

Time Series Domain Adaptation

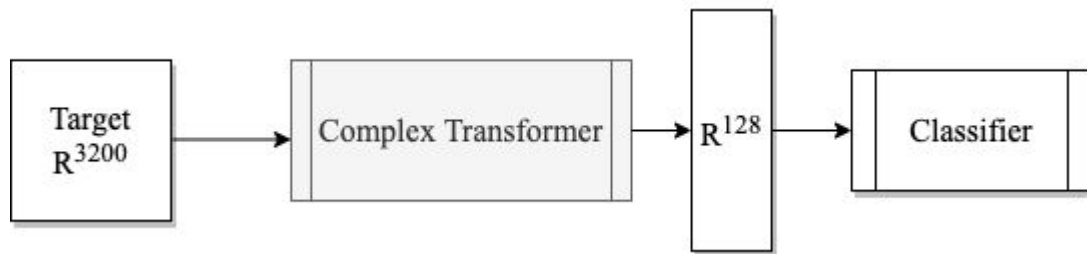
May 15, 2020

Baseline

$$L_{class_target} = - \sum_{(x'_i, y'_i) \in D_t^{label}} y'_i \log(C(T(x'_i)))$$

Only use 70% target-domain data for training, and evaluate at the rest 30%

Accuracy: 32%



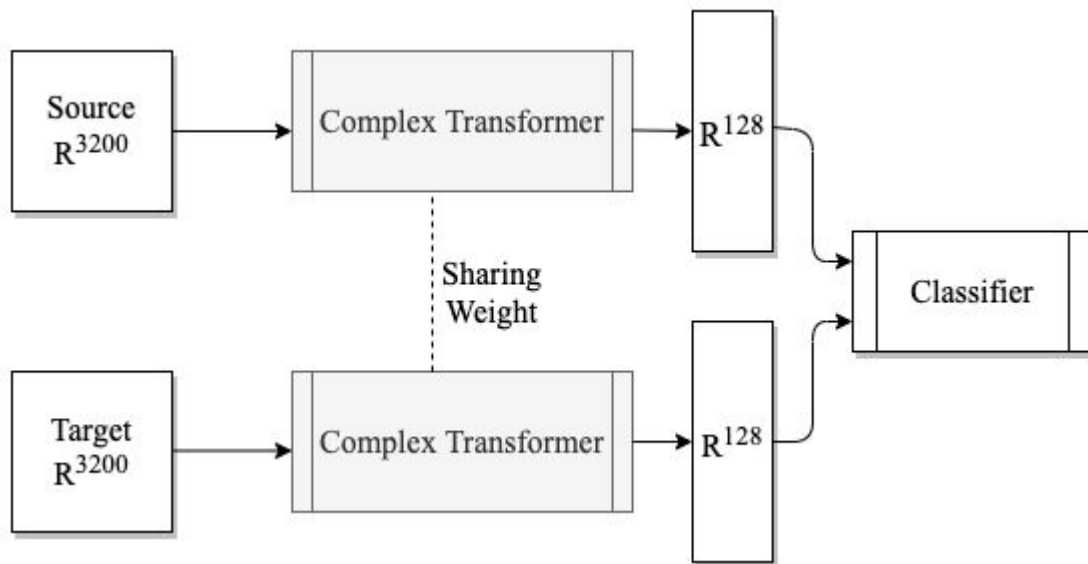
Naive Adaptation

Use both target-domain (70% training and 30% testing) and source-domain

Accuracy on 30% target-domain: 37%

$$L_{class_target} = - \sum_{(x'_i, y'_i) \in D_t^{label}} y'_i \log(C(T(x'_i)))$$

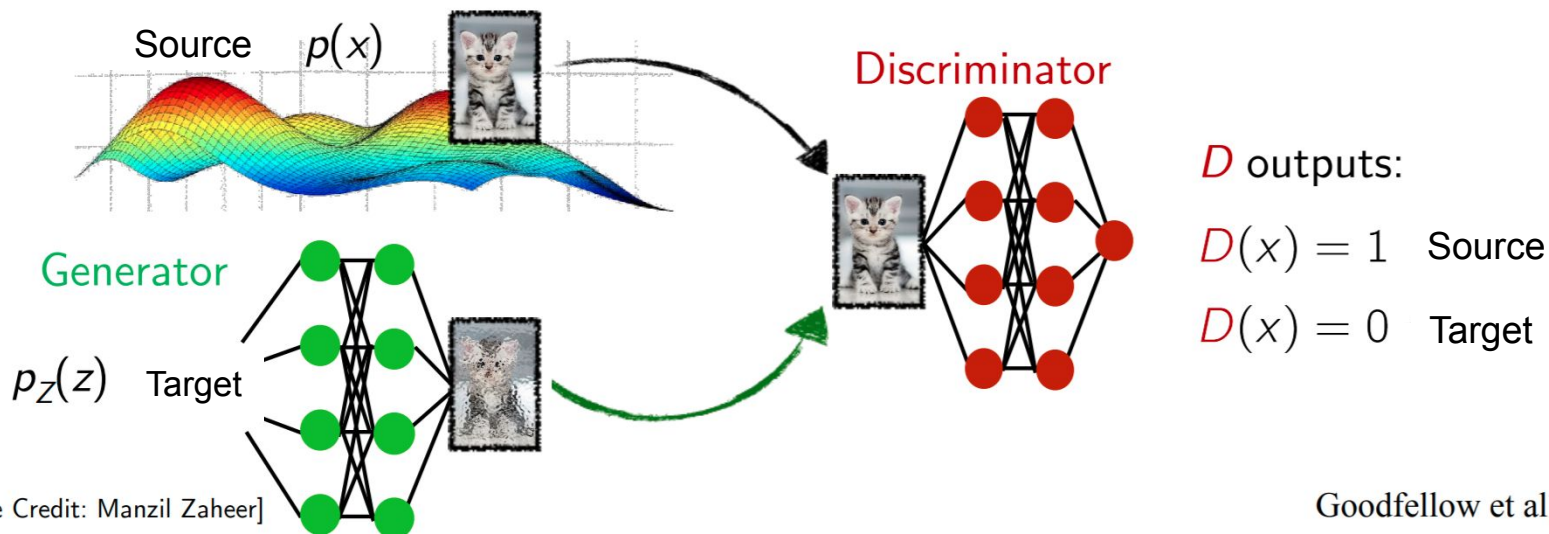
$$L_{class_source} = - \sum_{(x_i, y_i) \in D_s} y_i \log(C(T(x_i)))$$



GAN Background

- Min-Max game for adapting target distribution to source distribution

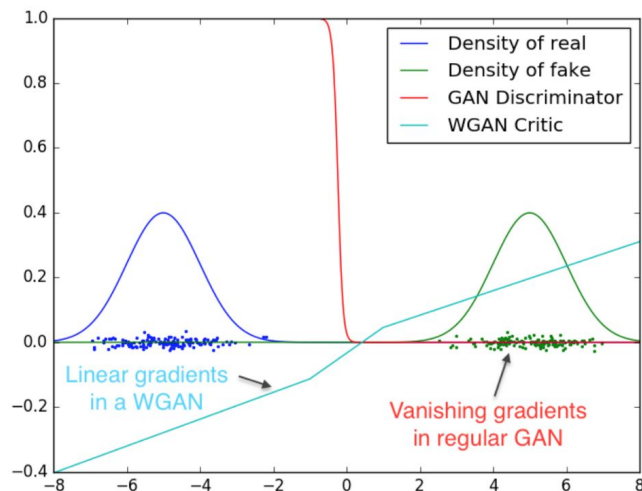
$$\min_G \max_D \mathbb{E}_{x \sim p} [\log D(x)] + \mathbb{E}_{z \sim p_Z} [\log (1 - D(G(z)))]$$



GAN Background

$$W(\mathbb{P}_r, \mathbb{P}_g) = \inf_{\gamma \in \Pi(\mathbb{P}_r, \mathbb{P}_g)} \mathbb{E}_{(x,y) \sim \gamma} [\|x - y\|]$$

- Wasserstein GAN
 - **Wasserstein Distance** is a measure of the distance between two probability distributions
 - Avoid **vanishing gradients** in normal GAN
 - State-of-the-art training for GAN

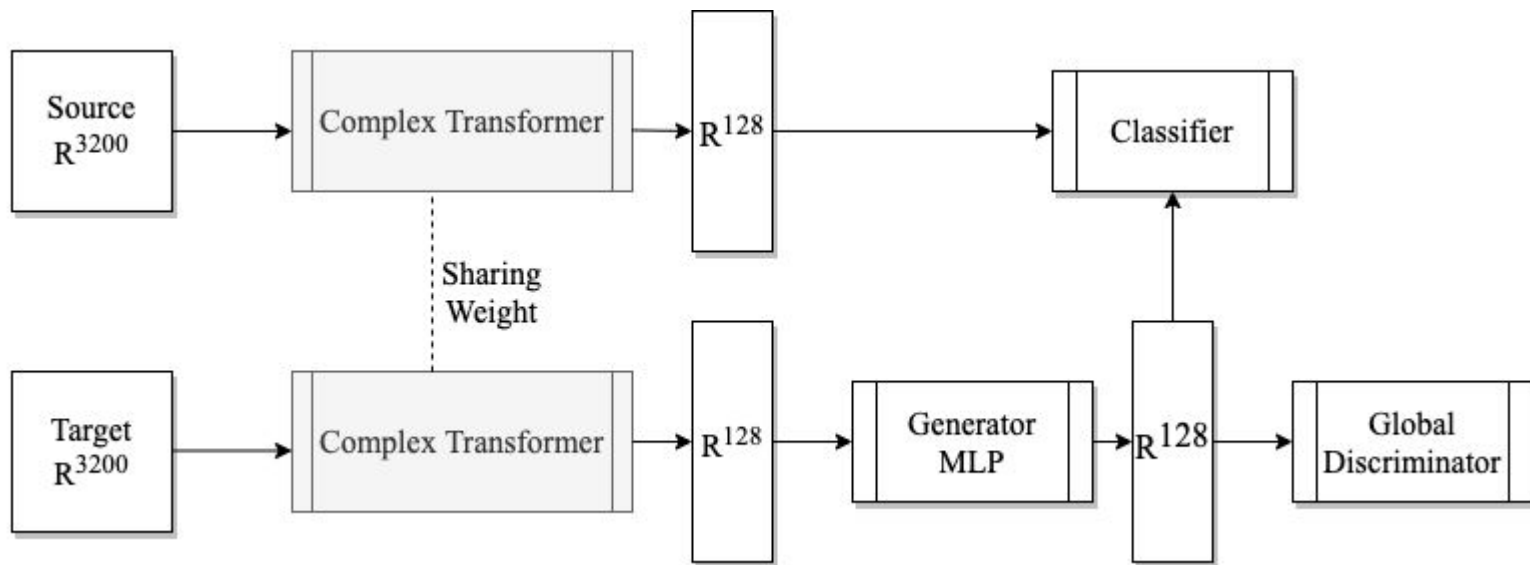


Global GAN

$$L_{global_GAN} = \mathbb{E}_{x' \sim P_t} [D(G(T(x')))] - \mathbb{E}_{x \sim P_s} [D(T(x))] + \lambda_{gp} * \mathbb{E}_{\hat{x} \sim P_{\hat{x}}} [(||\nabla_{\hat{x}} D(\hat{x})||_2 - 1)^2]$$

Minimize marginal distribution of source-domain and target-domain

Acc on rest 30% unlabeled target data: 40%

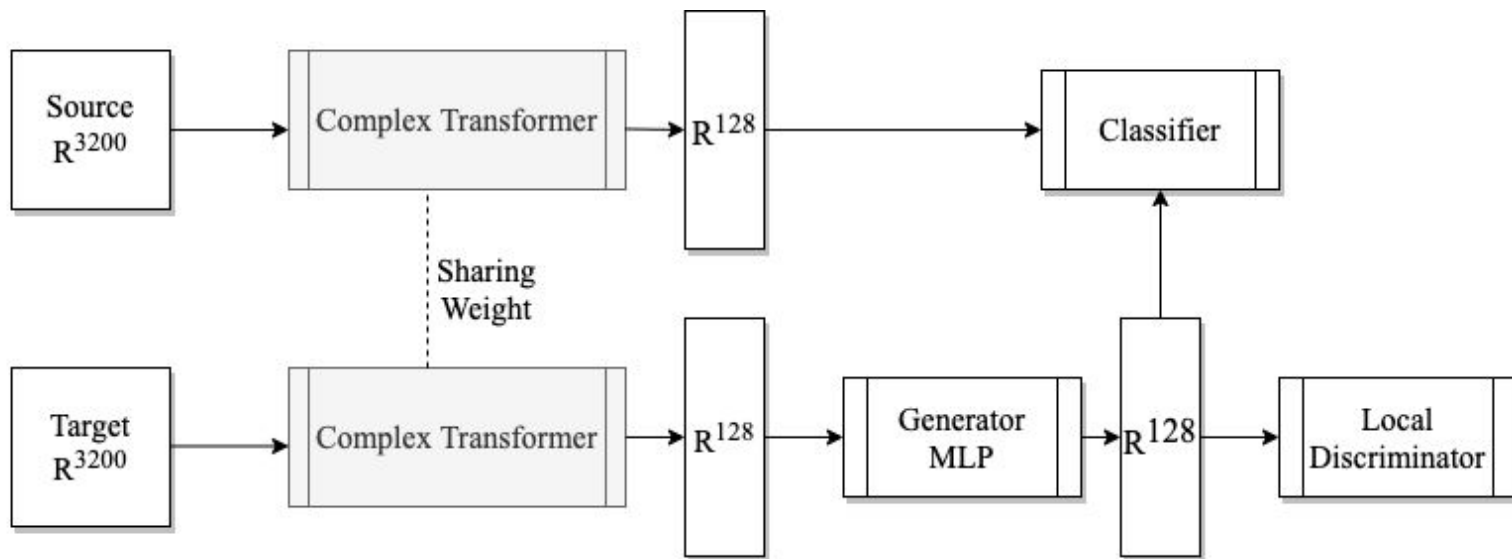


Conditional GAN

$$\begin{aligned} L_{\text{conditional_GAN}} = & \mathbb{E}_{y \sim P_y} [\mathbb{E}_{x' \sim P_t(x|y)} [D(G(T(x'), y))] \\ & - \mathbb{E}_{x \sim P_s(x|y)} [D(T(x))] \\ & + \lambda_{gp} * \mathbb{E}_{\hat{x} \sim P_{\hat{x}}(x|y)} [(||\nabla_{\hat{x}} D(\hat{x})||_2 - 1)^2] \end{aligned}$$

Minimize conditional distribution of source-domain and target-domain

Acc on rest 30% unlabeled target data: 44%



KL-divergence analysis

- Use MLP to approximate g .
- Train g by using the dual form of Jensen-shannon divergence
- Report on Kullback–Leibler divergence using the trained g

$$JS(P_s || P_t) = \sup_g \mathbb{E}_{P_s}[-softplus(-g(x))] - \mathbb{E}_{P_t}[softplus(g(x))]$$

$$g^* = \log \frac{p_s(x)}{p_t(x)}$$

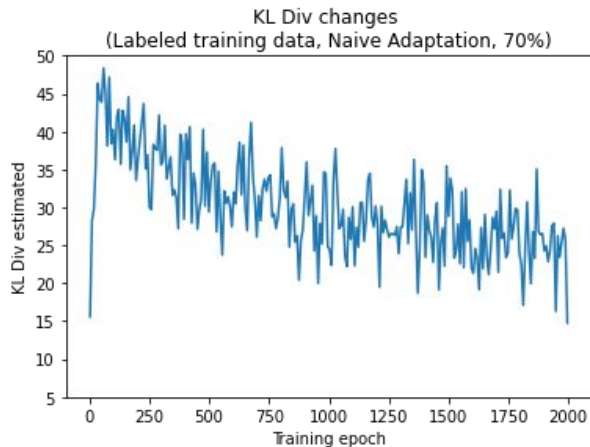
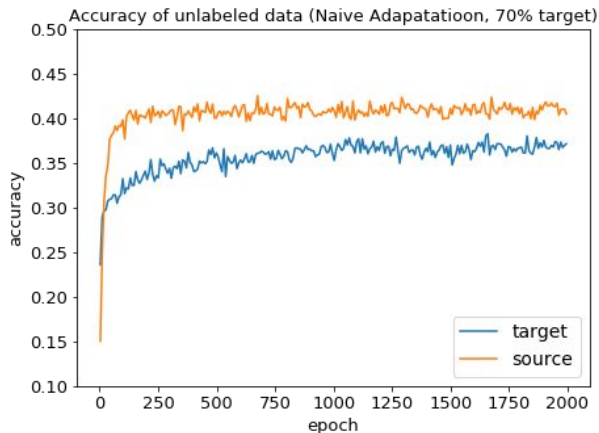
$$KL(P_s || P_t) = \mathbb{E}_{P_s} \log \frac{p_s(x)}{p_t(x)}$$

KL-divergence analysis

$$KL(P_s || P_t) = \mathbb{E}_{P_s} \log \frac{p_s(x)}{p_t(x)}$$

Naive Adaptation

- Target unlabeled accuracy: 32% -> 37%
- Shared-weight transformer and classifier
- Labeled KL divergence decrease to about 20.

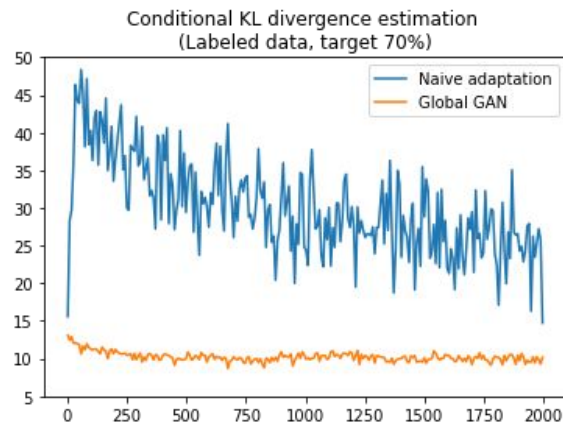
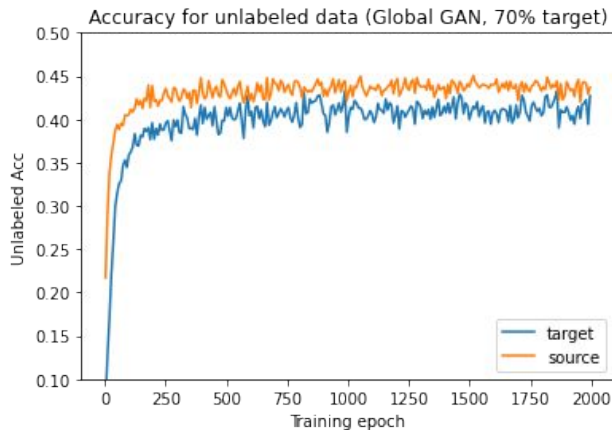
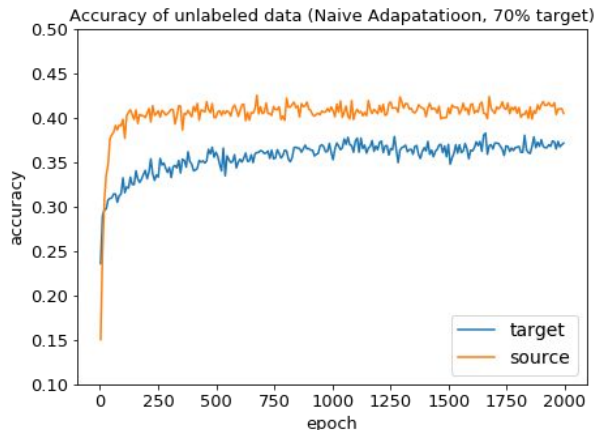


KL-divergence analysis

$$KL(P_s || P_t) = \mathbb{E}_{P_s} \log \frac{p_s(x)}{p_t(x)}$$

Global GAN

- Slightly improve unlabeled target accuracy (37% -> 41%)
- Slightly push target data hidden representation to source data hidden representation
- Push target and source testing accuracy together
- Labeled KL divergence decrease to about 10.

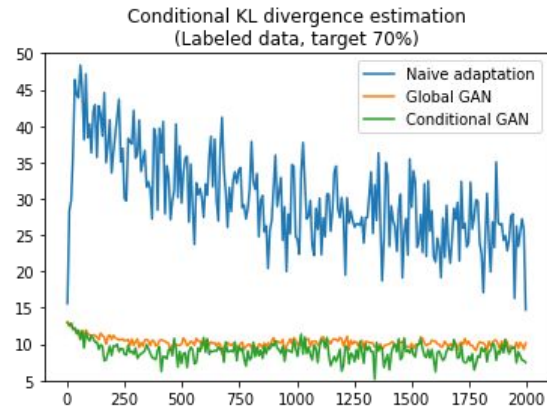
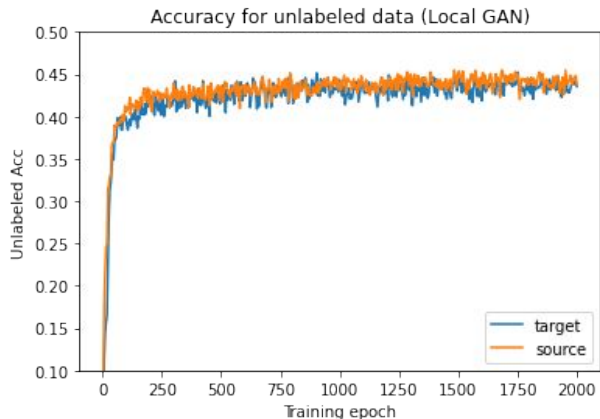
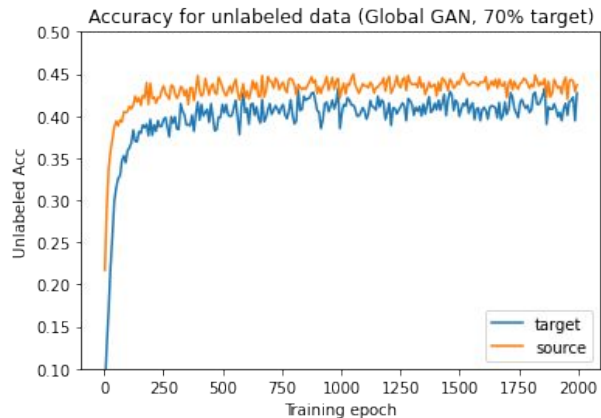


KL-divergence analysis

$$KL(P_s || P_t) = \mathbb{E}_{P_s} \log \frac{p_s(x)}{p_t(x)}$$

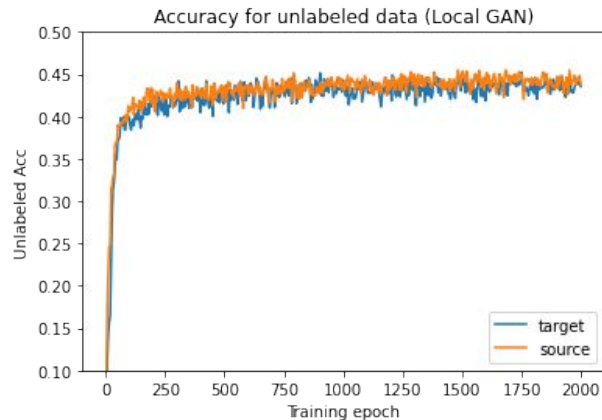
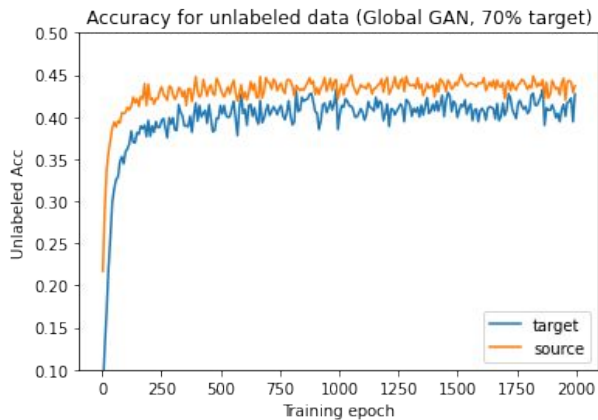
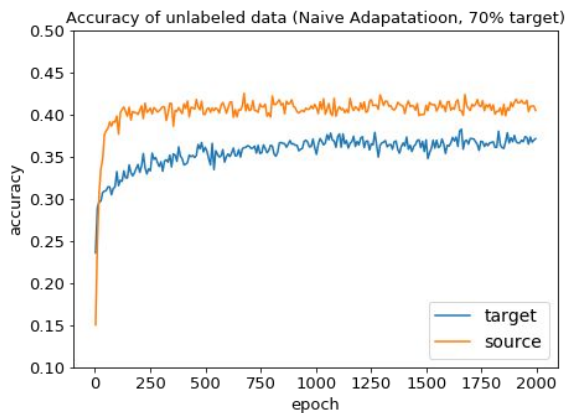
Conditional GAN

- Improve unlabeled target accuracy (41% -> 44%)
- Push target data hidden representation to source data hidden representation
- Push target and source testing accuracy together
- Labeled KL divergence decreases to about 9.



Testing accuracy analysis

- Native adaptation
 - Gap between target-domain and source-domain, because source-domain has more data than target-domain
- Global GAN
 - Shrinks the accuracy gap between domains
- Conditional (Local) GAN
 - Shrinks the accuracy gap even further



Testing accuracy summary

Target label seen during training	Baseline Test Accuracy	Naive adaptation Test Accuracy	Global GAN Test Accuracy	Conditional GAN Test Accuracy
10%	15%	13%	22%	21%
30%	22%	22%	28%	33%
50%	28%	28%	35%	38%
70%	32%	37%	41%	44%