

Exercise (Security of encrypt-and-sign). Consider a following message transmission protocol. A sender \mathcal{P}_1 knows the public encryption key pk_2 of a receiver \mathcal{P}_2 and the receiver \mathcal{P}_2 knows the public signing key pk_1 of the sender \mathcal{P}_1 . To encrypt a message m the sender sk computes $c \leftarrow \text{Enc}_{\text{pk}_2}(m)$, $s \leftarrow \text{Sign}_{\text{sk}_1}(c)$ and sends (c, s) over unreliable channel to \mathcal{P}_2 . The receiver \mathcal{P}_2 first checks the authenticity by computing $\text{Ver}_{\text{pk}_1}(c, s)$ and then decrypts the message $m \leftarrow \text{Dec}_{\text{sk}_2}(c)$. Prove that the protocol remains secure even if the adversary gets oracle access to the receiver, i.e., it can send any tuples c, s and obtain the corresponding decryption.

Solution. Let us first formalise two games that are analog of IND-CCA2 security games... Next let us prove that the decryption queries will yield $m \neq \perp$ with small enough probability Based on this let us define trivial decryption oracle and reduce the security to IND-CPA games...