b)
 $V = +40 \text{ J}$
 $\frac{dm}{dt} = +30 \frac{\text{kg}}{\text{s}}$



(same)

$$\vec{F}_{in} = 1200 \text{ N } \hat{i} \text{ (from before)}$$

$$\vec{F}_{out} = -\left(\frac{30 \text{ kg}}{\text{s}}\right)(40 \text{ J}) = -1200 \text{ N } \hat{i}$$

$$\Rightarrow \vec{F}_{net} = 1200 \text{ N } \hat{i} - 1200 \text{ N } \hat{i}$$

(c)
 $V = -40 \text{ J}$
 $\frac{dm}{dt} = 30 \frac{\text{kg}}{\text{s}}$
 same

$$\vec{F}_{in} = 1200 \text{ N } \hat{i}$$

$$\vec{F}_{out} = -\left(\frac{30 \text{ kg}}{\text{s}}\right)\left(-40 \frac{\text{m}}{\text{s}}\right) \hat{i}$$

$$= 1200 \text{ N } \hat{i}$$

$$\vec{F}_{net} = \vec{F}_{in} + \vec{F}_{out}$$

$$= 2400 \text{ N } \hat{i}$$

Discussion: Matches conceptual thinking (and back of book) and now I feel more comfortable w/ the sign conventions!