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REPORT

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# Digital Image Processing

## « Assignments »

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2014-2015

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# A. Histogram Equalization

## A.1 Problem statement

1. Write a computer program for computing the histogram of an image.
2. Implement the histogram equalization technique.
3. Your program must be general to allow any gray-level image as its input.

## A.2 Python implementation

Usage : `python problem1.py [-h] image_path`

## A.3 Figure 1

### A.3.1 Histogram

Original image : [A.1](#) | Original image's histogram : [A.2](#)

### A.3.2 Histogram equalization

Enhanced image : [A.3](#) | Enhanced image's histogram : [A.4](#)

## A.4 Figure 2

### A.4.1 Histogram

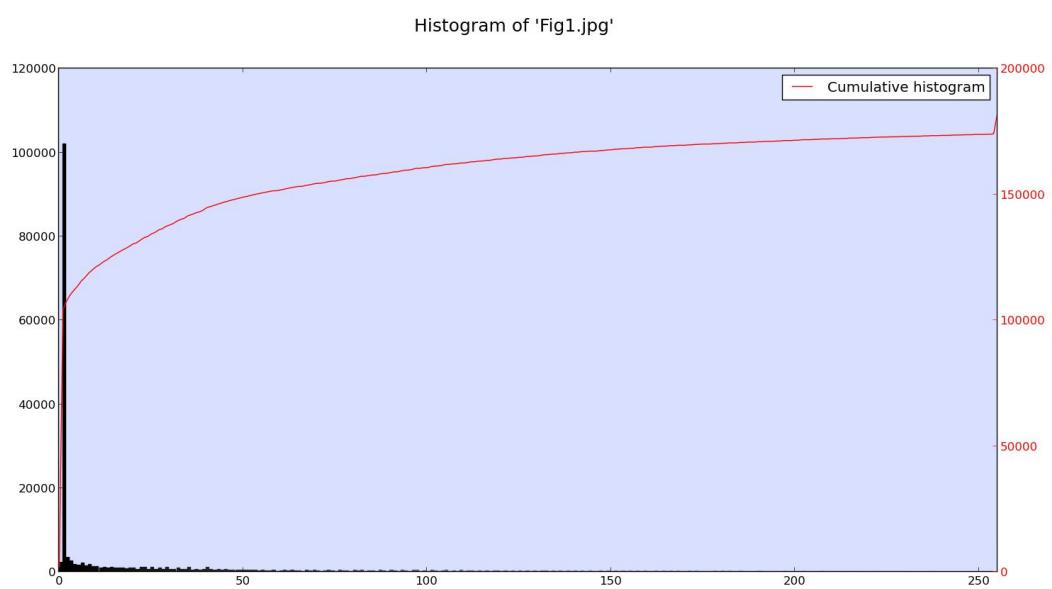
Original image : [A.5](#) | Original image's histogram : [A.6](#)

### A.4.2 Histogram equalization

Enhanced image : [A.7](#) | Enhanced image's histogram : [A.8](#)



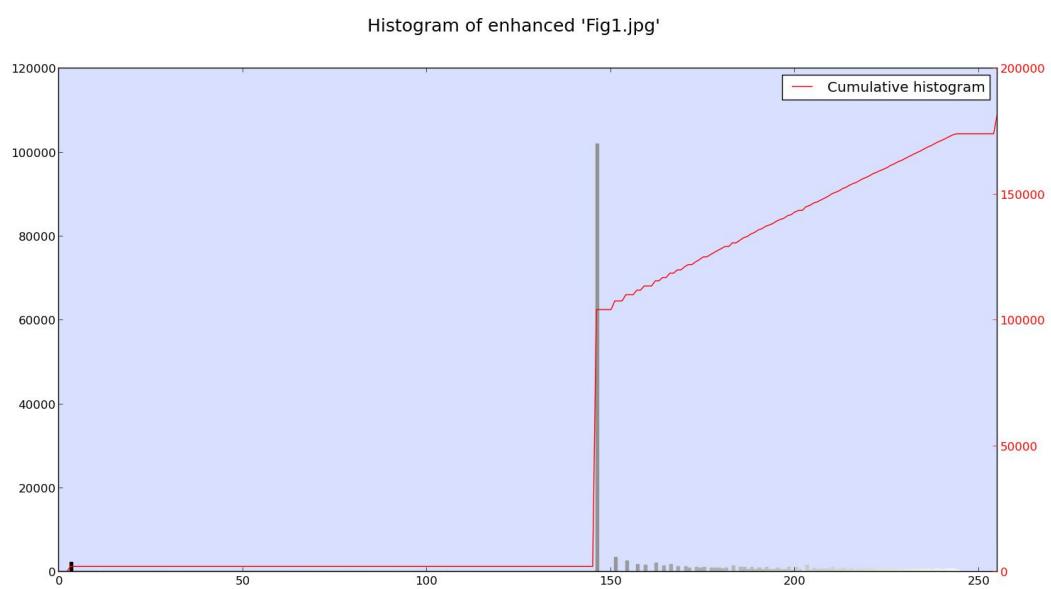
**FIGURE A.1** – Original *Fig1.jpg*



**FIGURE A.2** – Histogram of *Fig1.jpg*



**FIGURE A.3 – Enhanced Fig1.jpg**



**FIGURE A.4 – Equalized histogram of Fig1.jpg**

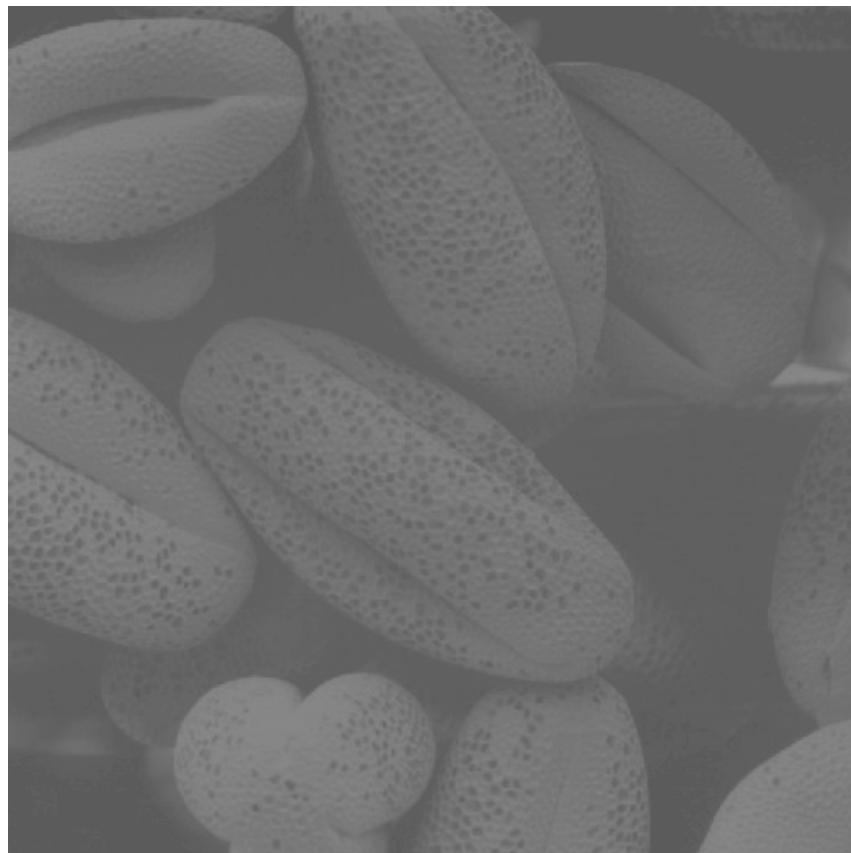


FIGURE A.5 – Original *Fig2.jpg*

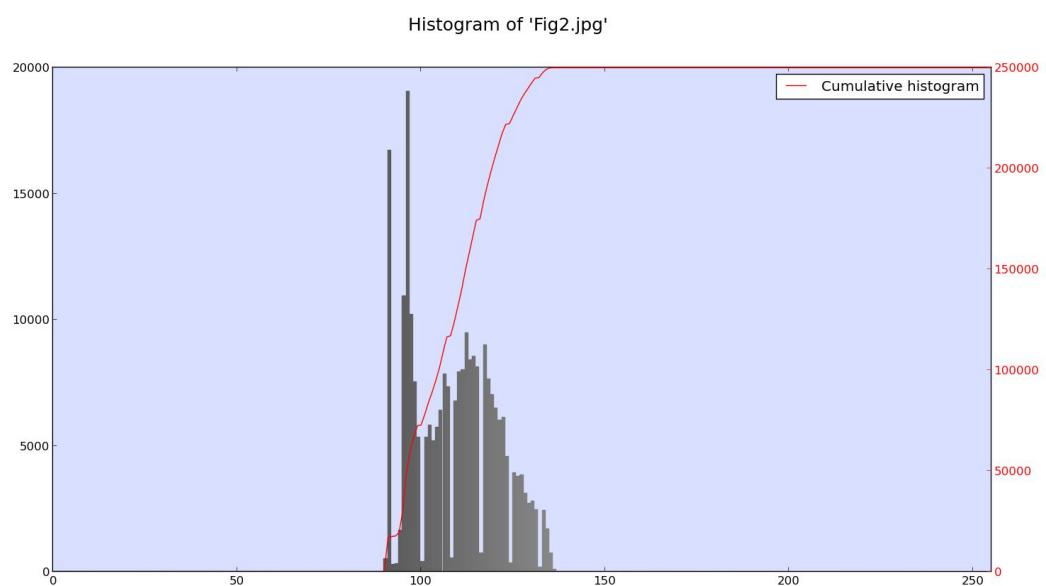
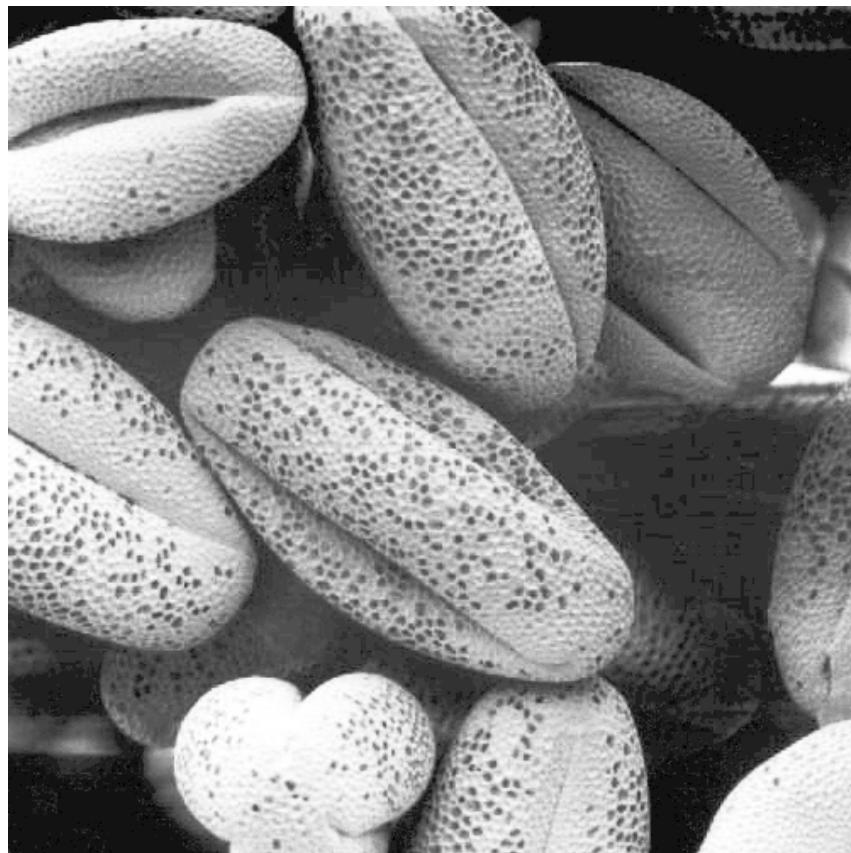
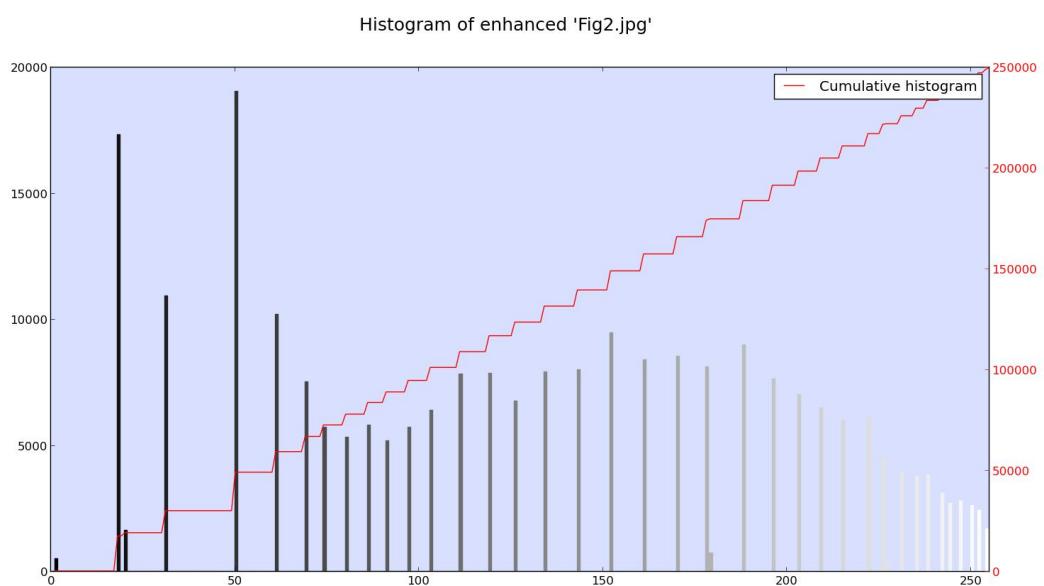


FIGURE A.6 – Histogram of *Fig2.jpg*



**FIGURE A.7** – Enhanced *Fig2.jpg*



**FIGURE A.8** – Equalized histogram of *Fig2.jpg*

# B. Spatial enhancement methods

## B.1 Problem statement

Implement the image enhancement task of Section 3.7 (Fig 3.43) (Section 3.8, Fig 3.46 in our slides).

The image to be enhanced is *skeleton\_orig.tif*.

You should implement all steps in Figure 3.43.

(You cannot directly use functions of Matlab such as imfilter or fspecial, implement all functions by yourself).

## B.2 Python implementation

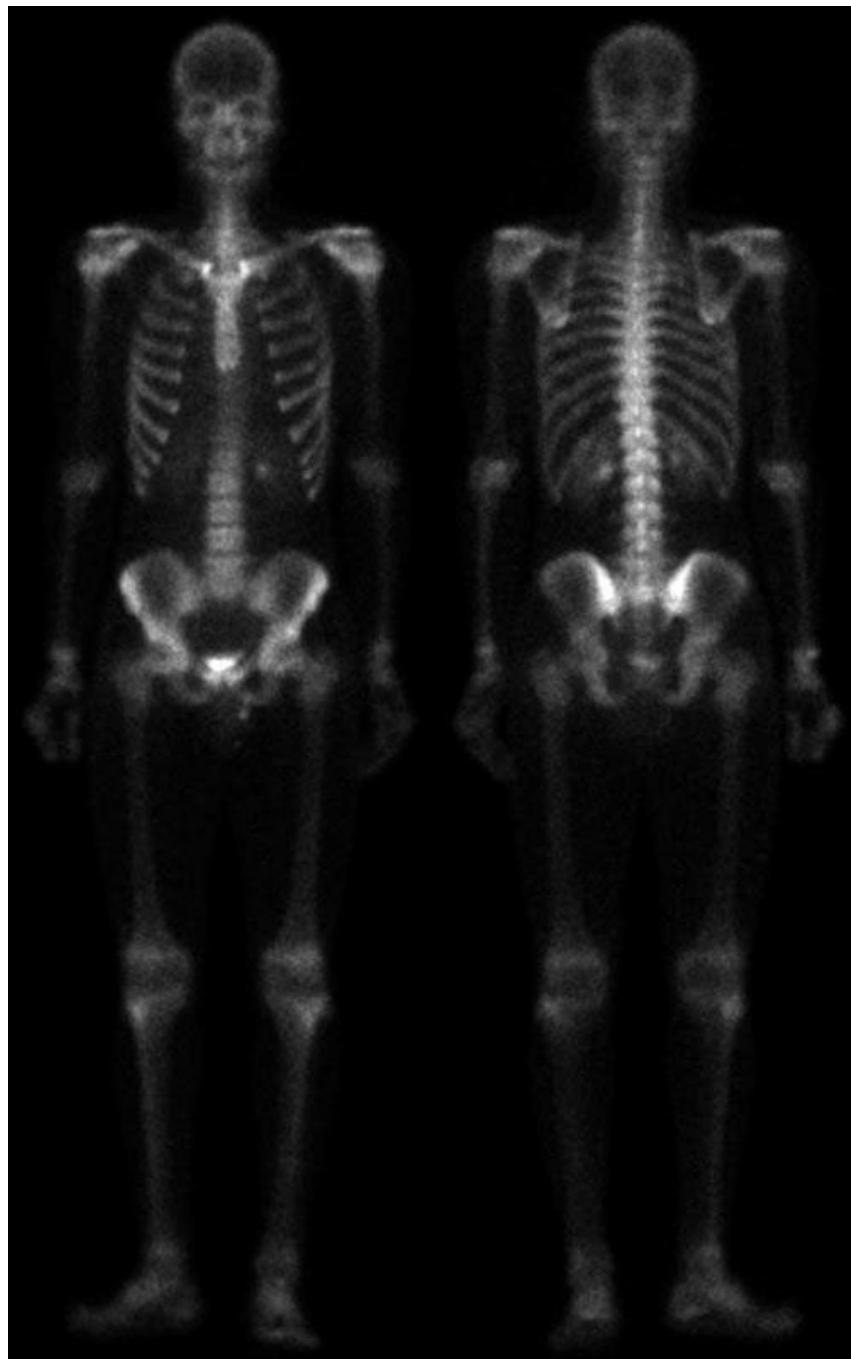
Usage : `python problem2.py [-h] [-laplacian] [-sobel] [-a A] [-g G] [-c C] image_path`

For example, to run the full image enhancement described in the assignment, using a  $3 \times 3$  Laplacian filter with  $A = 1.7$ , then a Sobel, a smoothing filter and a Power-Law transformation with  $c = 1$  and gamma = 0.5 type :

```
python problem2.py -laplacian -a 1.7 -sobel -g 0.5 -c 1 skeleton_orig.tif
```

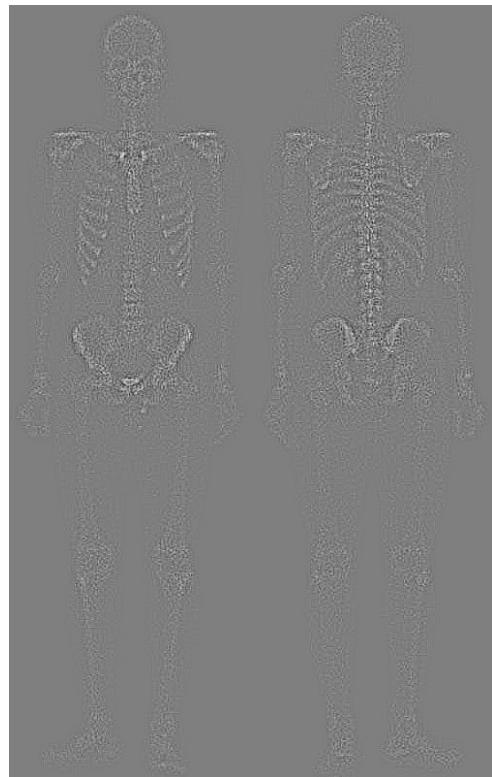
## B.3 Results

### B.3.1 Original image



**FIGURE B.1** – Original *skeleton\_orig.tif*

### B.3.2 3x3 Laplacian ( $A = 0$ )



**FIGURE B.2** – Laplacian ( $A=0$ )



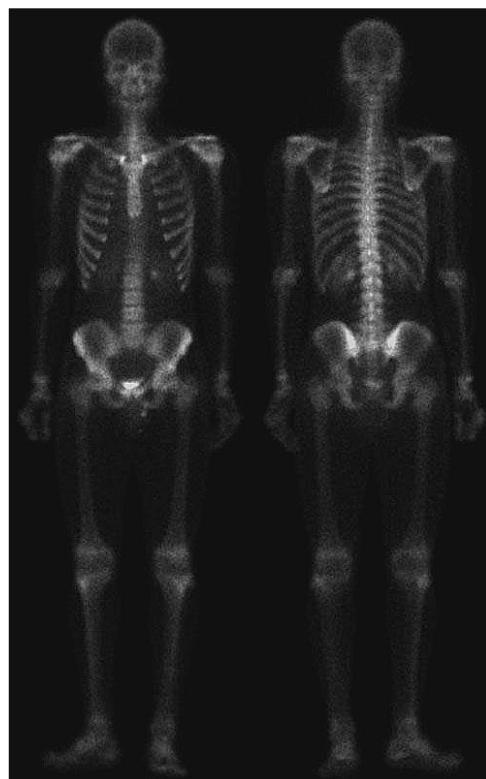
**FIGURE B.3** – Sharpened image

**FIGURE B.4** – Original image

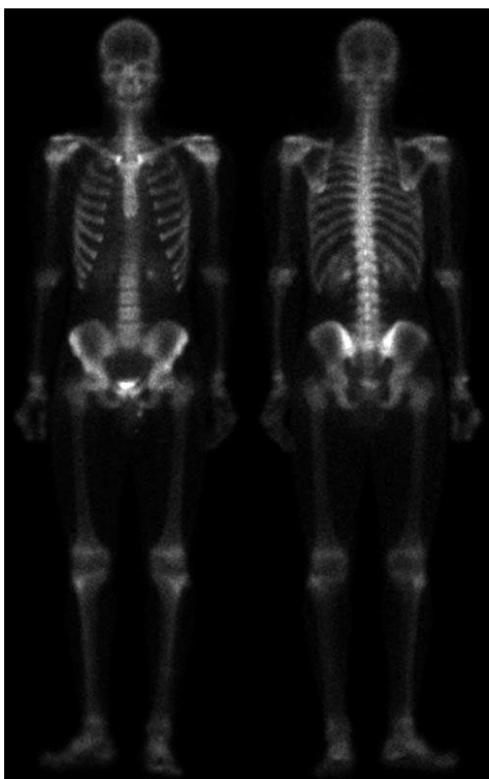
### B.3.3 3x3 Laplacian ( $A = 1$ )



**FIGURE B.5** – Laplacian ( $A=1$ )

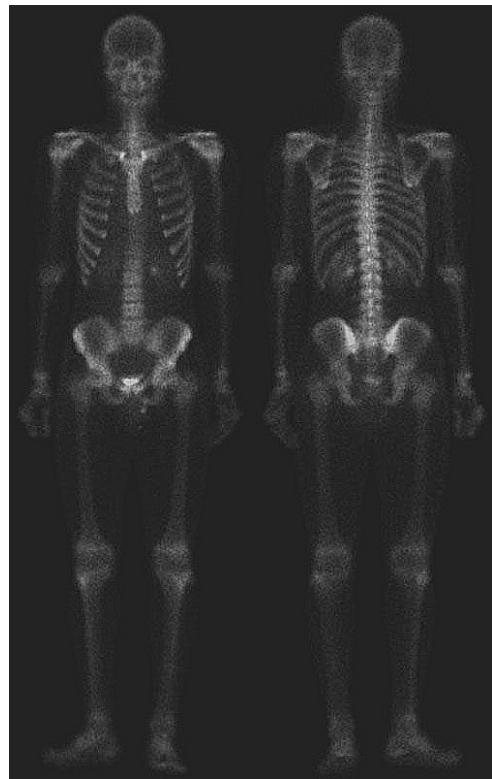


**FIGURE B.6** – Sharpened image

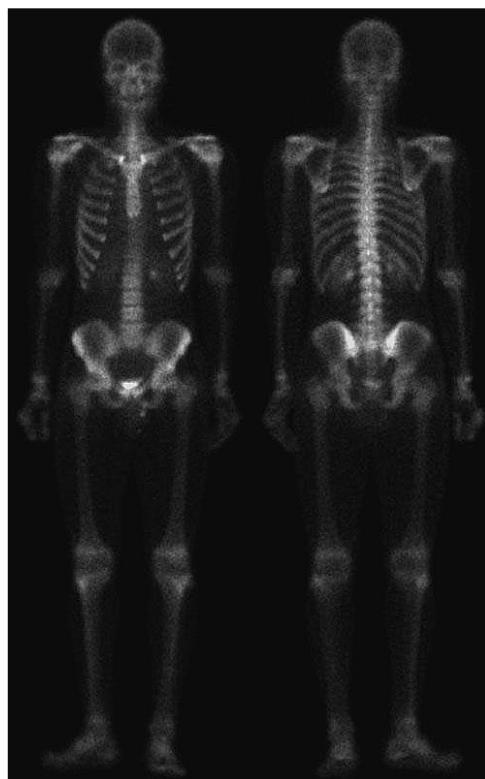


**FIGURE B.7** – Original image

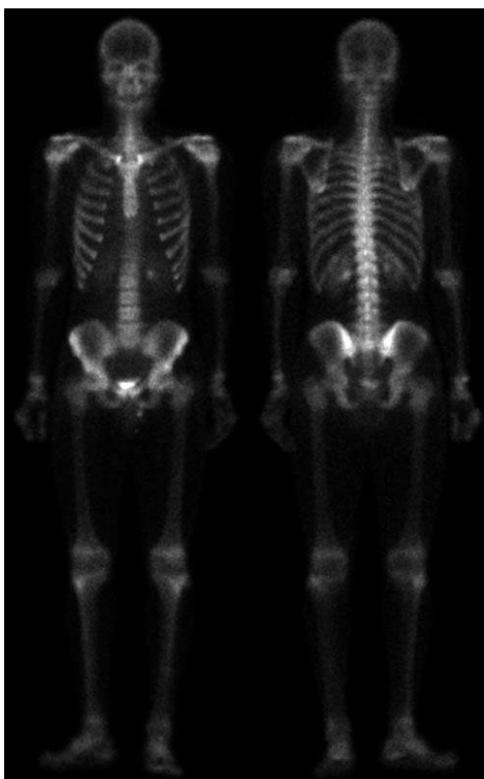
### B.3.4 3x3 Laplacian ( $A = 1.7$ )



**FIGURE B.8** – Laplacian ( $A=1.7$ )

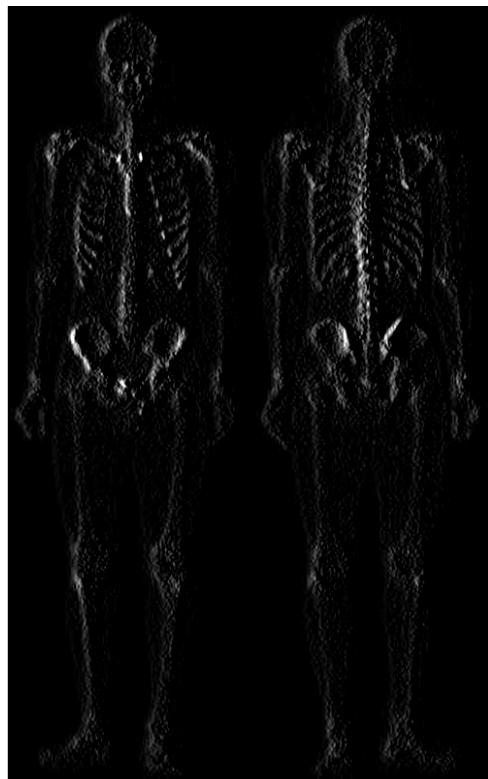


**FIGURE B.9** – Sharpened image

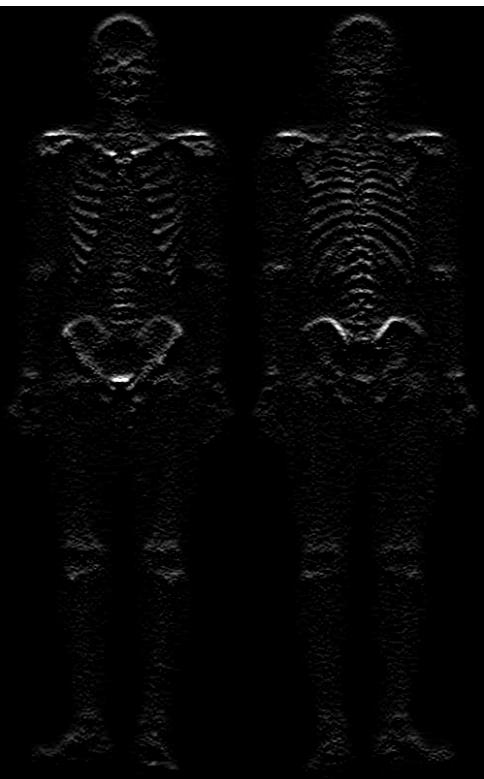


**FIGURE B.10** – Original image

### B.3.5 Sobel



**FIGURE B.11** – Sobel x-gradient



**FIGURE B.12** – Sobel y-gradient

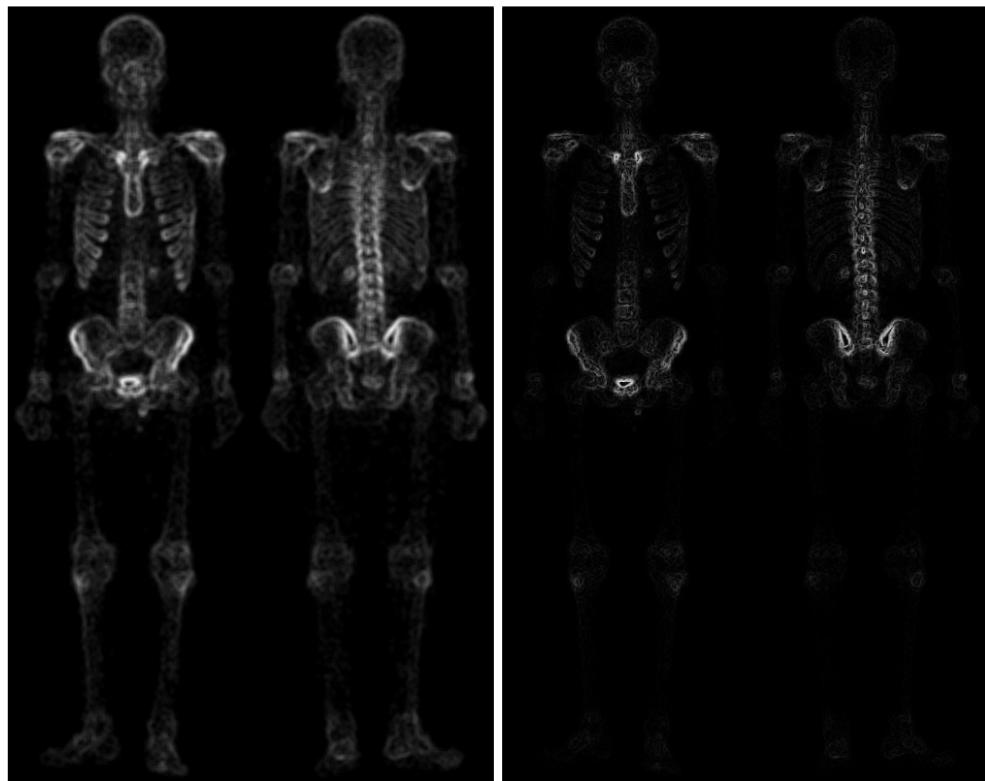


**FIGURE B.13** – Full Sobel



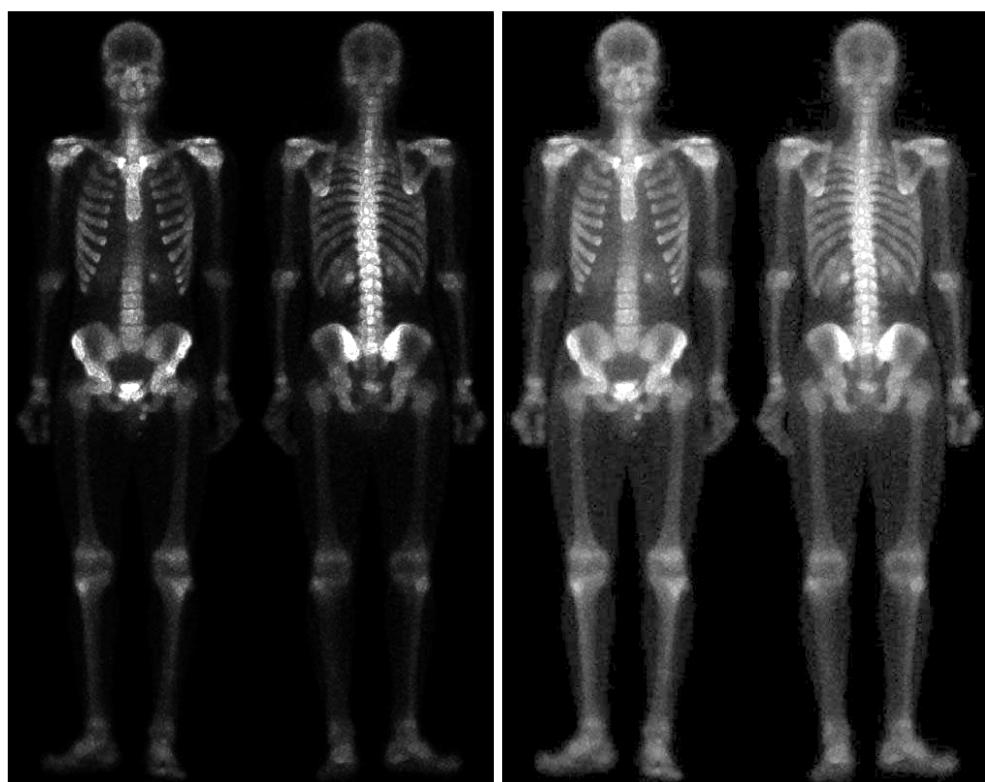
**FIGURE B.14** – Original image

### B.3.6 Smoothing, Sharpening and Power-Law transformation



**FIGURE B.15** – Smooth Sobel

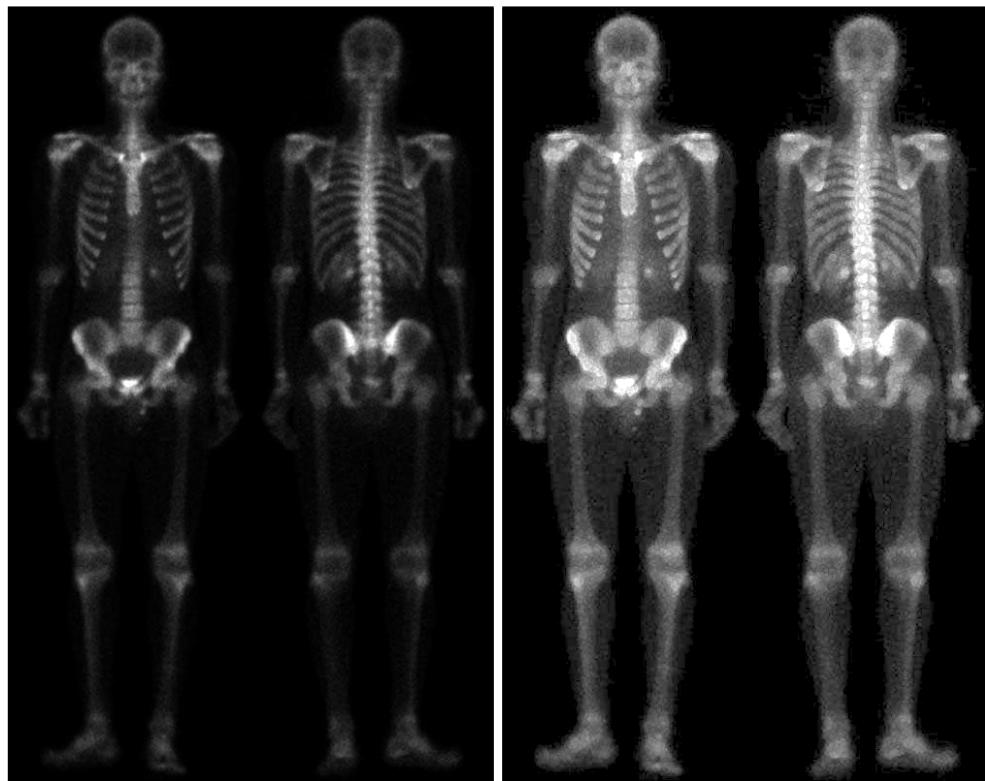
**FIGURE B.16** – Laplacian x Sobel



**FIGURE B.17** – Original + Laplacian x Smooth Sobel

**FIGURE B.18** – Final image (after Power-Law ( $c=1, g=0.5$ )))

### B.3.7 Comparison



**FIGURE B.19 –** Original

**FIGURE B.20 –** Final image

# C. Filtering in frequency domain

## C.1 Problem statement

Implement the ideal, Butterworth and Gaussian lowpass and highpass filters and test them under different parameters using *characters\_test\_pattern.tif*.

## C.2 Python implementation

```
Usage : python problem3.py [-h] [-ideal] [-butterworth] [-gaussian]
(-low | -high) [-d D] [-n N] image_path
```

Use `python problem3.py -h` to see the help.

## C.3 Results

### C.3.1 Original image

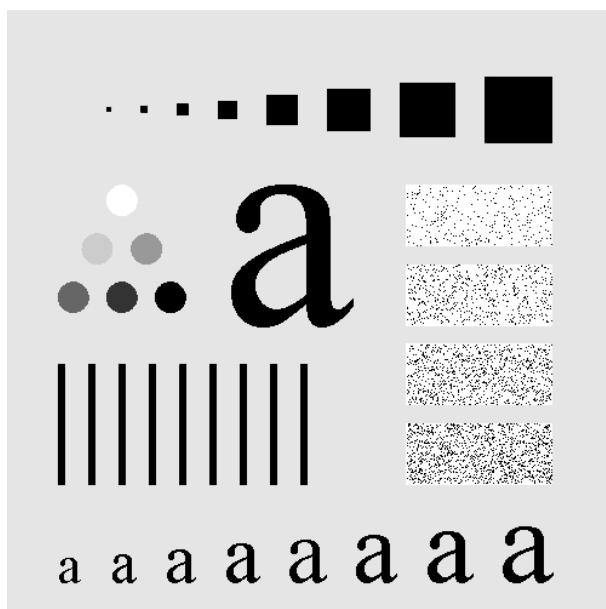


FIGURE C.1 – Original *characters\_test\_pattern.tif*

### C.3.2 Ideal filter

#### Low pass

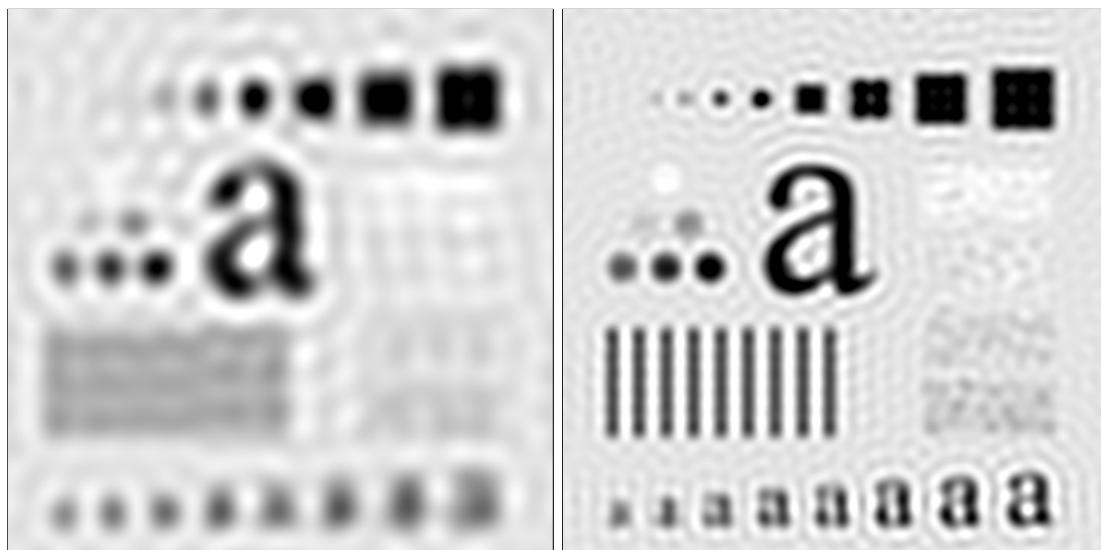
```
python problem3.py -ideal -d 5 -low characters_test_pattern.tif
```



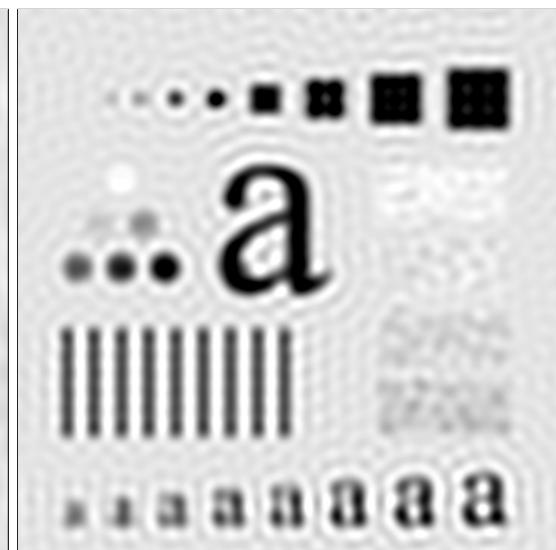
**FIGURE C.2** – Original image



**FIGURE C.3** – Ideal low 5



**FIGURE C.4** – Ideal low 15



**FIGURE C.5** – Ideal low 30

**High pass**

```
python problem3.py -ideal -d 5 -high characters_test_pattern.tif
```

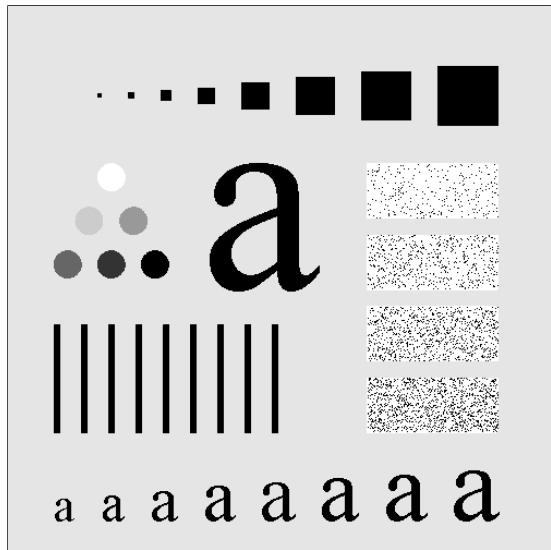


FIGURE C.6 – Original image



FIGURE C.7 – Ideal high 5

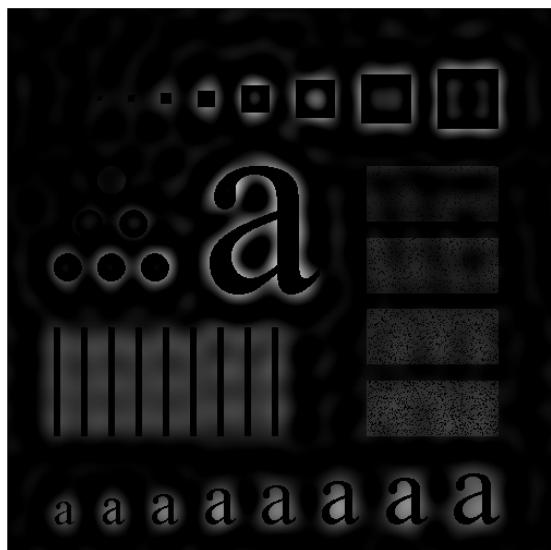


FIGURE C.8 – Ideal high 15

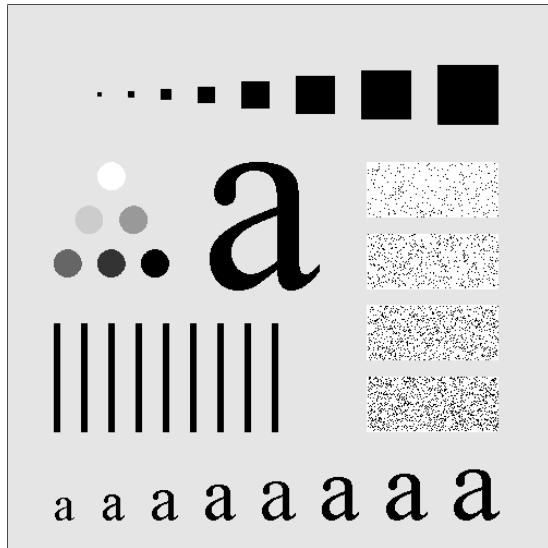


FIGURE C.9 – Ideal high 30

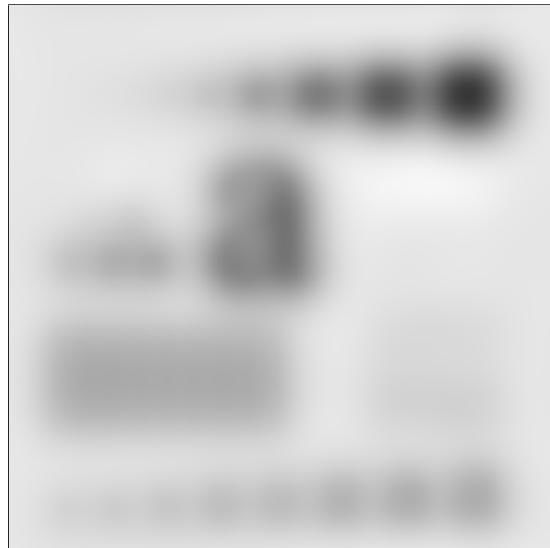
### C.3.3 Butterworth order 2 filter

#### Low pass

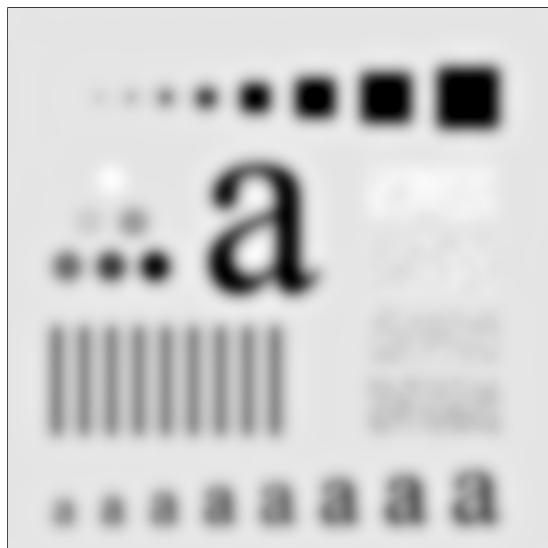
```
python problem3.py -butterworth -d 5 -n 2 -low characters_test_pattern.tif
```



**FIGURE C.10** – Original image



**FIGURE C.11** – Butterworth low 5



**FIGURE C.12** – Butterworth low 15



**FIGURE C.13** – Butterworth low 30

**High pass**

```
python problem3.py -butterworth -d 5 -n 2 -high characters_test_pattern.tif
```

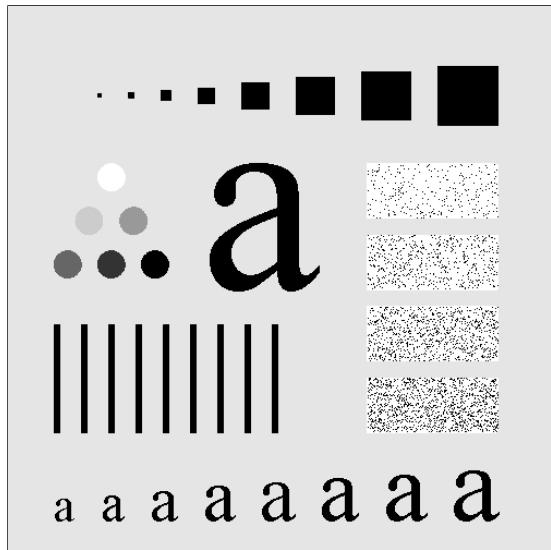


FIGURE C.14 – Original image



FIGURE C.15 – Butterworth high 5

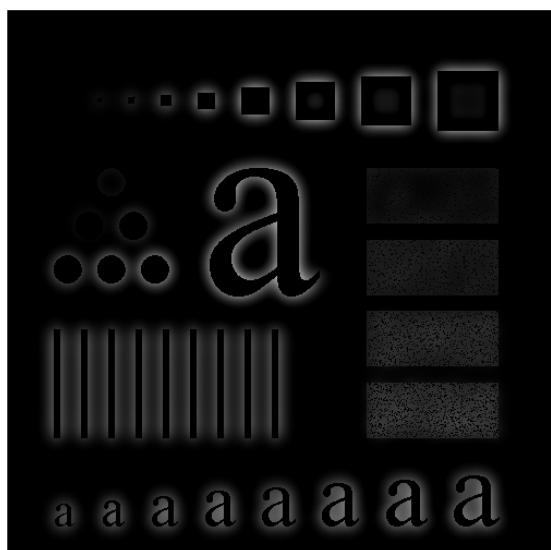


FIGURE C.16 – Butterworth high 15

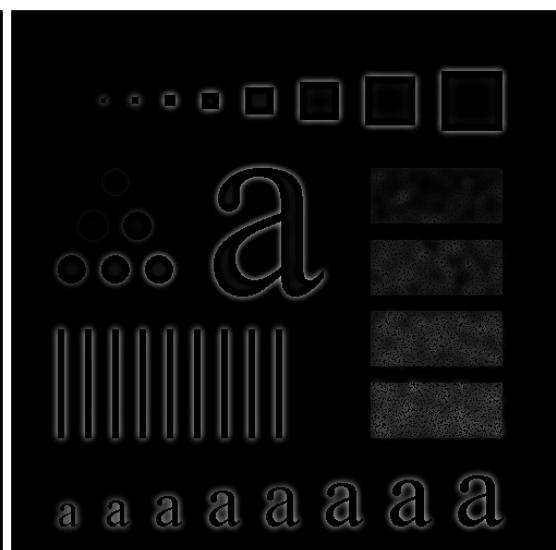
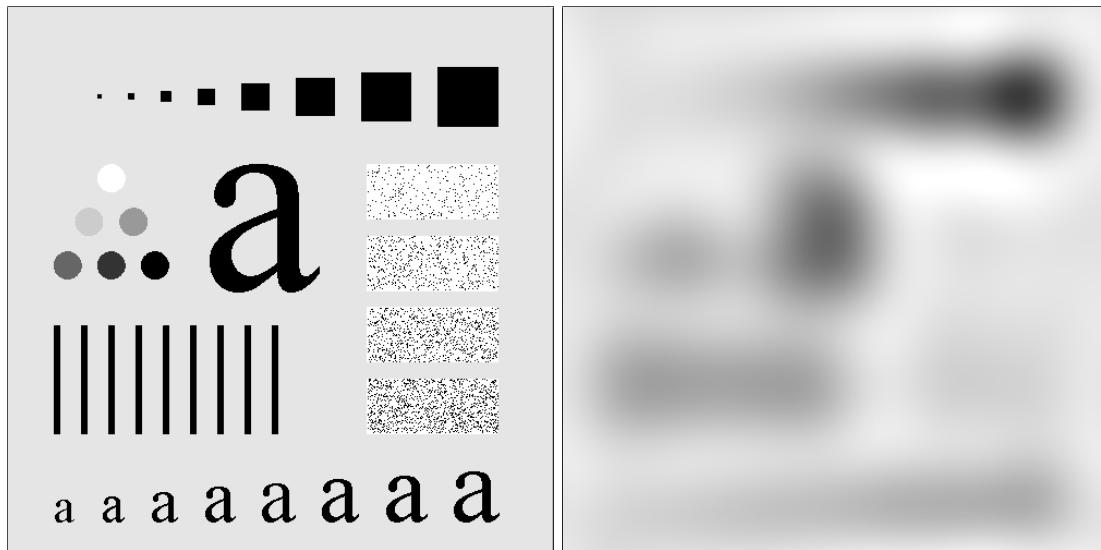


FIGURE C.17 – Butterworth high 30

### C.3.4 Butterworth order 5 filter

#### Low pass

```
python problem3.py -butterworth -d 5 -n 5 -low characters_test_pattern.tif
```



**FIGURE C.18** – Original image

**FIGURE C.19** – Butterworth low 5



**FIGURE C.20** – Butterworth low 15

**FIGURE C.21** – Butterworth low 30

**High pass**

```
python problem3.py -butterworth -d 5 -n 5 -high characters_test_pattern.tif
```

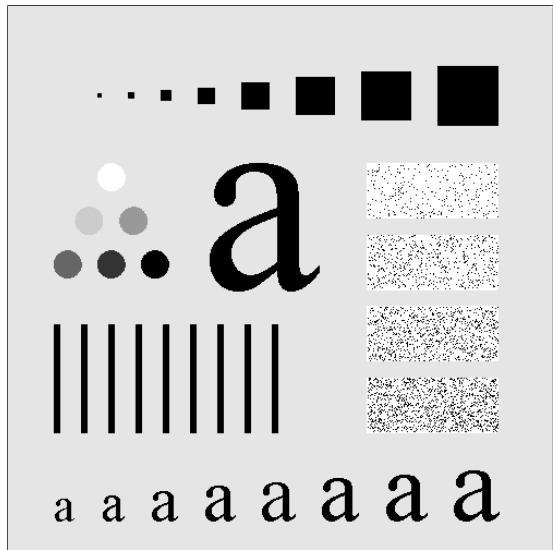


FIGURE C.22 – Original image



FIGURE C.23 – Butterworth high 5

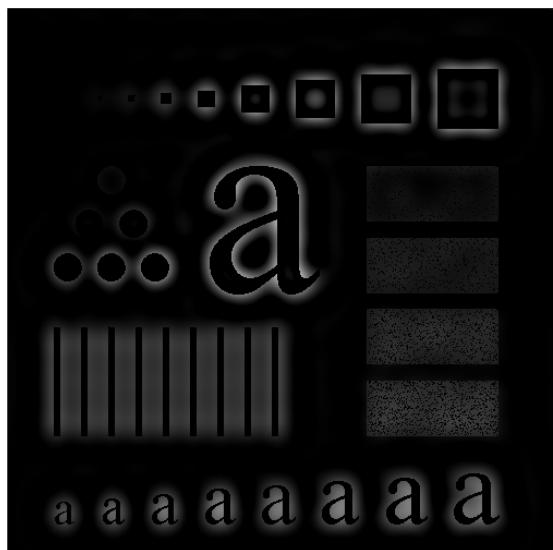


FIGURE C.24 – Butterworth high 15

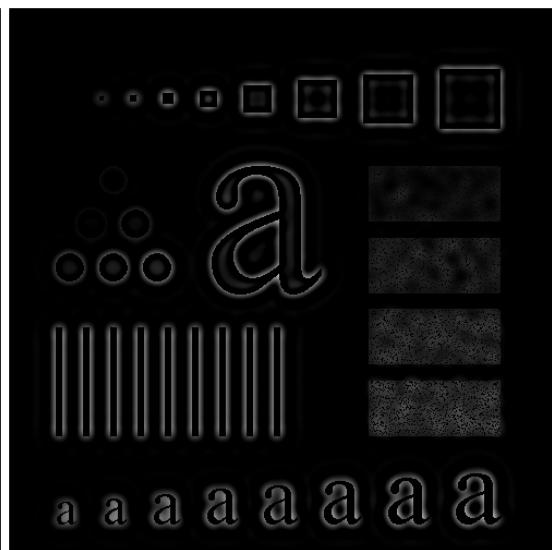
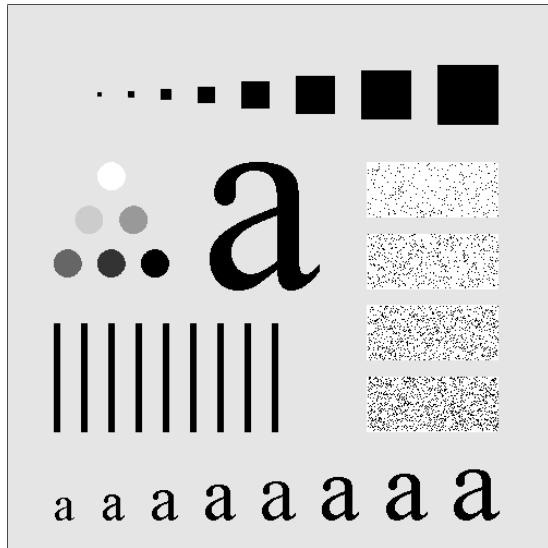


FIGURE C.25 – Butterworth high 30

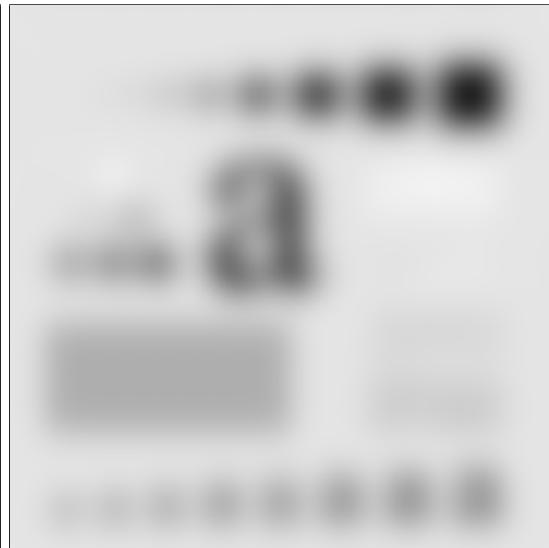
### C.3.5 Gaussian filter

#### Low pass

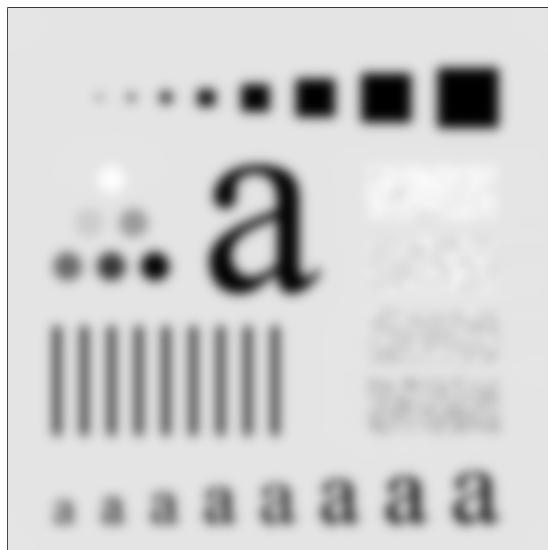
```
python problem3.py -gaussian -d 5 -low characters_test_pattern.tif
```



**FIGURE C.26** – Original image



**FIGURE C.27** – Gaussian low 5



**FIGURE C.28** – Gaussian low 15



**FIGURE C.29** – Gaussian low 30

**High pass**

```
python problem3.py -gaussian -d 5 -high characters_test_pattern.tif
```

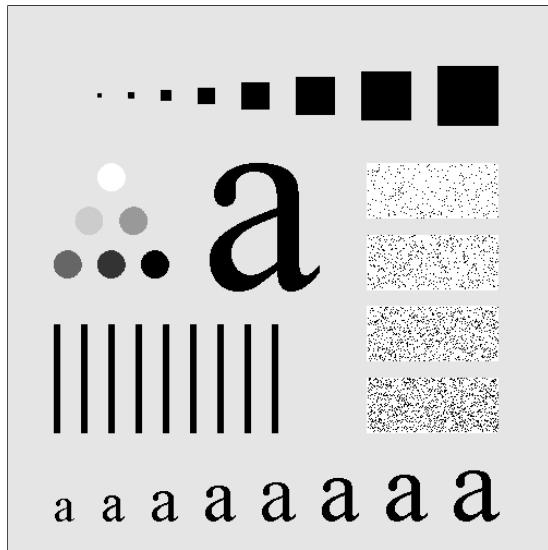


FIGURE C.30 – Original image

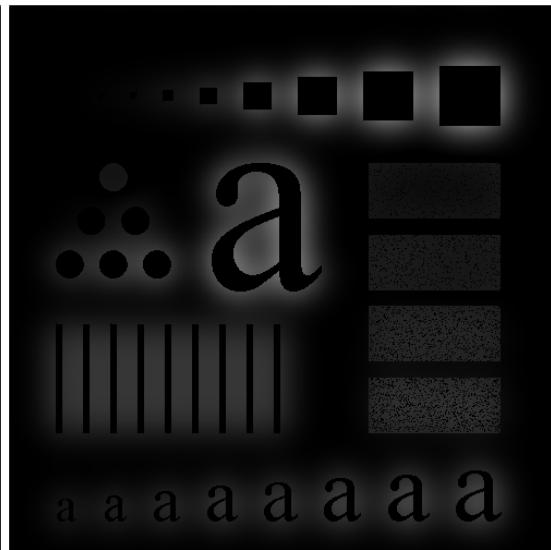


FIGURE C.31 – Gaussian high 5

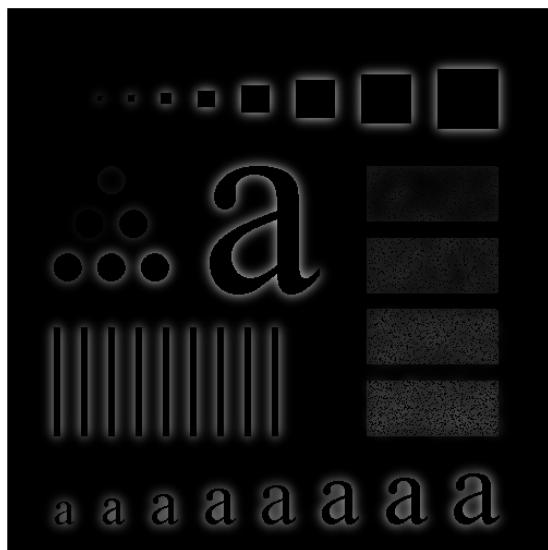


FIGURE C.32 – Gaussian high 15

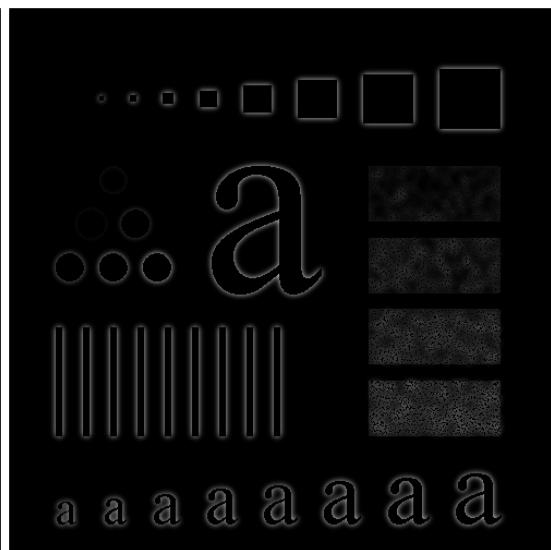


FIGURE C.33 – Gaussian high 30

# D. Noise generation and noise reduction

## D.1 Problem statement

In this problem, you are required to write a program to generate different types of random noises started from the Uniform noise and Gaussian noise.

And then add some of these noises to the circuit image and investigate the different mean filters and order statistics as the textbook did at pages 344-352.

## D.2 Python implementation

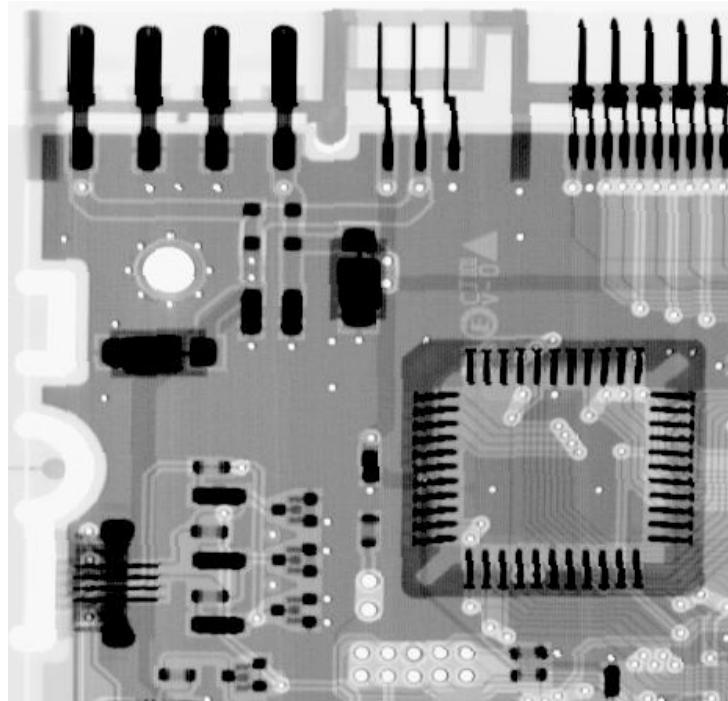
```
Usage : problem4.py [-h] (-uniform | -gaussian) [-histogram]
[-arithmetic] [-geometric] [-harmonic] [-contraharmonic] [-q Q]
[-median] [-max] [-min] [-midpoint] [-alpha] [-d D]
image_path
```

Use **python problem4.py -h** to see the help.

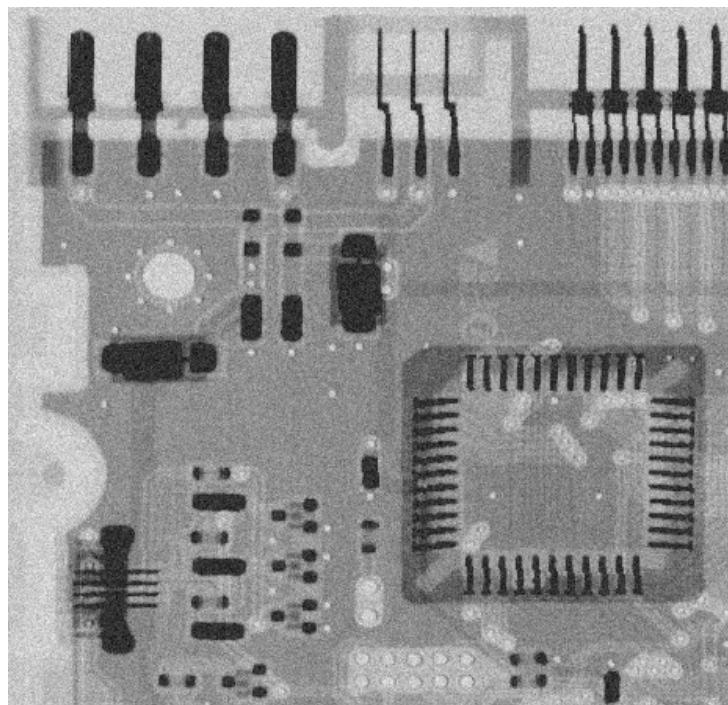
## D.3 Gaussian noise

### D.3.1 Noise generation and histogram

```
python problem4.py -gaussian circuit.tif
```

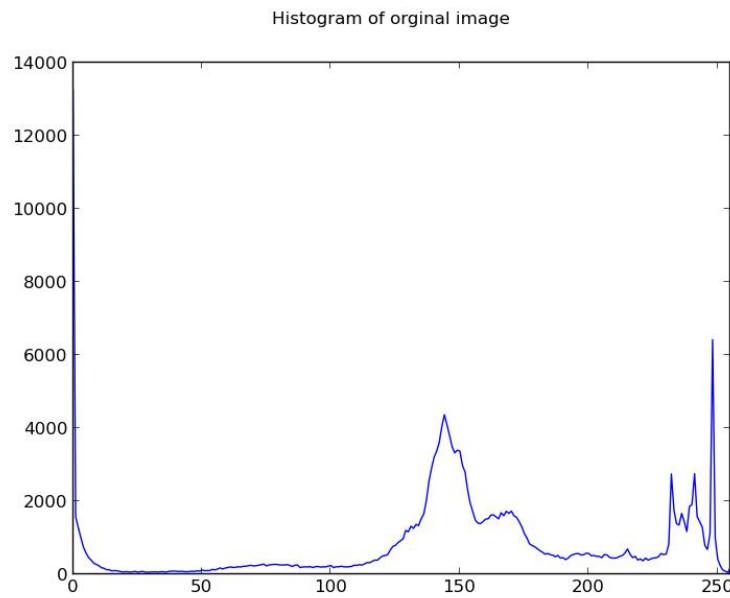


**FIGURE D.1** – Original image

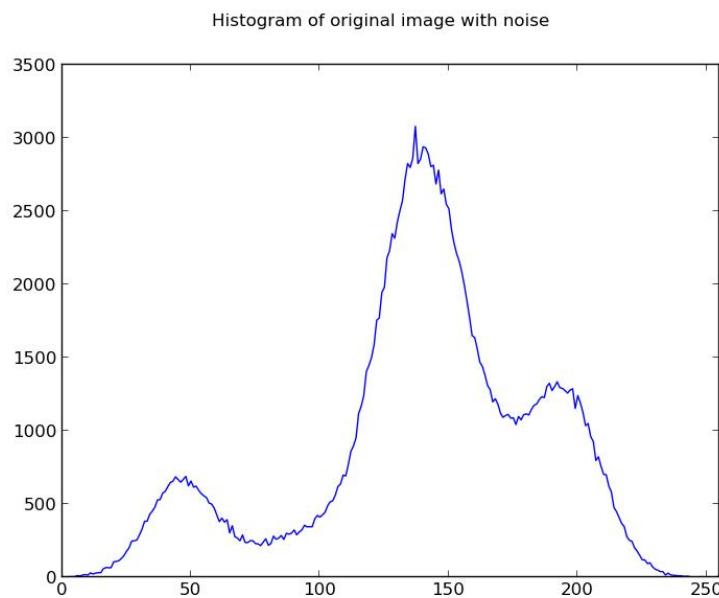


**FIGURE D.2** – Image + Gaussian noise ( $\mu = 0, \sigma = 20$ )

```
python problem4.py -gaussian -histogram circuit.tif
```



**FIGURE D.3** – Histogram of original image



**FIGURE D.4** – Histogram of image with Gaussian noise

### D.3.2 Noise reduction

#### Mean filters

```
python problem4.py -gaussian -arithmetic circuit.tif  
python problem4.py -gaussian -geometric circuit.tif
```

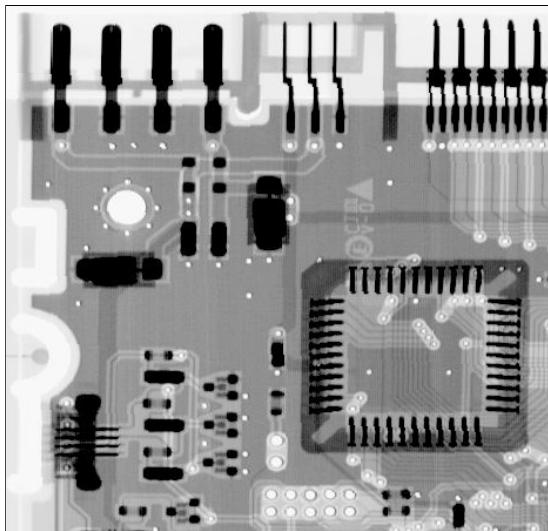


FIGURE D.5 – Original image

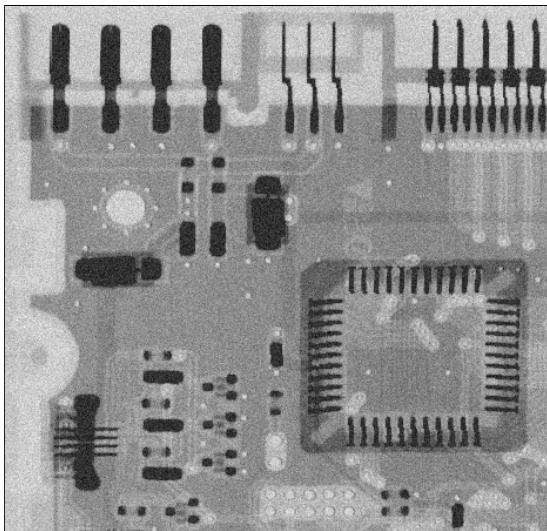


FIGURE D.6 – Image + Gaussian

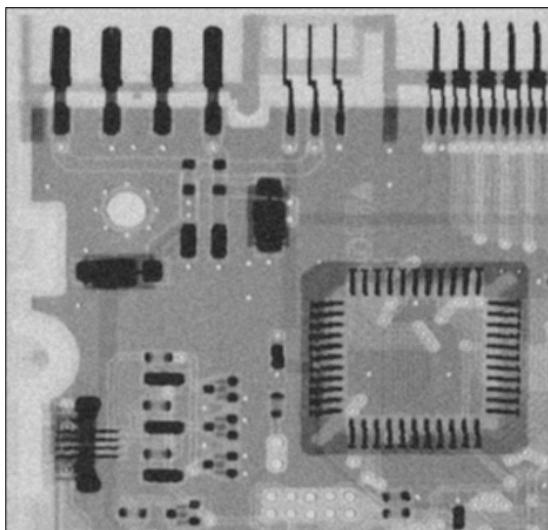


FIGURE D.7 – Arithmetic filter

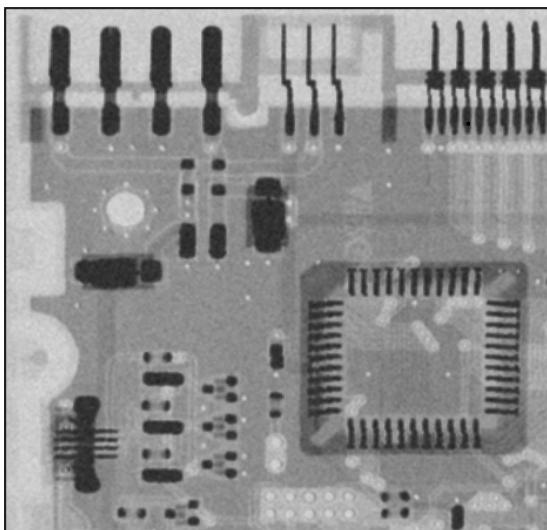
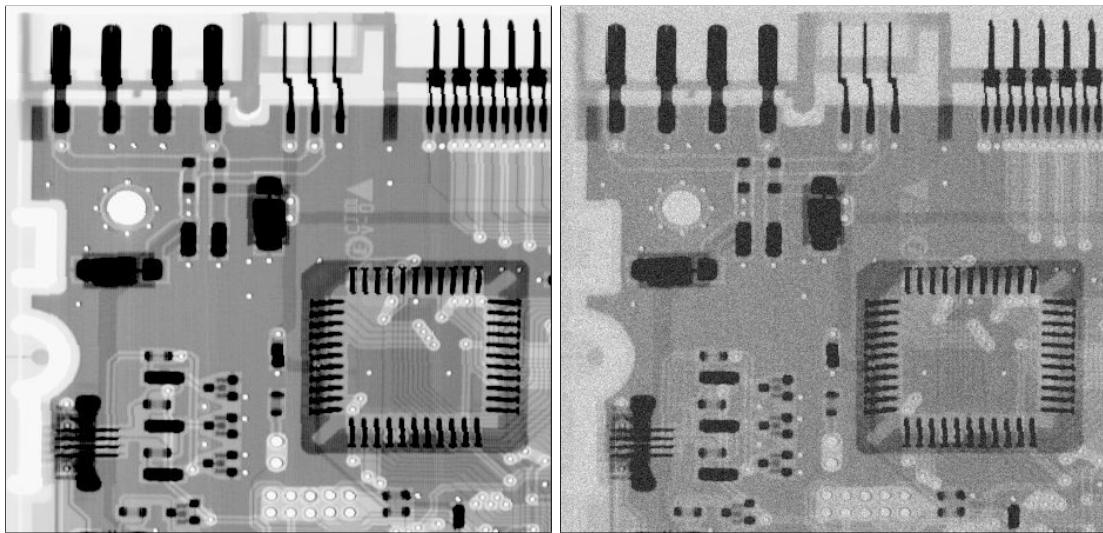


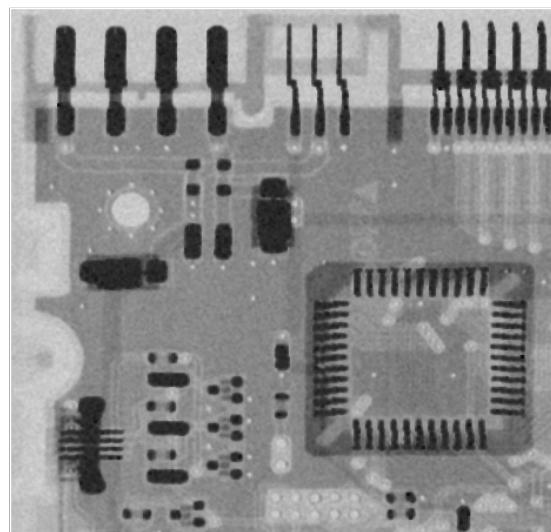
FIGURE D.8 – Geometric filter

```
python problem4.py -gaussian -harmonic circuit.tif
```



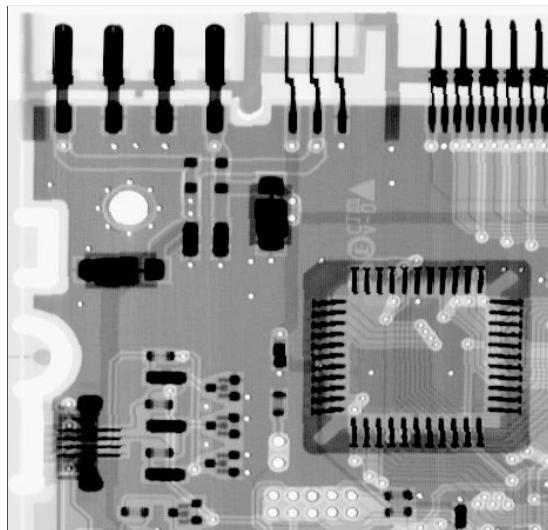
**FIGURE D.9** – Original image

**FIGURE D.10** – Image + Gaussian

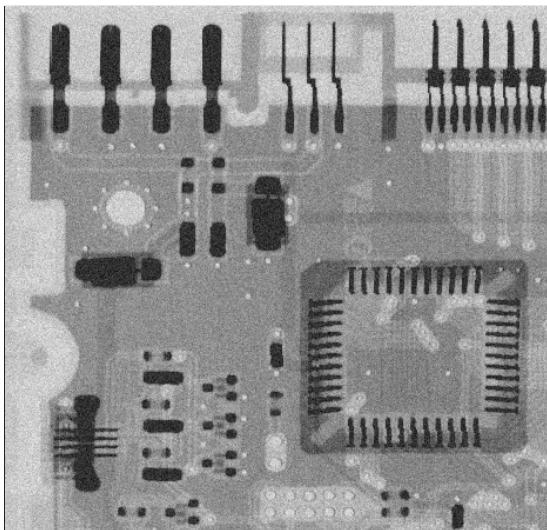


**FIGURE D.11** – Harmonic filter

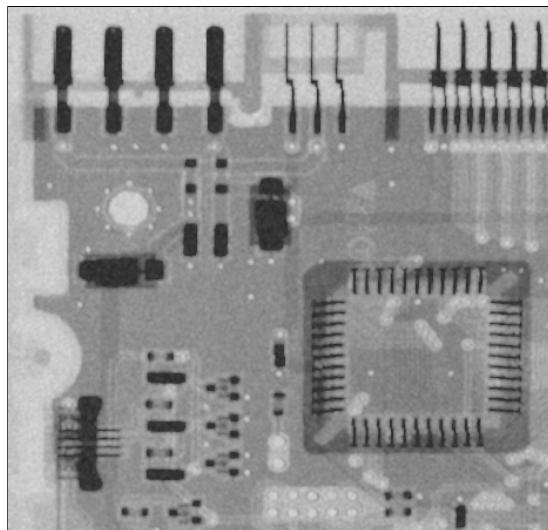
```
python problem4.py -gaussian -contraharmonic -q 1.5 circuit.tif  
python problem4.py -gaussian -contraharmonic -q -1.5 circuit.tif
```



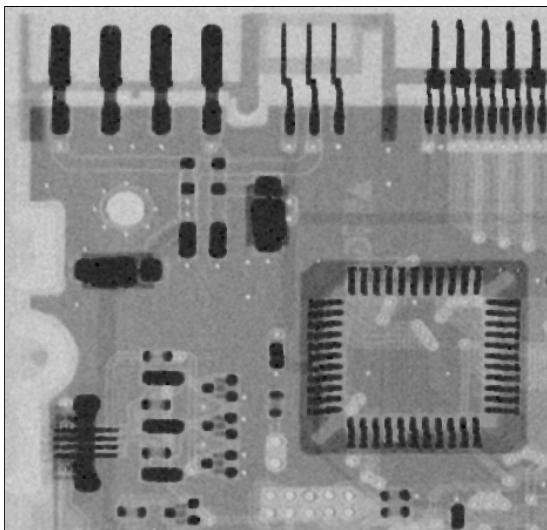
**FIGURE D.12** – Original image



**FIGURE D.13** – Image + Gaussian



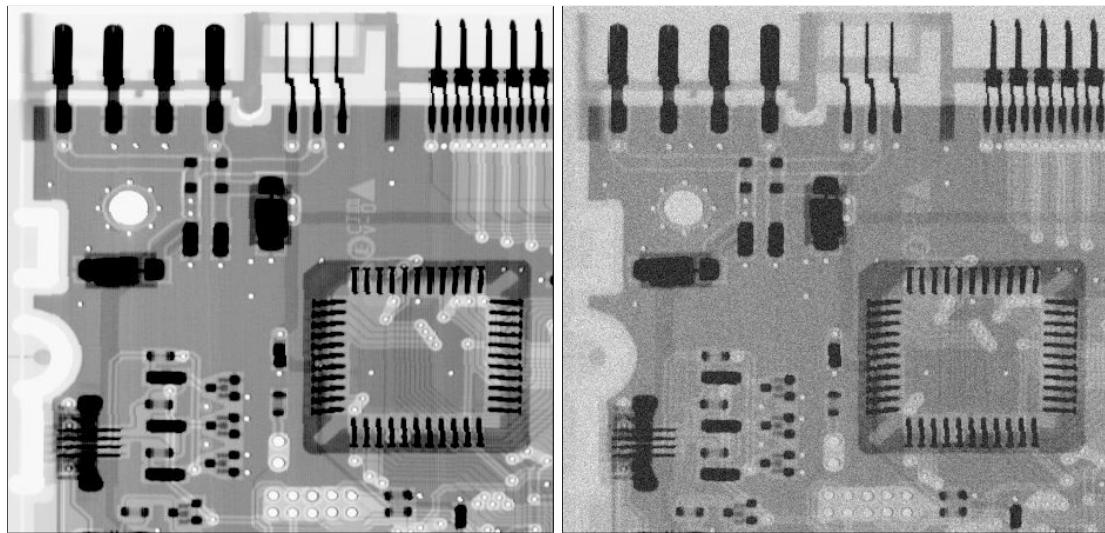
**FIGURE D.14** – Contra-harmonic filter (Q=1.5)



**FIGURE D.15** – Contra-harmonic filter (Q=-1.5)

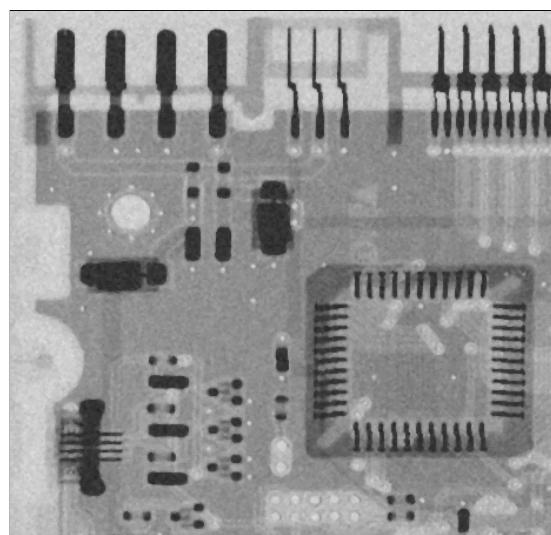
**Order-Statistic filters**

```
python problem4.py -gaussian -median circuit.tif
```



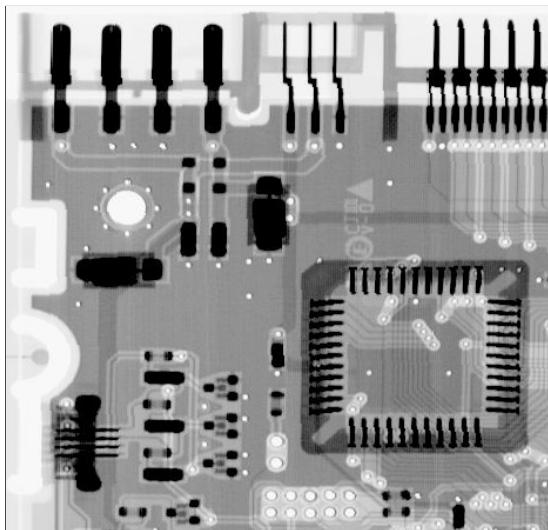
**FIGURE D.16** – Original image

**FIGURE D.17** – Image + Gaussian

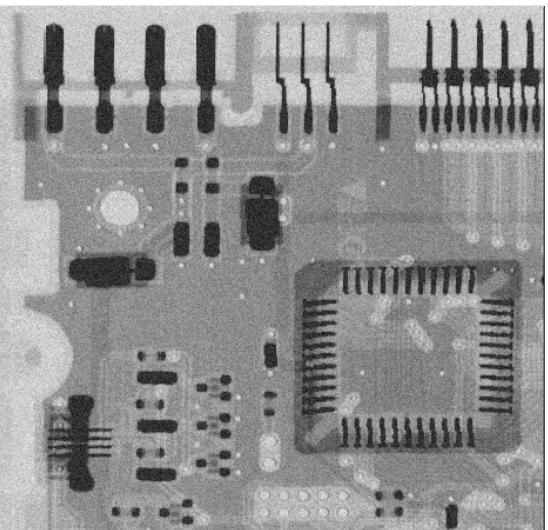


**FIGURE D.18** – Median filter

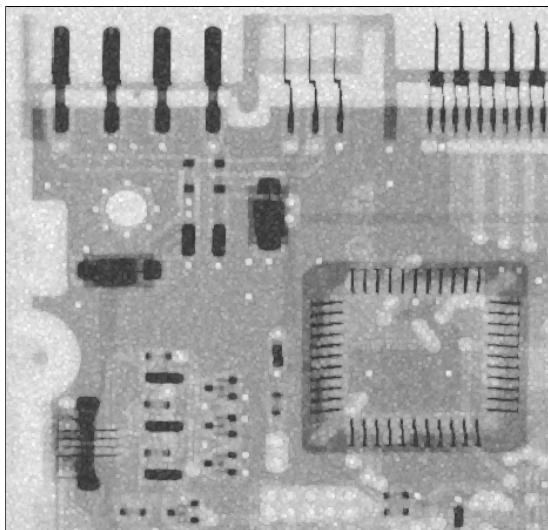
```
python problem4.py -gaussian -max circuit.tif  
python problem4.py -gaussian -min circuit.tif
```



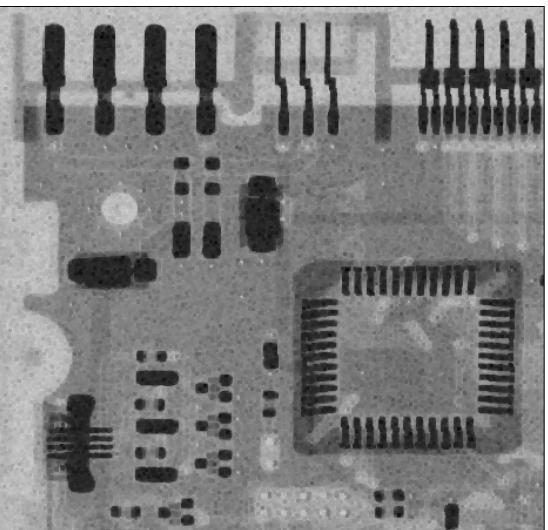
**FIGURE D.19** – Original image



**FIGURE D.20** – Image + Gaussian

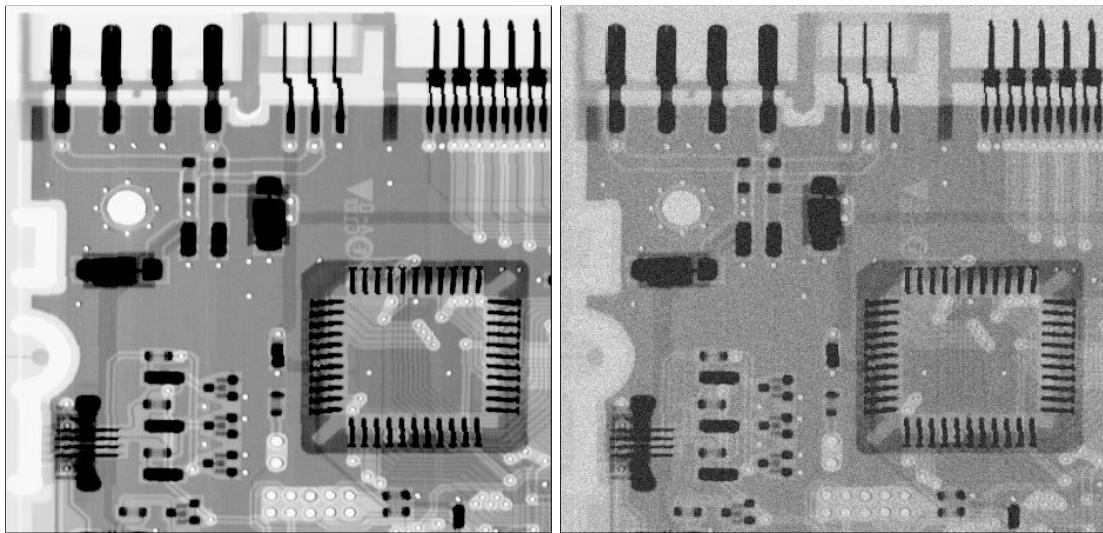


**FIGURE D.21** – Max filter



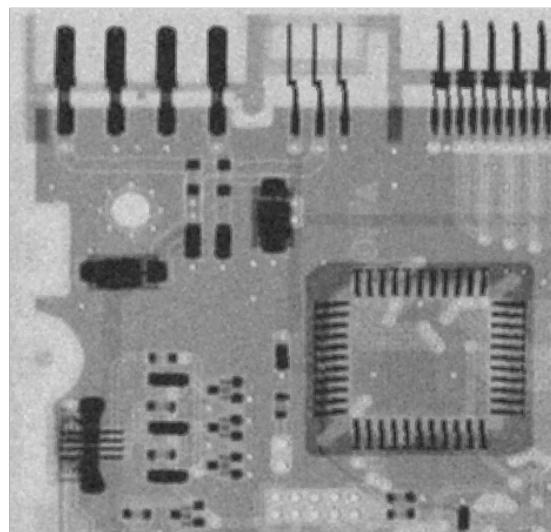
**FIGURE D.22** – Min filter

```
python problem4.py -gaussian -midpoint circuit.tif
```



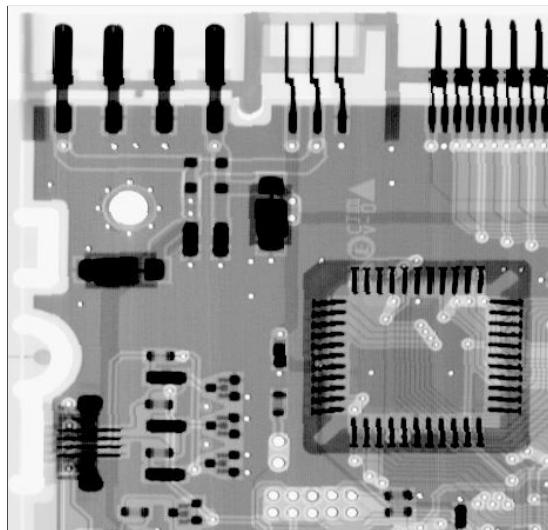
**FIGURE D.23** – Original image

**FIGURE D.24** – Image + Gaussian

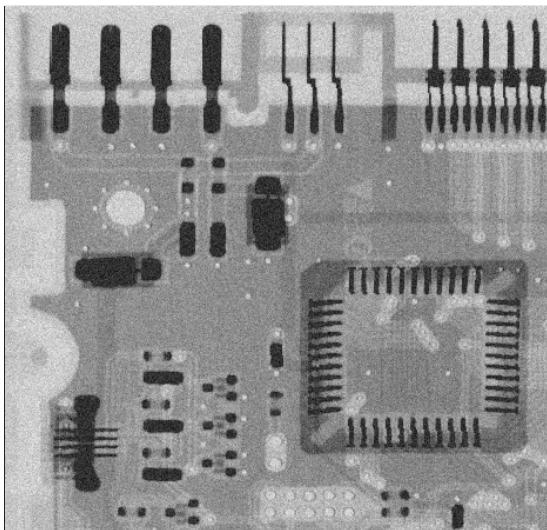


**FIGURE D.25** – Midpoint filter

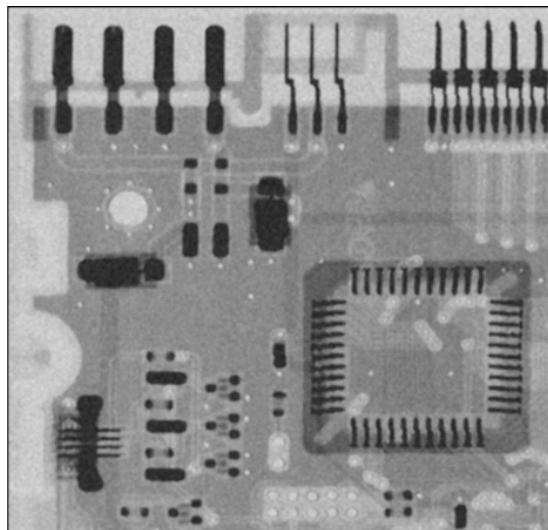
```
python problem4.py -gaussian -alpha -d 2 circuit.tif  
python problem4.py -gaussian -alpha -d 4 circuit.tif
```



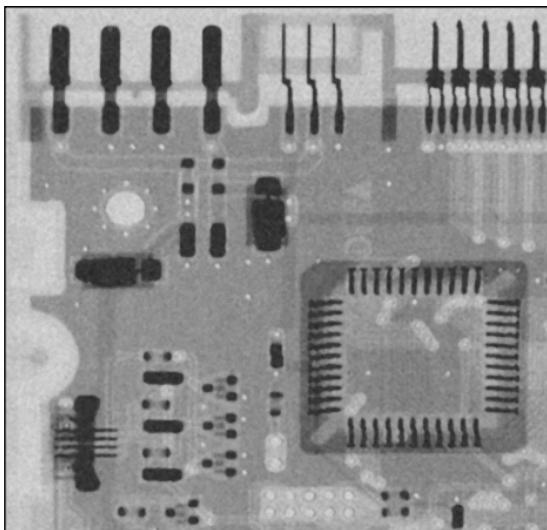
**FIGURE D.26** – Original image



**FIGURE D.27** – Image + Gaussian



**FIGURE D.28** – Alpha-trimmed filter  
( $d = 2$ )

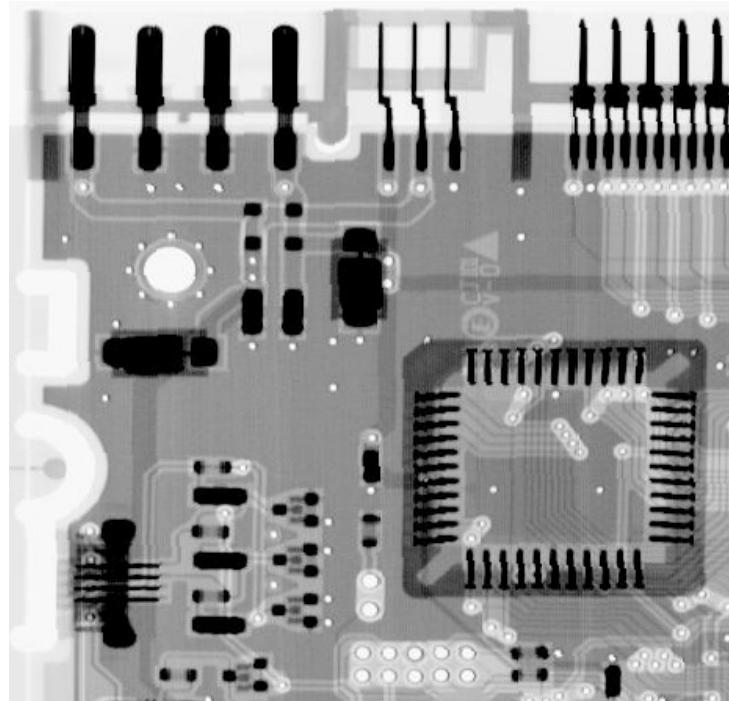


**FIGURE D.29** – Alpha-trimmed filter  
( $d = 4$ )

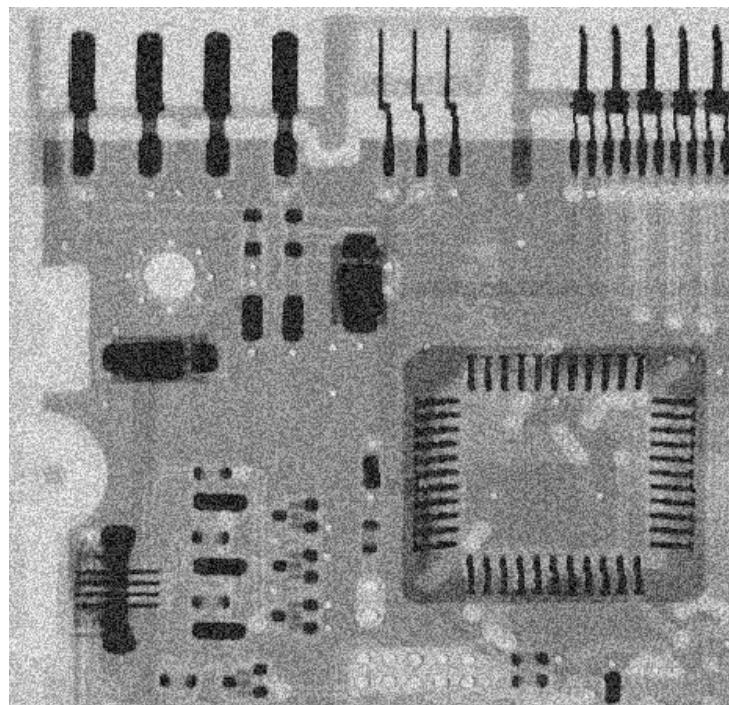
## D.4 Uniform noise

### D.4.1 Noise generation and histogram

```
python problem4.py -uniform circuit.tif
```

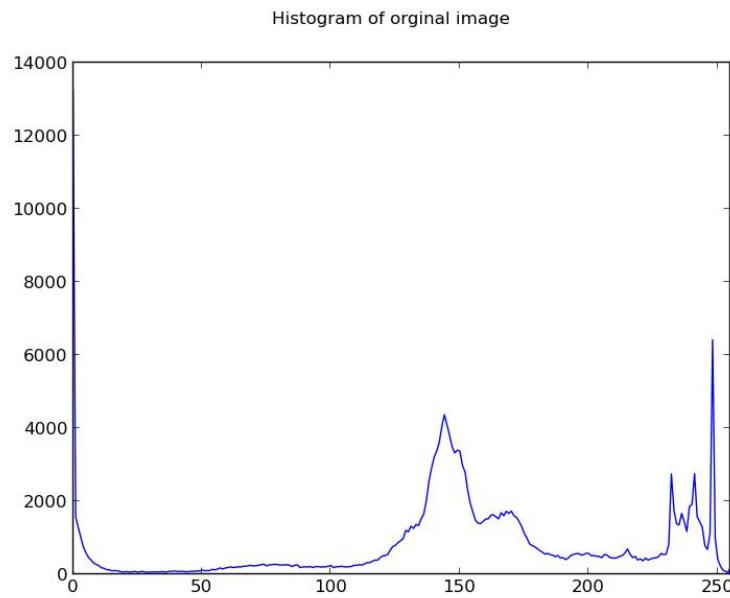


**FIGURE D.30** – Original image

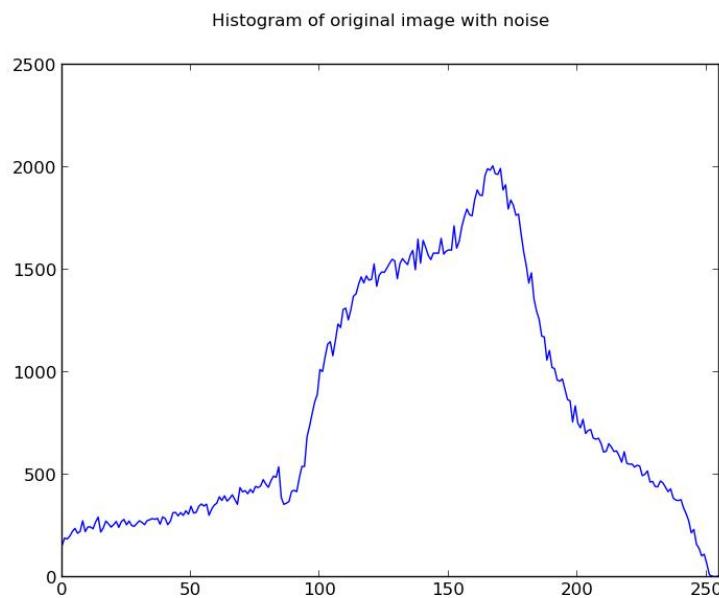


**FIGURE D.31** – Image + Uniform noise (min = 0, max = 128)

```
python problem4.py -uniform -histogram circuit.tif
```



**FIGURE D.32** – Histogram of original image

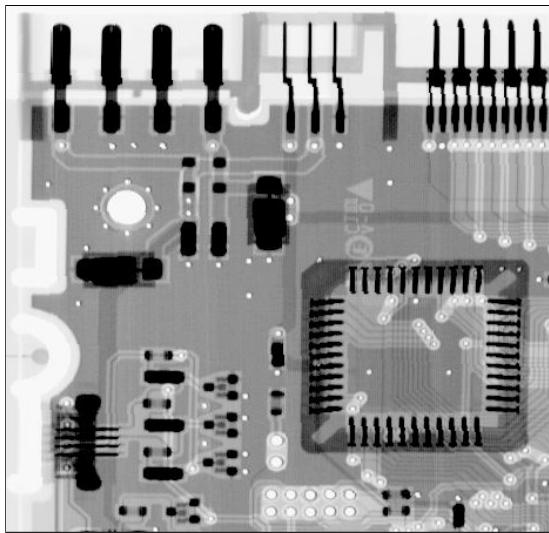


**FIGURE D.33** – Histogram of image with Uniform noise

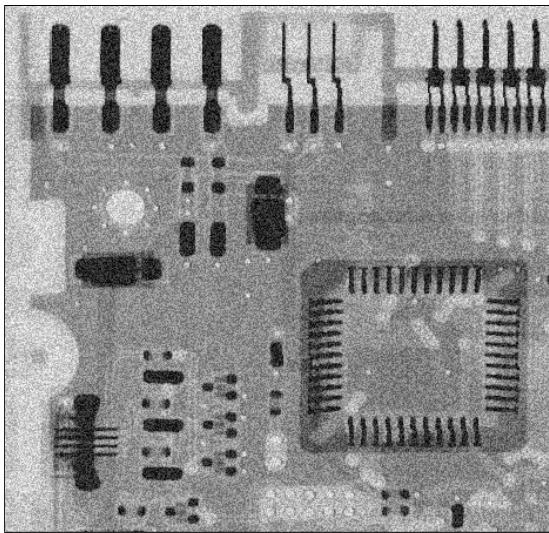
### D.4.2 Noise reduction

#### Mean filters

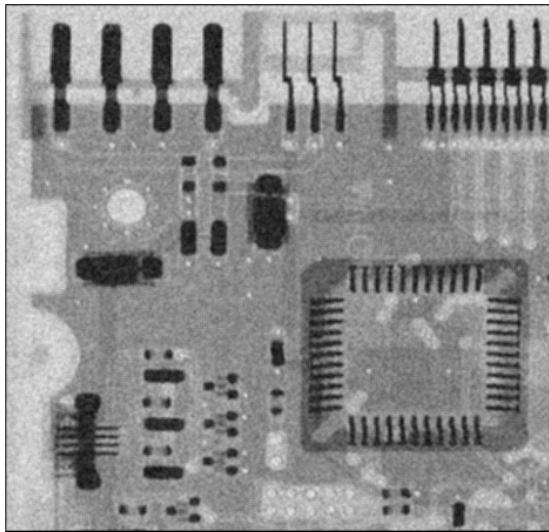
```
python problem4.py -uniform -arithmetic circuit.tif  
python problem4.py -uniform -geometric circuit.tif
```



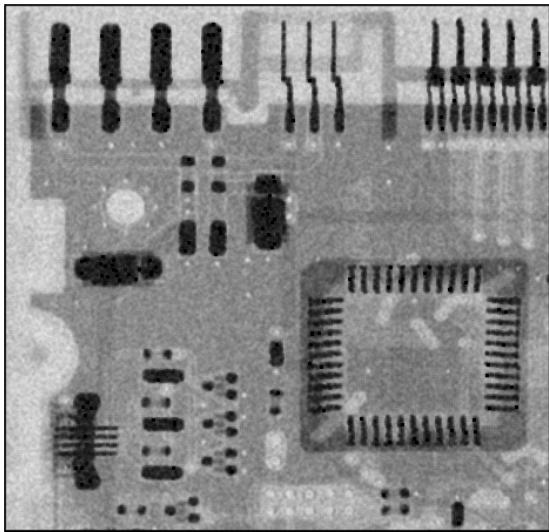
**FIGURE D.34** – Original image



**FIGURE D.35** – Image + Uniform

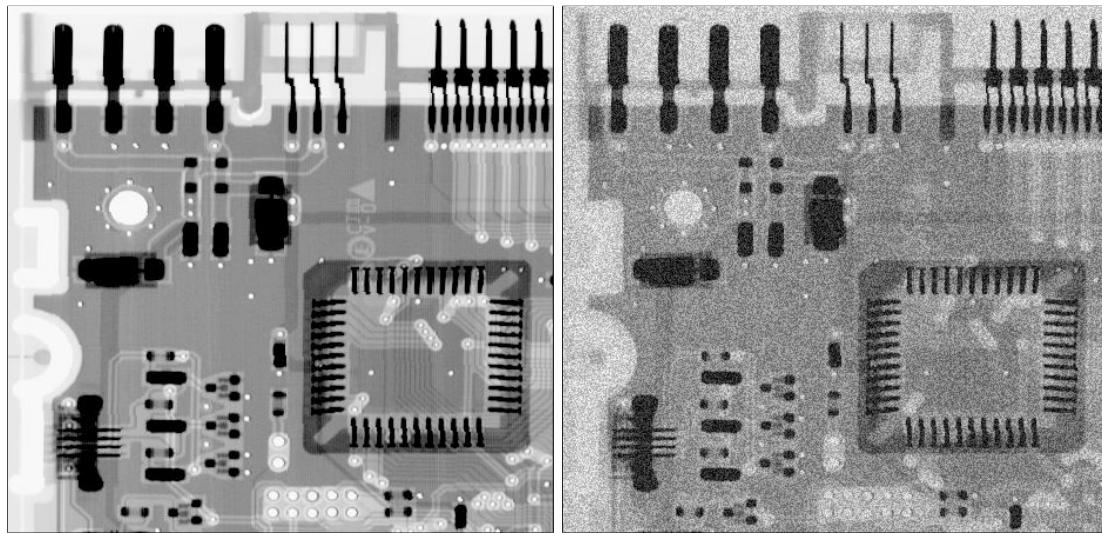


**FIGURE D.36** – Arithmetic filter



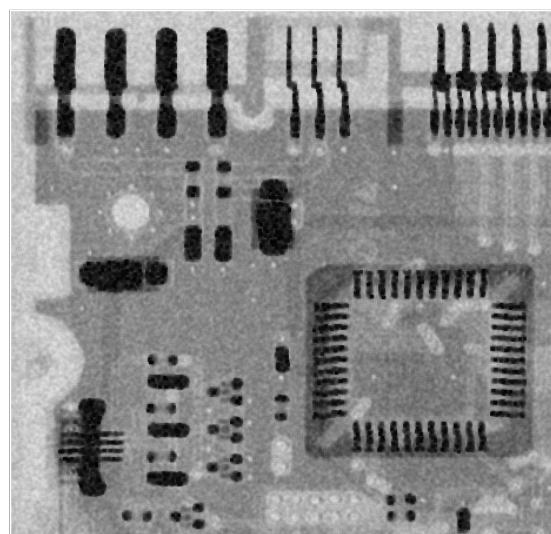
**FIGURE D.37** – Geometric filter

```
python problem4.py -uniform -harmonic circuit.tif
```



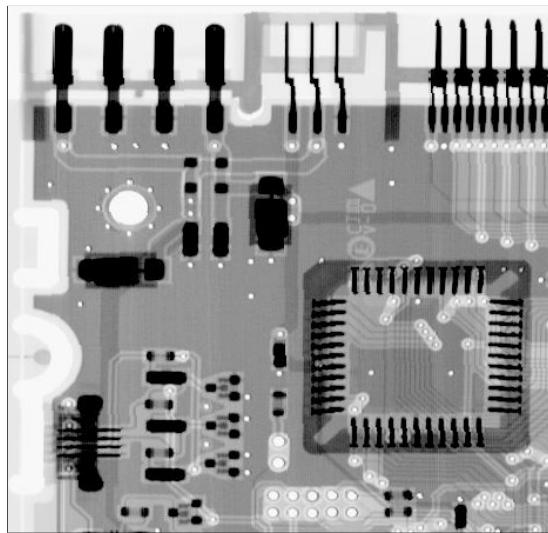
**FIGURE D.38** – Original image

**FIGURE D.39** – Image + Uniform

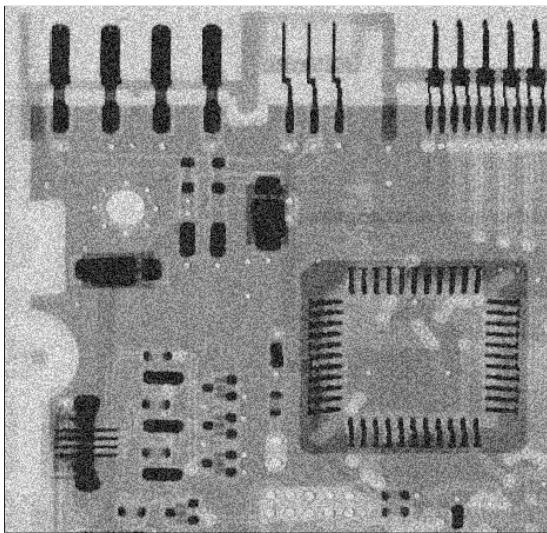


**FIGURE D.40** – Harmonic filter

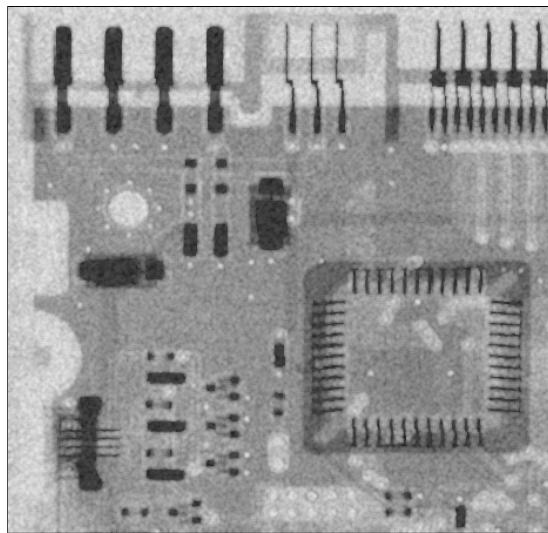
```
python problem4.py -uniform -contraharmonic -q 1.5 circuit.tif  
python problem4.py -uniform -contraharmonic -q -1.5 circuit.tif
```



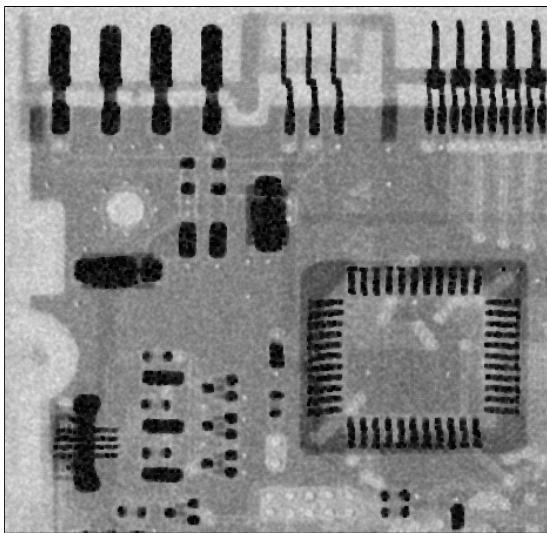
**FIGURE D.41** – Original image



**FIGURE D.42** – Image + Uniform



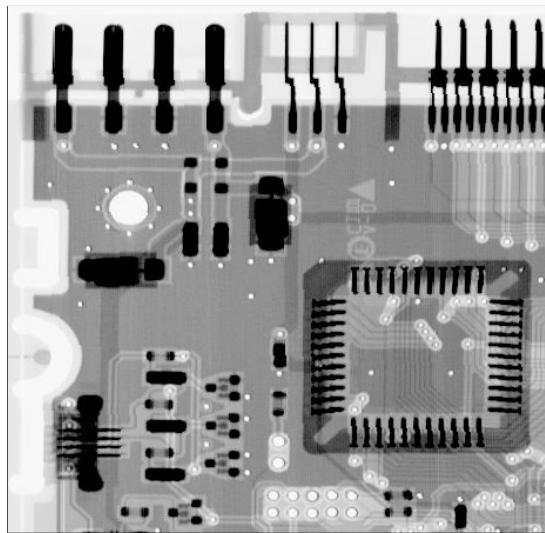
**FIGURE D.43** – Contra-harmonic filter (Q=1.5)



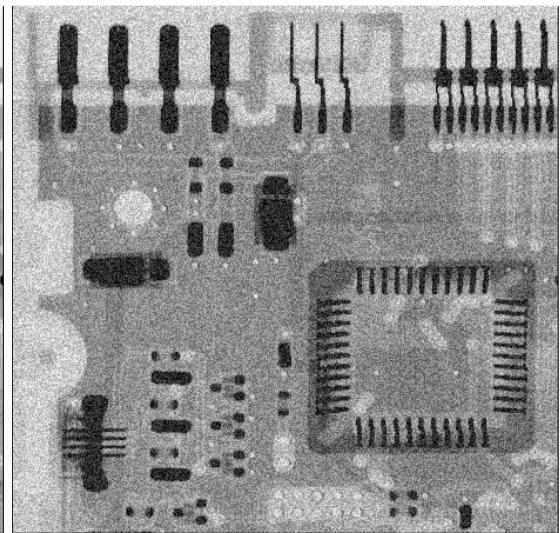
**FIGURE D.44** – Contra-harmonic filter (Q=-1.5)

**Order-Statistic filters**

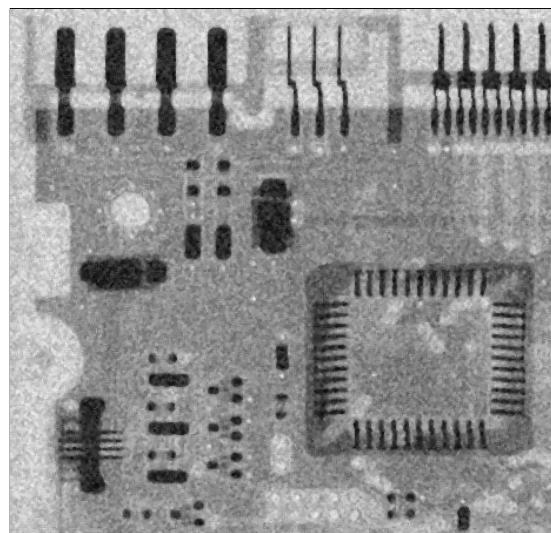
```
python problem4.py -uniform -median circuit.tif
```



**FIGURE D.45** – Original image

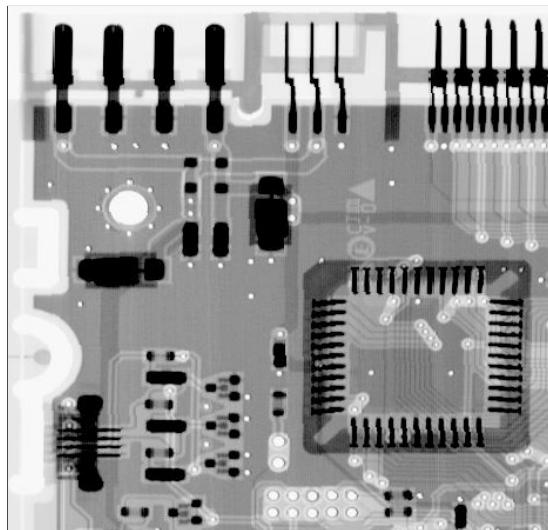


**FIGURE D.46** – Image + Uniform

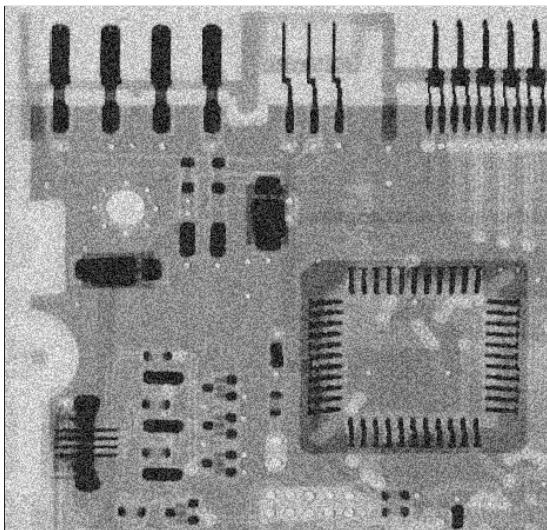


**FIGURE D.47** – Median filter

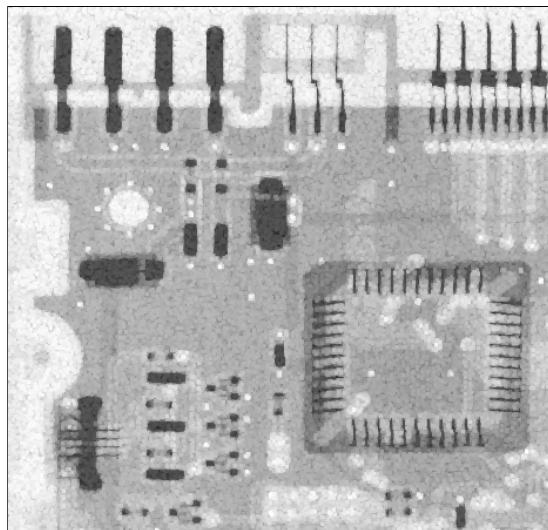
```
python problem4.py -uniform -max circuit.tif  
python problem4.py -uniform -min circuit.tif
```



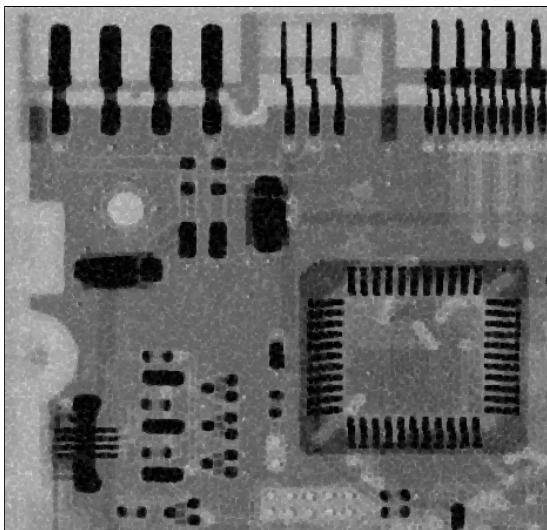
**FIGURE D.48** – Original image



**FIGURE D.49** – Image + Uniform

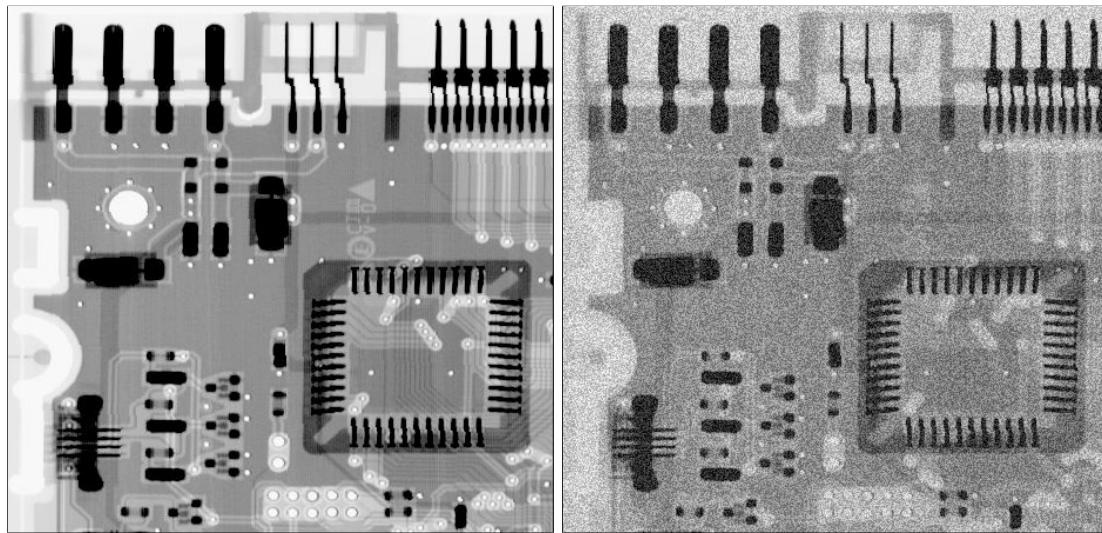


**FIGURE D.50** – Max filter



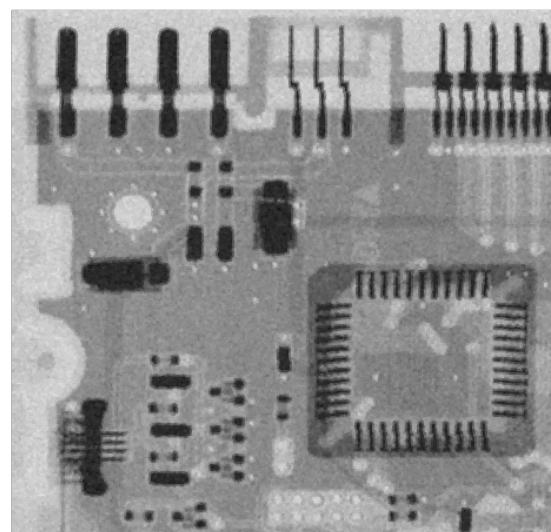
**FIGURE D.51** – Min filter

```
python problem4.py -uniform -midpoint circuit.tif
```



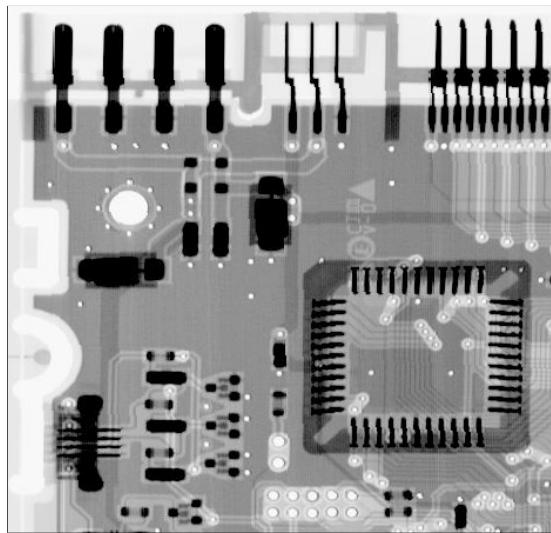
**FIGURE D.52** – Original image

**FIGURE D.53** – Image + Uniform

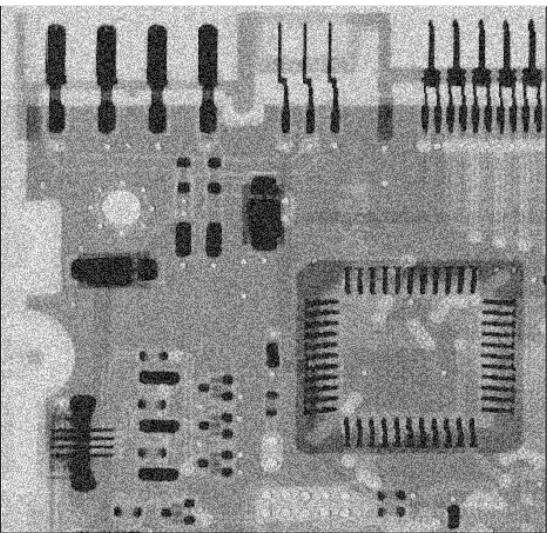


**FIGURE D.54** – Midpoint filter

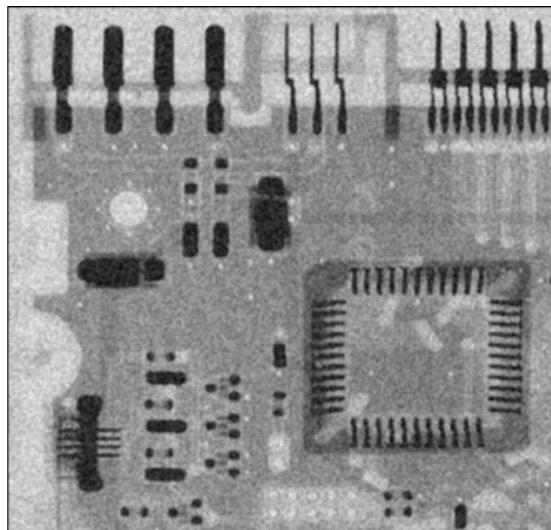
```
python problem4.py -uniform -alpha -d 2 circuit.tif  
python problem4.py -uniform -alpha -d 4 circuit.tif
```



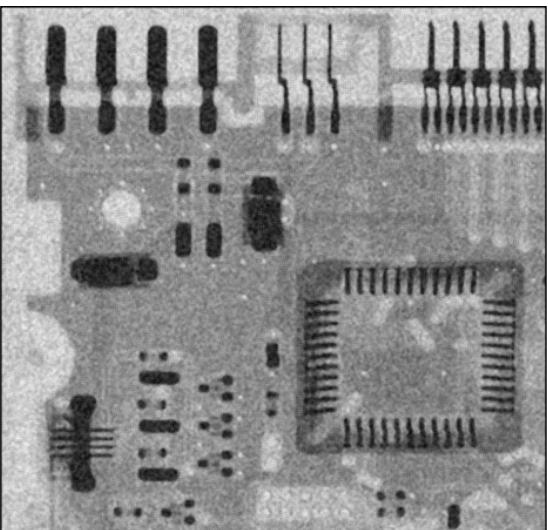
**FIGURE D.55** – Original image



**FIGURE D.56** – Image + Uniform



**FIGURE D.57** – Alpha-trimmed filter  
( $d = 2$ )



**FIGURE D.58** – Alpha-trimmed filter  
( $d = 4$ )

# E. Image restoration

## E.1 Problem statement

Suppose a blurring degradation function as

$$H(u, v) = T \times \text{sinc}(ua + vb) \times e^{-j\pi(ua+vb)} \quad (\text{E.1})$$

- (a) Implement a blurring filter using the equation above.
- (b) Blur the test image book\_cover.jpg using parameters  $a = b = 0.1$  and  $T = 1$ .
- (c) Add Gaussian noise of 0 mean and variance of 650 to the blurred image.
- (d) Restore the blurred image and the blurred noisy image using the inverse filter, Wiener deconvolution filter and the parametric Wiener filter, respectively.
- (e) Add Gaussian noise of 0 and different variances to the blurred image and repeat (d), investigate the performance of the Wiener deconvolution filter.

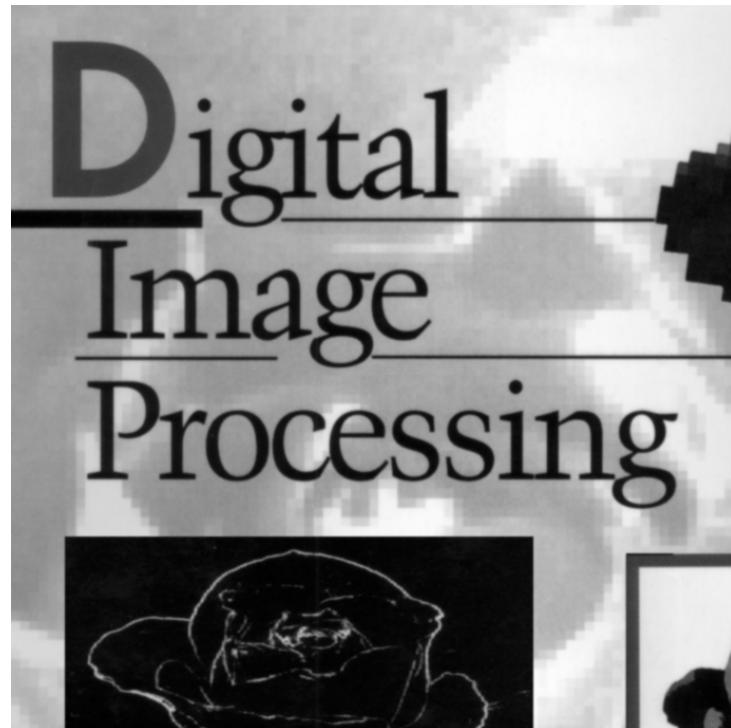
## E.2 Python implementation

```
Usage : problem5.py [-h] [-blurred BLURRED] [-noise] [-s S] [-inv]
[-wiener] [-a A] [-b B] [-T T] [-K K] image_path
```

Use **python problem5.py -h** to see the help.

### E.3 Blurring and noising

`python problem5.py book_cover.jpg`



**FIGURE E.1** – Original image



**FIGURE E.2** – Blurred image ( $a = b = 0.1; T = 1$ )

```
python problem5.py book_cover.jpg --noise -s 650
```

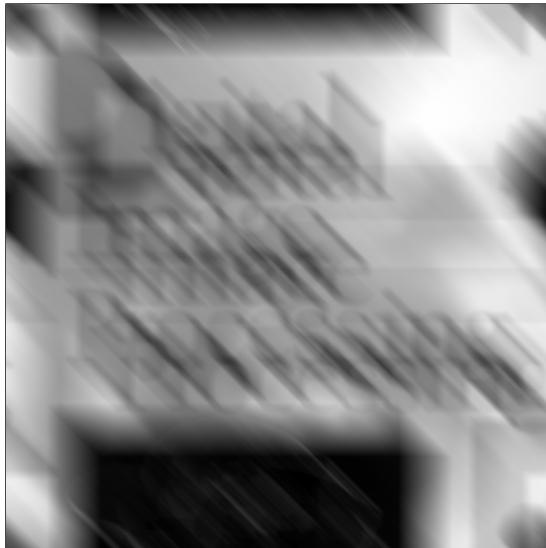


**FIGURE E.3** – Blur + Gaussian noise ( $\mu = 0, \sigma^2 = 650$ )

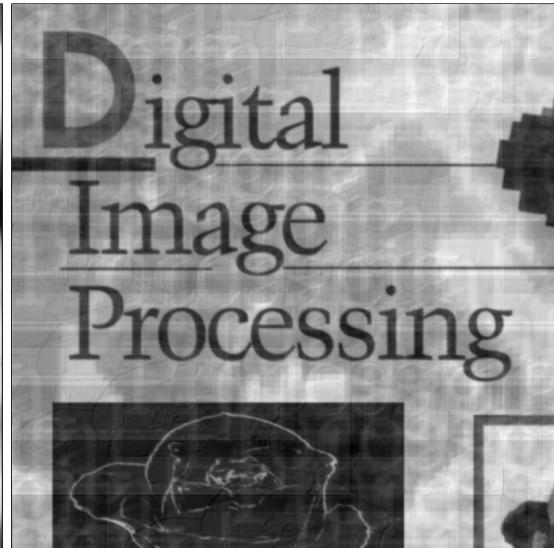
## E.4 Restoration

### E.4.1 Inverse filter

```
python problem5.py -inv book_cover.jpg  
python problem5.py -noise -s 650 -inv book_cover.jpg
```



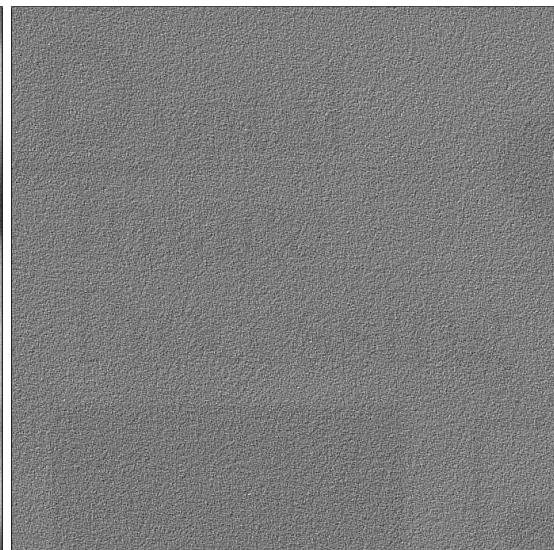
**FIGURE E.4 – Blurred image**



**FIGURE E.5 – Inverse blurred image**



**FIGURE E.6 – Blur + noise**



**FIGURE E.7 – Inverse 'blur + noise'**

The inverse filter is really affected by the noise because it ignores it (does not inverse it).

#### E.4.2 Wiener filter

```
python problem5.py --wiener book_cover.jpg  
python problem5.py --noise -s 650 --wiener book_cover.jpg
```



FIGURE E.8 – Blurred image

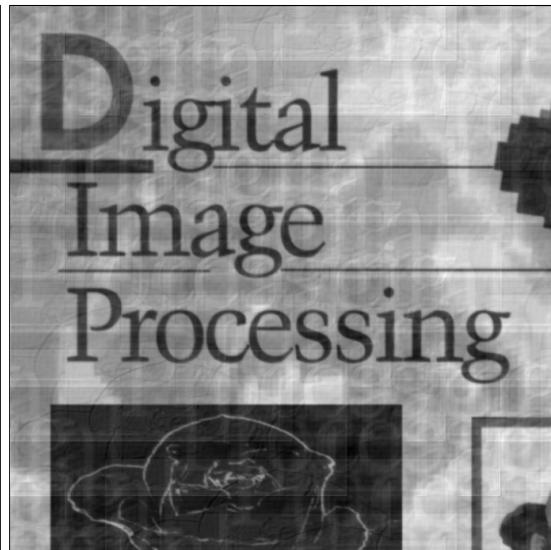


FIGURE E.9 – Wiener blurred image



FIGURE E.10 – Blur + noise



FIGURE E.11 – Wiener 'blur + noise'

The Wiener filter on the blurred image without noise is equivalent to the inverse filter (power spectrum of noise equals to 0).

The Wiener filter is more efficient to remove the noise as it takes it into consideration during the restoration process.

### E.4.3 Experimentations

Gaussian noise ( $\mu = 0, \sigma^2 = 300$ )

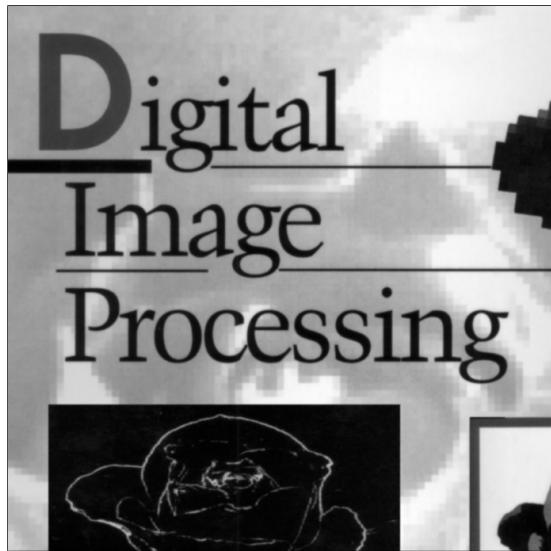


FIGURE E.12 – Original image

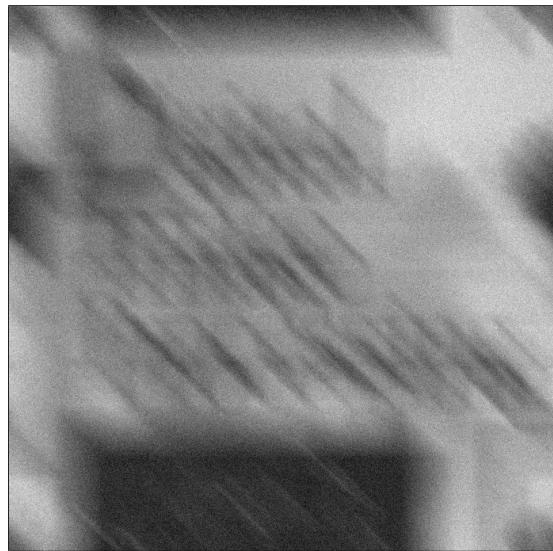


FIGURE E.13 – Blur + noise

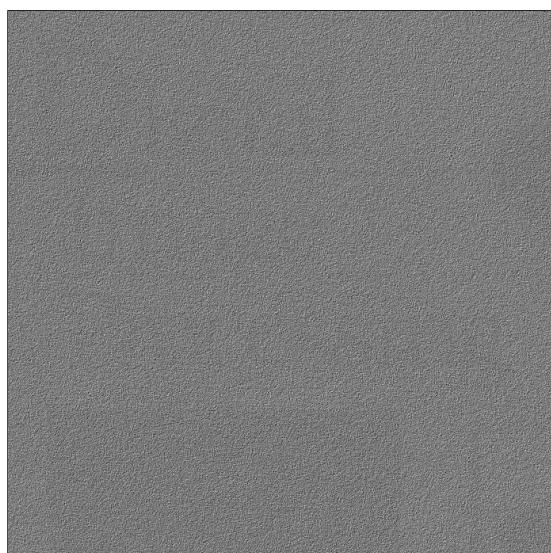


FIGURE E.14 – Inverse 'blur + noise'



FIGURE E.15 – Wiener 'blur + noise'

Gaussian noise ( $\mu = 0, \sigma^2 = 100$ )

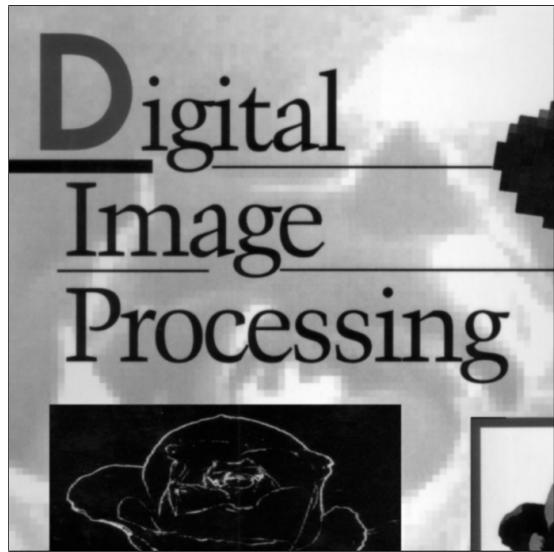


FIGURE E.16 – Original image



FIGURE E.17 – Blur + noise

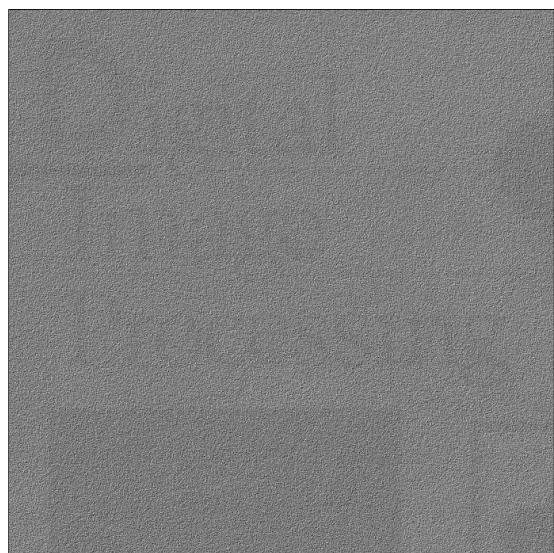


FIGURE E.18 – Inverse 'blur + noise'



FIGURE E.19 – Wiener 'blur + noise'

Gaussian noise ( $\mu = 0, \sigma^2 = 30$ )

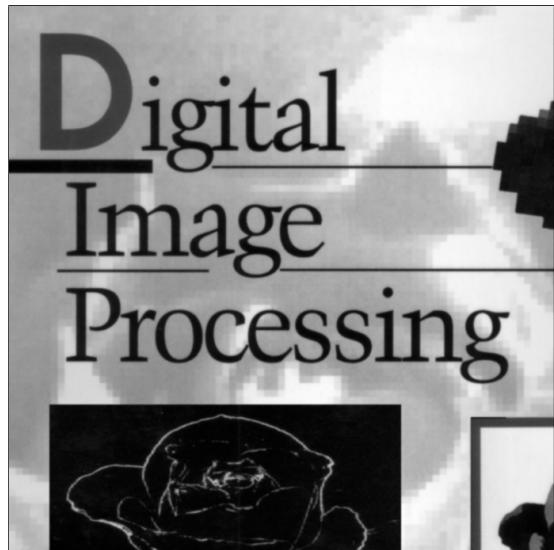


FIGURE E.20 – Original image



FIGURE E.21 – Blur + noise

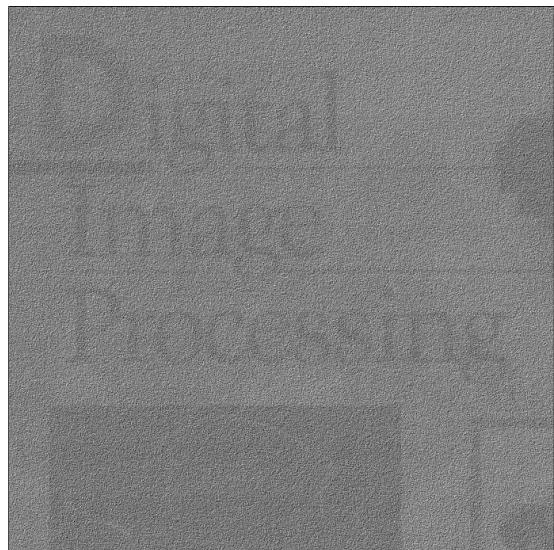


FIGURE E.22 – Inverse 'blur + noise'



FIGURE E.23 – Wiener 'blur + noise'

**Wiener performance**

**FIGURE E.24** – Wiener 'blur + noise ( $\sigma^2 = 30$ )'



**FIGURE E.25** – Wiener 'blur + noise ( $\sigma^2 = 100$ )'



**FIGURE E.26** – Inverse 'blur + noise ( $\sigma^2 = 300$ )'



**FIGURE E.27** – Wiener 'blur + noise ( $\sigma^2 = 650$ )'

# F. Geometric transforms

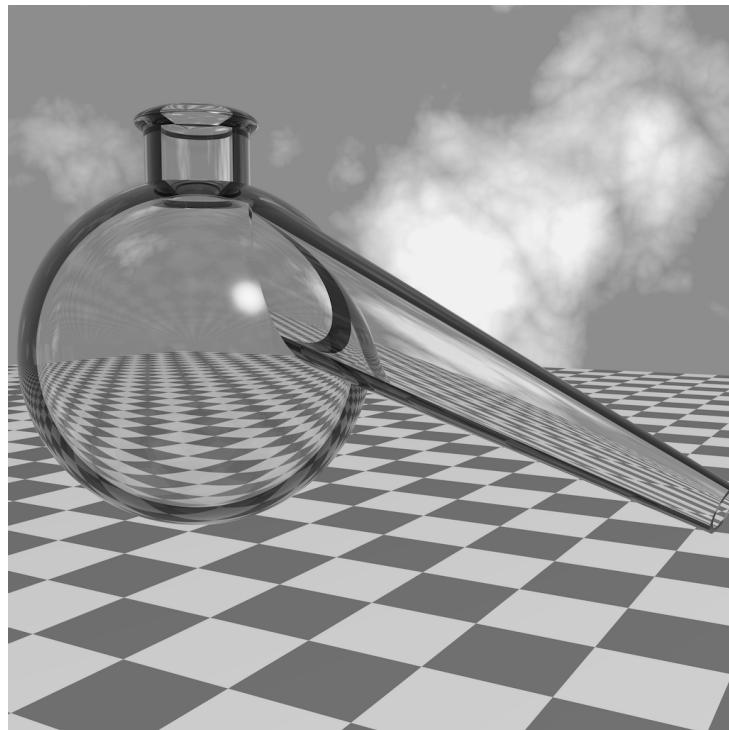
## F.1 Problem statement

Develop a geometric transform program that will rotate, translate, and scale an image by specified amounts, using the nearest neighbor and bilinear interpolation methods, respectively.

## F.2 Python implementation

```
Usage : problem6.py [-h] -i INPUT  
(-t TRANSLATE [TRANSLATE ...] | -r ROTATE | -s SCALE) (-nearest | -bilinear)  
[-ntruncate] [-debug]
```

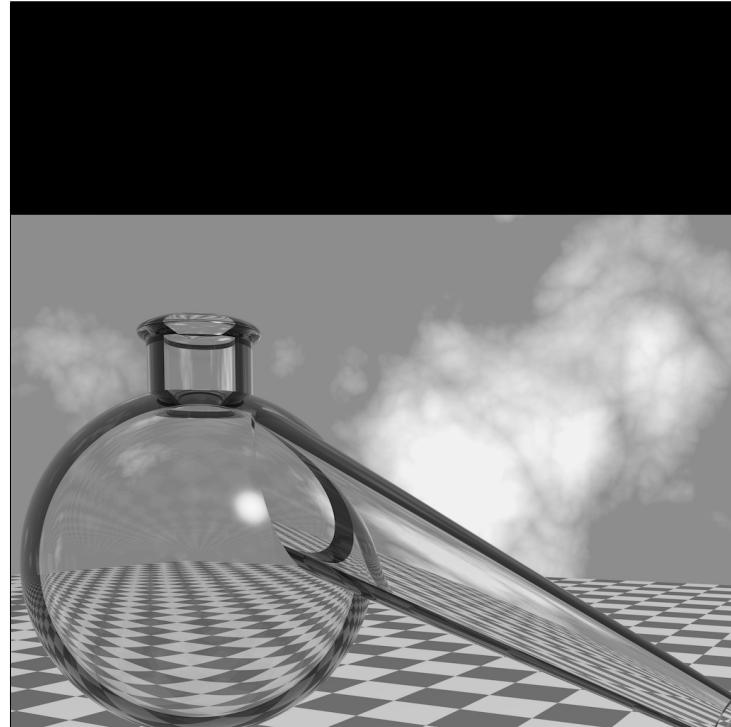
Use `python problem6.py -h` to see the help.



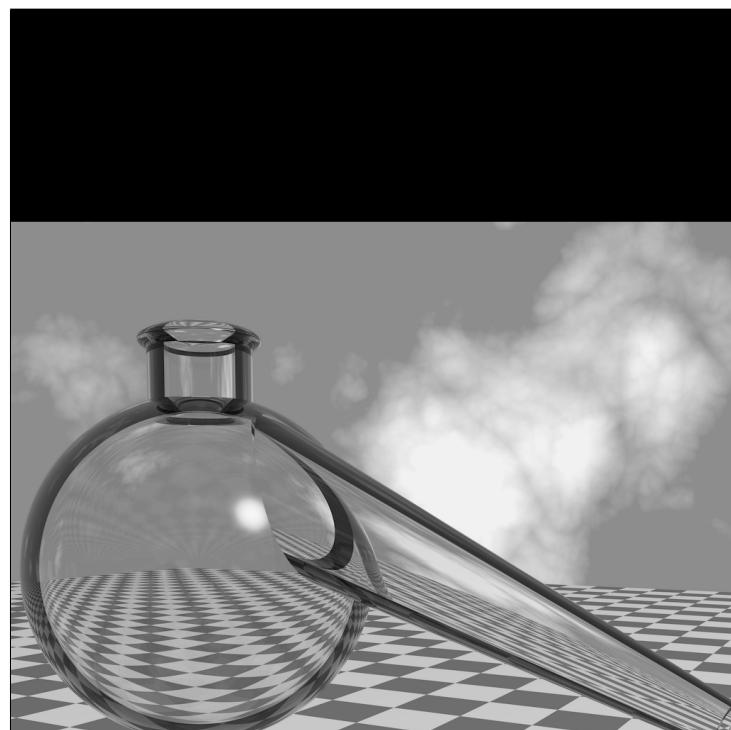
**FIGURE F.1** – Original image

### F.3 Translation

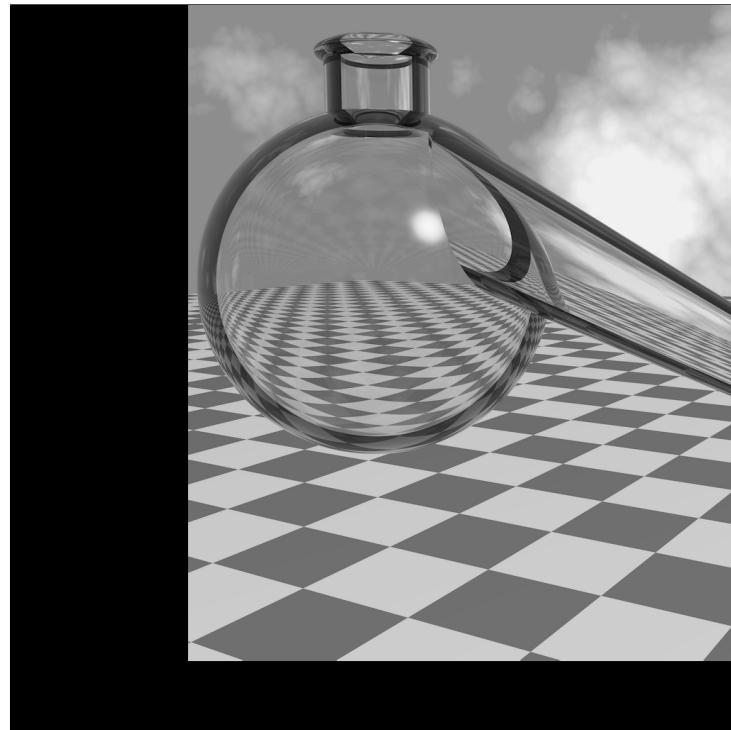
`python problem6.py -i ray_trace_bottle.tif -bilinear -t tx ty`, where  $(tx, ty)$  is the 2D translation vector.



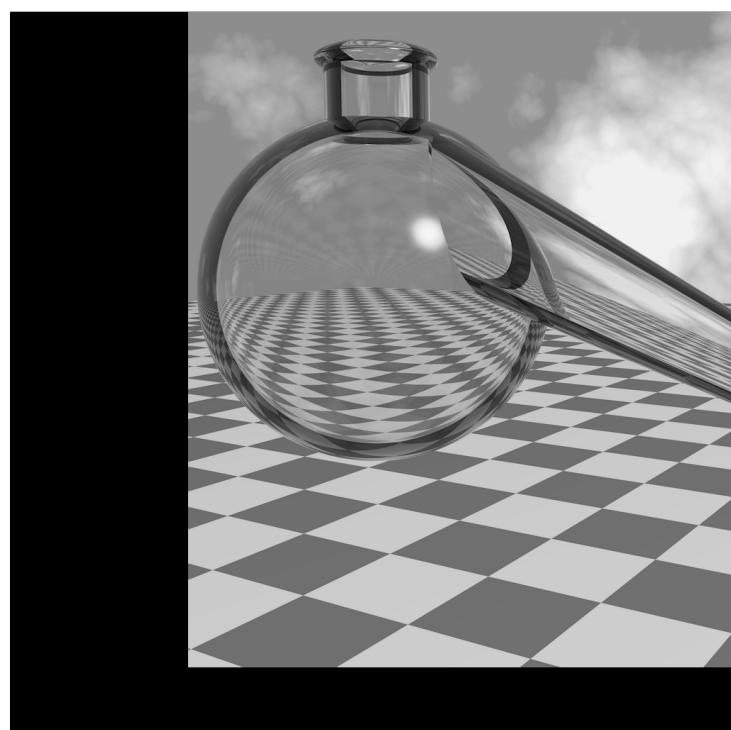
**FIGURE F.2** – Translation  $(0, 300)$  nearest



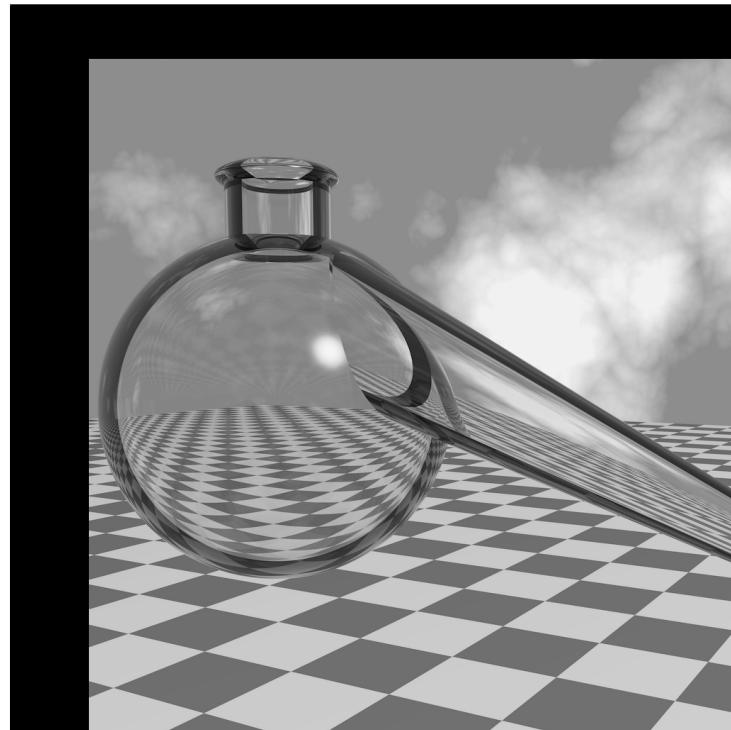
**FIGURE F.3** – Translate  $(0, 300)$  bilinear



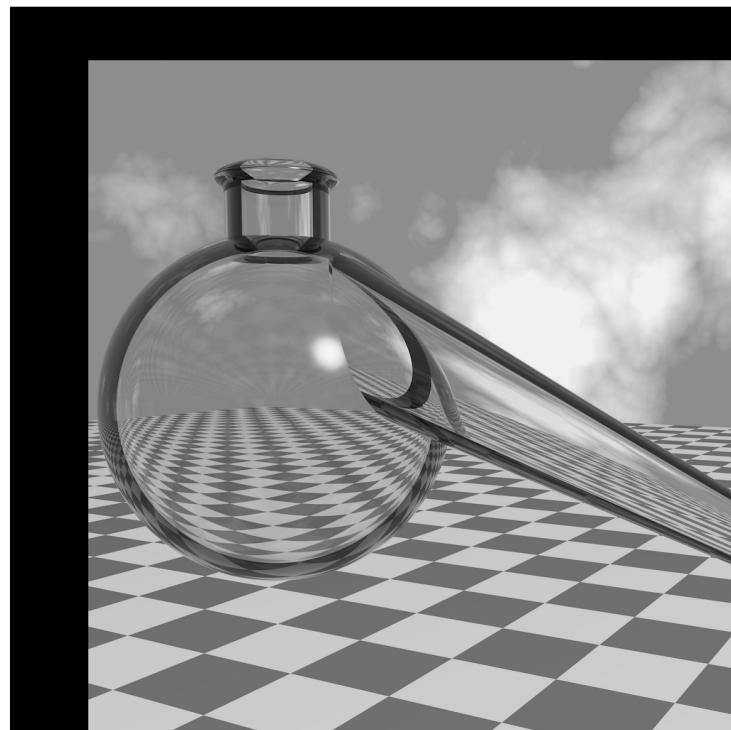
**FIGURE F.4** – Translation (250, -100) nearest



**FIGURE F.5** – Translate (250, -100) bilinear



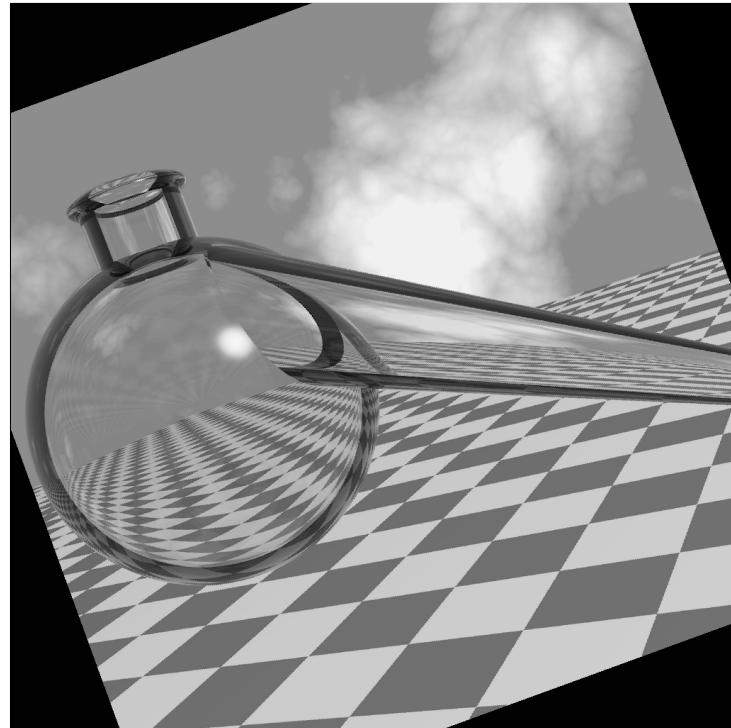
**FIGURE F.6** – Translation (109.8, 75.5) nearest



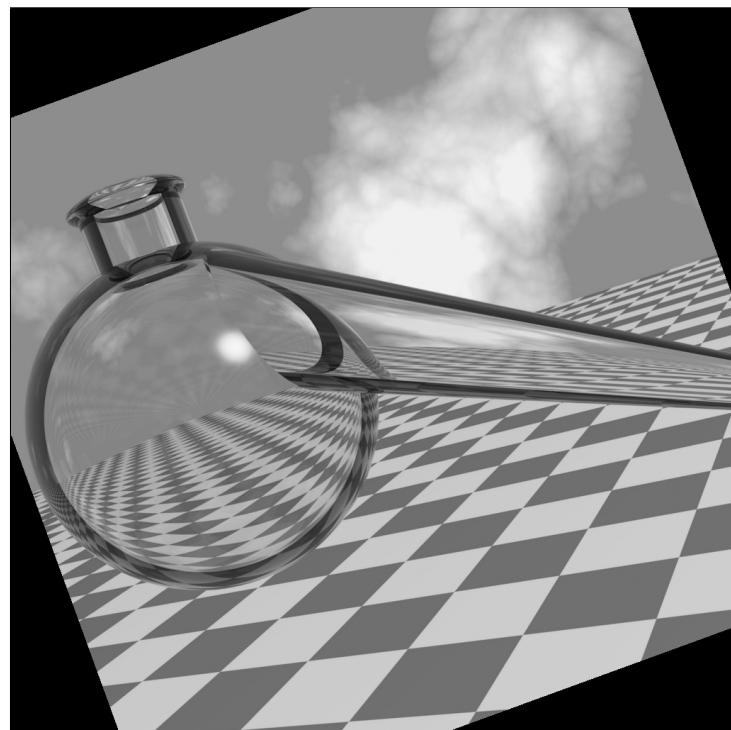
**FIGURE F.7** – Translation (109.8, 75.5) bilinear

## F.4 Rotation

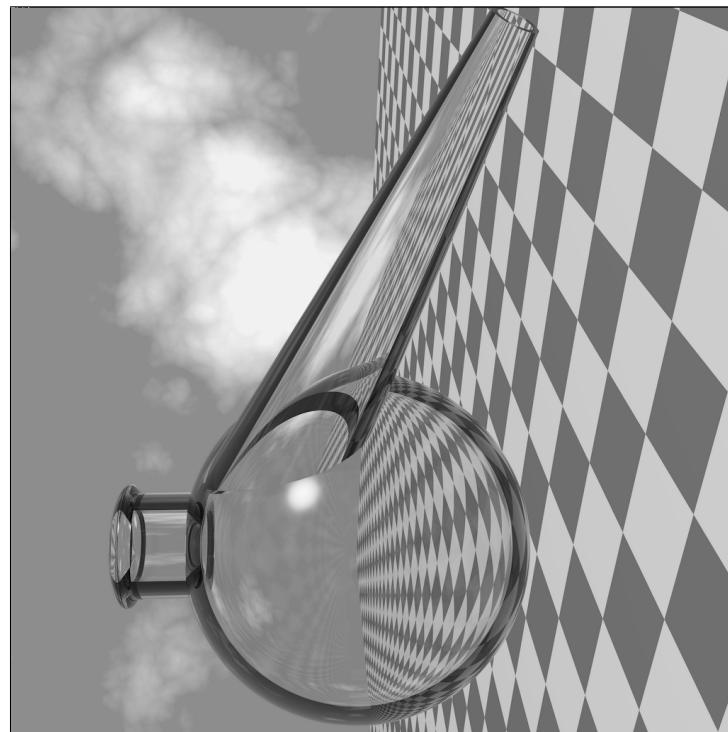
`python problem6.py -i ray_trace_bottle.tif -nearest -r theta`, where theta is the angle of rotation.



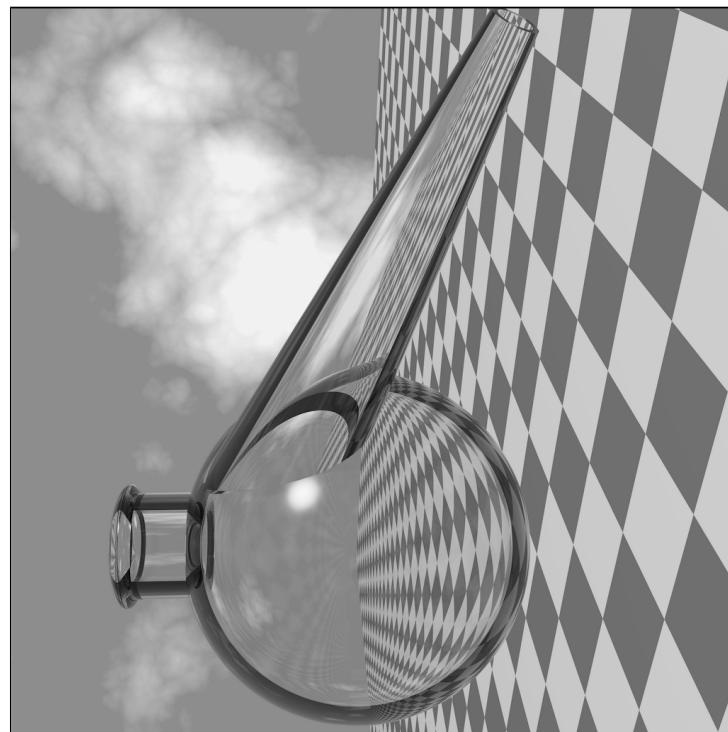
**FIGURE F.8** – Rotate 20° nearest



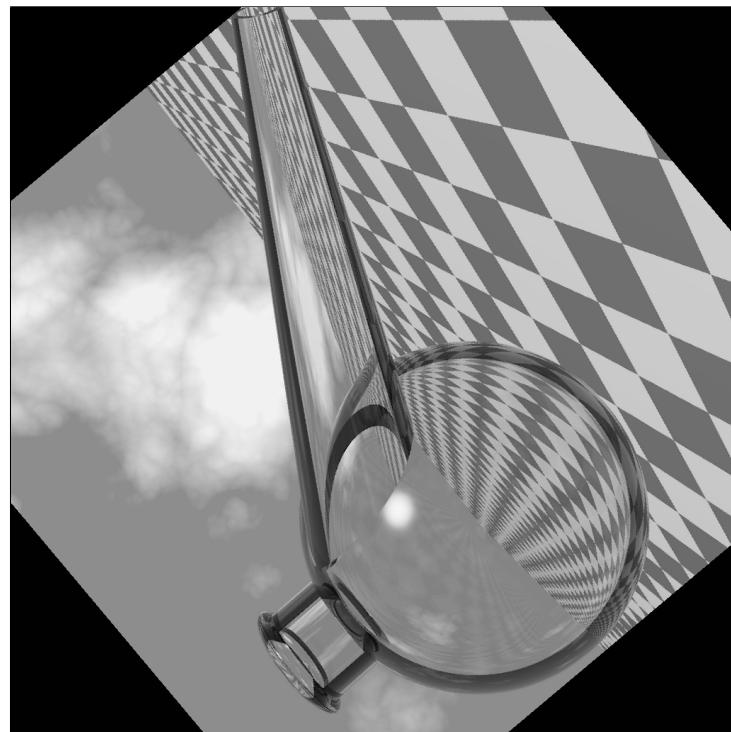
**FIGURE F.9** – Rotate 20° bilinear



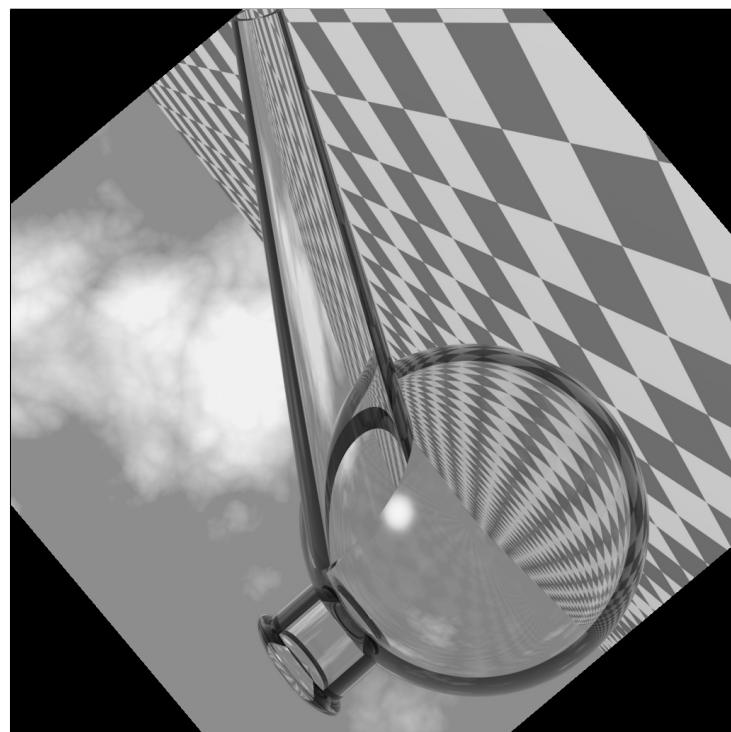
**FIGURE F.10** – Rotate 90° nearest



**FIGURE F.11** – Rotate 90° bilinear

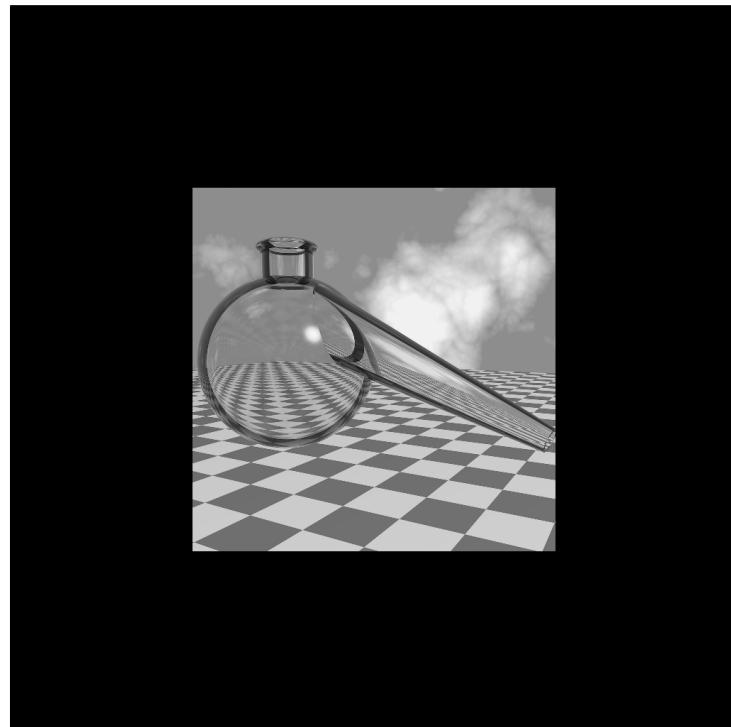


**FIGURE F.12** – Rotate 130° nearest

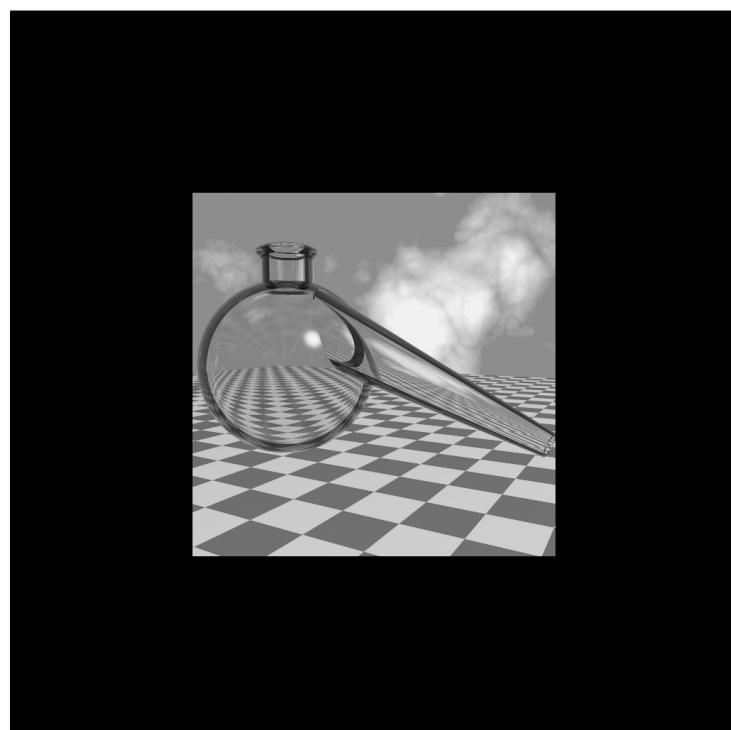


**FIGURE F.13** – Rotate 130° bilinear

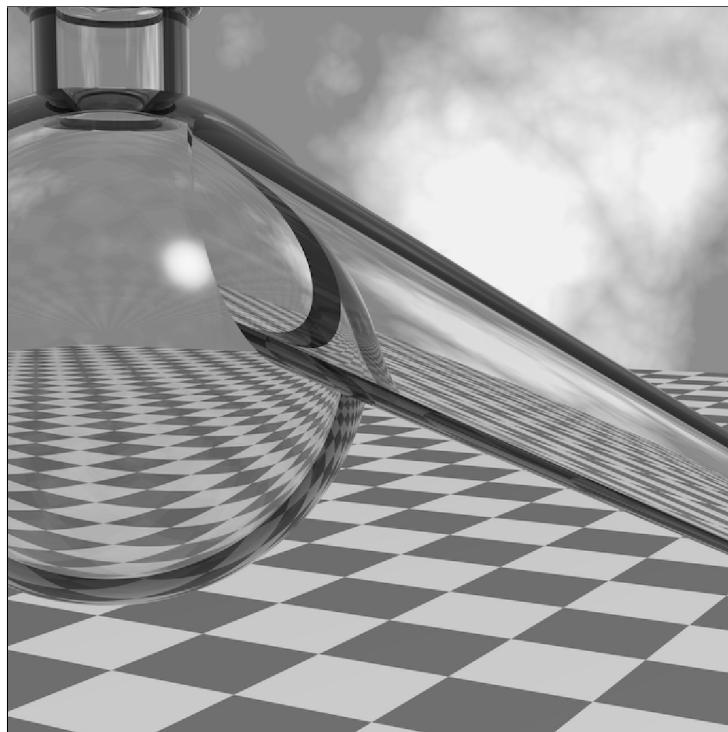
## F.5 Scaling



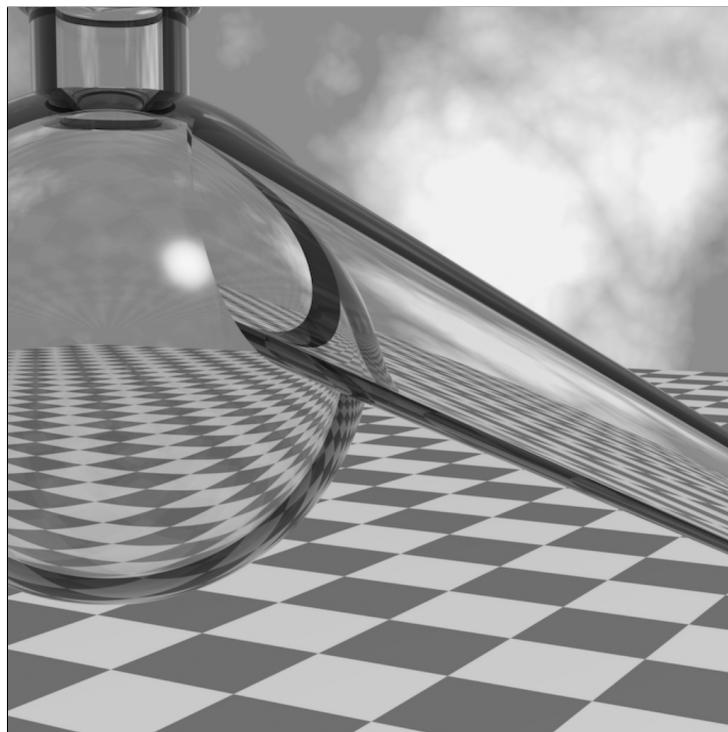
**FIGURE F.14** – Scaling 0.5 nearest



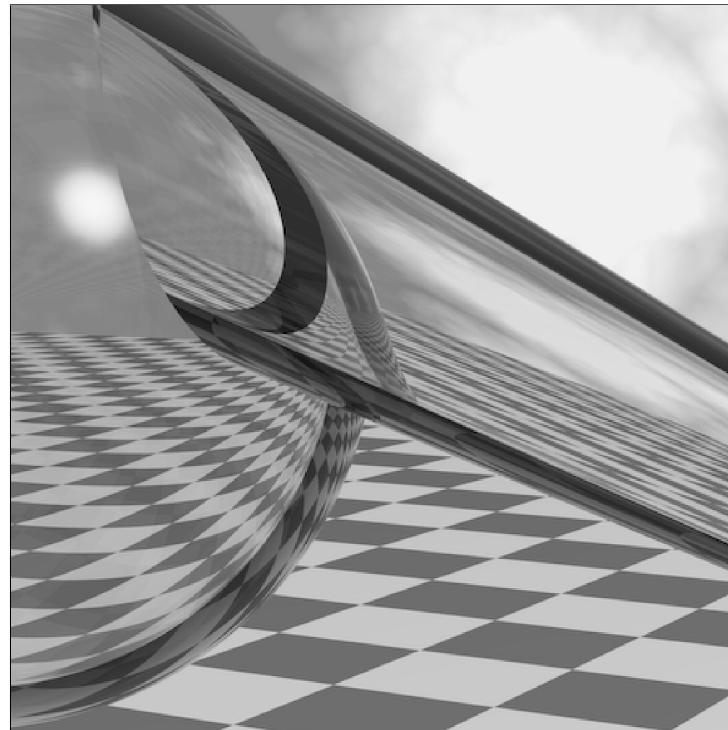
**FIGURE F.15** – Scaling 0.5 bilinear



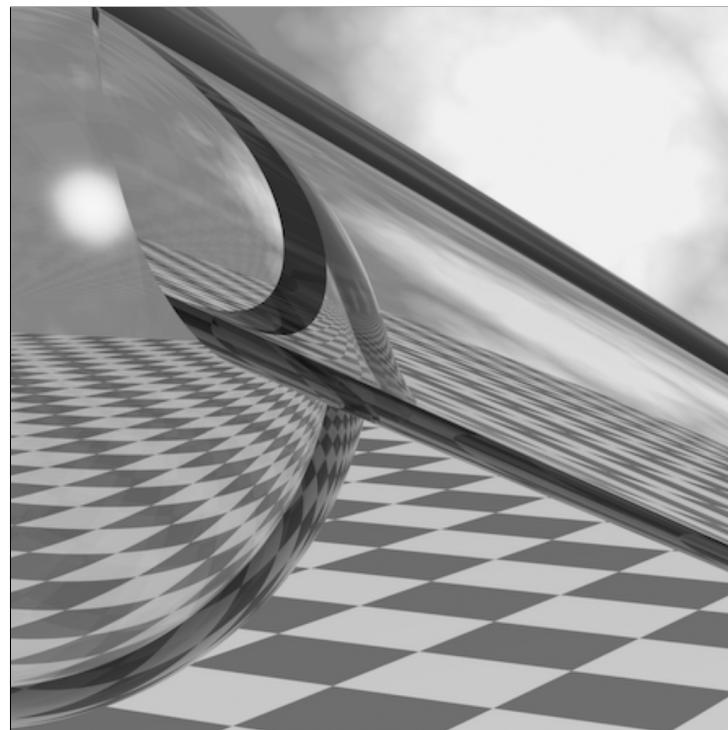
**FIGURE F.16** – Scaling 1.5 nearest



**FIGURE F.17** – Scaling 1.5 bilinear



**FIGURE F.18** – Scaling 2.3 nearest



**FIGURE F.19** – Scaling 2.3 bilinear

# G. Transform image compression

## G.1 Problem statement

- (a) Investigate image compression based on DCT. Divide the image into 8-by-8 subimages, compute the two-dimensional discrete cosine transform of each subimage, compress the test image to different qualities by discarding some DCT coefficients based on zonal mask and threshold mask and using the inverse discrete cosine transform with fewer transform coefficients. Display the original image, the reconstructed images and the difference images.
- (b) Investigate image compression based on wavelets.  
Consider four types of wavelets :
  - (a) Haar (2x2)
  - (b) Daubechies (8-tap)
  - (c) Symlet (8-tap)
  - (d) Cohen-Daubechies-Feauveau (17-tap)

## G.2 Python implementation

Two programs :

- DCT compression : **dct.py** Usage : **dct.py [-h] [-zonal | -threshold] [-z Z] image\_path**  
Use **python dct.py -h** to see the help.
- Wavelet compression : **wavelet.py** Usage : **wavelets.py [-h] [-haar | -daub | -symlet | -cohen] [-l LEVEL] [-t THRESHOLD] image\_path** Use **python wavelets.py -h** to see the help.



**FIGURE G.1** – Original image

## G.3 Image compression based on DCT

### G.3.1 Zonal mask

`python dct.py -zonal -z Z lenna.tif` where  $Z = 1, 4$  or  $7$ .

Example : Zonal 5

$$\begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (\text{G.1})$$

Example : Zonal 2

$$\begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (\text{G.2})$$



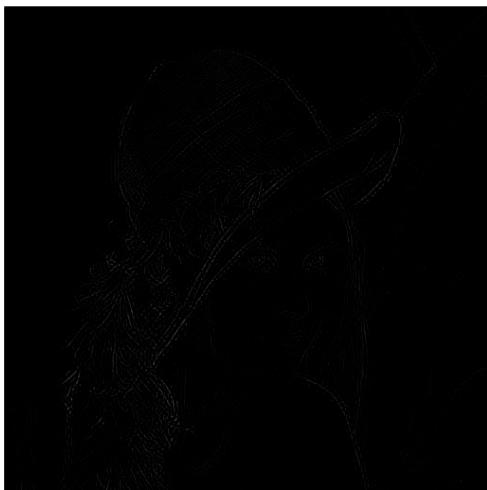
FIGURE G.2 – Zonal 7



FIGURE G.3 – Zonal 7 - Diff



**FIGURE G.4 – Zonal 4**



**FIGURE G.5 – Zonal 4 - Diff**



**FIGURE G.6 – Zonal 2**



**FIGURE G.7 – Zonal 2 - Diff**



**FIGURE G.8 – Zonal 1**



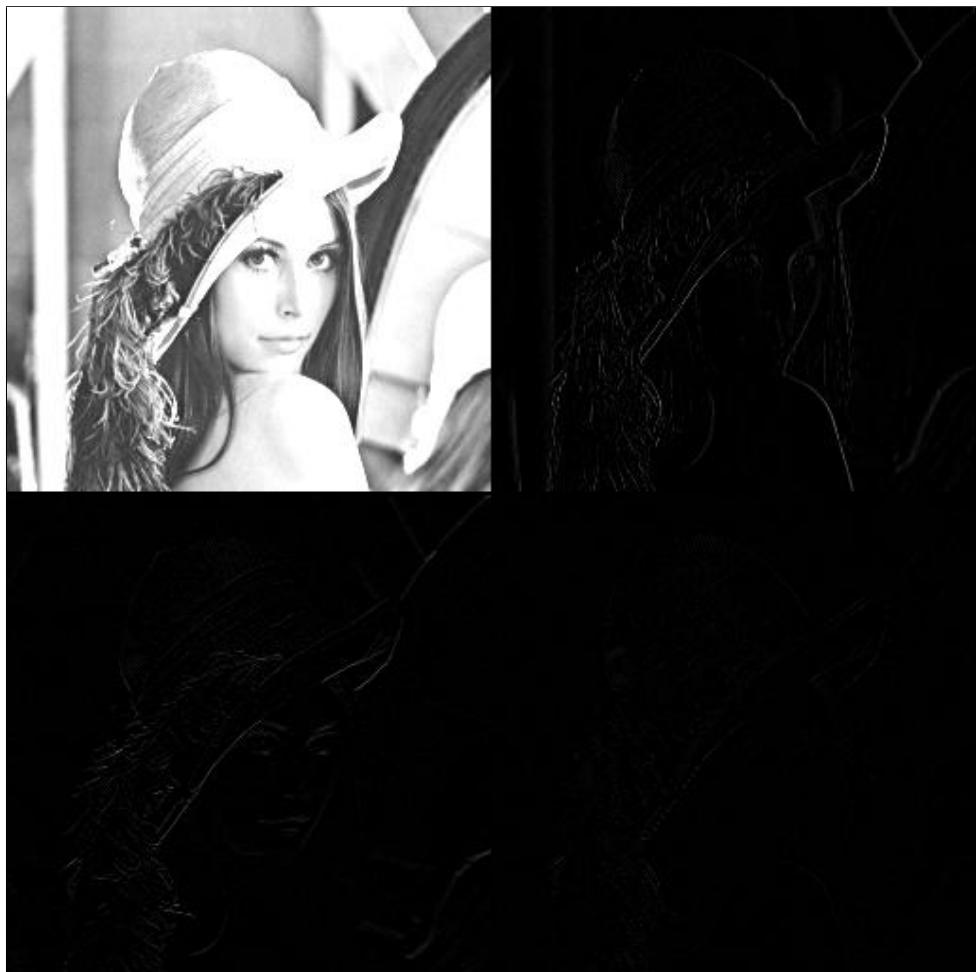
**FIGURE G.9 – Zonal 1 - Diff**

## G.4 Image compression based on Wavelets

Decompose the image by wavelets, truncate some coefficients to 0 below a threshold (0 in this case) and reconstructed the image.

```
python wavelets.py -haar lenna.tif -l 1 -t 0.
```

#### G.4.1 Haar



**FIGURE G.10 – Haar**



**FIGURE G.11 – Haar reconstructed**

**FIGURE G.12 – Haar difference**

#### G.4.2 Daubechies

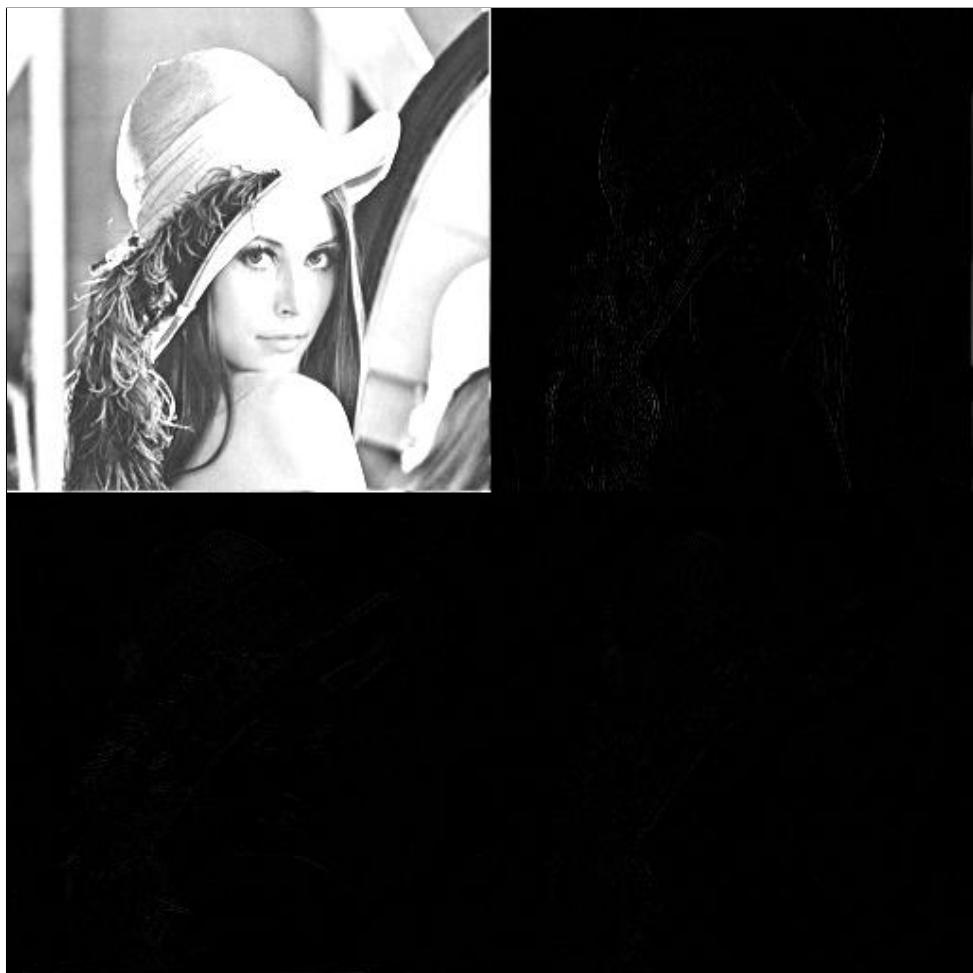


**FIGURE G.13** – Daubechies



**FIGURE G.14** – Daubechies reconstructed    **FIGURE G.15** – Daubechies difference

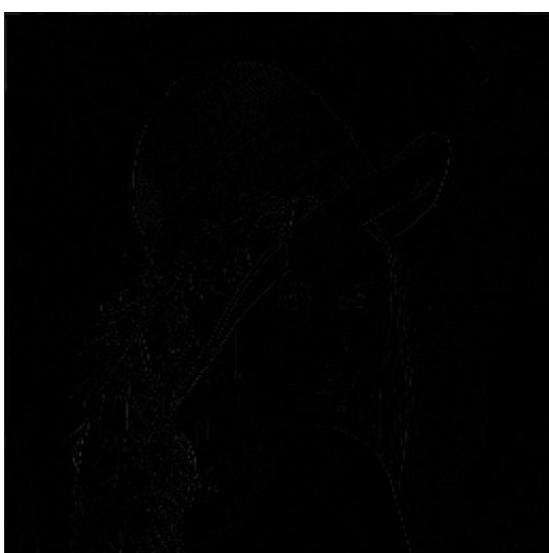
### G.4.3 Symlet



**FIGURE G.16 – Symlet**

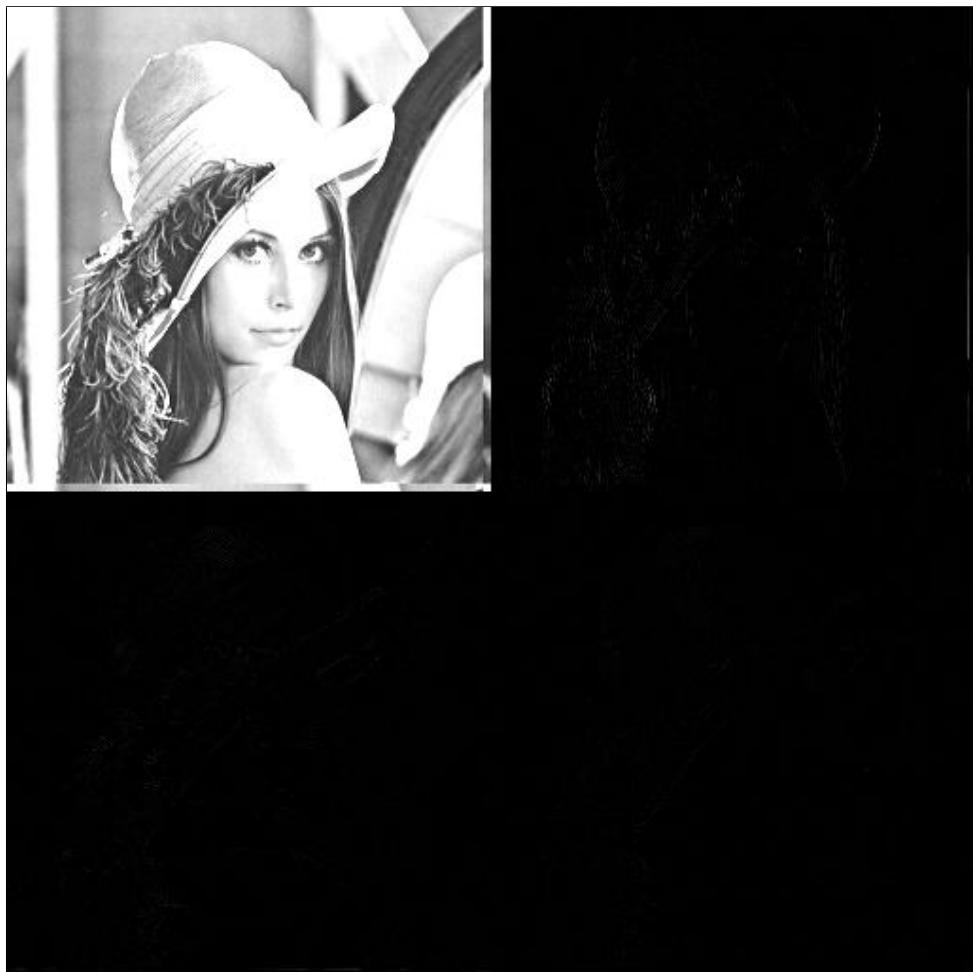


**FIGURE G.17 – Symlet reconstructed**



**FIGURE G.18 – Symlet difference**

#### G.4.4 Cohen-Daubechies-Feauveau



**FIGURE G.19** – Cohen



**FIGURE G.20** – Cohen reconstructed

**FIGURE G.21** – Cohen difference

# H. Morphological Processing

## H.1 Problem statement

- (a) Implement the morphological operations : erosion, dilation, opening and closing, and use the noisy\_fingerprint.tif to check your implementation.
- (b) Implement boundary extraction, hole filling, connected component extraction. Using lincoln\_from\_penny.tif, region\_filling\_reflection.tif and chickenfilet\_with\_bones.tif to the results, respectively.

## H.2 Python implementation

```
Usage : problem8.py [-h] [-debug] [-test] [-erosion] [-dilation]
[-opening] [-closing] [-boundary] [-filling]
[-connected]
image_path
```

Use **python problem8.py -h** to see the help.

### H.3 Erosion

```
python problem8.py -erosion noisy_fingerprint.tif
```



FIGURE H.1 – Original image



FIGURE H.2 – Erosion

### H.4 Dilation

```
python problem8.py -dilation noisy_fingerprint.tif
```



FIGURE H.3 – Original image



FIGURE H.4 – Dilation

## H.5 Opening

```
python problem8.py --opening noisy_fingerprint.tif
```



FIGURE H.5 – Original image

FIGURE H.6 – Opening

## H.6 Closing

```
python problem8.py --closing noisy_fingerprint.tif
```



FIGURE H.7 – Original image

FIGURE H.8 – Closing

## H.7 Boundary extraction

```
python problem8.py -boundary lincoln_from_penny.tif
```

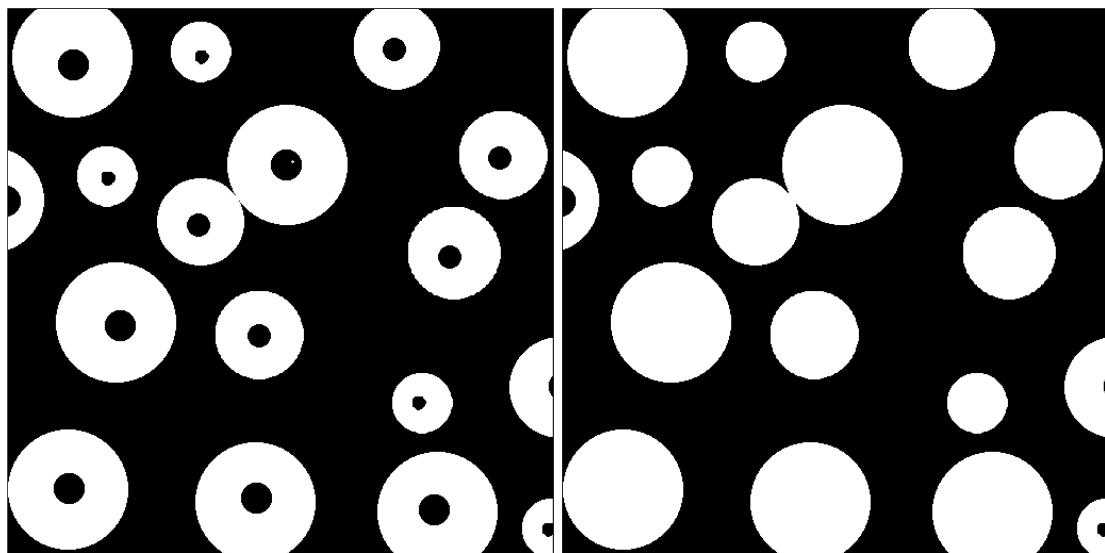


**FIGURE H.9** – Original image

**FIGURE H.10** – Boundary extraction

## H.8 Hole filling

```
python problem8.py -filling region_filling_reflections.tif
```

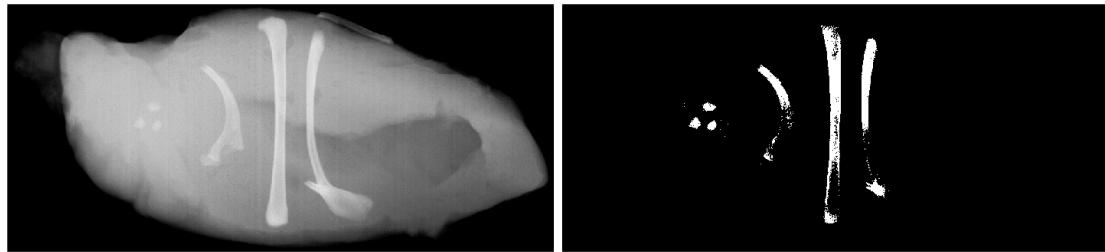


**FIGURE H.11** – Original image

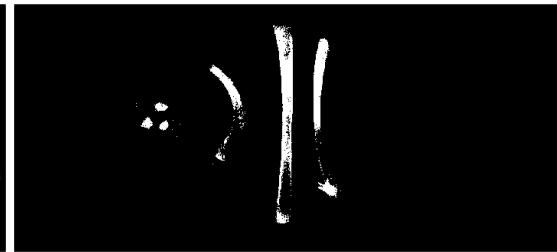
**FIGURE H.12** – Hole filling

## H.9 Connected component extraction

```
python problem8.py -connected chickenfilet_with_bones.tif
```



**FIGURE H.13** – Original image



**FIGURE H.14** – Thresholding



**FIGURE H.15** – Erosion 5×5

Connected components :

Connected component	No of pixels
01	836
02	690
03	44
04	148
05	1
06	18
07	19
08	26
09	2
10	14
11	11
12	13
13	28
14	87
15	18

# I. Image segmentation

## I.1 Problem statement

- (a) Develop a program to implement the Roberts, Prewitt, Sobel, the Marr-Hildreth and the Canny edge detectors. Use the image ‘building.tif’ to test your detectors. (For technique details of Marr-Hildreth and Canny, please refer to pp.736-747 (3rd edition, Gonzalez DIP) or MH-Canny.pdf at the same address of the slides.)
- (b) Develop a program to implement the Otsu’s method of thresholding segementation, and compare the results with the global thresholding method using test image ‘polymersomes.tif’. (For technique details, please refer to pp.763-770 (3rd edition, Gonzalez DIP), or Otsu.pdf at the same ftp address of slides.)

## I.2 Python implementation

Three programs :

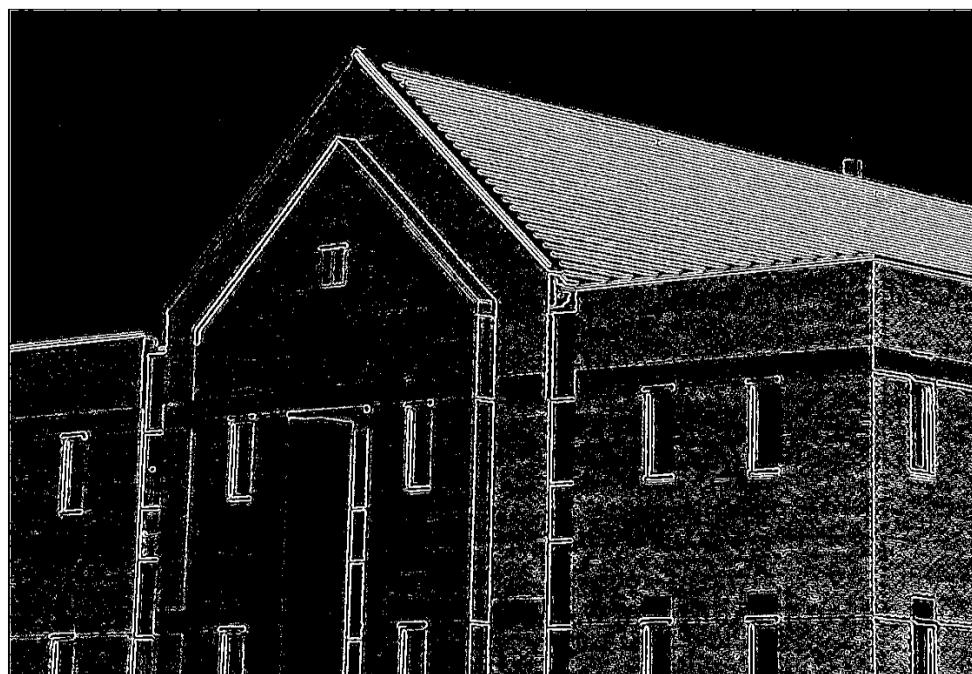
- Marr-Hildreth edge detector : **marr.py**  
Usage : **marr.py [-h] [-s SIGMA] image\_path**  
Use **python marr.py -h** to see the help.
- Canny edge detector : **canny.py**  
Usage : **canny.py [-h] (-roberts | -sobel | -prewitt) [-s SIGMA] [-th TH] [-tl TL] image\_path**  
Use **python canny.py -h** to see the help.
- Otsu’s method of thresholding segmentation : **otsu.py**  
Usage : **otsu.py [-h] [-o] [-g] image\_path**  
Use **python otsu.py -h** to see the help.

### I.3 Marr-Hildreth edge detector

```
python marr.py -s 4 building.tif
```



**FIGURE I.1** – Original image



**FIGURE I.2** – Marr-Hildreth

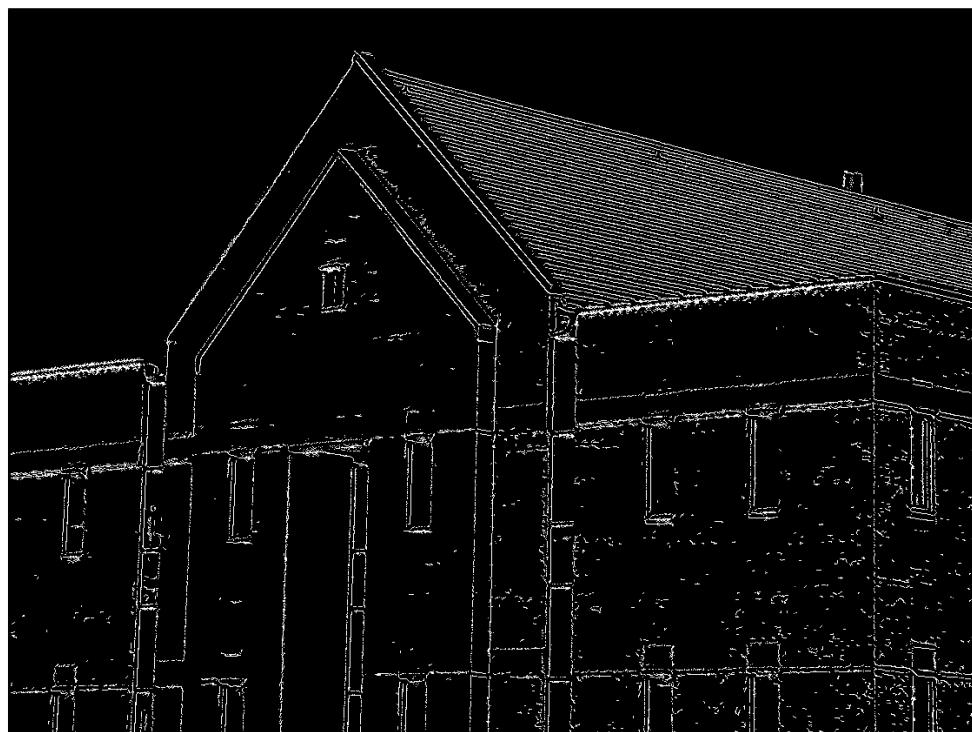
## I.4 Canny edge detector

### I.4.1 Roberts

```
python canny.py -roberts -s 4 -tl 0.04 -th 0.10 building.tif
```



**FIGURE I.3** – Original image



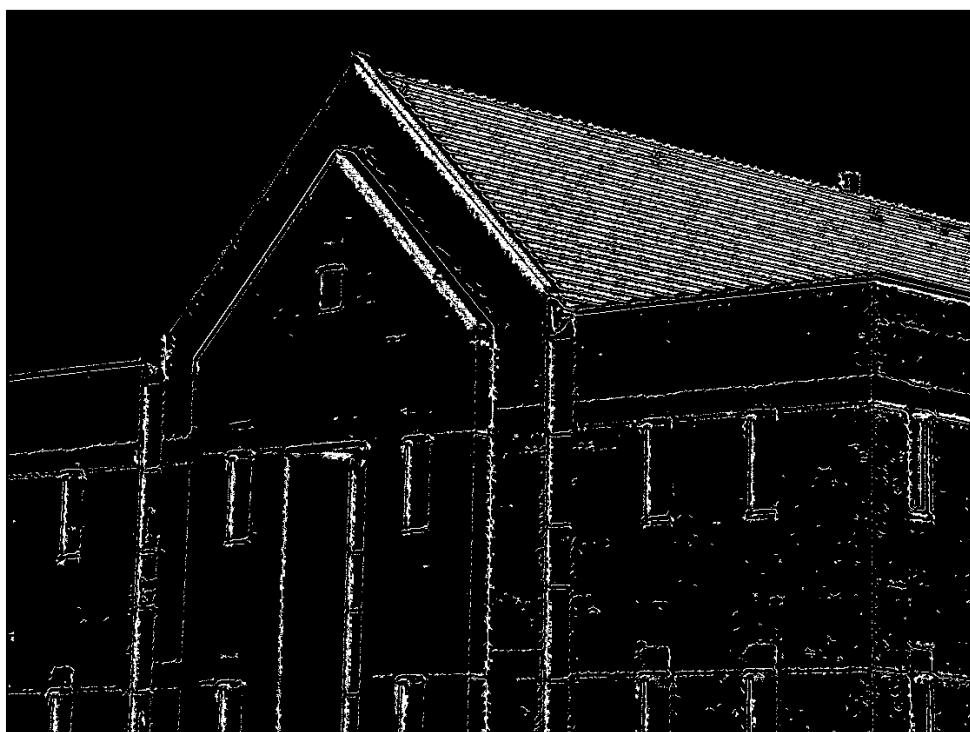
**FIGURE I.4** – Roberts

#### I.4.2 Prewitt

```
python canny.py -prewitt -s 4 -tl 0.04 -th 0.10 building.tif
```



**FIGURE I.5 – Original image**



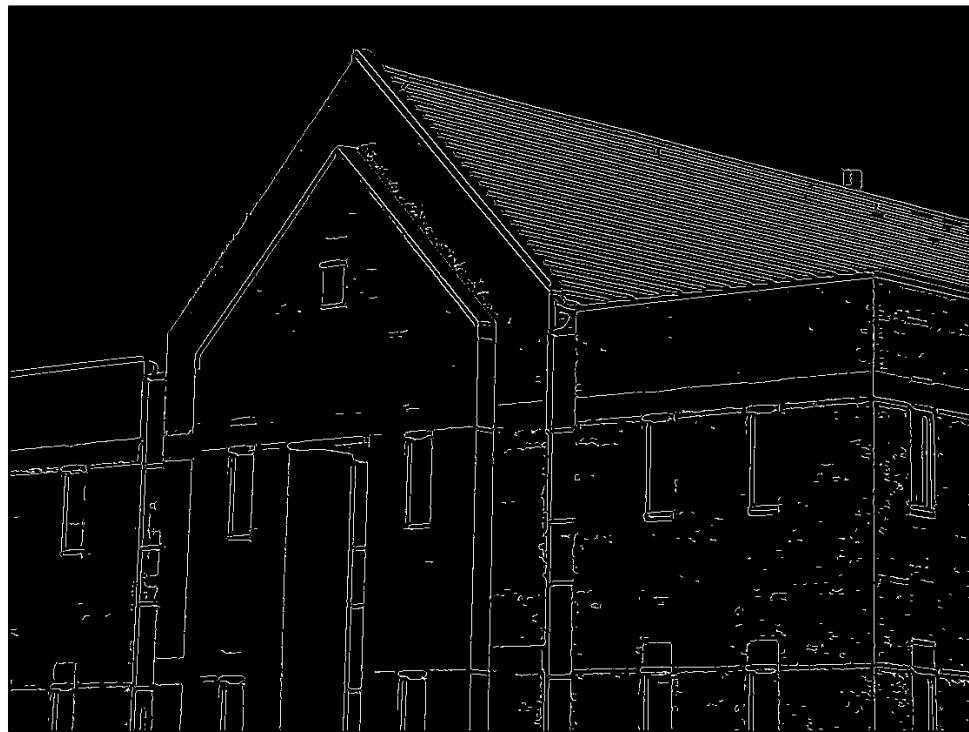
**FIGURE I.6 – Prewitt**

### I.4.3 Sobel

```
python canny.py --sobel -s 4 -tl 0.04 -th 0.10 building.tif
```



**FIGURE I.7** – Original image



**FIGURE I.8** – Sobel

## I.5 Thresholding segmentation

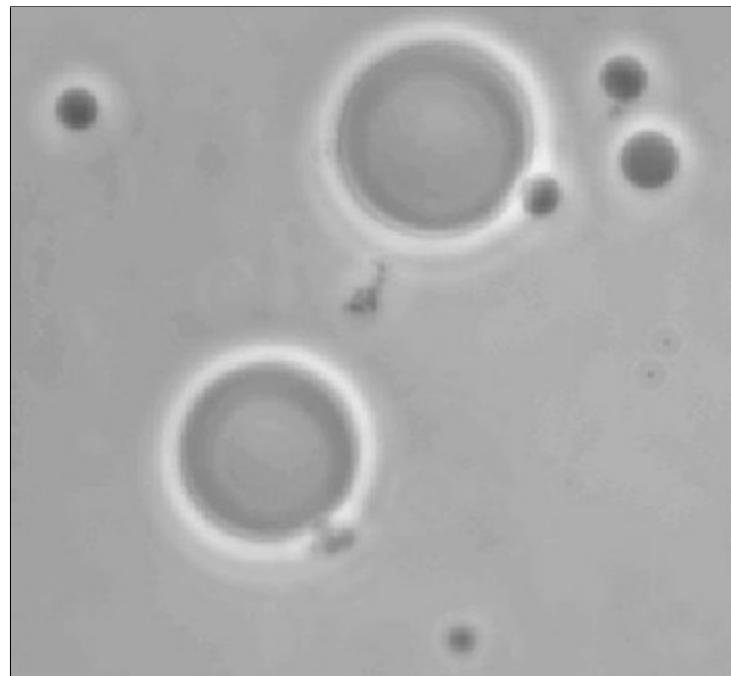


FIGURE I.9 – Original image

#### I.5.1 Otsu

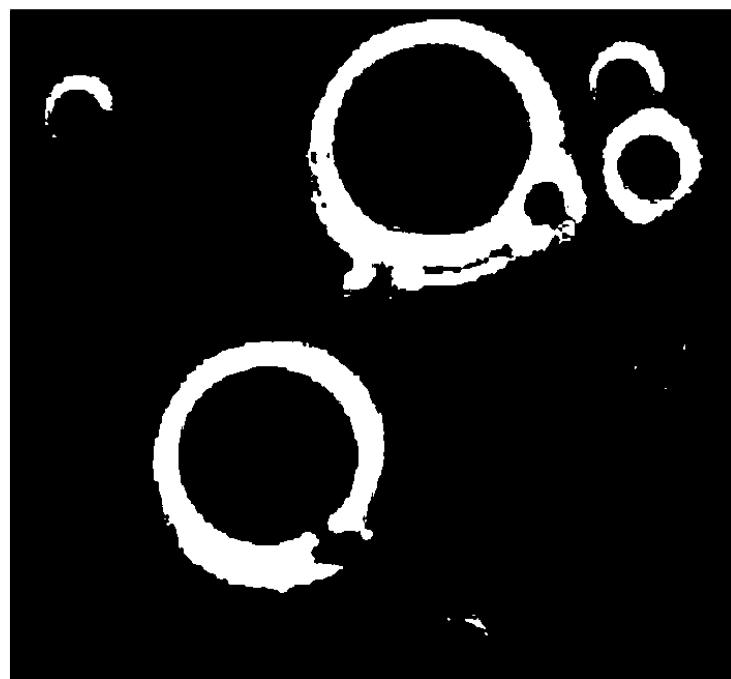


FIGURE I.10 – Otsu

#### I.5.2 Global thresholding



**FIGURE I.11** – Global thresholding

# J. Image representation and description

## J.1 Problem statement

- (a) Develop a program to implement the boundary following algorithm, the resampling grid and calculate the chain code and the first difference chain code. Use the image ‘noisy\_stroke.tif’ for test. (For technique details, please refer to pp.818-822 (3rd edition, Gonzalez DIP) or boundaryfollowing.pdf at the same address of the slides.)
- (b) Develop a program to implement the image description by the principal components (PC). Calculate and display the PC images and the reconstructed images from 2 PCs. Use the six images in ‘washingtonDC.rar’ as the test images.

## J.2 Python implementation

Four programs :

- Boundary following : **boundary.py**  
Usage : **boundary.py [-h] [-smooth] image\_path**  
Use **python boundary.py -h** to see the help.
- Resampling grid : **resampling.py**  
Usage : **resampling.py [-h] [-s SAMPLING [SAMPLING ...]] boundary\_image**  
Use **python resampling.py -h** to see the help.
- Chain code : **chaincode.py**  
Usage : **chaincode.py [-h] [-s SAMPLING [SAMPLING ...]] boundary\_image**  
Use **python chaincode.py -h** to see the help.
- Image description by the principal components (PC) : **pc.py**  
Usage : **pc.py [-h] [-n N] [-debug] [-diff] [-nshow]**  
Use **python pc.py -h** to see the help.

### J.3 Boundary following

`python boundary.py noisy_stroke.tif.`

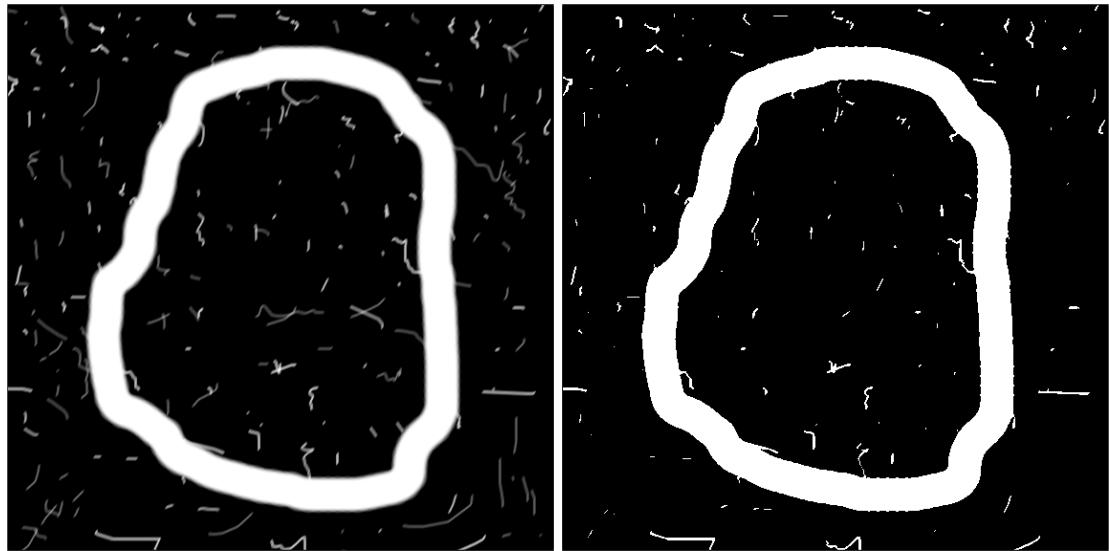


FIGURE J.1 – Original image

FIGURE J.2 – Black & white

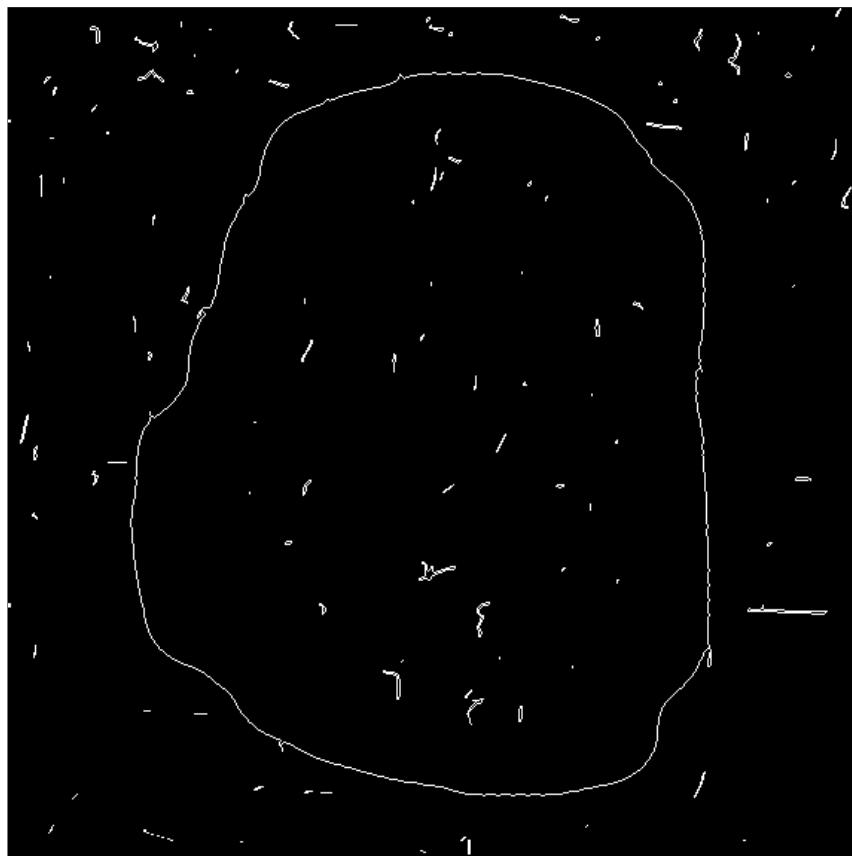
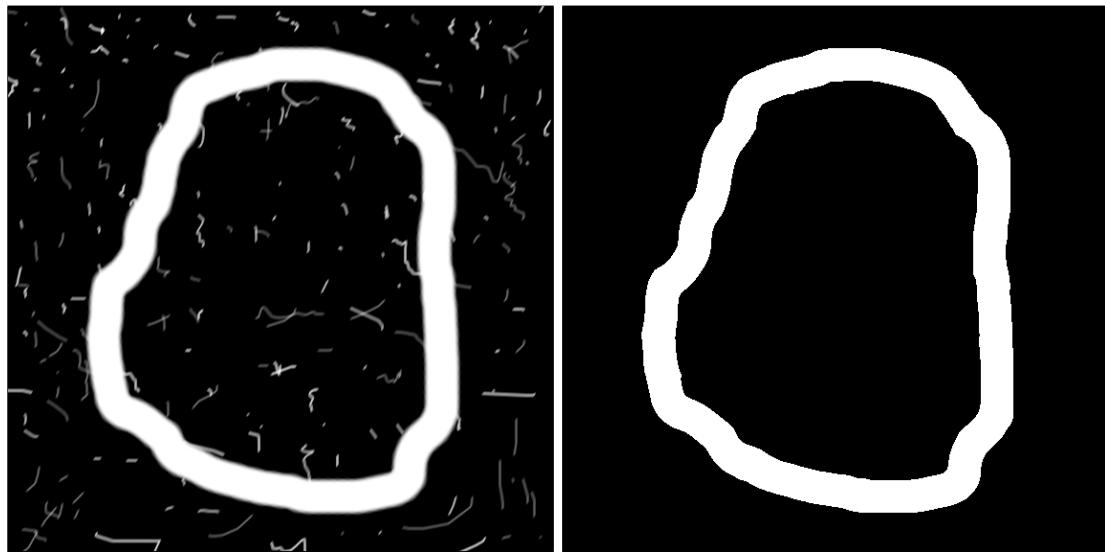


FIGURE J.3 – Boundaries

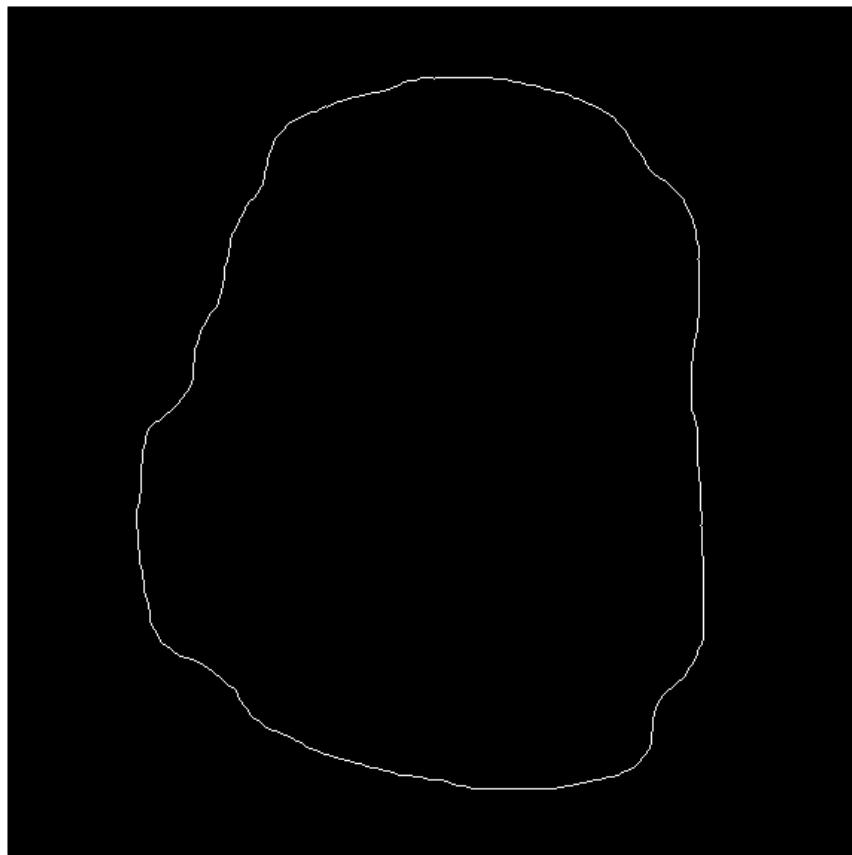
Even the boundaries of the noise are found... We need to remove the noise beforehand. For that, let use a Gaussian blur of mean 0 and variance 10.

```
python boundary.py noisy_stroke.tif -smooth.
```



**FIGURE J.4** – Original image

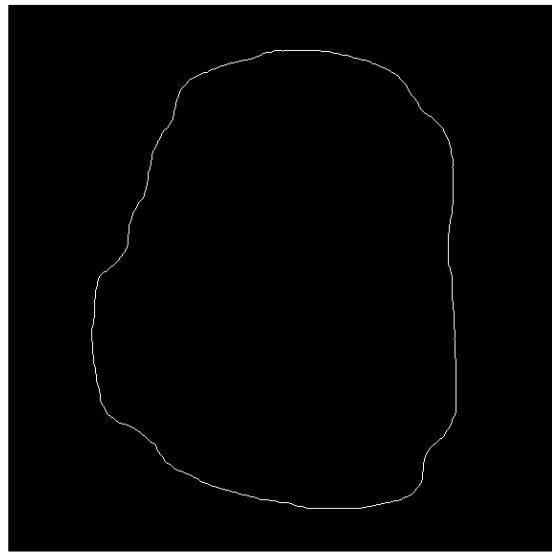
**FIGURE J.5** – Smoothing + binarisation



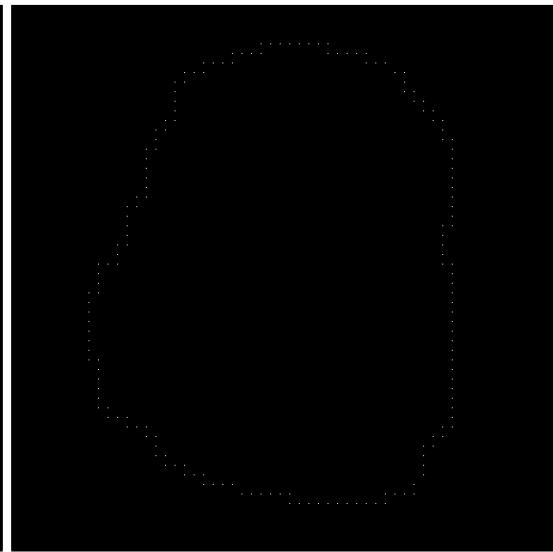
**FIGURE J.6** – Boundaries

## J.4 Resampling grid

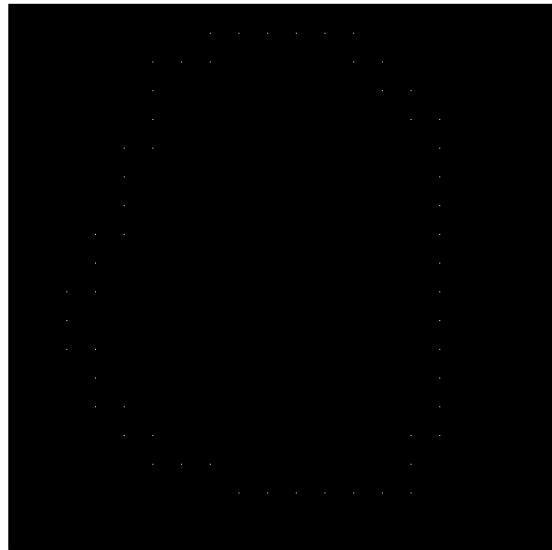
`python resampling.py noisy_stroke_boundary.png -s Sx Sy`, where  $Sx$  and  $Sy$  are the sampling intervalles along the X and Y axis.



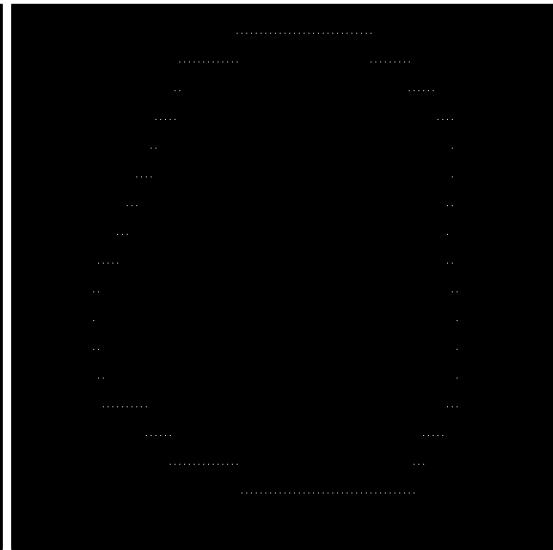
**FIGURE J.7** – Original image



**FIGURE J.8** – R-grid ( $S = (10, 10)$ )



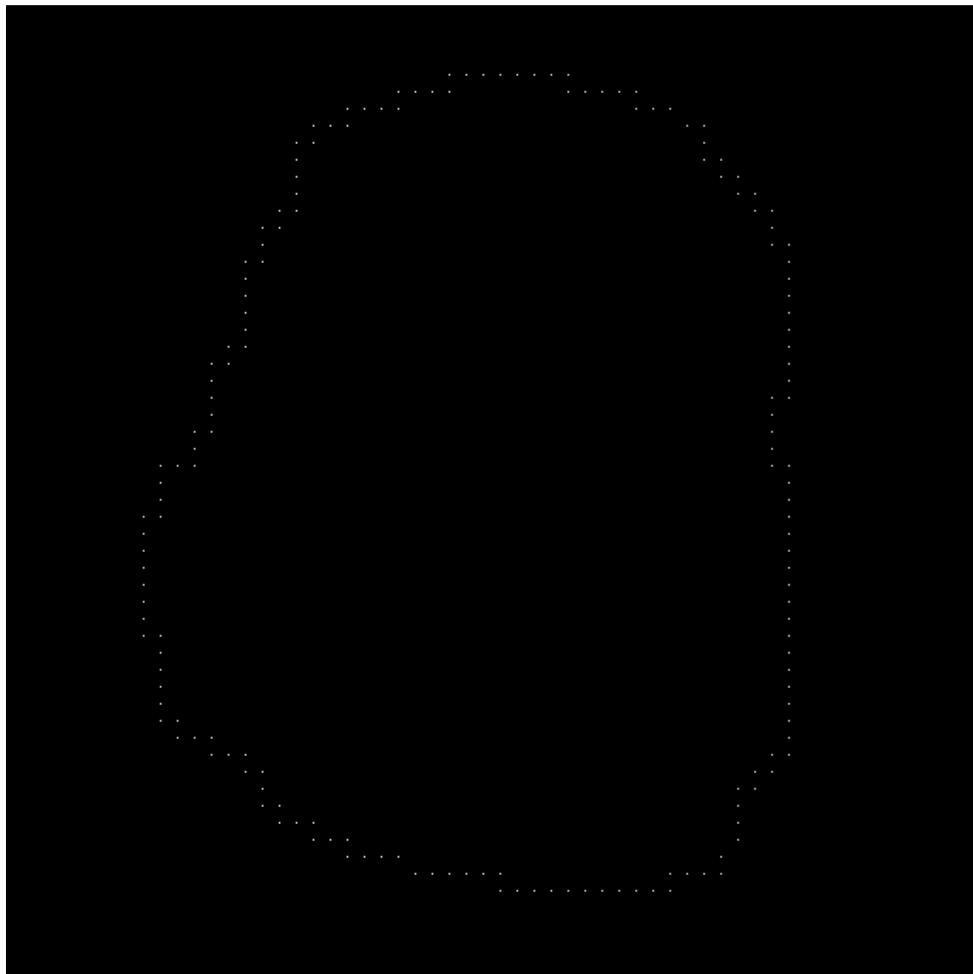
**FIGURE J.9** – R-grid ( $S = (30, 30)$ )



**FIGURE J.10** – R-grid ( $S = (5, 30)$ )

## J.5 Chain code and first difference chain code

### J.5.1 Chain code - resampling grid (10, 10)



**FIGURE J.11** – Resampling grid ( $S = (10, 10)$ )

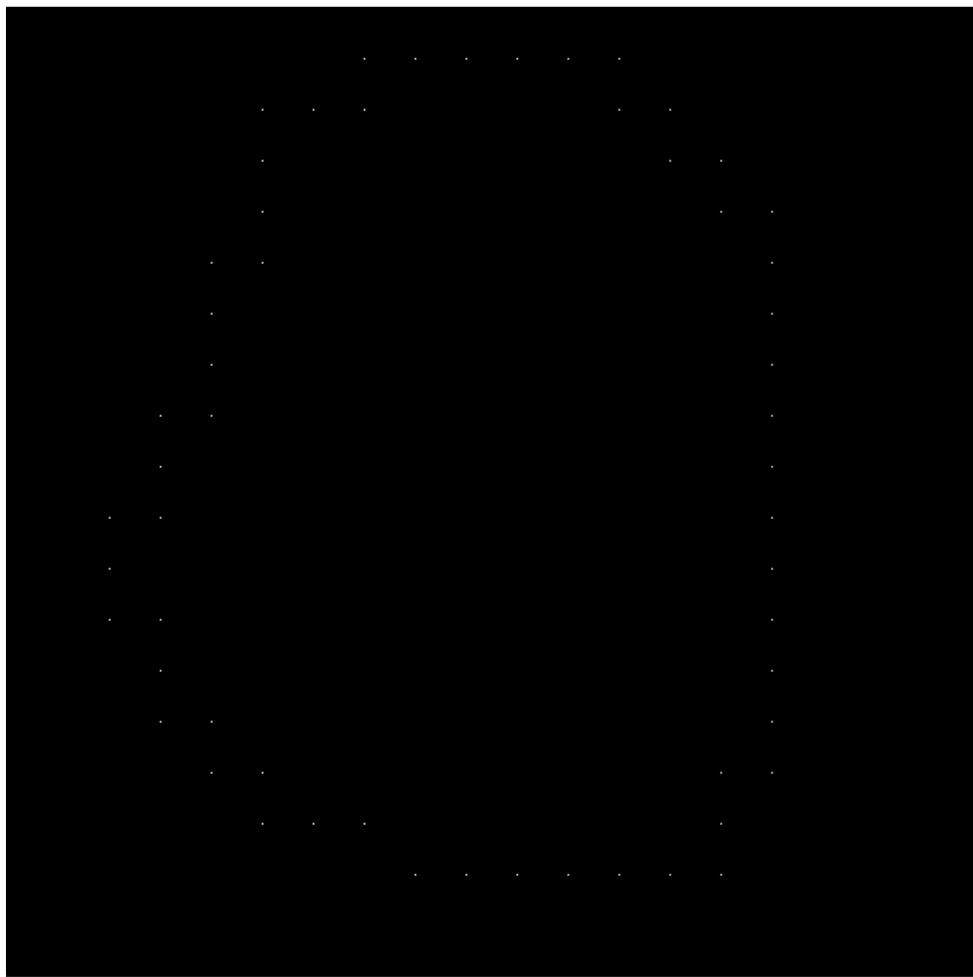
Chaincode (length = 170) :

```
00000060000600706606060606606666666  
6646666066666666666666646466656  
4446444444444424444344424424424224  
2442442422222422222202220022022220  
20222220220202220200200020002
```

First difference (length = 169) :

```
000006200062071602626260260000000  
0620002600000000000000062626200716  
0026000000000620007100620620626026  
206206260002600000620060206200062  
62000062062620006260260026002
```

### J.5.2 Chain code - resampling grid (30, 30)



**FIGURE J.12** – Resampling grid ( $S = (30, 30)$ )

Chaincode (length = 56) :

00060606066666666664664444434424242242202202220020

First difference (length = 55) :

0062626260000000000620600000710626260260620620062006026

## J.6 Principal components

```
python pc.py -diff -n 2
```

We keep only 2 principal components for the images reconstruction.



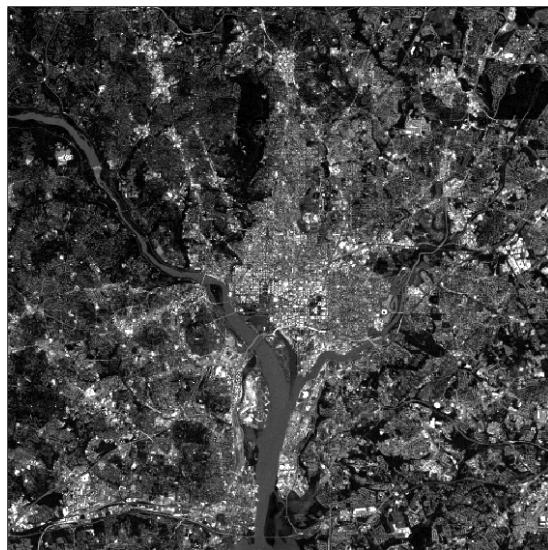
**FIGURE J.13** – Band 1



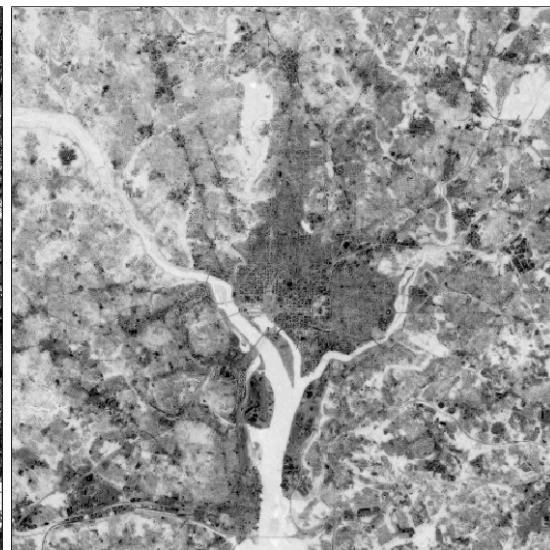
**FIGURE J.14** – Band 1 reconstructed



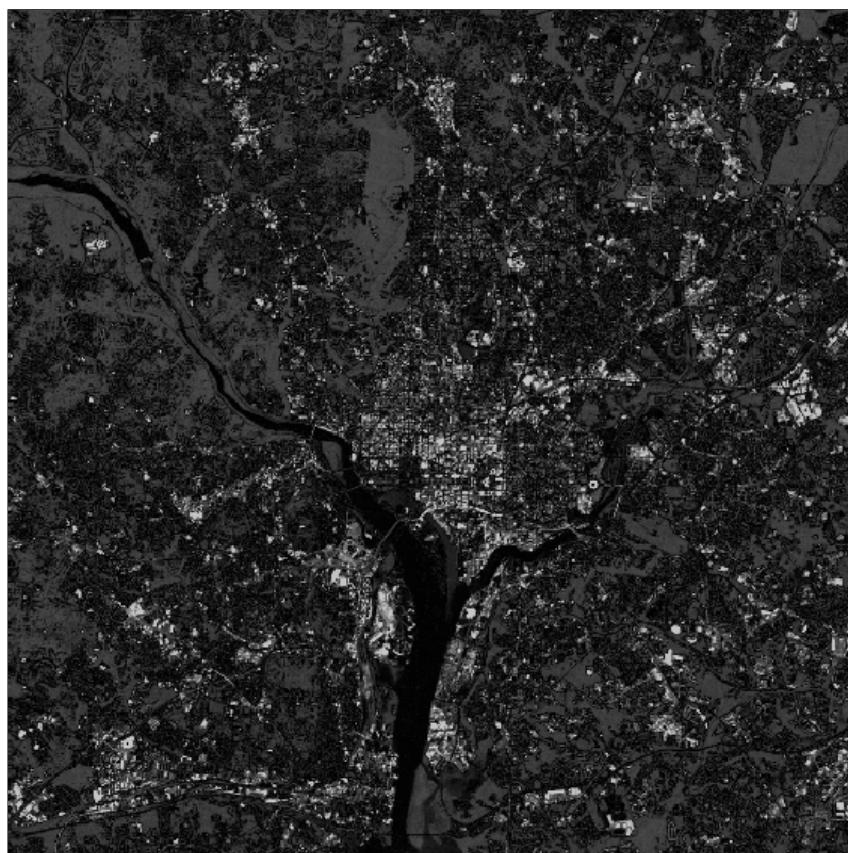
**FIGURE J.15** – Band 1 difference



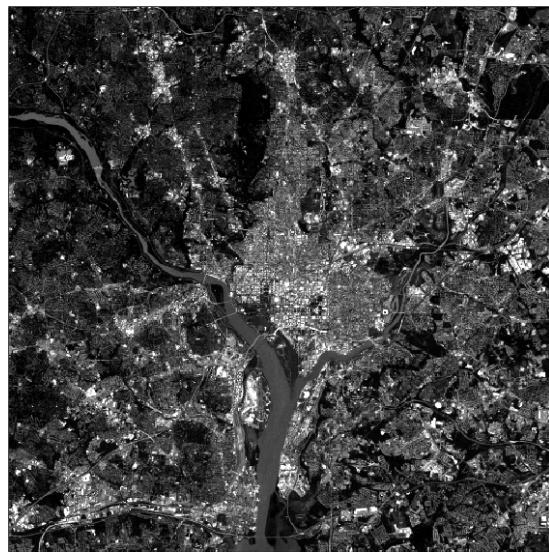
**FIGURE J.16** – Band 2



**FIGURE J.17** – Band 2 reconstructed



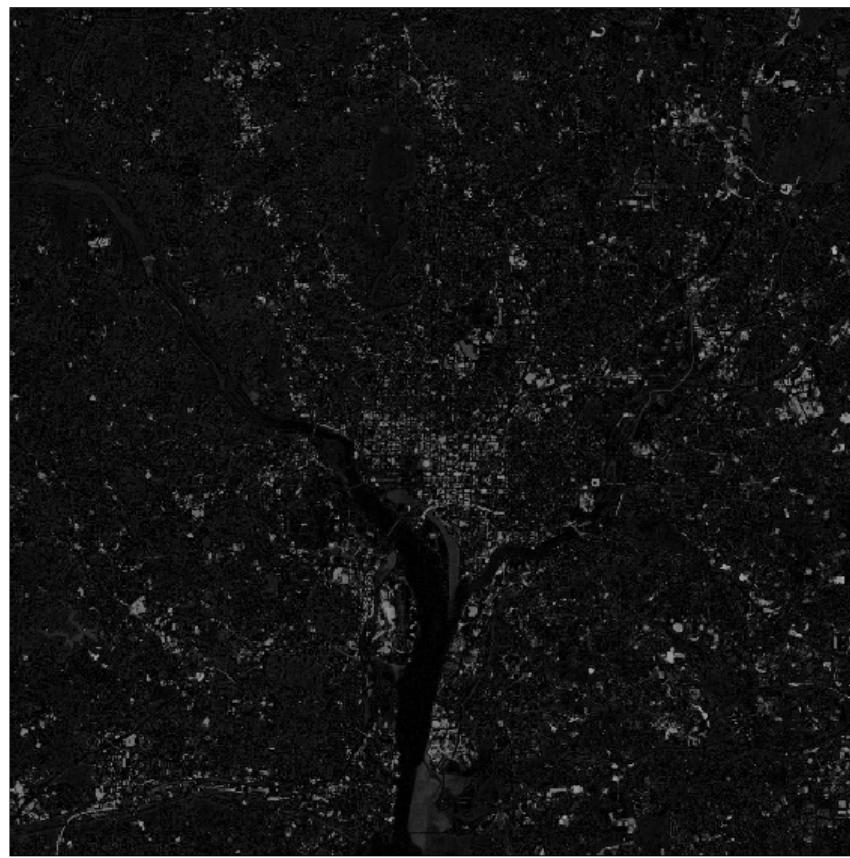
**FIGURE J.18** – Band 2 difference



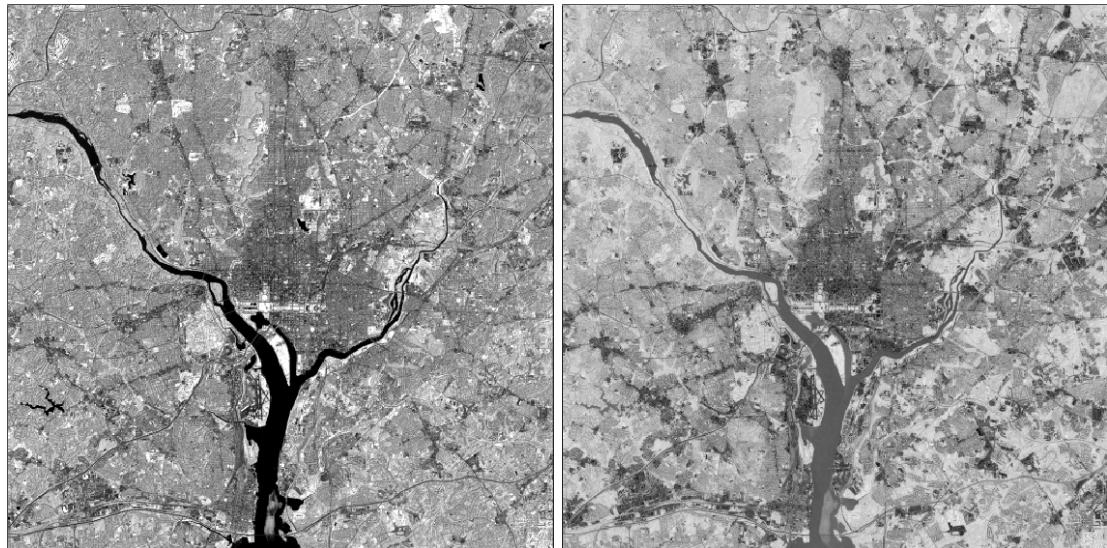
**FIGURE J.19** – Band 3



**FIGURE J.20** – Band 3 reconstructed



**FIGURE J.21** – Band 3 difference

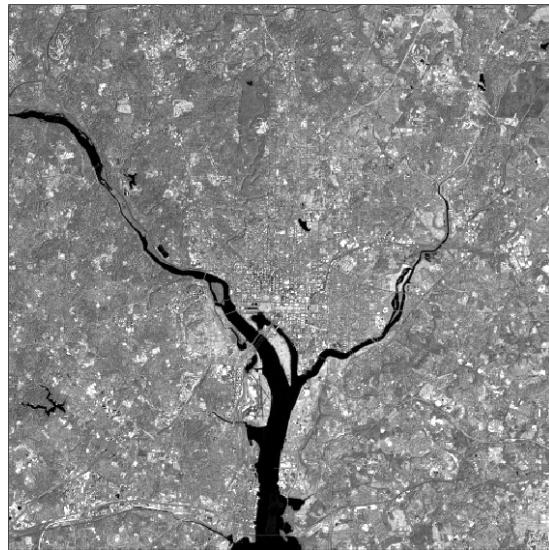


**FIGURE J.22** – Band 4

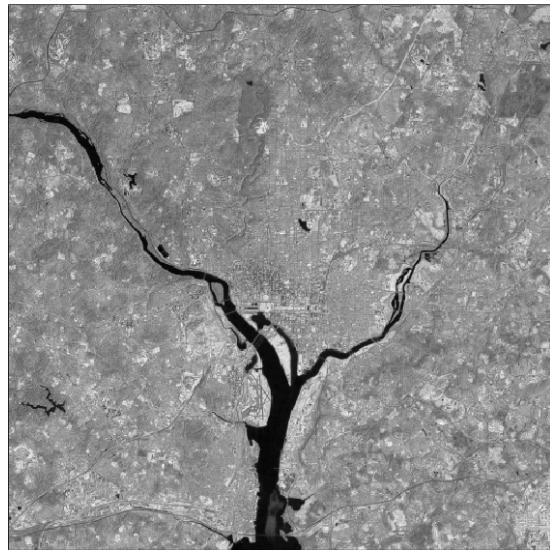
**FIGURE J.23** – Band 4 reconstructed



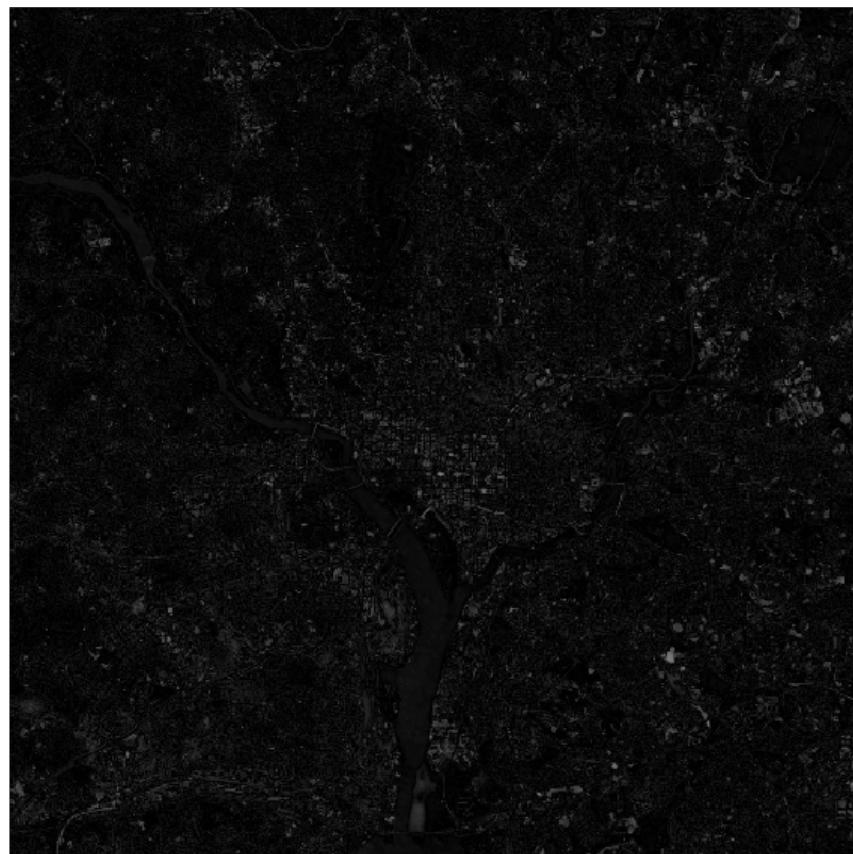
**FIGURE J.24** – Band 4 difference



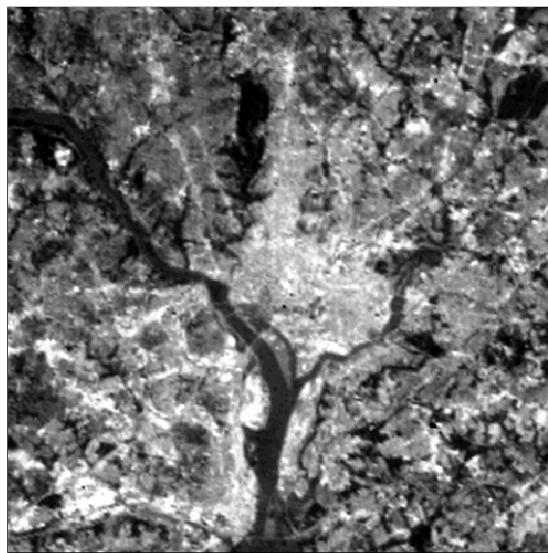
**FIGURE J.25** – Band 5



**FIGURE J.26** – Band 5 reconstructed



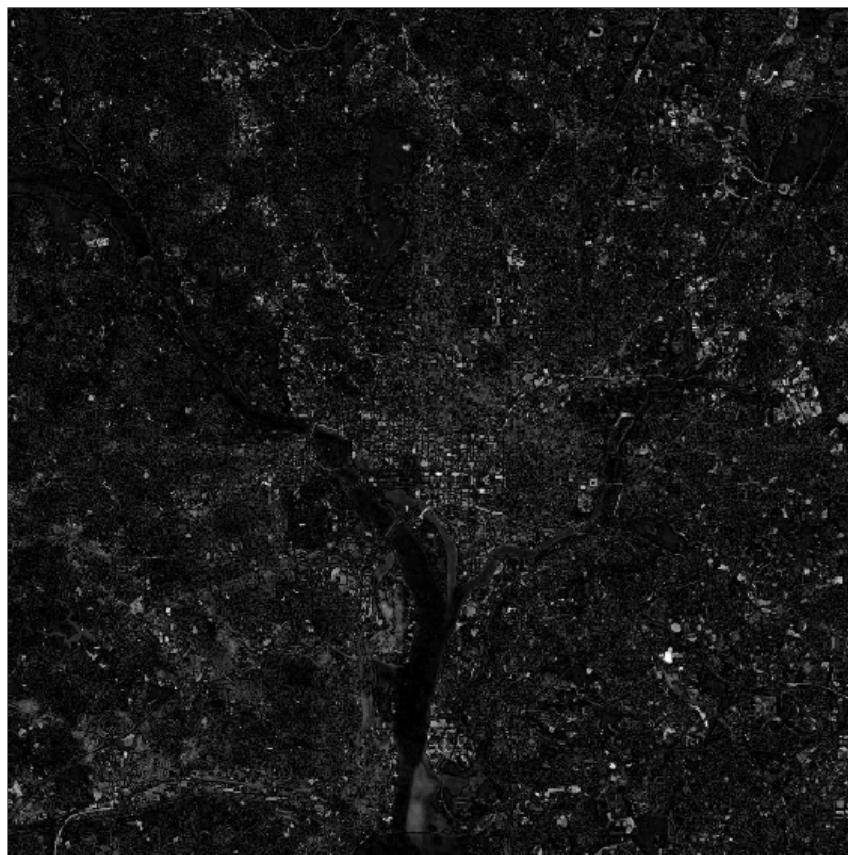
**FIGURE J.27** – Band 5 difference



**FIGURE J.28** – Band 6



**FIGURE J.29** – Band 6 reconstructed



**FIGURE J.30** – Band 6 difference