1. Introduction

MOCHIS is a software that allows the user to perform flexible non-parametric tests of differential gene expression. Such tests include the popular Mann-Whitney (Wilcoxon rank sum) test, which was recently promoted by Li et al. (2022) as an approach to perform differential analysis on RNA-seq data without incurring an inflated false positive rate. In this markdown document, we explore how MOCHIS can detect multiple kinds of differential gene expression signatures, including mean shifts or dispersion shifts. Dispersion shifts have recently been shown to characterize age-related changes in gene expression (see Schaum et al., 2020 and Yamamoto and Chung et al., 2022+). In particular, we:

- perform multiple kinds of two-sample tests on all single-cell tissue data provided in Tabula muris senis
- report and compare findings across the different kinds of tests For Section 3 (Analysis), all our analyses are followed by a summary of key findings, to help the reader quickly grasp the main points.

```
import scanpy
import numpy as np
import anndata
import pandas as pd
import matplotlib.pyplot as plt
from main_draft0 import *
import scipy
import statistics
import csv
import os
import seaborn as sns
from matplotlib_venn import venn2
import math

np.random.seed(2022)
```

2. Data

Publicly available *mus musculus* (house mice) single-cell RNA-seq data from the Chan-Zuckerberg Initiative (also known as *Tabula Muris Senis*) is used. We download senescence datasets from https://cellxgene.cziscience.com/collections/0b9d8a04-bb9d-44da-aa27-705bb65b54eb). These datasets are made up of single cell gene transcript levels measured using Smart-Seq2, across 22 distinct mice tissues. For each tissue, the cells originate from mice that are either 3 months, 18 months or 24 months old (with the exception of the mammary gland tissue, which has 3 months, 18 months and 21 months). There are also other cell labels like tissue location (identified with guidance from biologists) and mice sex.

Below, we perform the Mann-Whitney test to identify genes that are differentially expressed, also known as differentially expressed genes (DEGs), across age groups. We compare each pair of age group, so that for each gene $\binom{3}{2} = 3$ tests are performed.

We restrict our analysis to those regions where the zero counts are the fewest, using an 80% cut-off. This avoids running tests on genes that have pronounced zero inflation, which hinders the detection of differential expression.

We additionally compute a "ratio of variances" index, which heuristic measures of the difference in dispersion across the pair of age groups. The larger the ratio of variances, the more differentially dispersed the gene expression between the pair of age groups.

```
In [2]: |%%capture
        # Perform analysis for each tissue
        # There are 22 tissues
        all_tissues = sorted(["bone-marrow",
                      "brain-myeloid",
                      "heart",
                      "large-intestine",
                      "lung",
                      "skin-of-body",
                      "thymus",
                      "limb-muscle",
                      "spleen",
                      "subcutaneous-adipose-tissue",
                      "tongue",
                      "gonadal-fat-pad",
                      "pancreas",
                      "mammary-gland",
                      "trachea",
                      "mesenteric-fat-pad",
                      "liver",
                      "bladder-lumen",
                      "brown-adipose-tissue",
                      "diaphragm",
                      "kidney",
                      "aorta"])
        for tissue in all tissues:
            #os.mkdir(os.path.join("tissues/", tissue))
            tissue smartseq2 data = scanpy.read h5ad('tissues/' + tissue + '.h5ad')
            transcripts = tissue smartseq2 data.var.n cells.index
            ages = np.array(tissue smartseq2 data.obs['age'].index)
            smartseq2 raw counts = tissue smartseq2 data.raw.X.toarray()
            #print(smartseq2 raw counts.shape) # 14517 mice cells x 21069 regions
            # Get cutoff and restrict to only those genes
            cutoff = round(0.8*smartseq2 raw counts.shape[0])
            cell count sums by region = np.count nonzero(smartseg2 raw counts, axis
            highly_expressed_genes_indices = [i for i,v in enumerate(cell count sum
            smartseq2 high exp sparse mat = []
            for i in highly expressed genes indices:
                smartseq2 high exp sparse mat.append(smartseq2 raw counts[:, i])
            print("Found ", len(highly expressed genes indices), " genes out of ",
            highly expressed transcripts = [transcripts[i] for i in highly expresse
            # Grab age labels
            #smartseq2 df = anndata.AnnData(np.transpose(smartseq2 high exp sparse
            smartseq2 df = pd.DataFrame(np.append(np.transpose(smartseq2 high exp s
            # Run Mann-Whitney test for genes
```

```
gene_names = smartseq2_df.columns.values[:-1]
results_df = pd.DataFrame(columns=['TRANSCRIPT', 'MANN_WHITNEY_3_18'
print("How many cells of each age group?")
print(smartseq2_df['ages'].value_counts())
# Run test for each gene
for i in range(len(gene_names)):
   to run test = smartseq2 df[[gene names[i], 'ages']]
   if tissue == "mammary-gland":
       print("Reminder that mammary-gland has 3m, 18m and 21m age grou
        age 3m = to run_test.loc[to run_test["ages"] == "3m", gene_name
        age 18m = to run_test.loc[to_run_test["ages"] == "18m", gene_na
        age 24m = to run_test.loc[to_run_test["ages"] == "21m", gene_na
   else:
        age 3m = to run test.loc[to run test["ages"] == "3m", gene name
        age 18m = to run test.loc[to run test["ages"] == "18m", gene na
        age 24m = to run test.loc[to run test["ages"] == "24m", gene na
   age_3m = [float(i) for i in age_3m]
   age_18m = [float(i) for i in age_18m]
   age_24m = [float(i) for i in age_24m]
   wrs_test_3_18 = scipy.stats.mannwhitneyu(x=age_3m, y=age_18m, alter
   wrs test_18_24 = scipy.stats.mannwhitneyu(x=age_18m, y=age_24m, alt
   wrs test 24 3 = scipy.stats.mannwhitneyu(x=age 3m, y=age 24m, alter
   var 3 18 = max(statistics.variance(age 3m)/statistics.variance(age
   var_18_24 = max(statistics.variance(age_18m)/statistics.variance(ag
   var 24 3 = max(statistics.variance(age 24m)/statistics.variance(age
   results df = results df.append({
        'TRANSCRIPT': gene names[i],
        'MANN WHITNEY 3 18': wrs test 3 18.pvalue,
        'MANN_WHITNEY_18_24': wrs_test_18_24.pvalue,
        'MANN WHITNEY 24 3': wrs test 24 3.pvalue,
        'VAR_3_18': var 3 18,
        'VAR 18 24': var 18 24,
        'VAR_24_3': var 24 3
    }, ignore index=True)
print("Saving results for ", tissue)
results df.to csv("tissues/"+tissue+"/p val table.csv")
```

2.1 Mann-Whitney DEGs

Given we have the tables of p-values and ratios of variances from the previous step, we now select genes whose p-values, after a Benjamini-Hochberg adjustment procedure, lie below or equal to a 0.05 significance level. These are Mann-Whitney significant genes that would be flagged as

potentially carrying biological signal in a typical differential expression analysis procedure.

```
In [3]: def p_adjust_bh(p):
    """Benjamini-Hochberg p-value correction for multiple hypothesis testin
    p = np.asfarray(p)
    by_descend = p.argsort()[::-1]
    by_orig = by_descend.argsort()
    steps = float(len(p)) / np.arange(len(p), 0, -1)
    q = np.minimum(1, np.minimum.accumulate(steps * p[by_descend]))
    return q[by_orig]
```

```
In [4]: tissue transcript 3 18 = pd.DataFrame(columns=['TRANSCRIPT', 'MANN WHITNEY'
        tissue transcript 18 24 = pd.DataFrame(columns=['TRANSCRIPT', 'MANN WHITNEY
        tissue_transcript_24_3 = pd.DataFrame(columns=['TRANSCRIPT', 'MANN_WHITNEY'
        for tissue in all tissues:
            print("Reading in summary of p-values and ratios of variances for ", ti
            tissue mann whitney df = pd.read csv("tissues/"+tissue+"/p val table.cs
            # Pick genes where one of the three pairs (3m, 18m, 24m) has significan
            selected genes 3 18 = tissue mann whitney df[p adjust bh(tissue mann wh
            selected genes 3 18 = selected genes 3 18[["TRANSCRIPT", "MANN WHITNEY
            selected_genes_3_18= selected_genes_3_18.rename(columns={"MANN_WHITNEY"
            selected genes 3 18["TISSUE"] = [tissue for i in range(selected genes 3
            tissue transcript 3 18 = pd.concat([tissue transcript 3 18, selected ge
            selected genes 18 24 = tissue mann whitney df[p adjust bh(tissue mann w
            selected genes 18 24 = selected genes 18 24[["TRANSCRIPT", "MANN WHITNE
            selected genes 18 24 = selected genes 18 24.rename(columns={"MANN WHITN
            selected genes 18 24["TISSUE"] = [tissue for i in range(selected genes
            tissue transcript 18 24 = pd.concat([tissue transcript 18 24, selected
            selected genes 24 3 = tissue mann whitney df[p adjust bh(tissue mann wh
            selected_genes_24_3 = selected_genes_24_3[["TRANSCRIPT", "MANN_WHITNEY_
            selected genes 24 3 = selected genes 24 3.rename(columns={"MANN WHITNEY
            selected_genes_24_3["TISSUE"] = [tissue for i in range(selected_genes_2
            tissue transcript 24 3 = pd.concat([tissue transcript 24 3, selected ge
        tissue transcript 3 18.to csv("tissues/mw sig 3m 18m.csv")
        tissue transcript 18 24.to csv("tissues/mw sig 18m 24m.csv")
        tissue transcript 24 3.to csv("tissues/mw sig 24m 3m.csv")
        Reading in summary of p-values and ratios of variances for
                                                                    aorta
```

```
Reading in summary of p-values and ratios of variances for
                                                            bladder-lumen
Reading in summary of p-values and ratios of variances for
                                                            bone-marrow
Reading in summary of p-values and ratios of variances for
                                                            brain-myeloid
Reading in summary of p-values and ratios of variances for
                                                            brown-adipose
-tissue
Reading in summary of p-values and ratios of variances for
                                                            diaphragm
Reading in summary of p-values and ratios of variances for
                                                            gonadal-fat-p
Reading in summary of p-values and ratios of variances for
                                                            heart
Reading in summary of p-values and ratios of variances for
                                                            kidney
Reading in summary of p-values and ratios of variances for
                                                            large-intesti
ne
Reading in summary of p-values and ratios of variances for
                                                            limb-muscle
Reading in summary of p-values and ratios of variances for
                                                            liver
Reading in summary of p-values and ratios of variances for
                                                            lung
Reading in summary of p-values and ratios of variances for
                                                            mammary-gland
Reading in summary of p-values and ratios of variances for
                                                            mesenteric-fa
t-pad
Reading in summary of p-values and ratios of variances for
                                                            pancreas
Reading in summary of p-values and ratios of variances for
                                                            skin-of-body
Reading in summary of p-values and ratios of variances for
                                                            spleen
Reading in summary of p-values and ratios of variances for
                                                            subcutaneous-
adipose-tissue
```

```
Reading in summary of p-values and ratios of variances for thymus
Reading in summary of p-values and ratios of variances for tongue
Reading in summary of p-values and ratios of variances for trachea
```

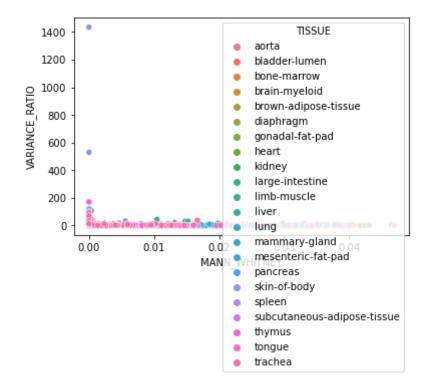
Let us visualize the raw p-values and variance ratios of the Mann-Whitney DEGs fished out from the above procedure.

```
In [5]: df_3_18 = pd.read_csv("tissues/mw_sig_3m_18m.csv")
    df_18_24 = pd.read_csv("tissues/mw_sig_18m_24m.csv")
    df_24_3 = pd.read_csv("tissues/mw_sig_24m_3m.csv")

df_3_18["PAIR"] = ["3m vs 18m" for i in range(df_3_18.shape[0])]
    df_18_24["PAIR"] = ["18m vs 24m" for i in range(df_18_24.shape[0])]
    df_24_3["PAIR"] = ["3m vs 24m" for i in range(df_24_3.shape[0])]
```

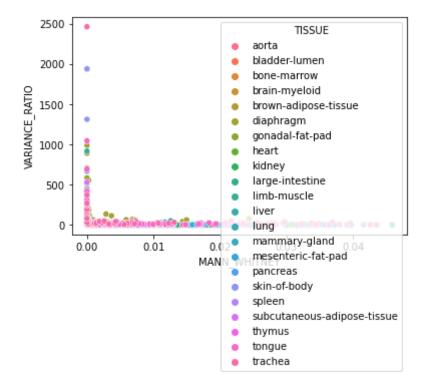
```
In [6]: sns.scatterplot(data=df_18_24, x='MANN_WHITNEY', y='VARIANCE_RATIO', hue='T
```

Out[6]: <AxesSubplot:xlabel='MANN WHITNEY', ylabel='VARIANCE RATIO'>



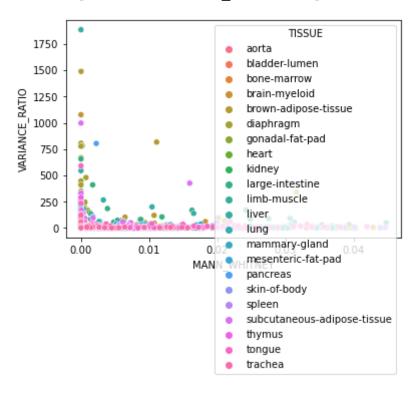
```
In [7]: sns.scatterplot(data=df_3_18, x='MANN_WHITNEY', y='VARIANCE_RATIO', hue='TI
```

Out[7]: <AxesSubplot:xlabel='MANN_WHITNEY', ylabel='VARIANCE_RATIO'>



```
In [8]: sns.scatterplot(data=df_24_3, x='MANN_WHITNEY', y='VARIANCE_RATIO', hue='TI
```

Out[8]: <AxesSubplot:xlabel='MANN_WHITNEY', ylabel='VARIANCE_RATIO'>



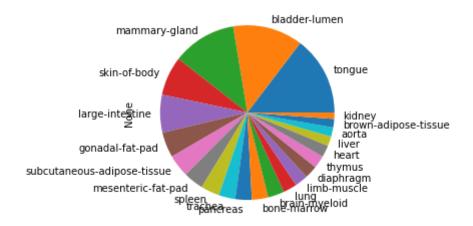
Next we look at the distribution, across tissues, of Mann-Whitney significant genes.

```
In [9]: print("No. MW significant genes for 3m vs 18m: ", df_3_18.shape[0])
    print("No. MW significant genes for 18m vs 24m: ", df_18_24.shape[0])
    print("No. MW significant genes for 24m vs 3m: ", df_24_3.shape[0])

No. MW significant genes for 3m vs 18m: 5571
    No. MW significant genes for 18m vs 24m: 5305
    No. MW significant genes for 24m vs 3m: 5634
```

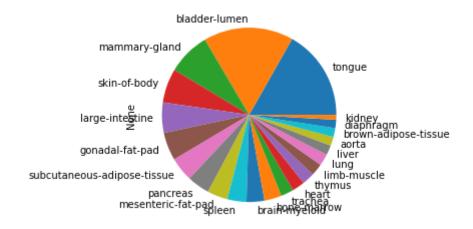
In [10]: df_3_18.value_counts("TISSUE").plot(kind="pie")

Out[10]: <AxesSubplot:ylabel='None'>



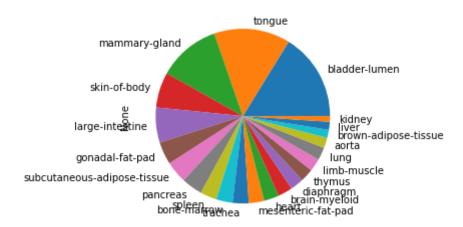
In [11]: df_18_24.value_counts("TISSUE").plot(kind="pie")

Out[11]: <AxesSubplot:ylabel='None'>



In [12]: df_24_3.value_counts("TISSUE").plot(kind="pie")

Out[12]: <AxesSubplot:ylabel='None'>



2.2 MOCHIS

We now repeat the DEG identification procedure above, now using our flexible non-parametric testing software MOCHIS. We run MOCHIS with test statistic $||S_{n,k}||_{p,w}^p$. We choose the following parametrization:

•
$$p = 1$$

• $\mathbf{w} = \left((\frac{j}{k} - \frac{1}{2})^2 : j = 1, \dots, k \right)$

This parametrization optimizes detection of dispersion shifts between two samples.

Step 1. Compute *p*-values.

When computing the p-values, we apply a tie-breaking routine (adding noise ranging from -0.25 to 0.25, which is less than the minimum spacing width of integer counts). To ensure that this routine does not overly contaminate the data, we also compute Mann-Whitney p-values and check that the Mann-Whitney DEGs identified after applying the tie-breaking routine are not markedly different from the original DEGs identified in Section 2.1. We report this latter comparison between post-contamination and original DEGs in Section 2.3. (Heads up: We find little difference.)

```
In [13]: %%capture
         for tissue in all tissues:
             #os.mkdir(os.path.join("tissues/", tissue))
             tissue_smartseq2_data = scanpy.read_h5ad('tissues/' + tissue + '.h5ad')
             transcripts = tissue_smartseq2_data.var.n_cells.index
             ages = np.array(tissue smartseq2 data.obs['age'].index)
             smartseq2 raw counts = tissue smartseq2 data.raw.X.toarray()
             print(smartseq2_raw_counts.shape) # 14517 mice cells x 21069 regions
             # Get cutoff and restrict to only those genes
             cutoff = round(0.8*smartseq2_raw_counts.shape[0])
             cell count sums by region = np.count nonzero(smartseq2 raw counts, axis
             highly expressed genes indices = [i for i,v in enumerate(cell count sum
             smartseq2 high_exp sparse_mat = []
             for i in highly expressed genes indices:
                 smartseq2 high exp sparse mat.append(smartseq2 raw counts[:, i])
             print("Found ", len(highly_expressed_genes_indices), " genes out of ",
             highly expressed transcripts = [transcripts[i] for i in highly expresse
             # Grab age labels
             #smartseq2 df = anndata.AnnData(np.transpose(smartseq2 high exp sparse
             smartseq2 df = pd.DataFrame(np.append(np.transpose(smartseq2 high exp s
             # Run Mann-Whitney test for genes
             gene names = smartseq2 df.columns.values[:-1]
             results df = pd.DataFrame(columns=['TRANSCRIPT',
                                                 'MOCHIS 3 18',
                                                 'MW 3 18',
                                                 'MOCHIS 18 24',
                                                 'MW 18 24',
                                                 'MOCHIS 24 3',
                                                 'MW 24 3',
                                                 'VAR_3_18',
                                                 'INV_3_18',
                                                 'VAR 18 24',
                                                 'INV 18 24',
                                                 'VAR 24 3',
                                                 'INV 24_3'])
             print("How many cells of each age group?")
             print(smartseq2 df['ages'].value counts())
             # Run test for each gene
             for i in range(len(gene names)):
                 to_run_test = smartseq2_df[[gene_names[i], 'ages']]
                 if tissue == "mammary-gland":
```

```
print("Reminder that mammary-gland has 3m, 18m and 21m age grou
    age_3m = to_run_test.loc[to_run_test["ages"] == "3m", gene_name
    age 18m = to run test.loc[to run test["ages"] == "18m", gene na
    age 24m = to run test.loc[to run test["ages"] == "21m", gene na
else:
    age 3m = to run_test.loc[to run_test["ages"] == "3m", gene_name
    age 18m = to run test.loc[to run test["ages"] == "18m", gene na
    age 24m = to run test.loc[to run test["ages"] == "24m", gene na
age 3m = [float(i) for i in age 3m]
age 18m = [float(i) for i in age 18m]
age_24m = [float(i) for i in age_24m]
# Add noise to break ties
noisy age 3m = \text{np.sort}([\text{value} + \text{np.random.uniform}(-1/4, 1/4)) for va
noisy_age_18m = np.sort([value + np.random.uniform(-1/4, 1/4) for v
noisy_age_24m = np.sort([value + np.random.uniform(-1/4, 1/4) for v
wrs_test_3_18 = scipy.stats.mannwhitneyu(x=noisy_age_3m, y=noisy_ag
wrs test 18 24 = scipy.stats.mannwhitneyu(x=noisy age 18m, y=noisy
wrs_test_24_3 = scipy.stats.mannwhitneyu(x=noisy_age_3m, y=noisy_ag
if len(noisy_age_3m) > len(noisy_age_18m):
    #print("3 > 18")
    k = len(age 18m) + 1
    mochis weights = [(i/k-0.5)**2 for i in range(1,k+1)]
    mochis_test_3_18 = mochis_py(x = noisy_age_18m,
                                  p = 1,
                                  wList = mochis_weights,
                                  alternative = "two.sided",
                                  approx = "chebyshev",
                                  n mom = 100,
                                  y = noisy age 3m)
else:
    #print(" 18 > 3")
    k = len(age 3m) + 1
    mochis weights = [(i/k-0.5)**2 for i in range(1,k+1)]
    mochis test 3 18 = mochis py(x = noisy age 3m,
                                  p = 1,
                                  wList = mochis weights,
                                  alternative = "two.sided",
                                  approx = "chebyshev",
                                  n mom = 100
                                  y = noisy age 18m)
if len(noisy_age_18m) > len(noisy_age_24m):
    #print("18 > 24")
```

```
k = len(noisy_age_24m) + 1
   mochis weights = [(i/k-0.5)**2 for i in range(1,k+1)]
   mochis_test_18_24 = mochis_py(x = noisy_age_24m,
                               p = 1,
                               wList = mochis_weights,
                               alternative = "two.sided",
                               approx = "chebyshev",
                               n_mom = 100,
                               y = noisy age 18m)
else:
   #print("24 > 18")
   k = len(noisy_age_18m) + 1
   mochis weights = [(i/k-0.5)**2 for i in range(1,k+1)]
   mochis test 18_{24} = mochis py(x = noisy_age_18m,
                               p = 1,
                               wList = mochis_weights,
                               alternative = "two.sided",
                               approx = "chebyshev",
                               n_mom = 100,
                               y = noisy_age_24m)
if len(noisy_age_3m) > len(noisy_age_24m):
   #print("3 > 24")
   k = len(noisy age 24m) + 1
   mochis weights = [(i/k-0.5)**2 for i in range(1,k+1)]
   mochis_test_24_3 = mochis_py(x = noisy_age_24m,
                               p = 1,
                               wList = mochis_weights,
                               alternative = "two.sided",
                               approx = "chebyshev",
                               n mom = 100,
                               y = noisy_age_3m)
else:
    #print(" 24 > 3")
   k = len(noisy age 3m) + 1
   mochis_weights = [(i/k-0.5)**2 for i in range(1,k+1)]
   mochis test 24 3 = mochis py(x = noisy age 3m,
                               p = 1,
                               wList = mochis weights,
                               alternative = "two.sided",
                               approx = "chebyshev",
                               n mom = 100,
                               y = noisy age 24m)
var 3 18 = max(statistics.variance(age 3m)/statistics.variance(age
var 18 24 = max(statistics.variance(age 18m)/statistics.variance(ag
```

```
invert_3_18 = False
    invert_18_24 = False
    invert 24 3 = False
    if var 3 18 == statistics.variance(age 3m)/statistics.variance(age
        invert_3_18 = True
    if var_18_24 == statistics.variance(age_18m)/statistics.variance(ag
        invert_18_24 = True
    if var_24_3 == statistics.variance(age_3m)/statistics.variance(age_
        invert 24 3 = True
    results_df = pd.concat([results_df, pd.DataFrame([{
        "TRANSCRIPT": gene_names[i],
        "MOCHIS 3 18": mochis test 3 18,
        "MW_3_18": wrs_test_3_18.pvalue,
        "MOCHIS 18 24": mochis test 18 24,
        "MW_18_24": wrs_test_18_24.pvalue,
        "MOCHIS_24_3": mochis_test_24_3,
        "MW_24_3": wrs_test_24_3.pvalue,
        "VAR_3_18": var_3_18,
        "INV 3 18": invert 3 18,
        "VAR_18_24": var_18_24,
        "INV_18_24": invert_18_24,
        "VAR 24 3": var 24 3,
        "INV_24_3": invert_24_3
    }])])
print("Saving results for ", tissue)
results_df.to_csv("tissues/"+tissue+"/mochis_p_val_table.csv")
```

In [14]: results_df

Out[14]:

	TRANSCRIPT	MOCHIS_3_18	MW_3_18	MOCHIS_18_24	MW_18_24	MOCHIS_24_3	ı
0	ENSMUSG00000032231	9.752003e-43	1.451935e- 01	2.950021e-01	1.198098e- 01	6.831664e-40	3.
0	ENSMUSG00000030057	1.062117e-60	9.997725e- 01	1.007576e-02	8.085033e- 03	4.367818e-55	8.
0	ENSMUSG00000090862	3.581052e-44	4.380674e- 14	7.863551e-04	7.343121e- 01	1.011570e-38	5.
0	ENSMUSG00000022982	1.767715e-57	1.068400e- 03	3.304904e-16	1.131972e- 04	2.384471e-24	4.
0	ENSMUSG00000041841	5.304230e-34	1.957629e- 05	1.354376e-03	2.027297e- 23	1.663534e-05	6.
0	ENSMUSG00000028410	1.495667e-51	2.803420e- 01	9.591054e-02	2.537637e- 01	2.629838e-69	1.
0	ENSMUSG00000023010	1.511680e-64	4.598110e- 01	6.458309e-10	7.323468e- 02	6.021564e-46	2.
0	ENSMUSG00000092341	2.145714e-31	7.465742e- 39	5.027337e-19	1.667774e- 02	5.120951e-14	1.
0	ENSMUSG00000060636	5.430763e-44	1.227435e- 05	5.456979e-07	2.240672e- 14	1.506204e-15	1.
0	ENSMUSG00000074884	4.274066e-32	9.358329e- 25	6.103167e-03	2.071193e- 21	6.389116e-33	9.

220 rows × 13 columns

Step 2. Identify MOCHIS significant genes (with FDR control at 0.05)

```
In [15]: tissue transcript 3 18 = pd.DataFrame(columns=['TRANSCRIPT', 'MOCHIS', 'VAR
         tissue_transcript_18_24 = pd.DataFrame(columns=['TRANSCRIPT', 'MOCHIS', 'VA
         tissue_transcript_24_3 = pd.DataFrame(columns=['TRANSCRIPT', 'MOCHIS', 'VAR
         for tissue in all tissues:
             print("Reading in summary of p-values and ratios of variances for ", ti
             tissue mochis df = pd.read csv("tissues/"+tissue+"/mochis p val table.c
             # Pick genes where one of the three pairs (3m, 18m, 24m) has significan
             selected genes 3 18 = tissue mochis df[p adjust bh(tissue mochis df['MO
             selected_genes_3_18 = selected_genes_3_18[["TRANSCRIPT", "MOCHIS_3_18",
             selected_genes_3_18= selected_genes_3_18.rename(columns={"MOCHIS_3_18":
             selected genes 3 18["TISSUE"] = [tissue for i in range(selected genes 3
             tissue_transcript_3_18 = pd.concat([tissue_transcript_3_18, selected_ge
             selected genes 18 24 = tissue mochis df[p adjust bh(tissue mochis df['M
             selected genes 18 24 = selected_genes_18_24[["TRANSCRIPT", "MOCHIS_18_2
             selected genes 18 24 = selected genes 18 24.rename(columns={"MOCHIS 18
             selected genes 18 24["TISSUE"] = [tissue for i in range(selected genes
             tissue_transcript_18_24 = pd.concat([tissue_transcript_18_24, selected_
             selected genes 24_3 = tissue mochis_df[p_adjust_bh(tissue mochis_df['MO
             selected_genes_24_3 = selected_genes_24_3[["TRANSCRIPT", "MOCHIS_24_3",
             selected genes 24 3 = selected genes 24 3.rename(columns={"MOCHIS 24 3"
             selected_genes_24_3["TISSUE"] = [tissue for i in range(selected_genes_2
             tissue transcript 24 3 = pd.concat([tissue transcript 24 3, selected ge
         tissue transcript 3 18.to csv("tissues/mochis sig 3m 18m.csv")
         tissue transcript 18 24.to csv("tissues/mochis sig 18m 24m.csv")
         tissue transcript 24 3.to csv("tissues/mochis sig 24m 3m.csv")
```

```
Reading in summary of p-values and ratios of variances for
                                                            aorta
Reading in summary of p-values and ratios of variances for
                                                            bladder-lumen
Reading in summary of p-values and ratios of variances for
                                                            bone-marrow
Reading in summary of p-values and ratios of variances for
                                                            brain-myeloid
Reading in summary of p-values and ratios of variances for
                                                            brown-adipose
-tissue
Reading in summary of p-values and ratios of variances for
                                                            diaphragm
Reading in summary of p-values and ratios of variances for
                                                            gonadal-fat-p
Reading in summary of p-values and ratios of variances for
                                                            heart
Reading in summary of p-values and ratios of variances for
                                                            kidney
Reading in summary of p-values and ratios of variances for
                                                            large-intesti
Reading in summary of p-values and ratios of variances for
                                                            limb-muscle
Reading in summary of p-values and ratios of variances for
                                                            liver
Reading in summary of p-values and ratios of variances for
                                                            lung
                                                            mammary-gland
Reading in summary of p-values and ratios of variances for
Reading in summary of p-values and ratios of variances for
                                                            mesenteric-fa
t-pad
Reading in summary of p-values and ratios of variances for
                                                            pancreas
Reading in summary of p-values and ratios of variances for
                                                            skin-of-body
Reading in summary of p-values and ratios of variances for
                                                            spleen
Reading in summary of p-values and ratios of variances for
                                                            subcutaneous-
adipose-tissue
```

Reading in summary of p-values and ratios of variances for thymus Reading in summary of p-values and ratios of variances for tongue Reading in summary of p-values and ratios of variances for trachea

Step 3. Visualization.

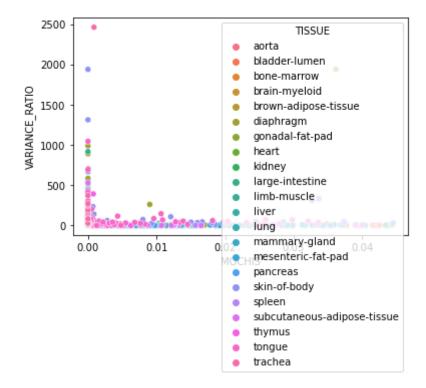
First, let us visualize the raw p-values and variance ratios of the MOCHIS DEGs fished out from the above procedure.

```
In [16]: df_3_18 = pd.read_csv("tissues/mochis_sig_3m_18m.csv")
    df_18_24 = pd.read_csv("tissues/mochis_sig_18m_24m.csv")
    df_24_3 = pd.read_csv("tissues/mochis_sig_24m_3m.csv")

df_3_18["PAIR"] = ["3m vs 18m" for i in range(df_3_18.shape[0])]
    df_18_24["PAIR"] = ["18m vs 24m" for i in range(df_18_24.shape[0])]
    df_24_3["PAIR"] = ["3m vs 24m" for i in range(df_24_3.shape[0])]
```

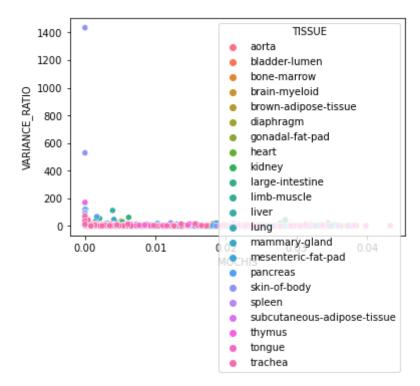
```
In [17]: sns.scatterplot(data=df_3_18, x='MOCHIS', y='VARIANCE_RATIO', hue='TISSUE')
```

Out[17]: <AxesSubplot:xlabel='MOCHIS', ylabel='VARIANCE_RATIO'>



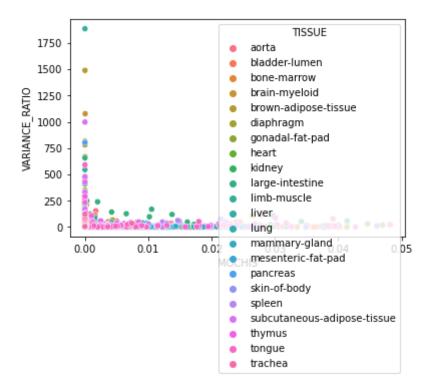
In [18]: sns.scatterplot(data=df_18_24, x='MOCHIS', y='VARIANCE_RATIO', hue='TISSUE'

Out[18]: <AxesSubplot:xlabel='MOCHIS', ylabel='VARIANCE_RATIO'>



```
In [19]: sns.scatterplot(data=df_24_3, x='MOCHIS', y='VARIANCE_RATIO', hue='TISSUE')
```

Out[19]: <AxesSubplot:xlabel='MOCHIS', ylabel='VARIANCE_RATIO'>



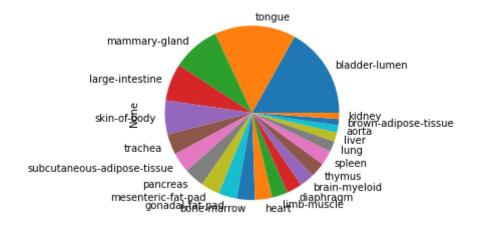
Next we look at the distribution, across tissues, of MOCHIS significant genes.

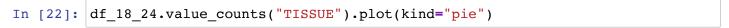
```
In [20]: print("No. MOCHIS significant genes for 3m vs 18m: ", df_3_18.shape[0])
print("No. MOCHIS significant genes for 18m vs 24m: ", df_18_24.shape[0])
print("No. MOCHIS significant genes for 24m vs 3m: ", df_24_3.shape[0])

No. MOCHIS significant genes for 3m vs 18m: 5731
No. MOCHIS significant genes for 18m vs 24m: 4787
No. MOCHIS significant genes for 24m vs 3m: 5486
```

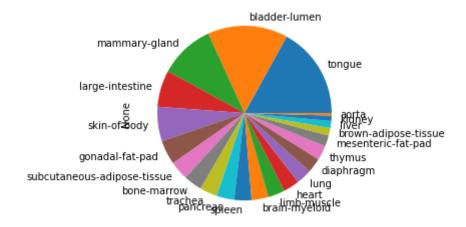
In [21]: df_3_18.value_counts("TISSUE").plot(kind="pie")

Out[21]: <AxesSubplot:ylabel='None'>



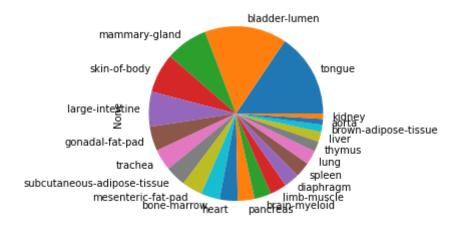


Out[22]: <AxesSubplot:ylabel='None'>



```
In [23]: df_24_3.value_counts("TISSUE").plot(kind="pie")
```

Out[23]: <AxesSubplot:ylabel='None'>



2.3 Impact of Tie Breaking on Mann-Whitney DEGs

In Section 2.2, we raised the issue of tie breaking potentially affecting the significance of Mann-Whitney DEGs. Here, we check for difference between post-contaminated Mann-Whitney DEGs (this Section) and original DEGs (Section 2.1).

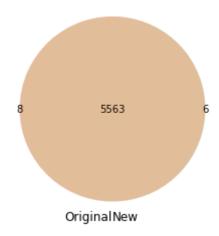
```
In [24]: tissue transcript 3 18 = pd.DataFrame(columns=['TRANSCRIPT', 'NEW MANN WHIT
         tissue_transcript_18_24 = pd.DataFrame(columns=['TRANSCRIPT', 'NEW_MANN_WHI
         tissue_transcript_24_3 = pd.DataFrame(columns=['TRANSCRIPT', 'NEW MANN WHIT
         for tissue in all tissues:
             print("Reading in summary of p-values and ratios of variances for ", ti
             tissue mann whitney df = pd.read csv("tissues/"+tissue+"/mochis p val t
             # Pick genes where one of the three pairs (3m, 18m, 24m) has significan
             selected genes 3 18 = tissue mann whitney df[p adjust bh(tissue mann wh
             selected_genes_3_18 = selected_genes_3_18[["TRANSCRIPT", "MW_3_18"]]
             selected_genes_3_18= selected_genes_3_18.rename(columns={"MW_3_18":"NEW
             selected genes 3 18["TISSUE"] = [tissue for i in range(selected genes 3
             tissue_transcript_3_18 = pd.concat([tissue_transcript_3_18, selected_ge
             selected genes 18 24 = tissue mann whitney df[p adjust bh(tissue mann w
             selected genes 18 24 = selected genes 18 24[["TRANSCRIPT", "MW 18 24"]]
             selected genes 18 24= selected genes 18 24.rename(columns={"MW 18 24":"
             selected genes 18 24["TISSUE"] = [tissue for i in range(selected genes
             tissue_transcript_18_24 = pd.concat([tissue_transcript_18_24, selected_
             selected genes 24 3 = tissue mann whitney df[p_adjust bh(tissue mann wh
             selected_genes_24_3 = selected_genes_24_3[["TRANSCRIPT", "MW_24_3"]]
             selected genes 24 3 = selected genes 24 3.rename(columns={"MW 24 3":"NE
             selected_genes_24_3["TISSUE"] = [tissue for i in range(selected_genes_2
             tissue transcript 24 3 = pd.concat([tissue transcript 24 3, selected ge
         # Compare against original MW significant genes
         og transcript 3 18 = pd.read csv("tissues/mw sig 3m 18m.csv")
         og transcript 18 24 = pd.read csv("tissues/mw sig 18m 24m.csv")
         og transcript 24 3 = pd.read csv("tissues/mw sig 24m 3m.csv")
```

```
Reading in summary of p-values and ratios of variances for
                                                            aorta
Reading in summary of p-values and ratios of variances for
                                                            bladder-lumen
Reading in summary of p-values and ratios of variances for
                                                            bone-marrow
Reading in summary of p-values and ratios of variances for
                                                            brain-myeloid
Reading in summary of p-values and ratios of variances for
                                                            brown-adipose
-tissue
Reading in summary of p-values and ratios of variances for
                                                            diaphragm
Reading in summary of p-values and ratios of variances for
                                                            gonadal-fat-p
ad
Reading in summary of p-values and ratios of variances for
                                                            heart
Reading in summary of p-values and ratios of variances for
                                                            kidney
Reading in summary of p-values and ratios of variances for
                                                            large-intesti
Reading in summary of p-values and ratios of variances for
                                                            limb-muscle
Reading in summary of p-values and ratios of variances for
                                                            liver
Reading in summary of p-values and ratios of variances for
Reading in summary of p-values and ratios of variances for
                                                            mammary-gland
Reading in summary of p-values and ratios of variances for
                                                            mesenteric-fa
t-pad
Reading in summary of p-values and ratios of variances for
                                                            pancreas
Reading in summary of p-values and ratios of variances for
                                                            skin-of-body
```

Reading in summary of p-values and ratios of variances for spleen
Reading in summary of p-values and ratios of variances for subcutaneousadipose-tissue
Reading in summary of p-values and ratios of variances for thymus
Reading in summary of p-values and ratios of variances for tongue
Reading in summary of p-values and ratios of variances for trachea

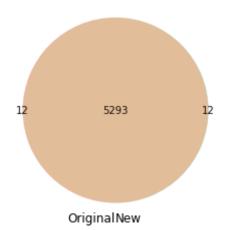
```
In [25]: set1 = set(og_transcript_3_18['TRANSCRIPT'] + "_" + og_transcript_3_18['TIS
    set2 = set(tissue_transcript_3_18['TRANSCRIPT'] + "_" + tissue_transcript_3
    venn2([set1, set2], set_labels = ('Original', 'New'))
```

Out[25]: <matplotlib_venn._common.VennDiagram at 0x7f9f49b00f40>



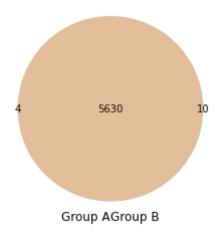
```
In [26]: # Compare 24m vs 3m
set1 = set(og_transcript_18_24['TRANSCRIPT'] + "_" + og_transcript_18_24['T
set2 = set(tissue_transcript_18_24['TRANSCRIPT'] + "_" + tissue_transcript_
venn2([set1, set2], set_labels = ('Original', 'New'))
```

Out[26]: <matplotlib venn. common.VennDiagram at 0x7f9eb045c6d0>



```
In [27]: # Compare 24m vs 3m
set1 = set(og_transcript_24_3['TRANSCRIPT'] + "_" + og_transcript_24_3['TIS
set2 = set(tissue_transcript_24_3['TRANSCRIPT'] + "_" + tissue_transcript_2
venn2([set1, set2], set_labels = ('Group A', 'Group B'))
```

Out[27]: <matplotlib venn. common.VennDiagram at 0x7f9eb0479e20>



We see that there are very few original Mann-Whitney DEGs that are no longer significant after tie breaking, and conversely there are also very few new Mann-Whitney DEGs that were originally non-significant. This suggests that the tie-breaking procedure hardly affected the gene expression distributions between age groups.

3 Analysis

We examine more closely the differences between Mann-Whitney DEGs and MOCHIS DEGs. Recall that Mann-Whitney DEGs are genes that are typically picked up by standard differential analysis routines, whereas MOCHIS DEGs are genes that are differentially expressed owing to shifts in dispersion. Below, we perform some analyses to answer the following questions.

- How many MOCHIS DEGs were previously not detected by Mann-Whitney?
- Does MOCHIS really pick up shifts in dispersion?
- · Are there other interesting questions we may answer with our newly detected MOCHIS DEGs?

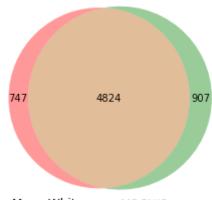
```
In [28]: ## Compare counts
# Load original DEGs from Section 2.1

og_transcript_3_18 = pd.read_csv("tissues/mw_sig_3m_18m.csv")
og_transcript_18_24 = pd.read_csv("tissues/mw_sig_18m_24m.csv")
og_transcript_24_3 = pd.read_csv("tissues/mw_sig_24m_3m.csv")

# Load MOCHIS DEGs from Section 2.2
tissue_transcript_3_18 = pd.read_csv("tissues/mochis_sig_3m_18m.csv")
tissue_transcript_18_24 = pd.read_csv("tissues/mochis_sig_18m_24m.csv")
tissue_transcript_24_3 = pd.read_csv("tissues/mochis_sig_24m_3m.csv")
```

```
In [29]: # Compare 3m vs 18m
set1 = set(og_transcript_3_18['TRANSCRIPT'] + "_" + og_transcript_3_18['TIS
set2 = set(tissue_transcript_3_18['TRANSCRIPT'] + "_" + tissue_transcript_3
venn2([set1, set2], set_labels = ('Mann-Whitney', 'MOCHIS'))
```

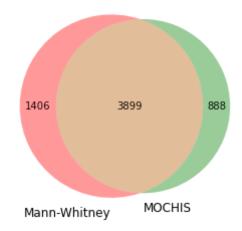
Out[29]: <matplotlib_venn._common.VennDiagram at 0x7f9f4d33c610>



Mann-Whitney MOCHIS

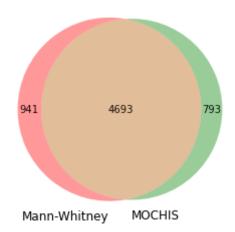
```
In [30]: # Compare 18m vs 24m
set1 = set(og_transcript_18_24['TRANSCRIPT'] + "_" + og_transcript_18_24['T
set2 = set(tissue_transcript_18_24['TRANSCRIPT'] + "_" + tissue_transcript_
venn2([set1, set2], set_labels = ('Mann-Whitney', 'MOCHIS'))
```

Out[30]: <matplotlib_venn._common.VennDiagram at 0x7f9eb5cd6ca0>



```
In [31]: # Compare 3m vs 24m
set1 = set(og_transcript_24_3['TRANSCRIPT'] + "_" + og_transcript_24_3['TIS
set2 = set(tissue_transcript_24_3['TRANSCRIPT'] + "_" + tissue_transcript_2
venn2([set1, set2], set_labels = ('Mann-Whitney', 'MOCHIS'))
```

Out[31]: <matplotlib venn. common.VennDiagram at 0x7f9f535c8a00>



Summary of Findings

- 1. In general, there are considerable differences in the genes picked up by Mann-Whitney and MOCHIS. For any pair of age groups, MOCHIS picks up at least 750 DEGs that were not picked up by Mann-Whitney.
- 2. The number of new genes picked up by MOCHIS is the largest for the pair "3m vs 18m" (= 905), and smallest for the pair "3m vs 21m" (= 794).

3. The number of Mann-Whitney significant genes that are not MOCHIS significant is greatest for the pair "18m vs 24m" (= 1397) and smallest for the pair "3m vs 18m" (= 753).

3.2 Visualizing Changes in Dispersion

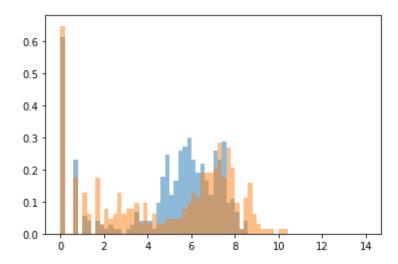
The skeptical reader may wonder if MOCHIS is really picking up a shift in dispersion between the two age groups. Since we realistically cannot compare gene expression distributions between age groups for each MOCHIS significant gene, here we show some gene expression visualizations of MOCHIS significant genes. We focus on MOCHIS DEGs that were not detected by Mann-Whitney. We show visualizations for each pair of age groups ("3m vs 18m", "18m vs 24m" and "3m vs 24m").

```
In [32]: set1 = set(og_transcript_3_18['TRANSCRIPT'] + "_" + og_transcript_3_18['TIS
         set2 = set(tissue_transcript_3_18['TRANSCRIPT'] + "_" + tissue_transcript 3
         mochis_unique = pd.DataFrame()
         for elem in set2:
             if elem not in set1:
                 tc = elem.split(" ")[0]
                 ts = elem.split("_")[1]
                 mochis unique = pd.concat([mochis unique,
                                            tissue transcript 3 18.loc[(tissue trans
                 mochis_unique.index = [i for i in range(1, len(mochis_unique)+1)]
         # Pick genes by hand (I choose the ones with biggest variance ratio in each
         curated degs df = pd.DataFrame()
         mu aorta = mochis unique[mochis unique['TISSUE']=='aorta']
         curated degs df = pd.concat([curated degs df, mu_aorta[mu_aorta['VARIANCE R
         mu_bladder_lumen = mochis_unique[mochis_unique['TISSUE']=='bladder_lumen']
         curated degs_df = pd.concat([curated_degs_df, mu_bladder_lumen[mu_bladder_l
         mu bone marrow = mochis unique[mochis unique['TISSUE']=='bone-marrow']
         curated_degs_df = pd.concat([curated_degs_df, mu_bone_marrow[mu_bone marrow
         mu brain myeloid = mochis unique[mochis unique['TISSUE']=='brain-myeloid']
         curated degs df = pd.concat([curated degs df,mu brain myeloid[mu brain myel
         mu_heart = mochis_unique[mochis_unique['TISSUE']=='heart']
         curated degs df = pd.concat([curated degs df,mu heart[mu heart['VARIANCE RA
         mu_pancreas = mochis_unique[mochis_unique['TISSUE']=='pancreas']
         mu pancreas["VARIANCE RATIO"] == max(mu pancreas["VARIANCE RATIO"]
         curated degs df = pd.concat([curated degs df,mu pancreas[mu pancreas['VARIA']
         # Generate plots
         for i in range(len(curated degs df)):
             tissue = curated degs df.iloc[i]['TISSUE']
             transcript = curated degs df.iloc[i]['TRANSCRIPT']
             tissue_smartseq2_data = scanpy.read_h5ad('tissues/' + tissue + '.h5ad')
             transcripts = tissue_smartseq2_data.var.n_cells.index
             ages = np.array(tissue smartseq2 data.obs['age'].values)
             smartseq2 raw counts = tissue smartseq2 data.raw.X.toarray()
             this gene exp level = pd.DataFrame({
                 'TRANSCRIPT': smartseq2 raw counts[:, np.where(transcripts==transcr
                 'AGE': ages
             })
             if tissue == 'bone-marrow':
                 print(len(smartseq2 raw counts))
             this gene exp level 3m = this gene exp level[this gene exp level['AGE']
             this gene exp level 18m = this gene exp level[this gene exp level['AGE'
             # Visualize
             bins = np.arange(0, 14.2, 0.2)
             print(transcript + " in " + tissue)
```

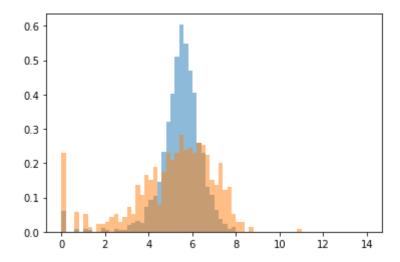
```
plt.hist([math.log(i+1) for i in this_gene_exp_level_3m['TRANSCRIPT'].v
plt.hist([math.log(i+1) for i in this_gene_exp_level_18m['TRANSCRIPT'].
plt.show()

#plt.legend(loc='upper right')
```

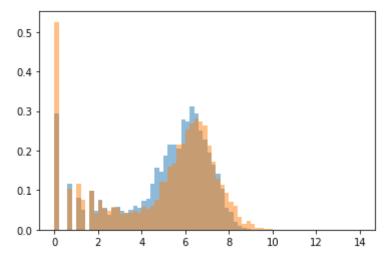
ENSMUSG00000032562 in aorta



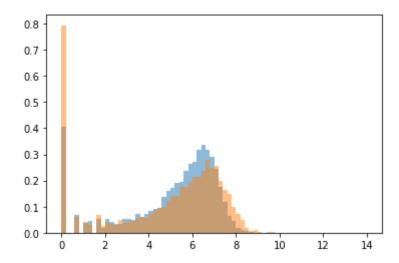
ENSMUSG00000020048 in bladder-lumen



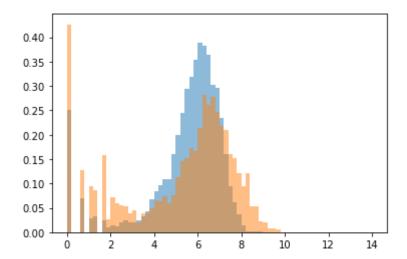
14517
ENSMUSG00000036438 in bone-marrow



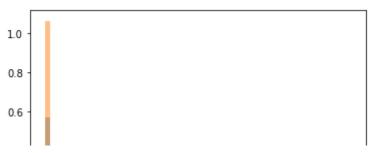
ENSMUSG00000029919 in brain-myeloid



ENSMUSG00000027523 in heart



ENSMUSG00000027712 in pancreas

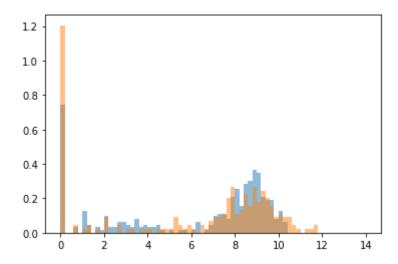


```
In [33]: set1 = set(og_transcript_18_24['TRANSCRIPT'] + "_" + og_transcript_18_24['T
         set2 = set(tissue_transcript_18_24['TRANSCRIPT'] + "_" + tissue_transcript
         mochis_unique = pd.DataFrame()
         for elem in set2:
             if elem not in set1:
                 tc = elem.split(" ")[0]
                 ts = elem.split("_")[1]
                 mochis unique = pd.concat([mochis unique,
                                            tissue transcript 18 24.loc[(tissue tran
                 mochis_unique.index = [i for i in range(1, len(mochis_unique)+1)]
         \# Pick genes by hand (I choose the ones with biggest variance ratio in each
         curated degs df = pd.DataFrame()
         mu_aorta = mochis_unique[mochis_unique['TISSUE']=='aorta']
         curated degs df = pd.concat([curated degs df, mu_aorta[mu_aorta['VARIANCE R
         mu bladder lumen = mochis unique[mochis unique['TISSUE']=='bladder-lumen']
         curated degs df = pd.concat([curated degs df, mu bladder lumen[mu bladder l
         mu_bone_marrow = mochis_unique[mochis_unique['TISSUE']=='bone-marrow']
         curated degs df = pd.concat([curated degs df, mu bone marrow[mu bone marrow
         mu_diaphragm = mochis_unique[mochis_unique['TISSUE']=='diaphragm']
         curated degs df = pd.concat([curated degs df,mu_diaphragm[mu_diaphragm['VAR
         mu_large_intestine = mochis_unique[mochis_unique['TISSUE']=='large_intestin
         curated degs df = pd.concat([curated degs df,mu_large intestine[mu_large_in
         mu limb muscle = mochis_unique[mochis_unique['TISSUE']=='limb-muscle']
         mu limb muscle[mu limb muscle['VARIANCE RATIO'] == max(mu limb muscle['VARI
         curated degs df = pd.concat([curated degs df,mu limb muscle[mu limb muscle[
         # Generate plots
         for i in range(len(curated degs df)):
             tissue = curated degs df.iloc[i]['TISSUE']
             transcript = curated degs df.iloc[i]['TRANSCRIPT']
             tissue_smartseq2_data = scanpy.read_h5ad('tissues/' + tissue + '.h5ad')
             transcripts = tissue smartseq2 data.var.n cells.index
             ages = np.array(tissue smartseq2 data.obs['age'].values)
             smartseq2_raw_counts = tissue_smartseq2_data.raw.X.toarray()
             this gene exp level = pd.DataFrame({
                  TRANSCRIPT': smartseq2_raw_counts[:, np.where(transcripts==transcr
                 'AGE': ages
             })
             this_gene_exp_level_18m = this_gene_exp_level[this_gene_exp_level['AGE'
             this_gene_exp_level_24m = this_gene_exp_level[this_gene_exp_level['AGE
             # Visualize
             bins = np.arange(0, 14.2, 0.2)
             print(transcript + " in " + tissue)
             plt.hist([math.log(i+1) for i in this gene exp level 18m['TRANSCRIPT'].
```

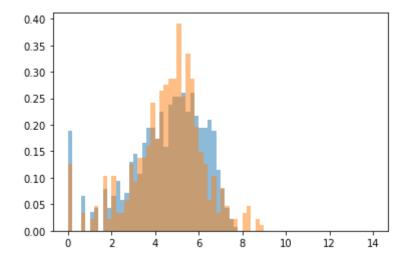
```
plt.hist([math.log(i+1) for i in this_gene_exp_level_24m['TRANSCRIPT'].
plt.show()

#plt.legend(loc='upper right')
```

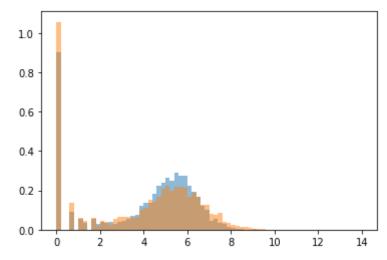
ENSMUSG00000037706 in aorta



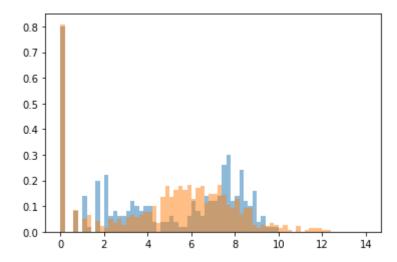
ENSMUSG00000018476 in bladder-lumen



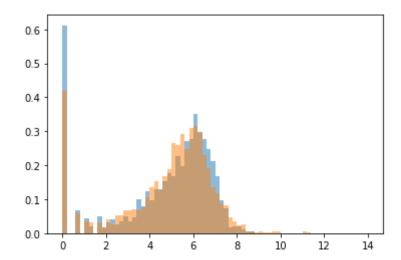
ENSMUSG00000022205 in bone-marrow



 ${\tt ENSMUSG00000071076} \ {\tt in} \ {\tt diaphragm}$



ENSMUSG00000090862 in large-intestine



ENSMUSG00000025492 in limb-muscle

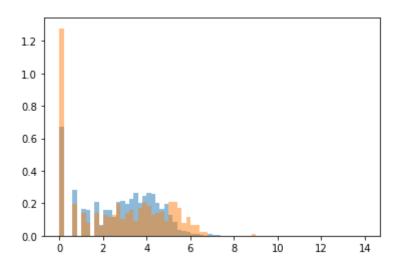


```
In [34]: set1 = set(og transcript 24 3['TRANSCRIPT'] + " " + og transcript 24 3['TIS
         set2 = set(tissue transcript 24 3['TRANSCRIPT'] + " " + tissue transcript 2
         mochis_unique = pd.DataFrame()
         for elem in set2:
             if elem not in set1:
                 tc = elem.split(" ")[0]
                 ts = elem.split("_")[1]
                 mochis unique = pd.concat([mochis unique,
                                            tissue transcript 24_3.loc[(tissue trans
                 mochis_unique.index = [i for i in range(1, len(mochis_unique)+1)]
         # Pick genes by hand (I choose the ones with biggest variance ratio in each
         curated degs df = pd.DataFrame()
         mu bladder_lumen = mochis_unique[mochis_unique['TISSUE']=='bladder_lumen']
         curated degs df = pd.concat([curated degs df, mu bladder lumen[mu bladder l
         mu bone marrow = mochis unique[mochis unique['TISSUE']=='bone-marrow']
         curated degs df = pd.concat([curated degs df, mu bone marrow[mu bone marrow
         mu brain myeloid = mochis unique[mochis unique['TISSUE']=='brain-myeloid']
         curated degs df = pd.concat([curated degs df, mu brain myeloid[mu brain mye
         mu brown adipose tissue = mochis unique[mochis unique['TISSUE']=='brown-adi
         curated degs df = pd.concat([curated degs df,mu brown adipose tissue[mu bro
         mu spleen = mochis unique[mochis unique['TISSUE']=='spleen']
         curated degs df = pd.concat([curated degs df,mu spleen[mu spleen['VARIANCE']
         mu thymus = mochis unique[mochis unique['TISSUE']=='thymus']
         curated degs df = pd.concat([curated degs df,mu thymus[mu thymus['VARIANCE']
         # Generate plots
         for i in range(len(curated degs df)):
             tissue = curated degs df.iloc[i]['TISSUE']
             transcript = curated degs df.iloc[i]['TRANSCRIPT']
             tissue smartseq2 data = scanpy.read h5ad('tissues/' + tissue + '.h5ad')
             transcripts = tissue smartseq2 data.var.n cells.index
             ages = np.array(tissue smartseq2 data.obs['age'].values)
             smartseq2 raw counts = tissue smartseq2 data.raw.X.toarray()
             this gene exp level = pd.DataFrame({
                 'TRANSCRIPT': smartseq2 raw counts[:, np.where(transcripts==transcr
                 'AGE': ages
             })
             this gene exp level 3m = this gene exp level[this gene exp level['AGE']
             this gene exp level 24m = this gene exp level[this gene exp level['AGE'
             # Visualize
             bins = np.arange(0, 14.2, 0.2)
```

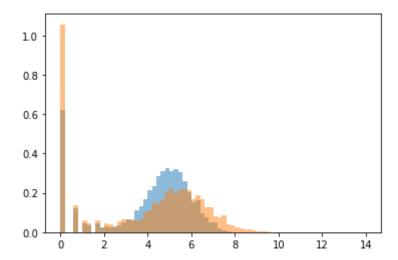
```
print(transcript + " in " + tissue)
plt.hist([math.log(i+1) for i in this_gene_exp_level_3m['TRANSCRIPT'].v
plt.hist([math.log(i+1) for i in this_gene_exp_level_24m['TRANSCRIPT'].
plt.show()
```

#plt.legend(loc='upper right')

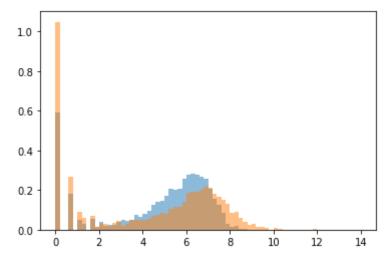
ENSMUSG00000020745 in bladder-lumen



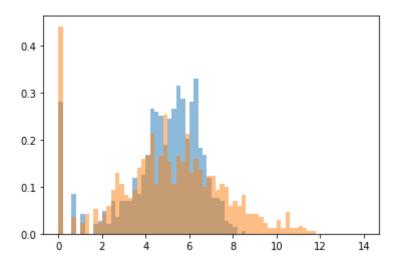
ENSMUSG00000022205 in bone-marrow



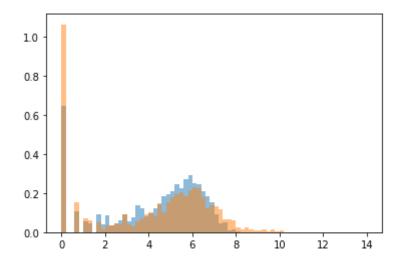
ENSMUSG00000000326 in brain-myeloid



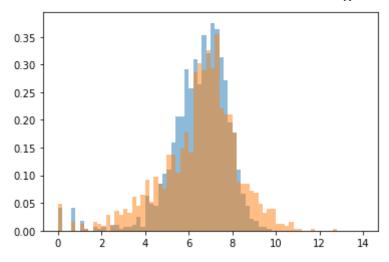
ENSMUSG00000056201 in brown-adipose-tissue



ENSMUSG00000030067 in spleen



ENSMUSG00000050708 in thymus



Summary of Findings

We find that

- 1. MOCHIS detects shifts in dispersions. These shifts can be in either direction (positive or negative).
- 2. Some of the shifts can be attributed to more pronounced zero inflation in one age group than another (based on post-analysis visualizations). This raises an important caveat in our analysis, namely, that our first step of filtering out genes that have more than 20% zero-inflation rate effectively removes all contribution by technical noise to the data. If we are skeptical, then we must find other ways to effectively remove contribution by technical noise.

3.3 Other Interesting Results

We show how we can further interpret our results to answer biologically meaningful questions. Gene Up-regulation vs Down-regulation. We have only looked at changes in dispersion, without explicitly tracking the directionality of change. We report, for each tissue and the corresponding pair of age groups, the fraction of positive and negative changes in dispersion, as measured by the ratio of variances.

```
In [35]: ## Report tissue-specific distribution of up-regulated
         ## and down-regulated genes between age groups
         # Define all tissues again
         mochis degs 3 18 = pd.read csv("tissues/mochis sig 3m 18m.csv")
         mochis degs 18 24 = pd.read csv("tissues/mochis sig 18m 24m.csv")
         mochis_degs_3 24 = pd.read_csv("tissues/mochis_sig_24m 3m.csv")
         up_down_reg_df = pd.DataFrame(columns = ['TISSUE',
                                                   'DOWN_3_18',
                                                   'UP 3 18',
                                                   'DOWN_18_24',
                                                   'UP 18 24',
                                                   'DOWN 3 24',
                                                   'UP_3_24'])
         for tissue in all tissues:
             results_df = pd.read_csv("tissues/" + tissue + "/mochis_p_val_table.csv
             # Analysis for 3m vs 18m
             # mochis degs 3 18 %>% subset(TISSUE == tissue))$TRANSCRIPT
             mochis degs 3 18 by tissue = mochis degs 3 18 [mochis degs 3 18 [TISSUE'
             # subset(TRANSCRIPT %in% (mochis degs 3 18 %>% subset(TISSUE == tissue)
             results df by tissue = results df[results df['TRANSCRIPT'].isin(mochis
             results df INV 3 18 = results df by tissue['INV 3 18']
             n_3_{18} down = sum(results df INV 3 18)
             n_3_18_up = len(results_df_by_tissue) - n_3_18_down
             # Analysis for 18m vs 24m
             # mochis degs 3 18 %>% subset(TISSUE == tissue))$TRANSCRIPT
             mochis degs 18 24 by tissue = mochis degs 18 24[mochis degs 18 24['TISS
             # subset(TRANSCRIPT %in% (mochis degs 3 18 %>% subset(TISSUE == tissue)
             results df by tissue = results df[results df['TRANSCRIPT'].isin(mochis
             results df INV 18 24 = results df by tissue['INV 18 24']
             n 18 24 down = sum(results df INV 18 24)
             n 18 24 up = len(results df by tissue) - n 18 24 down
             # Analysis for 3m vs 18m
             # mochis degs 3 18 %>% subset(TISSUE == tissue))$TRANSCRIPT
             mochis degs 3 24 by tissue = mochis degs 3 24 [mochis degs 3 24 [TISSUE]
             # subset(TRANSCRIPT %in% (mochis degs 3 18 %>% subset(TISSUE == tissue)
             results df by tissue = results df[results df['TRANSCRIPT'].isin(mochis
             results df INV 3 24 = results df by tissue['INV 24 3']
             n_3_24_{down} = sum(results df INV 3 24)
             n 3 24 up = len(results df by tissue) - n 3 24 down
             fig, (ax1, ax2, ax3) = plt.subplots(1, 3)
             fig.suptitle('Direction of Dispersion Shift for ' + tissue)
             ax1.pie([n 3 18 down, n 3 18 up])
             ax2.pie([n 18 24 down, n 18 24 up])
             ax3.pie([n 3 24 down, n 3 24 up])
```

```
plt.show()

up_down_reg_df = pd.concat([up_down_reg_df, pd.DataFrame([{
    'TISSUE': tissue,
    'DOWN_3_18': n_3_18_down,
    'UP_3_18': n_3_18_up,
    'DOWN_18_24': n_18_24_down,
    'UP_18_24': n_18_24_up,
    'DOWN_3_24': n_3_24_down,
    'UP_3_24': n_3_24_up
}
}])])
#print(s)
```

Direction of Dispersion Shift for liver



Direction of Dispersion Shift for lung

```
In [36]: print("The following tissues tend to exhibit increased gene regulation from
         up down reg df[up down reg df['UP 3 18']/(up down reg df['UP 3 18'] + up do
         The following tissues tend to exhibit increased gene regulation from 3m t
         o 18m:
Out[36]: 0
                                      aorta
          0
                             bladder-lumen
         0
                               bone-marrow
          0
                             brain-myeloid
                      brown-adipose-tissue
          0
          0
                                  diaphragm
          0
                           gonadal-fat-pad
                                      heart
          0
          0
                                     kidney
          0
                           large-intestine
                                limb-muscle
         0
         0
                                      liver
          0
                                       lung
          0
                        mesenteric-fat-pad
          0
                                   pancreas
          0
                              skin-of-body
         0
                                     spleen
          0
               subcutaneous-adipose-tissue
          0
                                     thymus
         0
                                     tonque
         0
                                    trachea
         Name: TISSUE, dtype: object
In [37]: print("The following tissues tend to exhibit increased gene regulation from
         up down reg df[up down reg df['UP 18 24']/(up down reg df['UP 18 24'] + up
         The following tissues tend to exhibit increased gene regulation from 18m
         to 24m:
Out[37]: 0
                                      aorta
                             bladder-lumen
          0
                               bone-marrow
          0
                             brain-myeloid
         0
                      brown-adipose-tissue
         0
                                      heart
          0
                                     kidney
          0
                           large-intestine
          0
                                      liver
         0
                                       lung
         0
                        mesenteric-fat-pad
          0
                                     spleen
         0
               subcutaneous-adipose-tissue
                                     thymus
         Name: TISSUE, dtype: object
```

```
In [38]: print("The following tissues tend to exhibit increased gene regulation from
up_down_reg_df[up_down_reg_df['UP_3_24']/(up_down_reg_df['UP_3_24'] + up_do
```

The following tissues tend to exhibit increased gene regulation from 3m to 24m:

```
Out[38]: 0
                                        aorta
          0
                               bladder-lumen
          0
                                 bone-marrow
          0
                               brain-myeloid
          0
                       brown-adipose-tissue
          0
                                   diaphragm
          0
                             gonadal-fat-pad
          0
                                        heart
          0
                                       kidney
          0
                             large-intestine
                                 limb-muscle
          0
          0
                                        liver
          0
                                         lung
          0
                         mesenteric-fat-pad
          0
                                    pancreas
          0
                                skin-of-body
          0
                                       spleen
          0
               subcutaneous-adipose-tissue
          0
                                       thymus
          0
                                       tonque
          0
                                      trachea
```

Name: TISSUE, dtype: object

Persistently Differentially Expressed Genes. It is possible that for some tissues, gene regulation is so dynamic over the lifecourse, manifesting in detectable gene expression changes across time. To this end, we consider DEGs that are persistently differentiated; these are genes that are differentially expressed among all pairs of age groups. For brevity, we shall refer to them as persistently DEGs. First, we ask how many such persistently DEGs there are.

```
In [39]: ## Identify persistently differentially expressed genes
         # Find all unique tissue-transcript pairs in results
         tissue_transcript_combined = pd.concat([
             tissue_transcript_3_18[['TISSUE', 'TRANSCRIPT']],
tissue_transcript_18_24[['TISSUE', 'TRANSCRIPT']],
             tissue_transcript_24_3[['TISSUE', 'TRANSCRIPT']]
         ]).drop_duplicates()
         # Compute the persistent DEGs
         age3m_vs_age18m = []
         age18m vs age24m = []
         age3m vs age24m = []
         for i in range(len(tissue transcript combined)):
             tissue transcript 24 3 subset = tissue transcript 24 3 (tissue transcri
                                                                       (tissue_transcrip
              if (len(tissue_transcript_24_3_subset)) > 0:
                  age3m vs age24m.append(1)
             else:
                  age3m vs age24m.append(0)
             tissue transcript 3 18 subset = tissue transcript 3 18 (tissue transcri
                                                                      (tissue_transcrip
              if (len(tissue transcript 3 18 subset)) > 0:
                  age3m vs age18m.append(1)
             else:
                  age3m vs age18m.append(0)
             tissue transcript 18 24 subset = tissue transcript 18 24 [(tissue transc
                                                                      (tissue transcrip
              if (len(tissue transcript 18 24 subset)) > 0:
                  age18m vs age24m.append(1)
             else:
                  age18m vs age24m.append(0)
         tissue transcript combined['AGE3M VS AGE18M'] = age3m vs age18m
         tissue transcript combined['AGE18M VS AGE24M'] = age18m vs age24m
         tissue transcript combined['AGE3M VS AGE24M'] = age3m vs age24m
         tissue transcript combined['PERSISTENCE'] = np.add(np.add(age3m vs age18m,
         # How many persistently DEGs are there?
         print("There are ",
                       np.count nonzero(tissue transcript combined['PERSISTENCE']==3)
                       " persistently DEGs.")
```

There are 3576 persistently DEGs.

In [40]: # Look closely at persistent DEGs

curated persistent_degs = tissue_transcript_combined[tissue_transcript_comb curated_persistent_degs

Out[40]:

	TISSUE	TRANSCRIPT	AGE3M_VS_AGE18M	AGE18M_VS_AGE24M	AGE3M_VS_AGE24
1	aorta	ENSMUSG00000090862	1	1	
3	aorta	ENSMUSG00000060743	1	1	
18	aorta	ENSMUSG00000004207	1	1	
31	aorta	ENSMUSG00000032399	1	1	
33	aorta	ENSMUSG00000037706	1	1	
5725	trachea	ENSMUSG00000015656	1	1	
5727	trachea	ENSMUSG00000023010	1	1	
5728	trachea	ENSMUSG00000092341	1	1	
5729	trachea	ENSMUSG00000060636	1	1	
5730	trachea	ENSMUSG00000074884	1	1	

3576 rows × 6 columns

To underscore the utility of our method at picking up DEGs that would otherwise be overlooked, we look at persistently DEGs (if there are any!) that would not be picked up by Mann-Whitney.

```
In [41]: ## Find and visualize some persistently DEGs
         ## that are not Mann-Whitney significant
         # Identify those in MOCHIS but not Mann-Whitney
         set1 = set(og_transcript_3_18['TRANSCRIPT'] + "_" + og_transcript_3_18['TIS
         set2 = set(tissue_transcript_3_18['TRANSCRIPT'] + "_" + tissue_transcript_3
         mochis unique 3 18 = pd.DataFrame()
         for elem in set2:
             if elem not in set1:
                 tc = elem.split("_")[0]
                 ts = elem.split("_")[1]
                 mochis_unique_3_18 = pd.concat([mochis_unique_3_18,
                                            tissue transcript 3 18.loc[(tissue trans
         set1 = set(og_transcript_18_24['TRANSCRIPT'] + "_" + og_transcript_18_24['T
         set2 = set(tissue_transcript_18_24['TRANSCRIPT'] + "_" + tissue_transcript
         mochis unique 18 24 = pd.DataFrame()
         for elem in set2:
             if elem not in set1:
                 tc = elem.split(" ")[0]
                 ts = elem.split("_")[1]
                 mochis unique 18 24 = pd.concat([mochis unique 18 24,
                                            tissue transcript 18 24.loc[(tissue tran
         set1 = set(og transcript 24 3['TRANSCRIPT'] + " " + og transcript 24 3['TIS
         set2 = set(tissue_transcript_24_3['TRANSCRIPT'] + "_" + tissue_transcript_2
         mochis unique 24 3 = pd.DataFrame()
         for elem in set2:
             if elem not in set1:
                 tc = elem.split(" ")[0]
                 ts = elem.split("_")[1]
                 mochis unique 24 3 = pd.concat([mochis unique 24 3,
                                            tissue transcript 24 3.loc[(tissue trans
         ## Identify persistently differentially expressed genes
         # Find all unique tissue-transcript pairs in results
         tissue transcript combined = pd.concat([
             mochis unique 3 18[['TISSUE', 'TRANSCRIPT']],
             mochis_unique_18_24[['TISSUE', 'TRANSCRIPT']],
             mochis_unique_24_3[['TISSUE', 'TRANSCRIPT']]
         ]).drop duplicates()
         # Compute the persistent DEGs
         age3m vs age18m = []
         age18m vs age24m = []
         age3m vs age24m = []
         for i in range(len(tissue transcript combined)):
             mochis unique 24 3 subset = mochis unique 24 3[(tissue transcript 24 3[
```

```
(tissue_transcrip
    if (len(mochis unique 24 3 subset)) > 0:
        age3m_vs_age24m.append(1)
    else:
        age3m_vs_age24m.append(0)
   mochis unique 3 18 subset = mochis unique 3 18[(tissue transcript 3 18[
                                                           (tissue transcrip
    if (len(mochis unique 3 18 subset)) > 0:
        age3m vs age18m.append(1)
    else:
        age3m_vs_age18m.append(0)
   mochis unique 18 24 subset = mochis unique 18 24 (tissue transcript 18
                                                           (tissue transcrip
    if (len(mochis_unique_18_24_subset)) > 0:
        age18m vs age24m.append(1)
    else:
        age18m_vs_age24m.append(0)
tissue transcript combined['AGE3M VS AGE18M'] = age3m vs age18m
tissue transcript combined['AGE18M VS AGE24M'] = age18m vs age24m
tissue transcript combined['AGE3M VS AGE24M'] = age3m vs age24m
tissue_transcript_combined['PERSISTENCE'] = np.add(np.add(age3m_vs_age18m,
# How many persistently DEGs are there?
print("There are ",
             np.count nonzero(tissue transcript combined['PERSISTENCE']==3)
             " persistently DEGs not previously detected by Mann-Whitney.")
```

```
<ipython-input-41-8a77d8d7523f>:56: UserWarning: Boolean Series key will
be reindexed to match DataFrame index.
    mochis_unique_24_3_subset = mochis_unique_24_3[(tissue_transcript_24_3
['TISSUE']==tissue_transcript_combined.iloc[i]['TISSUE']) &
<ipython-input-41-8a77d8d7523f>:63: UserWarning: Boolean Series key will
be reindexed to match DataFrame index.
    mochis_unique_3_18_subset = mochis_unique_3_18[(tissue_transcript_3_18
['TISSUE']==tissue_transcript_combined.iloc[i]['TISSUE']) &
<ipython-input-41-8a77d8d7523f>:70: UserWarning: Boolean Series key will
be reindexed to match DataFrame index.
    mochis_unique_18_24_subset = mochis_unique_18_24[(tissue_transcript_18_24['TISSUE']) &

There are 69 persistently DEGs not previously detected by Mann-Whitney.
```

In [42]: | # Look closely at persistent DEGs

curated persistent_degs = tissue_transcript_combined[tissue_transcript_comb curated_persistent_degs

Out[42]:

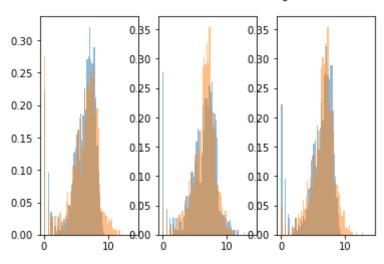
	TISSUE	TRANSCRIPT	AGE3M_VS_AGE18M	AGE18M_VS_AGE24M	AGE3M_VS_AG
3871	skin-of- body	ENSMUSG00000018583	1	1	
1468	diaphragm	ENSMUSG00000018593	1	1	
2559	limb- muscle	ENSMUSG00000058558	1	1	
1893	heart	ENSMUSG00000021025	1	1	
4538	thymus	ENSMUSG00000006699	1	1	
2935	mammary- gland	ENSMUSG00000056537	1	1	
5484	tongue	ENSMUSG00000010608	1	1	
112	bladder- lumen	ENSMUSG00000041959	1	1	
5519	trachea	ENSMUSG00000060743	1	1	
3861	skin-of- body	ENSMUSG000000040444	1	1	

69 rows × 6 columns

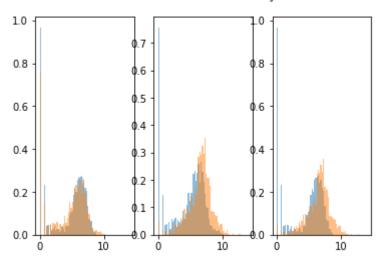
From the chunk above, we find that 66 tissue-specific genes are persistently DEGs. Moreover, most of them come from the bladder lumen and the heart. Let us visualize some of these genes.

```
In [47]: ## Visualizing MOCHIS-exclusive persistently DEGs
         # Generate plots of gene expressions for persistent DEGs
         plot_list = []
         for i in [7,17,29]:
             # Get raw read counts data for that tissue and transcript
             tissue = curated persistent degs.iloc[i]['TISSUE']
             transcript = curated persistent_degs.iloc[i]['TRANSCRIPT']
             # Create local list
             this deg plot list = []
             # Open tissue-specific data and select gene
             tissue smartseq2 data = scanpy.read h5ad('tissues/' + tissue + '.h5ad')
             transcripts = tissue_smartseq2_data.var.n cells.index
             ages = np.array(tissue_smartseq2_data.obs['age'].values)
             smartseq2_raw_counts = tissue_smartseq2_data.raw.X.toarray()
             this gene exp level = pd.DataFrame({
                 'TRANSCRIPT': smartseq2 raw counts[:, np.where(transcripts==transcr
                 'AGE': ages
             })
             this gene exp level 3m = this gene exp level[this gene exp level['AGE']
             this gene exp level 18m = this gene exp level[this gene exp level['AGE'
             this gene exp level 18m = this gene exp level[this gene exp level['AGE'
             # Visualize
             bins = np.arange(0, 14.2, 0.2)
             fig, (ax1, ax2, ax3) = plt.subplots(1, 3)
             fig.suptitle(transcript + " in " + tissue)
             ax1.hist([math.log(i+1) for i in this gene exp level 3m['TRANSCRIPT'].v
             ax1.hist([math.log(i+1) for i in this gene exp level 18m['TRANSCRIPT'].
             ax2.hist([math.log(i+1) for i in this_gene_exp_level_18m['TRANSCRIPT'].
             ax2.hist([math.log(i+1) for i in this_gene_exp level 24m['TRANSCRIPT'].
             ax3.hist([math.log(i+1) for i in this gene exp level 3m['TRANSCRIPT'].v
             ax3.hist([math.log(i+1) for i in this gene exp level 24m['TRANSCRIPT'].
             plt.show()
```

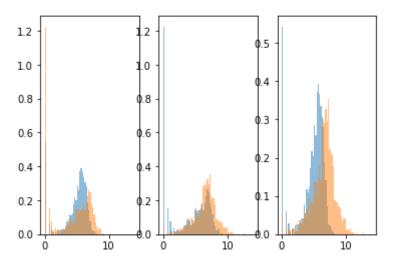
ENSMUSG00000021025 in tongue



ENSMUSG00000078578 in thymus



ENSMUSG00000031812 in trachea



In [44]: ## Generate dataframe summarizing direction of dispersion changes persistent degs direction df = pd.DataFrame(columns=['TISSUE', 'TRANSCRIPT' for i in range(len(curated persistent degs)): tissue = curated_persistent_degs.iloc[i]['TISSUE'] transcript = curated persistent_degs.iloc[i]['TRANSCRIPT'] results df = pd.read csv("tissues/" + tissue + "/mochis p val table.csv relevant_row = results_df[results_df['TRANSCRIPT']==transcript] inv 3 18 = '+' inv 18 24 = '+'inv_3_24 = '+' if relevant_row['INV_3_18'].values[0]: inv 3 18 = "-" if relevant_row['INV_18_24'].values[0]: inv 18 24 = "-" if relevant_row['INV_24_3'].values[0]: inv 3 24 = "-" persistent degs direction df = pd.concat([persistent degs direction df, 'TISSUE': tissue, 'TRANSCRIPT': transcript, 'AGE3M VS AGE18M': inv 3 18, 'AGE18M VS AGE24M': inv 18 24, 'AGE3M VS AGE24M': inv 3 24 }])]).sort values('TISSUE')

In [45]: persistent_degs_direction_df

Out[45]:

TISSUE	TRANSCRIPT	AGE3M_VS_AGE18M	AGE18M_VS_AGE24M	AGE3M_VS_AGE24M
bladder- lumen	ENSMUSG00000030824	+	-	+
bladder- lumen	ENSMUSG00000028757	+	-	+
bladder- lumen	ENSMUSG00000006498	+	-	+
bladder- lumen	ENSMUSG00000021877	+	-	+
bladder- lumen	ENSMUSG00000037373	+	-	+
			•••	
trachea	ENSMUSG00000026234	+	-	+
trachea	ENSMUSG00000055302	+	-	+
trachea	ENSMUSG00000028367	+	-	+
trachea	ENSMUSG00000024190	+	-	+
trachea	ENSMUSG00000031812	+	-	+
	bladder- lumen bladder- lumen bladder- lumen bladder- lumen trachea trachea trachea	bladder- lumen ENSMUSG00000030824 bladder- lumen ENSMUSG00000006498 bladder- lumen ENSMUSG000000021877 bladder- lumen ENSMUSG00000037373 bladder- lumen ENSMUSG00000037373 trachea ENSMUSG00000026234 trachea ENSMUSG00000055302 trachea ENSMUSG00000028367 trachea ENSMUSG00000024190	bladder-lumen ENSMUSG00000030824 + bladder-lumen ENSMUSG000000028757 + bladder-lumen ENSMUSG00000006498 + bladder-lumen ENSMUSG00000021877 + bladder-lumen ENSMUSG00000037373 + trachea ENSMUSG00000026234 + trachea ENSMUSG00000055302 + trachea ENSMUSG00000028367 + trachea ENSMUSG00000024190 +	bladder-lumen ENSMUSG000000030824 + - bladder-lumen ENSMUSG000000028757 + - bladder-lumen ENSMUSG00000006498 + - bladder-lumen ENSMUSG00000021877 + - bladder-lumen ENSMUSG00000037373 + - trachea ENSMUSG00000026234 + - trachea ENSMUSG00000055302 + - trachea ENSMUSG00000028367 + - trachea ENSMUSG000000024190 + -

69 rows × 5 columns