

Exercise (Asymmetric encryption as commitment). *Show that an asymmetric IND-CPA secure cryptosystem $\mathfrak{E} = (\text{Gen}, \text{Enc}, \text{Dec})$ with perfect decryption can be converted to perfectly binding and computationally binding commitment by using the following construction:*

Gen^*	$\text{Com}_{\text{pk}}(m)$	$\text{Open}_{\text{pk}}(c, m, r)$
$\left[\begin{array}{l} (\text{pk}, \text{sk}) \leftarrow \text{Gen} \\ \textbf{return} \text{ pk} \end{array} \right.$	$\left[\begin{array}{l} r \leftarrow \mathcal{R} \\ c \leftarrow \text{Enc}_{\text{pk}}(m; r) \\ \textbf{return} (c, (m, r)) \end{array} \right.$	$\left[\begin{array}{l} \hat{c} \leftarrow \text{Enc}_{\text{pk}}(m; r) \\ \text{if } c = \hat{c} \textbf{return} m \\ \text{else } \textbf{return} \perp . \end{array} \right.$

Solution.