

Computational Social Science

Data structures

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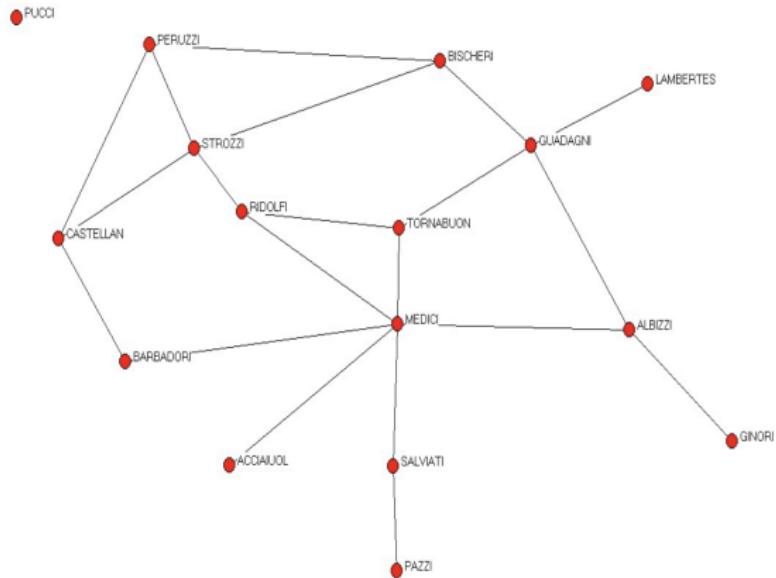
Rutgers University

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Plan

- ▶ Introductions
- ▶ Part I : Social networks and social network analysis
- ▶ Part II : Data structures in R

Part I: Social networks and social network analysis



Social networks

- ▶ A social network is a set of actors, or people, and the relationships between them
 - ▶ Family structures and kinship networks
 - ▶ Friendship and acquaintanceship networks
 - ▶ Organizations
 - ▶ Online social networks

Social network analysis

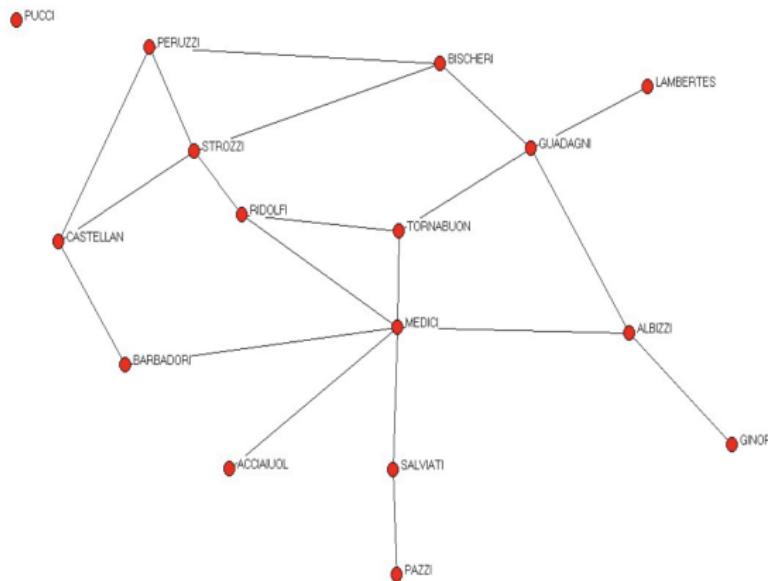
- ▶ Social network analysis is the study of social networks using mathematical and computational tools
- ▶ Networks can be represented using concepts from a branch of mathematics called graph theory
 - ▶ People or actors are represented as “nodes”
 - ▶ Relationships are represented as “edges”

Social network analysis

- ▶ Social scientists use these representations to study the structure and dynamics of social networks
 - ▶ What does the network look like?
 - ▶ What are the patterns of connectivity?
 - ▶ How does information flow through the network?
 - ▶ How does the network change over time?

Social network analysis

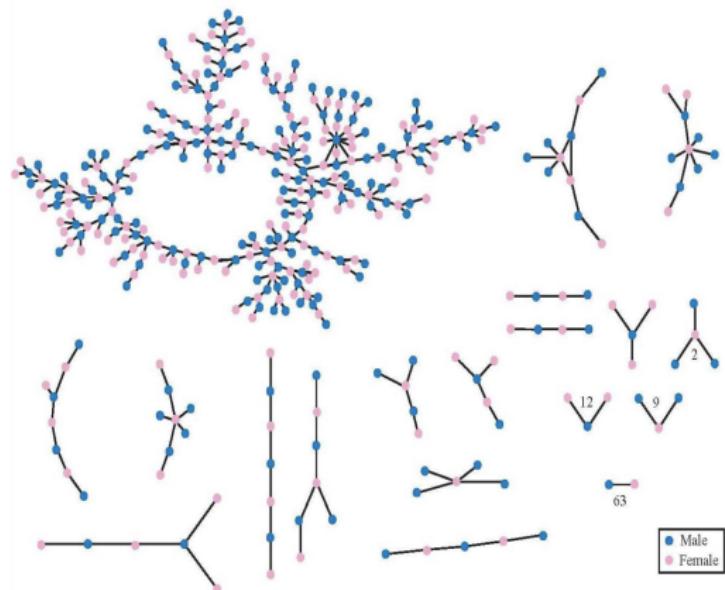
Visualizing networks: Marriages



15th century Florentine marriage network (depicted in Jackson 2008)

Social network analysis

Visualizing networks: Romantic encounters



Six months of relationships in an American high-school, nodes colored by sex (depicted in Jackson 2008)

Social network analysis

Visualizing networks: Friendships

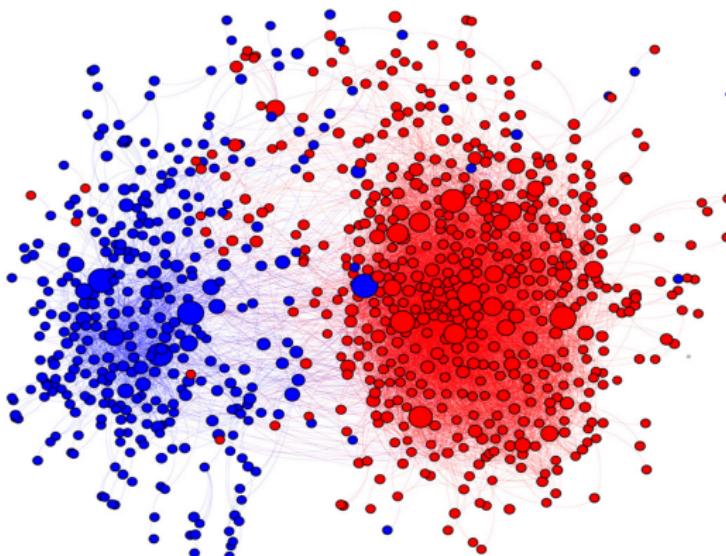


Six months of friendships in an American high-school, nodes colored by race/ethnicity (depicted in Jackson 2008)

Social network analysis

Visualizing networks: Book co-purchases

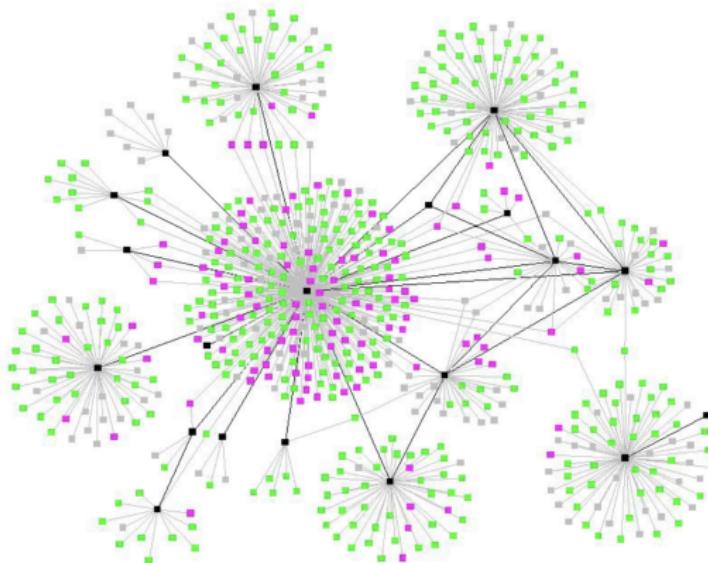
a



Book co-purchases on Amazon, nodes colored by ideology (depicted in Jackson 2008)

Social network analysis

Visualizing networks: Disease transmission



Spread of tuberculosis in a social network, nodes colored by transmission status (depicted in Easley and Kleinberg 2010)

Social network analysis

Visualizing networks: Game of Thrones

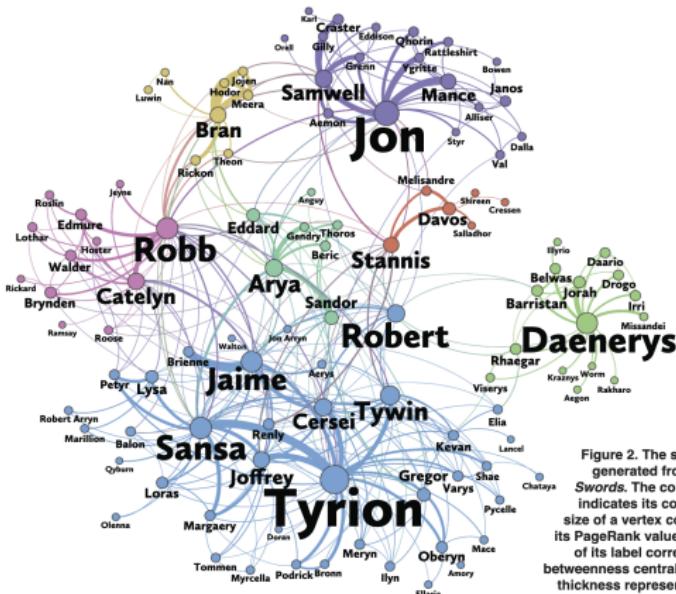


Figure 2. The social network generated from *A Storm of Swords*. The color of a vertex indicates its community. The size of a vertex corresponds to its PageRank value, and the size of its label corresponds to its betweenness centrality. An edge's thickness represents its weight.

Characters mentioned in *Game of Thrones* series, annotated with structural information (Beveridge and Shan 2010)

Part II: Data structures

Open RStudio and load `lecture2-data-structures.Rmd`, located in this week's Canvas Module.

Basic types

There are four basic types we will be using throughout the class. Here I used them to record some information about one of my cats. In R, it is convention to use the `<-` operator to assign an object to a name.

```
# Character (also known as "strings")
name <- "Gary"
# Numeric
weight <- 14.5
# Integer ("int" for short)
age <- 8L
# Logical
human <- FALSE
```

The other two are called `complex` and `raw`. See [documentation](#)

Basic types

There are a few useful commands for inspecting objects.

```
print(name) # Prints value in console
```

```
## [1] "Gary"
```

```
class(name) # Shows class of object
```

```
## [1] "character"
```

```
typeof(name) # Shows type of object, not always equal to class
```

```
## [1] "character"
```

Basic types

```
print(weight) # Prints value in console  
## [1] 14.5  
class(weight) # Shows class of object  
## [1] "numeric"  
typeof(weight) # Shows type of object, not always equal to class  
## [1] "double"
```

Basic types

We can use the `==` expression to verify the value of an object. We will discuss Boolean operations in more detail next lecture.

```
name == "Tabitha"
```

```
## [1] FALSE
```

```
age == 5L
```

```
## [1] FALSE
```

```
age >= 5L # is greater than
```

```
## [1] TRUE
```

```
age != 5L # is not
```

```
## [1] TRUE
```

Vectors

A vector is a collection of elements of the *same* type. We can define an empty vector with N elements of a type. Empty vectors assume certain default values depending on the type.

```
N <- 5  
x <- logical(N)  
print(x)
```

```
## [1] FALSE FALSE FALSE FALSE FALSE
```

```
y <- numeric(N)  
print(y)
```

```
## [1] 0 0 0 0 0
```

```
z <- character(N)  
print(z)
```

```
## [1] "" "" "" "" "" "
```

Vectors

Let's take a closer look at numeric vectors. We can use the combine function `c()` to concatenate multiple values into a vector.

```
v1 <- c(1,2,3,4,5)
v2 <- c(1,1,1,1,1)
class(v1) # check the class of v1

## [1] "numeric"
```

Vectors

We can easily perform various mathematical operations on numeric vectors

```
v1 + v2 # addition  
  
## [1] 2 3 4 5 6  
v1 - v2 # subtraction  
  
## [1] 0 1 2 3 4  
v1 * v2 # multiplication  
  
## [1] 1 2 3 4 5  
sum(v1) # sum over v1  
  
## [1] 15
```

Note how the different methods return different types of outputs. The arithmetic operations return vectors while `sum` returns a numeric value.

Vectors

What happens if we try to combine objects of different types using `combine`?

```
t <- c("a", 1, TRUE)
typeof(t)

## [1] "character"

t

## [1] "a"      "1"      "TRUE"
```

Vectors

There are lots of commands for generating special types of numeric vectors. Note how N has already been defined above.

```
seq(N) # generates a sequence from 1 to N
```

```
## [1] 1 2 3 4 5
```

```
rev(seq(N)) # reverses order
```

```
## [1] 5 4 3 2 1
```

```
rnorm(N) # samples N times from a normal distribution
```

```
## [1] -0.3009134 2.1994381 1.0805581 0.6802231 0.5983998
```

Vectors

We can use the help ? command to find information about each of these commands.

```
?seq
```

Vectors

We can use the index to access the specific elements of a vector. R uses square brackets for such indexing.

```
x <- rnorm(N)
```

```
print(x)
```

```
## [1] 1.8605945 -0.4196972 0.5123306 -0.3224507 0.7091184
```

```
print(x[1]) # R indexing starts at 1; Python and some others start at 0
```

```
## [1] 1.860594
```

```
x[1] <- 9 # We can combine indexing with assignment to modify elements
print(x)
```

```
## [1] 9.0000000 -0.4196972 0.5123306 -0.3224507 0.7091184
```

Vectors

The `head` and `tail` commands are useful when we're working with larger objects. Here we draw 10,000 observations from a normal distribution.

```
x <- rnorm(10000)
length(x)

## [1] 10000

head(x)

## [1] 1.0737876 0.3696161 -0.8709373 0.4168874 0.8907456 -1.133475

tail(x)

## [1] 0.1422095 -0.3611873 -0.5840297 -0.4308788 0.8762066 0.710140
```

Excercise: Vectors

Retrieve the final element from `x` using indexing.

Vectors

Vectors can also contain null elements to indicate missing values, represented by the NA symbol.

```
x <- c(1,2,3,4,NA)
is.na(x) # The is.na function indicates whether each value is missing.

## [1] FALSE FALSE FALSE FALSE  TRUE
!is.na(x) # Prepending ! denotes the inverse of a logical operation

## [1]  TRUE  TRUE  TRUE  TRUE FALSE
```

NA is a logical type but can exist within numeric and character vectors. It is an exception to the rule discussed above regarding the presence of multiple types in the same vector.

Lists

A list is an object that can contain different types of elements, including basic types and vectors.

```
print(v1)

## [1] 1 2 3 4 5

l1 <- list(v1) # We can easily convert the vector v1 into a list.
print(l1)

## [[1]]
## [1] 1 2 3 4 5
```

Lists

Lists have a slightly different form of indexing. This can be one of the most confusing aspects of R for beginners!

```
11[1] # The first element of the list contains the vector
```

```
## [[1]]
```

```
## [1] 1 2 3 4 5
```

```
11[[1]] # Double brackets allows us to access the vector itself
```

```
## [1] 1 2 3 4 5
```

```
class(11[1]) # first element is a list
```

```
## [1] "list"
```

```
class(11[[1]]) # double indexing gives us the contents
```

```
## [1] "numeric"
```

Lists

We can access specific elements of a list by using standard indexing.

```
11[[1]][1] # Followed by single brackets to access a specific element  
  
## [1] 1  
11[1][1] # If we're not careful, we will just get the entire sublist  
  
## [[1]]  
## [1] 1 2 3 4 5
```

Lists

We can easily combine multiple vectors into a list.

```
v.list <- list(v1,v2) # We could store both vectors in a list
print(v.list)

## [[1]]
## [1] 1 2 3 4 5
##
## [[2]]
## [1] 1 1 1 1 1

v.list[[2]][4] # We can use double brackets to get element 4 of list 1

## [1] 1
```

Lists

We index sublists using double brackets, then specific elements with single brackets.

```
v.list[[1]][4] # We can use double brackets to get element 4 of list 1
```

```
## [1] 4
```

Lists

We can make indexing easier if we start with an empty list and then add elements using a named index via the \$ operator.

```
v <- list() # initialize empty list
v$v1 <- v1 # the $ sign is used for named indexing
v$v2 <- v2
print(v)
```

```
## $v1
## [1] 1 2 3 4 5
##
## $v2
## [1] 1 1 1 1 1
```

Excercise: Lists

Combine \$ and square bracket indexing to extract the 5th element of v1 from the list v.

Lists

We can define lists more concisely by providing sublists as named arguments.

```
cats <- list(names = c("Gary", "Tabitha"), ages = c(8,4))
print(cats)
```

```
## $names
## [1] "Gary"      "Tabitha"
##
## $ages
## [1] 8 4
```

Matrices

A matrix is a two-dimensional data structure. Like vectors, matrices hold objects of a single type. Here we're defining a matrix using two arguments, the number of rows and columns.

```
matrix(nrow=5,ncol=5) # Here there is no content so the matrix is empty
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]    NA    NA    NA    NA    NA
## [2,]    NA    NA    NA    NA    NA
## [3,]    NA    NA    NA    NA    NA
## [4,]    NA    NA    NA    NA    NA
## [5,]    NA    NA    NA    NA    NA
```

Matrices

We can also pass an argument to define the initial contents of a matrix.

```
M <- matrix(0L, nrow=5, ncol=5) # 5x5 matrix of zeros
```

```
M
```

```
##      [,1] [,2] [,3] [,4] [,5]
## [1,]     0     0     0     0     0
## [2,]     0     0     0     0     0
## [3,]     0     0     0     0     0
## [4,]     0     0     0     0     0
## [5,]     0     0     0     0     0
```

Matrices

We can create a matrix by combining vectors using `cbind`.

```
M1 <- cbind(v1,v2) # Treat vectors as columns  
print(M1)
```

```
##          v1 v2  
## [1,]    1  1  
## [2,]    2  1  
## [3,]    3  1  
## [4,]    4  1  
## [5,]    5  1
```

Matrices

If we want to treat the vectors as rows, we alternatively use rbind.
We could also get the same result by *transposing* M1.

```
M2 <- rbind(v1, v2) # Vectors as rows  
print(M2)
```

```
##      [,1] [,2] [,3] [,4] [,5]  
## v1     1     2     3     4     5  
## v2     1     1     1     1     1  
  
print(t(M1)) # t() is the transpose function
```

```
##      [,1] [,2] [,3] [,4] [,5]  
## v1     1     2     3     4     5  
## v2     1     1     1     1     1
```

Matrices

The `dim` function provides us with information about the dimensions of a given matrix. It returns the number of rows and columns.

```
dim(M1) # Shows the dimensions of the matrix
```

```
## [1] 5 2
```

```
dim(M2)
```

```
## [1] 2 5
```

Matrices

We can get particular values using two-dimensional indexing. By convention i denotes the row and j the column.

```
i <- 1 # row index  
j <- 2 # column index  
M1[i,j] # Returns element i,j
```

```
## v2  
## 1  
M1[i,] # Returns row i
```

```
## v1 v2  
## 1 1  
M1[,j] # Returns column i  
  
## [1] 1 1 1 1 1
```

Matrices

Like lists, we can also name rows and columns to help make indexing easier. The `colnames` and `rownames` functions show the names of each column and row.

```
colnames(M1)
```

```
## [1] "v1" "v2"
```

```
rownames(M1)
```

```
## NULL
```

Matrices

We can use these functions to assign new names.

```
colnames(M1) <- c("X", "Y")
rownames(M1) <- seq(1, nrow(M1))
print(M1)
```

```
##   X Y
## 1 1 1
## 2 2 1
## 3 3 1
## 4 4 1
## 5 5 1
```

Putting it all together

Storing names in vectors

Let's see how these types of objects can be used to create formal representations of social networks. We can start by defining a vector of names for a fictional friend group.

```
names <- c("Jay", "Amy", "Pete", "Mia")
```

Putting it all together

Representing relationships in a matrix

Next, we can define a matrix to store relationship ties. Each person is referenced according to their index in the name vector

```
X <- matrix(0, nrow = length(names), ncol = length(names))
X[1,2] <- 1 # edge from Jay to Amy.
X[1,3] <- 1
X[3,2] <- 1
X[1,4] <- 1
X[4,2] <- 1

print(X)

##      [,1] [,2] [,3] [,4]
## [1,]     0     1     1     1
## [2,]     0     0     0     0
## [3,]     0     1     0     0
## [4,]     0     1     0     0
```

Putting it all together

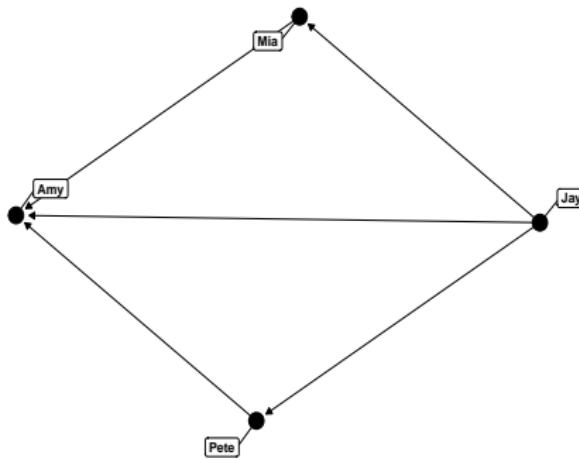
Storing information in a list

```
network_info <- list(names = names, network = X)
print(network_info)
```

```
## $names
## [1] "Jay"   "Amy"   "Pete"  "Mia"
##
## $network
##      [,1] [,2] [,3] [,4]
## [1,]    0    1    1    1
## [2,]    0    0    0    0
## [3,]    0    1    0    0
## [4,]    0    1    0    0
```

Putting it all together

Plotting the network



Questions?