```
pair < node *, int > find nth_elevent (int n)
      ( if (leaf ())
            & if ( Nom_ Key, =n)
                      raturn make-pair (NVLL, numikeys);
              return make -pair (elements [n-1], 0).
       int elem_index =0, elementy:0;
       for (auto i= children. begin (); i (= children. end(); == i, elem_index)
          E pair < nod , int > p = (*i) -> first_nth_derent (n-elements);
             " ( p. First)
                   retorn P:
             elem esty = p-second 21;
            if ( elementy == n && elem -index < num_ keys)
                return make -pour (elements (elem_index), o);
         3
       satisfy make pair (NVLL, eleventy -1);
  complexity of this algorithm is \Theta(|g(n)-k) where n is the # of body
 and the kin (in this cope 4th) element is the one to be tourd. The function
will call itself recordinaly until the smallest element is found. Since this
elevent is growteed to be in a leaf, we have at least A (1911) to get
to the loof. from there, the algorithm will begin scarring all of its greey jung
until K nodes have been found. This step is Q(K) in total we have
 O (19 (n-K))
```

## Question 4

A. If the tree has the maximum number of keys in all the nodes from the root down to the leaf in which the new element would be inserted, then the leaf node, and every node above it would have to be split, each giving one node to its parent. Eventually the root would have one key too many, and it would have to be split into two nodes, making the middle node a new root. This would add a new level to the tree, increasing the height by one. Otherwise insertion will have no effect on the height of the tree.

B. If the leaf node where the new element is to be inserted is not full, then it would be added to that leaf, having no effect on the number of leaves. If the leaf node is full, then it will be split into two, causing the number of leaves to increase by one.

C. If the leaf node is not full, then the new element would be inserted into that leaf, so there would be no effect on the number of internal nodes. If the leaf node is full, it will be split, sending its median key to its parent. Each parent has the possibility to split and send an element up to its parent, all the way until the root. Therefore a single insertion has the possibility to increase the number of internal nodes by up to h, where h is the height of the tree.