§1 SAT-GATES-STUCK INTRO 1

May 19, 2018 at 02:30

1. Intro. This shortish program inputs a Boolean circuit in GraphBase format, and generates data by which my SAT solvers are supposed to find a test pattern for a given single-stuck-at fault. (I hacked it from the simpler program SAT-GATES.)

The command line contains the name of the circuit file (e.g., foo-wires.gb, produced from foo.gb by GATES-TO-WIRES), and the name of the fault to be investigated (e.g., 0X1#2).

```
#include <stdlib.h>
#include <string.h>
#include "gb_graph.h"
#include "gb_gates.h"
#include "gb_save.h"
  main(\mathbf{int} \ argc, \mathbf{char} *argv[])
     register int j, k;
     register Graph *g;
     \textbf{register Vertex} *u, *v, *w, *fault;
     register Arc *a;
     \langle Process the command line 2 \rangle;
     (Check for improper wire names 3);
     \langle Locate the faulty wire 4 \rangle;
     (Emit clauses for the wires 5);
     (Emit clauses for the outputs 12);
  }
2. \langle \text{Process the command line } 2 \rangle \equiv
  if (argc \neq 3) {
     fprintf(stderr, "Usage: \_%s\_foo-wires.gb\_fault\n", argv[0]);
     exit(-1);
  }
  g = restore\_graph(argv[1]);
  if (\neg g) {
     fprintf(stderr, "I_{\square}couldn't_{\square}reconstruct_{\square}graph_{\square}%s!\n", argv[1]);
     exit(-2);
  if (argv[2][0] \neq 0, \land argv[2][0] \neq 1, ) {
     fprintf(stderr, "The_lfault_lname_lshould_lbegin_lwith_l0_lor_l1!\n");
     exit(-3);
  }
This code is used in section 1.
```

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3. If necessary, I could rename vertices whose name is empty or too long. But I don't want to bother with that unless it proves to be necessary.

```
#define prime_char '\','
#define sharp_char '#'
\langle Check for improper wire names 3\rangle \equiv
   for (j = 0, v = g \neg vertices; v < g \neg vertices + g \neg n; v \leftrightarrow) {
      for (k = 0; v \rightarrow name[k]; k++)
         if (v \rightarrow name[k] < "!" \lor v \rightarrow name[k] > """) break;
      if (v \rightarrow name[0] \equiv , \sim, \lor k \equiv 0 \lor v \rightarrow name[k]) {
         fprintf(stderr, "Sorry, \_the\_wire\_name\_'%s'\_is\_illegal! \n", v \rightarrow name);
         j = 1;
      } else if (k > 8) {
         fprintf(stderr, "Sorry, \_the\_wire\_name\_', "s', \_is\_too\_long! \n", v \rightarrow name);
      } else if (v \neg name[k-1] \equiv prime\_char \lor v \neg name[k-1] \equiv sharp\_char) {
         fprintf(stderr, "Sorry, _ \sqcup I_ \sqcup don't_ \sqcup like_ \sqcup the_ \sqcup last_ \sqcup character_ \sqcup of_ \sqcup the_ \sqcup wire_ \sqcup name_ \sqcup '%s'! \setminus n",
                v \rightarrow name);
         j = 1;
      } else if (v \rightarrow name[0] \equiv '\_' \land v \rightarrow name[1] \equiv '\_') {
         fprintf(stderr, "Sorry, LI'm_reserving_wire_names_that_begin_with_'.__'!\n");
      }
   if (j) exit(-3);
This code is used in section 1.
4. \langle Locate the faulty wire 4\rangle \equiv
   for (v = g \neg vertices, fault = \Lambda; \ v < g \neg vertices + g \neg n; \ v ++) \ 
      if (strcmp(v \rightarrow name, argv[2] + 1) \equiv 0) {
         fault = v;  break;
   if (\neg fault) {
      fprintf(stderr, \texttt{"Sorry,} \bot I \bot \texttt{can't} \bot \texttt{find} \bot \texttt{a} \bot \texttt{wire} \bot \texttt{named} \bot \texttt{`%s'!} \\ \texttt{`n"}, argv[2]+1);
      exit(-4);
This code is used in section 1.
```

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5. A wire is "tarnished" if it is the faulty wire or if one of its operands is tarnished. Tarnished wires g are represented by three variables in the output, namely g and g, and g, variable g, denotes the value computed when the fault is present, while g# denotes a wire on the "active path" from the fault location to an output.

Untarnished wires implicitly have g, identical to g and g# false.

When g# is true we ensure that $g \neq g$.

Wires that fan out from a common source actually share the same name, except for their "active" variables. For example, the three wires Q, Q#1, Q#2 generate at most five variables Q, Q', Q#, Q#1#, Q#2#, not nine. The base variable name is called the wire's ename.

```
#define tarnished x.I
\#define ename u.S
\langle \text{ Emit clauses for the wires 5} \rangle \equiv
  printf("\"argv[1], argv[1], argv[2]);
  for (v = g \rightarrow vertices; \ v < g \rightarrow vertices + g \rightarrow n; \ v \leftrightarrow)  {
                               /* innocent until proved guilty */
     v \rightarrow tarnished = 0;
     switch (v \rightarrow typ) {
     case 'I': break;
     case '~': (Handle a NOT gate 6); break;
     case '&': (Handle an AND gate 7); break;
     case '|': (Handle an OR gate 8); break;
     case '^': (Handle an XOR gate 9); break;
     case 'F': \langle Handle a fanout gate 10 \rangle; break;
     default: fprintf(stderr, "Sorry, LLdon'tLknowLtoLhandleLtypeL'%c'L(wireL%s)!\n",(int)
              v \rightarrow typ, v \rightarrow name);
        exit(-666);
     if (v \rightarrow typ \neq `F") {
        v \rightarrow ename = v \rightarrow name;
        if (v \rightarrow tarnished) {
           printf("~%s%c_{\sim}~%s~c^{\sim}, v\rightarrow name, sharp\_char, v\rightarrow name, v\rightarrow name, prime\_char);
           printf("~\%s\%c_{\square}\%s\%c\n", v\rightarrow name, sharp\_char, v\rightarrow name, v\rightarrow name, prime\_char);
     if (v \equiv fault) (Initiate the fault scenario 11);
```

This code is used in section 1.

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```
6. \langle Handle a NOT gate 6\rangle \equiv
   if (v \rightarrow arcs \equiv \Lambda \lor v \rightarrow arcs \rightarrow next \neq \Lambda) {
      fprintf(stderr, "The \ NOT \ gate \ %s \ should \ have \ only \ one \ argument! \ ", v \ name);
      exit(-10);
   }
   u = v \rightarrow arcs \rightarrow tip;
   printf("\%s \ \ \ ", v \rightarrow name, u \rightarrow ename);
   printf("~\%s_{\sqcup}~\%s\n", v\rightarrow name, u\rightarrow ename);
   if (u \rightarrow tarnished) {
      v \rightarrow tarnished = 1;
      printf("%s%c_{\square}%s%c_{n}", v \rightarrow name, prime\_char, u \rightarrow ename, prime\_char);
      printf("~%s%c_{\sim}~%s%c_{\sim}~, v\rightarrow name, prime\_char, u\rightarrow ename, prime\_char);
      printf("~\%s\%c_{\square}\%s\%c_{n}", u\rightarrow name, sharp\_char, v\rightarrow name, sharp\_char);
   }
This code is used in section 5.
7. \langle Handle an AND gate 7\rangle \equiv
   for (a = v \rightarrow arcs; a; a = a \rightarrow next) {
      u = a \rightarrow tip;
      printf("~\%s_{\square}\%s\n", v\rightarrow name, u\rightarrow ename);
      if (u \rightarrow tarnished) {
          v \rightarrow tarnished = 1;
          printf("~%s%c_{l}%s%c_{l}, u\rightarrow name, sharp\_char, v\rightarrow name, sharp\_char);
   }
   printf("\%s", v \rightarrow name);
   for (a = v \rightarrow arcs; a; a = a \rightarrow next) printf (" \ " \ " \ ", a \rightarrow tip \rightarrow ename);
   printf("\n");
   if (v \rightarrow tarnished) {
      for (a = v \rightarrow arcs; a; a = a \rightarrow next) {
          u = a \rightarrow tip;
          if (u - tarnished) printf("~%s%c_l%s%c\n", v - name, prime\_char, u - ename, prime\_char);
          else printf("~%s%c_{\sqcup}%s\n", v\rightarrow name, prime\_char, u\rightarrow ename);
      printf("%s%c", v \rightarrow name, prime\_char);
      for (a = v \rightarrow arcs; a; a = a \rightarrow next) {
          u = a \rightarrow tip;
          if (u¬tarnished) printf("□~%s%c", u¬ename, prime_char);
          else printf(" \_ ~\%s", u \rightarrow ename);
      printf("\n");
This code is used in section 5.
```

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```
8. \langle Handle an OR gate 8 \rangle \equiv
   for (a = v \rightarrow arcs; a; a = a \rightarrow next) {
      u = a \neg tip;
      printf("%s_{\square}~%s\n", v \rightarrow name, u \rightarrow ename);
      if (u \rightarrow tarnished) {
         v \rightarrow tarnished = 1;
         printf("~\%s\%c_{l}\%s\%c\n", u\rightarrow name, sharp\_char, v\rightarrow name, sharp\_char);
   printf("~\%s", v \rightarrow name);
   \textbf{for} \ (a = v \neg arcs; \ a; \ a = a \neg next) \ \ printf(" \bot \% \texttt{s"}, a \neg tip \neg ename);
   printf("\n");
   if (v \rightarrow tarnished) {
      for (a = v \rightarrow arcs; a; a = a \rightarrow next) {
         u = a \rightarrow tip;
         if (u-tarnished) printf("%s%c\n", v-name, prime_char, u-ename, prime_char);
         else printf("%s%c_{l}~%s\n", v\rightarrow name, prime\_char, u\rightarrow ename);
      printf("~\%s\%c", v\rightarrow name, prime\_char);
      for (a = v \rightarrow arcs; a; a = a \rightarrow next) {
         u = a \rightarrow tip;
         if (u \rightarrow tarnished) printf(" \ \ \%s\%c", u \rightarrow ename, prime\_char);
         else printf(" " ", u \rightarrow ename);
      printf("\n");
This code is used in section 5.
```

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9. I could handle XORs of any length. But I don't want to do that unless it's important, because it would involve generating new names for intermediate gates.

```
\langle Handle an XOR gate 9 \rangle \equiv
   for (k = 0, a = v \rightarrow arcs; a; a = a \rightarrow next) k++;
   if (k \neq 2) {
      fprintf(stderr, "Sorry, _\_I_\_do_\_XOR_\_only_\_of_\_two_\_operands, _\_not_\_%d_\_(gate_\_%s)!\n", k, v \neg name);
      exit(-5);
   }
   u = v \rightarrow arcs \rightarrow tip, w = v \rightarrow arcs \rightarrow next \rightarrow tip;
   printf("~\%s_{\square}\%s_{\square}\%s_{\square}", v \neg name, u \neg ename, w \neg ename);
   printf("~\%s_{\square}~\%s_{\square}~\%s_{\square}~\%s_{\square}~,v\rightarrow name,u\rightarrow ename,w\rightarrow ename);
   printf("\%s_{\square}^{-}\%s_{\square}\%s_{\square}", v \neg name, u \neg ename, w \neg ename);
   printf("%s_{\square}%s_{\square}^{-}%s_{\square}", v \rightarrow name, u \rightarrow ename, w \rightarrow ename);
   if (u \rightarrow tarnished) {
      v \rightarrow tarnished = 1;
      printf("~\%s\%c_{\square}\%s\%c\n", u\rightarrow name, sharp\_char, v\rightarrow name, sharp\_char);
      if (w \rightarrow tarnished) {
          printf("~\%s\%c_{\square}\%s\%c_{\square}, w\rightarrow name, sharp\_char, v\rightarrow name, sharp\_char);
          printf("~%s%c_{\sim}~%s%c\n", u\rightarrow name, sharp\_char, w\rightarrow name, sharp\_char);
          printf("^%s\c_\%s\%c_\%s\%c_\n", v-name, prime\_char, u-ename, prime\_char, w-ename, prime\_char);
          printf("^%s%c_"%s%c_"%s%c_",v \rightarrow name,prime\_char,u \rightarrow ename,prime\_char,w \rightarrow ename,prime\_char);
          printf("%s%c_"%s%c_"%s%c'", v \rightarrow name, prime\_char, u \rightarrow ename, prime\_char, w \rightarrow ename, prime\_char);
          printf("\%s\%c_{\square}\%s\%c_{\square}", v-name, prime\_char, u-ename, prime\_char, w-ename, prime\_char);
          printf("~\%s\%c_{\square}\%s\%c_{\square}\%s\%c_{\square}, v \rightarrow name, prime\_char, u \rightarrow ename, prime\_char, w \rightarrow ename);
          printf("~\%s\%c_{\sim}\%s\%c_{\sim}\%s\n", v\rightarrow name, prime\_char, u\rightarrow ename, prime\_char, w\rightarrow ename);
          printf("%s%c_{\square}~%s%c_{\square}~%s%c_{\square}~, v \rightarrow name, prime\_char, u \rightarrow ename, prime\_char, w \rightarrow ename);
          printf("%s%c_{\square}%s%c_{\square}", v \rightarrow name, prime\_char, u \rightarrow ename, prime\_char, w \rightarrow ename);
   } else if (w \neg tarnished) {
      v \rightarrow tarnished = 1;
      printf("~\%s\%c_{\square}\%s\%c\n", w\rightarrow name, sharp\_char, v\rightarrow name, sharp\_char);
      printf("~%s%c_{\perp}%s%c_{\perp}%s%c_{\parallel}, v \rightarrow name, prime\_char, w \rightarrow ename, prime\_char, u \rightarrow ename);
      printf("~\%s\%c_{\perp}~\%s\%c_{\perp}~\%s\n", v\rightarrow name, prime\_char, w\rightarrow ename, prime\_char, u\rightarrow ename);
      printf("%s%c_{\square}^{\sim}%s%c_{\square}%s^{n}", v \rightarrow name, prime\_char, w \rightarrow ename, prime\_char, u \rightarrow ename);
      printf("%s%c_{\square}%s%c_{\square}", v \rightarrow name, prime\_char, w \rightarrow ename, prime\_char, u \rightarrow ename);
```

This code is used in section 5.

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```
\langle Handle a fanout gate 10\rangle
  if (\neg v \neg arcs \lor v \neg arcs \neg next) {
     fprintf(stderr, "Eh? \_A\_fanout\_gate\_should\_have\_a\_unique\_parent! \n");
     exit(-6);
  }
  u = v \rightarrow arcs \rightarrow tip;
  v \rightarrow ename = u \rightarrow ename;
  v \rightarrow tarnished = u \rightarrow tarnished;
  if ((v-1) \rightarrow typ \equiv F' \wedge (v-1) \rightarrow arcs \rightarrow tip \equiv u) {
     if (v \rightarrow tarnished)
        printf("^%s%c_{\sc}%s%c_{\sc}, u-name, sharp\_char, (v-1)-name, sharp\_char, v-name, sharp\_char);
  } else if ((v+1) \rightarrow typ \neq F' \lor (v+1) \rightarrow arcs \rightarrow tip \neq u) {
     fprintf(stderr, "Eh? \_Fanout\_gates\_should\_occur\_in\_pairs! \n");
     exit(-7);
This code is used in section 5.
11. (Initiate the fault scenario 11) \equiv
     v \neg tarnished = 1;
     printf("%s%s%c\n", argv[2][0] \equiv '0' ? """ : "", v \rightarrow ename, prime\_char);
     printf("\%s\%s\n", argv[2][0] \equiv \texttt{'0'}?"": "~", v \rightarrow ename);
     printf("%s%c\n", v\rightarrow name, sharp\_char);
This code is used in section 5.
12. Here we conclude by emitting k+2 clauses to force an active path, if there are k tarnished outputs.
The first and last of these clauses can obviously be simplified; but we let the solver do that.
  (I could have simply output a single clause of length k. But I prefer to stick to 3SAT.)
\langle Emit clauses for the outputs 12\rangle \equiv
  printf("__0\n");
                             /* auxiliary variables begin with "__" */
  \textbf{for} \ (k=0, a=g \neg outs; \ a; \ a=a \neg next) \ \{
     if (u \rightarrow tarnished) {
        printf("%s%c_{\_}~_~%d_{\_}~%d\n", u \rightarrow name, sharp\_char, k, k + 1);
  }
  printf("~\__%d\n", k);
This code is used in section 1.
```

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13. Index.

 $a: \underline{1}.$ **Arc**: 1. arcs: 6, 7, 8, 9, 10. $argc: \underline{1}, 2.$ argv: 1, 2, 4, 5, 11.ename: 5, 6, 7, 8, 9, 10, 11. exit: 2, 3, 4, 5, 6, 9, 10. $fault: \underline{1}, 4, 5.$ fprintf: 2, 3, 4, 5, 6, 9, 10. $g: \underline{1}$. Graph: 1. j: $\underline{1}$. k: <u>1</u>. $main: \underline{1}.$ $name \colon \ \ 3, \ 4, \ 5, \ 6, \ 7, \ 8, \ 9, \ 10, \ 11, \ 12.$ $next{:}\quad 6,\ 7,\ 8,\ 9,\ 10,\ 12.$ outs: 12. $prime_char\colon \ \ \underline{3},\ 5,\ 6,\ 7,\ 8,\ 9,\ 11.$ printf: 5, 6, 7, 8, 9, 10, 11, 12. $restore_graph$: 2. sharp_char: 3, 5, 6, 7, 8, 9, 10, 11, 12. stderr: 2, 3, 4, 5, 6, 9, 10. strcmp: 4.tarnished: 5, 6, 7, 8, 9, 10, 11, 12.tip: 6, 7, 8, 9, 10, 12. typ: 5, 10. u: $\underline{1}$. v: $\underline{1}$. Vertex: 1. vertices: 3, 4, 5. w: $\underline{1}$.

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