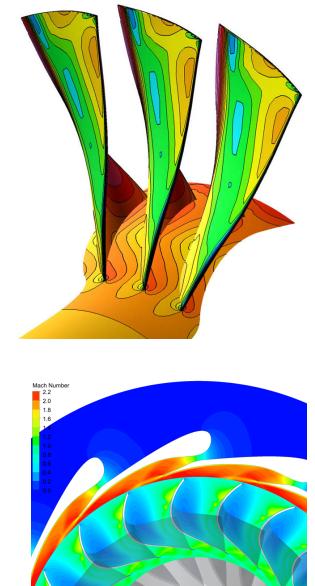


Recent Advances in Flow Analysis Capability and Adjoint-based Design for Turbomachinery with SU2

M. Pini, S. Vitale, A. Rubino, L. Azzini, N. Anand, P. Colonna
Propulsion and Power, Delft University of Technology

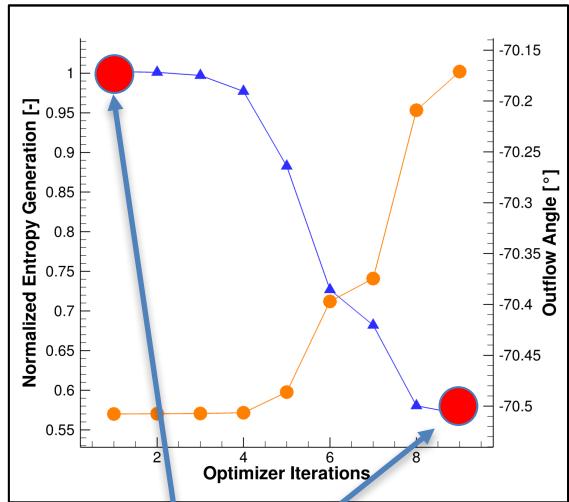
2nd Annual Developers Meeting, Stanford University



What Has Made It Possible?

Fluid: Air

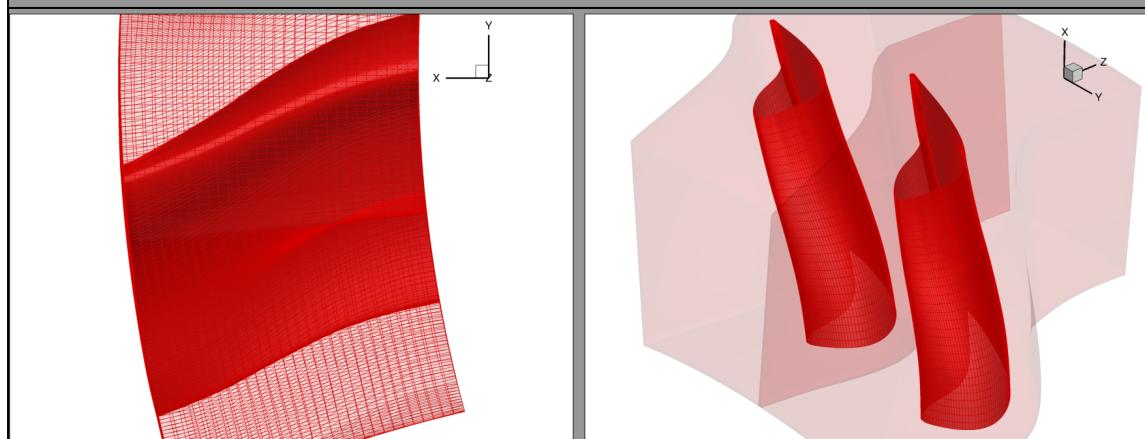
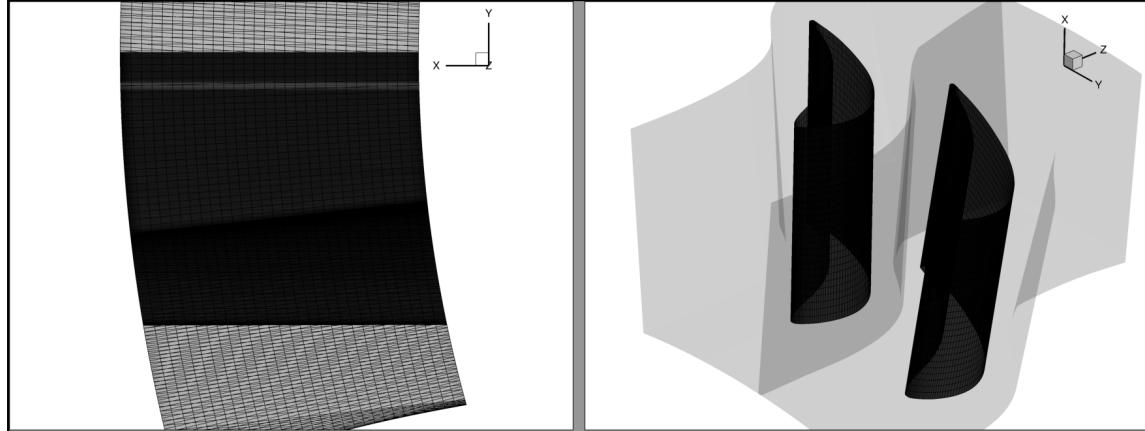
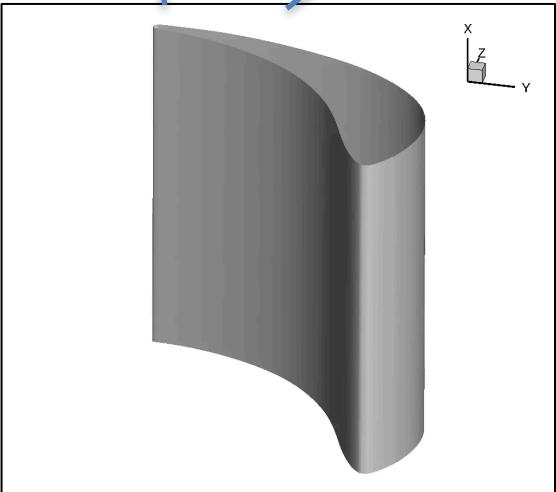
$$\left\{ \begin{array}{l} \min S_{\text{gen}} \\ \alpha_{\text{out}} < -70.0 \end{array} \right.$$



500k nodes

27 DVs

12h on 20 cores



The Secret Recipe...

SU2
The Open-Source CFD Code



Content

- SU2 for turbomachinery: What?
- (Some) Paradigmatic Examples
- Next steps

SU2 for Turbo: What...?

SU2 for Turbo: What...Direction?

**Provide Industrial-Strength Design Methods for
NextGen Turbomachines...of any kind!**

- ✓ Simulation of complex flows
(NICFD: pure fluids + mixtures, two-phase, unsteady, ROMs)

- ✓ Efficient automated design based on discrete adjoint

- ✓ Multi-physics analysis and design (FSI, topology)

SU2 for Turbo: What...is in it?

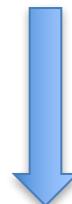
- NICFD → complex TMD models (hard-coded, FluidProp, look-up tables)
- Method of Moments for non-equilibrium condensation
- Turbo features → NRBC, MP, SLI for even pitches, HB
- Discrete turbo adjoint solver: steady/unsteady

For single and
multi-row

Emphasis (for now) is on compressible flows!

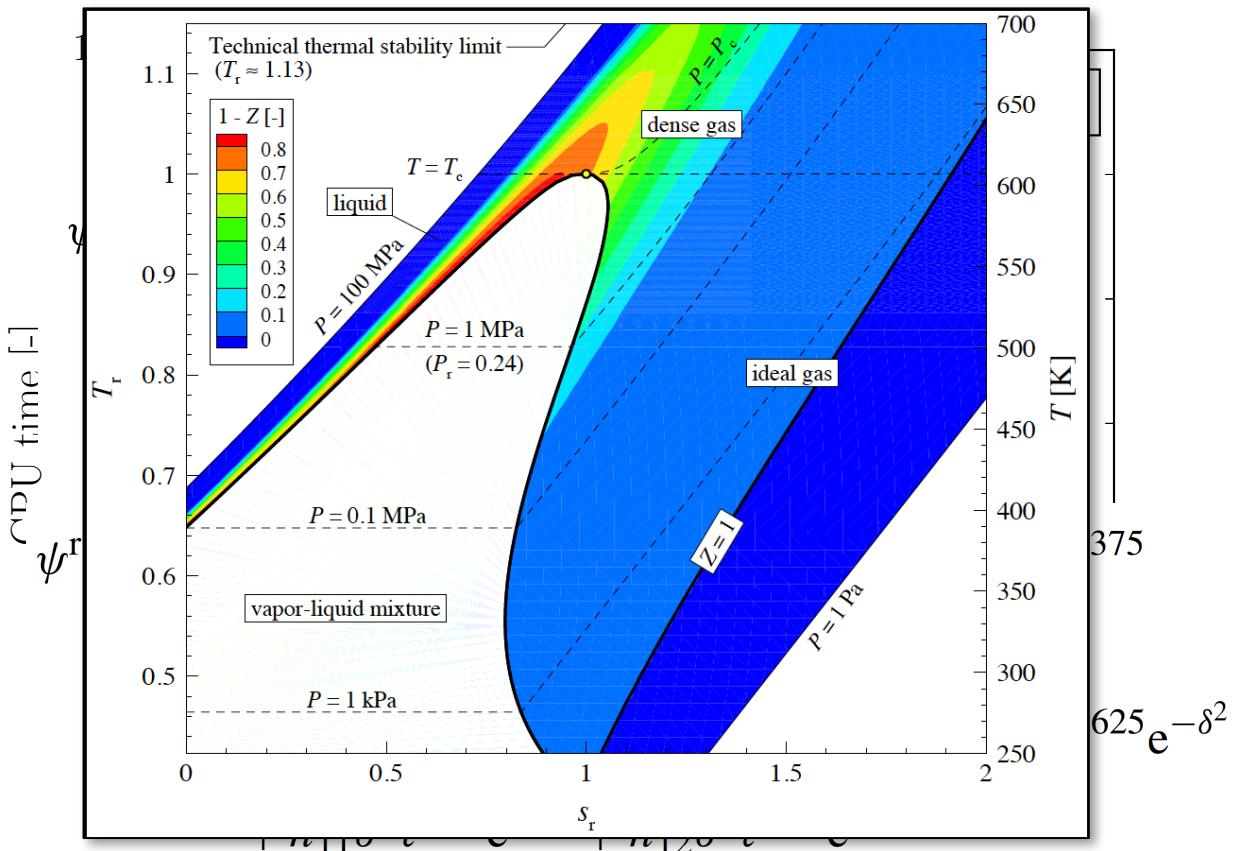
Look-up Tables → “Ideal” Cost

$$Pv = RT$$



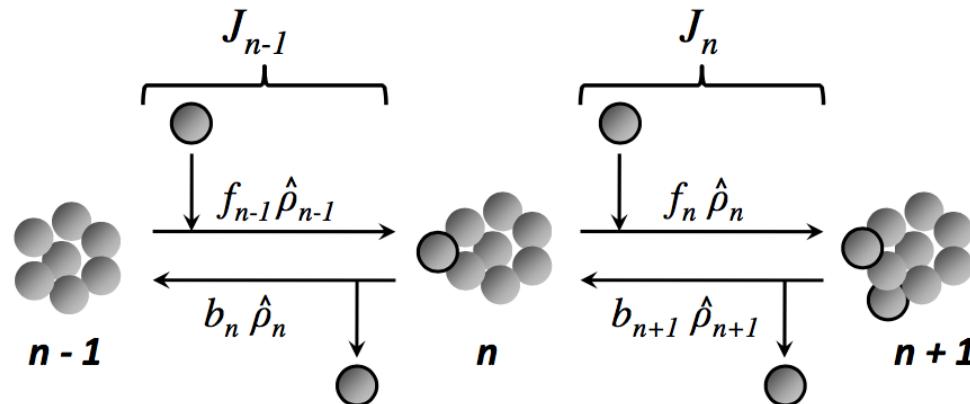
$$\frac{\Psi(T, \rho)}{RT} = \psi^0(\tau, \delta) + \psi^r(\tau, \delta)$$

- Explicit vs. Implicit
 - Secondary thermodynamic properties



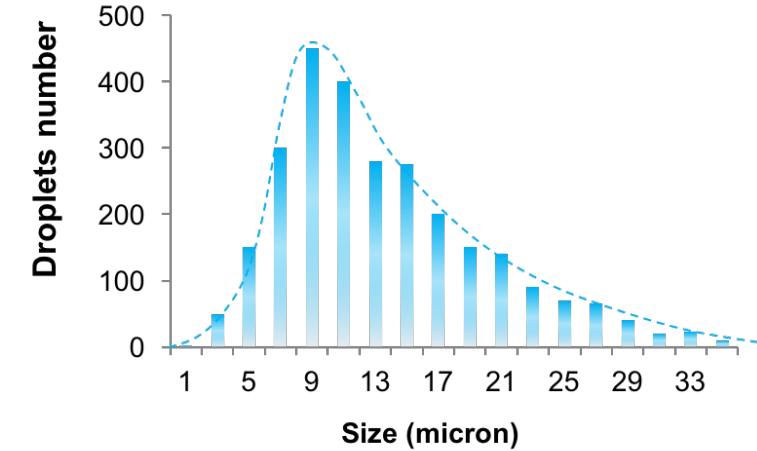
ROM for Dispersed Liquid Flows

- Method of Moments → 4 Transport Equations

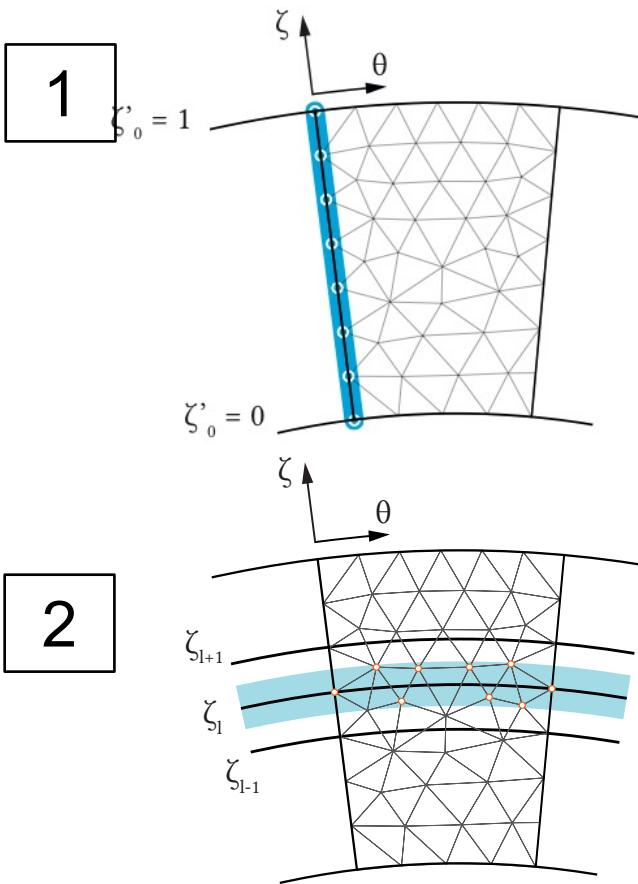


$$\mu_0 = N_{tot} \quad \mu_1 = N_{tot}R \quad \mu_2 = N_{tot}R^2 \quad \mu_3 = N_{tot}R^3$$

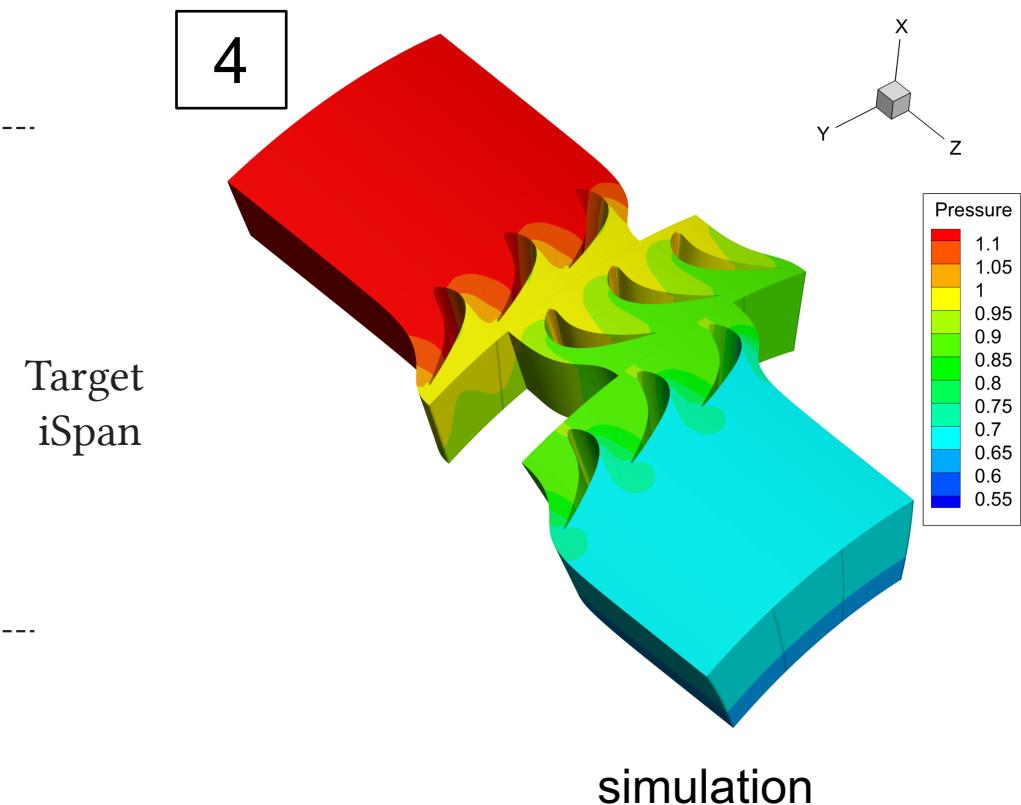
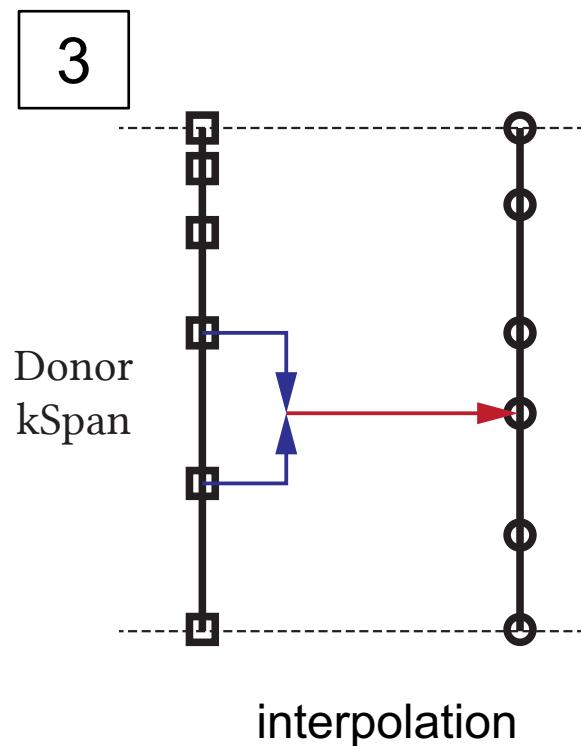
- ✓ Upwind flux, 1st – 2nd order
- ✓ Implicit time integration
- ✓ Segregated approach



Fluid-Fluid Interface for Generic Grids

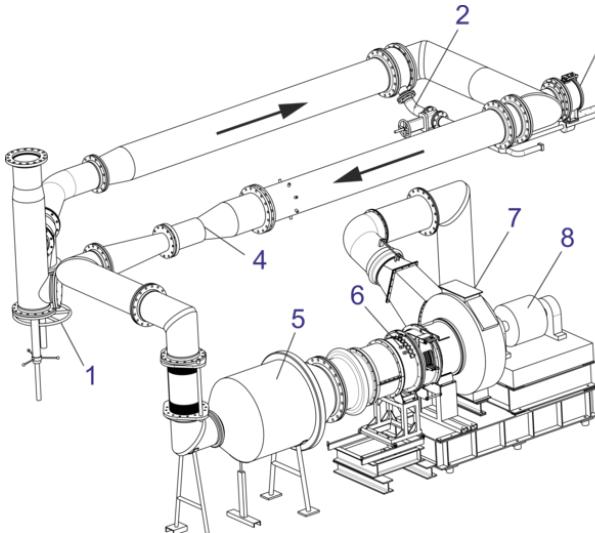


1,2: vertex ordering algorithm



Turbo vertex: same data structure for MP and SLI

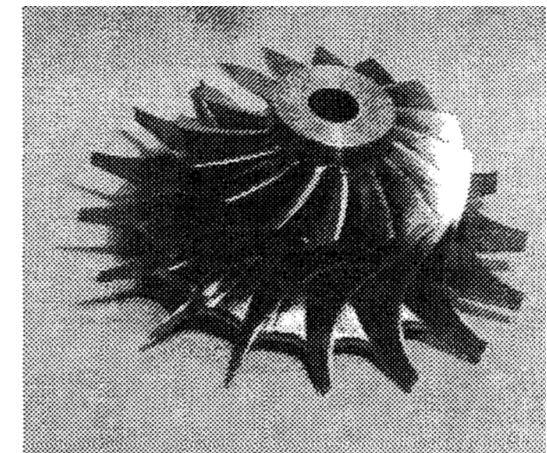
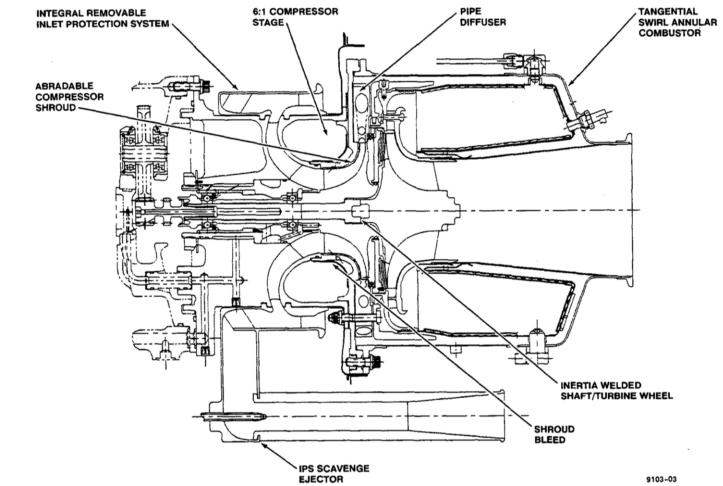
SU2 for Turbo: What...Accuracy?



Aachen turbine



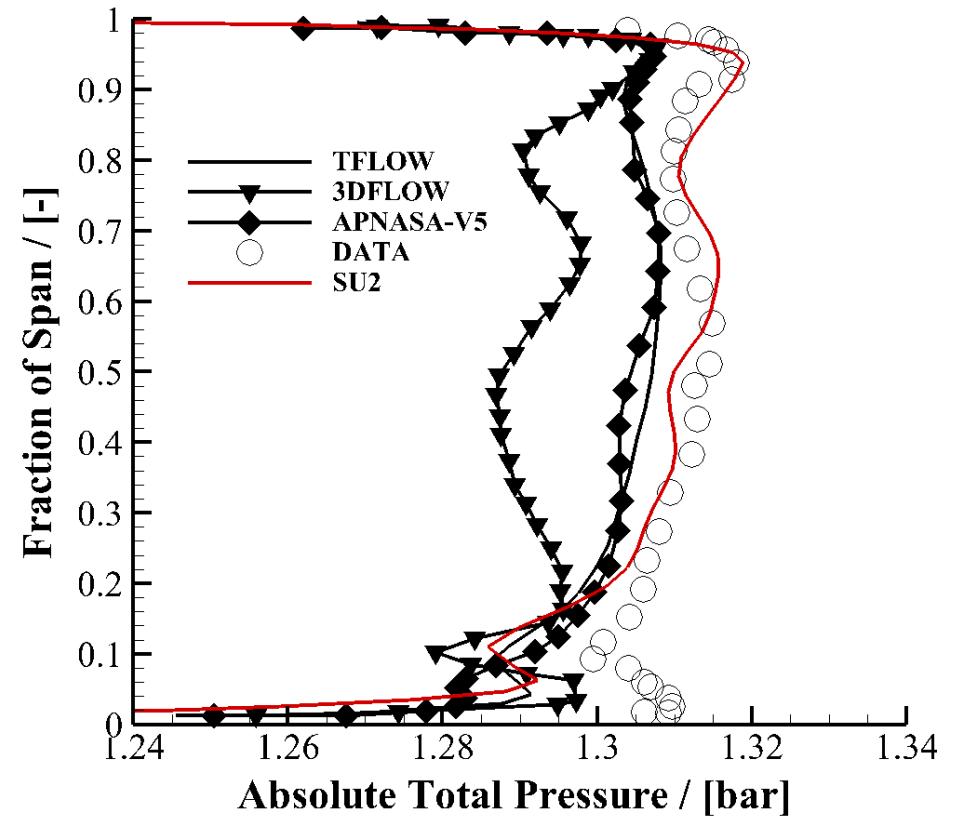
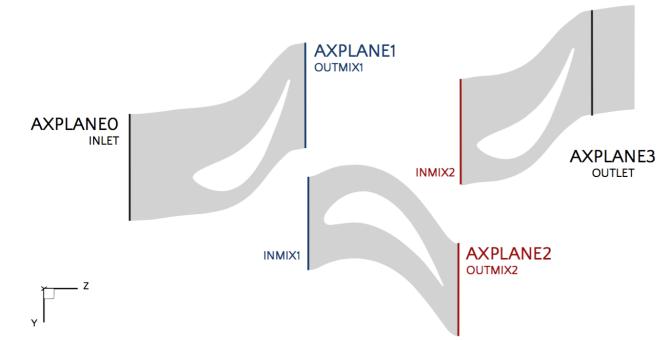
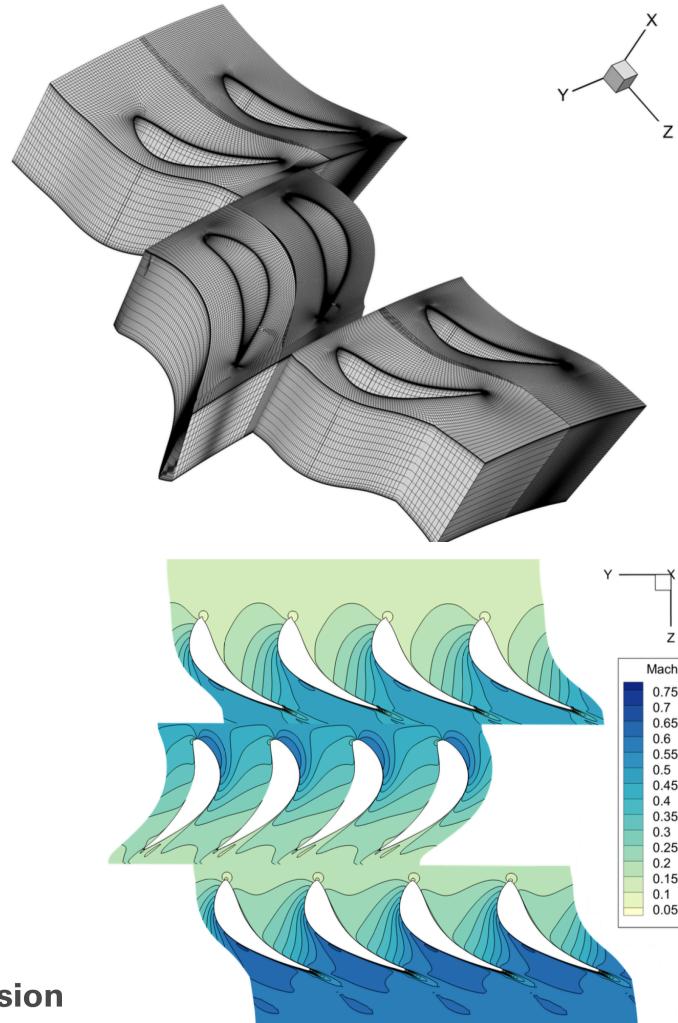
NASA rotor 37



APU turbine

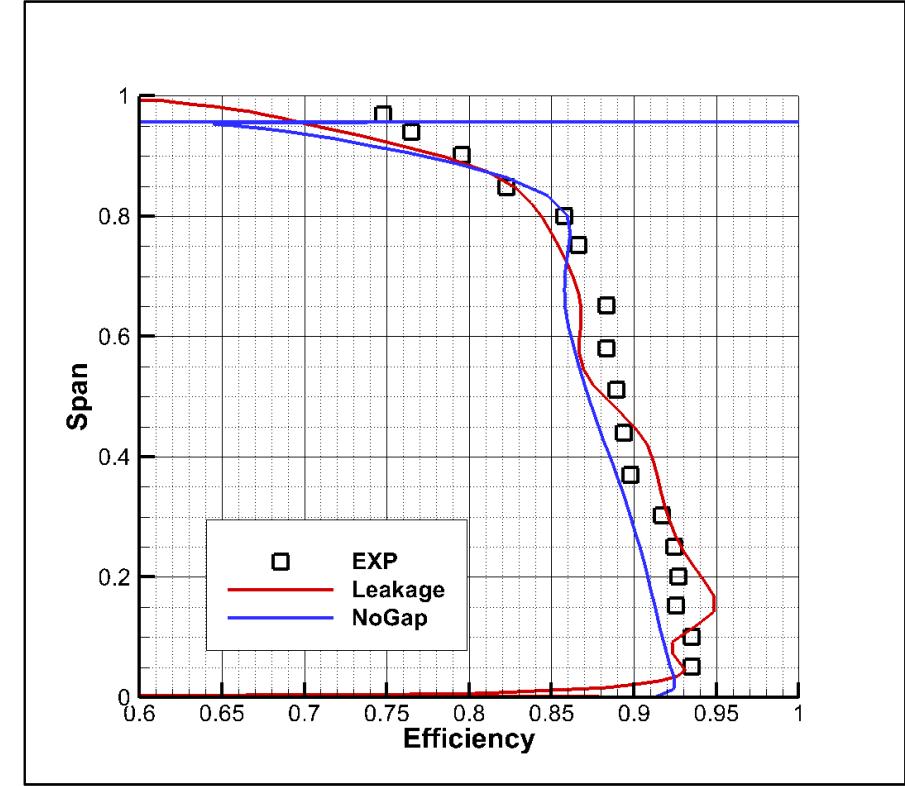
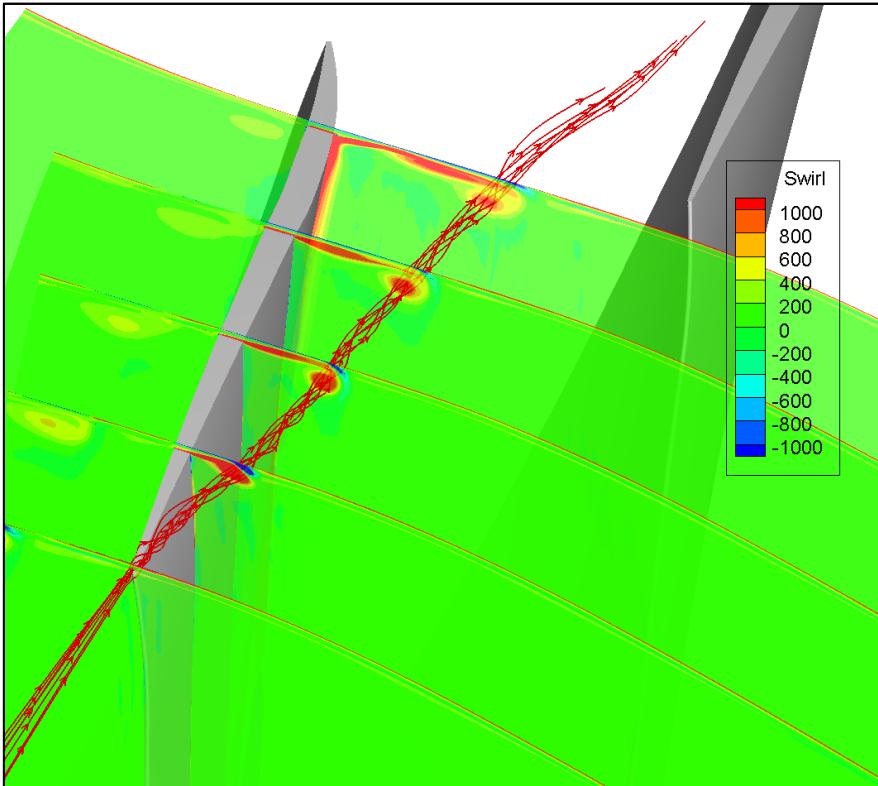
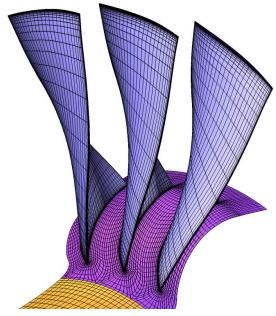
Axial Turbine

V&V Aachen 1.5 Stage Axial Turbine



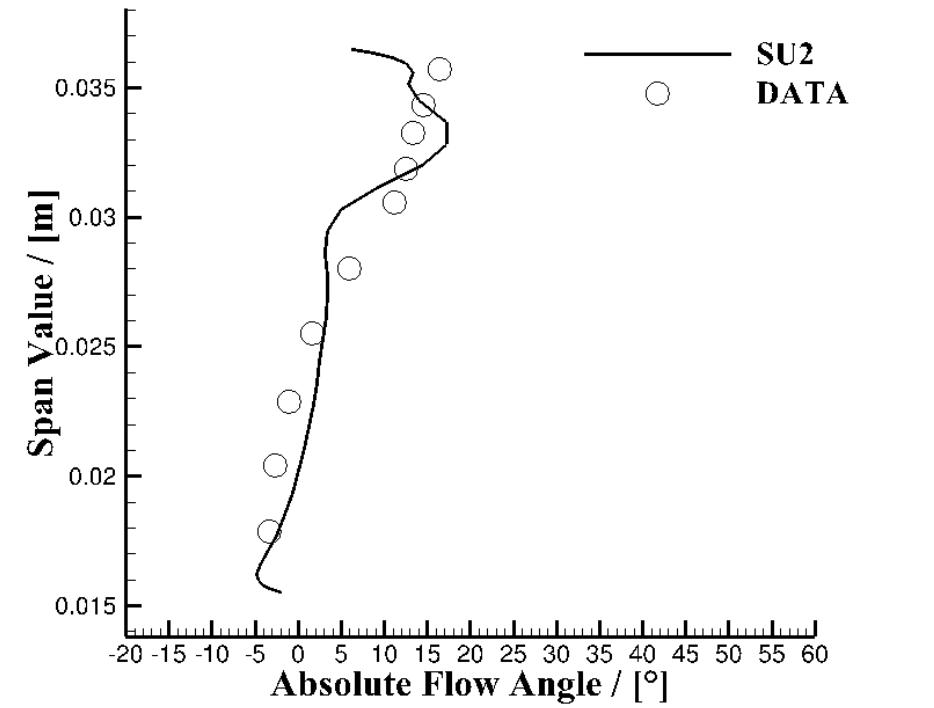
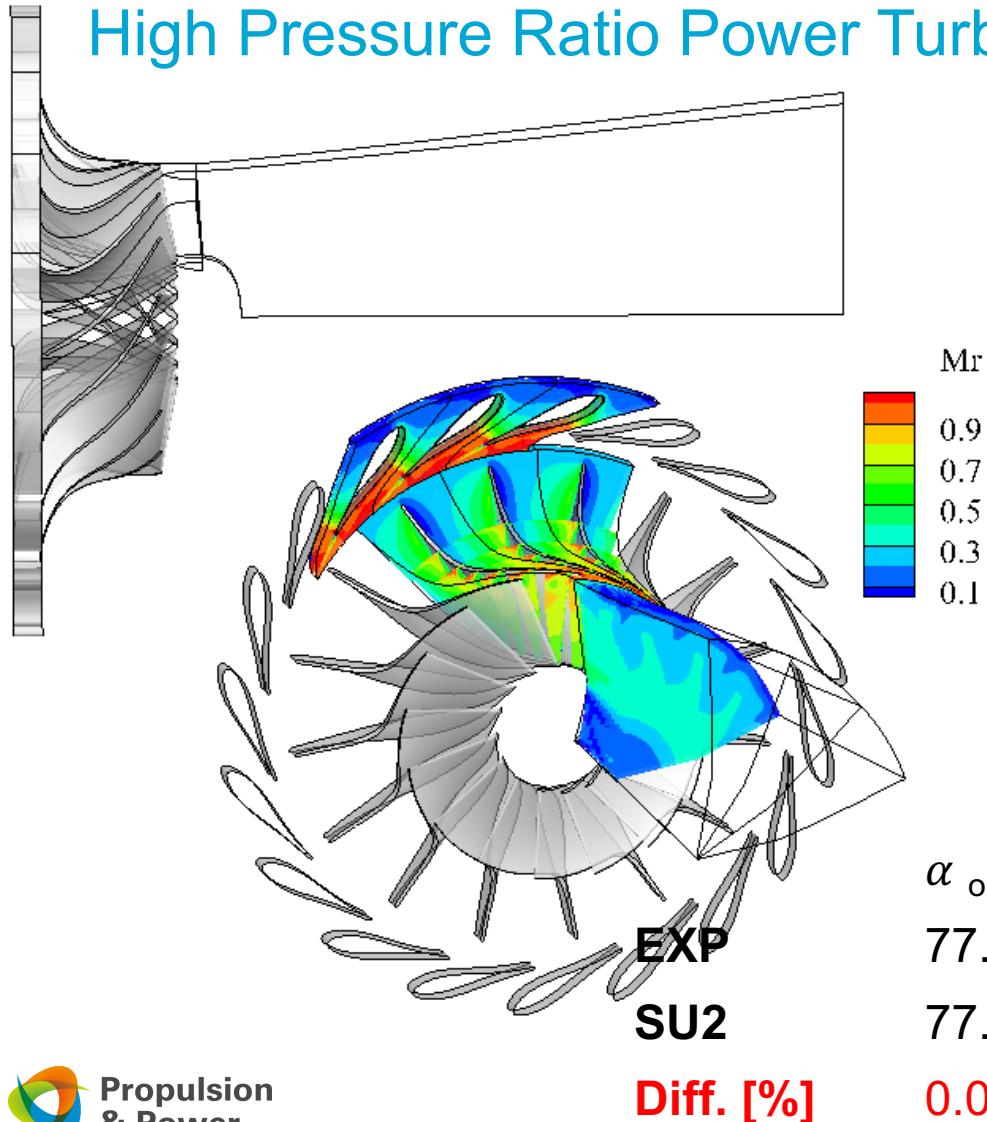
Transonic Compressor

Nasa Rotor 37 - Comparison with Experiments



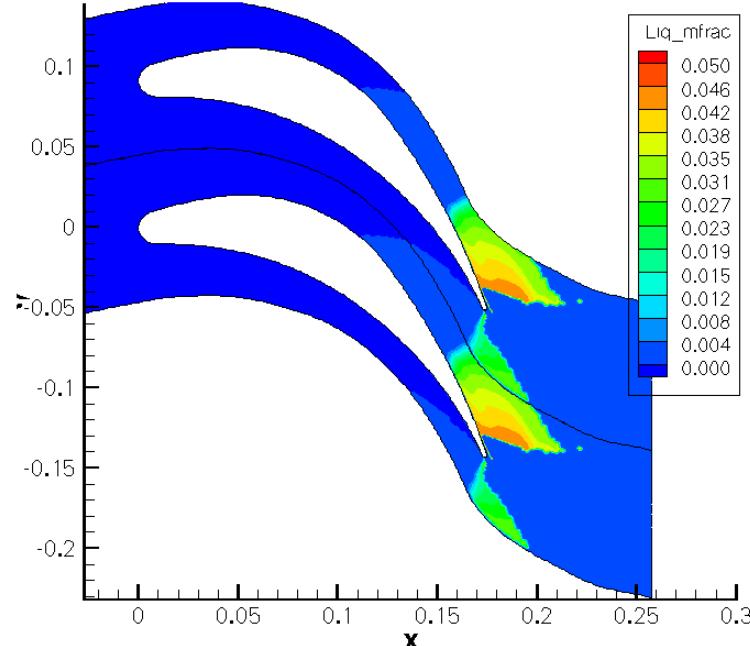
APU Turbine

High Pressure Ratio Power Turbine - Comparison with Experiments

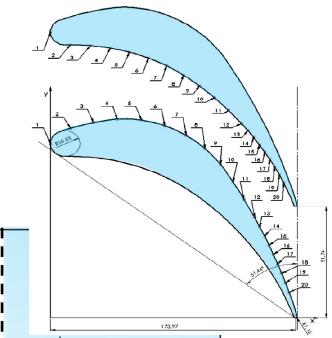
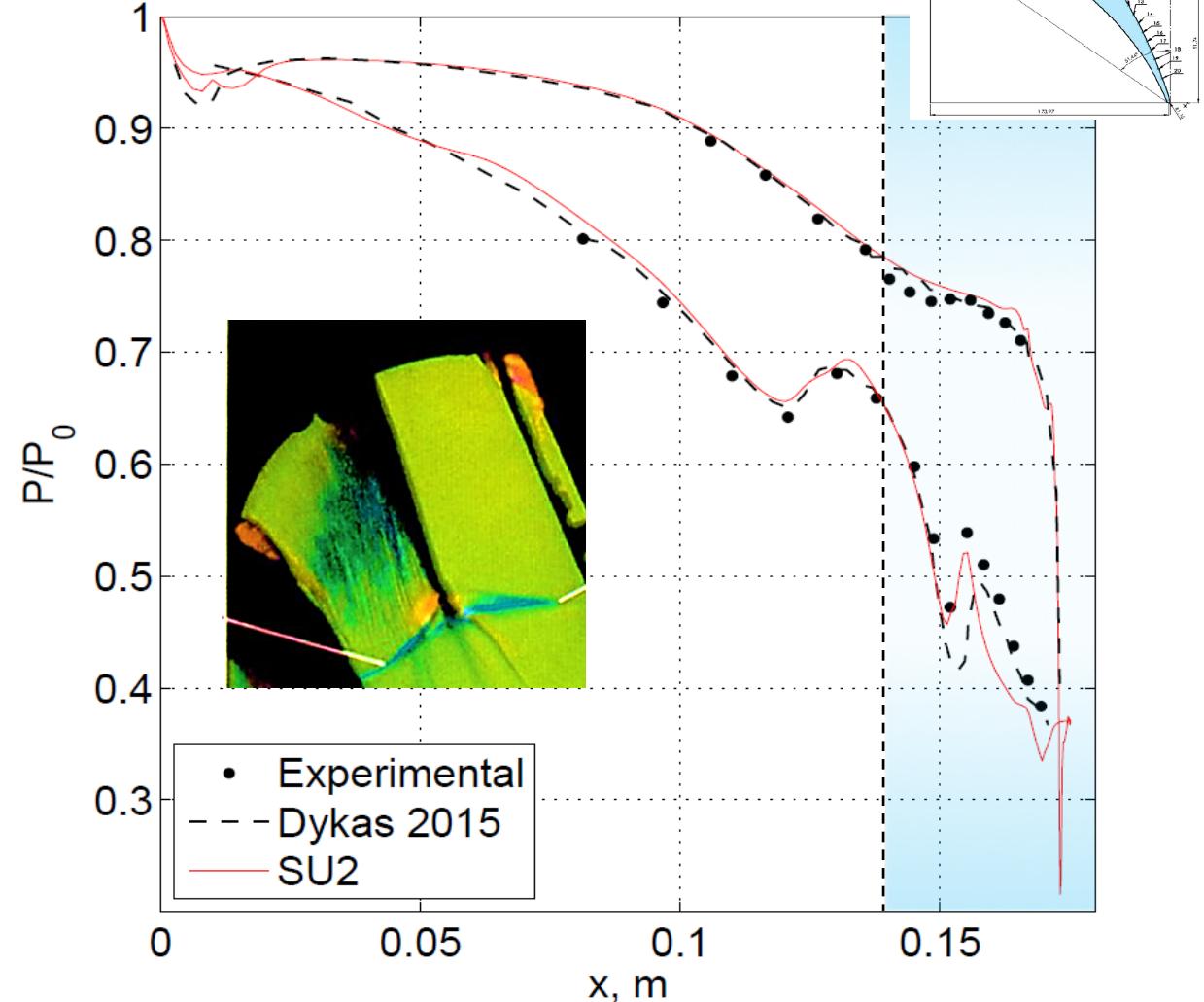


Steam Turbine Cascade

Prediction of metastable condensation



Liquid mass fraction

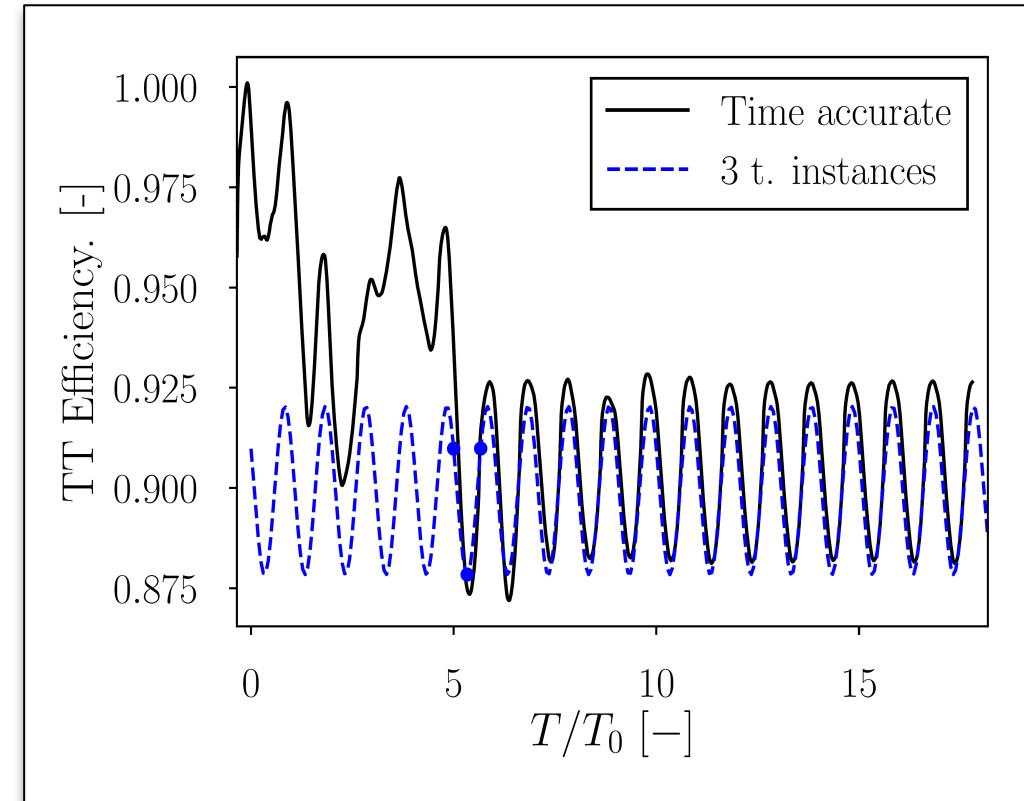
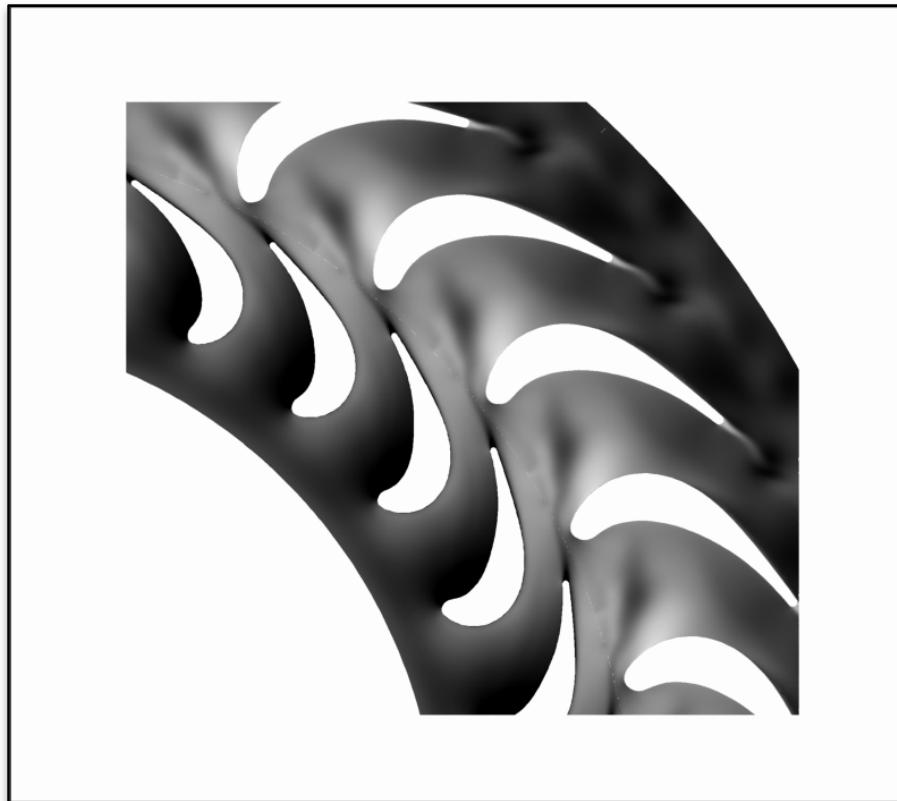


(Some) Paradigmatic Examples

Stator-Rotor Interaction with HB

Radial Outflow ORC Turbine Stage

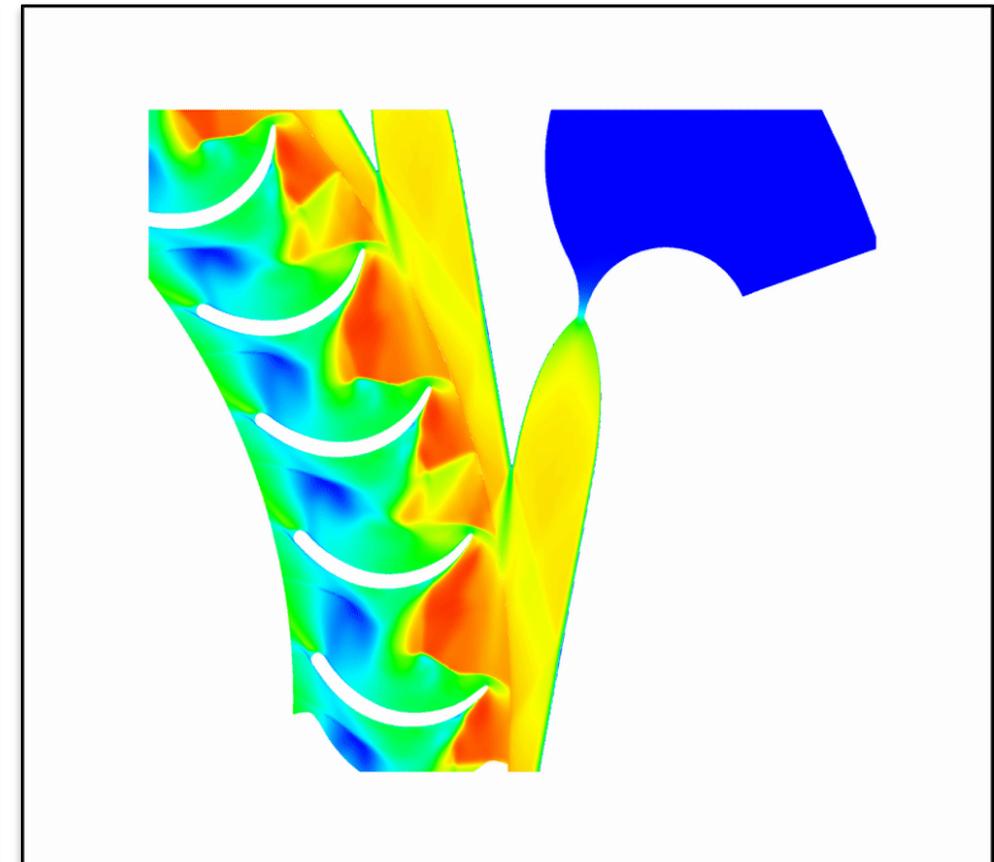
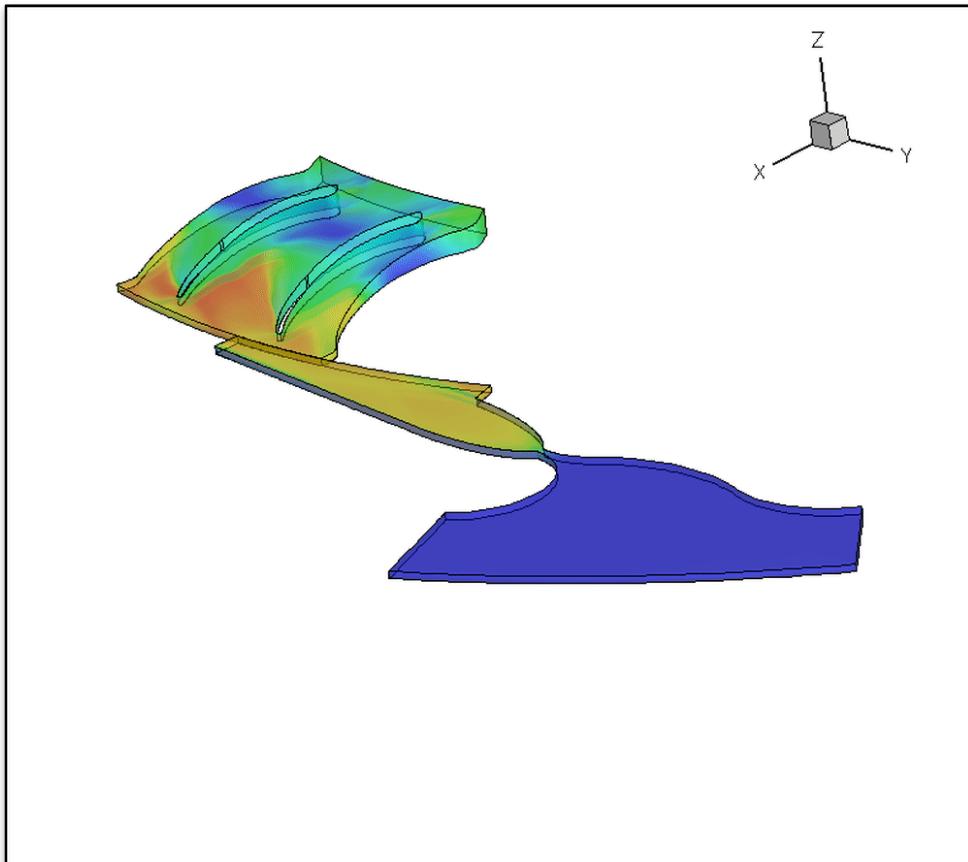
$$\frac{time_{UNST}}{time_{HB}} \approx 5$$



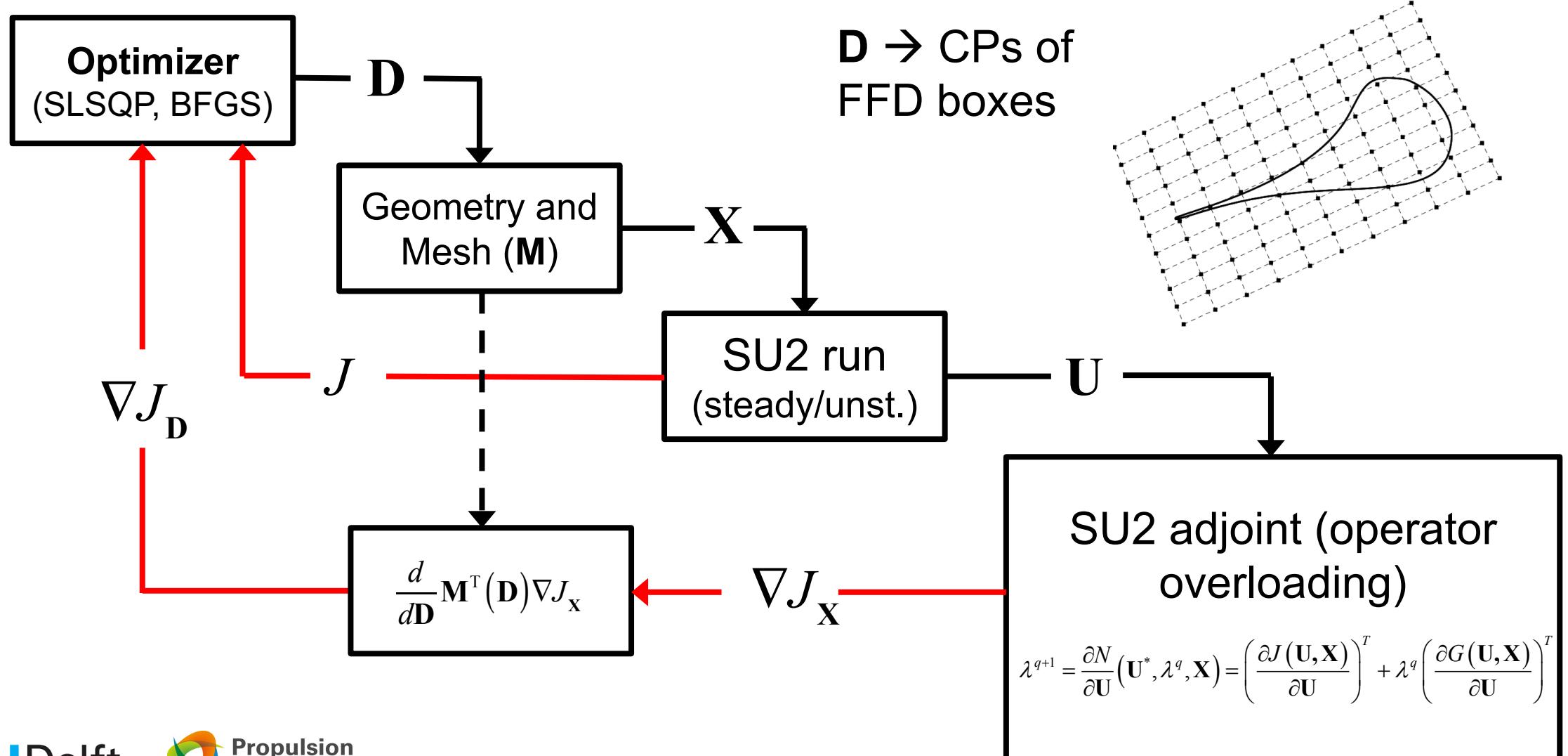
Stator-Rotor Interaction with HB

Supersonic ORC Radial-Inflow Turbine, Q3D

$$\frac{time_{UNST}}{time_{HB}} \cong 6$$

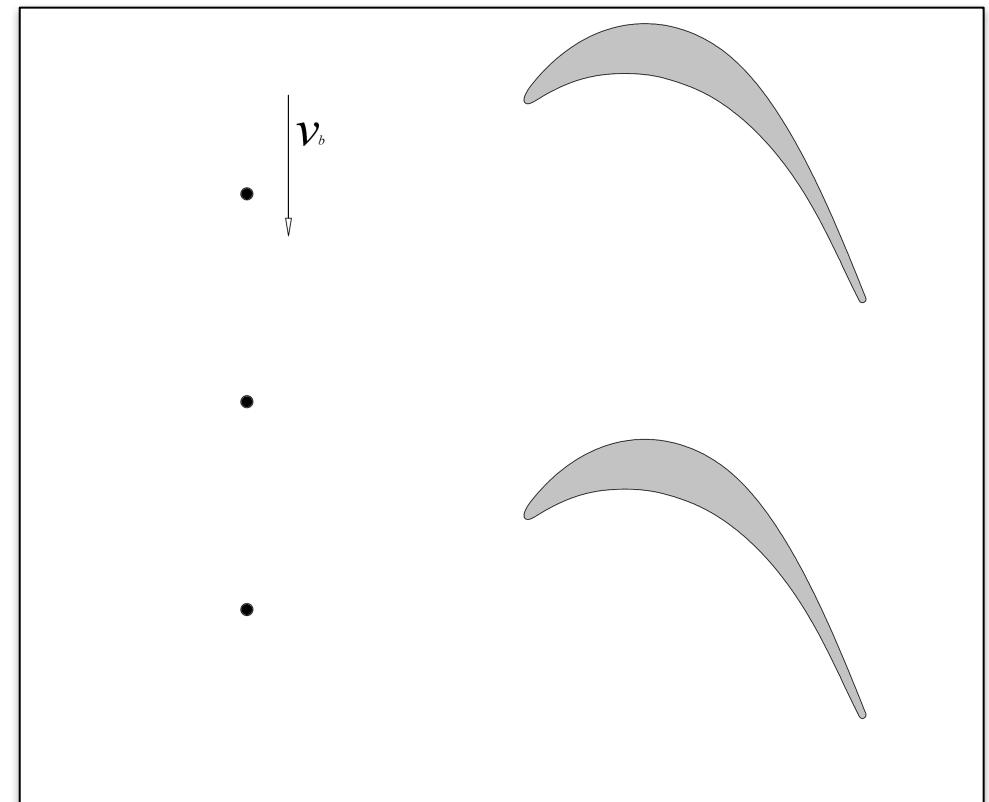
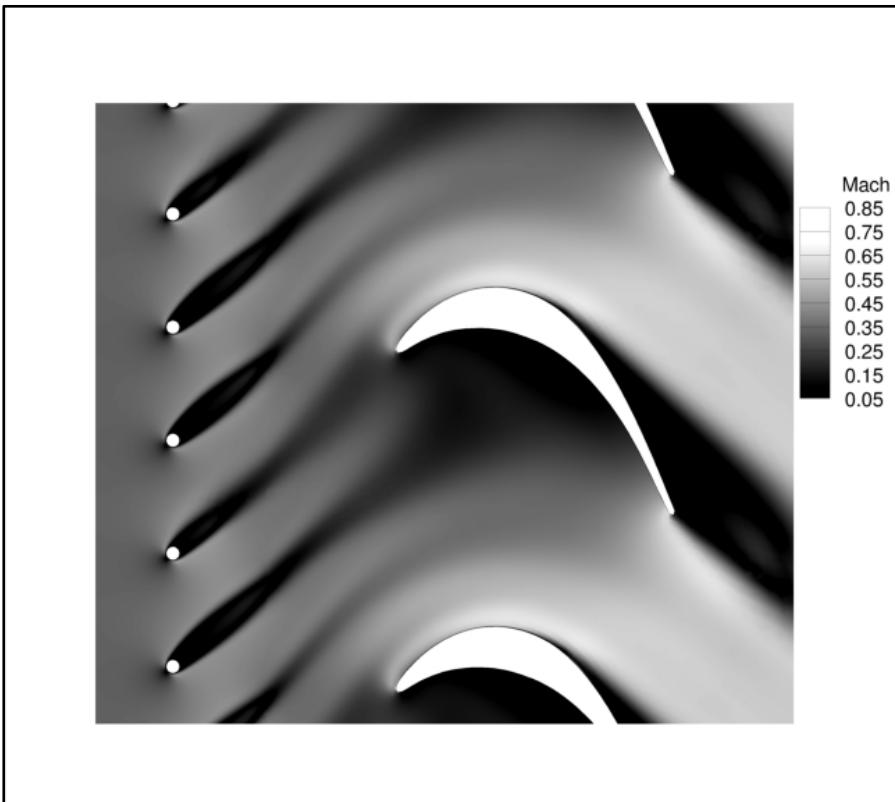


How We Solve the Turbo Design Problem



Unsteady Design Problem

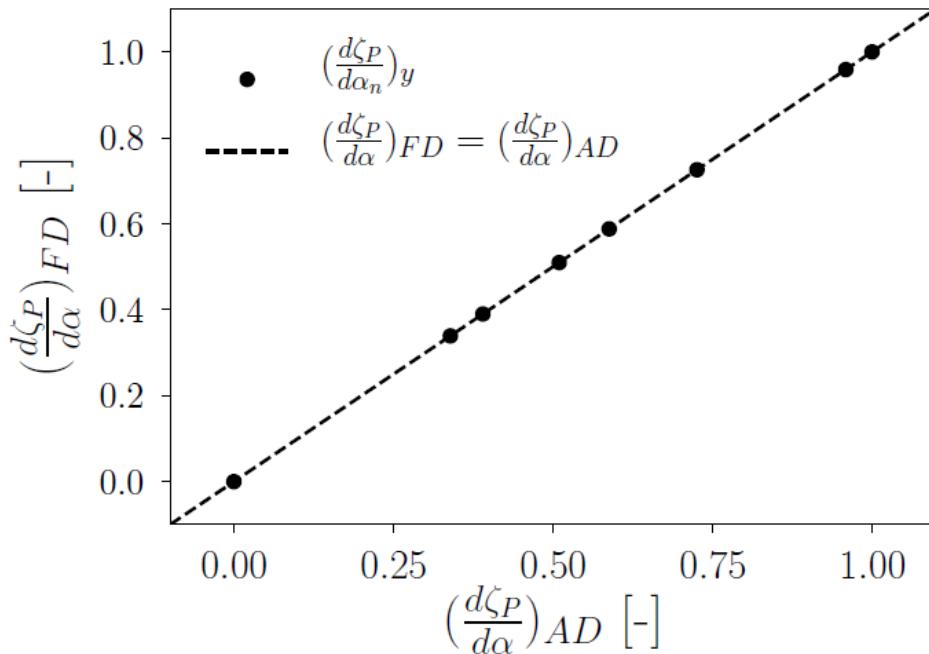
Wake-rotor interaction



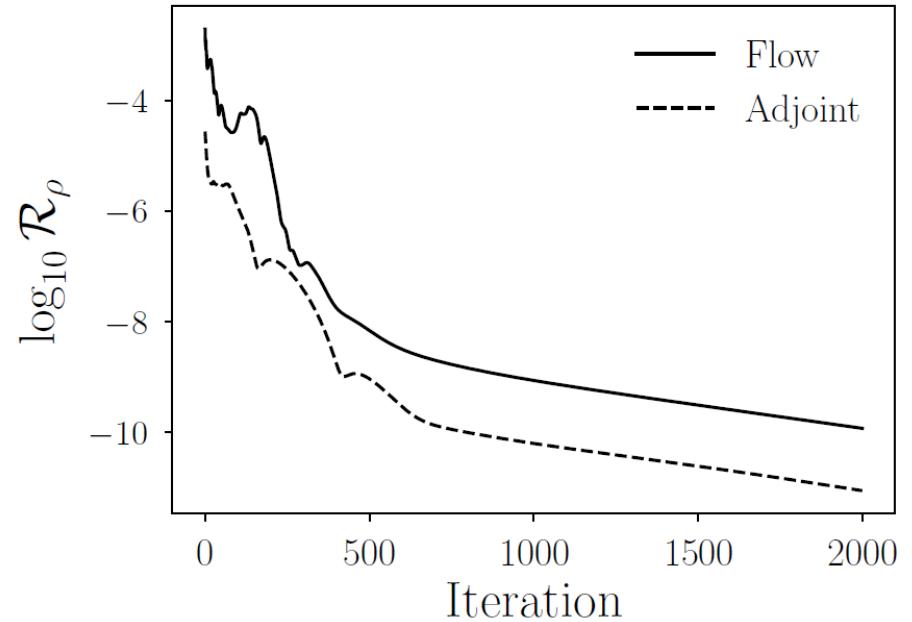
$$\frac{\text{running time HB}}{\text{running time unsteady}} = 0.3$$

Unsteady Design Problem

Adjoint harmonic balance gradient validation



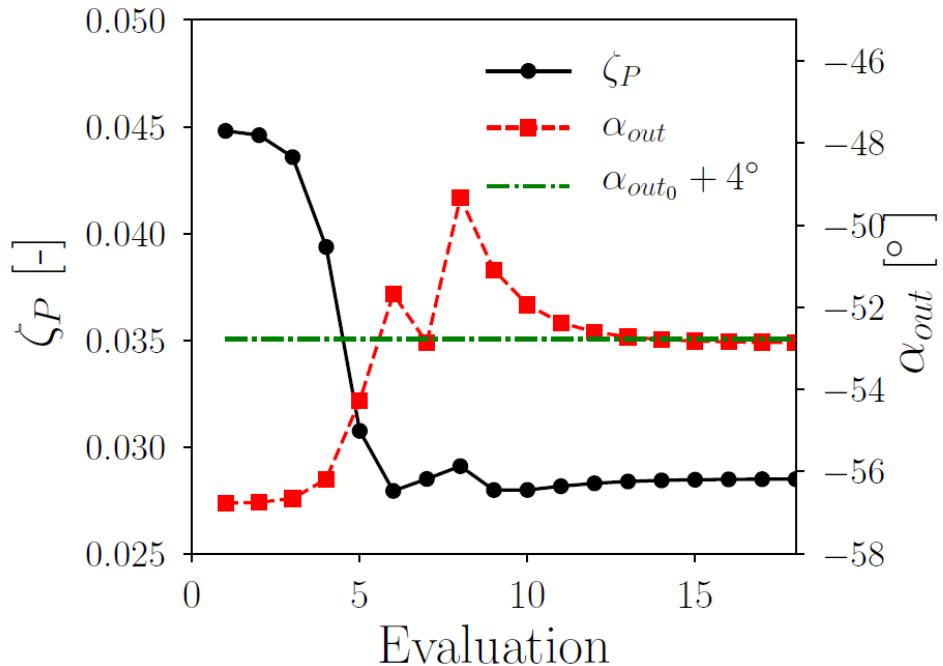
Gradient validation
(RMSE < 1E-5)



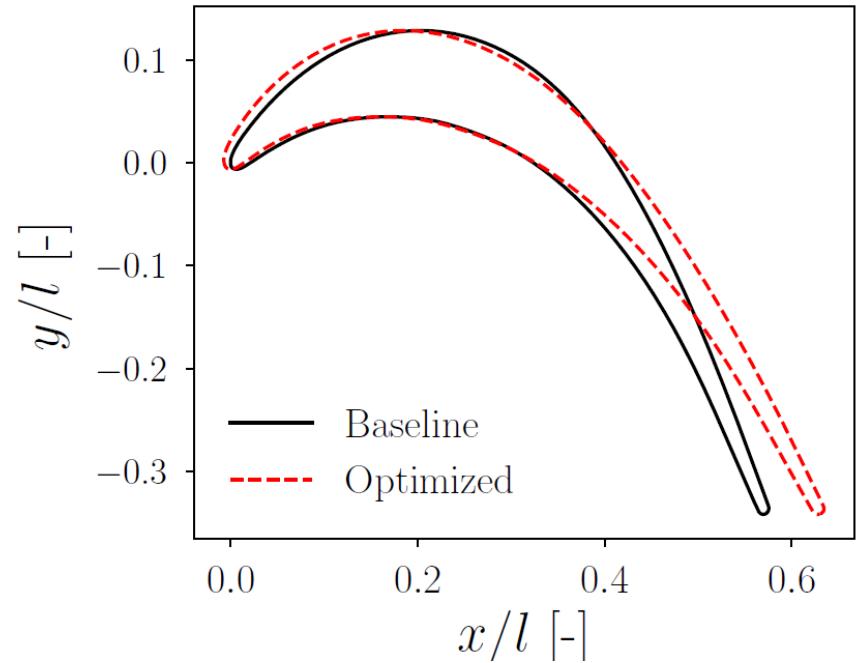
Adjoint vs Flow
convergence rate

Unsteady Design Problem

Optimization results



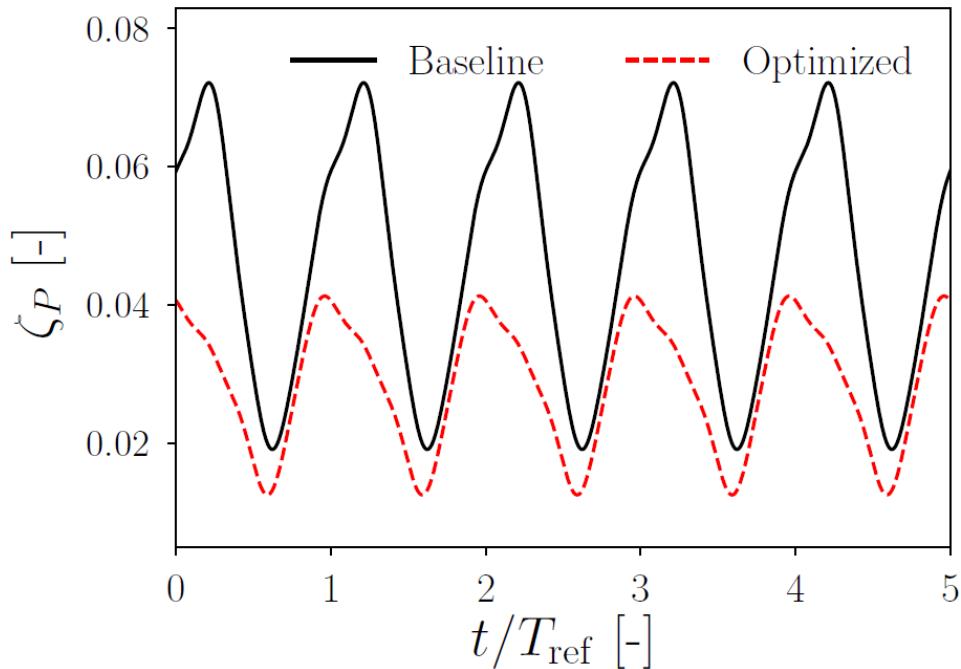
Optimization History



Baseline vs Optimized
Blade Profile

Unsteady Design Problem

Performance gain

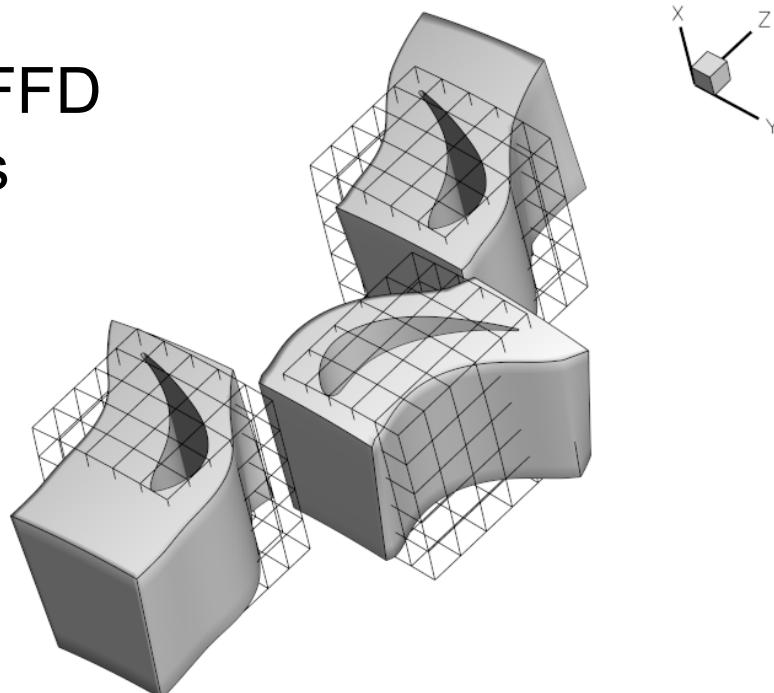


- Mean Loss reduction: **38%**
- Peak reduction: **44%**
- Amplitude reduction: **54%**
- CPU time: $\sim 5 \times$ Steady Opt.

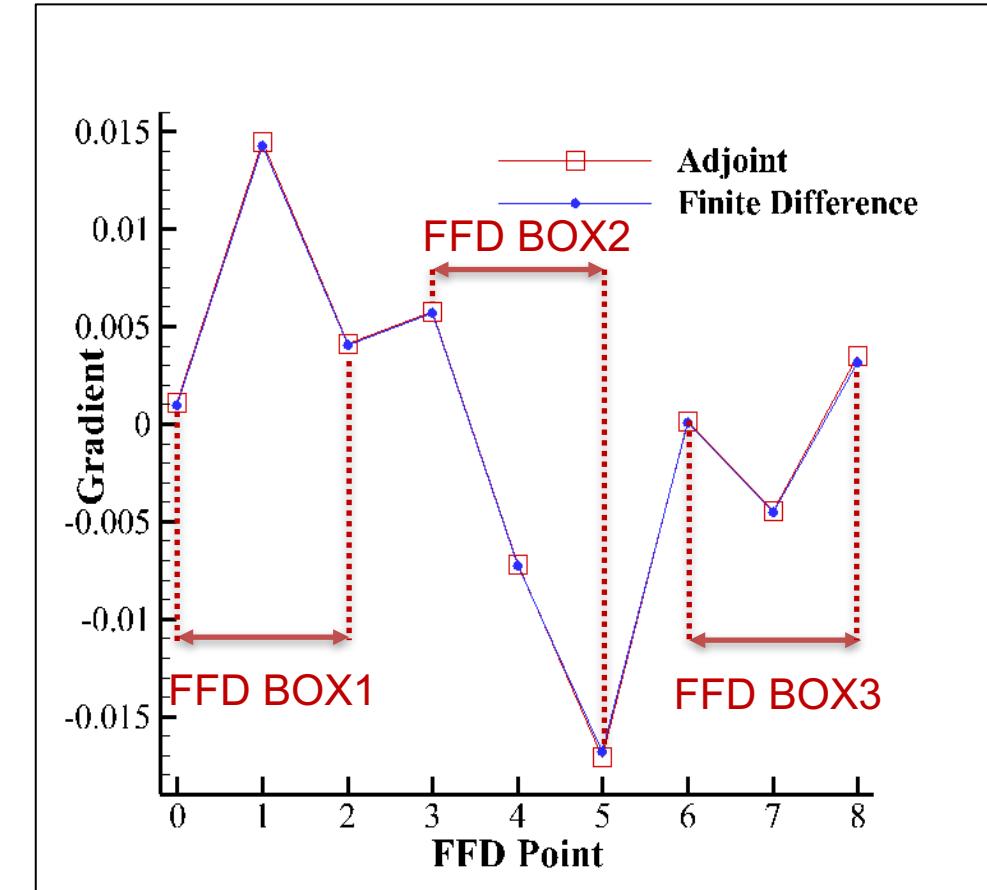
Steady Coupled Design Problem

Mixing-plane gradient validation (obj = stage efficiency)

79 FFD
DVs

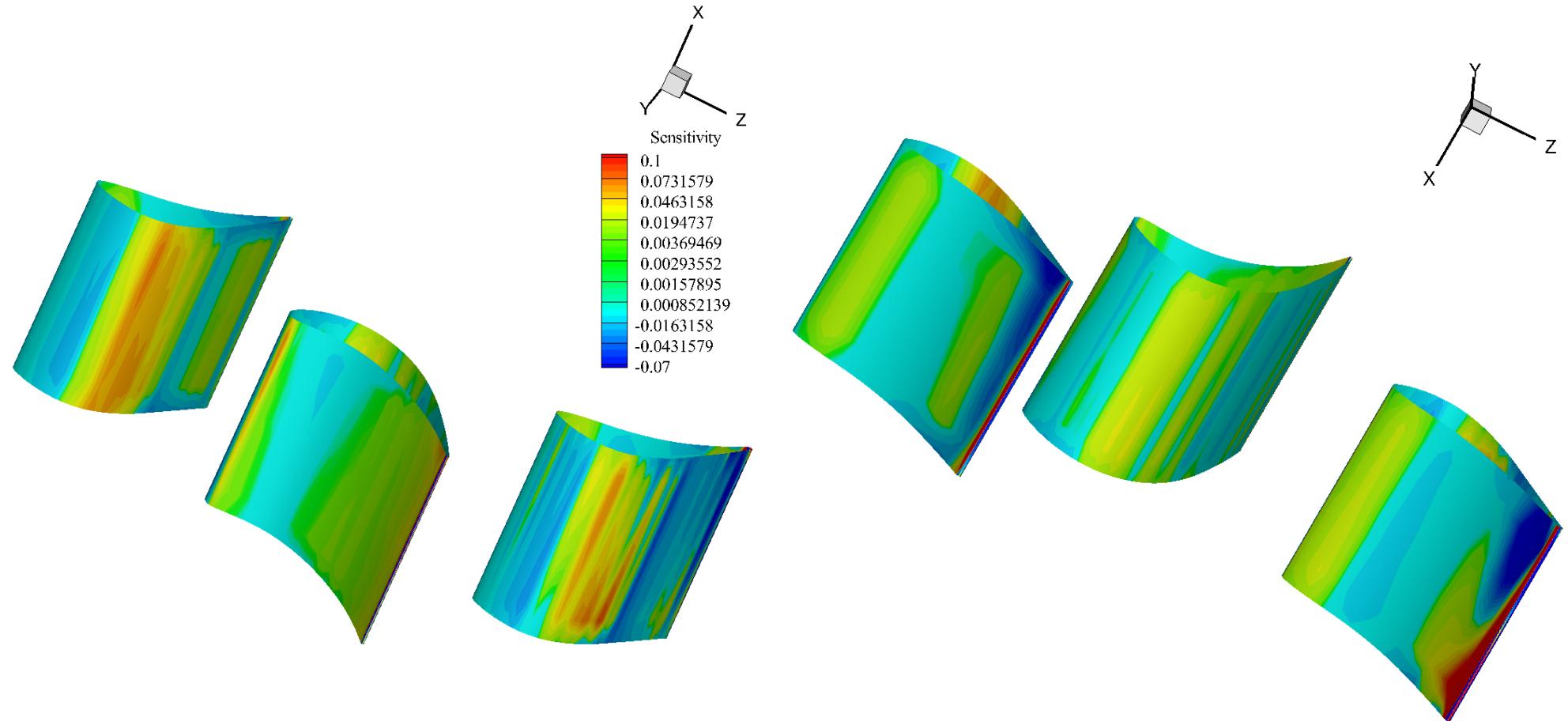


Only 3 points per each FFD Box are selected for the validation



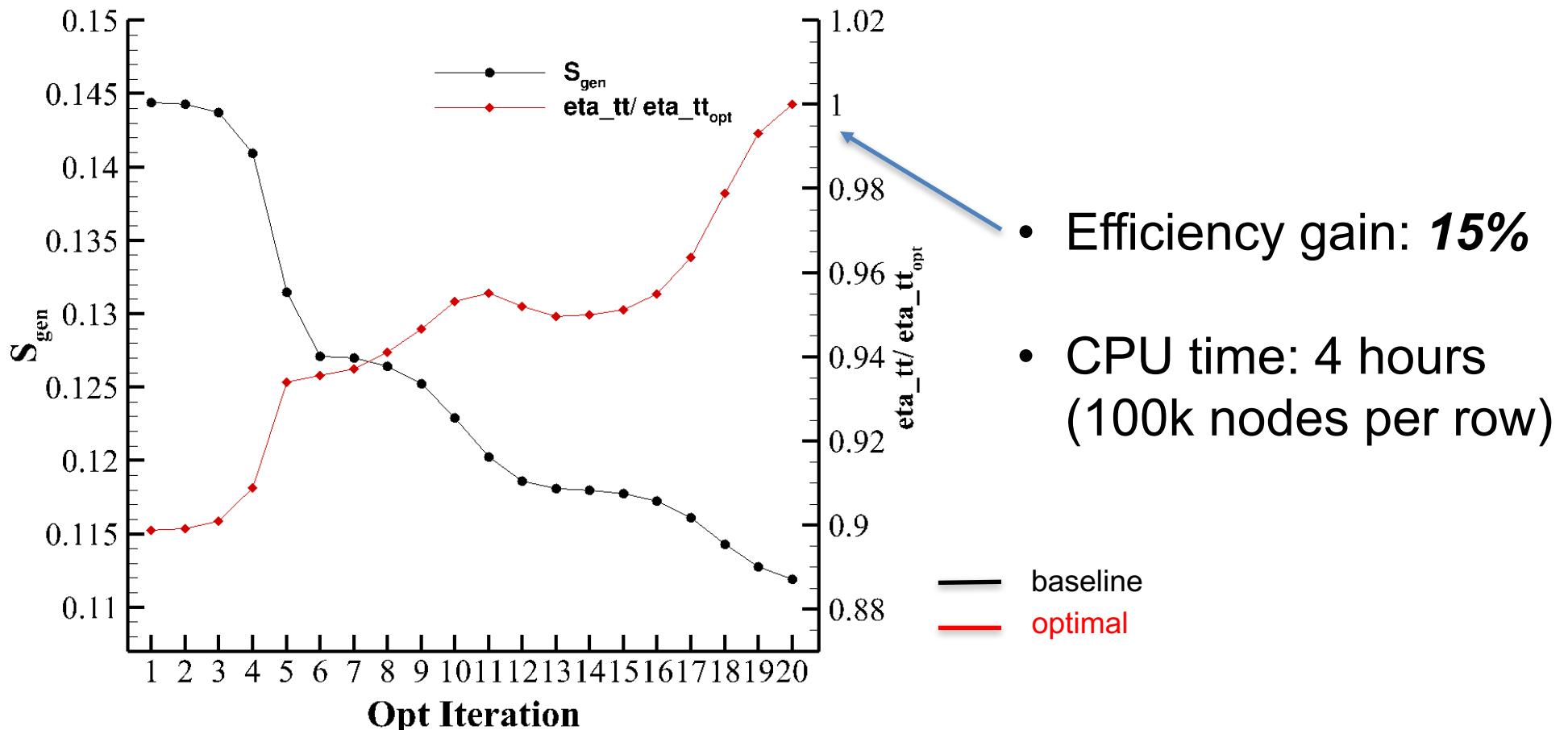
Steady Coupled Design Problem

3D sensitivity of stage efficiency



Steady Coupled Design Problem

Optimization results



Take-Aways

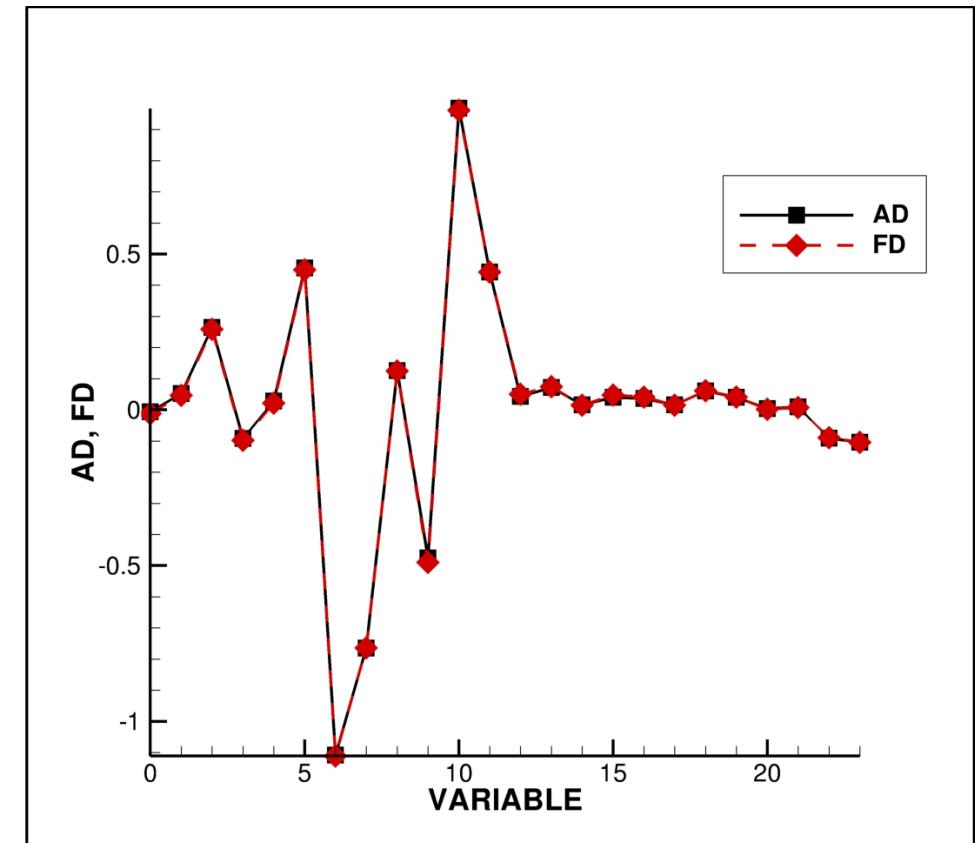
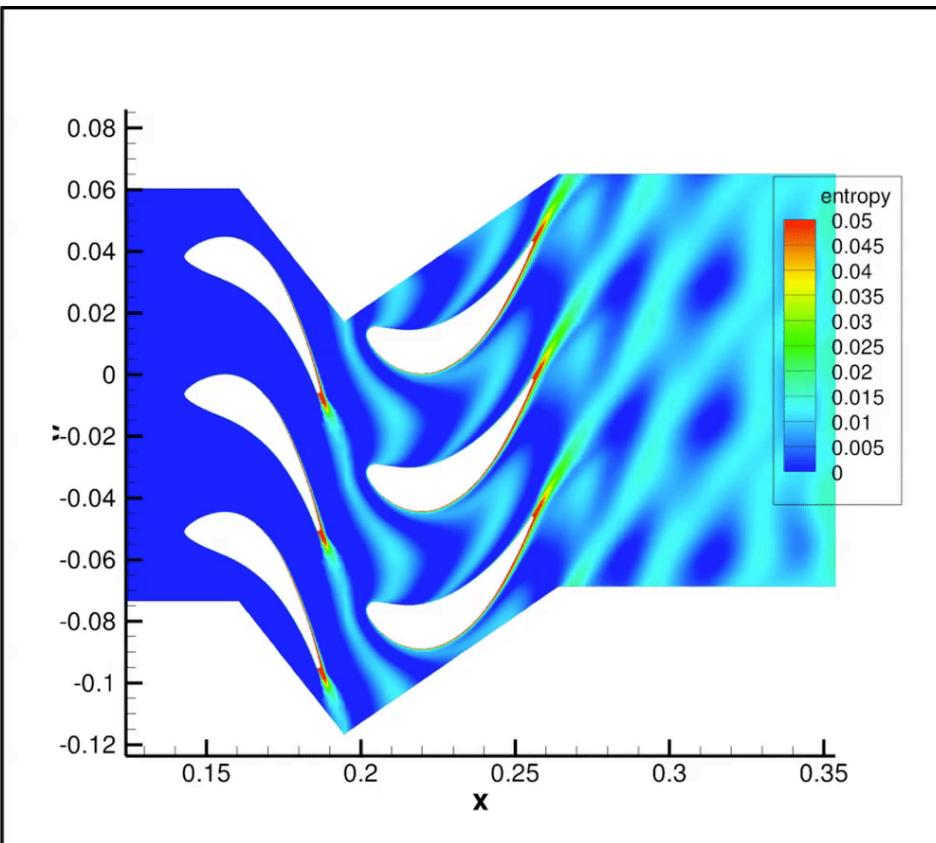
- SU2 accurate for (compressible, NICFD) turbomachinery flows
- First-ever fully turbulent unsteady optimization
- Multi-row design at manageable cost now possible
- Lots of modeling and adjoint-related work remains

Future...

- Release of “turboSU2” (6.0)
- Engage further turbomachinery companies and research institutes
- Partner with other (new) groups to extend capabilities
- Become reference for innovation in automated turbomachinery design

Next: Unsteady Stator-Rotor Design

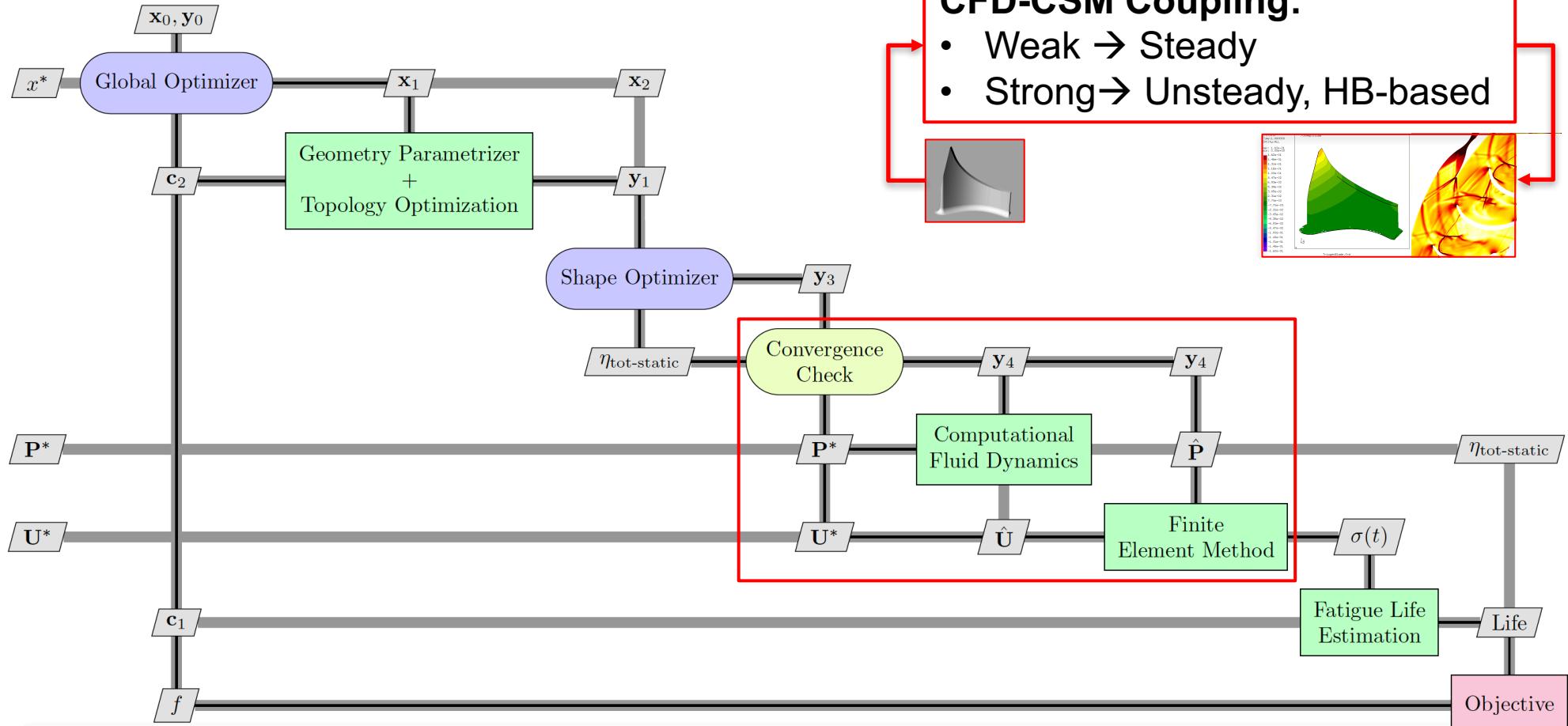
HB for Modeling and Design of Multiple Rows



Next: CAD-based MDO Design

SU2 + OpenFEM with adjoints

openMDAO

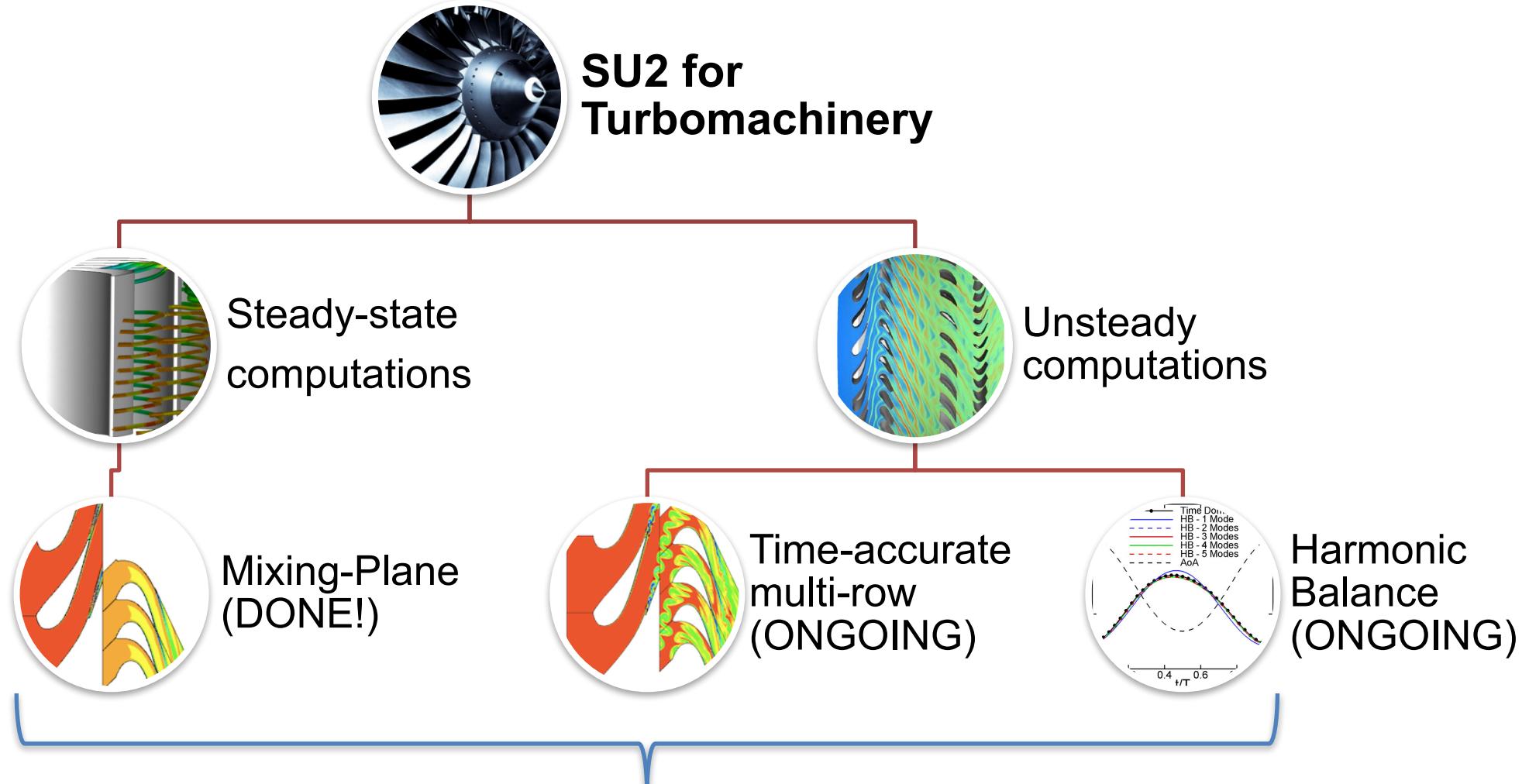


Further info upon request @
m.pini@tudelft.nl

Thank you



Development Roadmap



Governing Equations for NICFD

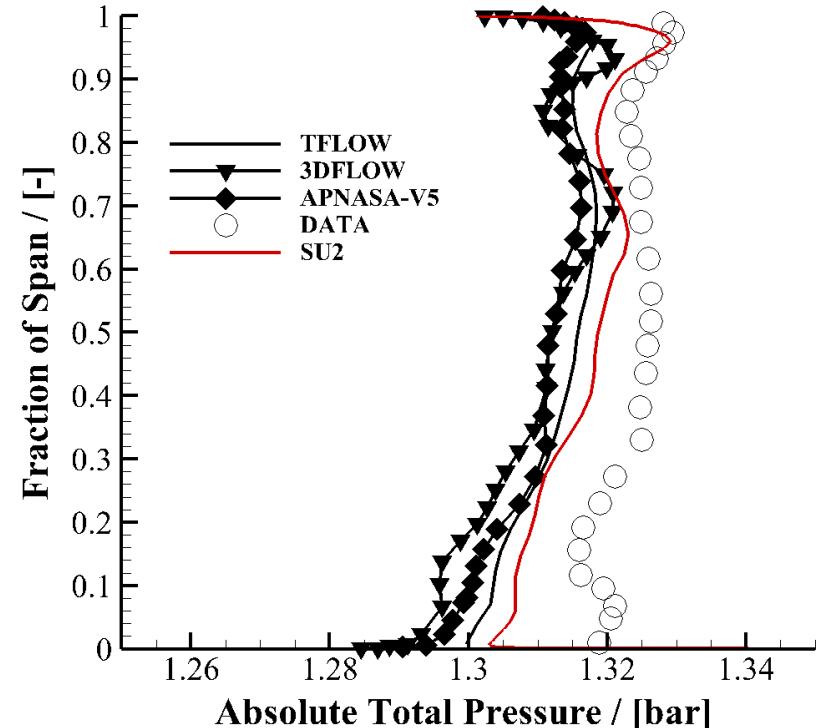
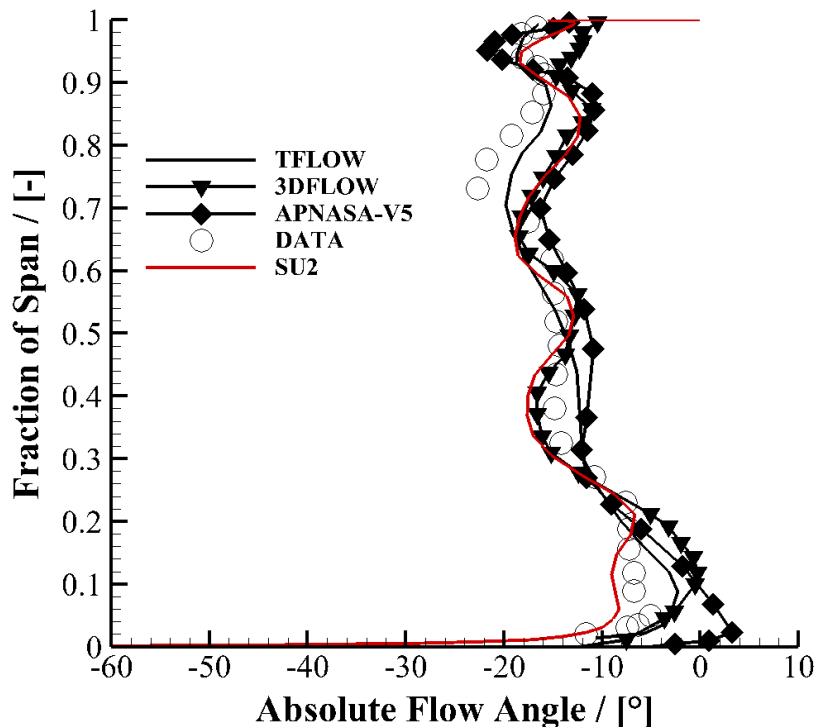
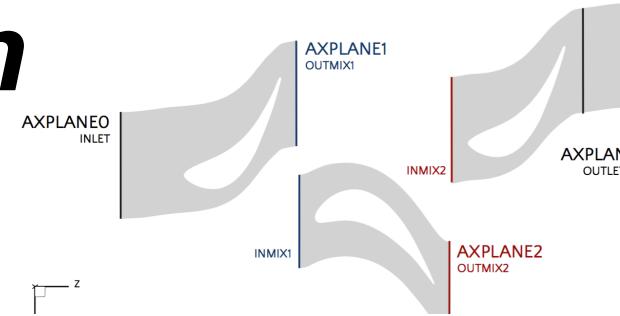
Inviscid equations for mono-component fluid at chemical and thermodynamic equilibrium

$$\left\{ \begin{array}{l} \partial_t \rho + \nabla \cdot (\rho \mathbf{u}) = 0, \\ \partial_t (\rho \mathbf{u}) + \nabla \cdot (\rho \mathbf{u} \otimes \mathbf{u} + P) = 0, \\ \partial_t E^t + \nabla \cdot [(E^t + P) \mathbf{u}] = 0, \end{array} \right. \quad \xrightarrow{\hspace{1cm}} \quad E^t = \rho e + \frac{1}{2} \rho |\mathbf{u}|^2$$

We need a thermodynamic closure $\rightarrow P = P(\rho, e) = (\gamma - 1)\rho e$ Perfect gas

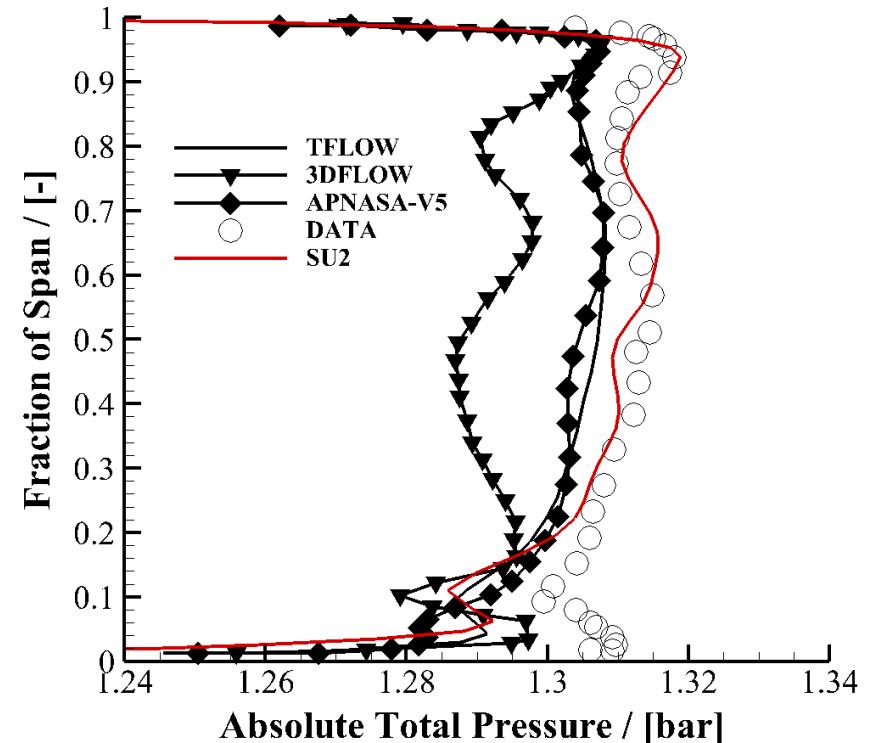
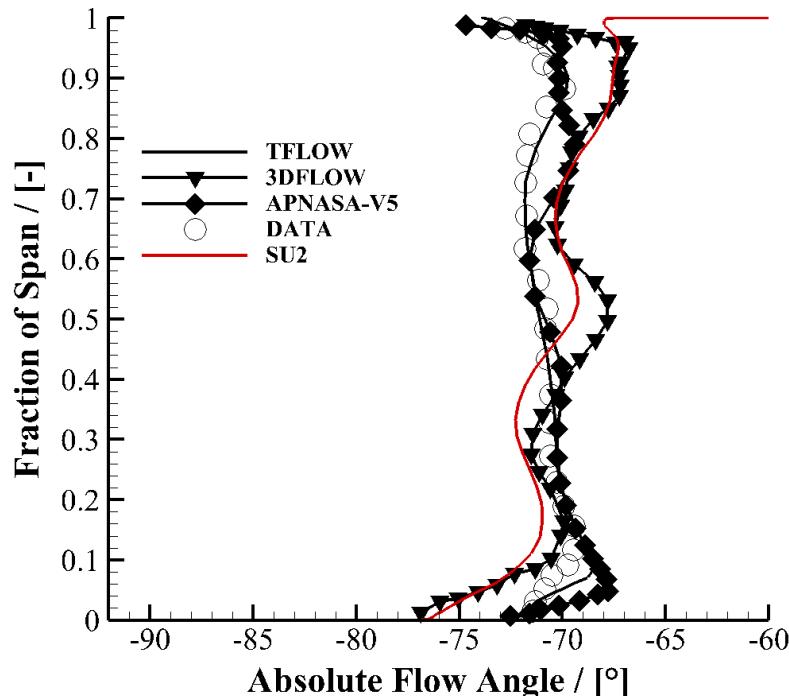
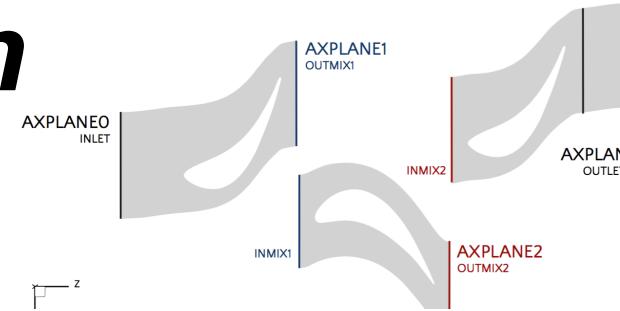
Verification and Validation

Aachen Turbine: plane 2

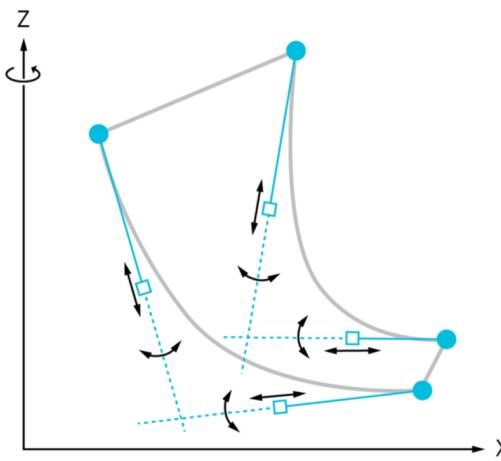


Verification and Validation

Aachen Turbine: plane 3

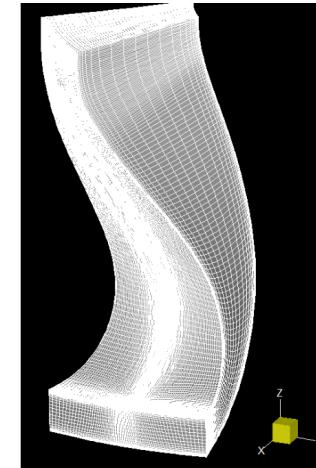


Geometry and Meshing



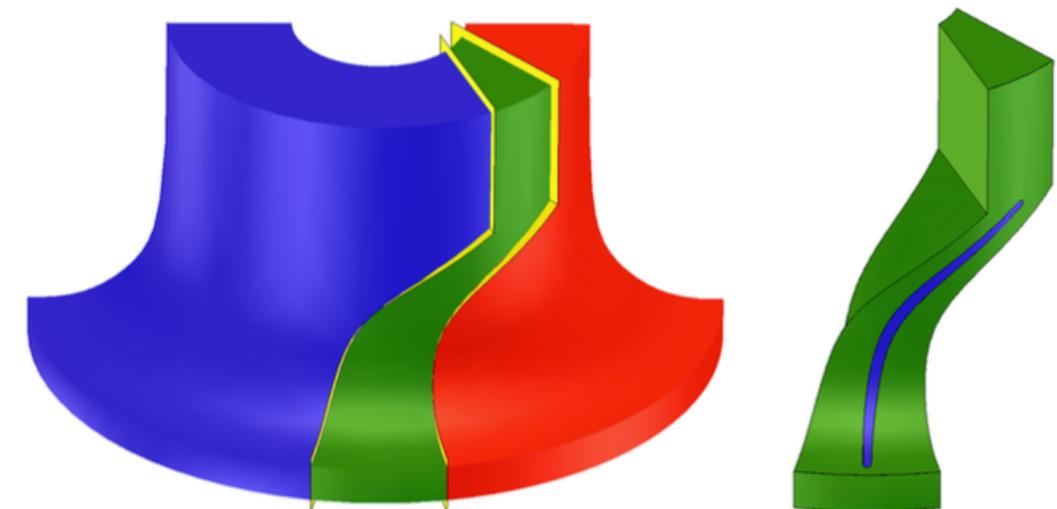
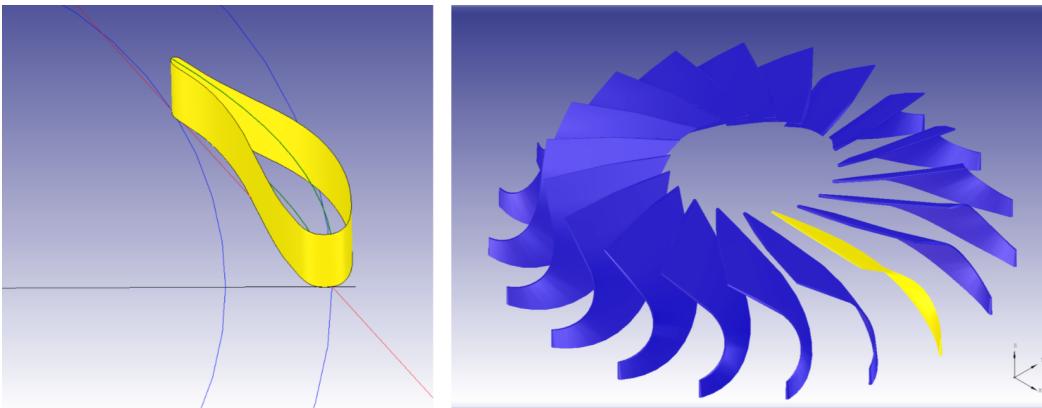
OptiBlade

- Based on OC
- Parametric
- Axial and Radial



Meshing

- Autogrid
- Turbogrid
- Salome



Steady Design of Turbine Cascades

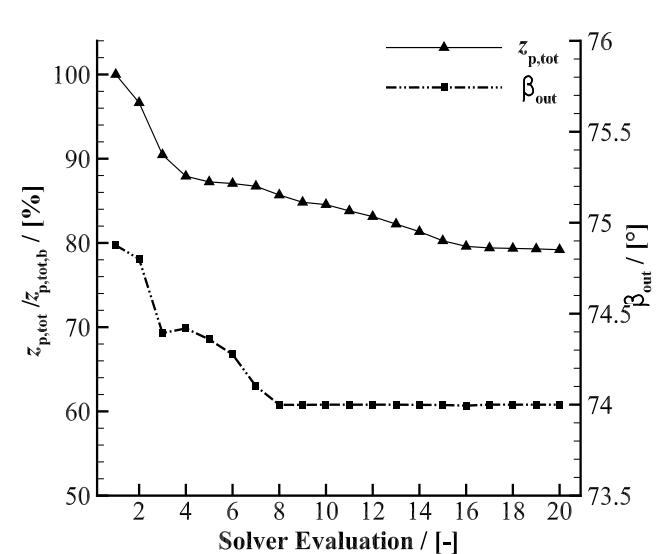
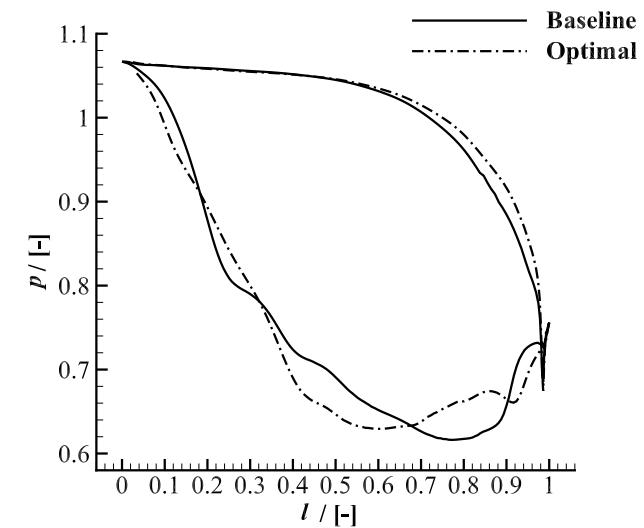
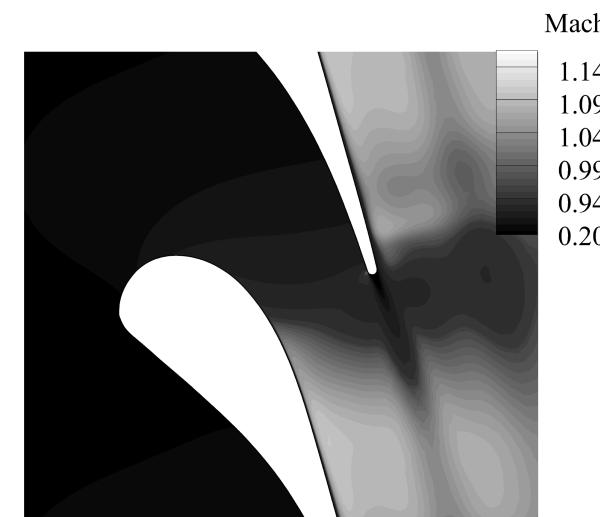
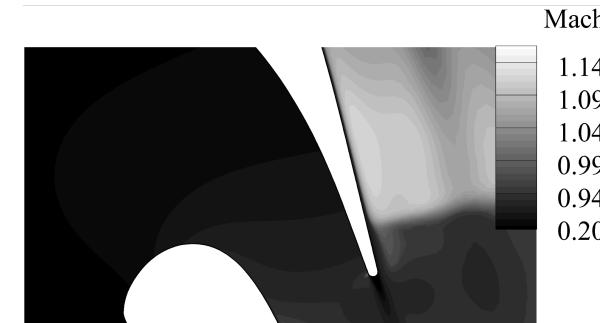
Fluid: Siloxane MDM

$$\min \quad J = z_{p,\text{tot}}$$

$$\text{subject to } \beta_{\text{out}} > 74^\circ$$

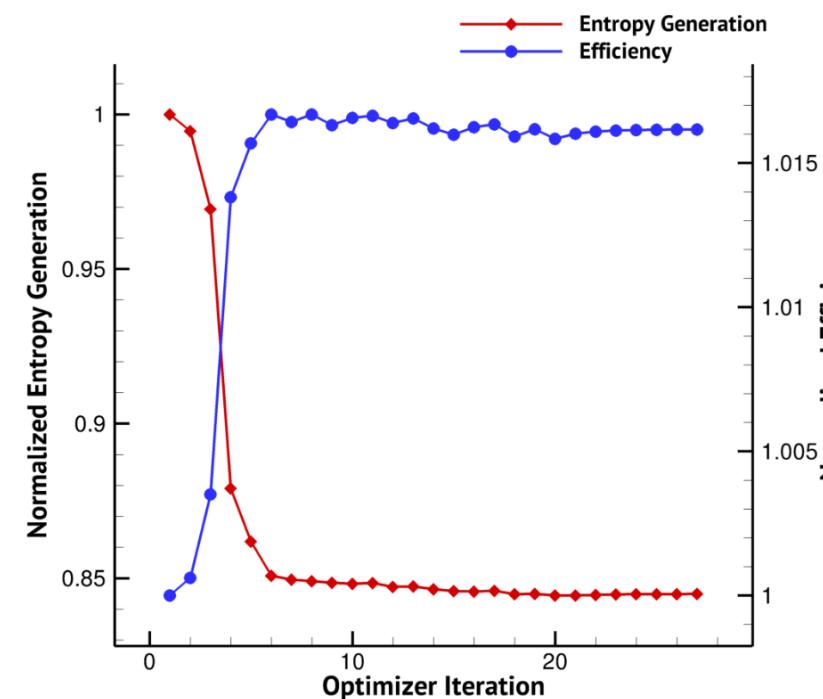
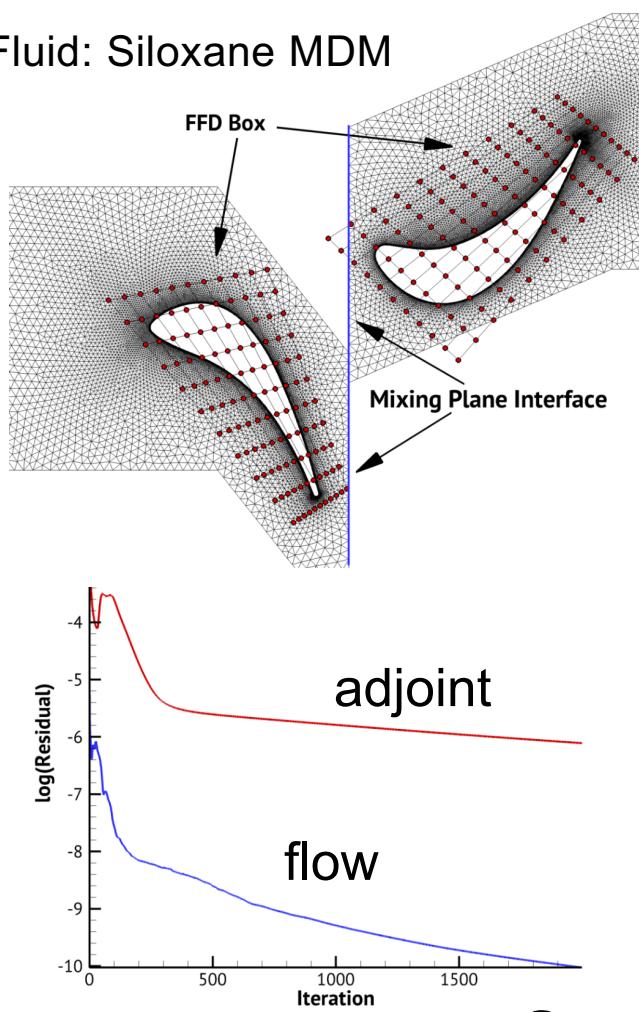
$$\frac{\text{running time adjoint}}{\text{running time flow}} = 1.3$$

$$\frac{\text{memory adjoint}}{\text{memory flow}} = 6 \div 8$$

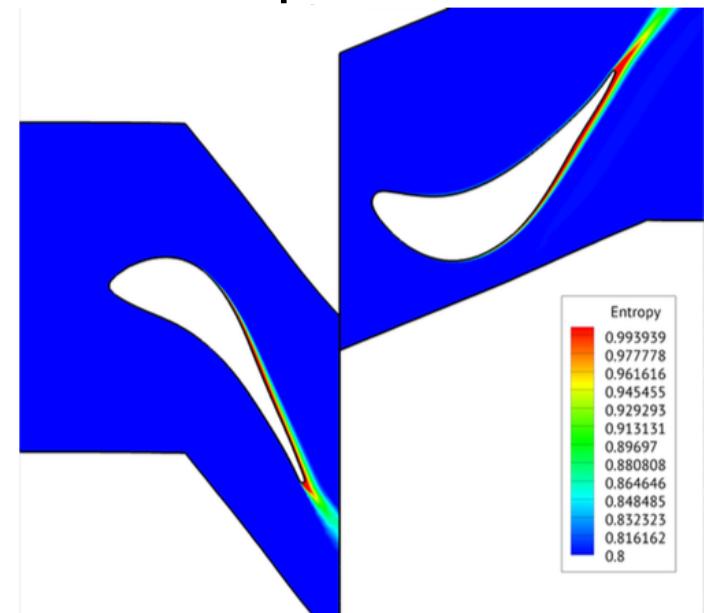


2D Steady Design of Turbine Stages

Fluid: Siloxane MDM



Optimized



$$\frac{\text{running time adjoint}}{\text{running time flow}} = 1.0$$

$$\frac{\text{memory adjoint}}{\text{memory flow}} = 4.5$$

Successful verification of the discrete adjoint mixing-plane

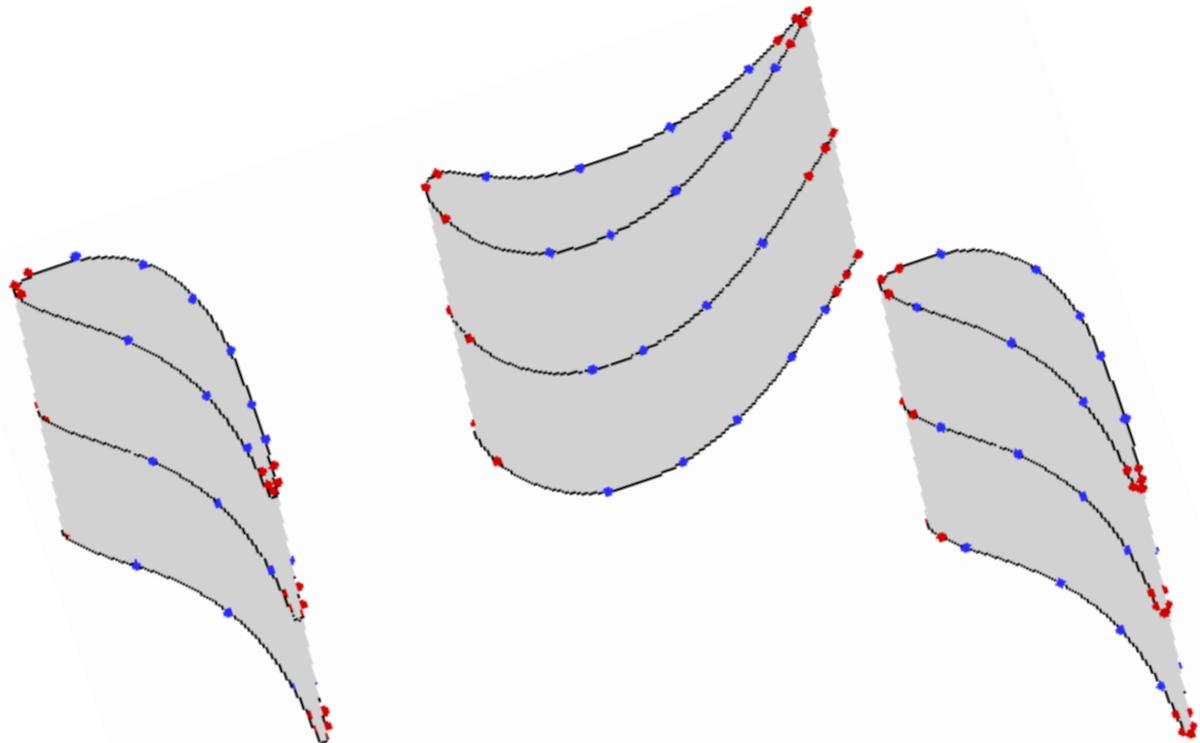
Steady Coupled Design Problem

Parametrization with direct FFD, 79 DVs

3 pilot profile x blade

72 x ● Geometrical Constraint to
preserve LE and TE round
shape

79 x ● Design Variables



Method of Moments

- 4 Transport Equations for Moments

$$\left\{ \begin{array}{l} \frac{\partial}{\partial t}(\rho) + \frac{\partial}{\partial x}(\rho v) = S_c \\ \frac{\partial}{\partial t}(\rho v) + \frac{\partial}{\partial x}(\rho v^2 + P) = S_c v \\ \frac{\partial}{\partial t}(\rho e_0) + \frac{\partial}{\partial x}(\rho h_0 v) = S_c h_{0,l} \end{array} \right. \quad \left\{ \begin{array}{l} \frac{\partial}{\partial t}(\rho_m \mu_0) + \frac{\partial}{\partial x}(\rho_m \mu_0 v_m) = \rho_m J_* \\ \frac{\partial}{\partial t}(\rho_m \mu_1) + \frac{\partial}{\partial x}(\rho_m \mu_1 v_m) = \rho_m J_* r_* + G \mu_0 \\ \frac{\partial}{\partial t}(\rho_m \mu_2) + \frac{\partial}{\partial x}(\rho_m \mu_2 v_m) = \rho_m J_* r_*^2 + 2G \mu_1 \\ \frac{\partial}{\partial t}(\rho_m \mu_3) + \frac{\partial}{\partial x}(\rho_m \mu_3 v_m) = \rho_m J_* r_*^3 + 3G \mu_2 \end{array} \right.$$

S_c Mass exchange at interface
J_{}, G* Nucleation, growth rate

- ✓ Upwind flux, 1st – 2nd order
- ✓ Implicit time integration
- ✓ Segregated approach

$$\mu_j = \int_0^\infty r^j \frac{\partial N}{\partial r} dr \rightarrow \frac{\partial}{\partial t}(\rho_m \mu_j) + \frac{\partial}{\partial x}(\rho_m \mu_j v_m) = j \int_0^\infty \rho_m r^{j-1} G \frac{\partial N}{\partial r} dr + \rho_m J_* R_*^j$$

$$\mu_0 = N_{tot} \quad \mu_1 = N_{tot} R \quad \mu_2 = N_{tot} R^2 \quad \mu_3 = N_{tot} R^3$$

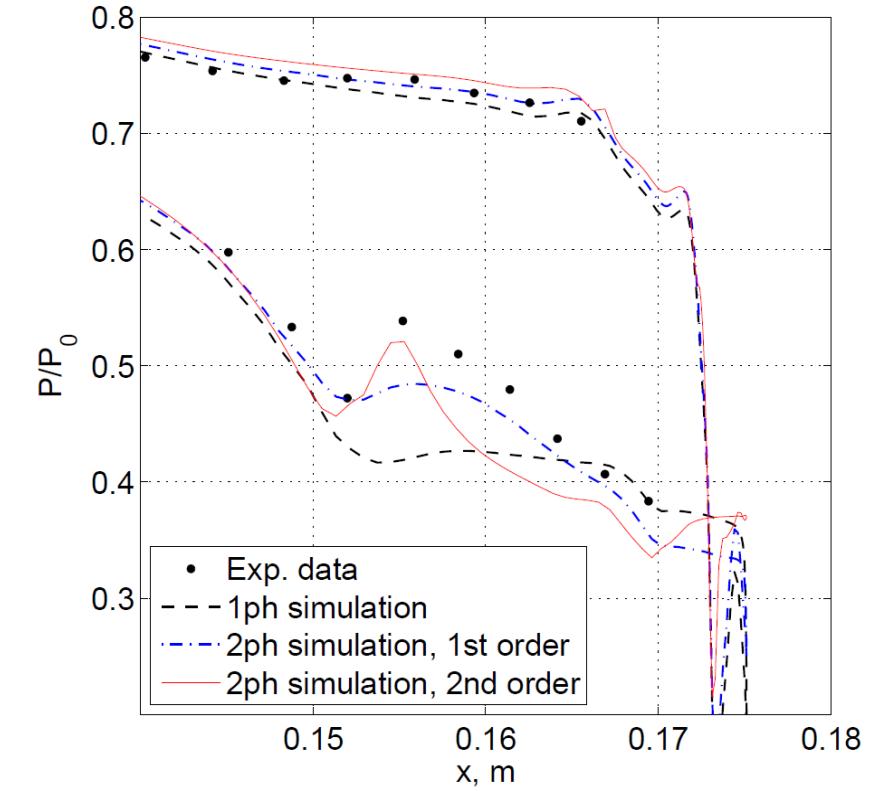
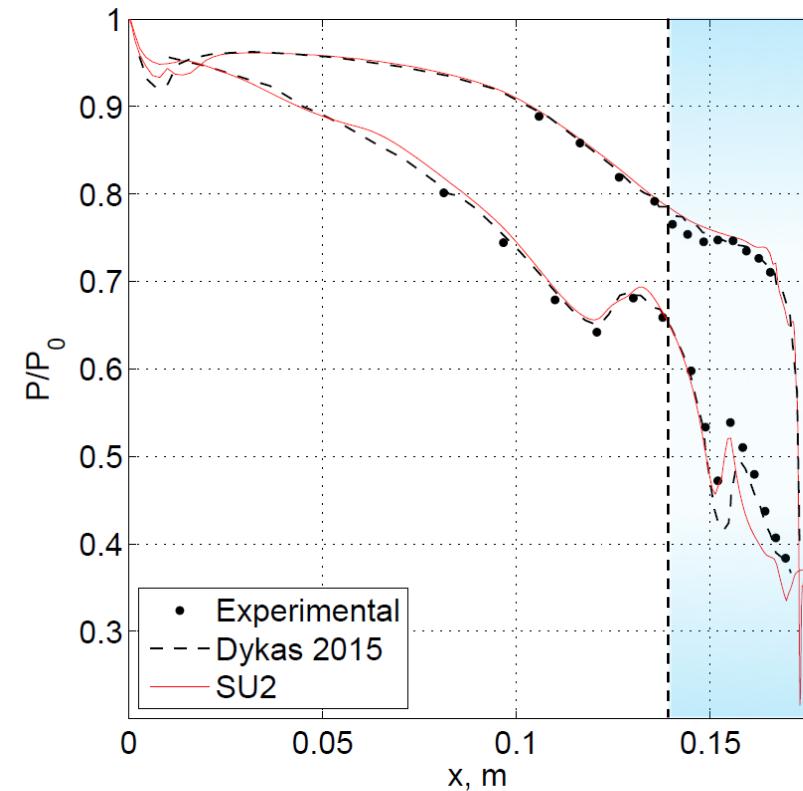
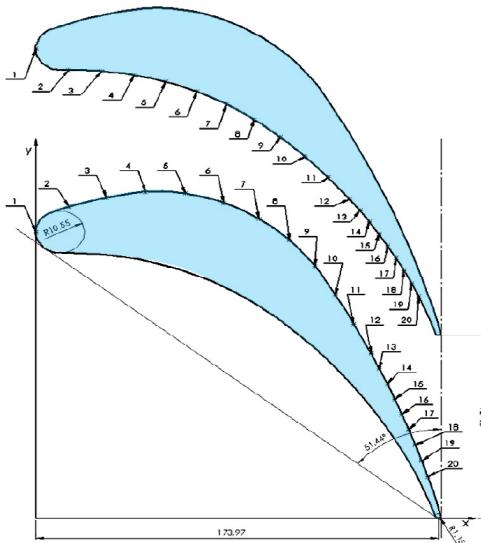
Metastable Condensation with MoM

Cascade [2]

$$T_0 = 373.15 \text{ K}$$

$$P_0 = 0.89 \text{ bar}$$

$$P_{\text{out}} = 0.39 \text{ bar}$$



[2] Dykas, S. et al., 2015. Experimental study of condensing steam flow in nozzles and linear blade cascade. International Journal of Heat and Mass Transfer, 80, pp.50–57