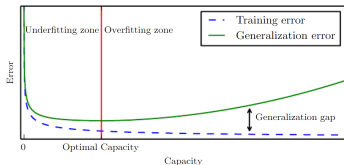


Introduction to Machine Learning

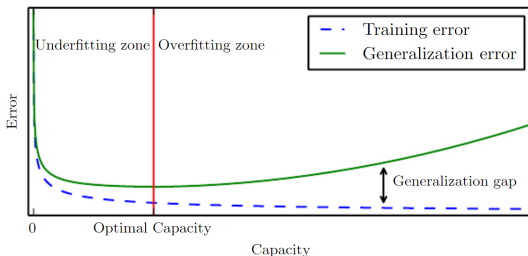
Capacity & Overfitting



Learning goals

- Know that the capacity of a hypothesis space impacts generalization
- Know that low capacity carries the risk of underfitting
- Know that too high capacity carries the risk of overfitting

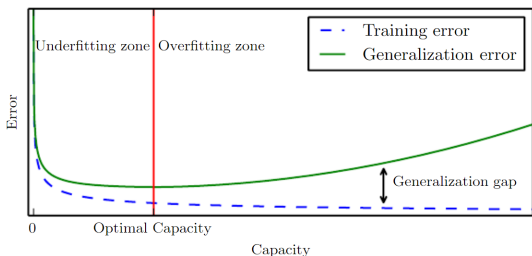
CAPACITY



Credit: Ian Goodfellow

- The performance of a learner depends on its ability to:
 - Minimize the training error
 - Generalize well to new data
- Failure to obtain a sufficiently low training error is known as **underfitting**.
- On the other hand, if there is a large difference in training and test error, this is known as **overfitting**.

CAPACITY



Credit: Ian Goodfellow

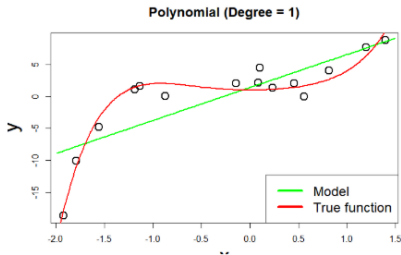
- The tendency of a model to over-/underfit is a function of its **capacity**, determined by the type of hypotheses it can learn.
- Loosely speaking, a model with low capacity can only learn a few simple hypotheses, whereas a model with large capacity can learn many, possibly complex, hypotheses.
- As the figure shows, the test error is minimized when the model neither underfits nor overfits, that is, when it has the right capacity.

OVERFITTING

- The capacity (or “complexity”) of a model can be increased by increasing the size of the hypothesis space.
- This (usually) also increases the number of learnable parameters.
- Examples: Increasing the degree of the polynomial in linear regression, increasing the depth of a decision tree or a neural network, adding additional predictors, etc.
- As the size of the hypothesis space increases, the tendency of a model to overfit also increases.
- Such a model might fit even the random quirks in the training data, thereby failing to generalize.

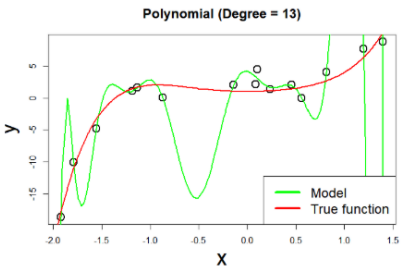
OVERFITTING: POLYNOMIAL REGRESSION

Degree = 1
(highest
degree of a
term in the
polynomial)



Underfitting
(Low Capacity)

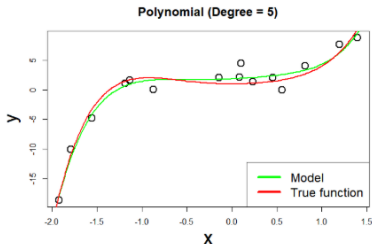
Degree = 13



Overfitting
(High Capacity)

OVERFITTING: POLYNOMIAL REGRESSION

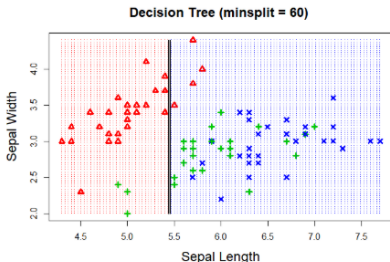
Degree = 5



	Degree = 1	Degree = 5	Degree = 13
Training error (RMSE)	3.87	1.23	0.48
Test error (RMSE)	4.11	1.55	148.5

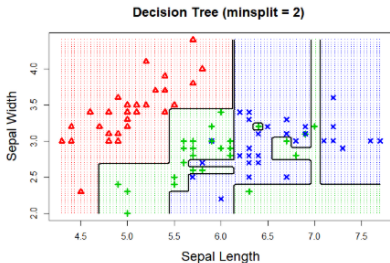
OVERFITTING: DECISION TREES

minsplit = 60
(minimum
number of
samples in a
node being
split)



Underfitting
(Low Capacity)

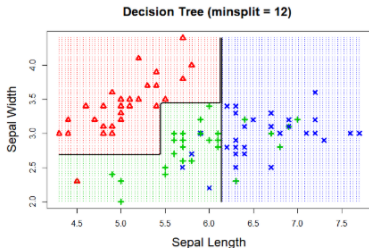
minsplit = 2



Overfitting
(High Capacity)

OVERFITTING: DECISION TREES

minsplit = 12

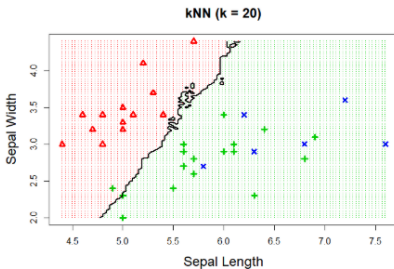


Good fit
(Appropriate
capacity)

	minsplit = 60	minsplit = 12	minsplit = 2
Training error (Misclassification)	0.36	0.12	0.02
Test error (Misclassification)	0.40	0.32	0.35

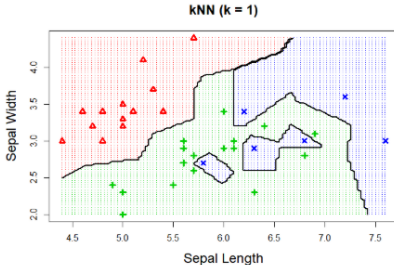
OVERFITTING: K-NEAREST NEIGHBORS

k = 20
(number of
neighbours)



Underfitting
(Low Capacity)

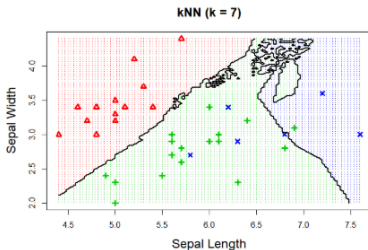
k = 1



Overfitting
(High Capacity)

OVERFITTING: K-NEAREST NEIGHBORS

$k = 7$



Good fit
(Appropriate
capacity)

	$k = 20$	$k = 7$	$k = 1$
Training error (Misclassification)	0.22	0.13	0
Test error (Misclassification)	0.40	0.25	0.33