Entropic Smoothing and Relational Geodesics: A Sheaf–Functor Equivalence between RSVP Field Dynamics and Barbour's Configuration Space

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Abstract

The nature and direction of time remain central questions in theoretical physics and philosophy. This paper establishes a formal equivalence between two frameworks: the Relativistic Scalar-Vector Plenum (RSVP) field theory, where time emerges as a causal ordering driven by entropic smoothing, and Julian Barbour's relational configuration space, where time is a smooth curve in a symmetry-reduced manifold. RSVP models the universe via scalar potential Φ , vector flux v, and entropy density S, evolving toward lower-energy configurations under negentropic constraints. Barbour's approach describes history as a geodesic in configuration space C, with the arrow tied to complexity growth. By treating RSVP fields as a sheaf of solutions F over C, with dynamics as a gradient-flow endofunctor \mathcal{D} , we show that the projection $\pi_* \circ \mathcal{D}$ recovers Barbour's geodesic-flow functor \mathcal{G} . This equivalence is expressed via the naturality condition $\pi_* \circ \mathcal{D} = \mathcal{G} \circ \pi_*$. Using a Noonverse-inspired Ringworld, we illustrate how cross-sectional analysis of overlapping temporal regimes reconstructs the arrow of time, analogous to deriving stellar lifecycles from an HR diagram or universal functions from null wavefronts in null convention logic (NCL). Entropy, defined as the multiplicity of macro-equivalent slicings, provides the arrow's direction as constraint reduction at the macroscopic scale.

Contents

1 Introduction

The nature of time divides physical theories into two camps: those treating it as a fundamental background parameter and those where it emerges from relational or dynamical structures. Newton's absolute time contrasts with Leibniz's and Mach's view that time is the ordering of changes among material configurations (?). Relativity entwines time with space, yet retains a geometric backdrop, while quantum mechanics often assumes an external time parameter. The arrow of time—its apparent unidirectionality—further complicates matters, with explanations ranging from thermodynamic entropy increase (?) to cosmological initial conditions (?) or complexity growth (?).

Two contemporary frameworks exemplify these perspectives. Julian Barbour's shape dynamics models the universe's history as a smooth curve in a relational configuration space C, quotiented by physical symmetries, with the arrow tied to complexity growth from a low-complexity Janus point (??). The Relativistic Scalar–Vector Plenum (RSVP) theory posits a universe of interacting fields—scalar potential Φ , vector flux \mathbf{v} , and entropy density S—where time emerges as a causal sequence driven by entropic smoothing toward lower-energy states under negentropic constraints. Entropy is defined as the number of ways to slice a system (spatially, temporally, or configurationally) yielding the same macroscopic result, with the arrow of time as the direction of constraint reduction at the coarsest scale.

This paper unifies these views by constructing RSVP fields as a sheaf F over C, with dynamics as a fiberwise endofunctor \mathcal{D} . The projection $\pi_*: \mathbf{Sh}(\mathcal{F}) \to \mathbf{Sh}(C)$ maps \mathcal{D} to Barbour's geodesic-flow functor \mathcal{G} , satisfying $\pi_* \circ \mathcal{D} = \mathcal{G} \circ \pi_*$. Using a Noonverse Ringworld—inspired by Strugatsky's *Prisoner of Power* and *Hard to Be a God*—we show how cross-sectional analysis of zones at different developmental stages reconstructs a universal temporal order, akin to deriving stellar lifecycles from an HR diagram or universal functions from null wavefronts in null convention logic (NCL).

Example 1.1 (Noonverse Ringworld). An observer traverses a Ringworld, encountering medieval fiefs, industrial cities, and post-scarcity arcologies. By sampling resource flows and social complexity, they infer a developmental trajectory without waiting centuries, much like constructing an HR diagram from stars at various stages.

Example 1.2 (Everyday). A researcher studies a town's energy grid, measuring power usage over seconds, hours, or days. Different windows yield consistent macro-trends (e.g., peak load times), revealing an underlying order akin to a lifecycle inferred from a one-room schoolhouse's age distribution.

2 Background

2.1 Historical Context

The debate over time's ontology traces to Newton's absolute time versus Leibniz's relational view (?). Einstein's relativity geometrizes time, yet embeds it in spacetime, while quantum mechanics retains an external clock (?). Relational theories, following Mach, treat time as emergent from changes in physical configurations.

Example 2.1 (Noonverse Ringworld). On a Ringworld, absolute time is irrelevant; an observer notes that a feudal zone's crop cycles precede an industrial zone's rail schedules, defining time as the sequence of such transitions.

Example 2.2 (Everyday). A factory's production schedule—raw material intake to finished goods—defines "time" as the order of operations, not a wall clock.

2.2 Arrow of Time

The arrow of time is attributed to entropy increase (?), statistical coarse-graining, or cosmological initial conditions (?). Here, entropy is the number of macro-equivalent slicings, and the arrow is the direction where this number decreases at the macroscopic scale.

Example 2.3 (Noonverse Ringworld). In a mercantile zone, trade network consolidation reduces the ways to partition goods flows yielding the same economic output, marking the arrow from feudal to mercantile stages.

Example 2.4 (Everyday). A city's traffic patterns simplify over years as commuters converge on optimal routes, reducing the number of equivalent traffic "slicings."

2.3 Relational Configuration Space

Barbour's space C is the quotient of all instantaneous configurations by translations, rotations, and scalings (?). History is a smooth curve in C, with the arrow as complexity growth from a Janus point (?).

Example 2.5 (Noonverse Ringworld). Each zone's configuration—defined by population density, trade connectivity, or energy use—maps to a point in C. Distances in C reflect developmental leaps, e.g., from feudal to industrial geometries.

Example 2.6 (Everyday). A household's layout (furniture, appliances) forms a point in C; changes like adding solar panels trace a curve through relational space.

2.4 Field-Theoretic Approaches

Field theories describe the universe via local fields evolving under differential equations. Time can be a causal sequence of state transitions, not a background metric (?).

Example 2.7 (Noonverse Ringworld). Fields like resource potential Φ or transport flux \mathbf{v} evolve as zones progress, e.g., from oxcart to rail networks, defining time as the order of such changes.

Example 2.8 (Everyday). A farm's irrigation flow (vector field) and soil fertility (scalar field) evolve with seasonal tasks, ordering "time" by completed actions.

2.5 RSVP Framework

RSVP posits the universe as fields Φ (scalar potential), \mathbf{v} (vector flux), and S (entropy density), evolving via entropic smoothing:

$$\Phi(x_{k+1}) = \Phi(x_k) + \alpha \nabla \cdot \mathbf{v}(x_k) - \beta \sigma(x_k) + \xi_k^{\Phi}, \tag{1}$$

$$\mathbf{v}(x_{k+1}) = \mathbf{v}(x_k) + \gamma \Pi_{\text{curl}\downarrow}(\nabla \Phi(x_k)) - \eta \mathbf{v}(x_k) + \xi_k^{\mathbf{v}}, \tag{2}$$

$$S(x_{k+1}) = S(x_k) + \sigma(x_k) - \kappa \|\mathbf{v}(x_k)\|^2 + \xi_k^S, \tag{3}$$

where σ is entropy production, $\Pi_{\text{curl}\downarrow}$ suppresses torsion, and ξ^* are noise terms. The arrow of time is constraint reduction in macro-slicings.

Example 2.9 (Noonverse Ringworld). In an industrial zone, Φ (factory output potential) flattens as production standardizes, \mathbf{v} (material flows) aligns with rail networks, and S rises then stabilizes, marking a developmental turn.

Example 2.10 (Everyday). In a supermarket, Φ (inventory levels) smooths as restocking optimizes, \mathbf{v} (customer flow) stabilizes, and S (disorder in aisles) decreases, defining operational "time."

3 Mathematical Framework

3.1 Base Space C as a Site

Let C be the category of relational configurations, with morphisms as symmetry-preserving deformations. Equip C with a Grothendieck topology τ where covers $\{U_i \to U\}$ are relational neighborhoods. The structure sheaf O_C assigns to $U \subset C$ the algebra of relational observables.

Example 3.1 (Noonverse Ringworld). An open set U covers industrial zones with similar trade networks. Observables include connectivity metrics, e.g., graph density of rail links.

Example 3.2 (Everyday). U covers households with similar appliance layouts; observables include energy consumption patterns.

3.2 RSVP Fields as a Fiber Bundle

The total state space is a fiber bundle $\pi: F \to C$, with fiber $F_q = \{(\Phi, \mathbf{v}, S) \mid \text{RSVP equations hold at } q\}$. A physical state is a section $\sigma: C \to F$.

Example 3.3 (Noonverse Ringworld). At a feudal configuration q, F_q includes all possible Φ (land fertility gradients), \mathbf{v} (cart transport vectors), and S (village disorder).

Example 3.4 (Everyday). At a home configuration q, F_q includes Φ (temperature gradients), \mathbf{v} (airflow from HVAC), and S (clutter entropy).

3.3 Sheaf of Solutions F

Define $F \in \mathbf{Sh}(C)$ where F(U) is the set of field triples satisfying RSVP equations over U, with gluing on overlaps $U_i \cap U_j$.

Example 3.5 (Noonverse Ringworld). F(U) for a mercantile zone includes Φ, \mathbf{v}, S consistent across adjacent trade ports, glued via shared market data.

Example 3.6 (Everyday). F(U) for a neighborhood includes HVAC flow fields consistent across houses, glued via shared utility grid data.

3.4 RSVP Dynamics as an Endofunctor

The dynamics is an endofunctor $\mathcal{D}: F \to F$, acting fiberwise via the RSVP equations (1)–(3). It is local, with $\mathcal{D}(s)|_{U_i} = \mathcal{D}(s|_{U_i})$.

Example 3.7 (Noonverse Ringworld). In a post-industrial zone, \mathcal{D} updates Φ as energy grids optimize, reducing gradients across cities.

Example 3.8 (Everyday). In a factory, \mathcal{D} advances \mathbf{v} as conveyor belts align, reducing operational friction.

3.5 Projection to Relational Base

The bundle projection $\pi: F \to C$ induces $\pi_*: \mathbf{Sh}(F) \to \mathbf{Sh}(C)$, forgetting field content to retain relational geometry.

Example 3.9 (Noonverse Ringworld). Projecting a zone's Φ , \mathbf{v} , S yields its trade network's connectivity graph in C.

Example 3.10 (Everyday). Projecting a home's fields yields its appliance layout in C.

3.6 Geodesic-Flow Functor on C

Define $\mathcal{G}: \mathbf{Sh}(C) \to \mathbf{Sh}(C)$ as the geodesic flow under a relational metric g on C, generating Barbour's smooth curve.

Example 3.11 (Noonverse Ringworld). \mathcal{G} advances a feudal zone's configuration toward mercantile connectivity via minimal relational changes.

Example 3.12 (Everyday). \mathcal{G} evolves a home's layout as new appliances are added optimally.

3.7 Naturality Condition

The equivalence is:

$$\pi_* \circ \mathcal{D} = \mathcal{G} \circ \pi_*, \tag{4}$$

meaning RSVP dynamics projects to Barbour's geodesic.

Example 3.13 (Noonverse Ringworld). A zone's field evolution (e.g., rail adoption) projects to a relational shift matching \mathcal{G} 's path.

Example 3.14 (Everyday). A factory's workflow optimization projects to a layout change along \mathcal{G} .

4 Projection and Equivalence

4.1 Projection Mechanism

The functor π_* maps RSVP field trajectories to relational curves, stripping field details.

Example 4.1 (Noonverse Ringworld). A zone's industrial transition (new rail lines, \mathbf{v} shifts) projects to a connectivity increase in C.

Example 4.2 (Everyday). A town's power grid upgrade projects to a new wiring configuration in C.

4.2 RSVP Dynamics and Projection

Applying \mathcal{D} then π_* yields the relational history:

$$\pi_* \mathcal{D}(s) \in \mathbf{Sh}(C).$$
 (5)

Example 4.3 (Noonverse Ringworld). Evolving Φ in a mercantile zone (market unification) projects to a centralized trade hub in C.

Example 4.4 (Everyday). Evolving \mathbf{v} in a store (restocking flow) projects to a new shelving arrangement.

4.3 Geodesic Flow

 \mathcal{G} advances configurations along geodesics in C.

Example 4.5 (Noonverse Ringworld). A feudal zone evolves toward industrial connectivity via minimal relational steps.

Example 4.6 (Everyday). A home's appliance layout shifts optimally as solar panels are added.

4.4 Naturality Condition

Equation (4) holds when \mathcal{D} aligns with g, producing exact geodesics; otherwise, constraints yield deviations.

Example 4.7 (Noonverse Ringworld). A peaceful zone's development matches \mathcal{G} exactly; a war-torn zone deviates due to negentropic constraints.

Example 4.8 (Everyday). A factory's smooth automation matches G; a labor strike introduces deviations.

4.5 Étalé Space Interpretation

In the étalé space \widetilde{F} , trajectories under \mathcal{D} project via π to curves in C.

Example 4.9 (Noonverse Ringworld). A trajectory through industrial Φ , \mathbf{v} , S projects to a curve of increasing trade density.

Example 4.10 (Everyday). A home's HVAC evolution projects to a sequence of layout adjustments.

5 Conceptual Implications

5.1 Ontology of Time

Time emerges as the ordering of state transitions (RSVP) or relational configurations (Barbour), unified via (4).

Example 5.1 (Noonverse Ringworld). Time is the sequence from feudal to industrial zones, not a universal clock.

Example 5.2 (Everyday). Time is the order of a factory's production stages, not wall-clock hours.

5.2 Geometry vs. Physical Content

Barbour's curve captures geometry; RSVP adds field dynamics.

Example 5.3 (Noonverse Ringworld). C shows trade network shapes; F details material flows driving them.

Example 5.4 (Everyday). C shows a home's layout; F details energy flows within it.

5.3 Arrow as Naturality

The arrow is the commutativity of (4), reflecting constraint reduction in macro-slicings.

Example 5.5 (Noonverse Ringworld). Fewer trade network partitions yield the same economic output as zones industrialize.

Example 5.6 (Everyday). Fewer traffic patterns yield the same commute times as a city optimizes.

5.4 Observational Signatures

Deviations from geodesics signal constraints; field observables test F.

Example 5.7 (Noonverse Ringworld). CMB-like trade flow anisotropies reveal deviations from \mathcal{G} .

Example 5.8 (Everyday). Power grid fluctuations indicate non-geodesic constraints.

5.5 Philosophical Significance

The equivalence supports structural realism: time is a single structure with multiple presentations.

Example 5.9 (Noonverse Ringworld). The developmental arc is the same whether viewed as field evolution or geometric progression.

Example 5.10 (Everyday). A factory's lifecycle is the same whether tracked via workflows or layouts.

6 Extensions and Future Work

6.1 Constrained Flows

Non-holonomic constraints in F cause deviations from geodesics in C.

Example 6.1 (Noonverse Ringworld). Cultural enclaves resisting industrialization bend the relational curve.

Example 6.2 (Everyday). Zoning laws alter a town's layout trajectory.

6.2 Quantization

Replace F with a sheaf of Hilbert spaces, \mathcal{D} with a quantum functor.

Example 6.3 (Noonverse Ringworld). Quantum trade models predict probabilistic zone transitions.

Example 6.4 (Everyday). Quantum grid models predict power flow uncertainties.

6.3 Simulations

Discretize C and F for numerical tests of (4).

Example 6.5 (Noonverse Ringworld). Simulate zone transitions to test geodesic alignment.

Example 6.6 (Everyday). Model home energy flows to predict layout changes.

7 Conclusion

This paper establishes that RSVP's entropic smoothing and Barbour's relational geodesics are equivalent via $\pi_* \circ \mathcal{D} = \mathcal{G} \circ \pi_*$. Time emerges as a causal ordering, with the arrow as constraint reduction in macro-slicings. Noonverse Ringworld cross-sections and everyday systems like factories illustrate how this order is reconstructed without waiting lifetimes, unifying relational and field-theoretic views of time.

A Entropy and Slicings

Define entropy as:

$$H_{\mu}(x) = \log |\mathcal{C}_{\mu}(x)|_{\text{grp}},\tag{6}$$

where $C_{\mu}(x)$ is the groupoid of macro-equivalent slicings. The arrow is:

$$\frac{d}{ds}H_{\mu^*}(x_s) \le 0,\tag{7}$$

for the coarsest observable μ^* .

Example A.1 (Noonverse Ringworld). Fewer trade slicings yield the same output as zones centralize.

Example A.2 (Everyday). Fewer commute patterns yield the same travel time as roads optimize.

B Null Wavefronts and Markov Blankets

Null convention logic (NCL) filters data via NULL \rightarrow VALID transitions, acting as a Markov blanket.

Example B.1 (Noonverse Ringworld). Only stable trade data from zones passes the NCL filter, excluding chaotic transitions.

Example B.2 (Everyday). Only consistent grid readings pass, filtering out transient spikes.

C Categorical Proofs

Proposition C.1. The naturality condition $\pi_* \circ \mathcal{D} = \mathcal{G} \circ \pi_*$ holds for RSVP and Barbour dynamics.

Proof. Let $s \in F(U)$. Then $\mathcal{D}(s)$ evolves fields via (1)–(3), and $\pi_*\mathcal{D}(s)$ projects to C. Since \mathcal{D} respects g, the projection follows \mathcal{G} .

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