

ass2.R

Subham

Thu Feb 23 21:22:11 2017

```
#ae13b063
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#assignment-2

#library(knitr)
#library(rmarkdown)
library(prob)
```

```
## Warning: package 'prob' was built under R version 3.3.2
```

```
## Loading required package: combinat
```

```
## Warning: package 'combinat' was built under R version 3.3.2
```

```
##
## Attaching package: 'combinat'
```

```
## The following object is masked from 'package:utils':
##
##      combn
```

```
## Loading required package: fAsianOptions
```

```
## Warning: package 'fAsianOptions' was built under R version 3.3.2
```

```
## Loading required package: timeDate
```

```
## Warning: package 'timeDate' was built under R version 3.3.2
```

```
## Loading required package: timeSeries
```

```
## Warning: package 'timeSeries' was built under R version 3.3.2
```

```
## Loading required package: fBasics
```

```
## Warning: package 'fBasics' was built under R version 3.3.2
```

```
##
```

```
## Rmetrics Package fBasics
```

```
## Analysing Markets and calculating Basic Statistics
```

```
## Copyright (C) 2005-2014 Rmetrics Association Zurich
```

```
## Educational Software for Financial Engineering and Computational Science
```

```
## Rmetrics is free software and comes with ABSOLUTELY NO WARRANTY.
```

```
## https://www.rmetrics.org --- Mail to: info@rmetrics.org
```

```
## Loading required package: fOptions
```

```
## Warning: package 'fOptions' was built under R version 3.3.2
```

```
##
```

```
## Rmetrics Package fOptions
```

```
## Pricing and Evaluating Basic Options
```

```
## Copyright (C) 2005-2014 Rmetrics Association Zurich
```

```
## Educational Software for Financial Engineering and Computational Science
```

```
## Rmetrics is free software and comes with ABSOLUTELY NO WARRANTY.
```

```
## https://www.rmetrics.org --- Mail to: info@rmetrics.org
```

```
##
```

```
## Attaching package: 'prob'
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
## intersect, setdiff, union
```

```
#Question-1
```

```
S= tosscoin(5, makespace = TRUE)
```

```
S
```

##	toss1	toss2	toss3	toss4	toss5	probs
## 1	H	H	H	H	H	0.03125
## 2	T	H	H	H	H	0.03125
## 3	H	T	H	H	H	0.03125
## 4	T	T	H	H	H	0.03125
## 5	H	H	T	H	H	0.03125
## 6	T	H	T	H	H	0.03125
## 7	H	T	T	H	H	0.03125
## 8	T	T	T	H	H	0.03125
## 9	H	H	H	T	H	0.03125
## 10	T	H	H	T	H	0.03125
## 11	H	T	H	T	H	0.03125
## 12	T	T	H	T	H	0.03125
## 13	H	H	T	T	H	0.03125
## 14	T	H	T	T	H	0.03125
## 15	H	T	T	T	H	0.03125
## 16	T	T	T	T	H	0.03125
## 17	H	H	H	H	T	0.03125
## 18	T	H	H	H	T	0.03125
## 19	H	T	H	H	T	0.03125
## 20	T	T	H	H	T	0.03125
## 21	H	H	T	H	T	0.03125
## 22	T	H	T	H	T	0.03125
## 23	H	T	T	H	T	0.03125
## 24	T	T	T	H	T	0.03125
## 25	H	H	H	T	T	0.03125
## 26	T	H	H	T	T	0.03125
## 27	H	T	H	T	T	0.03125
## 28	T	T	H	T	T	0.03125
## 29	H	H	T	T	T	0.03125
## 30	T	H	T	T	T	0.03125
## 31	H	T	T	T	T	0.03125
## 32	T	T	T	T	T	0.03125

```

#adding "number of heads" column to S
headcount <- vector(mode="numeric", length=0) #numeric null vector
for (j in 1:nrow(S)) {
  a=0
  for(i in 1:5){
    if(S[j,i]=="H"){
      a = a + 1
    }
  }
  headcount = c(headcount, a)
}
S$noofheads = headcount
S

```

##	toss1	toss2	toss3	toss4	toss5	probs	noofheads
## 1	H	H	H	H	H	0.03125	5
## 2	T	H	H	H	H	0.03125	4
## 3	H	T	H	H	H	0.03125	4
## 4	T	T	H	H	H	0.03125	3
## 5	H	H	T	H	H	0.03125	4
## 6	T	H	T	H	H	0.03125	3
## 7	H	T	T	H	H	0.03125	3
## 8	T	T	T	H	H	0.03125	2
## 9	H	H	H	T	H	0.03125	4
## 10	T	H	H	T	H	0.03125	3
## 11	H	T	H	T	H	0.03125	3
## 12	T	T	H	T	H	0.03125	2
## 13	H	H	T	T	H	0.03125	3
## 14	T	H	T	T	H	0.03125	2
## 15	H	T	T	T	H	0.03125	2
## 16	T	T	T	T	H	0.03125	1
## 17	H	H	H	H	T	0.03125	4
## 18	T	H	H	H	T	0.03125	3
## 19	H	T	H	H	T	0.03125	3
## 20	T	T	H	H	T	0.03125	2
## 21	H	H	T	H	T	0.03125	3
## 22	T	H	T	H	T	0.03125	2
## 23	H	T	T	H	T	0.03125	2
## 24	T	T	T	H	T	0.03125	1
## 25	H	H	H	T	T	0.03125	3
## 26	T	H	H	T	T	0.03125	2
## 27	H	T	H	T	T	0.03125	2
## 28	T	T	H	T	T	0.03125	1
## 29	H	H	T	T	T	0.03125	2
## 30	T	H	T	T	T	0.03125	1
## 31	H	T	T	T	T	0.03125	1
## 32	T	T	T	T	T	0.03125	0

```
event = subset(S, noofheads >= 3) #more heads than tails
Prob(event)
```

```
## [1] 0.5
```

```
#Question-2
#install.packages("gss")
library(gss)
```

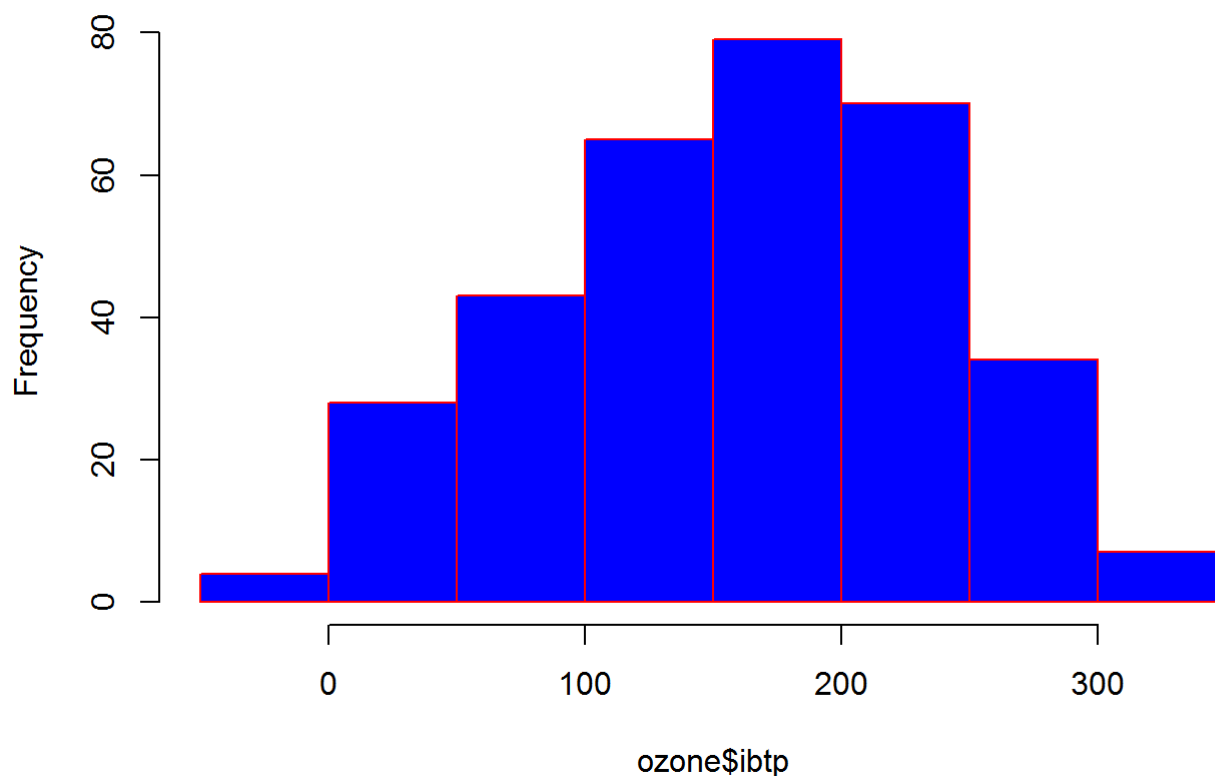
```
## Warning: package 'gss' was built under R version 3.3.2
```

```
data(ozone)
summary(ozone)
```

```
##      upo3      vdht      wdsp      hmdt
## Min.   : 1.00   Min.   :5320   Min.   : 0.000   Min.   :19.00
## 1st Qu.: 5.00   1st Qu.:5690   1st Qu.: 3.000   1st Qu.:47.00
## Median :10.00   Median :5760   Median : 5.000   Median :64.00
## Mean   :11.78   Mean   :5750   Mean   : 4.891   Mean   :58.13
## 3rd Qu.:17.00   3rd Qu.:5830   3rd Qu.: 6.000   3rd Qu.:73.00
## Max.   :38.00   Max.   :5950   Max.   :21.000   Max.   :93.00
##      sbtp      ibht      dgpg      ibtp
## Min.   :25.00   Min.   : 111.0   Min.   : -69.00   Min.   : -25.0
## 1st Qu.:51.00   1st Qu.: 877.5   1st Qu.: -9.00    1st Qu.:107.0
## Median :62.00   Median :2112.5   Median : 24.00    Median :167.5
## Mean   :61.75   Mean   :2572.9   Mean   : 17.37    Mean   :161.2
## 3rd Qu.:72.00   3rd Qu.:5000.0   3rd Qu.: 44.75    3rd Qu.:214.0
## Max.   :93.00   Max.   :5000.0   Max.   :107.00    Max.   :332.0
##      vsty      day
## Min.   : 0.0    Min.   : 3.00
## 1st Qu.: 70.0    1st Qu.: 90.25
## Median :120.0    Median :177.50
## Mean   :124.5    Mean   :181.73
## 3rd Qu.:150.0    3rd Qu.:275.75
## Max.   :350.0    Max.   :365.00
```

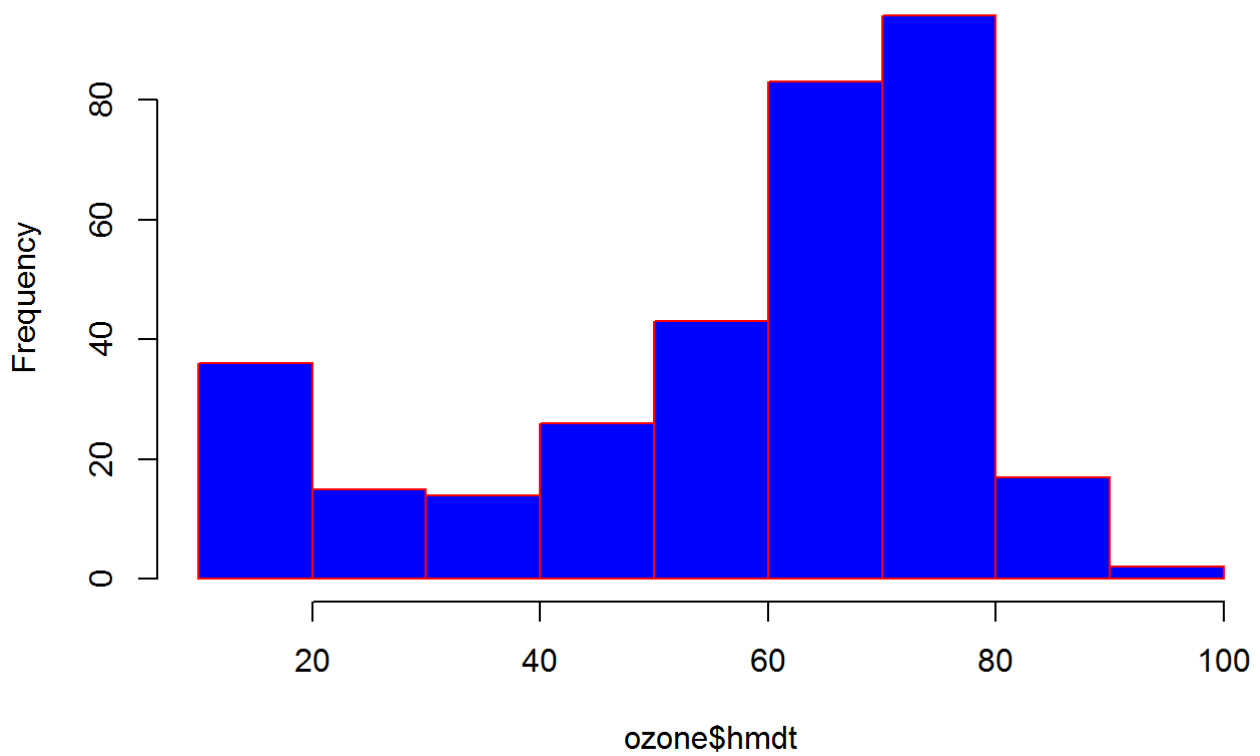
```
hist(ozone$ibtp,main = "Histogram of Inversion Base Temperature",border = "red",col = "blue")
```

Histogram of Inversion Base Temperature



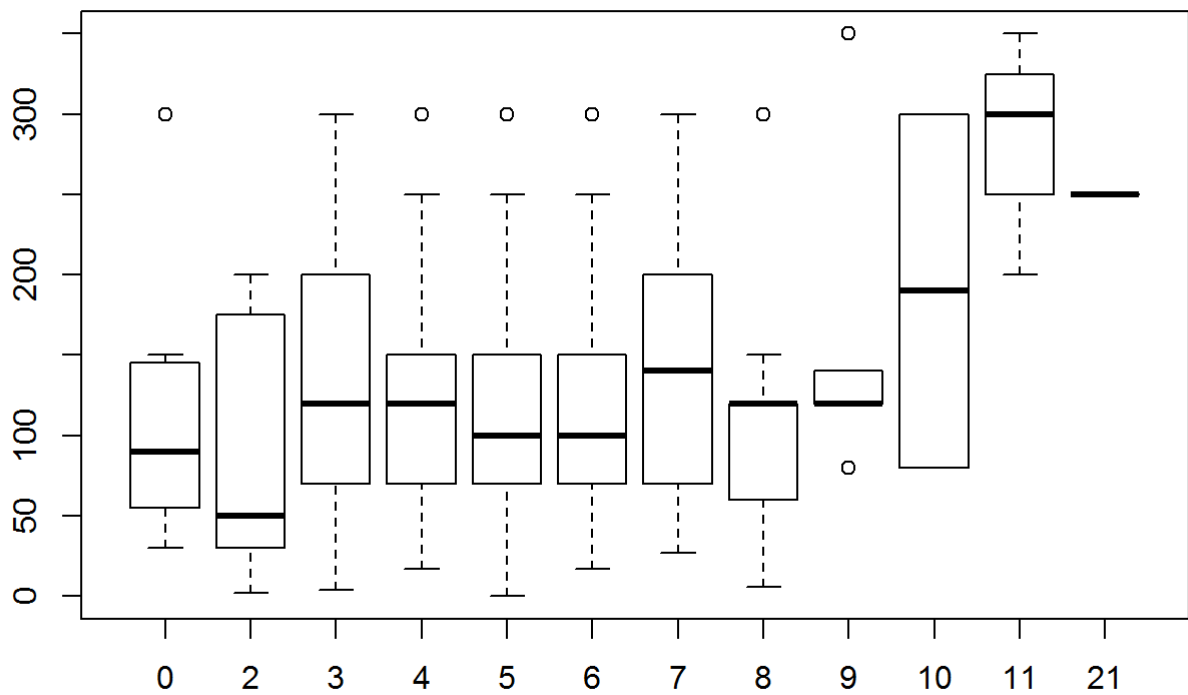
```
hist(ozone$hmdt,main = "Histogram of Humidity",border = "red",col = "blue")
```

Histogram of Humidity

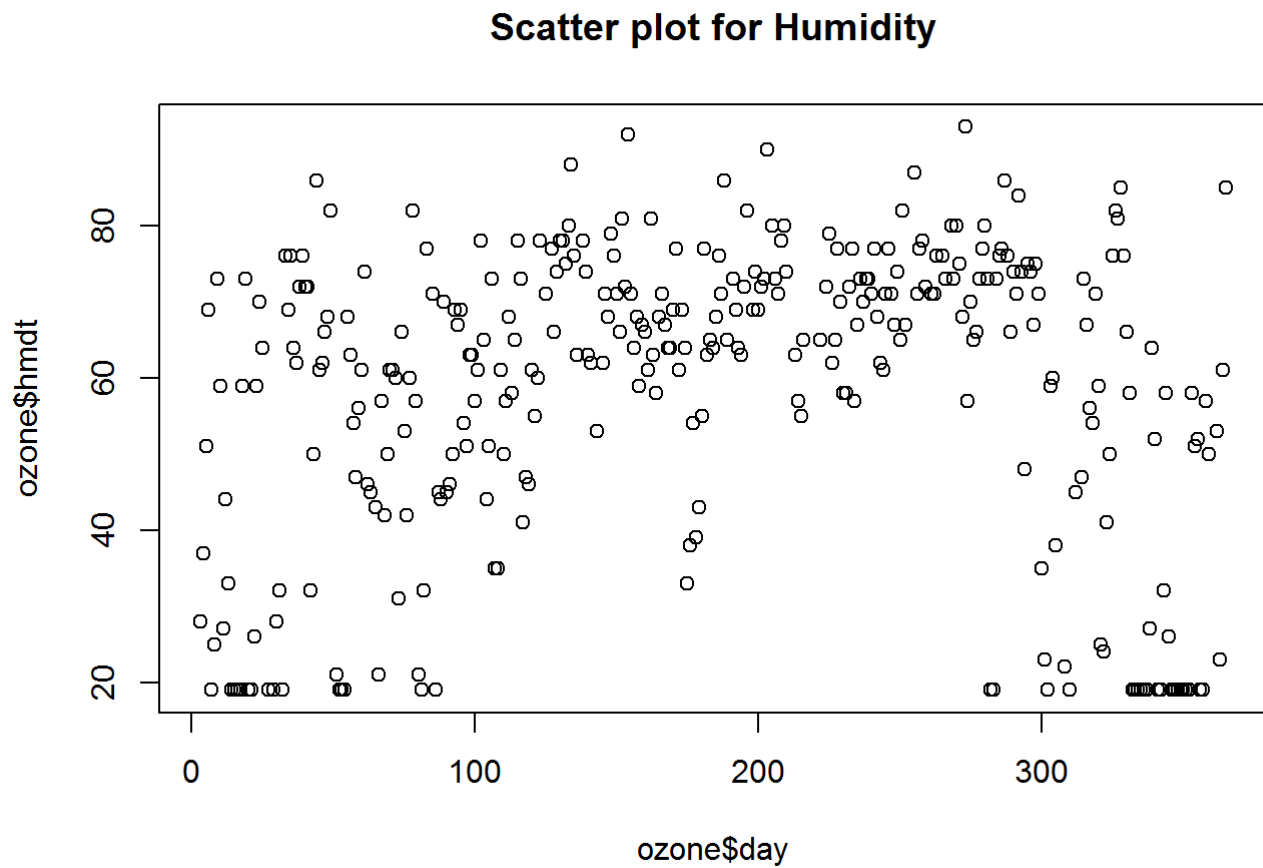


```
boxplot(ozone$vsty ~ ozone$wdsp, main="BoxPlot")
```

BoxPlot

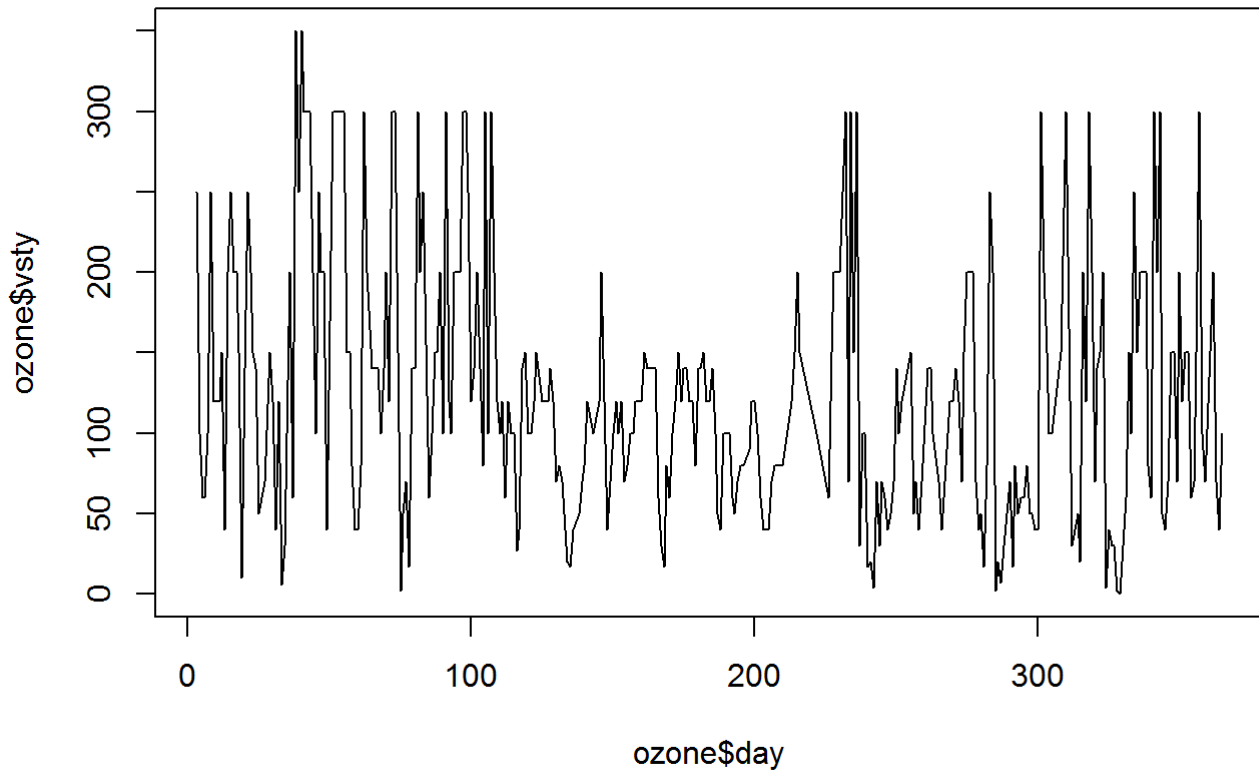


```
plot(x=ozone$day,y=ozone$hmdt, main = "Scatter plot for Humidity")
```



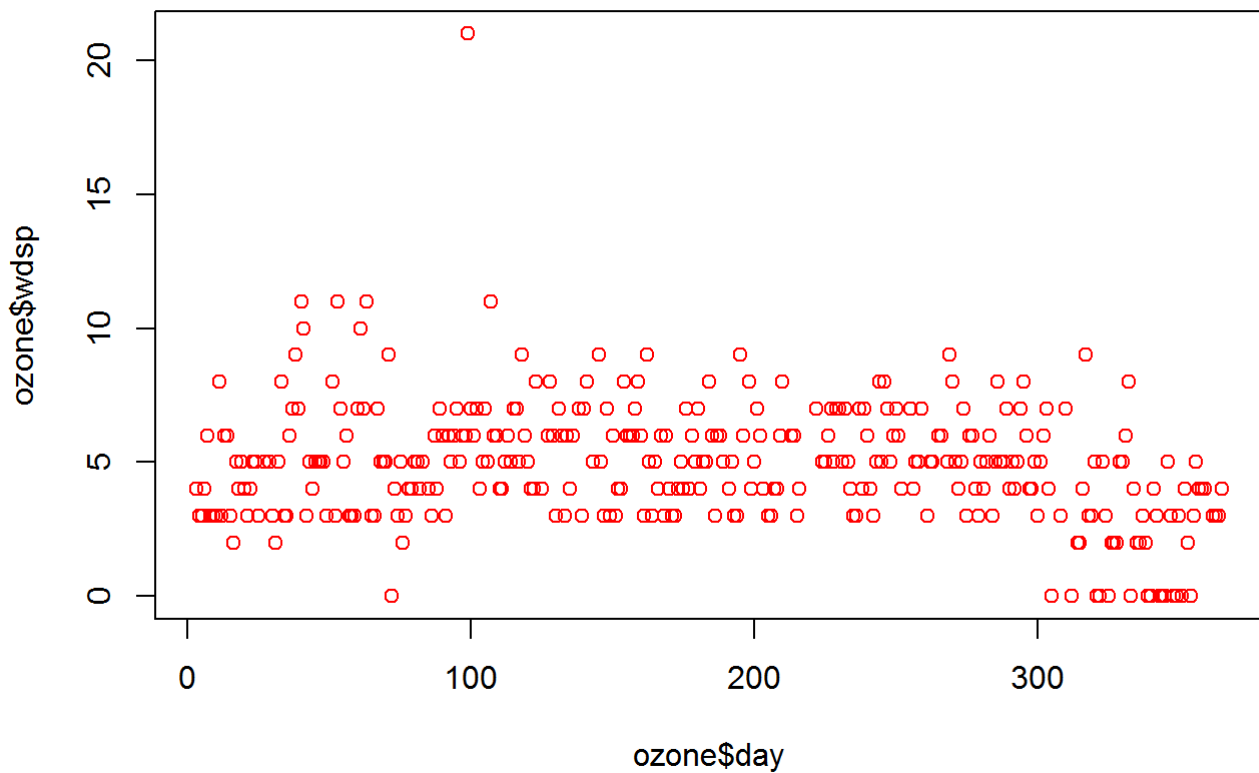
```
plot(x=ozone$day,y=ozone$dsty, main = "Scatter plot for Visibility", "l")
```

Scatter plot for Visibility



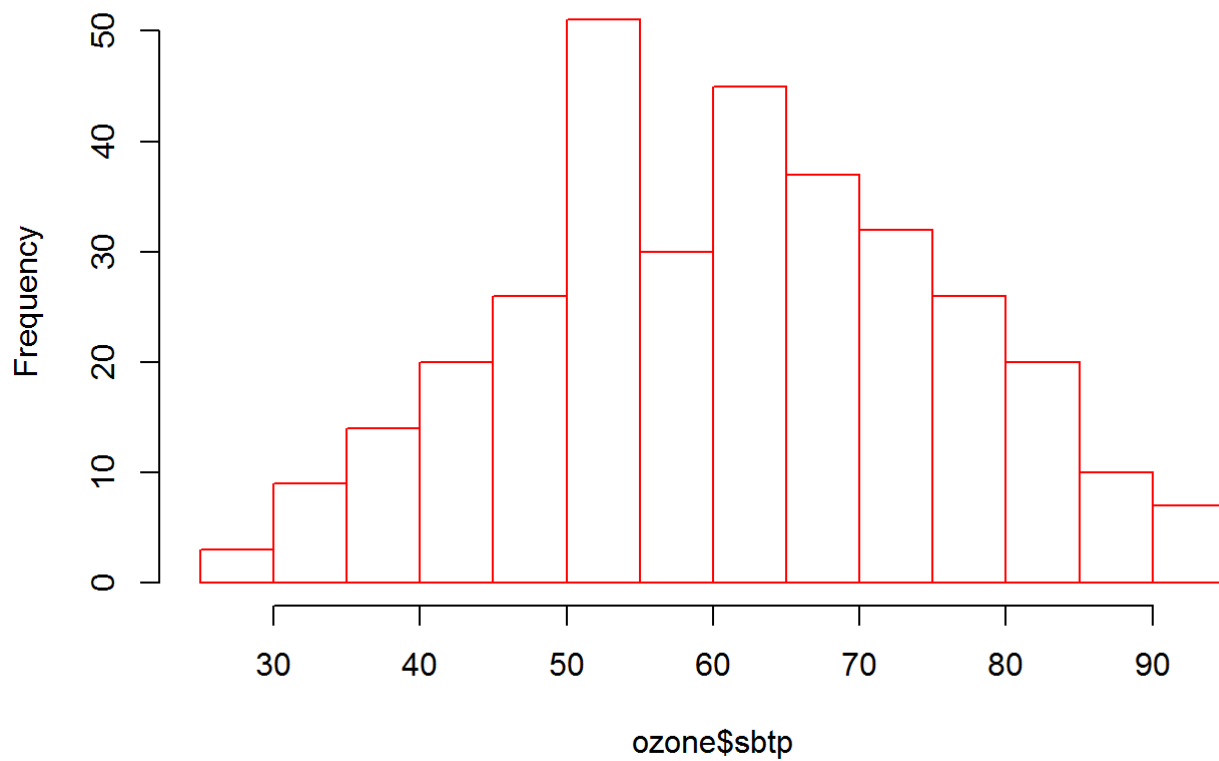
```
plot(x=ozone$day,y=ozone$wdsp, main = "Scatter plot for Wind Speed", col="Red")
```

Scatter plot for Wind Speed



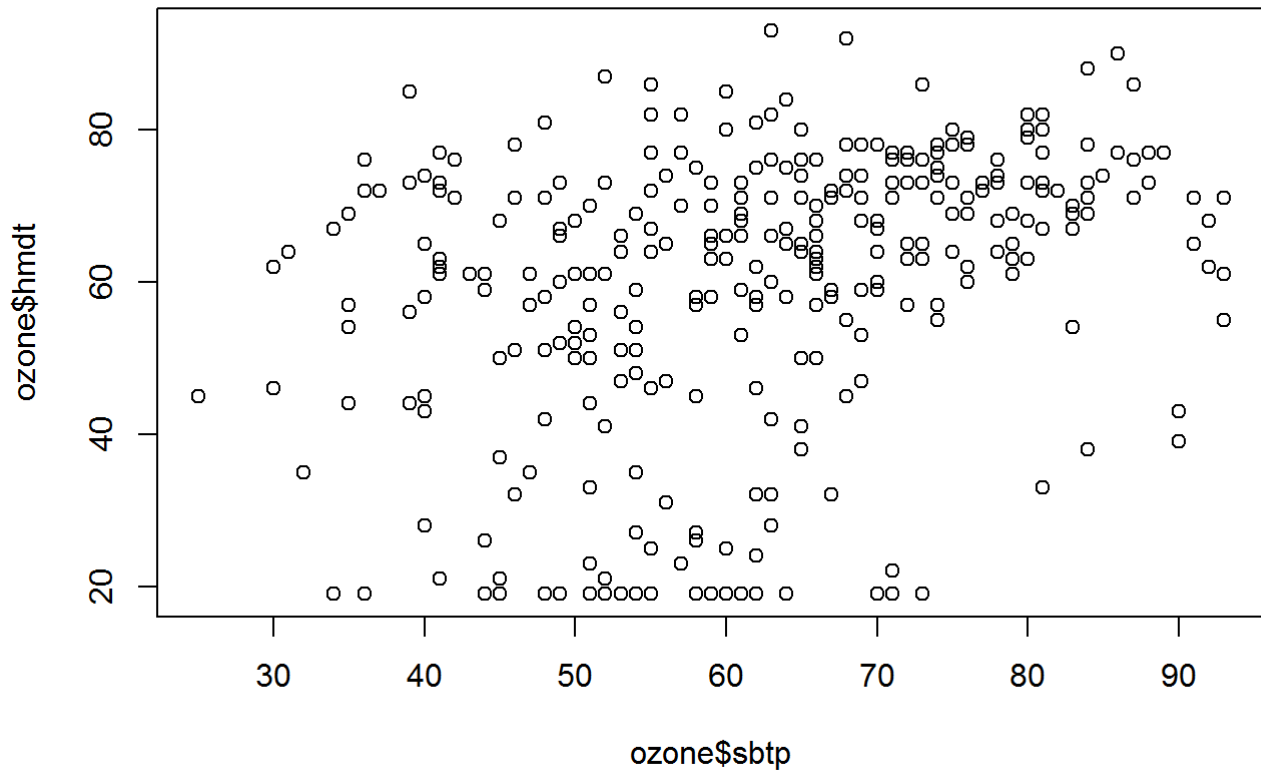

```
#humidity and sandburg airbase temperature  
hist(ozone$sbtp, main="Histogram for Sandburg airbase temperature", border="red")
```

Histogram for Sandburg airbase temperature



```
plot(x=ozone$sbtp,y=ozone$hmdt, main = "Scatter plot for Humidity and Sandburg Airbase Temp")
```

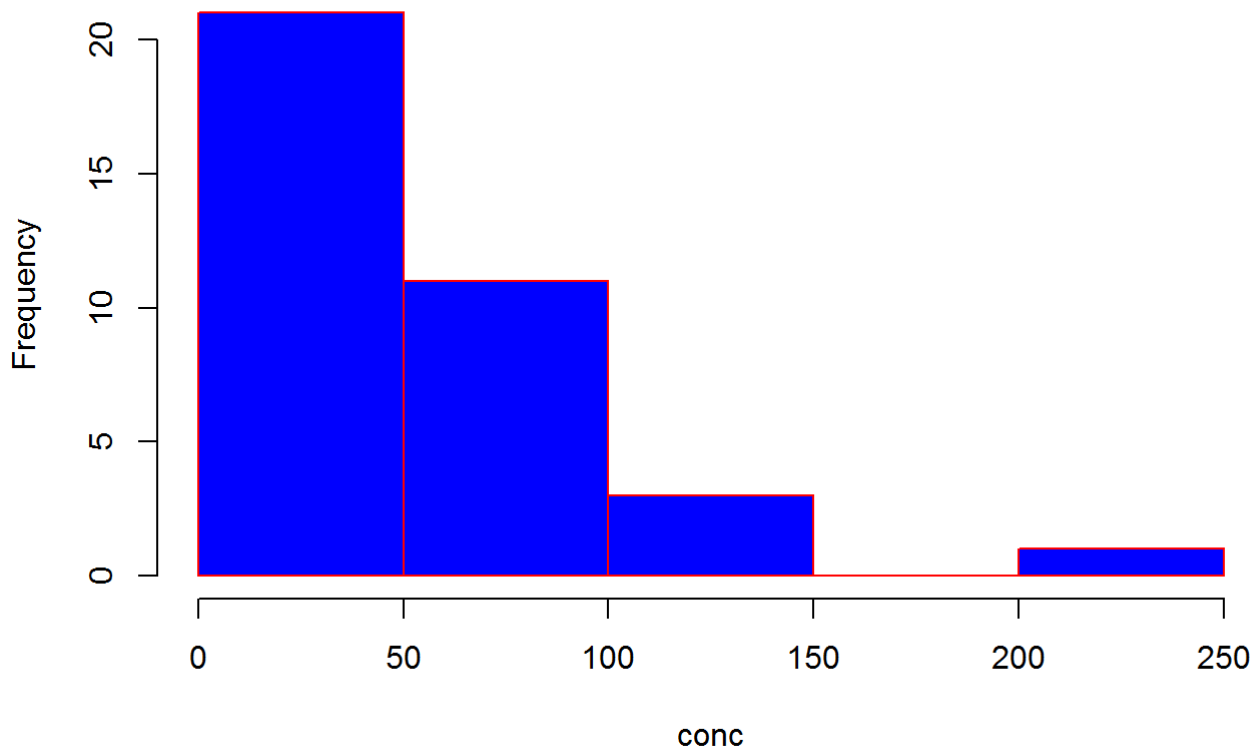
Scatter plot for Humidity and Sandburg Airbase Temp



#Question-3

```
conc <- c( 5, 18, 15, 7, 23, 220, 130, 85, 103, 25, 80, 7, 24, 6, 13, 65, 37, 25,24, 65, 82,
95, 77, 15, 70, 110, 44, 28, 33, 81, 29, 14, 45, 92, 17, 53)
hist(conc, main="Histogram for average particulate concentration", border="red", col="blue")
```

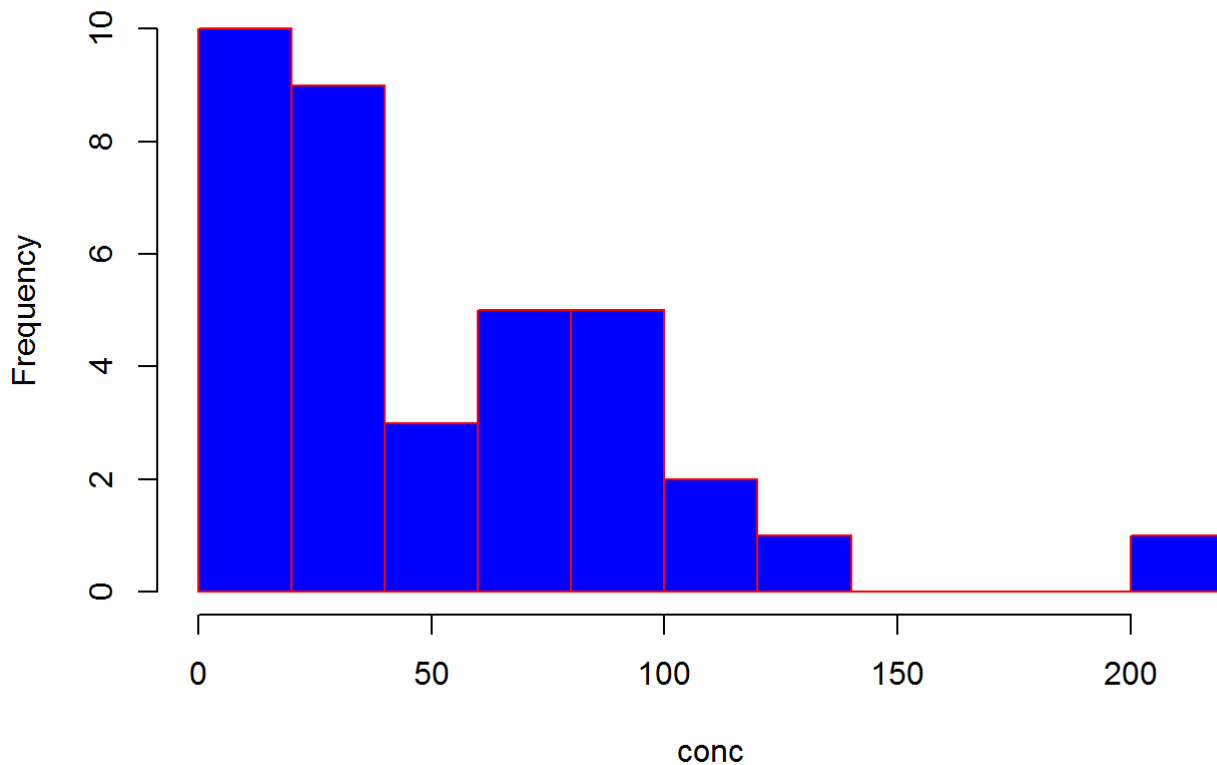
Histogram for average particulate concentration



#From the below graph, we can see that histogram is approximately normal

```
hist(conc, main="Histogram for average particulate concentration", border="red", col="blue",  
breaks = 10)
```

Histogram for average particulate concentration



#Question-4

#Label 1-5:defective, 6-15:partially defective, 16-40:Acceptable transistors

```
S = urnsamples(1:40, size=1)
```

```
p = rep(1, times=nrow(S))
```

```
S = probspace(S, probs = p) #equally likely
```

```
#EventA : does not fail immediately
```

```
A = subset(S, out>5)
```

```
#EventB : acceptable
```

```
B = subset(S, out>15)
```

```
Prob(B, given = A) #Answer
```

```
## [1] 0.7142857
```

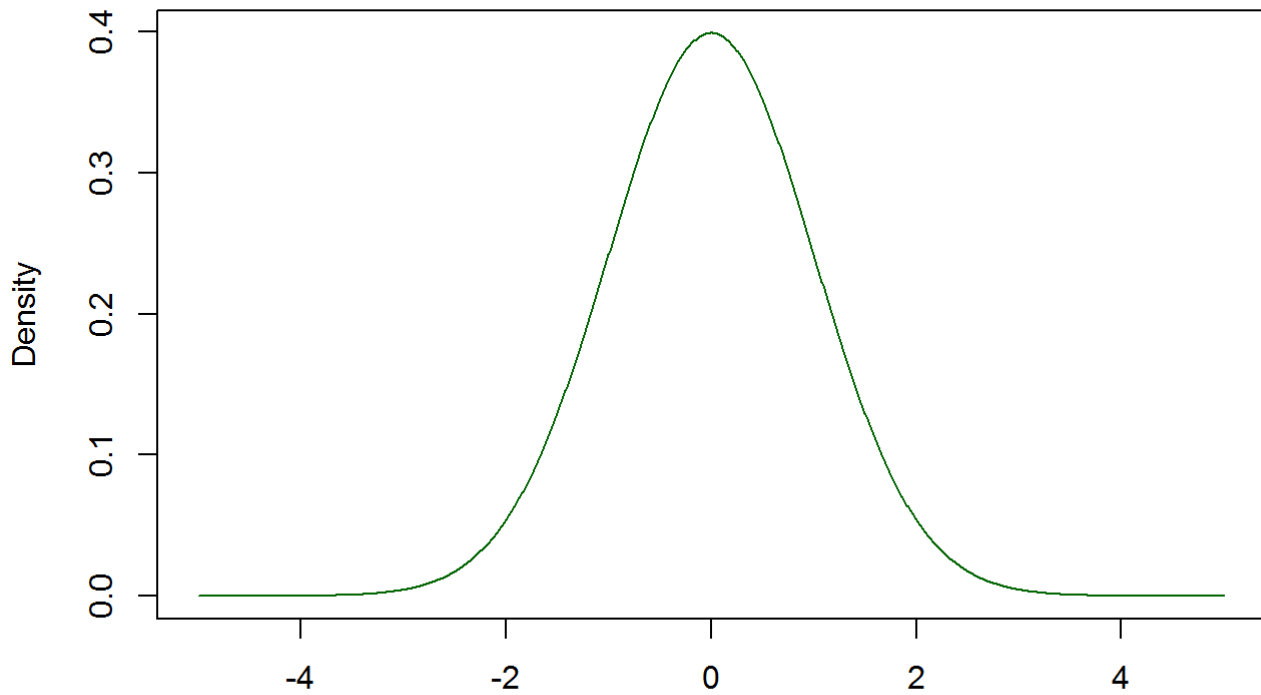
#Question-5

```
x <-seq(-5,5,.01)
```

```
densities <-dnorm(x, 0,1) #density calculation
```

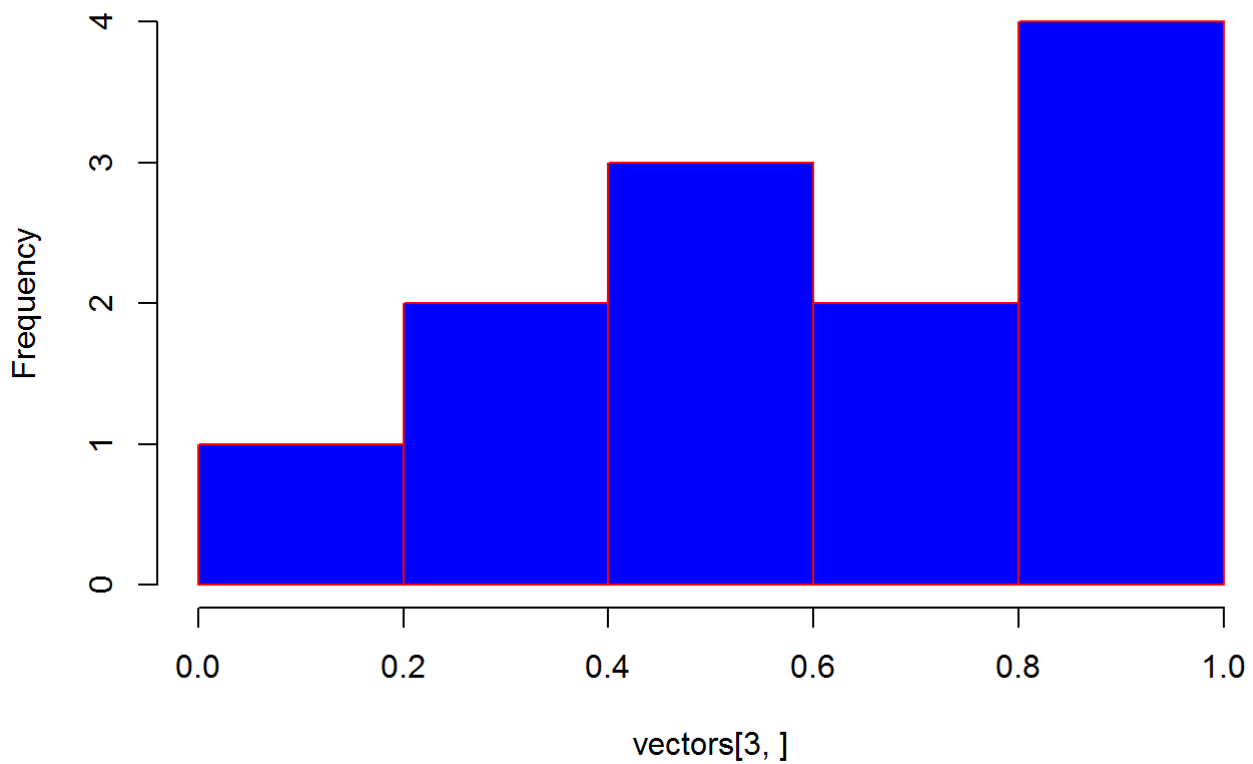
```
plot(x, densities, col="darkgreen",xlab="", ylab="Density", type="l", main="PDF of Standard Normal") #Plot
```

PDF of Standard Normal



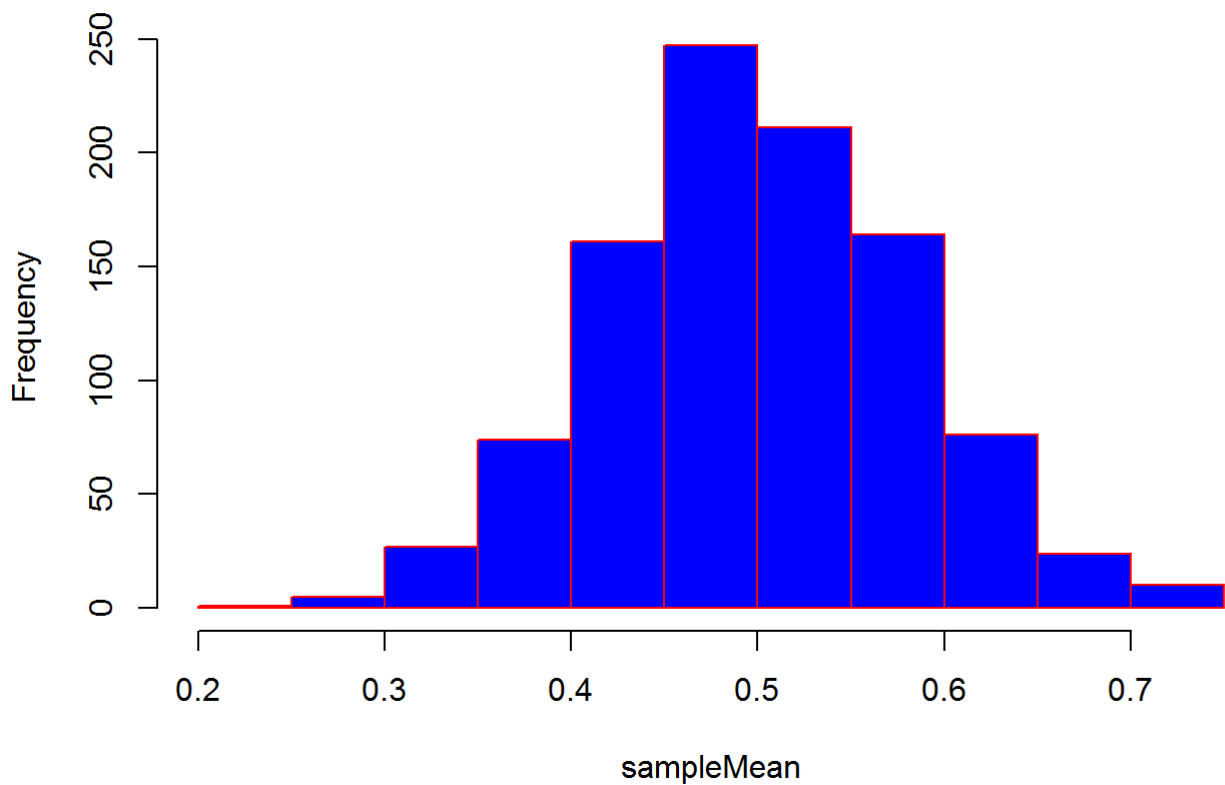
```
#Question-6
set.seed(100)
#Part1(Uniform Law)
vectors <- matrix(ncol = 12, nrow = 1000)
for(i in 1:1000){
  vec = runif(12,0,1)
  vectors[i,]=vec
}
hist(vectors[3,],main = "Histogram of generated values",border = "red",col = "blue") #hist of
generated values
```

Histogram of generated values



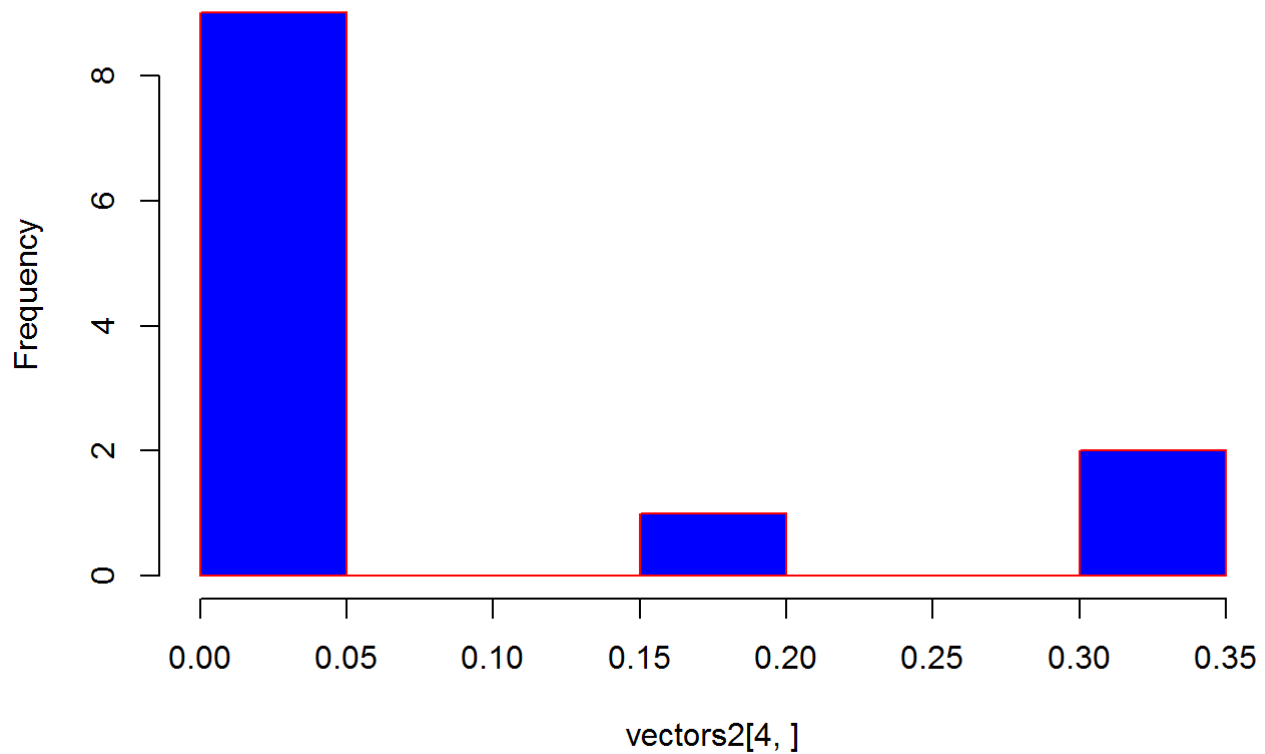
```
sampleMean = apply(vectors,1,mean)
hist(sampleMean,main = "Histogram of Sample Mean",border = "red",col = "blue")
```

Histogram of Sample Mean



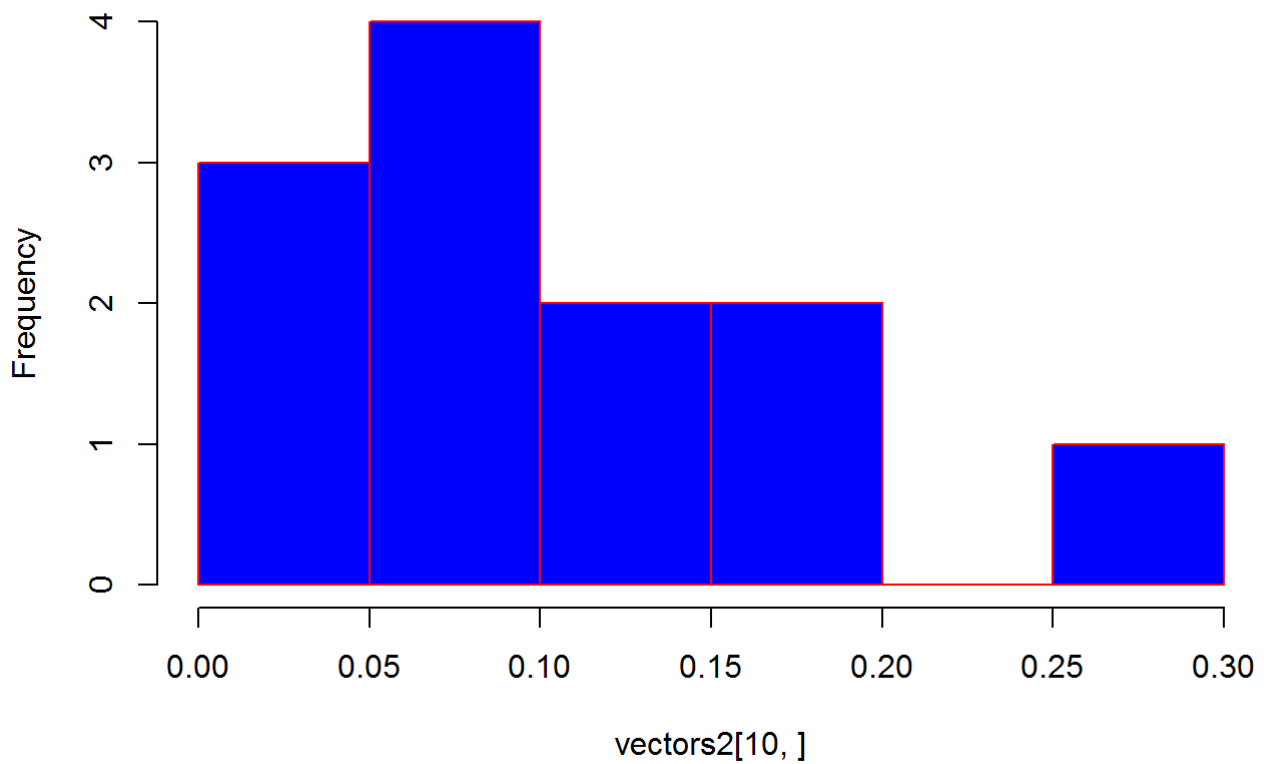
```
#Part-2(Exponential Law)
vectors2 <- matrix(ncol = 12, nrow = 1000)
for(i in 1:1000){
  vec = rexp(12,10)
  vectors2[i,]=vec
}
hist(vectors2[4,],main = "Histogram of generated values",border = "red",col = "blue")
```

Histogram of generated values



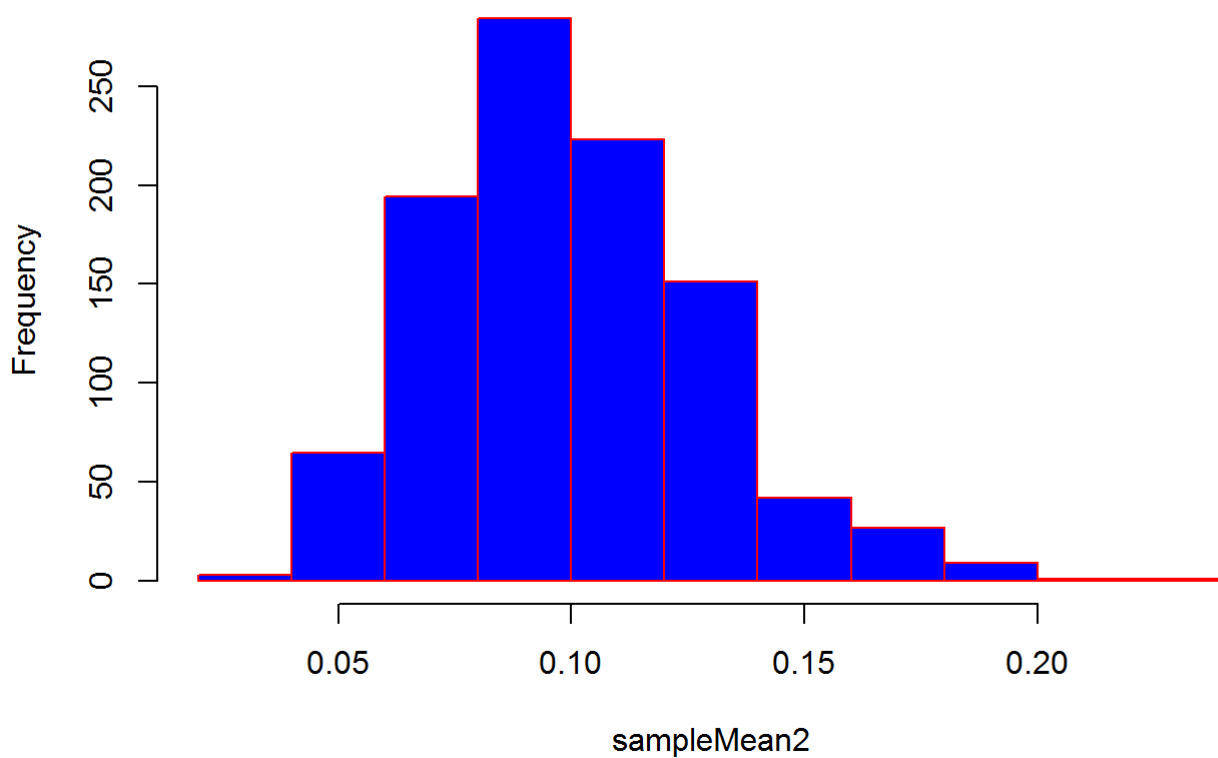
```
hist(vectors2[10,],main = "Histogram of generated values",border = "red",col = "blue")
```

Histogram of generated values



```
sampleMean2 = apply(vectors2,1,mean)
hist(sampleMean2,main = "Histogram of Sample Mean",border = "red",col = "blue")
```

Histogram of Sample Mean



##Exercise Problems from Lab session-3

#Exercise-1

```
S = rolldie(2, makespace = TRUE)
```

```
S
```

```
##      X1 X2      probs
## 1     1  1 0.02777778
## 2     2  1 0.02777778
## 3     3  1 0.02777778
## 4     4  1 0.02777778
## 5     5  1 0.02777778
## 6     6  1 0.02777778
## 7     1  2 0.02777778
## 8     2  2 0.02777778
## 9     3  2 0.02777778
## 10    4  2 0.02777778
## 11    5  2 0.02777778
## 12    6  2 0.02777778
## 13    1  3 0.02777778
## 14    2  3 0.02777778
## 15    3  3 0.02777778
## 16    4  3 0.02777778
## 17    5  3 0.02777778
## 18    6  3 0.02777778
## 19    1  4 0.02777778
## 20    2  4 0.02777778
## 21    3  4 0.02777778
## 22    4  4 0.02777778
## 23    5  4 0.02777778
## 24    6  4 0.02777778
## 25    1  5 0.02777778
## 26    2  5 0.02777778
## 27    3  5 0.02777778
## 28    4  5 0.02777778
## 29    5  5 0.02777778
## 30    6  5 0.02777778
## 31    1  6 0.02777778
## 32    2  6 0.02777778
## 33    3  6 0.02777778
## 34    4  6 0.02777778
## 35    5  6 0.02777778
## 36    6  6 0.02777778
```

```
A = subset(S, X1 == X2) #outcomes match
```

```
A
```

```
##      X1 X2      probs
## 1     1  1 0.02777778
## 8     2  2 0.02777778
## 15    3  3 0.02777778
## 22    4  4 0.02777778
## 29    5  5 0.02777778
## 36    6  6 0.02777778
```

```
B = subset(S, X1 + X2 >= 8) #sum of outcomes atleast 8  
B
```

```
##      X1 X2      probs  
## 12   6  2 0.02777778  
## 17   5  3 0.02777778  
## 18   6  3 0.02777778  
## 22   4  4 0.02777778  
## 23   5  4 0.02777778  
## 24   6  4 0.02777778  
## 27   3  5 0.02777778  
## 28   4  5 0.02777778  
## 29   5  5 0.02777778  
## 30   6  5 0.02777778  
## 32   2  6 0.02777778  
## 33   3  6 0.02777778  
## 34   4  6 0.02777778  
## 35   5  6 0.02777778  
## 36   6  6 0.02777778
```

```
Prob(A, given = B)
```

```
## [1] 0.2
```

```
Prob(B, given = A)
```

```
## [1] 0.5
```

```
#Exercise-2  
x1 = c("A", 2:10, "J", "Q", "K")  
x1
```

```
## [1] "A" "2" "3" "4" "5" "6" "7" "8" "9" "10" "J" "Q" "K"
```

```
x1 = rep(x1, 4) #as we have 4 suits  
S = urnsamples(x1, size=2, replace = FALSE, ordered = TRUE)  
p = rep(1, times=nrow(S))  
S = probspace(S, probs = p) #equally likely  
A = subset(S, X1=="A")  
B = subset(S, X2=="A")  
S2 = subset(S, X1=="A"& X2=="A") #both aces  
Prob(S2)
```

```
## [1] 0.004524887
```

#Exercise-3

#Label balls 1-7: Red, balls 8-10: Green

```
S = urnsamples(1:10, size=3, replace=FALSE, ordered=TRUE)
```

```
p = rep(1, times=nrow(S))
```

```
S = probspace(S, probs = p) #equally likely
```

```
A= subset(S, X1<8 & X2<8 & X3<8) #all 3 balls are red
```

```
Prob(A)
```

```
## [1] 0.2916667
```

```
B= subset(S, X1<8 & X2<8 & X3>7 | X1<8 & X2>7 & X3<8 | X1>7 & X2<8 & X3<8) #2 balls are red  
Prob(B)
```

```
## [1] 0.525
```

#Exercise-4

```
S = tosscoin(10, makespace = TRUE)
```

#We will find probability of no head and then subtract it from 1

```
nohead = S
```

```
for(i in 1:10){
```

```
  nohead = subset(nohead, nohead[,i]=="T")
```

```
}
```

```
ans = 1-Prob(nohead)
```

```
ans
```

```
## [1] 0.9990234
```