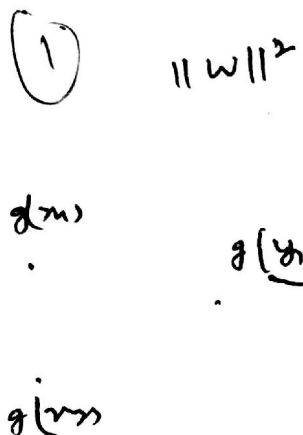


Part A

1. What are the following conditions that the transfer function, $f(x)$, of a neuron need NOT have for the Universal Approximation theorem to apply? (1 mark) ✓ (1)
 A) Differentiability, B) continuity, C) monotonicity, D) boundedness.
2. Indicate by selecting TRUE or FALSE if the following functions satisfy all the conditions of the Universal Approximation theorem: (5 marks) ✓ (5)
 - A) step function, T/F? If FALSE, what condition is violated? F, continuity
 - B) logistic function, T/F? If FALSE, what condition is violated? T
 - C) sign() function, T/F? If FALSE, what condition is violated? F, continuity at $x=0$
 - D) tanh() function T/F? If FALSE, what condition is violated? T
 - E) ramp() function. (Hint: $\text{ramp}(x) = x$, for $x > 0$, $\text{ramp}(x) = 0$ otherwise.) T/F? If FALSE, what condition is violated? F, boundedness.
3. Consider the two discriminant functions, (1 mark) X
 $y_1 = g(x_1 - x_2 - 0.5)$ and $y_2 = g(x_1 + x_2 - 0.5)$, $g(x)$ is the logistic function.
 If $y_1 > y_2$, $X \rightarrow$ Class #1, else $X \rightarrow$ Class #2. The decision surface separating the two classes is described as,
 A) $x_1 = 0$, B) $x_1 - x_2 = 0$, C) $x_1 + x_2 = 0$, D) $x_2 = 0$.
4. Consider the 3 layer MLP whose input/output function is defined as follows. $y_1 = g(x_1)$, $y_2 = g(x_2)$, and $y = g(y_1 + y_2 - 1.3)$ where $g(x)$ is the step function. Which of the following statements is TRUE? (2 marks) (2) ✓
 - A) ~~y~~ y is non-zero in the first and second quadrants.
 - B) y is non-zero in the first quadrant alone.
 - C) y is non-zero in the third quadrant alone.
 - D) y is zero in the firsts, second and fourth quadrants.
5. Which of the following is the correct formulation of learning for a linear Support Vector Machine? (1 mark) ✓ (1)
 - A) $\max \|w\|^2$, subject to $y_i(w \cdot x_j + b) \geq 1, j = 1, \dots, N$
 - B) $\min \|w\|^2$, subject to $y_i(w \cdot x_j + b) \geq 0, j = 1, \dots, N$ ✓
 - C) $\max \|w\|^2$, subject to $y_i(w \cdot x_j + b) \leq 1, j = 1, \dots, N$
 - D) $\min \|w\|^2$, subject to $y_i(w \cdot x_j + b) \geq 1, j = 1, \dots, N$ ✓



$y_1 + y_2 - 1.3$

8. For a linear decision surface $g(x) = 0$, where $g(x) = w^T x + w_0$, the distance of a point x from the decision surface is given as, (1 mark)

- A) $\frac{g(x)}{\|w\|^2}$, B) $\frac{g(x)}{\|w\|}$, C) $g(x)\|w\|$, D) $g(x)\|w\|^2$

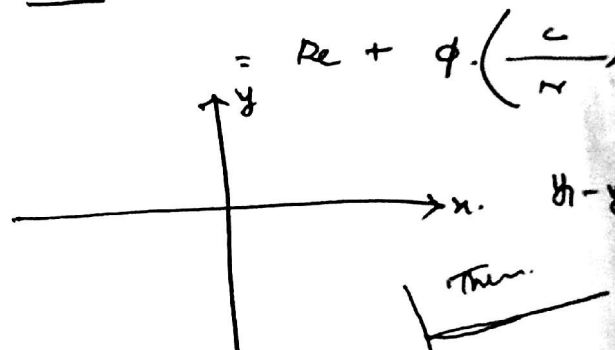
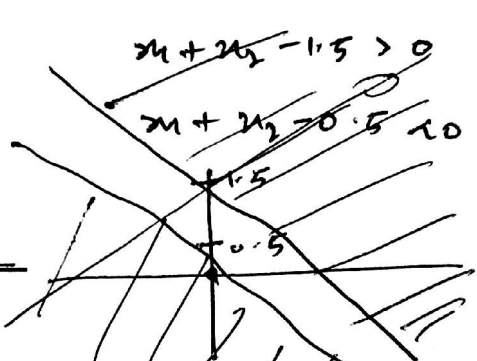
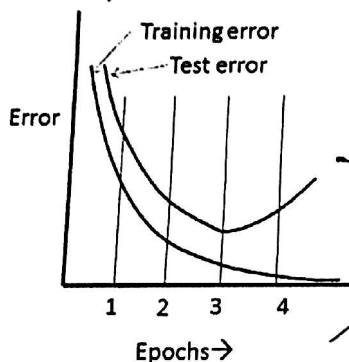
9. A linear discriminant function defined as $y = w^T x - w_0$, is used for a binary classification task such that if $y > 0$, $X \rightarrow$ Class #1 ($d = +1$), else $X \rightarrow$ Class #2 ($d = -1$). The learning equations for this task, which are invoked only when there is an erroneous classification, are: (1 mark)

- A) $\Delta w = \eta d_j x_j$; $\Delta w_0 = -\eta d_j$, B) $\Delta w = -\eta d_j x_j$; $\Delta w_0 = -\eta d_j$, C) $\Delta w = -\eta d_j x_j$; $\Delta w_0 = \eta d_j$, D) $\Delta w = \eta d_j x_j$; $\Delta w_0 = \eta d_j$

10. Consider a MLP defined as, $y_1 = g(x_1 + x_2 - 1.5)$, $y_2 = g(x_1 + x_2 - 0.5)$, and $y = g(y_1 - y_2 - 0.5)$. The region defined by $y > 0$ is best described as, (2 marks)

- A) An infinitely long rectangular strip, B) a semi-infinite region, C) an angular region with an infinite area, D) none of the above.

11. The graphs shown below depict training and test error of a MLP. Applied to the four points of interest, which of the following statements about the graph is true? (1 mark)



- A) The MLP has lowest training error at 1 and best generalization at 4.
B) The MLP has lowest training error at 3 and best generalization at 1.
C) The MLP has lowest training error at 4 and best generalization at 3.
D) The MLP has lowest training error at 3 and best generalization at 4.

Part B

1. Consider the two discriminant functions,

$$y_1 = g(x_1 - x_2 - 0.5) \text{ and } y_2 = g(x_1 + x_2 + 0.5), g(x) \text{ is the step function.}$$

If $y_1 = 1, y_2 = 0, X \rightarrow$ Class #1, else if $y_1 = 0, y_2 = 1, X \rightarrow$ Class #2. Mark the decision regions in the (x_1, x_2) plane. Indicate the 'gray zones' also. (5 marks)

2. Design a multilayer perceptron (MLP) that can implement an XNOR gate, by simple hand calculations. The MLP must have only 1 hidden layer and 2 neurons in that layer. The nonlinearity, $g(x)$, for every neuron is the step function. The XNOR gate is defined as: (5 marks)

X1	X2	D
0	0	1
0	1	0
1	0	0
1	1	1