R tutorial

Contents

0.0.1 Basic R commands

First function in R will ask you whether you want to save data and then it will close R:

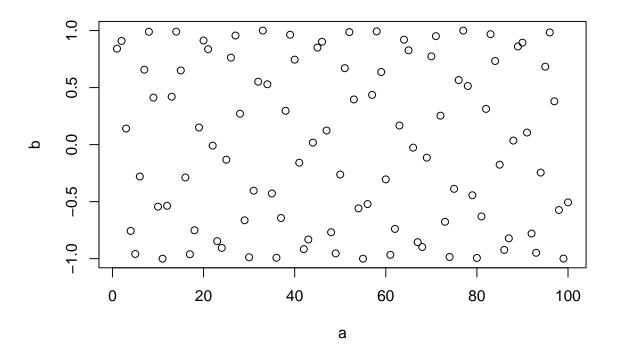
q()

This will close R without asking you:

```
q("n")
q(save="n")
```

To show plot as an example of function, type:

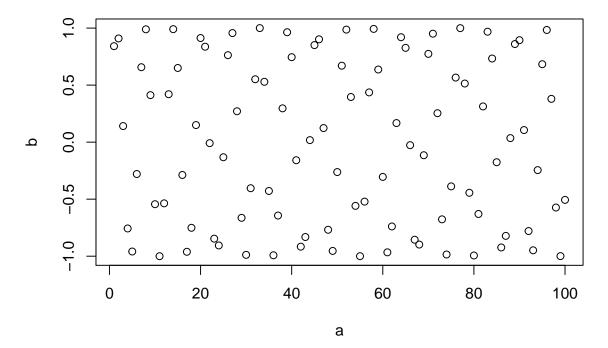
```
a <- 1:100
b <- sin(a)
plot(a, b)
```



This will work:

```
plot(a, b, main="My plot")
```

My plot



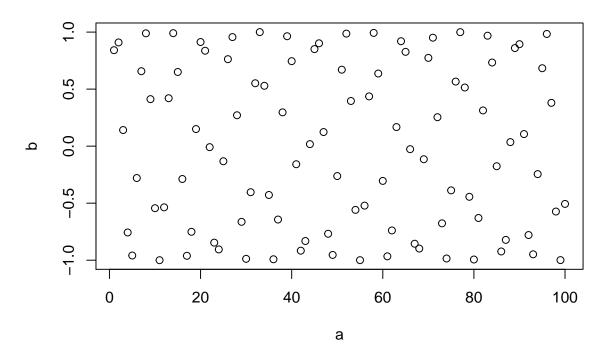
The R engine knows that first two parameters of the function plot are coordinates x and y, respectively. However, this will not work:

plot(a, b, "My plot")

because R does not know that "My plot" links to the parameter main (the main title). It is possible to specify all options:

plot(x=a, y=b, main="My plot")

My plot



```
Help could be found by:
```

help(plot)

?plot

apropos("svd")

help.search("svd")

Example or demo can be found as well:

example(image)

demo(graphics)

Basic operations:

1+1

[1] 2

2-1

[1] 1

3*3

[1] 9

6/3

[1] 2

R recognizes integers and floats from the context:

5/2

[1] 2.5

5.0/2.0

[1] 2.5

```
Power, modulo, integer division:
3^3
## [1] 27
3**3
## [1] 27
5%%2
## [1] 1
5%/%2
## [1] 2
R waits until command finished:
1
## [1] 2
The hash sign \# is used to add comments (code after \# is ignored)
## [1] 2
Spaces are ignored:
1+1
## [1] 2
1 + 1
## [1] 2
1+ 1
## [1] 2
1 +1
## [1] 2
Basic constants and fuctions:
рi
## [1] 3.141593
cos(pi)
## [1] -1
sin(pi)
## [1] 1.224647e-16
exp(1)
## [1] 2.718282
abs(-4)
## [1] 4
```

Logarithm is natural by default, decadic and binary are available as well:

```
log(exp(2))
## [1] 2
log10(1000)
## [1] 3
log2(16)
## [1] 4
Complex numbers are supported as well:
## [1] 0+2i
2i*2i
## [1] -4+0i
One can assign a value to a variable:
x <- 20
x
## [1] 20
y <- 10
У
## [1] 10
x+y
## [1] 30
Logical and string variables are available as well:
x<-FALSE
x
## [1] FALSE
y<-"string"
У
## [1] "string"
Equal works as well in most cases, but use <- to be on the safe side.
x = 20
y = 10
x+y
## [1] 30
It is possible to change (e.g. increment) the value of a variable:
x <- 10
x \leftarrow x + 1
X
## [1] 11
R recognizes capitals and small letters:
a<-1
A<-2
```

```
## [1] 1
Α
## [1] 2
a+A
## [1] 3
Vectors can be defined by function c():
x \leftarrow c(1, 3, 2)
## [1] 1 3 2
Vectors with increments of 1 can be easily generated by:
x <- 1:10
Х
## [1] 1 2 3 4 5 6 7 8 9 10
It can be used in the oposite way:
x<-10:1
X
## [1] 10 9 8 7 6 5 4 3 2 1
It is possible to print individual items from the vector:
x \leftarrow c(1,5,2,3,4,7)
## [1] 1 5 2 3 4 7
x[1]
## [1] 1
x[2]
## [1] 5
x[3:6]
## [1] 2 3 4 7
x[c(1,3)]
## [1] 1 2
Another way how to make a vector:
seq(from=6, to=21, by=2)
## [1] 6 8 10 12 14 16 18 20
rep((1:4), times=2)
## [1] 1 2 3 4 1 2 3 4
rep((1:4), each=2)
## [1] 1 1 2 2 3 3 4 4
It is possible to add, subtract, multiply or divide a vector by a number:
x<-1:5
```

x*2.5

```
## [1] 2.5 5.0 7.5 10.0 12.5
x/2.5
## [1] 0.4 0.8 1.2 1.6 2.0
## [1] 3.5 4.5 5.5 6.5 7.5
x-2.5
## [1] -1.5 -0.5 0.5 1.5 2.5
It is possible to sum or multiply two vectors element-wise:
x < -c(1,3,2)
y<-4:6
x+y
## [1] 5 8 8
x*y
## [1] 4 15 12
To get a dot product you need to type:
x%*%y
##
        [,1]
## [1,] 31
You can apply a function item-wise on a vector:
x < -1:4
exp(x)
## [1] 2.718282 7.389056 20.085537 54.598150
Matrix can be created by function matrix with two possible byrow option (FALSE is the default):
x<-matrix(1:12, ncol=3)</pre>
##
        [,1] [,2] [,3]
## [1,]
           1
                5
                     9
                     10
## [2,]
           2
                 6
                7
## [3,]
           3
                     11
## [4,]
           4
                 8
                     12
x<-matrix(1:12, ncol=3, byrow=TRUE)
        [,1] [,2] [,3]
##
## [1,]
                2
                      3
           1
## [2,]
           4
                 5
                      6
           7
                      9
## [3,]
                 8
## [4,]
          10
                     12
               11
Matrix can be transposes:
t(x)
        [,1] [,2] [,3] [,4]
## [1,]
                 4
                      7
                          10
           1
## [2,]
                 5
           2
                      8
                          11
## [3,]
```

Matrix can be created by combining and adding columns or rows:

12

3

6

9

```
x<-1:4
y < -c(3,2,6,5)
rbind(x, y)
   [,1] [,2] [,3] [,4]
## x
     1 2 3
        3
             2
                   6
## y
cbind(x, y)
##
        х у
## [1,] 1 3
## [2,] 2 2
## [3,] 3 6
## [4,] 4 5
Matrix elements can be accessed by indexes in square brackets ([1,] is for the first row, [,1] for the
first column):
x<-1:4
y < -c(3,2,6,5)
xy \leftarrow cbind(x, y)
хy
##
        х у
## [1,] 1 3
## [2,] 2 2
## [3,] 3 6
## [4,] 4 5
xy[1,]
## x y
## 1 3
xy[1,1]
## x
## 1
xy[1,2]
## y
## 3
xy[,1]
## [1] 1 2 3 4
xy[,2]
## [1] 3 2 6 5
Special object for data analysis in R is data.frame:
x<-1:4
y < -c(3,2,6,5)
mydata <- data.frame(x,y)</pre>
mydata
## x y
## 1 1 3
## 2 2 2
## 3 3 6
## 4 4 5
```

```
mydata[1]
##
   X
## 1 1
## 2 2
## 3 3
## 4 4
mydata[2]
## y
## 1 3
## 2 2
## 3 6
## 4 5
mydatax
## [1] 1 2 3 4
mydata[1,1]
## [1] 1
mydata[2,1]
## [1] 2
mydata[2,]
## x y
## 2 2 2
Logical operations can such as negation, or and and can be used in operations with data.frame, lets
show some:
x<-TRUE
! x
## [1] FALSE
y<-FALSE
x \mid x
## [1] TRUE
x \mid y
## [1] TRUE
у|у
## [1] FALSE
у&у
## [1] FALSE
x&y
## [1] FALSE
## [1] TRUE
1<2
## [1] TRUE
```

```
1>2
## [1] FALSE
1==1
## [1] TRUE
1==2
## [1] FALSE
Loops are not as important R as in classical programming languages, but it is possible to use them:
for(i in 1:3) {
  print(i)
}
## [1] 1
## [1] 2
## [1] 3
In R it is possible to define a new function:
sinpluscos <- function(x) {</pre>
y < -\sin(x) + \cos(x)
return(y)
}
sin(1) + cos(1)
## [1] 1.381773
sinpluscos(1)
## [1] 1.381773
R contains many pre-defined datasets:
head(faithful)
##
     eruptions waiting
          3.600
                      79
```

data()

```
## 1
## 2
          1.800
                      54
## 3
         3.333
                      74
## 4
         2.283
                      62
## 5
          4.533
                      85
## 6
          2.883
                      55
```

Beside standard R functions and datasets it is possible to install new packages from R repositories:

```
installed.packages()
install.packages("igraph")
library(igraph)
```

That's all, lets try to read some data in the next lesson and then we will analyze them.

0.0.1.1Tips and tricks

- you don't remember exactly the command (e.g. you are not sure whether it is len or length)? Just type the beginning of the command and double-click tabulator. You can use it also for parameters of a function.
- if the command is too long you can separate it on two or more lines (R waits until the command is closed).
- it is better not to use trivial names for variables because you can overwrite some existing variables.

• to generate a vector with constant increment (e.g. 2, 4, 6 ... 10):

```
x < -2*1:5
```

• you can reverse the order of a vector by:

```
x<-2*1:5
x[5:1]
## [1] 10 8 6 4 2
```

0.0.2 Reading and writing files in R

You can read data from unformated text files by function read.table:

```
mydata<-read.table("https://raw.githubusercontent.com/spiwokv/Rtutorial/master/data/mydata.txt")
mydata</pre>
```

```
## V1 V2 V3
## 1 1 2 3
## 2 4 5 6
```

Alternatively you can download the file to a working directory of your computer and open it:

```
mydata <- read.table ("mydata.txt")
```

If you don't know which directory is the working one, you can type:

```
getwd()
```

or you can change it by:

```
setwd("C:/Documents")
```

The function read.table can be modified by the parameter header, it indicates that the first line of the file contains names of columns. Separators can be changed by parameter sep. By default, sep is set to "", i.e. one or multiple spaces can act as separators. Special separators such as tabulator can be defined by regular expressions, e.g. sep="\t".

It is also possible to control quoting characters, strings which are to be interpreted as NA (not available) values or comment character.

There are special functions to read formated files, such as read.csv, read.csv2, read.delim, read.delim2, read.fwf and read.ftable. It is also possible to read data from Microsoft Excel, databases (MySQL, SQLite, Oracle, Microsoft SQL Server and others) XML, JSON and other files.

Data can be written by the function write.table:

mydata<-read.table("https://raw.githubusercontent.com/spiwokv/Rtutorial/master/data/mydata.txt")
head(mydata)</pre>

```
## V1 V2 V3
## 1 1 2 3
## 2 4 5 6
write.table(mydata, "mydata2.txt")
```

R also contains sample data for demonstration of functions. You can see the list by typing:

```
data()
```

For example faithful dataset contains waiting times between eruptions and the duration of eruptions of the Old Faithful geyser in Yellowstone National Park (Wyoming, USA).

```
head(faithful)
```

```
## eruptions waiting
## 1 3.600 79
## 2 1.800 54
```

```
## 3 3.333 74
## 4 2.283 62
## 5 4.533 85
## 6 2.883 55
```

0.0.2.1 Tips and tricks

• data in a file may be large and it is not useful to print it when you want to check whether data was read correctly. You can use head function instead to print the header with the first six lines.

head(faithful)

```
##
     eruptions waiting
## 1
          3.600
                      79
## 2
          1.800
                      54
## 3
          3.333
                      74
## 4
          2.283
                      62
## 5
          4.533
                      85
## 6
          2.883
                      55
```

Analogously you can use the tail function. ### Analyzing data in R

We can show how to extract and manipulate data from a dataset. Let us create a simple "dataset" containing names:

```
jmena <- c("Karina", "Radmila", "Diana", "Dalimil", "Melichar", "Vilma", "Cestmir", "Vladan", "Bretislav")</pre>
```

It is possible to iterate this vector of names by typing square brackets with element ID (R counts from 1, not from 0). To get the first name type:

```
jmena[1]
```

```
## [1] "Karina"
```

(returns Karina). You can evaluate some expression within the square brackets, e.g.:

```
jmena[1+1]
```

```
## [1] "Radmila"
```

returns Radmila, not Karina Karina. You can use colon operator:

```
jmena[1:3]
```

```
## [1] "Karina" "Radmila" "Diana"
```

This returns first three names. You can use more complicated operation:

```
jmena[1:3*2]
```

```
## [1] "Radmila" "Dalimil" "Vilma"
```

This returns element number 2, 4 and 6. Negative indexes can be used to remove some element:

```
jmena[-1]
```

```
## [1] "Radmila" "Diana" "Dalimil" "Melichar" "Vilma" "Cestmir"
## [7] "Vladan" "Bretislay"
```

(returns all elements except the first one). The last element can be obtained by jmena[9] if you know the number of elements or jmena[length(jmena)] in case you are lazy to count them. To inverse the order of elements you can use the colon operator as jmena[9:1] or jmena[length(jmena):1].

Let us move to more complicated dataset. You can load the results of municipal elections 2015 in Prague:

Parameter sep=";" indicates that individual items are separated by a semicolon. The option header=T indicates that the first line contains names of columns. In fact the first line contains the remark, because it starts with #. The option dec="," tells us that the Czech decimal is used. For users who can handle Czech characters you can replace "volby2013prahaASCII.txt" by "volby2013praha.txt".

For the first inspection you can type:

head(volby)

```
##
     partyno
                party order
                                             name age
                                                         cendid affiliation
## 1
                 SPOZ
                                     Abt Jaroslav 40
                                                           SP07
                                                                       SPOZ
          15
                         23
## 2
                          3 Adamek Frantisek Bc.
           1
                 CSSD
                                                   58
                                                           CSSD
                                                                       CSSD
## 3
          16 OBC 2011
                                                   61 OBC 2011
                         10
                                Adamek Karel Ing.
                                                                      BEZPP
## 4
          16 OBC_2011
                                    Adamek Ludvik 58 OBC_2011
                                                                   OBC 2011
                          1
## 5
          16 OBC_2011
                                 Adamek Lukas Bc. 28 OBC_2011
                                                                   OBC_2011
                         11
## 6
           4
               TOP 09
                           6 Adamova Marketa Ing. 29
                                                         TOP 09
                                                                     TOP 09
##
      abs rel mandate manord
## 1
        8 0.14
                             4
## 2 2492 3.01
## 3
       12 2.63
## 4
       33 7.25
## 5
       12 2.63
                             6
## 6 3626 2.68
```

This prints the first 10 lines. You can chose different number by n=2 option. Similarly you can print last lines by function tail.

Function:

```
dim(volby)
```

```
## [1] 680 11
```

prints the dimension (number of lines and colums). You can get these values separately for the number of lines and columns by functions nrow and ncol, respectively.

You can iterate on the lines and columns similarly to the previous example. For example, you can select the first candidate in the alphabetic order as:

```
volby[1,]
```

Columns can be selected by:

```
head(volby[,4])
```

```
## [1] Abt Jaroslav Adamek Frantisek Bc. Adamek Karel Ing.
## [4] Adamek Ludvik Adamek Lukas Bc. Adamova Marketa Ing.
## 680 Levels: Abt Jaroslav Adamek Frantisek Bc. ... Zubaty Jan Ing.
```

This prints names of candidates.

The function:

names(volby)

```
## [1] "partyno" "party" "order" "name" "age"
## [6] "cendid" "affiliation" "abs" "rel" "mandate"
## [11] "manord"
```

prints names of columns, such as party number and name, candidate's name and age etc.

As an alternative to volby[,4] you can use \$ operator followed by the name of the column:

head(volby\$name)

```
## [1] Abt Jaroslav Adamek Frantisek Bc. Adamek Karel Ing.
## [4] Adamek Ludvik Adamek Lukas Bc. Adamova Marketa Ing.
## 680 Levels: Abt Jaroslav Adamek Frantisek Bc. ... Zubaty Jan Ing.
```

The function levels determines levels of a vector. For example, if you type:

volby[,2]

##	[1]	SPOZ	CSSD	OBC 2011	OBC 2011	OBC_2011	TOP 09	KSCM
##	[8]	SPOZ	LEV 21	_	HLVZHURU	_	CSSD	SZ
##	[15]	KC	SsCR	Pirati	HLVZHURU	ODS	KDU-CSL	SsCR
##	[22]	Suveren.	PB	Zmena	Svobodni	SPOZ	Suveren.	ODS
##	[29]	CSSD	KC	ODS	ANO 2011	Usvit	OBC_2011	KSCM
##	[36]	OBC_2011	PB	SZ	OBC_2011	KC	LEV 21	Zmena
##	[43]	SPOZ	Suveren.	ODS	ANO 2011	KC	TOP 09	LEV 21
##	[50]	KC	Usvit	KC	SPOZ	KSCM	OBC_2011	HLVZHURU
##	[57]	SPOZ	KDU-CSL	KC	DSSS	SZ	DSSS	KC
##	[64]	SsCR	KDU-CSL	Zmena	SZ	PB	TOP 09	HLVZHURU
##	[71]	PB	SsCR	Svobodni	KC	Usvit	ODS	PB
##	[78]	Usvit	ANO 2011	Suveren.	KDU-CSL	KSCM	ODS	SsCR
##	[85]	SsCR	KDU-CSL	Pirati	Zmena	LEV 21	TOP 09	DSSS
##	[92]	${\tt Svobodni}$	KSCM	SZ	TOP 09	SPOZ	${\tt Svobodni}$	PB
##	[99]	KDU-CSL	ODS	SZ	Usvit	SZ	PB	Usvit
##	[106]	LEV 21	DSSS	SPOZ	LEV 21	SPOZ	Suveren.	Svobodni
##	[113]	SsCR	Zmena	Pirati	KSCM	Usvit	KC	Zmena
##	[120]	KDU-CSL	PB	ODS	ANO 2011	HLVZHURU	Pirati	Zmena
##	[127]	Zmena	SsCR	PB	LEV 21	SPOZ	TOP 09	KSCM
##	[134]	ODS	PB	Suveren.	KC	ODS	Usvit	KSCM
##		Suveren.		KC	ODS	Usvit	DSSS	KSCM
##	[148]		ANO 2011		Zmena	DSSS	TOP 09	CSSD
##		DSSS	CSSD	Svobodni		LEV 21		HLVZHURU
##	[162]		SPOZ	DSSS	Svobodni		PB	SsCR
##	[169]		Zmena	KDU-CSL	Zmena	SZ	DSSS	KDU-CSL
##		Suveren.		Suveren.	CSSD	KC	KSCM	ANO 2011
##		Suveren.		Pirati	Svobodni	Usvit	KSCM	LEV 21
##	[190]		KDU-CSL	KC	SZ	SsCR	ANO 2011	
##	[197]		Zmena	KSCM	KSCM	KDU-CSL	SZ	KSCM
##	[204]	TOP 09	Suveren.		Usvit	HLVZHURU		Svobodni
##	[211]	ODS	HLVZHURU		ANO 2011		KSCM	ODS
##		SZ	ANO 2011		DSSS	ODS	KDU-CSL	LEV 21
##		TOP 09	SsCR		Suveren.		Pirati	OBC_2011
##		Suveren.		HLVZHURU		Zmena	PB	KC
##		LEV 21	SZ	Svobodni		Pirati	HLVZHURU	
##		Usvit	Zmena	CSSD	SPOZ	KDU-CSL	HLVZHURU	
##	[253]	Suveren.	ODS	ODS	KSCM	KC	SZ	SZ
	[260] [267]		Suveren. CSSD	Zmena	TOP 09	TOP 09 KC	DSSS KSCM	ANO 2011
	[274]		Svobodni		ODS ODS	KC Usvit	KSCM	SPOZ
			Svobodni		HLVZHURU		Pirati	KDU-CSL HLVZHURU
	[288]		Usvit	CSSD	PB	TOP 09	SPOZ	Usvit
		DSSS	HLVZHURU		Svobodni		KDU-CSL	KDU-CSL
		HLVZHURU		KSCM		Svobodni		KDU-CSL KSCM
		Zmena	Zmena		ANO 2011 ANO 2011		TOP 09	LEV 21
		KSCM	KDU-CSL	SPOZ	Zmena	LEV 21	HLVZHURU	
		Svobodni		Usvit	SZ	KSCM	PB	HLVZHURU
	[330]		Usvit	PB	LEV 21	KC	KC	KSCM
	[337]		SPOZ	Pirati	Svobodni		CSSD	ODS
#	[001]		21 02	1 11 401	SVODOMIT			CDD

```
## [344] LEV 21
                   CSSD
                             SsCR
                                      KDU-CSL
                                                CSSD
                                                          KDU-CSL
   [351] Usvit
                   SPOZ
                             OBC_2011 CSSD
                                                PΒ
                                                          Pirati
                                                                   Suveren.
                             ANO 2011 ODS
   [358] Zmena
                   PΒ
                                                          CSSD
                                                SsCR
                                                                   Pirati
  [365] ANO 2011 Pirati
                             PΒ
                                                Svobodni LEV 21
                                                                   Svobodni
                                      Pirati
   [372] SZ
                   Usvit
                             DSSS
                                      KSCM
                                                LEV 21
                                                          DSSS
                                                                   KDU-CSL
## [379] Suveren. LEV 21
                                      TOP 09
                                                SsCR
                                                          TOP 09
                             PB
                                                                   SsCR
   [386] HLVZHURU LEV 21
                             SZ
                                      ODS
                                                Suveren.
                                                         KC
                                                                   Suveren.
                                                          SPOZ
   [393] SPOZ
                   KSCM
                                      PΒ
                                                SZ
                                                                   Usvit
                             Zmena
##
   [400] Suveren.
                  CSSD
                             LEV 21
                                      ANO 2011 DSSS
                                                          TOP 09
                                                                   KC
   [407] LEV 21
                   HLVZHURU
                            Zmena
                                      CSSD
                                                ANO 2011 KC
                                                                   CSSD
  [414] Zmena
                   SsCR
                             TOP 09
                                      ODS
                                                ODS
                                                          HLVZHURU HLVZHURU
   [421] KDU-CSL
                   TOP 09
                             KC
                                      ANO 2011 LEV 21
                                                          ODS
                                                                   Svobodni
  [428] CSSD
                   KSCM
                             TOP 09
                                      HLVZHURU Zmena
                                                          CSSD
                                                                   Usvit
## [435] DSSS
                   KDU-CSL
                                                         ANO 2011 TOP 09
                             SZ
                                      KDU-CSL
                                                Suveren.
   [442] PB
                   Pirati
                             SZ
                                      LEV 21
                                                ANO 2011 ODS
                                                                   Pirati
   [449] Svobodni
                   TOP 09
                             LEV 21
                                      PΒ
                                                Svobodni SsCR
                                                                   Pirati
  [456] KC
                            KDU-CSL
                                      HLVZHURU ANO 2011 LEV 21
##
                   Suveren.
                                                                   PB
## [463] SsCR
                   SPOZ
                                      DSSS
                                                LEV 21
                                                          HLVZHURU ANO 2011
                             Zmena
## [470] Suveren.
                   Suveren.
                                      Zmena
                                                KC
                                                          KDU-CSL
                                                                   ODS
## [477] OBC 2011 Zmena
                                                                   CSSD
                             SZ
                                      SZ
                                                SsCR
                                                          SZ
                                                                   Usvit
## [484] CSSD
                   Zmena
                             LEV 21
                                      KDU-CSL
                                                Suveren.
                                                         SZ
## [491] ANO 2011 Svobodni Svobodni ANO 2011 KC
                                                          ANO 2011 Suveren.
  [498] KDU-CSL
                   KDU-CSL
                             HLVZHURU Svobodni SPOZ
                                                          Suveren.
                                                                   KSCM
   [505] ODS
                   TOP 09
                             TOP 09
                                      Zmena
                                                Svobodni KSCM
                                                                   TOP 09
   [512] ANO 2011 Usvit
                             Svobodni Zmena
                                                SsCR
##
                                                          SPOZ
                                                                   Zmena
  [519] Usvit
                   DSSS
                             HLVZHURU TOP 09
                                                Usvit
                                                          Usvit
                                                                   KC
  [526] Usvit
                   Zmena
                             PΒ
                                      TOP 09
                                                Svobodni Svobodni Zmena
  [533] SZ
                   Svobodni Suveren. CSSD
                                                Pirati
                                                          SsCR
                                                                   Pirati
## [540] ODS
                   CSSD
                                      KDU-CSL
                                                Svobodni KDU-CSL
                                                                   DSSS
                             SsCR
   [547] DSSS
                   KSCM
                             SsCR
                                      Usvit
                                                Zmena
                                                          Usvit
                                                                   SsCR
   [554] Usvit
                   KDU-CSL
                             SZ
                                      SPOZ
                                                KSCM
                                                          HLVZHURU KSCM
   [561] SPOZ
                   ANO 2011
                            CSSD
                                      DSSS
                                                PΒ
                                                          DSSS
                                                                   TOP 09
   [568] PB
                   PB
                             LEV 21
                                      ANO 2011 Usvit
                                                          ANO 2011 CSSD
  [575] Svobodni
                             DSSS
                                                Svobodni HLVZHURU LEV 21
                   KC
                                      KSCM
  [582] HLVZHURU Svobodni
                            DSSS
                                      HLVZHURU KSCM
                                                          SsCR
                                                                   ODS
## [589] Zmena
                   SPOZ
                             PΒ
                                      KC
                                                SZ
                                                          Usvit
                                                                   LEV 21
                                                          TOP 09
## [596] KDU-CSL
                   CSSD
                             SZ
                                      KDU-CSL
                                                DSSS
                                                                   TOP 09
   [603] HLVZHURU SsCR
                             CSSD
                                      SPOZ
                                                SPOZ
                                                          CSSD
                                                                   LEV 21
   [610] TOP 09
                   ANO 2011 PB
                                      DSSS
                                                TOP 09
                                                          HLVZHURU Suveren.
   [617] Suveren. LEV 21
                             ANO 2011 ANO 2011 Pirati
                                                          SZ
                                                                   PΒ
                                                          TOP 09
                             ODS
                                      Svobodni ODS
##
   [624] Svobodni PB
                                                                   SPOZ
  [631] CSSD
                   SPOZ
                             CSSD
                                      HLVZHURU Suveren.
                                                         SsCR
                                                                   DSSS
   [638] DSSS
                   DSSS
                             DSSS
                                                          TOP 09
                                                                   TOP 09
                                      Usvit
                                                SsCR
  [645] CSSD
                   SPOZ
                                      CSSD
##
                             SPOZ
                                                LEV 21
                                                          Suveren.
                                                                   LEV 21
   [652] KSCM
                   SsCR
                             SsCR
                                      SsCR
                                                OBC_2011 Pirati
                                                                   SZ
   [659] Suveren.
                   ANO 2011
                            KDU-CSL
                                      DSSS
                                                CSSD
                                                          SZ
                                                                   CSSD
   [666] KDU-CSL
                   DSSS
                             HLVZHURU DSSS
                                                DSSS
                                                          Zmena
                                                                   ANO 2011
## [673] CSSD
                   Usvit
                             ANO 2011 DSSS
                                                HLVZHURU SZ
                                                                   SP07
## [680] Usvit
## 20 Levels: ANO 2011 CSSD DSSS HLVZHURU KC KDU-CSL KSCM LEV 21 ... Zmena
```

it will print a vector with 680 items (one for each candidate) with political parties of candidates in the alphabet order of their family names. If you place this into the function levels it will print each party only once:

levels(volby[,2])

```
## [1] "ANO 2011" "CSSD" "DSSS" "HLVZHURU" "KC" "KDU-CSL" ## [7] "KSCM" "LEV 21" "OBC_2011" "ODS" "PB" "Pirati"
```

```
## [13] "SPOZ" "SsCR" "Suveren." "Svobodni" "SZ" "TOP 09" ## [19] "Usvit" "Zmena"
```

By function nlevels you can get the number of political parties. Function table will print a table with numbers of candidates per party:

table(volby[,2])

```
##
## ANO 2011
                 CSSD
                           DSSS HLVZHURU
                                                 KC
                                                      KDU-CSL
                                                                   KSCM
                                                                           LEV 21
##
         36
                   36
                             36
                                       36
                                                           36
                                                                     36
                                                                               36
                                                 36
## OBC 2011
                  ODS
                             PΒ
                                               SPOZ
                                                         SsCR Suveren. Svobodni
                                   Pirati
##
          11
                    36
                             36
                                        21
                                                 36
                                                           36
                                                                     36
                                                                               36
               TOP 09
##
          SZ
                          Usvit
                                    Zmena
          36
                    36
                                        36
##
                             36
```

In order to print only the lines containing candidates of "Piráti" you can use following expressions: The expression volby[,2] will print parties in the alphabet order of names of candidates. You can extend it by volby[,2]=="Pirati". This will return the series of TRUE and FALSE values in the same order. For example, first 16 candidates in alphabet were not Pirates, so first 16 values are FALSE. The candidate number 17 is Pirate, so output number 17 is TRUE. You can apply sum function on the output. This function counts TRUE as 1 and FALSE as 0.

If you insert the previous expression volby[,2]=="Pirati" into the square brackets of volby[] you can select lines containing Pirates:

volby[volby[,2]=="Pirati",]

##		partyno	party	order	name age cendid	
##	12	3	Pirati	20	Bakovsky Pavel 21 Pirati	
##	17	3	Pirati	1	Bartos Ivan PhDr. PhD 33 Pirati	
##	87	3	Pirati	6	Derer Ivan Ing. 46 Pirati	
##	115		Pirati		Esner Vladislav Tobias 31 Pirati	
##	125	3	Pirati	13	Findeis Lukas 28 Pirati	
##	185	3	Pirati	17	Holovsky Sebastian 28 Pirati	
##	230	3	Pirati	8	Kallasch Ondrej 22 Pirati	
##	243	3	Pirati	19	Kheck Patrick Mgr. 32 Pirati	
##	286	3	Pirati	9	Krausova Michaela 21 Pirati	
##	339	3	Pirati	10	Mahrik Viktor 31 Pirati	
##	356	3	Pirati	21	Matousek Josef 57 Pirati	
##	364	3	Pirati	7	Michailidu Jana 23 Pirati	
##	366	3	Pirati	3	Michalek Jakub Mgr. Bc. 24 Pirati	
##	368	3	Pirati	11	Mikolas Ivan Ing. 48 Pirati	
##	443	3	Pirati	12	Podhajsky Jan Mgr. 37 Pirati	
##	448	3	Pirati	14	Polak Michael 39 Pirati	
##	455	3	Pirati	4	Profant Ondrej 25 Pirati	
##	537	3	Pirati	16	Sura Ales Ing. Bc. 36 Pirati	
##	539	3	Pirati	18 8	Svetnicka Karel Mgr. et Bc. 53 Pirati	
##	621	3	Pirati	5	Veverka Robert 36 Pirati	
##	657	3	Pirati	2	Wagnerova Lenka PhDr. 52 Pirati	
##		affiliat	tion a	bs rel	l mandate manord	
##	12	Pi	rati 3	14 1.47	7 – –	
##	17	Pi	rati 37	72 17.68	3	
##	87	BI	EZPP 4	16 1.95	5	
##	115	Pi	rati	59 0.27	7 – –	
##	125	Pi	rati	54 0.25	5	
##	185	Pi	rati 1	61 0.75		
##	230	Pi	rati 2	57 1.20) – –	
##	243	BI		89 0.41		
##	286	Pi	rati 5	24 2.45	5	
##	339	Pi	rati 2	16 1.01	1	

```
## 356
             BEZPP
                    450
                          2.11
            Pirati 371
## 364
                          1.73
            Pirati 1807
                          8.47
## 366
## 368
            Pirati 249
                          1.16
## 443
            Pirati
                    348
                         1.63
## 448
                    201
                         0.94
            Pirati
## 455
            Pirati
                    750
                          3.51
## 537
                     225
                          1.05
            Pirati
## 539
             BEZPP
                    208
                          0.97
## 621
             BEZPP 1085
                          5.08
## 657
            Pirati 1439
                         6.74
```

The square brackets contain comma inside, because we select lines or columns. The expression volby[,2]=="Pirati" is in front of the comma because we select lines. Lines with TRUE as the output of volby[,2]=="Pirati" are printed, others are not printed.

Let us look at numbers of votes in the column number 8. We can check the range by function range:

```
range(volby[,8])
```

```
## [1] 0 37794
```

This shows that the least successful candidate was not voted at all, the most successful got 37794 votes. You can print all votes sorted by the function **sort**:

```
head(sort(volby[,8]))
```

```
## [1] 0 0 0 1 1 1
```

To get the reverse order use option:

```
head(sort(volby[,8], decreasing=TRUE))
```

```
## [1] 37794 26866 18955 14953 10590 9004
```

You may be interested who scored the best and worst in elections. You can use function order. This function prints the index of the lowest value, the index of the second lowest value and so forth. The expression:

```
head(volby[order(volby[,8]),])
```

```
##
       partyno
                party order
                                         name age cendid affiliation abs
## 341
            12
                   PΒ
                          18
                              Machacek Vaclav
                                                36
                                                       PB
                                                                 BEZPP
                                                                         0 0.00
## 467
            22 LEV 21
                          32
                                Pucholt Milan 42 LEV 21
                                                                LEV 21
                                                                         0 0.00
## 553
            10
                 SsCR.
                          30
                                Sefl Ladislav 64
                                                     SsCR
                                                                  SsCR.
                                                                         0.00
## 77
            12
                   PB
                          17 Cernota Miroslav 55
                                                       PΒ
                                                                 BEZPP
                                                                         1 0.08
## 121
            12
                   PΒ
                          29 Fiedler Ladislav 45
                                                       PΒ
                                                                 BEZPP
                                                                         1 0.08
## 159
            22 LEV 21
                          16
                                Harvanek Petr 64 LEV 21
                                                               LEV 21
                                                                         1 0.26
##
       mandate manord
## 341
## 467
## 553
## 77
## 121
## 159
```

will print the table sorted by the number of votes from the lowest to highest. You can revert the order by option decreasing=T in the order function.

Finally, we are interested in number of votes for each party. This can be obtained manually, party by party as:

```
sum(volby[volby[,2]=="Pirati",8])
```

```
## [1] 12995
```

and so forth for each party. As an alternative you can use function aggregate:

```
aggregate(x=volby[,8], by=list(volby[,2]), FUN=sum)
```

```
##
       Group.1
                    x
## 1
      ANO 2011 47723
## 2
           CSSD 55212
## 3
          DSSS
                1039
## 4
      HLVZHURU
                1782
                  638
## 5
             KC
## 6
       KDU-CSL 36769
## 7
          KSCM 32534
## 8
        LEV 21
                  224
## 9
      OBC 2011
                  260
## 10
            ODS 91977
## 11
             PB
                  480
## 12
        Pirati 12995
## 13
          SPOZ
                3473
## 14
          \operatorname{SsCR}
                  457
## 15 Suveren.
                  400
## 16 Svobodni 11511
## 17
             SZ 39345
## 18
        TOP 09 95033
## 19
         Usvit 8170
## 20
         Zmena
                3035
```

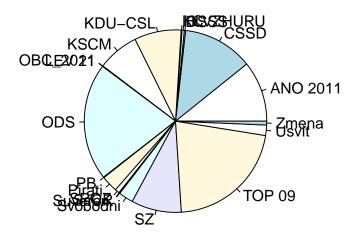
The function list is used because votes can be aggregated by multiple factors. Instead of function sum you can use other functions, for example average age of each party can be printed by:

aggregate(x=volby[,5], by=list(volby[,2]), FUN=mean)

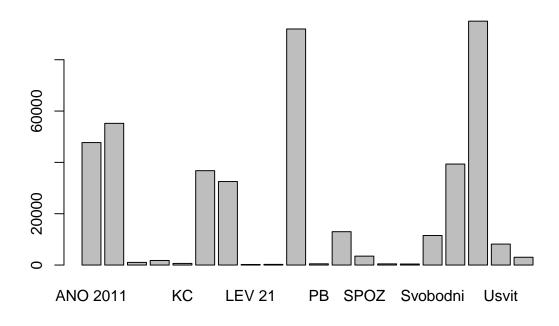
```
##
       Group.1
## 1
      ANO 2011 44.11111
## 2
          CSSD 50.55556
          DSSS 42.41667
## 3
## 4
     HLVZHURU 42.41667
            KC 54.33333
## 5
## 6
       KDU-CSL 45.83333
## 7
          KSCM 51.86111
## 8
        LEV 21 53.86111
     OBC 2011 49.36364
## 9
## 10
           ODS 47.02778
## 11
            PB 47.52778
## 12
        Pirati 34.42857
          SPOZ 47.08333
## 13
          SsCR 52.63889
## 14
## 15 Suveren. 48.44444
## 16 Svobodni 38.50000
## 17
            SZ 40.88889
## 18
        TOP 09 44.33333
         Usvit 45.58333
## 19
## 20
         Zmena 44.19444
```

You can plot numbers of votes as a pie chart or bar plot:

```
vysledky<-aggregate(x=volby[,8], by=list(volby[, 2]), FUN=sum)
pie(vysledky[,2], labels=vysledky[,1])</pre>
```



barplot(vysledky[,2], names.arg=vysledky[,1])



0.0.2.2 Tips and tricks

There is a family of "apply" functions. To calculate a sum for each row of an array or matrix use:

```
myarray <- matrix(1:10, nrow=5)
apply(myarray, 1, FUN=sum)</pre>
```

```
## [1] 7 9 11 13 15
```

If you want to calculate the same for columns replace 1 by 2. You can use any other function with a single input, or even a user defined function defined by function(). For example you can count values higher than 5 per column as:

```
apply(myarray, 2, function(x) length(x[x>5]))
```

```
## [1] 0 5
```

There are specialized packages for data analysis such as "dplyr". It uses a special "pipe" operator (%>%). The output of the operation before the pipe is used as an input of the operation after the pipe. Special functions mutate, select, filter, summarise, arrange and others are used in dplyr. You can replace the aggregate function from the previous example as:

```
library(dplyr)
```

```
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
## filter, lag
## The following objects are masked from 'package:base':
##
## intersect, setdiff, setequal, union
volby %>% group_by(party) %>% summarise(abs=sum(abs))
```

```
##
                  abs
      party
##
      <fct>
                <int>
   1 ANO 2011 47723
##
    2 CSSD
                55212
##
    3 DSSS
                 1039
##
    4 HLVZHURU
                1782
    5 KC
##
                  638
##
    6 KDU-CSL
                36769
##
    7 KSCM
                32534
##
   8 LEV 21
                  224
   9 OBC 2011
                  260
## 10 ODS
                91977
## 11 PB
                  480
## 12 Pirati
                12995
## 13 SPOZ
                 3473
## 14 SsCR
                  457
## 15 Suveren.
                  400
## 16 Svobodni 11511
## 17 SZ
                39345
## 18 TOP 09
                95033
## 19 Usvit
                 8170
## 20 Zmena
                 3035
```

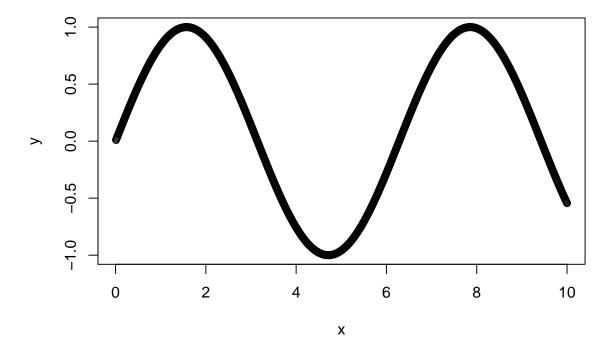
A tibble: 20 x 2

Another useful package for data analysis is "TidyR". Both dplyr and TidyR are from a tidyverse package of packages for data analysis. TidyR uses functions gather(), spread(), separate(), extract() and others to reshape data from untidy to tidy datasets.

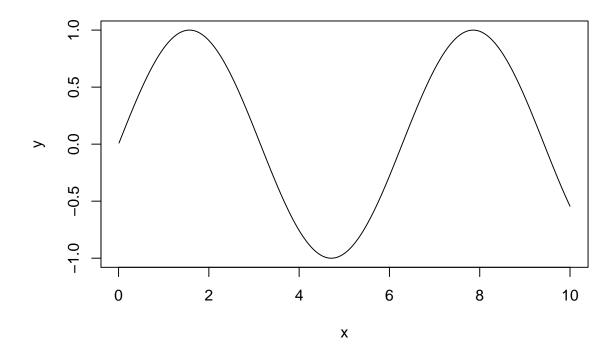
0.0.3 Plotting in R

The basic plotting function in R is plot:

```
x<-1:1000/100
y<-sin(x)
plot(x,y)</pre>
```

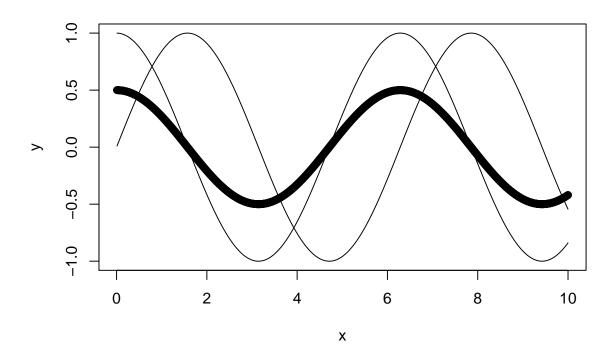


You can switch between points (default), lines (type="l"), both, histogram-like, steps, none and others: plot(x, y, type="l")



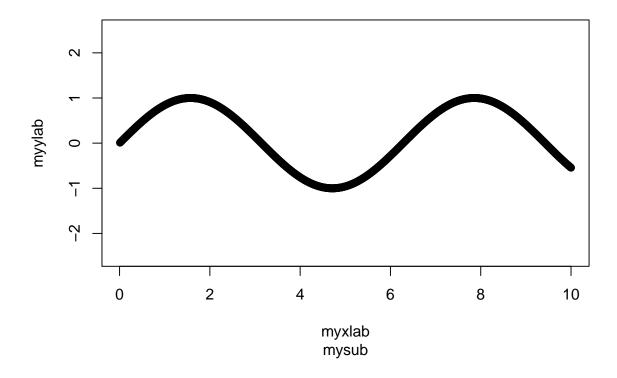
The function plot always plots a new plot. If you want to add new lines or points into the existing plot use lines and points. Simply open new plot by function plot and then use lines and points without closing the plot:

```
plot(x,y, type="1")
lines(x,cos(x))
points(x,0.5*cos(x))
```



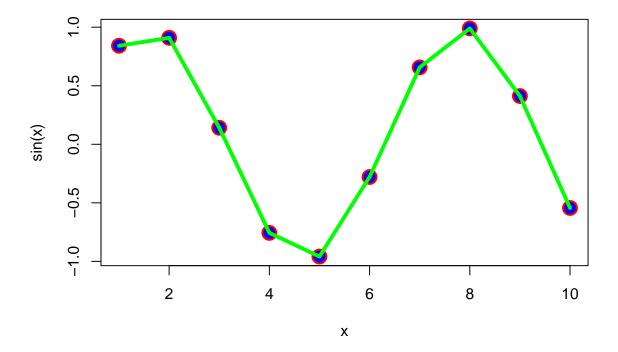
Sometimes it is useful to create an empty plot can vas by plot with type="n" and add lines and points. The function plot has many additional parameters:

parametr main



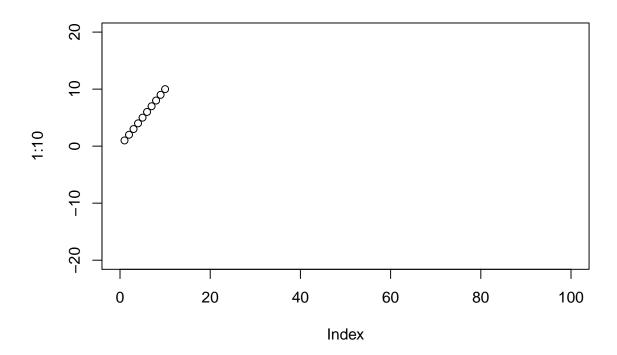
You can change colors of point and lines, shapes of points etc.:

```
x<-1:10
plot(x, sin(x), pch=21, col="red", bg="blue", cex=2, lwd=2)
lines(x, sin(x), col="green", lwd=4)</pre>
```



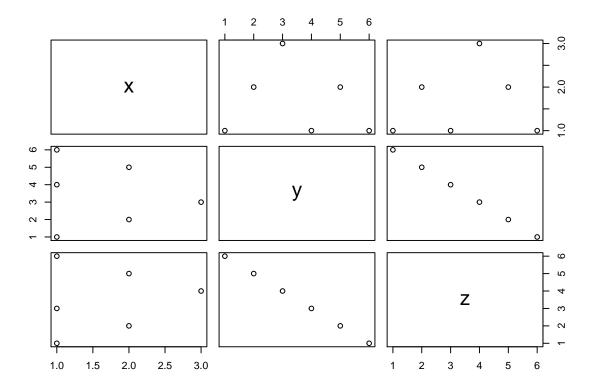
Range of the horizontal and vertical axis can be controlled by xlim and ylim:

```
plot(1:10, xlim=c(0,100), ylim=c(-20,20))
```



The function plot can be applied not only to a pair of vectors, but also to a single vector, data.frame and other objects. Lets try on data.frame:

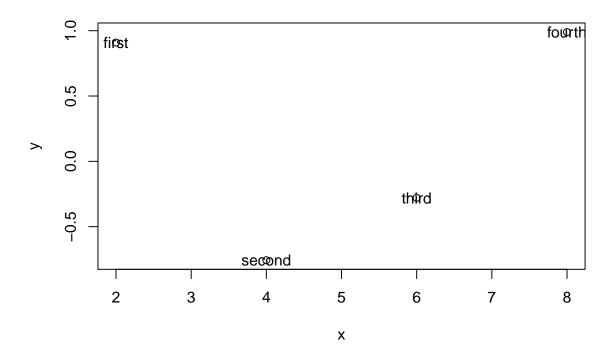
```
x<-c(1,2,3,1,2,1)
y<-1:6
z<-6:1
xyz<-data.frame(x,y,z)
plot(xyz)
```



The function plot can be used to other objects as will be shown later.

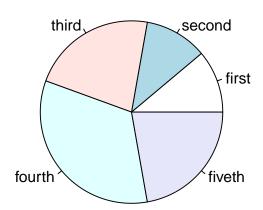
Using function text it is possible to add short strings to points with coordinates x and y:

```
x<-1:4*2
y<-sin(x)
pointnames<-c("first", "second", "third", "fourth")
plot(x,y)
text(x, y, labels=pointnames)</pre>
```



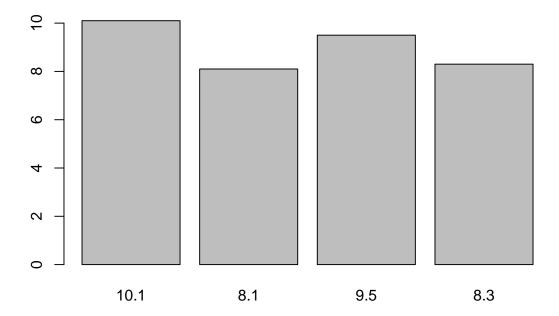
R can make pie charts:

```
x<-c(1,1,2,3,2)
nam<-c("first", "second", "third", "fourth", "fiveth")
pie(x, labels=nam)</pre>
```



Barplots can be drawn using function barplot:

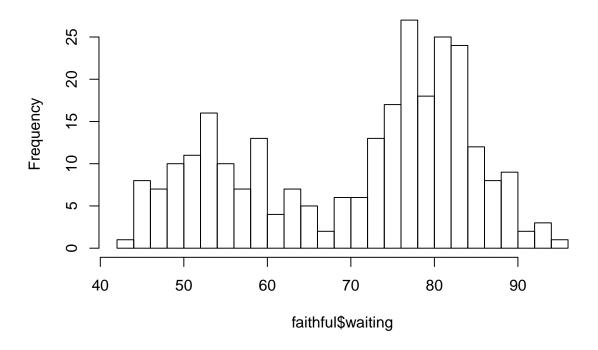
```
barplot(c(10.1,8.1,9.5,8.3), names.arg=c(10.1,8.1,9.5,8.3))
```



Histograms can be plotted by hist with breaks controllable by breaks parameter:

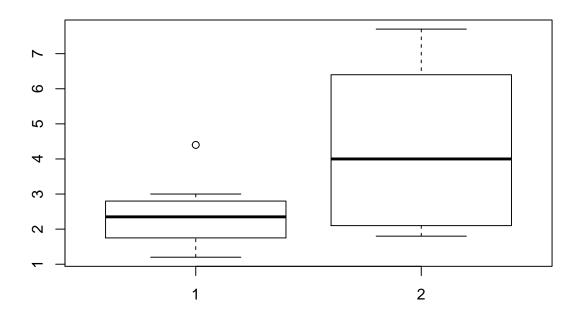
hist(faithful\$waiting, breaks=20)

Histogram of faithful\$waiting



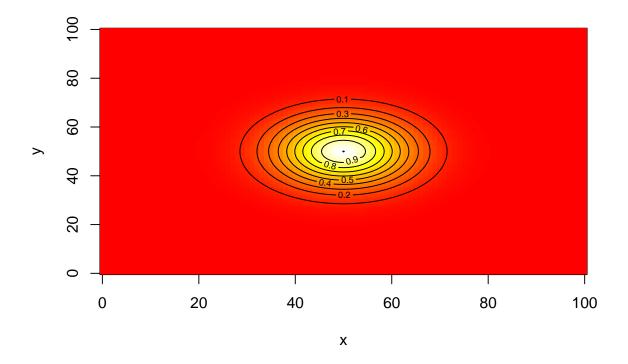
Tukey's boxplots can be ploted by boxplot function:

```
x<-c(1.2,2.2,1.3,4.4,3.0,2.2,2.5,2.6)
y<-c(3.3,2.3,1.8,5.5,7.7,7.3,1.9,4.7)
boxplot(x, y)
```

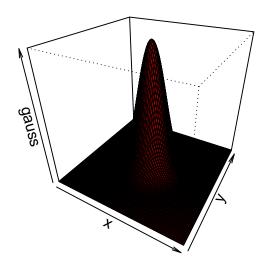


Three-dimensional plots can be presented using image, contour or persp function:

```
x<-0:100
y<-0:100
gauss<-exp(-outer((x-50)**2/200,(y-50)**2/200,"+"))
image(x, y, gauss, col=heat.colors(100))
contour(x, y, gauss, levels=0:10/10, add=TRUE)</pre>
```

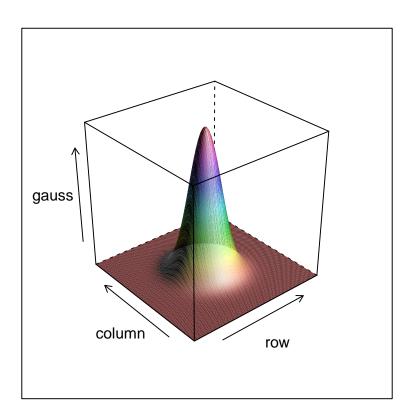


persp(x, y, gauss, col="red", theta=30, phi=30, shade=0.75, ltheta=100)



Nice 3D plots can be made by the wireframe function from the lattice library:

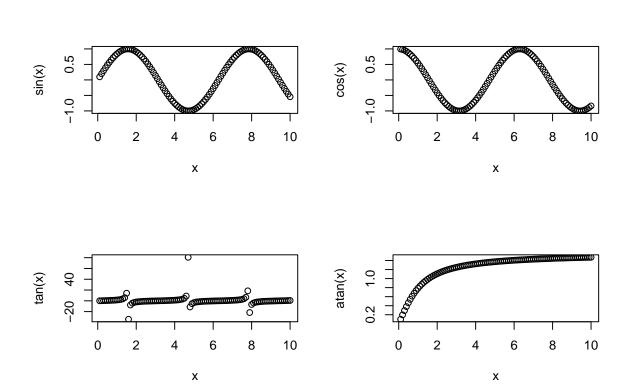
```
library(lattice)
wireframe(gauss, shade=TRUE,light.source = c(10,0,10))
```



The shape of plots can be modified by par function invoked before the function plot or other plotting

functions. As an example we can show plotting of four plots on one canvas:

```
par(mfrow=c(2,2))
x<-1:100/10
plot(x, sin(x))
plot(x, cos(x))
plot(x, tan(x))
plot(x, atan(x))</pre>
```



 ${\bf R}$ can use a wide range of colors. Pre-defined colors can be shown by functions colors:

colors()

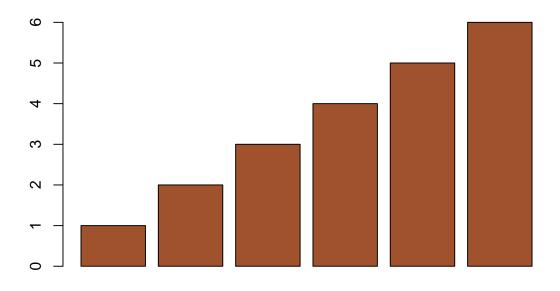
##	[1]	"white"	"aliceblue"	"antiquewhite"	
##	[4]	"antiquewhite1"	"antiquewhite2"	"antiquewhite3"	
##	[7]	"antiquewhite4"	"aquamarine"	"aquamarine1"	
##	[10]	"aquamarine2"	"aquamarine3"	"aquamarine4"	
##	[13]	"azure"	"azure1"	"azure2"	
##	[16]	"azure3"	"azure4"	"beige"	
##	[19]	"bisque"	"bisque1"	"bisque2"	
##	[22]	"bisque3"	"bisque4"	"black"	
##	[25]	"blanchedalmond"	"blue"	"blue1"	
##	[28]	"blue2"	"blue3"	"blue4"	
##	[31]	"blueviolet"	"brown"	"brown1"	
##	[34]	"brown2"	"brown3"	"brown4"	
##	[37]	"burlywood"	"burlywood1"	"burlywood2"	
##	[40]	"burlywood3"	"burlywood4"	"cadetblue"	
##	[43]	"cadetblue1"	"cadetblue2"	"cadetblue3"	
##	[46]	"cadetblue4"	"chartreuse"	"chartreuse1"	
##	[49]	"chartreuse2"	"chartreuse3"	"chartreuse4"	
##	[52]	"chocolate"	"chocolate1"	"chocolate2"	
##	[55]	"chocolate3"	"chocolate4"	"coral"	
##	[58]	"coral1"	"coral2"	"coral3"	

##	[61]	"coral4"	"cornflowerblue"	"cornsilk"
##	[64]	"cornsilk1"	"cornsilk2"	"cornsilk3"
##	[67]	"cornsilk4"	"cyan"	"cyan1"
##	[70]	"cyan2"	"cyan3"	"cyan4"
##	[73]	"darkblue"	"darkcyan"	"darkgoldenrod"
##	[76]	"darkgoldenrod1"	"darkgoldenrod2"	"darkgoldenrod3"
##	[79]	"darkgoldenrod4"	"darkgray"	"darkgreen"
##	[82]	"darkgrey"	"darkkhaki"	"darkmagenta"
##	[85]	"darkolivegreen"	"darkolivegreen1"	"darkolivegreen2"
##	[88]	"darkolivegreen3"	"darkolivegreen4"	"darkorange"
##	[91]	"darkorange1"	"darkorange2"	"darkorange3"
##	[94]	"darkorange4"	"darkorchid"	"darkorchid1"
##	[97]	"darkorchid2"	"darkorchid3"	"darkorchid4"
##	[100]	"darkred"	"darksalmon"	"darkseagreen"
##	[103]	"darkseagreen1"	"darkseagreen2"	"darkseagreen3"
##		"darkseagreen4"	"darkslateblue"	"darkslategray"
##		"darkslategray1"	"darkslategray2"	"darkslategray3"
##	[112]	"darkslategray4"	"darkslategrey"	"darkturquoise"
##	[115]	"darkviolet"	"deeppink"	"deeppink1"
##	[118]	"deeppink2"	"deeppink3"	"deeppink4"
##		"deepskyblue"	"deepskyblue1"	"deepskyblue2"
##		"deepskyblue3"	"deepskyblue4"	"dimgray"
##		"dimgrey"	"dodgerblue"	"dodgerblue1"
##		"dodgerblue2"	"dodgerblue3"	"dodgerblue4"
##		"firebrick"	"firebrick1"	"firebrick2"
##	[136]	"firebrick3"	"firebrick4"	"floralwhite"
##	[139]	"forestgreen"	"gainsboro"	"ghostwhite"
##	[142]	"gold"	"gold1"	"gold2"
##	[145]	"gold3"	"gold4"	"goldenrod"
##	[148]	"goldenrod1"	"goldenrod2"	"goldenrod3"
##	[151]	"goldenrod4"	"gray"	"gray0"
##	[154]	"gray1"	"gray2"	"gray3"
##	[157]	"gray4"	"gray5"	"gray6"
##	[160]	"gray7"	"gray8"	"gray9"
##	[163]	"gray10"	"gray11"	"gray12"
##	[166]	"gray13"	"gray14"	"gray15"
##	[169]	"gray16"	"gray17"	"gray18"
##	[172]	"gray19"	"gray20"	"gray21"
##	[175]	"gray22"	"gray23"	"gray24"
##	[178]	"gray25"	"gray26"	"gray27"
##	[181]	"gray28"	"gray29"	"gray30"
##	[184]	"gray31"	"gray32"	"gray33"
##	[187]	"gray34"	"gray35"	"gray36"
##	[190]	"gray37"	"gray38"	"gray39"
##	[193]	"gray40"	"gray41"	"gray42"
##	[196]	"gray43"	"gray44"	"gray45"
##	[199]	"gray46"	"gray47"	"gray48"
##	[202]	"gray49"	"gray50"	"gray51"
##	[205]	"gray52"	"gray53"	"gray54"
##	[208]	"gray55"	"gray56"	"gray57"
##	[211]	"gray58"	"gray59"	"gray60"
##	[214]	"gray61"	"gray62"	"gray63"
##	[217]	"gray64"	"gray65"	"gray66"
##	[220]	"gray67"	"gray68"	"gray69"
##	[223]	"gray70"	"gray71"	"gray72"
##	[226]	"gray73"	"gray74"	"gray75"
##	[229]	"gray76"	"gray77"	"gray78"
##	[232]	"gray79"	"gray80"	"gray81"

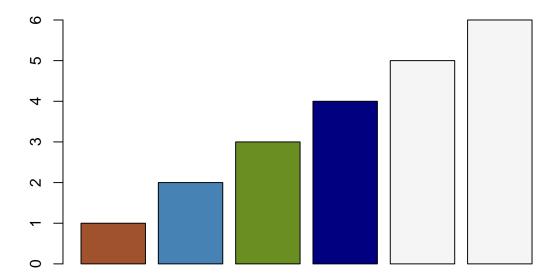
```
## [235] "gray82"
                                  "gray83"
                                                          "gray84"
## [238] "gray85"
                                  "gray86"
                                                          "gray87"
## [241] "gray88"
                                  "gray89"
                                                          "gray90"
## [244] "gray91"
                                  "gray92"
                                                          "gray93"
## [247] "gray94"
                                  "gray95"
                                                          "gray96"
## [250] "gray97"
                                  "gray98"
                                                           "gray99"
## [253] "gray100"
                                  "green"
                                                           "green1"
## [256] "green2"
                                  "green3"
                                                          "green4"
## [259] "greenyellow"
                                  "grey"
                                                          "grey0"
## [262] "grey1"
                                  "grey2"
                                                          "grey3"
## [265] "grey4"
                                  "grey5"
                                                          "grey6"
## [268] "grey7"
                                  "grey8"
                                                          "grey9"
## [271] "grey10"
                                  "grey11"
                                                          "grey12"
## [274] "grey13"
                                  "grey14"
                                                           grey15"
## [277] "grey16"
                                  "grey17"
                                                           "grey18"
                                  "grey20"
## [280] "grey19"
                                                          "grey21"
## [283] "grey22"
                                  "grey23"
                                                          "grey24"
## [286] "grey25"
                                  "grey26"
                                                          "grey27"
## [289] "grey28"
                                  "grey29"
                                                          "grey30"
## [292] "grey31"
                                  "grey32"
                                                          "grev33"
                                  "grey35"
## [295] "grey34"
                                                          "grey36"
## [298] "grey37"
                                  "grey38"
                                                           "grey39"
## [301] "grey40"
                                  "grey41"
                                                          "grey42"
## [304] "grey43"
                                  "grey44"
                                                          "grey45"
## [307] "grey46"
                                  "grey47"
                                                          "grey48"
## [310] "grey49"
                                  "grey50"
                                                          "grey51"
## [313] "grey52"
                                  "grey53"
                                                          "grey54"
## [316] "grey55"
                                  "grey56"
                                                          "grey57"
## [319] "grey58"
                                  "grey59"
                                                           "grey60"
## [322] "grey61"
                                  "grey62"
                                                           "grey63"
## [325] "grey64"
                                  "grey65"
                                                           "grey66"
## [328] "grey67"
                                  "grey68"
                                                          "grey69"
## [331] "grey70"
                                  "grey71"
                                                          "grey72"
## [334] "grey73"
                                  "grey74"
                                                          "grey75"
## [337] "grey76"
                                  "grey77"
                                                          "grey78"
## [340] "grey79"
                                  "grey80"
                                                          "grey81"
## [343] "grey82"
                                  "grey83"
                                                           "grey84"
## [346] "grey85"
                                  "grey86"
                                                          "grey87"
## [349] "grev88"
                                  "grey89"
                                                          "grey90"
## [352] "grey91"
                                  "grey92"
                                                          "grey93"
## [355] "grey94"
                                  "grey95"
                                                          "grey96"
## [358] "grey97"
                                  "grey98"
                                                          "grey99"
## [361] "grey100"
                                  "honeydew"
                                                          "honeydew1"
## [364] "honeydew2"
                                  "honeydew3"
                                                          "honeydew4"
## [367] "hotpink"
                                  "hotpink1"
                                                          "hotpink2"
## [370] "hotpink3"
                                  "hotpink4"
                                                          "indianred"
## [373] "indianred1"
                                  "indianred2"
                                                          "indianred3"
## [376] "indianred4"
                                  "ivory"
                                                          "ivory1"
                                  "ivory3"
## [379] "ivory2"
                                                          "ivory4"
                                  "khaki1"
## [382] "khaki"
                                                          "khaki2"
## [385] "khaki3"
                                  "khaki4"
                                                          "lavender"
## [388] "lavenderblush"
                                  "lavenderblush1"
                                                          "lavenderblush2"
## [391] "lavenderblush3"
                                  "lavenderblush4"
                                                          "lawngreen"
## [394] "lemonchiffon"
                                  "lemonchiffon1"
                                                          "lemonchiffon2"
## [397] "lemonchiffon3"
                                  "lemonchiffon4"
                                                          "lightblue"
## [400] "lightblue1"
                                  "lightblue2"
                                                          "lightblue3"
                                                          "lightcyan"
## [403] "lightblue4"
                                  "lightcoral"
## [406] "lightcyan1"
                                  "lightcyan2"
                                                          "lightcyan3"
```

```
## [409] "lightcyan4"
                                  "lightgoldenrod"
                                                          "lightgoldenrod1"
## [412] "lightgoldenrod2"
                                  "lightgoldenrod3"
                                                          "lightgoldenrod4"
## [415] "lightgoldenrodyellow"
                                 "lightgray"
                                                          "lightgreen"
## [418] "lightgrey"
                                  "lightpink"
                                                          "lightpink1"
## [421] "lightpink2"
                                  "lightpink3"
                                                          "lightpink4"
## [424] "lightsalmon"
                                  "lightsalmon1"
                                                          "lightsalmon2"
## [427] "lightsalmon3"
                                                          "lightseagreen"
                                  "lightsalmon4"
## [430] "lightskyblue"
                                  "lightskyblue1"
                                                          "lightskyblue2"
## [433] "lightskyblue3"
                                  "lightskyblue4"
                                                          "lightslateblue"
## [436] "lightslategray"
                                  "lightslategrey"
                                                          "lightsteelblue"
## [439] "lightsteelblue1"
                                  "lightsteelblue2"
                                                          "lightsteelblue3"
## [442] "lightsteelblue4"
                                  "lightyellow"
                                                          "lightyellow1"
## [445] "lightyellow2"
                                  "lightyellow3"
                                                          "lightyellow4"
## [448] "limegreen"
                                  "linen"
                                                          "magenta"
                                  "magenta2"
                                                          "magenta3"
## [451] "magenta1"
## [454] "magenta4"
                                  "maroon"
                                                          "maroon1"
## [457] "maroon2"
                                  "maroon3"
                                                          "maroon4"
## [460] "mediumaquamarine"
                                  "mediumblue"
                                                          "mediumorchid"
## [463] "mediumorchid1"
                                  "mediumorchid2"
                                                          "mediumorchid3"
## [466] "mediumorchid4"
                                  "mediumpurple"
                                                          "mediumpurple1"
## [469] "mediumpurple2"
                                  "mediumpurple3"
                                                          "mediumpurple4"
## [472] "mediumseagreen"
                                  "mediumslateblue"
                                                          "mediumspringgreen"
## [475] "mediumturquoise"
                                  "mediumvioletred"
                                                          "midnightblue"
## [478] "mintcream"
                                  "mistyrose"
                                                          "mistyrose1"
## [481] "mistyrose2"
                                                          "mistyrose4"
                                  "mistyrose3"
## [484] "moccasin"
                                  "navajowhite"
                                                          "navajowhite1"
## [487] "navajowhite2"
                                  "navajowhite3"
                                                          "navajowhite4"
## [490] "navv"
                                  "navvblue"
                                                          "oldlace"
## [493] "olivedrab"
                                                          "olivedrab2"
                                  "olivedrab1"
## [496] "olivedrab3"
                                  "olivedrab4"
                                                          "orange"
## [499] "orange1"
                                  "orange2"
                                                          "orange3"
## [502] "orange4"
                                  "orangered"
                                                          "orangered1"
## [505] "orangered2"
                                  "orangered3"
                                                          "orangered4"
## [508] "orchid"
                                                          "orchid2"
                                  "orchid1"
## [511] "orchid3"
                                  "orchid4"
                                                          "palegoldenrod"
## [514] "palegreen"
                                                          "palegreen2"
                                  "palegreen1"
## [517] "palegreen3"
                                  "palegreen4"
                                                          "paleturquoise"
## [520] "paleturquoise1"
                                                          "paleturquoise3"
                                  "paleturquoise2"
## [523] "paleturquoise4"
                                  "palevioletred"
                                                          "palevioletred1"
## [526] "palevioletred2"
                                  "palevioletred3"
                                                          "palevioletred4"
## [529] "papayawhip"
                                  "peachpuff"
                                                          "peachpuff1"
## [532] "peachpuff2"
                                  "peachpuff3"
                                                          "peachpuff4"
## [535] "peru"
                                  "pink"
                                                          "pink1"
## [538] "pink2"
                                  "pink3"
                                                          "pink4"
                                  "plum1"
                                                          "plum2"
## [541] "plum"
## [544] "plum3"
                                  "plum4"
                                                          "powderblue"
## [547] "purple"
                                  "purple1"
                                                          "purple2"
## [550] "purple3"
                                  "purple4"
                                                          "red"
## [553] "red1"
                                  "red2"
                                                          "red3"
## [556] "red4"
                                  "rosybrown"
                                                          "rosybrown1"
## [559] "rosybrown2"
                                  "rosybrown3"
                                                          "rosybrown4"
## [562] "royalblue"
                                  "royalblue1"
                                                          "royalblue2"
## [565] "royalblue3"
                                  "royalblue4"
                                                          "saddlebrown"
## [568] "salmon"
                                  "salmon1"
                                                          "salmon2"
## [571] "salmon3"
                                  "salmon4"
                                                          "sandybrown"
## [574] "seagreen"
                                  "seagreen1"
                                                          "seagreen2"
## [577] "seagreen3"
                                  "seagreen4"
                                                          "seashell"
## [580] "seashell1"
                                  "seashell2"
                                                          "seashell3"
```

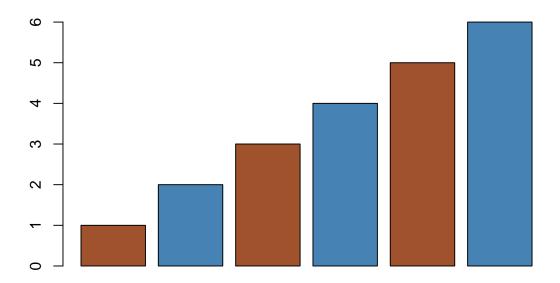
```
## [583] "seashell4"
                                 "sienna"
                                                          "sienna1"
## [586] "sienna2"
                                 "sienna3"
                                                          "sienna4"
## [589] "skyblue"
                                 "skyblue1"
                                                          "skyblue2"
                                 "skyblue4"
## [592] "skyblue3"
                                                          "slateblue"
## [595] "slateblue1"
                                 "slateblue2"
                                                          "slateblue3"
## [598] "slateblue4"
                                  "slategray"
                                                          "slategray1"
## [601] "slategray2"
                                  "slategray3"
                                                          "slategray4"
## [604] "slategrey"
                                  "snow"
                                                          "snow1"
## [607] "snow2"
                                                          "snow4"
                                  "snow3"
## [610] "springgreen"
                                 "springgreen1"
                                                          "springgreen2"
## [613] "springgreen3"
                                                          "steelblue"
                                 "springgreen4"
## [616] "steelblue1"
                                  "steelblue2"
                                                          "steelblue3"
## [619] "steelblue4"
                                  "tan"
                                                          "tan1"
## [622] "tan2"
                                  "tan3"
                                                          "tan4"
## [625] "thistle"
                                  "thistle1"
                                                          "thistle2"
## [628] "thistle3"
                                  "thistle4"
                                                          "tomato"
## [631] "tomato1"
                                 "tomato2"
                                                          "tomato3"
## [634] "tomato4"
                                 "turquoise"
                                                          "turquoise1"
                                 "turquoise3"
## [637] "turquoise2"
                                                          "turquoise4"
## [640] "violet"
                                  "violetred"
                                                          "violetred1"
## [643] "violetred2"
                                  "violetred3"
                                                          "violetred4"
## [646] "wheat"
                                  "wheat1"
                                                          "wheat2"
## [649] "wheat3"
                                                          "whitesmoke"
                                  "wheat4"
## [652] "yellow"
                                  "yellow1"
                                                          "yellow2"
## [655] "yellow3"
                                  "yellow4"
                                                          "yellowgreen"
barplot(1:6, col="sienna")
```



If colors are supplied as a vector, they alternate as shown bellow:



barplot(1:6, col=c("sienna", "steelblue"))



Shades of gray can be used by the function gray:

```
x<-1:50/50
gray(x)
```

```
## [1] "#050505" "#0A0A0A" "#0F0F0F" "#141414" "#1A1A1A" "#1F1F1F" "#242424"

## [8] "#292929" "#2E2E2E" "#333333" "#38388" "#3D3D3D" "#424242" "#474747"

## [15] "#4D4D4D" "#525252" "#575757" "#5C5C5C" "#616161" "#666666" "#6B6B6B"

## [22] "#707070" "#757575" "#7A7A7A" "#808080" "#858585" "#8A8A8A" "#8F8F8F"

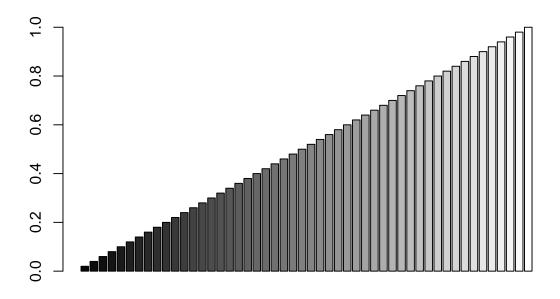
## [29] "#949494" "#999999" "#9E9E9E" "#A3A3A3" "#A8A8A8" "#ADADAD" "#B3B3B3"

## [36] "#B8B8B8" "#BDBDBD" "#C2C2C2" "#C7C7C7" "#CCCCCC" "#D1D1D1" "#D6D6D6"

## [43] "#DBDBDB" "#E0E0E0" "#E6E6E6" "#EBEBEB" "#F0F0F0" "#F5F5F5" "#FAFAFA"

## [50] "#FFFFFF"

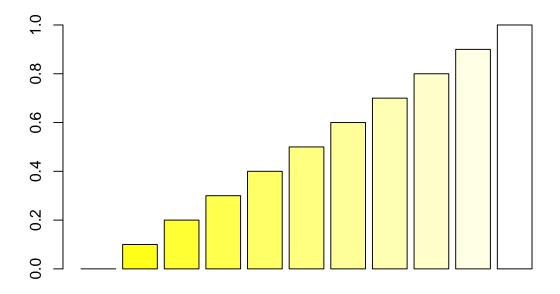
barplot(x, col=gray(x))
```



Colors can be also mixed from red, green and blue by the function rgb:

```
x<-0:10/10
rgb(1,1,x)

## [1] "#FFFF00" "#FFFF1A" "#FFFF33" "#FFFF4D" "#FFFF66" "#FFFF80" "#FFFF99"
## [8] "#FFFFB3" "#FFFFCC" "#FFFFE6" "#FFFFFF"
barplot(x, col=rgb(1,1,x))</pre>
```



You can try attractive palettes such as rainbow, heat.colors, terrain.colors, topo.colors and cm.colors.

Plots can be saved in many bitmap and vector graphical formats by functions png, jpeg, pdf, svg or ps. After invoking this function with file name as the argument no plot is shown. Instead it is saved to file. This property can be stopped by function dev.off():

```
png("plot.png")
barplot(1:6)
dev.off()

## pdf
## 2
```

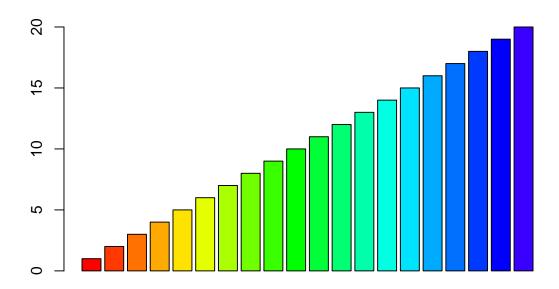
The plot is saved into working directory (see functions getwd and setwd).

R together with its packages makes it possible to plot graphs (in the sense of graph theory), heatmaps, word clouds, geographical maps and other special plot types.

0.0.3.1 Tips and tricks

• i often use function rainbow without the violet color:

```
barplot(1:20, col=rainbow(27)[1:20])
```



- high-resolution bitmap plots can be made in vector format and then converted to bitmap using your favorit graphical software
- alternatively, it is possible to use functions for bitmap plotting (e.g. png) with following modification:

```
x<-0:100
y<-0:100
png("plot.png", height=8, width=8, units='cm', res=600, pointsize=6)
gauss<-exp(-outer((x-50)**2/400,(y-50)**2/400,"+"))
image(x, y, gauss, col=heat.colors(100), axes=F)
contour(x, y, gauss, levels=0:10/10, add=TRUE, lwd=2, labcex=1.2)
axis(1, lwd=2)
axis(2, lwd=2)
box(lwd=2)
dev.off()</pre>
```

pdf ## 2

This plots the plot in doubled size. In order to further increase the size it is possible to multiply width, height and pointsize in png. However, it keeps the same widths of lines and other parameters. To fix this, avoid plotting axes by function image (axes=F) and instead plot wide axes and box separately. It can be easily modified for other plotting functions.

• to make a movie, use the output file name with regular expression and a loop:

```
png("plot%03d.png")
x<-0:100
y<-0:100
for(i in 25:75) {
   gauss<-exp(-outer((x-i)**2/400,(y-i)**2/400,"+"))
   image(x, y, gauss, col=heat.colors(100))
   contour(x, y, gauss, levels=0:10/10, add=TRUE)
}</pre>
```

```
dev.off()
## pdf
## 2
```

You can then use some video software (e.g. mencoder from Mplayer) to make a movie.

• a nice and popular plotting library from the "tidyverse" family is "ggplot2".

0.0.4 Random numbers in R

R can generate random numbers with different distributions. It is possible to generate ten random number with normal distribution with mean set to 20 and standard deviation set to 2 (default values are 0 and 1, respectively):

```
x<-rnorm(10, mean=20, sd=2)
x

## [1] 18.20982 20.95447 21.15001 18.33001 20.22682 22.18029 20.00108
## [8] 22.02769 21.65802 16.95783

mean(x)

## [1] 20.1696
sd(x)

## [1] 1.790716

The true mean and standard deviation are not exactly equal to pre-set values, but you can try with larger sets:
    x<-rnorm(10, mean=20, sd=2)
    mean(x)</pre>
```

```
mean(x)

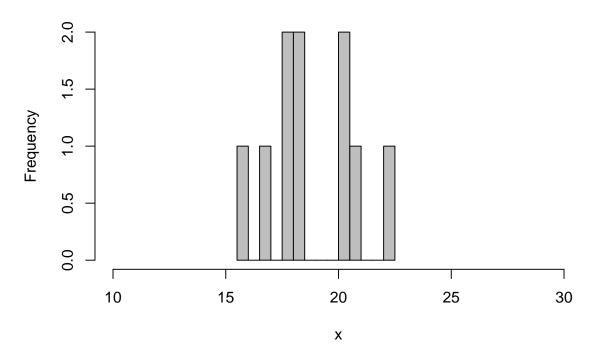
## [1] 18.79891

sd(x)

## [1] 2.041641
```

```
hist(x, br=20, xlim=c(10,30), col="gray")
```

Histogram of x

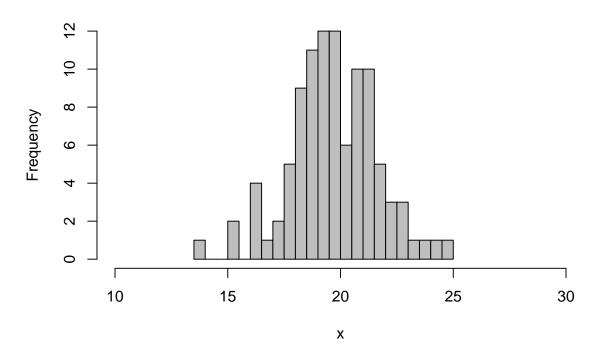


```
x<-rnorm(100, mean=20, sd=2)
mean(x)

## [1] 19.692
sd(x)

## [1] 1.948213
hist(x, br=20, xlim=c(10,30), col="gray")</pre>
```

Histogram of x



```
x<-rnorm(1000, mean=20, sd=2)
mean(x)
```

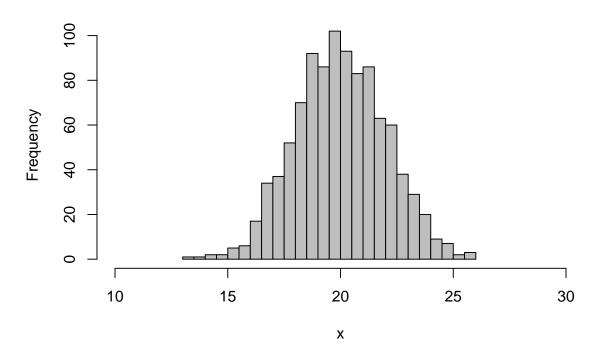
[1] 20.00122

sd(x)

[1] 1.999247

hist(x, br=20, xlim=c(10,30), col="gray")

Histogram of x



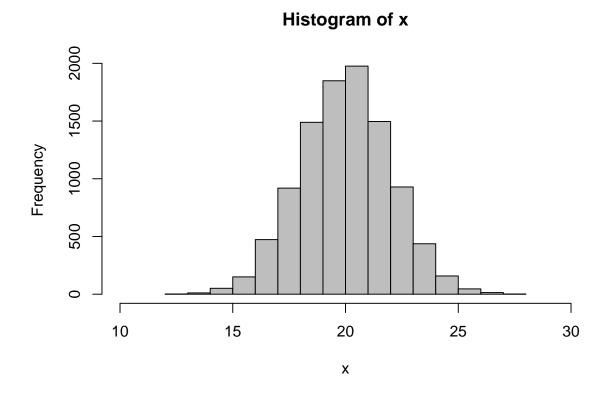
```
x<-rnorm(10000, mean=20, sd=2)
mean(x)</pre>
```

[1] 20.00076

sd(x)

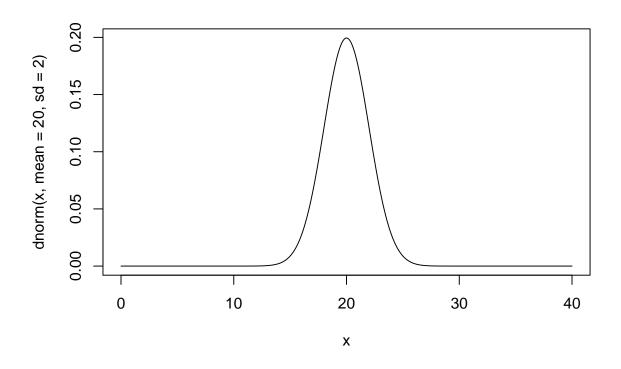
[1] 1.997412

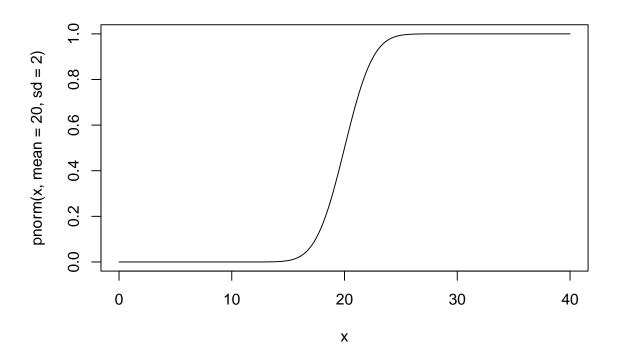
hist(x, br=20, xlim=c(10,30), col="gray")



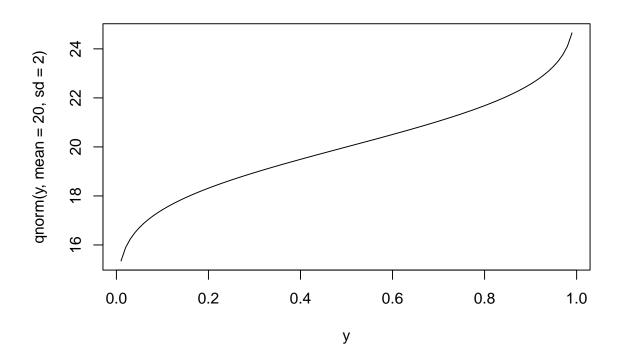
For normal distribution you can also calculate density by \mathtt{dnorm} , distribution function by \mathtt{pnorm} and quantile function by \mathtt{qnorm} :

```
x<-0:400/10
plot(x, dnorm(x, mean=20, sd=2), type="1")</pre>
```





y<-1:99/100 plot(y, qnorm(y, mean=20, sd=2), type="1")



The function pnorm is an integral of dnorm as you can see:

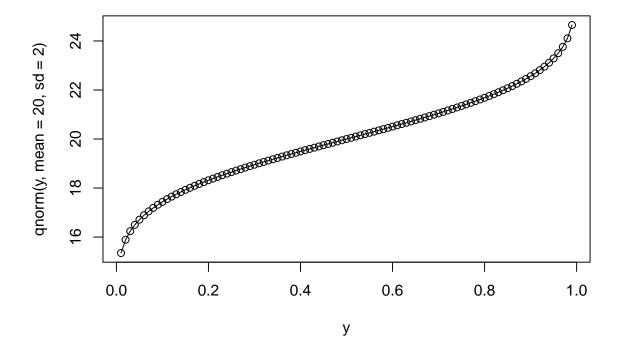
```
x<-0.1*0:230
sum(0.1*dnorm(x, mean=20, sd=2))

## [1] 0.9363903
pnorm(23, mean=20, sd=2)

## [1] 0.9331928

The function qnorm is an inverse function of pnorm:
y<-1:99/100
plot(y, qnorm(y, mean=20, sd=2), type="1")</pre>
```

```
y<-1:99/100
plot(y, qnorm(y, mean=20, sd=2), type="1")
x<-qnorm(y, mean=20, sd=2)
points(pnorm(x, mean=20, sd=2), x)</pre>
```



There are similar functions for other distributions such as chi-squared distribution (dchisq, pchisq, qchisq and rchisq), t-distribution (dt, pt, qt and rt), F-distribution (df, pf, qf and rf) and many others.

0.0.4.1 Tips and tricks

• you can set seed if you want to generate same random numbers:

```
set.seed(666)
rnorm(5)

## [1] 0.7533110 2.0143547 -0.3551345 2.0281678 -2.2168745
rnorm(5)

## [1] 0.75839618 -1.30618526 -0.80251957 -1.79224083 -0.04203245
set.seed(666)
rnorm(5)
```

0.0.5 Univariate descriptive statistics in R

Lets create a sample with mean and standard deviation set to 20 and 2, respectively:

```
x<-rnorm(10, mean=20, sd=2)
```

Basic measures of descriptive statistics, namely minimum, lower quartile, median, mean, upper quartile and maximum, can be obtained by function summary:

```
summary(x)
##
      Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                  Max.
     16.42
              16.77
                      19.16
                               19.29
                                        21.20
                                                 24.30
These values can be accessed by special functions:
min(x)
## [1] 16.41552
quantile(x, probs=0.25)
##
## 16.76667
median(x)
## [1] 19.15545
mean(x)
## [1] 19.29477
quantile(x, probs=0.75)
##
        75%
## 21.20466
max(x)
```

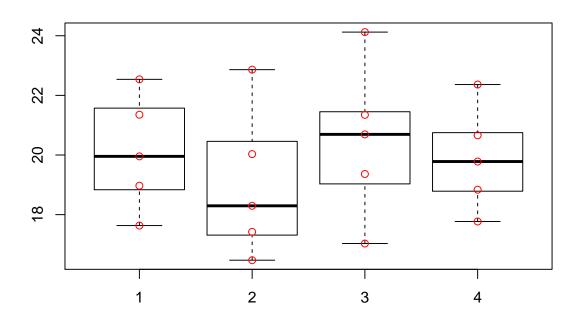
[1] 24.30009

Another useful function can be range.

distant it is depicted as a point. See bellow:

Important plot of univariate descriptive statistics is Tukey's box plot. It plots a box with bottom and top at lower and upper quartile (exactly, at values nearest to lower and upper quartile). The horizontal line is located at median. The whiskers start from the bottom and top of the box. Each whisker goes to maximum/minimum, but it is not longer than 1.5-times of interquartile range. It some point is more

```
x1<-rnorm(10, mean=20, sd=2)
x2<-rnorm(10, mean=20, sd=2)
x3<-rnorm(10, mean=20, sd=2)
x4<-rnorm(10, mean=20, sd=2)
boxplot(x1, x2, x3, x4)
points(1:4, c(min(x1),min(x2),min(x3),min(x4)), col="red")
points(1:4, c(max(x1),max(x2),max(x3),max(x4)), col="red")
points(1:4, c(median(x1),median(x2),median(x3),median(x4)), col="red")
points(1:4, c(quantile(x1,0.25),quantile(x2,0.25),quantile(x3,0.25),quantile(x4,0.25)), col="red")
points(1:4, c(quantile(x1,0.75),quantile(x2,0.75),quantile(x3,0.75),quantile(x4,0.75)), col="red")</pre>
```



Mean estimate can be calculated by function mean, or manually:

[1] 0.8531457

```
mean(x)
## [1] 19.29477
sum(x)/length(x)
## [1] 19.29477
Variance estimate can be calculated by function var, or manually:
var(x)
## [1] 7.278577
sum((x-mean(x))**2/(length(x)-1))
## [1] 7.278577
Standard deviation estimate can be calculated by function sd, or manually:
sd(x)
## [1] 2.697884
sqrt(var(x))
## [1] 2.697884
sqrt(sum((x-mean(x))**2/(length(x)-1)))
## [1] 2.697884
Standard error of the mean does not have own function in (basic) R, so we can calculate it manually:
sd(x)/sqrt(length(x))
```

0.0.5.1 Tips and tricks

• it is possible to index the function summary, e.g. to get minimum by index 1:

```
## Min.
## 16.41552
```

It is not really useful for this function, but you can use it later for other functions.

0.0.6 Confidence intervals in R

Confidence intervals can be calculated in R, for example, as mean +/- s.e.m. multiplied by quantile of t-distribution.

```
x<-rnorm(10, mean=20, sd=2)
sem<-sd(x)/sqrt(length(x))
mean(x)+sem*qt(p=c(0.025,0.975), df=(length(x)-1))</pre>
```

```
## [1] 18.31697 21.51018
```

The function qt(p=c(0.025,0.975), df=(length(x)-1)) returns quantile of t-distribution for p=0.025 and 0.975, i.e. for 95 % probability. For 90 % use p=c(0.05,0.95), for 99 % use p=c(0.005,0.995) etc.

If you generate 100 random samples (each with 10 items) with mean set to 20 and standard deviation set to 2, you should expect that 95 samples will contain 20 in the confidence interval and 5 will not. Let's try:

```
good<-0
for(i in 1:100) {
    x<-rnorm(10, mean=20, sd=2)
    sem<-sd(x)/sqrt(length(x))
    ci<-mean(x)+sem*qt(p=c(0.025,0.975), df=(length(x)-1))
    if((ci[1]<20)&&(ci[2]>20)) {
       good<-good+1
    }
}
good</pre>
```

[1] 96

I obtained 97, close to expected 95.

0.0.6.1 Tips and tricks

• confidence interval can be obtained more easily by t.test as will be shown later:

```
x<-rnorm(10, mean=20, sd=2)
t.test(x)$conf.int

## [1] 18.72790 20.51576
## attr(,"conf.level")
## [1] 0.95
t.test(x)$conf.int[1:2]

## [1] 18.72790 20.51576
sem<-sd(x)/sqrt(length(x))
mean(x)+sem*qt(p=c(0.025,0.975), df=(length(x)-1))</pre>
```

[1] 18.72790 20.51576

0.0.7 One-sample t-test in R

Confidence interval and one-sample t-test are two sides of the same coin. Let us calculate 95 % confidence interval for a sample generated by function rnorm:

```
x<-rnorm(10, mean=20, sd=2)
sem<-sd(x)/sqrt(length(x))
mean(x)+sem*qt(p=c(0.025,0.975), df=(length(x)-1))</pre>
```

```
## [1] 18.40536 21.46257
```

We can make a two-tailed t-test (at the significance level of 5%) with the null hypothesis that the mean of x is equal to 20. The null hypothesis is rejected if 20 is outside the confidence interval. You can replace p=c(0.025,0.975) by p=c(0.005, 0.995) for the significance level 1 % etc.

Another option is to calculate criterion R and compare it with corresponding quantile of t-distribution:

```
R<-abs(mean(x)-20)*sqrt(length(x))/sd(x)
R
```

```
## [1] 0.09772072
qt(p=0.975, df=(length(x)-1))
```

```
## [1] 2.262157
```

sample estimates:

mean of x ## 19.93397

The null hypothesis is rejected if R is bigger than the quantile of t-distribution.

The most convinient t-test option is to use the function t.test:

```
t.test(x, mu=20)
```

```
##
## One Sample t-test
##
## data: x
## t = -0.097721, df = 9, p-value = 0.9243
## alternative hypothesis: true mean is not equal to 20
## 95 percent confidence interval:
## 18.40536 21.46257
## sample estimates:
## mean of x
## 19.93397
```

The null hypothesis is rejected if p-value is lower than 0.05 (or 0.01 for the significance level of 1 %). The function t.test also provides the criterion R (called t), degrees of freedom, confidence interval and mean.

```
One-tailed t-test can be done similarly:
mean(x)+sem*qt(p=c(0,0.95), df=(length(x)-1))

## [1]    -Inf 21.17265

t.test(x, mu=20, alternative="less")

##
## One Sample t-test
##
## data: x
## t = -0.097721, df = 9, p-value = 0.4621
## alternative hypothesis: true mean is less than 20
## 95 percent confidence interval:
##    -Inf 21.17265
```

```
mean(x)+sem*qt(p=c(0.05,1), df=(length(x)-1))
## [1] 18.69528
                     Inf
t.test(x, mu=20, alternative="greater")
##
##
    One Sample t-test
##
## data: x
## t = -0.097721, df = 9, p-value = 0.5379
## alternative hypothesis: true mean is greater than 20
## 95 percent confidence interval:
## 18.69528
## sample estimates:
## mean of x
## 19.93397
0.0.7.1 Tips and tricks
  • you can iterate on the results of the function t.test:
tt < -t.test(x, mu=20)
tt
##
##
   One Sample t-test
##
## data: x
## t = -0.097721, df = 9, p-value = 0.9243
## alternative hypothesis: true mean is not equal to 20
## 95 percent confidence interval:
## 18.40536 21.46257
## sample estimates:
## mean of x
## 19.93397
tt[3]
## $p.value
## [1] 0.9242958
  • you can change the significance level for the confidence interval by parameter conf.level:
t.test(x, mu=20)
##
## One Sample t-test
##
## data: x
## t = -0.097721, df = 9, p-value = 0.9243
## alternative hypothesis: true mean is not equal to 20
## 95 percent confidence interval:
## 18.40536 21.46257
## sample estimates:
## mean of x
## 19.93397
t.test(x, mu=20, conf.level=0.99)
##
```

One Sample t-test

```
##
## data: x
## t = -0.097721, df = 9, p-value = 0.9243
## alternative hypothesis: true mean is not equal to 20
## 99 percent confidence interval:
## 17.73796 22.12997
## sample estimates:
## mean of x
## 19.93397
t.test(x, mu=20, conf.level=0.999)
##
##
   One Sample t-test
##
## data: x
## t = -0.097721, df = 9, p-value = 0.9243
## alternative hypothesis: true mean is not equal to 20
## 99.9 percent confidence interval:
## 16.70337 23.16456
## sample estimates:
## mean of x
## 19.93397
```

0.0.8 Two-sample t-test in R

Let us skip a "manual" version of the t-test and proceed directly to the function t.test. There are two variants of two-sample t-test, one for equal variances and one for unequal variances. First let us test whether the variances are equal:

```
healthy<-rnorm(10, mean=12.3, sd=3.3)
healthy
## [1] 12.596588 13.572485 10.099827 10.561580 9.708413 11.412490 15.757506
   [8] 8.584591 14.155399 14.302581
sick<-rnorm(10, mean=8.5, sd=3.3)
sick
##
   [1] 5.909912 3.763672 13.606515 9.789544 7.131921 9.517881 9.578317
   [8] 9.001416 12.707699 9.659650
var.test(healthy, sick)
##
##
   F test to compare two variances
##
## data: healthy and sick
## F = 0.64615, num df = 9, denom df = 9, p-value = 0.5256
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 0.1604936 2.6013805
## sample estimates:
## ratio of variances
            0.6461461
##
```

The null hypothesis of the var.test is that variance of both samples are equal. We can reject the null hypothesis when p-value is lower than 0.05 (for the significance level of 5 %).

The null hypothesis of t-test is that both means are equal. We can reject the null hypothesis when p-value is lower than 0.05 (for the significance level of 5%). For samples with equal variances we will use t-test

with var.equal=TRUE. For samples with unequal variances we will use t-test with var.equal=FALSE (default):

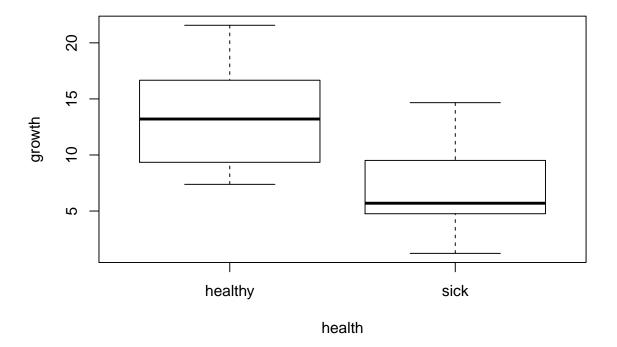
```
t.test(healthy, sick, var.equal=TRUE)
   Two Sample t-test
##
##
## data: healthy and sick
## t = 2.5344, df = 18, p-value = 0.02077
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.5145616 5.5024248
## sample estimates:
## mean of x mean of y
## 12.075146 9.066653
t.test(healthy, sick, var.equal=FALSE)
##
##
   Welch Two Sample t-test
##
## data: healthy and sick
## t = 2.5344, df = 17.205, p-value = 0.02125
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.5062757 5.5107107
## sample estimates:
## mean of x mean of y
## 12.075146 9.066653
Paired t-test is used when values in both samples can be paired, e.g. one sample represents blood pressure
of patients before and one sample after treatment. It is better to evaluate differences for individual
patients one by one, rather than whole samples. The t-test can be switched to paired by paired=TRUE:
x<-rnorm(10, mean=20, sd=5)
X
## [1] 21.857982 17.924920 7.460842 12.732419 21.253695 25.524013 21.579099
## [8] 21.658019 22.710094 22.366305
y<-x+rnorm(10, mean=2, sd=0.5)
У
    [1] 23.52077 19.22655 10.37449 14.20998 22.78327 27.48872 24.22182
   [8] 24.61163 25.39220 24.07541
t.test(x,y)
##
## Welch Two Sample t-test
##
## data: x and y
## t = -0.8602, df = 17.999, p-value = 0.401
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -7.173033 3.005540
## sample estimates:
## mean of x mean of y
## 19.50674 21.59049
t.test(x,y, paired=TRUE)
```

```
##
## Paired t-test
##
## data: x and y
## t = -10.23, df = 9, p-value = 2.96e-06
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -2.544514 -1.622978
## sample estimates:
## mean of the differences
## -2.083746
```

0.0.8.1 Tips and tricks

- the function t.test always gives a résumé on the alternative hypothesis, you can use it if you are not sure which variant of test should be used
- the function t.test (as well as plot) can use class 'formula' as the input. We will use it frequently in next lessons, so let us try it now:

```
healthy<-rnorm(10, mean=12.3, sd=3.3)
sick<-rnorm(10, mean=8.5, sd=3.3)
growth<-c(healthy, sick)
health<-rep(c("healthy", "sick"), each=10)
df<-data.frame(health, growth)
plot(growth~health, data=df)</pre>
```



```
t.test(growth~health, data=df)

##
## Welch Two Sample t-test
##
## data: growth by health
```

```
## t = 3.1218, df = 17.969, p-value = 0.005901
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.010189 10.287258
## sample estimates:
## mean in group healthy mean in group sick
## 13.247098 7.098375
```

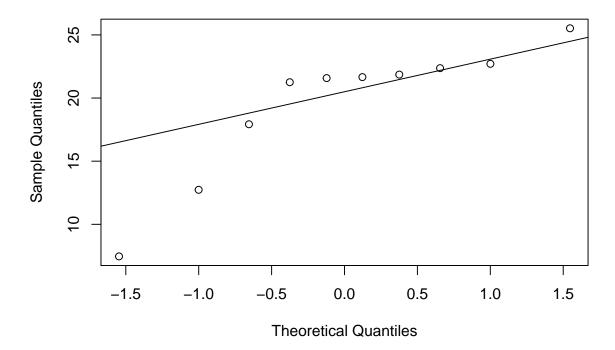
0.0.9 Non-parametric tests

Let us try with something non-normal

Up to now we considered normal distribution of a variable. Here we will show how we can test whether the variable follows the normal distribution and what can we do if data do not follow normal distribution. There is a graphical tool to do that known as QQ-plot.

```
qqnorm(x)
qqline(x)
```

Normal Q-Q Plot



The function calculates the mean and the standard deviation for the sample and from this it calculates quantiles. Then it plots the values of the sample vs. quantiles. This plot should be linear. If not, it means that the distribution is right or left skewed, bimodal or non-normal in some other way.

QQ-plot is good for visual evaluation, but for a quantitative evaluation it is useful to use some test of normality. One of them is the test developed by Shapiro and Wilk. You can run it by:

```
x<-rnorm(20)
shapiro.test(x)

##
## Shapiro-Wilk normality test
##
## data: x
## W = 0.94727, p-value = 0.3276</pre>
```

```
x<-c(rnorm(10), rnorm(10, mean=4))
shapiro.test(x)
##</pre>
```

```
## Shapiro-Wilk normality test
##
## data: x
## W = 0.90985, p-value = 0.06332
```

The null hypothesis is that the sample follows the normal distribution.

What about if data do not follow the normal distribution? A non-parametric (i.e. not requiring normal distribution) alternative to t-test is Wilcoxon test. The two-sample variant is also known as Mann-Whitney test. We can use the function wilcox.test. It is used the same way as t-test:

```
x < -rnorm(10)
y < -rnorm(10, mean=2)
wilcox.test(x,y)
##
    Wilcoxon rank sum test
##
##
## data: x and y
## W = 1, p-value = 2.165e-05
## alternative hypothesis: true location shift is not equal to 0
Let us try to compare with t-test:
t.test(x,y)
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -5.5487, df = 17.62, p-value = 3.107e-05
\#\# alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -3.123008 -1.405660
## sample estimates:
## mean of x mean of y
## -0.3262392 1.9380948
```

0.0.9.1 Tips and tricks

• non-parametric variant of analysis of variance will be shown later.

0.0.10 Analysis of Variance

Analysis of Variance (ANOVA) is an extension of t-test to more than two samples. The null hypothesis is that all samples have the same mean. We simply cannot do a pairwise t-test because this increases probability of rejection of the null hypothesis simply by chance. First, let us show a "manual" version of ANOVA for three samples, one representing a biological parameter of patients who were administered a drug, one representing a control group and one representing patients administered a placebo:

```
drug<-rnorm(10, mean=70, sd=30)
control<-rnorm(10, mean=100, sd=25)
placebo<-rnorm(10, mean=90, sd=25)
drug</pre>
```

```
## [1] 66.72068 56.33683 81.62437 83.51047 116.77867 47.73066 84.01318 ## [8] 58.20104 57.83262 61.71645
```

control

```
## [1] 61.57471 105.89935 94.36642 147.30065 96.95527 101.27382 98.30794
## [8] 53.29537 106.48794 64.26199
placebo
```

```
## [1] 100.11741 65.28788 105.92620 46.17389 85.25819 73.85201 119.71384 ## [8] 124.62775 110.25343 81.03393
```

First, let us calculate variances in each group:

```
sdrug<-sum((drug-mean(drug))^2)
scontrol<-sum((control-mean(control))^2)
splacebo<-sum((placebo-mean(placebo))^2)</pre>
```

We will sum this and we will call it sum of squares within the group (SSW):

```
SSW<-scontrol+sdrug+splacebo
```

Next, we will concatenate all samples and calculate mean of this supersample. We will call the variance of the supersample as sum of squares total (SST):

```
all<-c(control, drug, placebo)
SST<-sum((all-mean(all))^2)</pre>
```

In an extreme example that means of all samples are the same, the SSW and SST are the same, otherwise SST is bigger than SSW. The difference of SST and SSW is thus a measure of difference between the samples. We will call this sum of squares between the groups (SSB):

```
SSB<-SST-SSW
```

The criterion with the F-distribution is calculated as:

```
FE<-(SSB*27)/(SSW*2)
FE
```

```
## [1] 2.373428
```

with two degrees of freedom, 27 is the total number of values minus number of samples (30-3), and 2 is number of samples minus 1. Finally, we will compare this with the value of the quantile of F-distribution:

```
qf(p=0.95, df1=2, df2=27)
```

```
## [1] 3.354131
```

If the FE is higher than qf we can reject the null hypothesis (i.e. that means of samples are the same).

In an automated way we can make use of a data frame:

```
labels<-rep(c("control", "drug", "placebo"), each=10)
all<-c(control, drug, placebo)
df<-data.frame(labels, all)</pre>
```

We will make a model by the function analysis of variance and we will obtain all results by summary of the model:

```
mymodel<-aov(all~labels, data=df)
mymodel</pre>
```

```
## Call:
## aov(formula = all ~ labels, data = df)
##
## Terms:
## labels Residuals
## Sum of Squares 2858.616 16259.737
## Deg. of Freedom 2 27
```

```
##
## Residual standard error: 24.54002
## Estimated effects may be unbalanced
summary(mymodel)
##
               Df Sum Sq Mean Sq F value Pr(>F)
## labels
                2
                    2859 1429.3
                                    2.373 0.112
## Residuals
                   16260
                            602.2
               27
We can reject the null hypothesis on the basis of the p-value. The same result can be obtained by:
anova(lm(all~labels, data=df))
## Analysis of Variance Table
##
## Response: all
             Df Sum Sq Mean Sq F value Pr(>F)
## labels
              2 2858.6 1429.31 2.3734 0.1123
## Residuals 27 16259.7 602.21
```

Data for ANOVA must follow normal distribution and there must be homogeneous variances of samples. For other than normal distribution try data transformation or Kruskal-Walis test (bellow). For different variances try transformation.

0.0.10.1 Tips and Tricks

Terms:

Sum of Squares

##

- to test normality of data you can use the function mshapiro.test. It is a multivariate alternative to Shapiro and Wilk test.
- to test homogeneity of variances you can use bartlett.test or fligner.test.
- Kruskal-Wallis rank sum test (kruskal.test) is a non-parametric alternative to ANOVA:

```
###
## Kruskal-Wallis rank sum test
##
## data: all by labels
```

• two-way ANOVA will be introduced together with linear models.

Kruskal-Wallis chi-squared = 4.2916, df = 2, p-value = 0.117

0.0.11 P-value adjustment and other approaches for multiple comparisons

In the previous chapter we have shown ANOVA on drug testing example:

labels Residuals

136.47 15732.58

```
drug<-rnorm(10, mean=70, sd=30)
control<-rnorm(10, mean=100, sd=25)
placebo<-rnorm(10, mean=90, sd=25)
labels<-rep(c("control", "drug", "placebo"), each=10)
all<-c(control, drug, placebo)
df<-data.frame(labels, all)
mymodel<-aov(all~labels, data=df)
mymodel</pre>
## Call:
## aov(formula = all ~ labels, data = df)
###
```

```
## Deg. of Freedom 2 27
##
## Residual standard error: 24.13893
## Estimated effects may be unbalanced
summary(mymodel)
## Df Sum Sq Mean Sq F value Pr(>F)
```

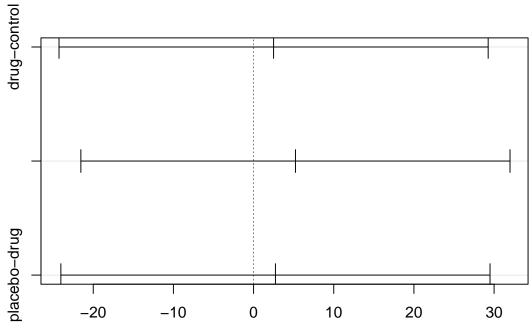
labels 2 136 68.2 0.117 0.89 ## Residuals 27 15733 582.7

This shows that there is a difference between the means. Next we want to know which samples are statistically significantly lower and higher. Again we cannot make a pairwise t-tests because of probability of rejection of the null hypothesis by chance. Instead we can use Tukey Honest Significance Test:

TukeyHSD(mymodel)

```
##
     Tukey multiple comparisons of means
##
       95% family-wise confidence level
##
## Fit: aov(formula = all ~ labels, data = df)
##
## $labels
##
                       diff
                                   lwr
                                            upr
## drug-control
                   2.495872 -24.27008 29.26183 0.9709940
## placebo-control 5.222671 -21.54328 31.98863 0.8795351
                   2.726799 -24.03916 29.49275 0.9654842
## placebo-drug
plot(TukeyHSD(mymodel))
```

95% family-wise confidence level



Differences in mean levels of labels

Alternatively it is possible to do a pairwise t-test and adjust p-values by pairwise.t.test:

```
pairwise.t.test(all, labels, p.adjust.method="none")
```

##

```
## Pairwise comparisons using t tests with pooled SD
##
## data: all and labels
##
## control drug
## drug 0.82 -
## placebo 0.63 0.80
##
## P value adjustment method: none
```

The option p.adjust.method can be "none" (no adjustment), "bonferroni" (Bonferroni correction), "holm" (Holm and Bonferroni) and "BH" or "fdr" (Benjamini and Hochberg). There is also an option pool.sd defining whether variances are homogeneous.

0.0.11.1 Tips and Tricks

##

##

##

• in biological sciences we often compare every sample with a single control. For this it is useful to use Dunnett test. It requires package multicomp:

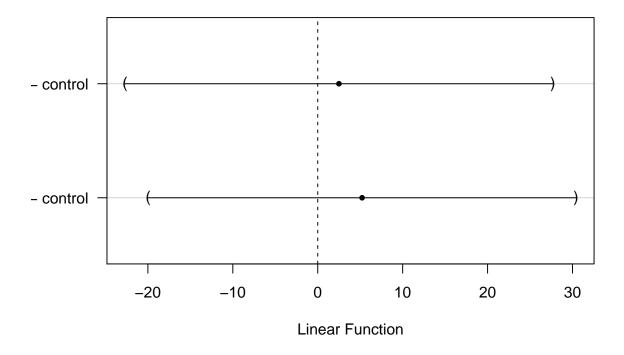
```
require(multcomp)
## Loading required package: multcomp
## Loading required package: mvtnorm
## Loading required package: survival
## Loading required package: TH.data
## Loading required package: MASS
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
##
## Attaching package: 'TH.data'
## The following object is masked from 'package:MASS':
##
##
       geyser
mydata <- data.frame(labels, all)</pre>
We must define that the first sample is the control:
mydata$labels <- relevel(mydata$labels, ref=1)</pre>
Finally, we will do the Dunnett test:
mydata.aov <- aov(all~labels, data=mydata)</pre>
mydata.dunnett <- glht(mydata.aov, linfct = mcp(labels="Dunnett"))</pre>
summary(mydata.dunnett)
##
##
     Simultaneous Tests for General Linear Hypotheses
```

Multiple Comparisons of Means: Dunnett Contrasts

Fit: aov(formula = all ~ labels, data = mydata)

```
## Linear Hypotheses:
##
                           Estimate Std. Error t value Pr(>|t|)
## drug - control == 0
                              2.496
                                        10.795
                                                  0.231
                                                           0.962
## placebo - control == 0
                              5.223
                                        10.795
                                                  0.484
                                                           0.845
## (Adjusted p values reported -- single-step method)
Confidence intervals can be calculated as:
confint(mydata.dunnett)
##
     Simultaneous Confidence Intervals
##
## Multiple Comparisons of Means: Dunnett Contrasts
##
##
## Fit: aov(formula = all ~ labels, data = mydata)
## Quantile = 2.3335
## 95% family-wise confidence level
##
## Linear Hypotheses:
                           Estimate lwr
                                              upr
## drug - control == 0
                             2.4959 -22.6953
                                              27.6870
## placebo - control == 0
                             5.2227 -19.9685 30.4138
You can also make a plot:
plot(mydata.dunnett)
```

95% family-wise confidence level



• in biological sciences it is popular to use barplots and other similar plots with star symbols indicating the significance of a test, often with a horizontal lines that connect tested samples. In R you can generate such plots by the package "ggplot2" with "ggsignif" and "ggpubr".

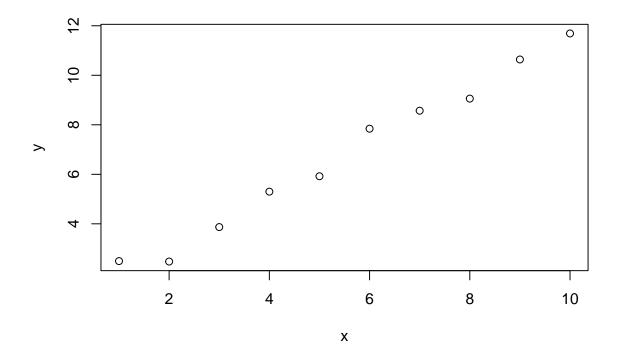
0.0.12 Bi- and multivariate descriptive statistics

Let us generate a set of two well correlating variables ${\tt x}$ and ${\tt y}$:

```
x<-1:10
y<-2:11+rnorm(10, sd=0.5)
x

## [1] 1 2 3 4 5 6 7 8 9 10
y

## [1] 2.494846 2.476638 3.869040 5.299605 5.921994 7.842900 8.569087
## [8] 9.058114 10.638189 11.689659
plot(x,y)</pre>
```



Covariance can be calculated manually as:

```
sum((x-mean(x))*(y-mean(y)))/(length(x)-1)
```

[1] 9.864383

Pearson correlation can be calculated as:

```
 sum((x-mean(x))*(y-mean(y)))/sqrt(sum((x-mean(x))^2)*sum((y-mean(y))^2))
```

[1] 0.9934884

In R they can be calculated as:

```
cov(x,y)
```

```
## [1] 9.864383
cor(x,y)
```

[1] 0.9934884

Correlation can be calculated by dividing covariance by standard deviations of both variables:

```
cov(x,y)/(sd(x)*sd(y))
```

```
## [1] 0.9934884
```

0.0.12.1 Tips and Tricks

• it is possible to apply these functions on data frame or matrix. This will make a pairwise correlation of all columns.

0.0.13 Linear models

In R you can use function 1m to build a linear model. It can fit a dependent variable by one or multiple independent variables. Independent variables can quantitative, categorical or both.

```
x<-1:10
y<-2:11+rnorm(10, sd=0.5)
linfit <- lm(y~x)
linfit

##
## Call:
## lm(formula = y ~ x)
##
## Coefficients:
## (Intercept) x
## 1.4602 0.9131</pre>
```

This will show that "y" grows with "x". However, if you fit two noisy variables you will always obtain a result that "y" grows or descends with "x", there almost no chance to get zero slope even if the two variables completely uncorrelated. The question is whether the non-zero slope is statistically significant. This you can learn by function summary:

```
summary(linfit)
```

```
##
## Call:
## lm(formula = y \sim x)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -0.34555 -0.27653 -0.07201 0.24391
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                1.46017
                           0.22603
                                       6.46 0.000196 ***
## x
                                      25.07 6.87e-09 ***
                0.91309
                           0.03643
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.3309 on 8 degrees of freedom
## Multiple R-squared: 0.9874, Adjusted R-squared: 0.9859
## F-statistic: 628.3 on 1 and 8 DF, p-value: 6.869e-09
```

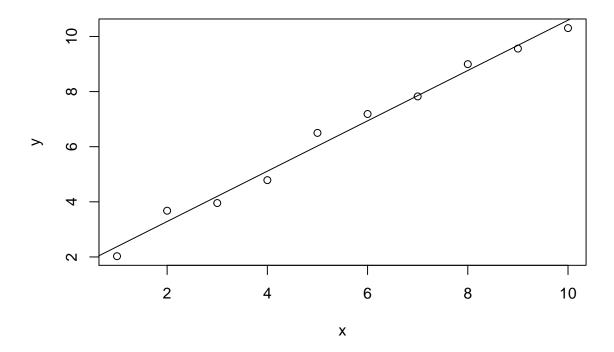
This is an extension of ANOVA in the way that the independent variable is not categorical (such as "control", "placebo" and "drug") but it is quantitative. The testing procedure is similar to that of ANOVA, the program calculates a sum of squares of error under assumption of null and alternative hypothesis and compares them.

There are several possibilities to describe models in the lm function:

function	expression in 1m
f(x) = alpha	y~1
f(x) = alpha + beta x	y~x
f(x) = beta x	y~-1+x
$f(x) = alpha + beta x + gamma x^2$	y~x+I(x^2)
$f(x) = alpha + beta_1 x_1 + beta_2 x_2$	y~x1+x2
$f(x) = alpha + beta_1 x_1 + beta_2 x_2 + gamma x_1 x_2$	y~x1*x2

To get values of coefficients you can print coefficients:

```
linfit$coefficients
## (Intercept)
     1.4601671
                  0.9130868
They can be iterated:
linfit$coefficients[1]
## (Intercept)
      1.460167
##
linfit$coefficients[2]
##
## 0.9130868
Alternatively you may use the function coef:
coef(linfit)[1]
## (Intercept)
      1.460167
coef(linfit)[2]
##
## 0.9130868
To plot a model into data you can use function abline:
plot(x,y)
abline(linfit)
```



The function predict predicts values of y for values of x based on the model. If you use:

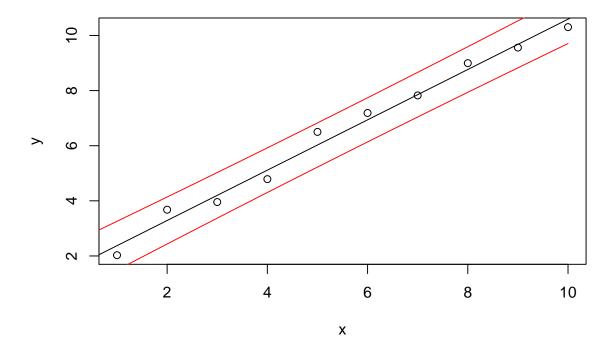
```
newy<-predict(object=linfit)</pre>
```

it will calculate values of y for each x by a linear model. If you want to calculate this for some other values of x (here called "newx") you can type:

```
newx<-0:100/10
newy<-predict(object=linfit, newdata=data.frame(x=newx))</pre>
```

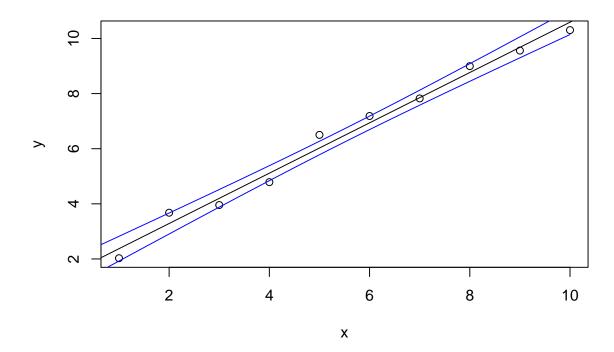
More interesting is calculation of confidence intervals. You can use:

```
newx<-0:100/10
newy<-predict(object=linfit, newdata=data.frame(x=newx), interval = 'prediction')
plot(x,y)
abline(linfit)
lines(newx, newy[,2], col="red")
lines(newx, newy[,3], col="red")</pre>
```



This will plot an interval to which 95 % of samples should fall (the level could be changed by option level). If you change "prediction" to "confidence" it will print confidence intervals for the model. Provided that there is some exact linear relationships between x and (inaccurately measured) y, we can accurately determine this relationship by doing an infinite number of measurements. If we do enough measurements we can get a vary narrow confidence interval:

```
newx<-0:100/10
newy<-predict(object=linfit, newdata=data.frame(x=newx), interval = 'confidence')
plot(x,y)
abline(linfit)
lines(newx, newy[,2], col="blue")
lines(newx, newy[,3], col="blue")</pre>
```



Prediction intervals are analogous to standard deviation, confidence intervals to standard error of the mean.

0.0.13.1 Tips and Tricks

- you can compare models "model1" and "model2" by anova(model2, model1). This will tell you whether "model2" is significantly better than "model1".
- as already mentioned, linear models can use continuous as well as categorical independent variables. In order to do ANOVA with two factors use a linear model with y~x1+x2. In order to do ANOVA with two factors and their interactions use a linear model with y~x1+x2. Beside other ANOVA presumptions (normal distribution, homogeneity of variances) it is necessary to
- contingency tables are an alternative to ANOVA with categorical dependent and independent variables. To test statistical significance you can use chisq.test function.

0.0.14 Principal Component Analysis

Principal Component Analysis (PCA) is frequently used data analysis method. Let us demonstrate it on the results of Tour de France 2013. You can load the data by typing:

tdf <- read.table("https://raw.githubusercontent.com/spiwokv/Rtutorial/master/data/tourdefrance2013.

Every frame corresponds to a single rider (riders that did not finish the race were removed). The numbers in the table corresponds to their order in each stage. Each column corresponds to one stage. One stage was removed. It was a team time trial where order is given to teams rather than individual riders. It is very complicated to somehow visualize this data, because they are 20-dimensional (because of 20 stages). This is a great opportunity for PCA. Let us try on column 3-22 containing the results:

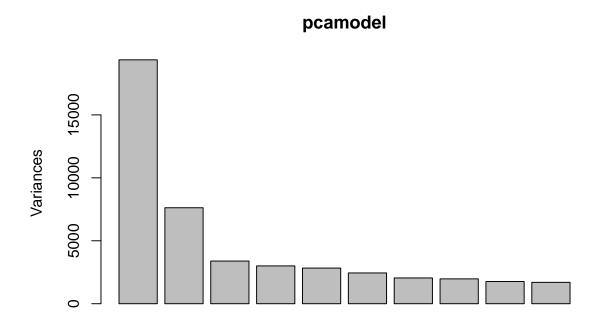
```
pcamodel <- prcomp(tdf[,3:22])
summary(pcamodel)</pre>
```

Importance of components:

```
##
                               PC1
                                       PC2
                                                 PC3
                                                          PC4
                                                                  PC5
                                                                           PC6
## Standard deviation
                          139.1883 87.3118 58.21738 54.80780 53.2064 49.44327
## Proportion of Variance
                                    0.1376  0.06118  0.05422  0.0511  0.04413
                            0.3497
## Cumulative Proportion
                            0.3497
                                    0.4873
                                            0.54851
                                                      0.60274
                                                               0.6538
                                                                       0.69797
##
                               PC7
                                        PC8
                                                  PC9
                                                          PC10
                                                                  PC11
## Standard deviation
                          45.24812 44.44331 42.01020 41.20537 39.0335 37.1382
## Proportion of Variance
                          0.03696
                                    0.03566
                                             0.03186
                                                      0.03065
                                                                0.0275
                                                                        0.0249
## Cumulative Proportion
                           0.73493
                                    0.77058
                                             0.80244
                                                       0.83309
                                                                0.8606
                                                                        0.8855
##
                              PC13
                                       PC14
                                                 PC15
                                                          PC16
                                                                   PC17
## Standard deviation
                          36.58104 31.85483 30.65858 27.58704 26.54836
## Proportion of Variance
                          0.02416
                                    0.01832
                                             0.01697
                                                      0.01374
                                                               0.01272
## Cumulative Proportion
                           0.90965
                                    0.92797
                                             0.94493
                                                       0.95867
##
                              PC18
                                       PC19
                                                 PC20
## Standard deviation
                          24.58404 23.35946 20.84627
## Proportion of Variance
                                    0.00985
                                             0.00784
                           0.01091
## Cumulative Proportion
                           0.98231
                                    0.99216
                                             1.00000
```

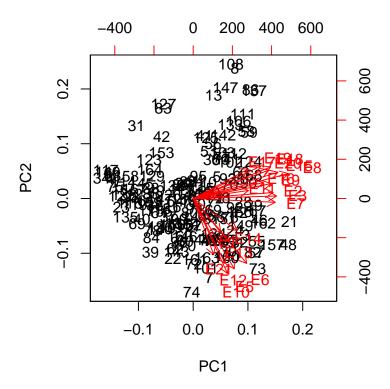
To plot importance of components you can use plot function on the model:

plot(pcamodel)



This shows that there is 1-2 important components describing the data very well. You can plot PC1 vs. PC2:

biplot(pcamodel)



Each number in black corresponds to the number of line in the tdf table. You can print their names as: tdf [108,2]

```
## [1] Mark_Cavendish_GBr_Omega_Pharma_Quick_Step
## 170 Levels: Adam_Hansen_Aus_Lotto_Belisol ... Yury_Trofimov_Rus_Katusha
```

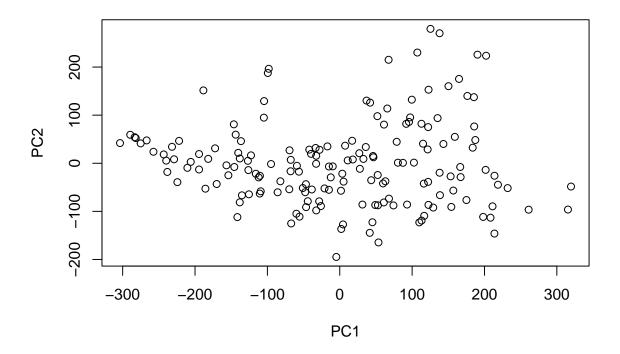
to reveal the identity of the rider 108. The red arrows show the relationships between the original data and the results of the PCA. For example, some arrows point right and some point to the bottom. The former correspond to mountain stages. The later to flat stages.

From the results of PCA you can recognize that rider on left side of the plot are those who reached best in the overall classification of the race. These are typically slim mountain stage specialists who scored well in mountain stages (the arrow points right, more right means higher place in a mountain stage).

Riders at the top reached good results in flat stages. These are typically masculine riders who perform poorly in mountain stages. Riders in the bottom right cloud are "domestiques" who don't care much about their own results or rides who bet on just one stage and performed poorly in other stages.

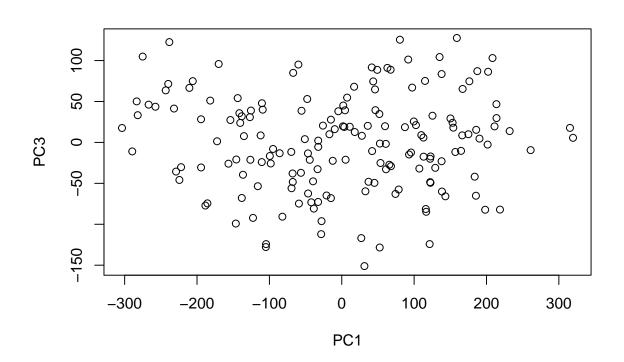
0.0.14.1 Tips and Tricks

- the data can be centered and or normalized before PCA. Centering is a usual step in PCA and PCA without centering is rarely used. Normalization is used if you analyze apples and pears. They are controlled by: center, scale. (note: there is a dot after "scale").
- you can use PC1 and PC2 values using predict function, e.g.:



To plot PC1 vs. PC3 use:

plot(predict(pcamodel)[,c(1,3)])



0.0.15 Cluster Analysis

We can demonstrate cluster analysis on the same dataset as PCA:

```
tdf <- read.table("https://raw.githubusercontent.com/spiwokv/Rtutorial/master/data/tourdefrance2013.
```

First let us try non-hierarchical clustering by K-means method. For this we have to chose the number of cluster (the value of K). For example we have some feeling that there are 5 clusters of riders such as general classification specialists, sprinters, combined, domestiques and those who bet on just one or few stages. This can be done by:

```
kmodel \leftarrow kmeans(tdf[,3:22], 5)
kmodel
## K-means clustering with 5 clusters of sizes 31, 49, 16, 37, 37
## Cluster means:
##
                                      E2
                                                       E3
                                                                        E5
                                                                                          E6
                                                                                                           E7
                                                                                                                            E8
## 1 119.22581 140.16129 141.64516 148.22581 145.64516 142.96774 144.77419
## 2 114.73469
                          78.20408 69.61224 104.85714 106.87755
                                                                                                73.77551
                                                                                                                 64.59184
## 3 87.50000 155.62500 152.56250
                                                            35.62500
                                                                               39.62500 146.56250 152.75000
## 4 72.02703
                         48.54054
                                           43.29730
                                                              55.10811
                                                                               45.37838
                                                                                                40.45946
## 5 102.32432 111.97297 125.64865 104.70270 116.51351
                                                                                                99.78378 112.70270
##
                                    E10
                                                                       E12
                    E9
                                                     E11
                                                                                        E13
                                                                                                         E14
                                                                                                                           E15
## 1 130.96774 138.16129 119.32258 133.32258 128.25806 136.90323 136.35484
## 2 75.59184 103.55102 90.67347 104.71429 113.48980 104.97959
                                                                                                                 63.22449
## 3 146.25000
                          22.06250 129.31250
                                                             53.62500
                                                                               95.56250
                                                                                                85.75000 146.50000
         40.32432 56.51351
                                            48.45946
                                                              54.48649
                                                                               49.75676
                                                                                                55.40541 36.91892
## 4
                                                              80.00000
## 5
                                                                                                63.97297 110.32432
         95.97297 102.86486
                                            91.70270
                                                                               73.35135
##
                   E16
                                    E17
                                                     E18
                                                                       E19
                                                                                        E20
                                                                                                         E21
## 1 126.87097
                           98.77419 127.64516 122.22581 117.58065 109.00000
## 2 66.69388 74.59184 62.02041 58.16327
                                                                               70.79592
## 3 126.56250 119.25000 146.62500 132.18750 142.00000
                                                                                                25.31250
## 4 44.56757 48.43243 41.40541 47.97297 34.16216
## 5 109.97297 118.18919 104.16216 108.27027 105.00000 100.62162
##
## Clustering vector:
          \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 3 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 2 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 1 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \begin{smallmatrix} 4 \end{smallmatrix} \\ 4 \end{smallmatrix} \begin{smallmatrix} 5 \end{smallmatrix} \end{smallmatrix} 
       [36] 3 2 4 2 4 5 4 1 5 5 1 2 1 2 3 1 5 5 2 1 3 1 3 3 2 2 2 5 4 5 1 1 4 4 1
       [71] \ 5 \ 2 \ 1 \ 2 \ 4 \ 5 \ 5 \ 2 \ 2 \ 2 \ 5 \ 1 \ 4 \ 2 \ 2 \ 3 \ 5 \ 2 \ 5 \ 1 \ 5 \ 1 \ 5 \ 5 \ 5 \ 2 \ 5 \ 4 \ 2 \ 1 \ 2 \ 5 \ 5 \ 5 \ 2 
## [106] 3 5 3 5 5 3 3 2 4 5 4 4 2 4 1 1 4 4 5 5 5 4 4 4 2 2 2 3 5 4 2 3 4 1 4
## [141] 5 3 2 2 4 2 3 5 1 2 1 2 4 2 2 1 1 4 4 2 2 1 2 4 2 5 4 1 5 2
##
## Within cluster sum of squares by cluster:
## [1] 1109263.0 1561950.2 562254.8 1012247.7 1283058.7
      (between SS / total SS = 40.9 %)
##
## Available components:
##
## [1] "cluster"
                                      "centers"
                                                                "totss"
                                                                                          "withinss"
## [5] "tot.withinss" "betweenss"
                                                                                          "iter"
                                                                "size"
## [9] "ifault"
```

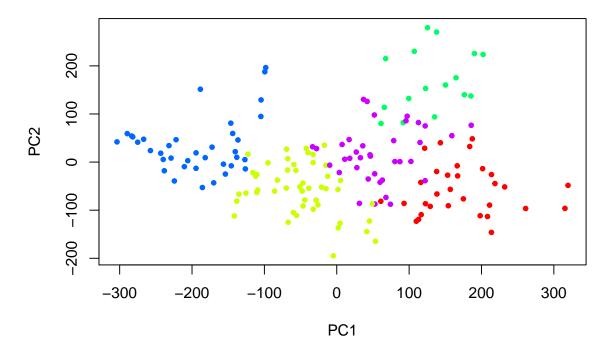
Each rider was placed into one of 5 clusters and the vector with this results can be printed as:

kmodel\$cluster

[141] 5 3 2 2 4 2 3 5 1 2 1 2 4 2 2 1 1 4 4 2 2 1 2 4 2 5 4 1 5 2

We can illustrate the results on the plot from PCA:

```
pcamodel <- prcomp(tdf[,3:22])
plot(predict(pcamodel), col=rainbow(5)[kmodel$cluster], pch=20)</pre>
```

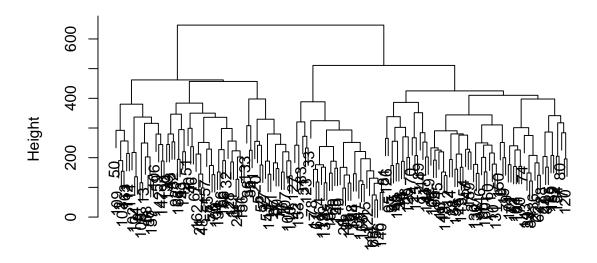


You can see that the distribution into clusters works very well.

Hierarchial clustering can be done by typing:

```
distances <- dist(tdf[,3:22])
hmodel <- hclust(distances)
plot(hmodel)</pre>
```

Cluster Dendrogram



distances hclust (*, "complete")

You can again inspect identities of riders to find which branch corresponds to sprinters, which corresponds to general classification specialists etc.

0.0.15.1 Tips and Tricks

- the algorithm used for K-means clustering can be controlled by algorithm option.
- the type of distance can be changes by method option of dist function.
- the parameter method controls the method used to construct the tree in hclust.

0.0.16 Programming

R is a programming language. You can make loops and other programming constructions in R.

0.0.16.1 Tips and Tricks

• you can make a for-loop by:

```
for(i in 1:10) {
   print(i)
}

## [1] 1
## [1] 2
## [1] 3
## [1] 4
## [1] 5
## [1] 6
## [1] 7
## [1] 8
## [1] 9
## [1] 10
```

- always use print function to print something in a loop
- you can "if" statement by:

```
for(i in 1:10) {
  if(i==3) {
    print(i)
  }
}
```

[1] 3

If-else statement and switch statement works as well.

• you can define a function:

```
sem <- function(x) {
  return(sd(x)/sqrt(length(x)))
}
sem(rnorm(10))</pre>
```

[1] 0.3281054

• to run a program in R in a command line save the code to "program.R" and run it by typing: Rscript program.R

or

```
R --no-save < program.R
```

- you can use a kind of object oriented programming in R
- you can use generic function, such as plot, defined to an object you define

0.0.17 Next Steps

0.0.17.1 Tips and Tricks

- you can use any or packages available in CRAN
- you can use tidyverse family of packages for data analysis
- you can use Bioconductor family of packages for data analysis
- you can read R Journal to learn more about news in R community and new R packages
- you can make your own package and submit it to CRAN.
- there are special R user conferences (UseR!, eRum, ...)
- there are special R user communities such as R ladies