

**Exercise (Signatures  $\Rightarrow$  Entity authentication).** Let  $(\text{Gen}, \text{Sign}, \text{Ver})$  be a signature scheme that is  $(t, \varepsilon)$ -secure against universal one-more signature attack where the message distribution is uniform distribution over the message space  $\mathcal{M}$ . Prove that the entity authentication protocol where the verifier  $\mathcal{V}$  chooses  $m \xleftarrow{u} \mathcal{M}$  and the prover sends back the signature  $s \leftarrow \text{Sign}_{\text{sk}}(m)$  there can be no black-box knowledge extractors for the secret key that is also efficient.

**Solution.** Let  $\mathcal{K}^{\mathcal{P}^*}$  be a black-box knowledge extractor algorithm that succeeds in time  $t_2$  and with probability  $\varepsilon_2$  for all provers  $\mathcal{P}_*$  that run in time  $t_1$  and are at least  $\varepsilon_1$  successful. Then we can construct an adversary  $\mathcal{B}$  can conduct successful one-more signature attacks....