

Exercise (Almost regular hash function as pseudorandom generator). Let $h : \mathcal{X} \rightarrow \mathcal{Y}$ be an almost regular hash function, i.e. the distribution $h(x)$ for $x \leftarrow_{\mathcal{U}} \mathcal{X}$ is statistically ε -close to the uniform distribution over the set $h(\mathcal{X})$. Show that h is a pseudorandom generator provided that $|h(\mathcal{X})| \approx \mathcal{Y}$. Analyse how the distinguishing advantage depends on $|h(\mathcal{X})|$.

Solution.