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```
.bashrc
                                          ef12
build()(
 g++ $0 -o $1.e -DLOC -std=c++11
      -Wall -Wextra -Wfatal-errors -Wshadow \
      -Wlogical-op -Wconversion -Wfloat-equal
b() ( build $@ -02 )
d() ( build $@ -fsanitize=address, undefined \
              -D_GLIBCXX_DEBUG -q )
run()($1 $2 && echo start >&2 && time ./$2.e)
100()(
  set -e; $1 $2; $1 $3
  for ((;;)) {
    ./$3.e > gen.in
    time ./$2.e < gen.in > gen.out
cmp()(
  set -e; $1 $2; $1 $3; $1 $4
  for ((;;)) {
    ./$4.e > gen.in;
                              echo -n 0
    ./$2.e < gen.in > p1.out; echo -n 1
    ./$3.e < gen.in > p2.out; echo -n 2
    diff pl.out p2.out;
                              echo -n Y
# Other flags:
# -Wformat=2 -Wshift-overflow=2 -Wcast-qual
# -Wcast-align -Wduplicated-cond
# -D GLIBCXX DEBUG PEDANTIC -D FORTIFY SOURCE=2
# -fno-sanitize-recover -fstack-protector
                                          8b2d
.vimrc
se ai aw cin cul ic is nocp nohls nu sc scs
se bg=dark sw=4 ts=4 so=7 ttm=9
vn _ :w !cpp -dD -P -fpreprocessed \|
 tr -d '[:space:]' \| md5sum \| cut -c-4 <CR>
template.cpp
                                          ec3d
#include <bits/stdc++.h>
using namespace std;
using 11 = long long;
using Vi = vector<int>;
using Pii = pair<int,int>;
#define mp make pair
#define pb push back
#define x first
#define v second
#define rep(i,b,e) for(int i=(b); i<(e); i++)
#define each (a, x) for (auto \& a : (x))
#define all(x)
                   (x).begin(),(x).end()
#define sz(x)
                   int((x).size())
int main() {
  cin.sync_with_stdio(0); cin.tie(0);
  cout << fixed << setprecision(18);</pre>
  // Don't call destructors:
  cout << flush; _Exit(0);</pre>
} // 4799
// > Debug printer
#define tem template<class t, class u, class...w>
```

```
#define pri(x,y,z)tem auto operator << (t&o,u a) \
 ->decltype(x,o) { o << z; return o << y; }
pri(a.print(), '}', '{'; a.print())
pri(a.y, ')', '(' << a.x << ", " << a.y)
pri(all(a), ']', '['; auto d="";
 for (auto i : a) (o << d << i, d = ", "))
void DD(...) {}
tem void DD(t s, u a, w... k) {
 for (int b=1; *s && *s - b*44; cerr << *s++)
   b += 2 / (*s*2 - 81);
 cerr << ": " << a << *s++; DD(s, k...);
} // fd6d
#ifdef LOC
#define deb(...) (DD("[,\b :] "#__VA_ARGS__, \
 __LINE__, __VA_ARGS__), cerr << endl)
#else
#define deb(...)
#endif
#define DBP(...) void print() { \
 DD (# VA ARGS , VA ARGS ); } // 813f
// > Utils
// Return smallest k such that 2^k > n
// Undefined for n = 0!
int uplq(int n) { return 32- builtin clz(n); }
int uplg(ll n) { return 64-__builtin_clzll(n); }
// Compare with certain epsilon (branchless)
// Returns -1 if a < b: 1 if a > b: 0 if equal
// a and b are assumed equal if |a-b| <= eps
int cmp (double a, double b, double eps=1e-10) {
 return (a > b+eps) - (a+eps < b);
} // 81c1
various.h
                                         cbc4
// If math constants like M_PI are not found
// add this at the beginning of file
#define _USE_MATH_DEFINES
// Pragmas
#pragma GCC optimize("Ofast,unroll-loops,
                     no-stack-protector")
#pragma GCC target("popcnt,avx,tune=native")
// Clock
while (clock() < duration*CLOCKS PER SEC)
// Automatically implement operators:
// 1. != if == is defined
// 2. >, <= and >= if < is defined
using namespace rel_ops;
// Mersenne twister for randomization.
mt19937_64 rnd(chrono::steady_clock::now()
 .time_since_epoch().count());
// To shuffle randomly use:
shuffle(all(vec), rnd)
// To pick random integer from [A;B] use:
uniform_int_distribution <> dist(A, B);
int value = dist(rnd);
// To pick random real number from [A;B] use:
uniform_real_distribution  dist(A, B);
double value = dist(rnd);
geometry/convex hull.h
                                         1da8
#include "vec2.h"
```

```
// Translate points such that lower-left point
// is (0, 0). Returns old point location; O(n)
vec2 normPos(vector<vec2>€ points) {
 auto q = points[0].yxPair();
 each (p, points) q = min(q, p.yxPair());
 vec2 ret{q.y, q.x};
 each (p, points) p = p-ret;
 return ret;
} // 193b
// Find convex hull of points; time: O(n lq n)
// Points are returned counter-clockwise,
// first point is the lowest-left.
vector<vec2> convexHull(vector<vec2> points) {
 vec2 pivot = normPos(points);
 sort(all(points));
 vector<vec2> hull;
 each (p, points) {
   while (sz(hull) >= 2) {
     vec2 a = hull.back() - hull[sz(hull)-2];
     vec2 b = p - hull.back();
     if (a.cross(b) > 0) break;
     hull.pop_back();
   } // ad91
   hull.pb(p);
 } // 5908
 // Translate back, optional
 each(p, hull) p = p+pivot;
 return hull:
} // 62ed
// Find point p that minimizes dot product p*q.
// Returns point index in hull; time: O(lq n)
// If multiple points have same dot product
// one with smallest index is returned.
// Points are expected to be in the same order
// as output from convexHull function.
int minDot(const vector<vec2>& hull, vec2 q) {
 auto search = [&](int b, int e, vec2 p) {
   while (b+1 < e) {
     int m = (b+e) / 2;
      (p.dot(hull[m-1]) > p.dot(hull[m])
       ? b : e) = m;
   } // 184c
   return b;
 }; // 62e8
 int m = search(0, sz(hull), \{0, -1\});
 int i = search(0, m, q);
 int j = search(m, sz(hull), q);
 return q.dot(hull[i]) > q.dot(hull[j])
   ? j : i;
} // 4599
geometry/convex hull dist.h 2859
#include "vec2.h"
// Check if p is inside convex polygon. Hull
// must be given in counter-clockwise order.
// Returns 2 if inside, 1 if on border,
// 0 if outside; time: O(n)
int insideHull(vector<vec2>& hull, vec2 p) {
 int ret = 1:
 rep(i, 0, sz(hull)) {
   auto v = hull[(i+1)%sz(hull)] - hull[i];
   auto t = v.cross(p-hull[i]);
   ret = min(ret, cmp(t, 0)); // For doubles
   //ret = min(ret, (t>0) - (t<0)); // Ints
```

} // 0d40

```
return int(max(ret+1, 0));
} // 1f39
#include "segment2.h"
// Get distance from point to hull; time: O(n)
double hullDist(vector<vec2>€ hull, vec2 p) {
 if (insideHull(hull, p)) return 0;
 double ret = 1e30;
 rep(i, 0, sz(hull)) {
    seg2 seg{hull[(i+1)%sz(hull)], hull[i]};
    ret = min(ret, seq.distTo(p));
 } // f3be
 return ret;
} // a00c
// Compare distance from point to hull
// with sqrt(d2); time: O(n)
// -1 if smaller, 0 if equal, 1 if greater
int cmpHullDist(vector<vec2>& hull,
                vec2 p, 11 d2) {
 if (insideHull(hull,p)) return (d2<0)-(d2>0);
 int ret = 1:
  rep(i, 0, sz(hull)) {
    seg2 seg{hull[(i+1)%sz(hull)], hull[i]};
    ret = min(ret, seg.cmpDistTo(p, d2));
 1 // 28cb
 return ret;
} // 30f3
geometry/convex_hull sum.h
                                          31b0
#include "vec2.h"
// Get edge sequence for given polygon
// starting from lower-left vertex; time: O(n)
// Returns start position.
vec2 edgeSeq(vector<vec2> points,
            vector<vec2>& edges) {
 int i = 0, n = sz(points);
 rep(j, 0, n) {
    if (points[i].yxPair()>points[j].yxPair())
     i = j;
 } // 14e2
 rep(j, 0, n) edges.pb(points[(i+j+1)%n] -
                        points[(i+j)%n]);
 return points[i];
} // 20e2
// Minkowski sum of given convex polygons.
// Vertices are required to be in
// counter-clockwise order; time: O(n+m)
vector<vec2> hullSum (vector<vec2> A,
                    vector<vec2> B) {
 vector\langle vec2 \rangle sum, e1, e2, es(sz(A) + sz(B));
 vec2 pivot = edgeSeq(A, e1) + edgeSeq(B, e2);
 merge(all(e1), all(e2), es.begin());
  sum.pb(pivot):
 each (e, es) sum.pb (sum.back() + e);
  sum.pop_back();
 return sum:
} // f183
geometry/halfplanes.h
                                          78b5
#include "vec2.h"
#include "line2.h"
// Intersect given halfplanes and output
// hull vertices to out.
// Returns 0 if intersection is empty.
// 1 if intersection is non-empty and bounded,
// 2 if intersection is unbounded.
```

```
// Output vertices are valid ONLY IF
// intersection is non-empty and bounded.
// Works only with floating point vec2/line2.
// CURRENTLY DOESN'T WORK FOR NON-EMPTY
// AND UNBOUNDED CASES!
int intersectHalfPlanes(vector<line2> lines,
                        vector<vec2>& out) {
  deque<line2> H;
  out.clear();
  if (sz(lines) <= 1) return 2;</pre>
  sort(all(lines), [](line2 a, line2 b) {
    int t = cmp(a.norm.angle(),b.norm.angle());
    return t ? t < 0 : cmp(a.off*b.norm.len(),</pre>
     b.off*a.norm.len()) < 0;
  }); // dfa1
  auto bad = [](line2 a, line2 b, line2 c) {
   if (cmp(a.norm.cross(c.norm), 0) <= 0)</pre>
     return false;
    vec2 p; assert(a.intersect(c, p));
    return b.side(p) <= 0;</pre>
  }; // c1e8
  each(e, lines) {
    if (!H.empty() &&
     !cmp(H.back().norm.angle(),
      e.norm.angle())) continue;
    while (sz(H) > 1 &  bad(H[sz(H)-2])
     H.back(), e)) H.pop back();
    while (sz(H) > 1 \& \& bad(e, H[0], H[1]))
     H.pop front();
   H.pb(e);
  ) // 5714
  while (sz(H) > 2 &  bad(H[sz(H)-2])
   H.back(), H[0])) H.pop back();
  while (sz(H) > 2 && bad(H.back(),
   H[0], H[1])) H.pop_front();
  out.resize(sz(H));
  rep(i, 0, sz(H)) {
   auto a = H[i], b = H[(i+1)%sz(H)];
    if (a.norm.cross(b.norm) <= 0)</pre>
      return cmp(a.off*b.norm.len(),
       -b.off*a.norm.len()) <= 0 ? 0 : 2;
    assert(a.intersect(b, out[i]));
  } // c550
  rep(i, 0, sz(H)) {
   auto a = out[i], b = out[(i+1)%sz(H)];
    if (H[i].norm.perp().cross(b-a) <= 0)</pre>
      return 0:
  } // 54b6
 return 1;
} // 019f
geometry/line2.h
                                          4bb7
#include "vec2.h"
// 2D line/halfplane structure
// PARTIALLY TESTED
// Base class of versions for ints and doubles
template < class T, class P, class S>
struct bline2 {
  // For lines: norm*point == off
  // For halfplanes: norm*point <= off
  // (i.e. normal vector points outside)
  P norm: // Normal vector [A: B]
```

T off; // Offset (C parameter of equation)

DBP (norm, off);

```
// Line through 2 points; normal vector
 // points to the right of ab vector
  static S through (P a, P b) {
   return { (a-b).perp(), a.cross(b) };
 1 // 9ac7
  // Parallel line through point
  static S parallel (P a, S b) {
   return { b.norm, b.norm.dot(a) };
 } // 6a39
  // Perpendicular line through point
  static S perp(P a, S b) {
   return { b.norm.perp(), b.norm.cross(a) };
 } // 10a5
  // Distance from point to line
 double distTo(P a) {
   return fabs(norm.dot(a)-off) / norm.len();
}; // 3c15
// Version for integer coordinates (long long)
struct line2i : bline2<11, vec2i, line2i> {
 line2i() : bline2{{}, 0} {}
 line2i(vec2i n, ll c) : bline2{n, c} {}
 // Returns 0 if point a lies on the line,
 // 1 if on side where normal vector points,
  // -1 if on the other side.
 int side(vec2i a) {
   11 d = norm.dot(a);
   return (d > off) - (d < off);</pre>
 } // e4ab
}; // ealb
// Version for double coordinates
// Requires cmp() from template
struct line2d : bline2<double, vec2d, line2d> {
 line2d() : bline2{{}, 0} {}
 line2d(vec2d n, double c) : bline2{n, c} {}
 // Returns 0 if point a lies on the line,
 // 1 if on side where normal vector points,
  // -1 if on the other side.
 int side(vec2d a) {
   return cmp(norm.dot(a), off);
 } // 73cb
  // Intersect this line with line a, returns
  // true on success (false if parallel).
  // Intersection point is saved to 'out'.
 bool intersect (line2d a, vec2d& out) {
   double d = norm.cross(a.norm);
   if (cmp(d, 0) == 0) return false;
   out = (norm*a.off-a.norm*off).perp() / d;
   return true;
} // 1531
}; // 516b
using line2 = line2d;
geometry/rmst.h
                                         476a
#include "../structures/find union.h"
// Rectilinear Minimum Spanning Tree
// (MST in Manhattan metric); time: O(n lq n)
// Returns MST weight. Outputs spanning tree
// to G, vertex indices match point indices.
// Edge in G is pair (target, weight).
```

ll rmst (vector < Pii > & points,

vector<vector<Pii>>> G) {

```
int n = sz(points);
 vector<pair<int, Pii>> edges;
 vector<Pii> close;
 Vi ord(n), merged(n);
 iota(all(ord), 0);
  function<void(int,int)> octant =
     [&] (int begin, int end) {
   if (begin+1 >= end) return;
   int mid = (begin+end) / 2;
   octant (begin, mid);
   octant (mid, end);
   int i = mid:
   Pii best = {INT MAX, -1};
   merged.clear();
   rep(i, begin, mid) {
     int v = ord[i];
     Pii p = points[v];
     while (j < end) {
       int e = ord[j];
        Pii q = points[e];
        if (q.x-q.y > p.x-p.y) break;
       best = min(best, make_pair(q.x+q.y, e));
        merged.pb(e);
        j++;
     } // 8576
     if (best.v != -1) {
       int alt = best.x-p.x-p.y;
        if (alt < close[v1.x)</pre>
          close[v] = {alt, best.v};
     } // 4208
     merged.pb(v);
   } // f3ff
   while (j < end) merged.pb(ord[j++]);</pre>
   copy(all(merged), ord.begin()+begin);
 }; // a4e1
  rep(i, 0, 4) {
   rep(j, 0, 2) {
     sort(all(ord), [&](int 1, int r) {
       return points[l] < points[r];</pre>
     1): // fe33
     close.assign(n, {INT MAX, -1});
     octant(0, n);
     rep(k, 0, n) {
       Pii p = close[k];
        if (p.y != -1) edges.pb(\{p.x, \{k, p.y\}\});
       points[k].x \star = -1;
     } // 1c1d
   1 // 9b38
   each (p, points) p = \{p.y, -p.x\};
 } // d06f
 11 sum = 0;
 FAU fau(n);
 sort(all(edges));
 G.assign(n, {});
 each(e, edges) if (fau.join(e.y.x, e.y.y)) {
   sum += e.x:
   G[e.y.x].pb({e.y.y, e.x});
   G[e.y.y].pb({e.y.x, e.x});
 } // b04a
 return sum;
} // f586
```

```
geometry/segment2.h
                                         6504
#include "vec2.h"
// 2D segment structure; NOT HEAVILY TESTED
// Base class of versions for ints and doubles
template < class P, class S> struct bseq2 {
 P a, b; // Endpoints
 // Distance from segment to point
 double distTo(P p) const {
   if ((p-a).dot(b-a) < 0) return (p-a).len();</pre>
    if ((p-b).dot(a-b) < 0) return (p-b).len();</pre>
    return double(abs((p-a).cross(b-a)))
                  / (b-a).len();
 1 // 62a2
}; // 85bc
// Version for integer coordinates (long long)
struct seg2i : bseg2<vec2i, seg2i> {
 seq2i() {}
 seq2i(vec2i c, vec2i d) : bseq2{c, d} {}
  // Check if segment contains point p
 bool contains(vec2i p) {
    return (a-p).dot(b-p) <= 0 &&
           (a-p).cross(b-p) == 0;
  // Compare distance to p with sqrt(d2)
  // -1 if smaller, 0 if equal, 1 if greater
 int cmpDistTo(vec2i p, 11 d2) const {
   if ((p-a).dot(b-a) < 0) {
      11 1 = (p-a).len2();
      return (1 > d2) - (1 < d2);
    } // dla6
    if ((p-b).dot(a-b) < 0) {
      11 1 = (p-b).len2();
      return (1 > d2) - (1 < d2);
    } // 9e65
    11 c = abs((p-a).cross(b-a));
    d2 = (b-a).len2();
    return (c*c > d2) - (c*c < d2);
 1 // 726d
}; // 4df2
// Version for double coordinates
// Requires cmp() from template
struct seg2d : bseg2<vec2d, seg2d> {
 seq2d() {}
 seg2d(vec2d c, vec2d d) : bseg2{c, d} {}
 bool contains(vec2d p) {
    return cmp((a-p).dot(b-p), 0) <= 0 &&
           cmp((a-p).cross(b-p), 0) == 0;
 } // b507
}; // 2036
using seg2 = seg2d;
geometry/vec2.h
                                         fbc2
// 2D point/vector structure; PARTIALLY TESTED
// Base class of versions for ints and doubles
template < class T, class S> struct bvec2 {
 T x, y;
 S operator+(S r) const {return{x+r.x,v+r.v};}
 S operator-(S r) const {return{x-r.x,y-r.y};}
 S operator*(T r) const { return {x*r, y*r}; }
 S operator/(T r) const { return {x/r, y/r}; }
 T dot(S r) const { return x*r.x+v*r.v; }
 T cross(S r) const { return x*r.y-y*r.x; }
```

```
const { return x*x + y*y; }
  T len2()
  double len() const { return sqrt(len2()); }
  S perp()
               const { return {-y,x}; } //90deg
  pair<T, T> yxPair() const { return {y,x}; }
  double angle() const { //[0;2*PI] CCW from OX
    double a = atan2(y, x);
    return (a < 0 ? a+2*M PI : a);
  } // 7095
}; // 9a6b
// Version for integer coordinates (long long)
struct vec2i : bvec2<11, vec2i> {
  vec2i() : bvec2{0, 0} {}
  vec2i(11 a, 11 b) : bvec2{a, b} {}
  bool operator==(vec2i r) const {
   return x == r.x && y == r.y;
  } // 136e
  // Compare by angle, length if angles equal
  bool operator<(vec2i r) const {</pre>
    if (upper() != r.upper()) return upper();
    auto t = cross(r);
    return t > 0 || (!t && len2() < r.len2());</pre>
  } // d6ec
  bool upper() const {
    return y > 0 \mid | (y == 0 && x >= 0);
 } // ef96
}; // 06c6
// Version for double coordinates
// Requires cmp() from template
struct vec2d : bvec2<double, vec2d> {
  vec2d() : bvec2\{0, 0\} \{\}
  vec2d(double a, double b) : bvec2{a, b} {}
  vec2d unit() const { return *this/len(); }
  vec2d rotate (double a) const { // CCW
    return {x*cos(a) - y*sin(a),
            x*sin(a) + y*cos(a); // 1890
  bool operator==(vec2d r) const {
    return !cmp(x, r.x) && !cmp(y, r.y);
  } // 81cd
  // Compare by angle, length if angles equal
  bool operator<(vec2d r) const {</pre>
   int t = cmp(angle(), r.angle());
    return t < 0 || (!t && len2()<r.len2());</pre>
 } // 84fb
}; // 3c62
using vec2 = vec2d;
graphs/2sat.h
// 2-SAT solver; time: O(n+m), space: O(n+m)
// Variables are indexed from 1 and
// negative indices represent negations!
// Usage: SAT2 sat(variable count);
```

```
// Add new var and return its index
  int addVar() {
   G.resize(sz(G)+2); return sz(G)/2;
  } // 98f3
  // Add (i => j) constraint
  void imply(int i, int j) {
   i = max(i*2-1, -i*2-2);
    j = max(j*2-1, -j*2-2);
   G[i].pb(j); G[j<sup>1</sup>].pb(i<sup>1</sup>);
  } // 7be6
  // Add (i v j) constraint
  void either(int i, int j) { imply(-i, j); }
  // Constraint at most one true variable
  void atMostOne(Vi& vars) {
    int x = addVar();
    each(i, vars) {
      int y = addVar();
      imply(x, y); imply(i, -x); imply(i, y);
      x = y;
   } // 5228
  } // 9760
  // Solve and save assignments in `values`
 bool solve() { // O(n+m), Kosaraju is used
    assign(sz(G)/2+1, -1);
    flags.assign(sz(G), 0);
    rep(i, 0, sz(G)) dfs(i);
    while (!order.empty()) {
      if (!propag(order.back()^1, 1)) return 0;
      order.pop_back();
    } // 5594
    return 1;
  } // 1e58
  void dfs(int i) {
    if (flags[i]) return;
    flags[i] = 1;
    each (e, G[i]) dfs(e);
   order.pb(i);
  } // d076
  bool propag(int i, bool first) {
   if (!flags[i]) return 1;
    flags[i] = 0;
    if (at(i/2+1) >= 0) return first;
    at (i/2+1) = i&1;
    each(e, G[i]) if (!propag(e, 0)) return 0;
    return 1;
 } // 4c1b
}; // b60c
 11 a, b, c; // a - b >= c
```

```
graphs/bellman ineq.h
                                        cd51
struct Ineq {
1: // 663a
// Solve system of inequalities of form a-b>=c
// using Bellman-Ford; time: O(n*m)
bool solveIneq(vector<Ineq>& edges,
              vector<ll>& vars) {
  rep(i, 0, sz(vars)) each(e, edges)
   vars[e.b] = min(vars[e.b], vars[e.a]-e.c);
  each (e, edges)
   if (vars[e.a]-e.c < vars[e.b]) return 0;</pre>
  return 1;
} // 241e
graphs/biconnected.h
                                        7907
```

// Biconnected components; time: O(n+m)

```
// Usage: Biconnected bi(graph);
// bi[v] = indices of components containing <math>v
// bi.verts[i] = vertices of i-th component
// bit.edges[i] = edges of i-th component
// Bridges <=> components with 2 vertices
// Articulation points <=> vertices that belong
                          to > 1 component
// Isolated vertex <=> empty component list
struct Biconnected : vector<Vi> {
 vector<Vi> verts;
 vector<vector<Pii>>> edges;
 vector<Pii> S;
 Biconnected() {}
 Biconnected (vector < Vi>& G) : S(sz(G)) {
   resize(sz(G));
   rep(i, 0, sz(G)) if (!S[i].x) dfs(G,i,-1);
   rep(c, 0, sz(verts)) each(v, verts[c])
     at (v).pb(c);
 } // 0685
 int dfs(vector<Vi>& G, int v, int p) {
   int low = S[v].x = sz(S)-1;
   S.pb(\{v, -1\});
   each(e, G[v]) if (e != p) {
     if (S[e].x < S[v].x) S.pb(\{v, e\});
     low = min(low, S[e].x ?: dfs(G, e, v));
   } // 446d
   if (p != -1 && low >= S[p].x) {
     verts.pb({p}); edges.pb({});
     rep(i, S[v].x, sz(S)) {
        if (S[i].y == -1)
         verts.back().pb(S[i].x);
          edges.back().pb(S[i]);
     } // 4fab
     S.resize(S[v].x);
   } // 6d66
   return low;
 } // 6681
1: // 497a
                                         405b
graphs/bridges online.h
// Dynamic 2-edge connectivity queries
// Usage: Bridges bridges (vertex count);
// - bridges.addEdge(u, v); - add edge (u, v)
// - bridges.cc[v] = connected component ID
// - bridges.bi(v) = 2-edge connected comp ID
struct Bridges {
 vector<Vi> G; // Spanning forest
 Vi cc, size, par, bp, seen;
 int cnt{0};
  // Initialize structure for n vertices; O(n)
 Bridges (int n = 0) : G(n), cc(n), size(n, 1),
                      par(n, -1), bp(n, -1),
                       seen(n) {
   iota(all(cc), 0);
 } // ed70
 // Add edge (u, v); time: amortized O(lg n)
 void addEdge(int u, int v) {
   if (cc[u] == cc[v]) {
     int r = lca(u, v);
     while ((v = root(v)) != r)
       v = bp[bi(v)] = par[v];
     while ((u = root(u)) != r)
```

u = bp[bi(u)] = par[u];

```
} else {
     G[u].pb(v); G[v].pb(u);
     if (size[cc[u]] > size[cc[v]]) swap(u,v);
     size[cc[v]] += size[cc[u]];
     dfs(u, v);
   } // abc7
 } // d31c
 // Get 2-edge connected component ID
 int bi(int v) { // amortized time: < O(lg n)</pre>
   return bp[v] == -1 ? v : bp[v] = bi(bp[v]);
 } // a8d0
 int root(int v) {
   return par[v] == -1 || bi(par[v]) != bi(v)
     ? v : par[v] = root(par[v]);
 } // 2d27
 void dfs(int v, int p) {
   par[v] = p; cc[v] = cc[p];
   each(e, G[v]) if (e != p) dfs(e, v);
 } // 3d81
 int lca(int u, int v) { // Don't use this!
   for (cnt++;; swap(u, v)) if (u != -1) {
     if (seen[u = root(u)] == cnt) return u;
      seen[u] = cnt; u = par[u];
   } // afed
 } // 7f56
}; // bdf6
graphs/dense dfs.h
                                         4 fbd
#include "../math/bit_matrix.h"
// DFS over bit-packed adjacency matrix
// G = NxN adjacency matrix of graph
      G(i,j) \iff (i,j) \text{ is edge}
// V = 1xN matrix containing unvisited vertices
      V(0,i) <=> i-th vertex is not visited
// Total DFS time: O(n^2/64)
struct DenseDFS {
 BitMatrix G, V; // space: O(n^2/64)
 // Initialize structure for n vertices
 DenseDFS(int n = 0) : G(n, n), V(1, n) {
   reset();
 } // 79e4
  // Mark all vertices as unvisited
 void reset() { each(x, V.M) x = -1; }
  // Get/set visited flag for i-th vertex
 void setVisited(int i) { V.set(0, i, 0); }
 bool isVisited(int i) { return !V(0, i); }
 // DFS step: func is called on each unvisited
 // neighbour of i. You need to manually call
 // setVisited(child) to mark it visited
 // or this function will call the callback
 // with the same vertex again.
 template<class T>
 void step(int i, T func) {
   ull* E = G.row(i);
   for (int w = 0; w < G.stride;) {</pre>
     ull x = E[w] & V.row(0)[w];
     if (x) func((w<<6) | __builtin_ctzll(x));</pre>
     else w++;
   } // 4c0a
 } // f045
}; // 8edb
graphs/edmonds karp.h
                                         d2ae
```

using flow t = int;

```
constexpr flow t INF = 1e9+10;
// Edmonds-Karp algorithm for finding
// maximum flow in graph; time: O(V*E^2)
// NOT HEAVILY TESTED
struct MaxFlow {
  struct Edge {
   int dst, inv;
   flow t flow, cap;
  }; // a53c
  vector<vector<Edge>> G;
  vector<flow_t> add;
  Vi prev;
  // Initialize for n vertices
 MaxFlow(int n = 0) : G(n) {}
  // Add new vertex
  int addVert() {
   G.emplace back(); return sz(G)-1;
  // Add edge between u and v with capacity cap
  // and reverse capacity rcap
  void addEdge(int u, int v,
               flow_t cap, flow_t rcap = 0) {
   G[u].pb({v, sz(G[v]), 0, cap });
   G[v].pb({ u, sz(G[u])-1, 0, rcap });
  // Compute maximum flow from src to dst.
  // Flow values can be found in edges,
  // vertices with `add` >= 0 belong to
  // cut component containing `s`.
  flow_t maxFlow(int src, int dst) {
   flow t f = 0;
    each (v, G) each (e, v) e.flow = 0;
    do {
     queue<int> 0:
     O.push(src);
     prev.assign(sz(G), -1);
     add.assign(sz(G), -1);
     add[src] = INF;
      while (!O.empty()) {
       int i = 0.front();
       flow t m = add[i];
       () goq. ();
       if (i == dst) {
          while (i != src) {
            auto& e = G[i][prev[i]];
           e.flow -= m;
           G[e.dst][e.inv].flow += m;
           i = e.dst;
         1 // 35e6
         f += m;
         break:
       } // 857e
        each(e, G[i]) if (add[e.dst] < 0) {
         if (e.flow < e.cap) {</pre>
           Q.push (e.dst);
           prev[e.dst] = e.inv;
           add[e.dst] = min(m, e.cap-e.flow);
         } // 4cdb
       } // 1ea5
     } // bbb0
    } while (prev[dst] != -1);
    return f;
  } // d492
```

```
// Get if v belongs to cut component with src
 bool cutSide(int v) {
   return add[v] >= 0;
 } // 41e9
}; // afff
graphs/gomory hu.h
                                         a520
#include "edmonds karp.h"
//#include "push relabel.h" // if you need
struct Edge {
 int a, b; // vertices
 flow t w; // weight
}; // c331
// Build Gomory-Hu tree; time: O(n*maxflow)
// Gomory-Hu tree encodes minimum cuts between
// all pairs of vertices: mincut for u and v
// is equal to minimum on path from u and v
// in Gomory-Hu tree. n is vertex count.
// Returns vector of Gomory-Hu tree edges.
vector<Edge> gomoryHu (vector<Edge> edges,
                      int n) {
 MaxFlow flow(n);
 each (e, edges) flow.addEdge (e.a,e.b,e.w,e.w);
 vector<Edge> ret(n-1);
 rep(i, 1, n) ret[i-1] = {i, 0, 0};
 rep(i, 1, n) {
   ret[i-1].w = flow.maxFlow(i, ret[i-1].b);
   rep(j, i+1, n)
      if (ret[j-1].b == ret[i-1].b &&
          flow.cutSide(j)) ret[j-1].b = i;
 } // 5ae4
 return ret;
} // afdb
graphs/matroids.h
// Find largest subset S of [n] such that
// S is independent in both matroid A and B.
// A and B are given by their oracles,
// see example implementations below.
// Returns vector V such that V[i] = 1 iff
// i-th element is included in found set;
// time: O(r^2*init + r^2*n*add),
// where r is max independent set,
// `init` is max time of oracles init
// and `add` is max time of oracles canAdd.
template < class T, class U>
vector<bool> intersectMatroids (T& A, U& B,
                               int n) {
 vector<bool> ans(n);
 bool ok = 1:
 A.init(ans);
 B.init(ans);
 rep(i, 0, n) if (A.canAdd(i) && B.canAdd(i))
    ans[i] = 1, A.init(ans), B.init(ans);
  while (ok) {
   vector<Vi> G(n);
    vector<bool> good(n);
    queue<int> que;
    Vi prev(n, -1);
   A.init(ans);
   B.init(ans);
    ok = 0;
   rep(i, 0, n) if (!ans[i]) {
```

```
if (A.canAdd(i)) que.push(i), prev[i]=-2;
             good[i] = B.canAdd(i);
           } // 9581
           rep(i, 0, n) if (ans[i]) {
             ans[i] = 0;
             A.init(ans);
             B.init(ans);
             rep(j, 0, n) if (i != j && !ans[j]) {
               if (A.canAdd(j)) G[i].pb(j);
               if (B.canAdd(j)) G[j].pb(i);
             } // bd2a
             ans[i] = 1;
           } // bf3e
           while (!que.empty()) {
             int i = que.front();
             que.pop();
             if (good[i]) {
               ans[i] = 1;
               while (prev[i] >= 0) {
                 ans[i = prev[i]] = 0;
                 ans[i = prev[i]] = 1;
               } // 51c8
               ok = 1;
               break;
             } // 384b
             each(j, G[i]) if (prev[j] == -1)
               que.push(j), prev[j] = i;
           } // 6eb6
         } // e092
         return ans:
       } // ae8e
       // Matroid where each element has color
       // and set is independent iff for each color c
       // #{elements of color c} <= maxAllowed[c].</pre>
55ef | struct LimOracle {
         Vi color: // color[i] = color of i-th element
         Vi maxAllowed; // Limits for colors
         // Init oracle for independent set S: O(n)
         void init(vector<bool>& S) {
           tmp = maxAllowed;
           rep(i, 0, sz(S)) tmp[color[i]] -= S[i];
         1 // 4dfb
         // Check if S+{k} is independent; time: O(1)
         bool canAdd(int k) {
           return tmp[color[k]] > 0;
        } // e312
       1: // 7b5d
       // Graphic matroid - each element is edge,
       // set is independent iff subgraph is acyclic.
       struct GraphOracle {
         vector<Pii> elems; // Ground set: graph edges
         int n; // Number of vertices, indexed [0;n-1]
         Vi par:
         int find(int i) {
           return par[i] == -1 ? i
             : par[i] = find(par[i]);
         } // b8b7
         // Init oracle for independent set S; ~O(n)
         void init(vector<bool>& S) {
           par.assign(n, -1);
           rep(i, 0, sz(S)) if (S[i])
             par[find(elems[i].x)] = find(elems[i].y);
```

```
1 // 1827
  // Check if S+{k} is independent; time: ~O(1)
 bool canAdd(int k) {
    return
      find(elems[k].x) != find(elems[k].y);
 } // 8ca4
}; // c506
// Co-graphic matroid - each element is edge,
// set is independent iff after removing edges
// from graph number of connected components
// doesn't change.
struct CographOracle {
 vector<Pii> elems; // Ground set: graph edges
 int n: // Number of vertices, indexed [0:n-1]
 vector<Vi> G;
 Vi pre, low:
 int cnt;
 int dfs(int v, int p) {
   pre[v] = low[v] = ++cnt;
    each(e, G[v]) if (e != p)
     low[v] = min(low[v], pre[e] ?: dfs(e,v));
    return low[v]:
 } // 9d30
  // Init oracle for independent set S; O(n)
 void init(vector<bool>& S) {
   G.assign(n, {});
    pre.assign(n, 0);
    low.resize(n);
    cnt = 0;
    rep(i, 0, sz(S)) if (!S[i]) {
      Pii e = elems[i];
      G[e.x].pb(e.v);
      G[e.v].pb(e.x);
    } // 79a1
    rep(v, 0, n) if (!pre[v]) dfs(v, -1);
 } // 1200
  // Check if S+{k} is independent; time: O(1)
 bool canAdd(int k) {
    Pii e = elems[k];
    return max(pre[e.x], pre[e.y])
      != max(low[e.x], low[e.v]);
 } // 2550
}; // a5cc
// Matroid equivalent to linear space with XOR
struct XorOracle {
 vector<ll> elems; // Ground set: numbers
 vector<11> base:
  // Init for independent set S; O(n+r^2)
 void init(vector<bool>& S) {
    base.assign(63, 0);
    rep(i, 0, sz(S)) if (S[i]) {
      11 e = elems[i];
      rep(j, 0, sz(base)) if ((e >> j) & 1) {
       if (!base[j]) {
          base[j] = e;
         break:
       } // 1df5
        e ^= base[j];
      } // 8495
   } // 655e
 } // b68c
  // Check if S+{k} is independent; time: O(r)
 bool canAdd(int k) {
    11 e = elems[k];
```

```
rep(i, 0, sz(base)) if ((e >> i) & 1) {
     if (!base[i]) return 1;
     e ^= base[i];
    } // 49d1
    return 0;
 } // 66ff
}; // 4af3
graphs/push_relabel.h
                                          2a0c
using flow t = int;
constexpr flow_t INF = 1e9+10;
// Push-relabel algorithm for maximum flow;
// O(V^2*sqrt(E)), but very fast in practice.
// Preflow is not converted to flow!
// UNTESTED
struct MaxFlow {
  struct Edge {
    int to, inv;
    flow_t rem, cap;
  }; // bc77
  vector<basic_string<Edge>> G;
  vector<flow_t> extra;
  Vi hei, arc, prv, nxt, act, bot;
  queue<int> Q;
  int n, high, cut, work;
  // Initialize for n vertices
  MaxFlow(int k = 0) : G(k) {}
  // Add new vertex
  int addVert() {
   G.emplace_back();
   return sz(G)-1;
  } // 907a
  // Add edge between u and v with
  // capacity cap and reverse capacity rcap
  void addEdge(int u, int v,
               flow t cap, flow t rcap = 0) {
    G[u].pb({ v, sz(G[v]), 0, cap });
   G[v].pb({ u, sz(G[u])-1, 0, rcap });
  } // Of10
  void raise(int v, int h) {
    if (hei[v] < n)</pre>
     prv[nxt[prv[v]] = nxt[v]] = prv[v];
    if ((hei[v] = h) < n) {</pre>
     if (extra[v] > 0) {
       bot[v] = act[h], act[h] = v;
       high = max(high, h);
      } // Oae9
      cut = max(cut, h);
     nxt[v] = nxt[prv[v] = h += n];
     prv[nxt[nxt[h] = v]] = v;
    } // 9bcf
  ) // 1c35
  void global(int t) {
   hei.assign(n, n);
    act.assign(n, -1);
    iota(all(prv), 0);
    iota(all(nxt), 0);
    hei[t] = high = cut = work = 0;
    for (Q.push(t); !Q.empty(); Q.pop()) {
     int v = 0.front();
      each(e, G[v])
       if (hei[e.to]==n && G[e.to][e.inv].rem)
          Q.push (e.to), raise (e.to, hei[v]+1);
    1 // 4edc
 } // d78f
```

```
void push(int v, Edge& e) {
    auto f = min(extra[v], e.rem);
    if (f > 0) {
     if (!extra[e.to]) {
        bot[e.to] = act[hei[e.to]];
        act[hei[e.to]] = e.to;
     } // 9d90
      e.rem -= f; G[e.to][e.inv].rem += f;
     extra[v] -= f; extra[e.to] += f;
   } // a86a
 } // 94aa
 void discharge(int v) {
   int h = n;
    auto go = [&] (int a, int b) {
     rep(i, a, b) {
        auto& e = G[v][i];
        if (e.rem) {
         if (hei[v] == hei[e.to]+1) {
           push(v, e);
            if (extra[v] <= 0)</pre>
              return arc[v] = i, 0;
         } else h = min(h, hei[e.to]+1);
       } // 8adf
     } // 6369
     return 1;
   }; // 0671
    if (go(arc[v], sz(G[v])) & go(0, arc[v])){
      int k = hei[v] + n;
     if (nxt[k] == prv[k]) {
        rep(i, k, cut+n+1)
          while (nxt[j] < n) raise(nxt[j], n);</pre>
        cut = k-n-1;
     } else raise(v, h), work++;
   } // dcb2
 ) // 4d2f
  // Compute maximum flow from src to dst
 flow t maxFlow(int src, int dst) {
   extra.assign(n = sz(G), 0);
   hei.assign(n, 0);
    arc.assign(n, 0);
   prv.resize(n*2);
   nxt.resize(n*2);
    act.resize(n);
   bot.resize(n);
    each (v, G) each (e, v) e.rem = e.cap;
    extra[dst] = -(extra[src] = INF);
    each (e, G[src]) push (src, e);
   global (dst);
    for (; high; high--)
     while (act[high] != -1) {
        int v = act[high];
        act[high] = bot[v];
        if (hei[v] == high) {
          discharge(v);
          if (work > 4*n) global(dst);
       } // 21cf
      } // b0c8
   return extra[dst] + INF;
  } // 8e2f
  // Get if v belongs to cut component with src
 bool cutSide(int v) { return hei[v] >= n; }
}; // 44ea
```

```
graphs/scc.h
                                          1c43
// Tarjan's SCC algorithm; time: O(n+m)
// Usage: SCC scc(graph);
// scc[v] = index of SCC for vertex v
// scc.comps[i] = vertices of i-th SCC
// Components are in reversed topological order
struct SCC : Vi {
 vector<Vi> comps;
 Vi S;
  SCC() {}
  SCC(vector\langle Vi \rangle \& G): Vi(sz(G),-1), S(sz(G)) {
   rep(i, 0, sz(G)) if (!S[i]) dfs(G, i);
  } // f0fa
  int dfs(vector<Vi>& G, int v) {
   int low = S[v] = sz(S);
    S.pb(v);
    each(e, G[v]) if (at(e) < 0)
      low = min(low, S[e] ?: dfs(G, e));
    if (low == S[v]) {
      comps.pb({});
      rep(i, S[v], sz(S)) {
        at(S[i]) = sz(comps)-1;
        comps.back().pb(S[i]);
      } // 8ed0
      S.resize(S[v]);
    } // ecc7
    return low;
 } // f3c6
1: // 215e
graphs/turbo matching.h
                                          d400
// Find maximum bipartite matching; time: ?
// G must be bipartite graph!
// Returns matching size (edge count).
// match[v] = vert matched to v or -1
int matching (vector < Vi>& G, Vi& match) {
 vector<bool> seen;
  int n = 0, k = 1;
  match.assign(sz(G), -1);
  function<int(int)> dfs = [&](int i) {
    if (seen[i]) return 0;
    seen[i] = 1;
    each(e, G[i]) {
      if (match[e] < 0 || dfs(match[e])) {</pre>
        match[i] = e; match[e] = i;
        return 1;
     } // 893d
    1 // 9532
    return 0;
  1: // d332
  while (k) {
    seen.assign(sz(G), 0);
    k = 0;
    rep(i, 0, sz(G)) if (match[i] < 0)
      k += dfs(i);
   n += k;
 } // 1128
 return n;
1 // 0d38
// Convert maximum matching to vertex cover
// time: O(n+m)
Vi vertexCover(vector<Vi>& G, Vi& match) {
 Vi ret, col(sz(G)), seen(sz(G));
```

```
function<void(int, int)> dfs =
      [&] (int i, int c) {
   if (col[i]) return;
   col[i] = c+1;
   each(e, G[i]) dfs(e, !c);
 }; // 1f1b
 function<void(int) > aug = [&](int i) {
   if (seen[i] || col[i] != 1) return;
   seen[i] = 1;
   each(e, G[i]) seen[e] = 1, aug(match[e]);
 }; // 2465
 rep(i, 0, sz(G)) dfs(i, 0);
 rep(i, 0, sz(G)) if (match[i] < 0) aug(i);
 rep(i, 0, sz(G))
   if (seen[i] == col[i]-1) ret.pb(i);
 return ret:
} // 6f72
math/berlekamp massev.h
                                         c714
constexpr int MOD = 1e9+7;
11 modInv(11 a, 11 m) { // a^(-1) mod m
 if (a == 1) return 1;
 return ((a - modInv(m%a, a))*m + 1) / a;
1 // c437
// Find shortest linear recurrence that matches
// given starting terms of recurrence; O(n^2)
// Returns vector C such that for each i >= |C|
// A[i] = sum A[i-j-1]*C[j] for j = 0...|C|-1
// UNTESTED
vector<ll> massey (vector<ll>& A) {
 int n = sz(A), len = 0, k = 0;
 11 s = 1:
 vector<ll> B(n), C(n), tmp;
 B[0] = C[0] = 1;
 rep(i, 0, n) {
   11 d = 0;
   k++;
   rep(j, 0, len+1)
     d = (d + C[j] * A[i-j]) % MOD;
   if (d) {
     11 q = d * modInv(s, MOD) % MOD;
     tmp = C;
      rep(j, k, n)
       C[j] = (C[j] - q * B[j-k]) % MOD;
     if (len*2 <= i) {</pre>
       B.swap(tmp);
       len = i-len+1;
       s = d + (d < 0) * MOD;
       k = 0;
     } // c350
   } // 79c7
 } // f70c
 C.resize(len+1);
 C.erase(C.begin());
 each (x, C) x = (MOD - x) % MOD;
 return C:
} // 4a08
                                         13eb
math/bit gauss.h
constexpr int MAX_COLS = 2048;
```

// Solve system of linear equations over Z 2

// - A - extended matrix, rows are equations,

// time: $O(n^2*m/W)$, where W is word size

```
columns are variables.
         m-th column is equation result
         (A[i][j] - i-th row and j-th column)
// - ans - output for variables values
// - m - variable count
// Returns 0 if no solutions found, 1 if one,
// 2 if more than 1 solution exist.
int bitGauss (vector < bitset < MAX COLS >> & A,
             vector<bool>& ans, int m) {
  Vi col;
  ans.assign(m, 0);
  rep(i, 0, sz(A)) {
   int c = int(A[i]._Find_first());
   if (c >= m) {
     if (c == m) return 0;
     continue;
    } // a6bb
    rep(k, i+1, sz(A)) if (A[k][c]) A[k]^=A[i];
    swap(A[i], A[sz(col)]);
    col.pb(c);
  } // a953
  for (int i = sz(col); i--;) if (A[i][m]) {
   ans[col[i]] = 1;
    rep(k,0,i) if(A[k][col[i]]) A[k][m].flip();
  } // 4ca1
  return sz(col) < m ? 2 : 1;</pre>
} // 996e
                                         2e3f
math/bit matrix.h
using ull = uint64 t;
// Matrix over Z_2 (bits and xor)
// TODO: arithmetic operations
struct BitMatrix {
  vector<ull> M:
  int rows, cols, stride:
  // Create matrix with n rows and m columns
  BitMatrix(int n = 0, int m = 0) {
   rows = n; cols = m;
   stride = (m+63)/64;
   M.resize(n*stride);
  } // 7ef0
  // Get pointer to bit-packed data of i-th row
  ull* row(int i) { return &M[i*stride]; }
  // Get value in i-th row and j-th column
  bool operator()(int i, int j) {
   return (row(i)[j/64] >> (j%64)) & 1;
  } // 28bd
  // Set value in i-th row and j-th column
  void set(int i, int j, bool val) {
   ull \&w = row(i)[j/64], m = 1ull << (j%64);
   if (val) w |= m;
   else w &= ~m;
  } // 98a8
1: // 4df7
math/crt.h
                                         8a85
using Pll = pair<11, 11>;
ll egcd(ll a, ll b, ll& x, ll& y) {
  if (!a) return x=0, y=1, b;
 11 d = egcd(b%a, a, y, x);
  x = b/a*v;
  return d;
} // 23c8
```

```
// Chinese Remainder Theoerem; time: O(lg lcm)
// Solves x = a.x \pmod{a.y}, x = b.x \pmod{b.y}
// Returns pair (x mod lcm, lcm(a.y, b.y))
// or (-1, -1) if there's no solution.
// WARNING: a.x and b.x are assumed to be
// in [0;a.y) and [0;b.y) respectively.
// Works properly if lcm(a.y, b.y) < 2^63.
Pll crt(Pll a, Pll b) {
  if (a.y < b.y) swap(a, b);</pre>
 ll x, y, g = egcd(a.y, b.y, x, y);
 11 c = b.x-a.x, d = b.y/g, p = a.y*d;
  if (c % q) return {-1, -1};
 11 s = (a.x + c/g*x % d * a.y) % p;
  return {s < 0 ? s+p : s, p};
1 // 35a8
math/fft complex.h
                                          31ee
using dbl = double;
using cmpl = complex<dbl>;
// Default std::complex multiplication is slow.
// You can use this to achieve small speedup.
cmpl operator*(cmpl a, cmpl b) {
  dbl ax = real(a), ay = imag(a);
  dbl bx = real(b), by = imag(b);
  return {ax*bx-ay*by, ax*by+ay*bx};
1 // 3b78
cmpl operator*=(cmpl& a,cmpl b) {return a=a*b;}
// Compute DFT over complex numbers; O(n lq n)
// Input size must be power of 2!
void fft(vector<cmpl>& a) {
  static vector<cmpl> w(2, 1);
  int n = sz(a);
  for (int k = sz(w); k < n; k *= 2) {
   w.resize(n);
    rep(i,0,k) w[k+i] = \exp(\text{cmpl}(0, M_PI*i/k));
 } // 92a9
  rep(i,0,n) rev[i] = (rev[i/2] | i\%2*n) / 2;
  rep(i,0,n) if(i<rev[i]) swap(a[i],a[rev[i]]);
  for (int k = 1; k < n; k *= 2) {
   for (int i=0; i < n; i += k*2) rep(j,0,k) {
      auto d = a[i+j+k] * w[j+k];
      a[i+j+k] = a[i+j] - d;
     a[i+j] += d;
   } // b389
 } // 84bf
} // adf8
// Convolve complex-valued a and b.
// store result in a; time: O(n lq n), 3x FFT
void convolve(vector<cmpl>& a, vector<cmpl> b){
  int len = max(sz(a) + sz(b) - 1, 0);
  int n = 1 << (32 - __builtin_clz(len));</pre>
  a.resize(n); b.resize(n);
  fft(a); fft(b);
  rep(i, 0, n) a[i] \star= b[i] / dbl(n);
  reverse(a.begin()+1, a.end());
  fft(a);
 a.resize(len);
} // 7987
// Convolve real-valued a and b, returns result
// time: O(n lq n), 2x FFT
// Rounding to integers is safe as long as
// (max coeff<sup>2</sup>) *n*log 2(n) < 9*10<sup>14</sup>
// (in practice 10^16 or higher).
```

```
vector<dbl> convolve(vector<dbl>& a.
                     vector<dbl>& b) {
  int len = \max(sz(a) + sz(b) - 1, 0);
  int n = 1 << (32 - __builtin_clz(len));</pre>
  vector<cmpl> in(n), out(n);
  rep(i, 0, sz(a)) in[i].real(a[i]);
  rep(i, 0, sz(b)) in[i].imag(b[i]);
  fft(in);
  each(x, in) x \star = x;
  rep(i,0,n) out[i] = in[-i&(n-1)]-conj(in[i]);
  fft (out);
  vector<dbl> ret(len);
  rep(i, 0, len) ret[i] = imag(out[i]) / (n*4);
  return ret;
} // 19ed
constexpr 11 MOD = 1e9+7;
// High precision convolution of integer-valued
// a and b mod MOD; time: O(n lg n), 4x FFT
// Input is expected to be in range [0;MOD)!
// Rounding is safe if MOD*n*log 2(n) < 9*10^14
// (in practice 10^16 or higher).
vector<ll> convMod(vector<ll>& a,
                   vector<11>& b) {
  vector<11> ret(sz(a) + sz(b) - 1);
  int n = 1 \ll (32 - builtin clz(sz(ret)));
  11 cut = 11(sqrt(MOD))+1;
  vector<cmpl> c(n), d(n), g(n), f(n);
  rep(i, 0, sz(a))
    c[i] = {dbl(a[i]/cut), dbl(a[i]%cut)};
  rep(i, 0, sz(b))
    d[i] = {dbl(b[i]/cut), dbl(b[i]%cut)};
  fft(c); fft(d);
  rep(i, 0, n) {
    int j = -i & (n-1);
    f[j] = (c[i] + conj(c[j])) * d[i] / (n*2.0);
    q[j] =
      (c[i]-conj(c[j])) * d[i] / cmpl(0, n*2);
  } // e877
  fft(f); fft(q);
  rep(i, 0, sz(ret)) {
    11 t = llround(real(f[i])) % MOD * cut;
    t += llround(imag(f[i]));
    t = (t + llround(real(g[i]))) % MOD * cut;
    t = (t + llround(imag(g[i]))) % MOD;
    ret[i] = (t < 0 ? t+MOD : t);
  } // e75d
  return ret:
} // 513f
math/fft mod.h
                                          17aa
// Number Theoretic Tranform (NTT)
// For functions below you can choose 2 params:
// 1. M - prime modulus that MUST BE of form
         a*2^k+1, computation is done in Z_M
// 2. R - generator of Z M
// Modulus often seen on Codeforces:
//M = (119 << 23) + 1, R = 62; M is 998244353
// Parameters for 11 computation with CRT:
//M = (479 << 21) + 1, R = 62; M is > 10^9
// M = (483<<21)+1, R = 62; M is > 10^9
ll modPow(ll a, ll e, ll m) {
```

```
11 t = 1 % m;
  while (e) {
    if (e % 2) t = t*a % m;
    e /= 2; a = a*a % m;
 } // 66ca
 return t:
} // 1973
// Compute DFT over Z M with generator R.
// Input size must be power of 2; O(n lq n)
// Input is expected to be in range [0;MOD)!
// dit == true <=> inverse transform * 2^n
                   (without normalization)
template<11 M, 11 R, bool dit>
void ntt(vector<11>& a) {
  static vector<ll> w(2, 1);
  int n = sz(a);
  for (int k = sz(w); k < n; k *= 2) {
    w.resize(n, 1);
    ll c = modPow(R, M/2/k, M);
    if (dit) c = modPow(c, M-2, M);
    rep(i, k+1, k*2) w[i] = w[i-1]*c % M;
  } // 0d98
  for (int t = 1; t < n; t *= 2) {
    int k = (dit ? t : n/t/2);
    for (int i=0; i < n; i += k*2) rep(j,0,k) {
      11 &c = a[i+j], &d = a[i+j+k];
      ll e = w[j+k], f = d;
      d = (dit ? c - (f=f*e%M) : (c-f)*e % M);
      if (d < 0) d += M;
      if ((c += f) >= M) c -= M;
    } // e4a6
 } // 8d38
} // 01f5
// Convolve a and b mod M (R is generator).
// store result in a; time: O(n lq n), 3x NTT
// Input is expected to be in range [0:MOD]!
template<11 M = (119<<23)+1, 11 R = 62>
void convolve(vector<11>& a, vector<11> b) {
 int len = \max(sz(a) + sz(b) - 1, 0);
  int n = 1 << (32 - __builtin_clz(len));</pre>
 11 t = modPow(n, M-2, M);
  a.resize(n); b.resize(n);
  ntt < M, R, 0 > (a); ntt < M, R, 0 > (b);
  rep(i, 0, n) a[i] = a[i] *b[i] % M * t % M;
  ntt<M,R,1>(a);
 a.resize(len):
} // 4b4d
ll egcd(ll a, ll b, ll& x, ll& y) {
 if (!a) return x=0, y=1, b;
 ll d = egcd(b%a, a, y, x);
 x = b/a*v:
 return d:
} // 23c8
// Convolve a and b with 64-bit output.
// store result in a; time: O(n lg n), 6x NTT
// Input is expected to be non-negative!
void convLong(vector<11>& a, vector<11> b) {
  const 11 M1 = (479<<21)+1, M2 = (483<<21)+1;
  const 11 MX = M1*M2, R = 62;
  vector<11> c = a, d = b;
  each(k, a) k %= M1; each(k, b) k %= M1;
  each(k, c) k %= M2; each(k, d) k %= M2;
  convolve<M1, R>(a, b);
  convolve<M2, R>(c, d);
```

```
ll x, y; egcd(M1, M2, x, y);
  rep(i, 0, sz(a)) {
   a[i] += (c[i]-a[i]) *x % M2 * M1;
   if ((a[i] %= MX) < 0) a[i] += MX;</pre>
  } // 2279
} // ef93
math/fwht.h
                                          3e6f
// Fast Walsh-Hadamard Transform; O(n lg n)
// Input must be power of 2!
// Uncommented version is for XOR.
// OR version is equivalent to sum-over-subsets
// (Zeta transform, inverse is Moebius).
// AND version is same as sum-over-supersets.
// TESTED ON RANDS
template < bool inv, class T>
void fwht(vector<T>& b) {
  for (int s = 1; s < sz(b); s *= 2) {
    for (int i = 0; i < sz(b); i += s*2) {
      rep(j, i, i+s) {
       auto &x = b[j], &y = b[j+s];
       tie(x, y) =
           mp(x+y, x-y);
       // inv ? mp(x-y, y) : mp(x+y, y); //AND
       // inv ? mp(x, y-x) : mp(x, x+y); //OR
     } // eea9
   } // a3d5
  } // 95ed
  // ONLY FOR XOR:
 if (inv) each(e, b) e /= sz(b);
} // 0779
// Compute convolution of a and b such that
// ans[i#j] += a[i]*b[j], where # is OR, AND
// or XOR, depending on FWHT version.
// Stores result in a; time: O(n lg n)
// Both arrays must be of same size = 2^n!
template<class T>
void bitConv(vector<T>& a, vector<T> b) {
  fwht<0>(a);
  fwht<0>(b);
  rep(i, 0, sz(a)) a[i] *= b[i];
 fwht<1>(a);
} // 7b82
math/gauss.h
                                          7f0b
// Solve system of linear equations; O(n^2*m)
// - A - extended matrix, rows are equations,
         columns are variables,
         m-th column is equation result
         (A[i][i] - i-th row and i-th column)
// - ans - output for variables values
// - m - variable count
// Returns 0 if no solutions found, 1 if one,
// 2 if more than 1 solution exist.
int gauss (vector < vector < double >> & A,
          vector<double>& ans, int m) {
  ans.assign(m, 0);
  rep(i, 0, sz(A)) {
    int c = 0:
    while (c <= m && !cmp(A[i][c], 0)) c++;</pre>
    // For Zp:
    //while (c <= m && !A[i][c].x) c++;
    if (c >= m) {
     if (c == m) return 0;
      continue;
```

```
} // a6bb
    rep(k, i+1, sz(A)) {
     auto mult = A[k][c] / A[i][c];
     rep(j, 0, m+1) A[k][j] -= A[i][j]*mult;
   } // 8dd5
    swap(A[i], A[sz(col)]);
   col.pb(c);
 } // ea2c
  for (int i = sz(col); i--;) {
   ans[col[i]] = A[i][m] / A[i][col[i]];
   rep(k, 0, i)
     A[k][m] = ans[col[i]] * A[k][col[i]];
  return sz(col) < m ? 2 : 1;</pre>
} // 0b76
math/matrix.h
                                          9hf7
#include "modular.h"
// UNTESTED
using Row = vector<Zp>;
using Matrix = vector<Row>;
// Create n x n identity matrix
Matrix ident(int n) {
 Matrix ret(n, Row(n));
 rep(i, 0, n) ret[i][i] = 1;
 return ret;
} // ad1d
// Add matrices
Matrix& operator+= (Matrix& 1, const Matrix& r) {
 rep(i, 0, sz(l)) rep(k, 0, sz(l[0]))
   l[i][k] += r[i][k];
 return 1:
} // b6bf
Matrix operator+ (Matrix 1, const Matrix& r) {
 return 1 += r;
} // d9b3
// Subtract matrices
Matrix& operator = (Matrix& 1, const Matrix& r) {
 rep(i, 0, sz(1)) rep(k, 0, sz(1[0]))
   l[i][k] = r[i][k];
 return 1;
1 // 90a1
Matrix operator-(Matrix 1, const Matrix& r) {
 return 1 -= r;
} // dc4f
// Multiply matrices
Matrix operator*(const Matrix& 1,
                 const Matrix& r) {
 Matrix ret(sz(1), Row(sz(r[0])));
 rep(i, 0, sz(l)) rep(j, 0, sz(r[0]))
   rep(k, 0, sz(r))
     ret[i][j] += l[i][k] * r[k][j];
 return ret;
} // 52ca
Matrix& operator *= (Matrix& 1, const Matrix& r) {
 return 1 = 1*r;
} // da8a
// Square matrix power; time: O(n^3 * 1g e)
Matrix pow (Matrix a, 11 e) {
 Matrix t = ident(sz(a));
 while (e) {
   if (e % 2) t *= a;
   e /= 2; a *= a;
                                                  // Miller-Rabin primality test
```

```
1 // 4400
 return t;
} // 65ea
// Transpose matrix
Matrix transpose (const Matrix& m) {
 Matrix ret(sz(m[0]), Row(sz(m)));
 rep(i, 0, sz(m)) rep(j, 0, sz(m[0]))
   ret[i][i] = m[i][i];
 return ret;
} // 5650
// Transform matrix to echelon form
// and compute its determinant sign and rank.
int echelon(Matrix& A, int& sign) { // O(n^3)
 int rank = 0;
 sign = 1;
 rep(c, 0, sz(A[0])) {
   if (rank >= sz(A)) break;
   rep(i, rank+1, sz(A)) if (A[i][c].x) {
     swap(A[i], A[rank]);
     sign *=-1;
     break:
   } // f98a
   if (A[rank][c].x) {
     rep(i, rank+1, sz(A)) {
        auto mult = A[i][c] / A[rank][c];
       rep(j, 0, sz(A[0]))
         A[i][j] -= A[rank][j]*mult;
     } // f519
     rank++;
   } // 4cd8
 } // 36e9
return rank;
} // 6882
// Compute matrix rank; time: O(n^3)
#define rank rank
int rank (Matrix A) {
int s; return echelon(A, s);
1 // c599
// Compute square matrix determinant: O(n^3)
Zp det (Matrix A) {
 int s; echelon(A, s);
 Zp ret = s:
 rep(i, 0, sz(A)) ret *= A[i][i];
 return ret;
1 // b252
// Invert square matrix if possible; O(n^3)
// Returns true if matrix is invertible.
bool invert (Matrix & A) {
 int s, n = sz(A);
 rep(i, 0, n) A[i].resize(n*2), A[i][n+i] = 1;
 echelon(A, s):
 for (int i = n; i--;) {
   if (!A[i][i].x) return 0;
   auto mult = A[i][i].inv();
   each(k, A[i]) k \star= mult;
   rep(k, 0, i) rep(j, 0, n)
     A[k][n+j] -= A[i][n+j]*A[k][i];
 } // 1e97
 each (r, A) r.erase (r.begin(), r.begin()+n);
 return 1;
} // 65b9
math/miller rabin.h
                                         7005
#include "modular64.h"
```

```
// time O(k*lg^2 n), where k = number of bases
// Deterministic for p <= 10^9
// constexpr 11 BASES[] = {
// 336781006125, 9639812373923155
// }; // d41d
// Deterministic for p <= 2^64
constexpr 11 BASES[] = {
 2,325,9375,28178,450775,9780504,1795265022
}; // b8e0
bool isPrime(ll p) {
 if (p <= 2) return p == 2;</pre>
 if (p%2 == 0) return 0:
 11 d = p-1, t = 0;
 while (d%2 == 0) d /= 2, t++;
  each(a, BASES) if (a%p) {
    // 11 a = rand() % (p-1) + 1;
   11 b = modPow(a\%p, d, p);
    if (b == 1 || b == p-1) continue;
    rep(i, 1, t)
     if ((b = modMul(b, b, p)) == p-1) break;
    if (b != p-1) return 0;
 } // 9342
 return 1;
} // bec2
                                         2882
math/modinv precompute.h
constexpr 11 MOD = 234567899;
vector<ll> modInv(MOD); // You can lower size
// Precompute modular inverses; time: O(MOD)
void initModInv() {
 modInv[1] = 1;
 rep(i, 2, sz(modInv)) modInv[i] =
    (MOD - (MOD/i) * modInv[MOD%i]) % MOD;
} // 22c1
math/modular.h
                                         71e5
// Modulus often seen on Codeforces:
constexpr int MOD = 998244353;
// Some big prime: 15*(1<<27)+1 ~ 2*10^9
ll modInv(ll a, ll m) { // a^{(-1)} \mod m
 if (a == 1) return 1;
 return ((a - modInv(m%a, a)) *m + 1) / a;
11 modPow(11 a, 11 e, 11 m) { // a^e mod m
 11 t = 1 % m;
 while (e) {
    if (e % 2) t = t*a % m;
   e /= 2; a = a*a % m;
 } // 66ca
 return t:
} // 1973
// Wrapper for modular arithmetic
struct Zp {
 11 x; // Contained value, in range [0; MOD-1]
 Zp() : x(0) {}
 Zp(11 a) : x(a\%MOD) { if (x < 0) x += MOD; }
  #define OP(c,d) Zp\& operator c#=(Zp r) \{ \
     x = x d; return *this; } \
    Zp operator c(Zp r) const { \
      Zp t = *this; return t c##= r; } // e986
 OP(+, +r.x - MOD*(x+r.x >= MOD));
 OP(-, -r.x + MOD*(x-r.x < 0));
```

```
OP(*, *r.x % MOD);
  OP(/, *r.inv().x % MOD);
  Zp operator-()
    const { Zp t; t.x = MOD-x; return t; }
  // For composite modulus use modInv, not pow
  Zp inv() const { return pow(MOD-2); }
  Zp pow(ll e) const{ return modPow(x,e,MOD); }
  void print() { cerr << x; } // For deb()</pre>
}; // 407f
// Extended Euclidean Algorithm
ll egcd(ll a, ll b, ll& x, ll& y) {
 if (!a) return x=0, y=1, b;
 11 d = egcd(b%a, a, y, x);
  x = b/a*y;
  return d;
1 // 23c8
math/modular64.h
                                         4b73
// Modular arithmetic for modulus < 2^62
11 modAdd(11 x, 11 y, 11 m) {
 x += y;
  return x < m ? x : x-m;</pre>
} // b653
11 modSub(11 x, 11 y, 11 m) {
 x -= y;
 return x >= 0 ? x : x+m;
1 // b073
// About 4x slower than normal modulo
11 modMul(ll a, ll b, ll m) {
 11 c = 11((long double) a * b / m);
 11 r = (a*b - c*m) % m;
  return r < 0 ? r+m : r;
) // 1815
ll modPow(ll x, ll e, ll m) {
 11 t = 1:
  while (e) {
   if (e & 1) t = modMul(t, x, m);
   e >>= 1;
   x = modMul(x, x, m);
  } // bd61
  return t;
} // c8ba
                                         845b
math/modular generator.h
#include "modular.h" // modPow
// Get unique prime factors of n; O(sqrt n)
vector<ll> factorize(ll n) {
  vector<ll> fac:
  for (ll i = 2; i*i <= n; i++) {
   if (n%i == 0) {
     while (n%i == 0) n /= i;
```

```
math/modular_generator.h 845b
#include "modular.h" // modPow

// Get unique prime factors of n; O(sqrt n)
vector<11> factorize(l1 n) {
    vector<11> fac;
    for (l1 i = 2; i*i <= n; i++) {
        if (n%i == 0) {
            while (n%i == 0) n /= i;
            fac.pb(i);
        } // 6069
    } // a0cc
    if (n > 1) fac.pb(n);
    return fac;
} // 4a2a

// Find smallest primitive root mod n;
// time: O(sqrt(n) + g*log^2 n)
// Returns -1 if generator doesn't exist.
// For n <= 10^7 smallest generator is <= 115.
// You can use faster factorization algorithm
// to get rid of sqrt(n). [UNTESTED]
ll generator(l1 n) {</pre>
```

```
if (n \le 1 \mid | (n > 4 \&\& n \% 4 == 0)) return -1;
  vector<ll> fac = factorize(n);
 if (sz(fac) > (fac[0] == 2)+1) return -1;
 11 phi = n;
  each (p, fac) phi = phi / p * (p-1);
  fac = factorize(phi);
 for (ll q = 1; q++) if ( qcd(q, n) == 1) {
   each(f, fac) if (modPow(g, phi/f, n) == 1)
     goto nxt;
    return q;
   nxt::
 } // db24
} // 7641
                                         ac62
math/modular log.h
#include "modular.h" // modInv
// Baby-step giant-step algorithm; O(sqrt(p))
// Finds smallest x such that a^x = b \pmod{p}
// or returns -1 if there's no solution.
11 dlog(11 a, 11 b, 11 p) {
 int m = int(min(ll(sqrt(p))+2, p-1));
 unordered_map<11, int> small;
 11 t = 1;
 rep(i, 0, m) {
   int& k = small[t];
   if (!k) k = i+1;
   t = t*a % p;
 } // f1d0
 t = modInv(t, p);
 rep(i, 0, m) {
   int j = small[b];
   if (j) return i*ll(m) + j - 1;
   b = b*t % p;
 } // c7ed
 return -1;
} // 5c26
                                          db16
```

math/modular sqrt.h #include "modular.h" // modPow // Tonelli-Shanks algorithm for modular sgrt // modulo prime; O(lg^2 p), O(lg p) for most p // Returns -1 if root doesn't exists or else // returns square root x (the other one is -x). // UNTESTED ll modSgrt(ll a, ll p) { a %= p; **if** (a < 0) a += p; if (a <= 1) return a; if (modPow(a, p/2, p) != 1) return -1: if (p%4 == 3) return modPow(a, p/4+1, p); 11 s = p-1, n = 2;int r = 0, j; while (s%2 == 0) s /= 2, r++;while (modPow(n, p/2, p) != p-1) n++;ll x = modPow(a, (s+1)/2, p); ll b = modPow(a, s, p), g = modPow(n, s, p); for (;; r = j) { 11 t = b; for (j = 0; j < r && t != 1; j++) t = t*t % p; if (!j) return x;

ll gs = modPow(g, 1LL << (r-j-1), p);

```
q = qs*qs % p;
   x = x*gs % p;
   b = b*q % p;
 } // f83f
} // 7a97
math/montgomery.h
                                         a4ba
#include "modular.h" // modInv
// Montgomery modular multiplication
// MOD < MG MULT, gcd (MG MULT, MOD) must be 1
// Don't use if modulo is constexpr; UNTESTED
constexpr 11 MG SHIFT = 32:
constexpr ll MG MULT = 1LL << MG SHIFT;</pre>
constexpr 11 MG MASK = MG MULT - 1;
const 11 MG INV = MG MULT-modInv(MOD, MG MULT);
// Convert to Montgomery form
11 MG(11 x) { return (x*MG_MULT) % MOD; }
// Montgomery reduction
// redc(mg * mg) = Montgomery-form product
11 redc(11 x) {
ll q = (x * MG_INV) & MG_MASK;
 x = (x + q*MOD) >> MG_SHIFT;
 return (x >= MOD ? x-MOD : x):
} // d0f5
math/nimber.h
                                         474f
// Nimbers are defined as sizes of Nim heaps.
// Operations on nimbers are defined as:
// a+b = mex({a'+b : a' < a} u {a+b' : b' < b})
// ab = mex(\{a'b+ab'+a'b' : a' < a, b' < b\})
// Nimbers smaller than M = 2^2k form a field.
// Addition is equivalent to xor, meanwhile
// multiplication can be evaluated
// in O(lg^2 M) after precomputing.
using ull = uint64 t:
ull nbuf[64][64]; // Nim-products for 2^i * 2^j
// Multiply nimbers; time: O(1g^2 M)
// WARNING: Call initNimMul() before using.
ull nimMul(ull a, ull b) {
 ull ret = 0;
 for (ull s = a; s; s &= (s-1))
   for (ull t = b; t; t &= (t-1))
     ret ^= nbuf[ builtin ctzll(s)]
                 [__builtin_ctzll(t)];
 return ret;
} // 25be
// Initialize nim-products lookup table
void initNimMul() {
 rep(i, 0, 64)
   nbuf[i][0] = nbuf[0][i] = 1ull << i:
 rep (b, 1, 64) rep (a, 1, b+1) {
   int i = 1 << (63 - __builtin_clzll(a));</pre>
   int j = 1 << (63 - __builtin_clzll(b));</pre>
   ull t = nbuf[a-i][b-i];
   if (i < j)
     t = nimMul(t, 1ull << i) << j;
     t = nimMul(t, 1ull << (i-1)) ^ (t << i);
   nbuf[a][b] = nbuf[b][a] = t;
 } // ca24
} // 1811
// Compute a^e under nim arithmetic: O(1g^3 M)
// WARNING: Call initNimMul() before using.
ull nimPow(ull a, ull e) {
```

```
ull t = 1:
  while (e) {
   if (e % 2) t = nimMul(t, a);
   e \neq 2; a = nimMul(a, a);
 } // da53
 return t:
} // c06c
// Compute inverse of a in 2^64 nim-field;
// time: O(1q^3 M)
// WARNING: Call initNimMul() before using.
ull nimInv(ull a) {
 return nimPow(a, ull(-2));
1 // c6d9
// If you need to multiply many nimbers by
// the same value you can use this to speedup.
// WARNING: Call initNimMul() before using.
struct NimMult {
 ull M[64] = \{0\};
  // Initialize lookup; time: O(lg^2 M)
 NimMult(ull a) {
    for (ull t=a; t; t &= (t-1)) rep(i, 0, 64)
     M[i] ^= nbuf[__builtin_ctzll(t)][i];
  // Multiply by b; time: O(lq M)
 ull operator() (ull b) {
   ull ret = 0:
    for (ull t = b; t; t &= (t-1))
     ret ^= M[__builtin_ctzll(t)];
    return ret:
 } // e480
}; // 1b80
                                          8703
math/phi large.h
#include "pollard rho.h"
// Compute Euler's totient of large numbers
// time: O(n^{(1/4)}) \leftarrow factorization
ll phi(ll n) {
 each (p, factorize (n)) n = n / p.x * (p.x-1);
 return n:
} // 798e
math/phi precompute.h
                                          728b
Vi phi(1e7+1);
// Precompute Euler's totients; time: O(n lg n)
void calcPhi() {
 iota(all(phi), 0);
 rep(i, 2, sz(phi)) if (phi[i] == i)
    for (int j = i; j < sz(phi); j += i)</pre>
      phi[j] = phi[j] / i * (i-1);
1 // 3c65
math/phi prefix sum.h
                                         a9e0
#include "phi precompute.h"
vector<11> phiSum; // [k] = sum \ from \ 0 \ to \ k-1
// Precompute Euler's totient prefix sums
// for small values; time: O(n lg n)
void calcPhiSum() {
 calcPhi():
 phiSum.resize(sz(phi)+1);
 rep(i, 0, sz(phi))
   phiSum[i+1] = phiSum[i] + phi[i];
} // 3855
// Get prefix sum of phi(0) + ... + phi(n-1).
// WARNING: Call calcPhiSum first!
```

```
// For n > 4*10^9, answer will overflow.
// If you wish to get answer mod M use
// commented lines.
ll getPhiSum(ll n) { // time: O(n^{(2/3)})
  static unordered map<11, 11> big;
  if (n < sz(phiSum)) return phiSum[n];</pre>
  if (big.count(--n)) return big[n];
  11 ret = n*(n+1)/2;
  // 11 ret = (n\%2 ? n\%M * ((n+1)/2 % M)
                   : n/2%M * (n%M+1)) % M;
  for (11 s, i = 2; i \le n; i = s+1) {
   s = n / (n/i);
    ret -= (s-i+1) * getPhiSum(n/i+1);
    // ret -= (s-i+1) %M * getPhiSum(n/i+1) % M;
  // ret = (ret%M + M) % M;
  return big[n] = ret;
} // 820b
math/pi large.h
                                           fcbd
constexpr int MAX_P = 1e7;
vector<ll> pis, prl;
// Precompute prime counting function
// for small values; time: O(n lg lg n)
void initPi() {
  pis.assign(MAX_P+1, 1);
  pis[0] = pis[1] = 0;
  for (int i = 2; i*i <= MAX P; i++)
   if (pis[i])
      for (int j = i*i; j <= MAX_P; j += i)</pre>
       pis[j] = 0;
  rep(i, 1, sz(pis)) {
    if (pis[i]) prl.pb(i);
    pis[i] += pis[i-1];
  } // 0672
1 // 6d92
ll partial(ll x, ll a) {
  static vector <unordered map <11, 11>> big;
  big.resize(sz(prl));
  if (!a) return (x+1) / 2;
  if (big[a].count(x)) return big[a][x];
  ll ret = partial(x, a-1)
    - partial(x / prl[a], a-1);
  return big[a][x] = ret;
} // 774f
// Count number of primes <= x;
// \text{ time: } O(n^{(2/3)} * log(n)^{(1/3)})
// Set MAX_P to be > sqrt(x) and call initPi
// before using!
ll pi(ll x) {
  static unordered map<11, 11> big;
  if (x < sz(pis)) return pis[x];</pre>
  if (big.count(x)) return big[x];
  11 a = 0:
  while (prl[a]*prl[a]*prl[a] < x) a++;</pre>
  11 ret = 0, b = --a;
  while (++b < sz(prl) && prl[b]*prl[b] < x) {
   11 w = x / prl[b];
    ret -= pi(w);
    for (ll j = b; prl[j]*prl[j] <= w; j++)</pre>
     ret -= pi(w / prl[j]) - j;
  } // a584
```

```
ret += partial(x, a) + (b+a-1)*(b-a)/2;
 return big[x] = ret;
} // eald
                                         7fc0
math/pi large precomp.h
#include "sieve.h"
// Count primes in given interval
// using precomputed table.
// Set MAX_P to sqrt(MAX_N) and run sieve()!
// Precomputed table will contain N BUCKETS
// elements - check source size limit.
constexpr ll MAX N = 1e11+1;
constexpr 11 N BUCKETS = 10000;
constexpr 11 BUCKET SIZE = (MAX N/N BUCKETS)+1;
constexpr ll precomputed[] = {/* ... */};
ll sieveRange(ll from, ll to) {
 bitset < BUCKET SIZE > elems:
 from = max(from, 2LL);
 to = max(from, to);
 each (p. primesList) {
   ll c = max((from+p-1) / p, 2LL);
   for (11 i = c*p; i < to; i += p)
     elems.set(i-from);
 1 // a29f
 return to-from-elems.count():
1 // c646
// Run once on local computer to precompute
// table. Takes about 10 minutes for n = 1e11.
// Sanity check (for default params):
// 664579, 606028, 587253, 575795, ...
void localPrecompute() {
 for (ll i = 0; i < MAX N; i += BUCKET SIZE) {</pre>
   11 to = min(i+BUCKET_SIZE, MAX_N);
   cout << sieveRange(i, to) << ',' << flush;</pre>
 } // f6a7
 cout << endl:
} // 2b1e
// Count primes in [from; to) using table.
// O(N_BUCKETS + BUCKET_SIZE*lg lg n + sqrt(n))
11 countPrimes(11 from, 11 to) {
 ll bFrom = from/BUCKET SIZE+1,
    bTo = to/BUCKET SIZE;
 if (bFrom > bTo) return sieveRange(from, to);
 11 ret = accumulate(precomputed+bFrom,
                     precomputed+bTo, 0);
 ret += sieveRange(from, bFrom*BUCKET_SIZE);
 ret += sieveRange (bTo*BUCKET SIZE, to);
 return ret;
} // cced
math/pollard rho.h
                                          ef01
#include "modular64.h"
#include "miller rabin.h"
using Factor = pair<11, int>;
void rho(vector<11>& out, 11 n) {
 if (n <= 1) return;</pre>
 if (isPrime(n)) out.pb(n);
 else if (n\%2 == 0) rho(out,2), rho(out,n/2);
 else for (ll a = 2;; a++) {
   11 x = 2, y = 2, d = 1;
   while (d == 1) {
     x = modAdd(modMul(x, x, n), a, n);
     y = modAdd (modMul (y, y, n), a, n);
     y = modAdd (modMul (y, y, n), a, n);
     d = \_gcd(abs(x-y), n);
```

```
1 // 3378
    if (d != n) return rho(out,d),rho(out,n/d);
 } // 047e
1 // ba89
// Pollard's rho factorization algorithm
// Las Vegas version; time: n^(1/4)
// Returns pairs (prime, power), sorted
vector<Factor> factorize(ll n) {
 vector<Factor> ret;
 vector<11> raw:
  rho (raw, n);
  sort(all(raw));
  each(f, raw) {
   if (ret.empty() || ret.back().x != f)
      ret.pb({ f, 1 });
      ret.back().v++;
 } // 2ab1
 return ret;
} // 471c
math/polvnomial.h
                                          c486
#include "modular.h"
#include "fft mod.h"
// UNTESTED
using Poly = vector<Zp>;
// Cut off trailing zeroes; time: O(n)
void norm(Poly& P) {
 while (!P.empty() && !P.back().x)
   P.pop_back();
} // 8a8a
// Evaluate polynomial at x; time: O(n)
Zp eval (const Poly& P, Zp x) {
 Zp n = 0, y = 1;
  each (a, P) n += a*y, y *= x;
 return n:
} // d865
// Add polynomial; time: O(n)
Poly& operator+=(Poly& 1, const Poly& r) {
 1.resize(max(sz(1), sz(r)));
 rep(i, 0, sz(r)) l[i] += r[i];
 norm(1);
 return 1;
1 // 656e
Poly operator+(Poly 1, const Poly& r) {
 return 1 += r;
} // d9b3
// Subtract polynomial; time: O(n)
Polv& operator = (Polv& 1, const Polv& r) {
 1.resize(max(sz(1), sz(r)));
  rep(i, 0, sz(r)) l[i] -= r[i];
  norm(1);
 return 1;
} // c68b
Poly operator-(Poly 1, const Poly& r) {
 return 1 -= r;
} // dc4f
// Multiply by polynomial; time: O(n lg n)
Polv& operator*=(Poly& 1, const Poly& r) {
 if (\min(sz(1), sz(r)) < 50) {
    // Naive multiplication
    Poly P(sz(1)+sz(r));
    rep(i, 0, sz(l)) rep(j, 0, sz(r))
     P[i+j] += l[i]*r[j];
    l.swap(P);
```

```
} else {
    // FFT multiplication
    vector<ll> a, b;
    each(k, l) a.pb(k.x);
    each(k, r) b.pb(k.x);
    // Choose appropriate convolution method,
    // see fft_mod.h and fft_complex.h
    convolve<MOD, 62>(a, b);
    1.assign(all(a));
 } // f730
 norm(1);
 return 1;
} // 28de
Poly operator* (Poly 1, const Poly € r) {
 return 1 *= r:
} // 2de3
// Derivate polynomial; time: O(n)
Poly derivate (Poly P) {
 if (!P.empty()) {
    rep(i, 1, sz(P)) P[i-1] = P[i] * i;
    P.pop_back();
 } // bd78
 return P:
} // c6c5
// Integrate polynomial; time: O(n)
Poly integrate (Poly P) {
 if (!P.empty()) {
    P.pb(0);
    for (int i = sz(P); --i;) P[i] = P[i-1]/i;
    P[01 = 0;
 } // eec1
 return P;
} // e2f3
// Compute inverse series mod x^n; O(n lq n)
Poly invert (const Poly& P, int n) {
  assert(!P.empty() && P[0].x != 0);
  Poly tmp, ret = \{P[0].inv()\};
  for (int i = 1; i < n; i *= 2) {
    tmp.clear():
    rep(j, 0, min(i*2, sz(P))) tmp.pb(-P[j]);
    tmp *= ret:
    tmp[0] += 2;
    ret *= tmp;
    ret.resize(i*2);
 1 // 139b
  ret.resize(n);
 return ret;
} // 4d3e
// Floor division by polynomial; O(n lq n)
Poly operator/(Poly 1, Poly r) {
 norm(1); norm(r);
  int d = sz(1)-sz(r)+1;
  if (d <= 0) return {};</pre>
  reverse (all(1));
  reverse (all(r));
  l.resize(d);
 1 \star = invert(r, d);
 l.resize(d);
 reverse (all(1));
 return 1:
} // d4a4
Poly& operator/=(Poly& 1, const Poly& r) {
 return 1 = 1/r;
} // e12e
// Compute modulo by polynomial; O(n lg n)
```

```
Poly operator% (const Poly& 1, const Poly& r) {
                                                     1 // 681d
  return 1 - r \star (1/r);
} // 4fc8
                                                   } // dd92
Poly& operator%=(Poly& 1, const Poly& r) {
  return 1 -= r*(1/r);
} // 80bb
// Evaluate polynomial P in given points;
// time: O(n 1g^2 n)
Poly eval(const Poly € P, Poly points) {
  int len = 1;
  while (len < sz(points)) len *= 2;
  vector<Poly> tree(len*2, {1});
  rep(i, 0, sz(points))
   tree[len+i] = \{-points[i], 1\};
  for (int i = len; --i;)
   tree[i] = tree[i\star2] \star tree[i\star2+1];
  tree[0] = P;
  rep(i, 1, len*2)
   tree[i] = tree[i/2] % tree[i];
  rep(i, 0, sz(points)) {
    auto& vec = tree[len+i];
                                                   1 // 7c2c
    points[i] = vec.empty() ? 0 : vec[0];
  } // c1c2
  return points;
} // 69b0
// Given n points (x, f(x)) compute n-1-degree
// polynomial f that passes through them;
// time: O(n la^2 n)
// For O(n^2) version see polynomial interp.h.
Poly interpolate (const vector < pair < Zp, Zp>>& P) {
  int len = 1;
  while (len < sz(P)) len \star= 2;
  vector < Poly> mult(len*2, {1}), tree(len*2);
  rep(i, 0, sz(P))
   mult[len+i] = {-P[i].x, 1};
  for (int i = len; --i;)
   mult[i] = mult[i*2] * mult[i*2+1];
                                                   } // d5ca
  tree[0] = derivate(mult[1]);
  rep(i, 1, len*2)
   tree[i] = tree[i/2] % mult[i];
  rep(i, 0, sz(P))
   tree[len+i][0] = P[i].y / tree[len+i][0];
  for (int i = len: --i:)
    tree[i] = tree[i\star2]\starmult[i\star2+1]
            + mult[i*2]*tree[i*2+1];
  return tree[1];
} // b706
math/polynomial interp.h
                                           a4cc
// Interpolate set of points (i, vec[i])
// and return it evaluated at x; time: O(n)
                                                   1 // 82b6
template < class T>
T polyExtend(vector<T>& vec, T x) {
  int n = sz(vec);
  vector<T> fac(n, 1), suf(n, 1);
  rep(i, 1, n) fac[i] = fac[i-1] \star i;
  for (int i=n; --i;) suf[i-1] = suf[i]*(x-i);
  T pref = 1, ret = 0;
  rep(i, 0, n) {
    T d = fac[i] * fac[n-i-1] * ((n-i) *2*2-1);
    ret += vec[i] * suf[i] * pref / d;
    pref *= x-i;
                                                       n /= f;
```

```
return ret;
                                                   return ret;
                                                  } // bb65
// Given n points (x, f(x)) compute n-1-degree
// polynomial f that passes through them;
// time: O(n^2)
// For O(n lg^2 n) version see polynomial.h
template<class T>
vector<T> polyInterp(vector<pair<T, T>> P) {
 int n = sz(P);
  vector<T> ret(n), tmp(n);
                                                  void sieve() {
 T last = 0;
  tmp[0] = 1;
                                                    vector<Pii> dels;
  rep(k, 0, n-1) rep(i, k+1, n)
                                                    primes.set();
   P[i].y = (P[i].y-P[k].y) / (P[i].x-P[k].x);
                                                    primes.reset(0);
  rep(k, 0, n) rep(i, 0, n) {
    ret[i] += P[k].y * tmp[i];
                                                      if (primes[i/2]) {
    swap(last, tmp[i]);
                                                        int ;
    tmp[i] = last * P[k].x;
  } // af1c
  return ret;
                                                     } // 9e62
math/sieve.h
                                          3f3d
                                                  } // ff49
constexpr int MAX P = 1e6:
bitset<MAX P+1> primes;
Vi primesList;
// Erathostenes sieve; time: O(n lg lg n)
void sieve() {
                                                   1 // 97ae
 primes.set();
                                                  } // 6456
 primes.reset(0);
 primes.reset (1);
                                                  bool isPrime(int x) {
  for (int i = 2; i*i <= MAX P; i++)</pre>
                                                  } // 422c
    if (primes[i])
      for (int j = i*i; j <= MAX_P; j += i)</pre>
        primes.reset(j);
  rep(i, 0, MAX_P+1) if (primes[i])
   primesList.pb(i);
math/sieve factors.h
                                          312d
constexpr int MAX P = 1e6;
                                                  // UNTESTED
Vi factor (MAX_P+1);
// Erathostenes sieve with saving smallest
// factor for each number; time: O(n lg lg n)
void sieve() {
 for (int i = 2; i*i <= MAX P; i++)
    if (!factor[i])
                                                    return 1; } // f164
      for (int j = i*i; j <= MAX_P; j += i)</pre>
                                                  OP (&) OP (|) OP (^)
        if (!factor[i])
          factor[i] = i;
 rep(i, 0, MAX P+1) if (!factor[i]) factor[i]=i;
                                                  struct Fenwick {
// Factorize n <= MAX_P; time: O(lg n)</pre>
                                                   using T = int:
// Returns pairs (prime, power), sorted
                                                    T ID = 0;
vector<Pii> factorize(ll n) {
  vector<Pii> ret:
  while (n > 1) {
                                                    vector<T> s:
    int f = factor[n];
    if (ret.empty() | ret.back().x != f)
      ret.pb({ f, 1 });
      ret.back().y++;
```

```
1 // 664c
                                         849b
math/sieve segmented.h
constexpr int MAX P = 1e9;
bitset<MAX P/2+1> primes; // Only odd numbers
// Cache-friendly Erathostenes sieve
// ~1.5s on Intel Core i5 for MAX_P = 10^9
// Memory usage: MAX P/16 bytes
 constexpr int SEG_SIZE = 1<<18;</pre>
 int pSqrt = int(sqrt(MAX P)+0.5);
  for (int i = 3; i <= pSqrt; i += 2) {
     for (i = i*i; i <= pSgrt; i += i*2)
       primes.reset(i/2);
     dels.pb(\{i, i/2\});
  for (int seg = pSgrt/2;
      seg <= sz(primes); seg += SEG SIZE) {
   int lim = min(seg+SEG_SIZE, sz(primes));
   each(d, dels) for (;d.y < \lim; d.y += d.x)
     primes.reset(d.y);
 return x == 2 || (x%2 && primes[x/2]);
structures/bitset plus.h
                                         6737
// Undocumented std::bitset features:
// - _Find_first() - returns first bit = 1 or N
// - Find next(i) - returns first bit = 1
                    after i-th bit
                    or N if not found
// Bitwise operations for vector<bool>
#define OP(x) vector<bool>& operator x##=(
   vector<bool>& 1, const vector<bool>& r) {
  assert(sz(1) == sz(r));
 auto a = 1.begin(); auto b = r.begin();
 while (a<1.end()) *a._M_p++ x##= *b._M_p++; \
structures/fenwick tree.h
                                         b467
// Fenwick tree (BIT tree); space: O(n)
// Default version: prefix sums
 T f(T a, T b) { return a+b; }
 Fenwick(int n = 0) : s(n, ID) {}
 //A[i] = f(A[i], v); time: O(lq n)
 void modify(int i, T v) {
   for (; i < sz(s); i |= i+1) s[i]=f(s[i],v);</pre>
 ) // a047
```

```
// Get f(A[0], ..., A[i-1]); time: O(lq n)
 T query(int i) {
   T v = ID;
   for (; i > 0; i \in [i-1]) v = f(v, s[i-1]);
   return v;
 1 // 9810
 // Find smallest i such that
 // f(A[0],...,A[i-1]) >= val; time: O(lq n)
 // Prefixes must have non-descreasing values.
 int lowerBound(T val) {
   if (val <= ID) return 0;</pre>
   int i = -1, mask = 1;
   while (mask \leq sz(s)) mask *= 2:
   T off = ID;
   while (mask /= 2) {
     int k = mask+i;
     if (k < sz(s)) {
       T \times = f(off, s[k]);
       if (val > x) i=k, off=x;
     } // de7f
   1 // 929c
   return i+2;
 } // 4be9
}: // 1470
structures/fenwick tree 2d.h 4945
// Fenwick tree 2D (BIT tree 2D); space: O(n*m)
// Default version: prefix sums 2D
// Change s to hashmap for O(q 1g^2 n) memory
struct Fenwick2D {
 using T = int:
 T ID = 0;
 T f(T a, T b) { return a+b; }
 vector<T> s:
 int w, h;
 Fenwick2D(int n = 0, int m = 0)
   : s(n*m, ID), w(n), h(m) {}
 // A[i,j] = f(A[i,j], v); time: O(lg^2 n)
 void modify(int i, int j, T v) {
   for (; i < w; i |= i+1)
      for (int k = j; k < h; k = k+1)
       s[i*h+k] = f(s[i*h+k], v);
 } // d46b
 // Ouerv prefix; time: O(lg^2 n)
 T query(int i, int j) {
   T v = ID;
   for (; i>0; i&=i-1)
     for (int k = j; k > 0; k &= k-1)
       v = f(v, s[i*h+k-h-1]);
   return v;
 } // 08cf
}; // 36b4
structures/find union.h
                                         b4de
// Disjoint set data structure; space: O(n)
// Operations work in amortized O(alfa(n))
struct FAU {
 Vi G:
 FAU(int n = 0) : G(n, -1) {}
 // Get size of set containing i
 int size(int i) { return -G[find(i)]; }
  // Find representative of set containing i
 int find(int i) {
   return G[i] < 0 ? i : G[i] = find(G[i]);</pre>
```

```
} // 5bc1
                                                       return u/d + ((u^d) >= 0 || !(u%d));
                                                                                                       Node(T x = T()) : val(x) \{\}
                                                     } // f27f
                                                                                                     }; // 11ee
                                                                                                                                                      } // 5b13
 // Union sets containing i and j
                                                                                                                                                    }; // 09f3
                                                                                                     using Vnode = vector<Node>;
 bool join(int i, int j) {
                                                     bool operator<(const Line& r) const {</pre>
   i = find(i); j = find(j);
                                                                                                     Vnode& M:
                                                                                                                                                    structures/rmq.h
                                                       return modeO ? end < r.end : a < r.a;</pre>
                                                                                                     int root{-1};
   if (i == j) return 0;
                                                     } // cfab
                                                                                                                                                     // Range Minimum Query; space: O(n lg n)
   if (G[i] > G[j]) swap(i, j);
                                                   }; // 6046
                                                                                                     int unlink(int& i) {
                                                                                                                                                     struct RMO {
   G[i] += G[j]; G[j] = i;
                                                                                                       if (i >= 0) M[i].prev = -1;
                                                                                                                                                      using T = int;
   return 1;
                                                   multiset<Line> S;
                                                                                                       int x = i; i = -1;
                                                                                                                                                      T ID = INT MAX;
                                                   Hull() { S.insert({ 0, -INF, INF }); }
 } // c721
                                                                                                       return x;
                                                                                                                                                      T f(T a, T b) { return min(a, b); }
}; // 62a4
                                                   // Updates segment end
                                                                                                     1 // d9f6
                                                                                                                                                      vector<vector<T>>> s;
structures/hull offline.h
                                         3030
                                                   bool update(multiset<Line>::iterator it) {
                                                                                                     void link(int host, int& i, int val) {
                                                     auto cur = it++; cur->end = INF;
                                                                                                       if (i \geq = 0) M[i].prev = -1;
constexpr 11 INF = 2e18;
                                                     if (it == S.end()) return false;
                                                                                                                                                      RMO(const vector<T>& vec = {}) {
// constexpr double INF = 1e30;
                                                                                                       i = val;
                                                     cur->end = cur->intersect(*it);
                                                                                                                                                        s = \{vec\};
// constexpr double EPS = 1e-9;
                                                                                                       if (i >= 0) M[i].prev = host;
                                                     return cur->end >= it->end;
                                                                                                                                                        for (int h = 1; h \le sz(vec); h *= 2) {
                                                                                                     } // 47d5
// MAX of linear functions; space: O(n)
                                                   1 // 63b8
                                                                                                                                                          s.emplace back();
                                                                                                     int merge(int 1, int r) {
// Use if you add lines in increasing `a` order
                                                                                                                                                           auto& prev = s[sz(s)-21;
                                                   // Insert f(x) = ax+b; time: O(\lg n)
// Default uncommented version is for int64
                                                                                                       if (1 < 0) return r;
                                                                                                                                                          rep(i, 0, sz(vec)-h*2+1)
                                                   void insert(ll a, ll b) {
                                                                                                       if (r < 0) return 1;
struct Hull {
                                                                                                                                                            s.back().pb(f(prev[i], prev[i+h]));
                                                     auto it = S.insert({ a, b, INF });
 using T = 11; // Or change to double
                                                                                                       if (Cmp()(M[1].val, M[r].val)) swap(l, r);
                                                                                                                                                        } // b5ff
                                                     while (update(it)) it = --S.erase(++it);
                                                                                                                                                      } // cf67
  struct Line {
                                                     rep(i, 0, 2)
                                                                                                       link(1, M[1].next, unlink(M[r].child));
                                                       while (it != S.begin() && update(--it))
                                                                                                       link(r, M[r].child, 1);
   T a, b, end;
                                                                                                                                                      // Query f(s[b], ..., s[e-1]); time: O(1)
   T intersect (const Line& r) const {
                                                         update(it = --S.erase(++it));
                                                                                                       return r;
                                                                                                                                                      T query(int b, int e) {
                                                                                                     } // fc42
     // Version for double:
                                                                                                                                                        if (b >= e) return ID;
     //if (r.a-a < EPS) return b>r.b?INF:-INF;
                                                                                                                                                        int k = 31 - __builtin_clz(e-b);
                                                   // Query max(f(x) for each f): time: O(lg n)
                                                                                                     int mergePairs(int v) {
     //return (b-r.b) / (r.a-a);
                                                                                                                                                        return f(s[k][b], s[k][e - (1<<k)]);</pre>
                                                   11 query(11 x) {
                                                                                                       if (v < 0 || M[v].next < 0) return v;</pre>
     if (a==r.a) return b > r.b ? INF : -INF;
                                                                                                                                                      } // caaa
                                                     mode0 = 1;
                                                                                                       int v2 = unlink(M[v].next);
     11 u = b-r.b, d = r.a-a;
                                                                                                                                                    }; // e694
                                                     auto 1 = \starS.upper_bound({ 0, 0, x });
                                                                                                       int v3 = unlink(M[v2].next);
     return u/d + ((u^d) >= 0 || !(u%d));
                                                     mode0 = 0:
                                                                                                       return merge(merge(v, v2), mergePairs(v3));
   } // f27f
                                                     return 1.a*x + 1.b;
                                                                                                     } // 2eea
 }; // 10dc
                                                   } // 7533
                                                                                                                                                     // Segment tree configurations to be used
                                                 }; // 037e
 vector<Line> S;
                                                                                                     // Initialize heap with given node storage
 Hull() \{ S.pb(\{ 0, -INF, INF \}); \}
                                                                                                                                                     // See comments in TREE_PLUS version
                                                 bool Hull::mode() = false;
                                                                                                     // Just declare 1 Vnode and pass it to heaps
                                                                                                                                                     // to understand how to create custom ones.
  // Insert f(x) = ax+b; time: amortized O(1)
                                                 structures/max queue.h
                                                                                           3e9e
                                                                                                     PHeap(Vnode& mem) : M(mem) {}
                                                                                                                                                     // Capabilities notation: (update; query)
  void push(T a, T b) {
   Line 1{a, b, INF};
                                                                                                     // Add given key to heap, returns index; O(1)
                                                                                                                                                     #if TREE_PLUS // (+; sum, max, max count)
                                                 // Queue with max query on contained elements
                                                                                                     int push (const T& x) {
   while (true) {
                                                 struct MaxQueue {
                                                                                                                                                      // time: O(lg n) [UNTESTED]
     T e = S.back().end=S.back().intersect(1);
                                                   using T = int;
                                                                                                       int index = sz(M);
                                                                                                                                                      using T = int; // Data type for update
                                                                                                       M.emplace back(x);
     if (sz(S) < 2 | | S[sz(S)-2].end < e)
                                                   deque<T> Q, M;
                                                                                                                                                                      // operations (lazy tag)
                                                                                                       root = merge(root, index);
       break:
                                                                                                                                                      T ID = 0;
                                                                                                                                                                      // Neutral value for
                                                   // Add v to the back; time: amortized O(1)
                                                                                                       return index;
     S.pop_back();
                                                                                                                                                                      // updates and lazy tags
                                                   void push(T v) {
                                                                                                     1 // e744
   } // 044f
                                                     while (!M.empty() && M.back() < v)</pre>
                                                                                                                                                      // This structure keeps aggregated data
   S.pb(1);
                                                       M.pop_back();
                                                                                                     // Change key of i to smaller value; O(1)
                                                                                                                                                      struct Agg {
  } // 978e
                                                                                                     void decrease(int i, T val) {
                                                     M.pb(v); Q.pb(v);
                                                                                                                                                        // Aggregated data: sum, max, max count
                                                                                                       assert(!Cmp()(M[i].val, val));
  // Ouerv max(f(x) for each f): time: O(lq n)
                                                   } // 57a2
                                                                                                                                                        // Default values should be neutral
                                                                                                       M[i].val = val;
 T query(T x) {
                                                   // Pop from the front; time: O(1)
   auto t = *upper_bound(all(S), x,
                                                                                                                                                        T sum{0}, vMax{INT MIN}, nMax{0};
                                                                                                       int prev = M[i].prev;
                                                   void pop() {
     [](int 1, const Line& r) {
                                                                                                       if (prev < 0) return;</pre>
                                                     if (M.front() == Q.front()) M.pop_front();
                                                                                                                                                         // Initialize as leaf (single value)
       return 1 < r.end;</pre>
                                                     Q.pop_front();
     }); // de77
                                                                                                       auto& p = M[prev];
                                                   } // 101c
                                                                                                       link (prev, (p.child == i ? p.child
   return t.a*x + t.b;
                                                                                                                                                        // Combine data with aggregated data
                                                   // Get max element value; time: O(1)
                                                                                                            : p.next), unlink(M[i].next));
 } // b8de
                                                                                                                                                        // from node to the right
}; // 1d64
                                                   T max() const { return M.front(); }
                                                                                                                                                        void merge(const Agg& r) {
                                                                                                       root = merge(root, i);
                                                 }; // b6c4
                                                                                                                                                          if (vMax < r.vMax) nMax = r.nMax;</pre>
                                                                                                     } // 1a67
structures/hull online.h
                                         2a7b
                                                 structures/pairing heap.h
                                                                                           b2a7
                                                                                                     bool empty() { return root < 0; }</pre>
constexpr 11 INF = 2e18;
                                                                                                                                                           vMax = max(vMax, r.vMax);
                                                                                                     const T& top() { return M[root].val; }
                                                 // Pairing heap implementation; space O(n)
                                                                                                                                                          sum += r.sum;
// MAX of linear functions online; space: O(n)
                                                 // Elements are stored in vector for faster
                                                                                                                                                        } // 8850
                                                                                                     // Merge with other heap. Must use same vec.
struct Hull {
                                                 // allocation. It's MINIMUM queue.
                                                                                                     void merge(PHeap& r) { // time: O(1)
  static bool modeQ; // Toggles operator< mode</pre>
                                                                                                                                                        // Apply update provided in `x`:
                                                 // Allows to merge heaps in O(1)
                                                                                                       assert(&M == &r.M);
                                                                                                                                                        // - update aggregated data
  struct Line (
                                                 template < class T, class Cmp = less < T>>
                                                                                                       root = merge(root, r.root); r.root = -1;
                                                                                                                                                        // - update lazv tag `lazv`
   mutable 11 a, b, end;
                                                 struct PHeap {
                                                                                                     } // 9623
                                                                                                                                                        // - `size` is amount of elements
                                                   struct Node {
   ll intersect (const Line& r) const {
                                                                                                                                                        // - return 0 if update should branch
                                                                                                     // Remove min element; time: O(lg n)
                                                     T val;
     if (a==r.a) return b > r.b ? INF : -INF;
                                                                                                     void pop() {
                                                     int child{-1}, next{-1}, prev{-1};
     11 u = b-r.b, d = r.a-a;
```

```
11
   root = mergePairs (unlink (M[root].child));
                                        4551
  // Initialize RMO structure; time: O(n lg n)
structures/segtree config.h 7ef8
// in segtree general and segtree persistent.
   // values, i.e. "aggregate over empty set"
   void leaf() { sum = vMax = 0; nMax = 1; }
     else if (vMax == r.vMax) nMax += r.nMax;
   // (to be used in "segement tree beats")
   // - if you change value of `x` changed
```

```
12
```

```
// value will be passed to next node
    // to the right during updates
   bool apply (T& lazy, T& x, int size) {
     lazy += x;
     sum += x*size;
     vMax += x;
     return 1;
   } // 4858
 }; // 9bf5
#elif TREE MAX // (max; max, max count)
 // time: O(lg n) [UNTESTED]
  using T = int;
 T ID = INT MIN;
  struct Agg {
    // Aggregated data: max value, max count
   T vMax{INT MIN}, nMax{0};
   void leaf() { vMax = 0; nMax = 1; }
    void merge(const Agg& r) {
     if (vMax < r.vMax) nMax = r.nMax;</pre>
     else if (vMax == r.vMax) nMax += r.nMax;
     vMax = max(vMax, r.vMax);
   } // f56b
   bool apply (T& lazy, T& x, int size) {
     if (vMax <= x) nMax = size;</pre>
     lazy = max(lazy, x);
     vMax = max(vMax, x);
     return 1;
   } // 8bd5
  }; // 15b6
#elif TREE_SET // (=; sum, max, max count)
 // time: O(lq n) [UNTESTED]
  // Set ID to some unused value.
  using T = int:
 T ID = INT MIN;
  struct Agg {
    // Aggregated data: sum, max, max count
   T sum{0}, vMax{INT_MIN}, nMax{0};
   void leaf() { sum = vMax = 0; nMax = 1; }
    void merge(const Agg& r) {
     if (vMax < r.vMax) nMax = r.nMax;</pre>
     else if (vMax == r.vMax) nMax += r.nMax;
     vMax = max(vMax, r.vMax);
     sum += r.sum;
   } // 8850
   bool apply (T& lazy, T& x, int size) {
     lazy = x;
     sum = x*size:
     vMax = x;
     nMax = size:
     return 1;
   } // 845b
 }; // 7488
#elif TREE BEATS // (+, min; sum, max)
 // time: amortized O(lg n) if not using +
          amortized O(lg^2 n) if using +
  // Lazy tag is pair (add, min).
  // To add x: run update with {x, INT_MAX},
  // to min x: run update with {0, x}.
  // When both parts are provided addition
  // is applied first, then minimum.
  using T = Pii;
 T ID = \{0, INT_MAX\};
  struct Agg {
    // Aggregated data: max value, max count,
                        second max value, sum
```

```
int vMax{INT_MIN}, nMax{0}, max2{INT_MIN};
   int sum{0};
   void leaf() { sum = vMax = 0; nMax = 1; }
   void merge(const Agg& r) {
     if (r.vMax > vMax) {
       max2 = vMax;
       vMax = r.vMax;
       nMax = r.nMax;
     } else if (r.vMax == vMax) {
       nMax += r.nMax;
     } else if (r.vMax > max2) {
       max2 = r.vMax:
     1 // b074
     max2 = max(max2, r.max2);
     sum += r.sum;
   } // 3124
   bool apply (T& lazy, T& x, int size) {
     if (\max 2 != INT MIN \&\& \max 2 + x.x >= x.y)
       return 0:
     lazy.x += x.x;
     sum += x.x*size;
     vMax += x.x;
     if (max2 != INT_MIN) max2 += x.x;
     if (x.y < vMax) {
       sum -= (vMax-x.y) * nMax;
       vMax = x.y;
     } // 7025
     lazy.y = vMax;
     return 1:
   } // fe0c
 }; // 2924
#endif
structures/segtree general.h 725a
// Highly configurable statically allocated
// (interval; interval) segment tree;
// space: O(n) [UNTESTED]
struct SegTree {
 // Choose/write configuration
 #include "segtree_config.h"
 // Root node is 1, left is i*2, right i*2+1
 vector<Agg> agg; // Aggregated data for nodes
 vector<T> lazy; // Lazy tags for nodes
 int len{1};
                  // Number of leaves
  // Initialize tree for n elements; time: O(n)
 SegTree(int n = 0) {
   while (len < n) len *= 2;
   agg.resize(len*2);
   lazy.resize(len*2, ID);
   rep(i, 0, n) agg[len+i].leaf();
   for (int i = len; --i;)
     (agg[i] = agg[i*2]).merge(agg[i*2+1]);
 } // 4417
 void push(int i, int s) {
   if (lazy[i] != ID) {
     agg[i*2].apply(lazy[i*2], lazy[i], s/2);
     agg[i*2+1].apply(lazy[i*2+1],
                      lazy[i], s/2);
     lazv[i] = ID:
   } // 3ba9
 } // 5d19
 // Modify interval [vb;ve) with val; O(lq n)
 T update(int vb, int ve, T val, int i = 1,
          int b = 0, int e = -1) {
```

```
int m = (b+e) / 2;
   push(i, e-b);
   val = update(vb, ve, val, i*2, b, m);
   val = update(vb, ve, val, i*2+1, m, e);
   (agg[i] = agg[i*2]).merge(agg[i*2+1]);
   return val;
 } // aa8e
 // Query interval [vb;ve); time: O(lg n)
 Agg query(int vb, int ve, int i = 1,
           int b = 0, int e = -1) {
   if (e < 0) e = len;
   if (vb >= e || b >= ve) return {};
   if (b >= vb && e <= ve) return agg[i];</pre>
   int m = (b+e) / 2;
   push(i, e-b);
   Agg t = query (vb, ve, i*2, b, m);
   t.merge(query(vb, ve, i*2+1, m, e));
 } // lale
}; // db5c
structures/segtree persist.h dcfc
// Highly configurable (interval; interval)
// persistent segment tree;
// space: O(queries lg n) [UNTESTED]
// First tree version number is 0.
struct SegTree {
 // Choose/write configuration
  #include "segtree_config.h"
 vector<Agg> agg; // Aggregated data for nodes
 vector<T> lazy; // Lazy tags for nodes
 vector<bool> cow; // Copy children on push?
                  // Children links
 Vi L. R:
 int len{1};
                   // Number of leaves
  // Initialize tree for n elements; O(lq n)
 SegTree(int n = 0) {
   int k = 1:
   while (len < n) len \star= 2, k++;
   agg.resize(k);
   lazy.resize(k, ID);
   cow.resize(k, 1);
   L.resize(k);
   R.resize(k);
   agg[--k].leaf();
   while (k--) {
      (agg[k] = agg[k+1]).merge(agg[k+1]);
     L[k] = R[k] = k+1;
   } // 211f
 } // 83cf
 // New version from version `i`; time: O(1)
  // First version number is 0.
 int fork(int i) {
   L.pb(L[i]); R.pb(R[i]); cow.pb(cow[i] = 1);
   agg.pb(agg[i]); lazy.pb(lazy[i]);
   return sz(L)-1;
 } // a21b
 void push(int i, int s, bool w) {
   bool has = (lazy[i] != ID);
```

if (e < 0) e = len;</pre>

return val:

if (b >= vb && e <= ve &&

if (vb >= e || b >= ve) return val;

agg[i].apply(lazy[i], val, e-b))

```
if ((has || w) && cow[i]) {
     int a = fork(L[i]), b = fork(R[i]);
     L[i] = a; R[i] = b; cow[i] = 0;
   } // 1a3e
   if (has) {
     agg[L[i]].apply(lazy[L[i]],lazy[i],s/2);
     agg[R[i]].apply(lazy[R[i]],lazy[i],s/2);
     lazv[i] = ID;
   } // eca6
 } // 9f84
 // Modify interval [vb;ve) with val
 // in tree version `i`; time: O(lq n)
 T update(int i, int vb, int ve, T val,
          int b = 0, int e = -1) {
   if (e < 0) e = len;</pre>
   if (vb >= e || b >= ve) return val;
   if (b >= vb && e <= ve &&
       agg[i].apply(lazy[i], val, e-b))
     return val:
   int m = (b+e) / 2;
   push(i, e-b, 1);
   val = update(L[i], vb, ve, val, b, m);
   val = update(R[i], vb, ve, val, m, e);
    (agg[i] = agg[L[i]]).merge(agg[R[i]]);
   return val;
 } // 776e
 // Ouerv interval [vb;ve)
 // in tree version `i`; time: O(lq n)
 Agg query (int i, int vb, int ve,
           int b = 0, int e = -1) {
   if (e < 0) e = len;</pre>
   if (vb >= e || b >= ve) return {};
   if (b >= vb && e <= ve) return agg[i];</pre>
   int m = (b+e) / 2;
   push(i, e-b, 0);
   Agg t = query(L[i], vb, ve, b, m);
   t.merge(query(R[i], vb, ve, m, e));
   return t:
 } // abf4
1: // 8a44
                                          2b0f
structures/segtree point.h
// Segment tree (point, interval)
// Configure by modifying:
// - T - stored data type
// - ID - neutral element for query operation
// - f(a, b) - combine results
struct SegTree {
 using T = int:
 T ID = INT MIN;
```

```
// Segment tree (point, interval)
// Segment tree (point, interval)
// Configure by modifying:
// - T - stored data type
// - ID - neutral element for query operation
// - f(a, b) - combine results
struct SegTree {
    using T = int;
    T ID = INT_MIN;
    T f(T a, T b) { return max(a,b); }
    vector<T> V;
    int len;
// Initialize tree for n elements; time: O(n)
    SegTree(int n = 0, T def = 0) {
        for (len = 1; len < n; len *= 2);
        V.resize(len*2, ID);
        rep(i, 0, n) V[len+i] = def;
        for (int i = len; --i;)
        V[i] = f(V[i*2], V[i*2+1]);
    } // 459e
// Set element 'i' to 'val'; time: O(lg n)
void set(int i, T val) {
    V[i += len] = val;
}</pre>
```

```
T query(int b, int e) {
   b += len; e += len-1;
    if (b > e) return ID;
   if (b == e) return V[b];
   T \times = f(V[b], V[e]);
    while (b/2 < e/2) {
     if (^{\sim}b_{\&1}) x = f(x, V[b^{\sim}1]);
     if (e&1) x = f(x, V[e^1]);
     b /= 2; e /= 2;
   } // 444a
    return x;
 } // de36
}; // d571
structures/treap.h
                                          bbb4
// "Set" of implicit keyed treaps; space: O(n)
// Nodes are keyed by their indices in array
// of all nodes. Treap key is key of its root.
// "Node x" means "node with key x".
// "Treap x" means "treap with key x".
// Key -1 is "null".
// Put any additional data in Node struct.
struct Treap {
  struct Node {
    // E[0] = left child, <math>E[1] = right child
    // weight = node random weight (for treap)
    // size = subtree size, par = parent node
    int E[2] = \{-1, -1\}, weight{rand()};
    int size{1}, par{-1};
   bool flip{0}; // Is interval reversed?
  }; // c082
  vector<Node> G; // Array of all nodes
  // Initialize structure for n nodes
  // with keys 0, ..., n-1; time: O(n)
  // Each node is separate treap,
  // use join() to make sequence.
  Treap(int n = 0) : G(n) {}
  // Create new treap (a single node),
  // returns its key; time: O(1)
  int make() {
   G.emplace back(); return sz(G)-1;
  } // 907a
  // Get size of node x subtree. x can be -1.
  int size(int x) { // time: O(1)
    return (x \ge 0 ? G[x].size : 0);
  // Propagate down data (flip flag etc).
  // x can be -1; time: O(1)
  void push(int x) {
   if (x >= 0 && G[x].flip) {
     G[x].flip = 0;
      swap (G[x].E[0], G[x].E[1]);
      each(e, G[x].E) if (e>=0) G[e].flip ^= 1;
    } // + any other lazy operations
  } // ed19
  // Update aggregates of node x.
  // x can be -1; time: O(1)
  void update(int x) {
    if (x >= 0) {
     int& s = G[x].size = 1;
```

while (i \neq 2)

} // 4bcd

V[i] = f(V[i*2], V[i*2+1]);

// Query interval [b;e); time: O(lg n)

```
G[x].par = -1;
    each(e, G[x].E) if (e >= 0) {
     s += G[e].size;
      G[e].par = x;
    } // f7a7
  } // + any other aggregates
} // 46a3
// Split treap x into treaps 1 and r
// such that 1 contains first i elements
// and r the remaining ones.
// x, 1, r can be -1; time: ^{\circ}O(\lg n)
void split(int x, int& l, int& r, int i) {
  push(x): 1 = r = -1:
  if (x < 0) return;
  int key = size(G[x].E[0]);
  if (i <= key) {
    split(G[x].E[0], 1, G[x].E[0], i);
    r = x:
    split(G[x].E[1], G[x].E[1], r, i-key-1);
  } // fe19
  update(x);
} // 8211
// Join treaps 1 and r into one treap
// such that elements of 1 are before
// elements of r. Returns new treap.
// 1, r and returned value can be -1.
int join(int 1, int r) { // time: ~O(lq n)
  push(1); push(r);
  if (1 < 0 || r < 0) return max(1, r);</pre>
  if (G[1].weight < G[r].weight) {</pre>
    G[1].E[1] = join(G[1].E[1], r);
    update(1);
    return 1;
  } // 18c7
  G[r].E[0] = join(1, G[r].E[0]);
  update(r);
 return r:
1 // b559
// Find i-th node in treap x.
// Returns its key or -1 if not found.
// x can be -1; time: ^{\circ}O(\lg n)
int find(int x, int i) {
  while (x \ge 0) {
    push(x):
    int key = size(G[x].E[0]);
    if (key == i) return x;
    x = G[x].E[key < i];
    if (key < i) i -= key+1;
  1 // 054c
  return -1;
} // Ob9b
// Get key of treap containing node x
// (key of treap root). x can be -1.
int root(int x) { // time: ~O(lg n)
  while (G[x].par >= 0) x = G[x].par;
  return x:
} // be8b
// Get position of node x in its treap.
// x is assumed to NOT be -1; time: ~O(lq n)
int index(int x) {
  int p, i = size(G[x].E[G[x].flip]);
  while ((p = G[x].par) >= 0) {
    if (G[p].E[1] == x) i+=size(G[p].E[0])+1;
```

```
if (G[p].flip) i = G[p].size-i-1;
     x = p;
   } // 3f81
   return i;
 } // ddad
 // Reverse interval [1;r) in treap x.
 // Returns new key of treap; time: ~O(lg n)
 int reverse(int x, int 1, int r) {
   int a, b, c;
   split(x, b, c, r);
   split (b, a, b, 1);
   if (b >= 0) G[b].flip ^= 1;
   return join(join(a, b), c);
 } // e418
}; // 6a6c
structures/wavelet tree.h
                                          69f4
// Wavelet tree ("merge-sort tree over values")
// Each node represent interval of values.
// seq[1]
             = original sequence
// seq[i]
              = subsequence with values
                represented by i-th node
// left[i][j] = how many values in seq[0:j)
                go to left subtree
struct WaveletTree {
 vector<Vi> seq, left;
 int len:
 // Build wavelet tree for sequence `elems`;
 // time and space: O((n+maxVal) log maxVal)
  // Values are expected to be in [0; maxVal).
 WaveletTree(const Vi& elems, int maxVal) {
   for (len = 1; len < maxVal; len *= 2);</pre>
   seq.resize(len*2);
   left.resize(len*2);
   seq[1] = elems;
   build(1, 0, len);
  } // a5e9
 void build(int i, int b, int e) {
   if (i >= len) return;
   int m = (b+e) / 2;
   left[i].pb(0);
   each(x, seq[i]) {
     left[i].pb(left[i].back() + (x < m));
     seq[i*2 + (x >= m)].pb(x);
   } // ac25
   build(i*2, b, m);
   build(i*2+1, m, e);
 } // 8153
 // Find k-th smallest element in [begin; end)
  // [begin;end); time: O(log maxVal)
 int kth(int begin, int end, int k, int i=1) {
   if (i >= len) return seq[i][0];
   int x = left[i][begin], y = left[i][end];
   if (k < y-x) return kth(x, y, k, i*2);
   return kth (begin-x, end-y, k-y+x, i*2+1);
 } // 7861
 // Count number of elements >= vb and < ve
 // in [begin;end); time: O(log maxVal)
 int count (int begin, int end, int vb, int ve,
            int i = 1, int b = 0, int e = -1) {
   if (e < 0) e = len;</pre>
   if (b >= ve || vb >= e) return 0;
   if (b >= vb && e <= ve) return end-begin;</pre>
   int m = (b+e) / 2;
   int x = left[i][begin], y = left[i][end];
   return count(x, y, vb, ve, i*2, b, m) +
```

```
count (begin-x, end-y, vb, ve, i*2+1, m, e);
 } // 71cf
}; // dd48
structures/ext/hash table.h 2d30
#include <ext/pb ds/assoc container.hpp>
using namespace __gnu_pbds;
// gp_hash_table<K, V> = faster unordered_set
// Anti-anti-hash
const size_t HXOR = mt19937_64(time(0))();
template < class T > struct SafeHash {
 size t operator()(const T& x) const {
    return hash<T>() (x ^ T(HXOR));
 1 // 3a78
1; // 7d0e
structures/ext/rope.h
                                         051f
#include <ext/rope>
using namespace __gnu_cxx;
// rope<T> = implicit cartesian tree
structures/ext/tree.h
                                         a3bc
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template < class T, class Cmp = less < T>>
using ordered_set = tree<</pre>
 T, null_type, Cmp, rb_tree_tag,
 tree order statistics node update
// Standard set functions and:
// t.order of key(key) - index of first >= key
// t.find_by_order(i) - find i-th element
// t1.join(t2) - assuming t1<>t2 merge t2 to t1
structures/ext/trie.h
                                         5cc2
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/trie_policy.hpp>
using namespace __gnu_pbds;
using pref trie = trie<
 string, null_type,
 trie_string_access_traits , pat_trie_tag,
 trie_prefix_search_node_update
text/aho corasick.h
                                         697d
constexpr char AMIN = 'a'; // Smallest letter
constexpr int ALPHA = 26: // Alphabet size
// Aho-Corasick algorithm for linear-time
// multiple pattern matching.
// Add patterns using add(), then call build().
struct Aho {
 vector<array<int, ALPHA>> nxt{1};
 Vi suf = \{-1\}, accLink = \{-1\};
 vector<Vi> accept{1};
  // Add string with given ID to structure
  // Returns index of accepting node
 int add(const string& str, int id) {
    int i = 0:
    each(c, str) {
      if (!nxt[i][c-AMIN]) {
       nxt[i][c-AMIN] = sz(nxt);
       nxt.pb({}); suf.pb(-1);
       accLink.pb(1); accept.pb({});
      } // 5ead
```

13

```
i = nxt[i][c-AMIN];
   } // ace9
    accept[i].pb(id);
    return i;
  } // 27c8
  // Build automata; time: O(V*ALPHA)
  void build() {
   queue<int> que;
    each(e, nxt[0]) if (e) {
     suf[e] = 0; que.push(e);
    } // c34d
    while (!que.empty()) {
     int i = que.front(), s = suf[i], j = 0;
     que.pop();
     each(e, nxt[i]) {
       if (e) que.push(e);
        (e ? suf[e] : e) = nxt[s][j++];
     } // 8521
      accLink[i] = (accept[s].empty() ?
          accLink[s] : s);
   } // 1e8a
  } // 2561
  // Append `c` to state `i`
  int next(int i, char c) {
   return nxt[i][c-AMIN];
  } // 6bb7
  // Call `f` for each pattern accepted
  // when in state `i` with its ID as argument.
  // Return true from `f` to terminate early.
  // Calls are in descreasing length order.
  template < class F > void accepted (int i, F f) {
    while (i !=-1) {
     each(a, accept[i]) if (f(a)) return;
     i = accLink[i];
   } // c175
 } // 1f0d
}; // 2768
                                          5729
text/kmp.h
// Computes prefsuf array; time: O(n)
// ps[i] = max prefsuf of <math>[0;i); ps[0] := -1
template < class T > Vi kmp (const T& str) {
 Vi ps; ps.pb(-1);
  each(x, str) {
    int k = ps.back();
    while (k \ge 0 \&\& str[k] != x) k = ps[k];
   ps.pb(k+1);
  } // 05aa
  return ps;
} // 8a6c
// Finds occurences of pat in vec; time: O(n)
// Returns starting indices of matches.
template<class T>
Vi match (const T& str, T pat) {
 int n = sz(pat);
  pat.pb(-1); // SET TO SOME UNUSED CHARACTER
  pat.insert(pat.end(), all(str));
  Vi ret, ps = kmp(pat);
  rep(i, 0, sz(ps)) {
   if (ps[i] == n) ret.pb(i-2*n-1);
  } // ale9
  return ret:
} // f986
text/kmr.h
                                          ee8c
// KMR algorithm for O(1) lexicographical
```

```
// comparison of substrings.
struct KMR {
 vector<Vi> ids;
 KMR() {}
 // Initialize structure; time: O(n lg^2 n)
 // You can change str type to Vi freely.
 KMR (const string& str) {
   ids.clear();
   ids.pb(Vi(all(str)));
   for (int h = 1; h \le sz(str); h *= 2) {
     vector<pair<Pii, int>> tmp;
     rep(j, 0, sz(str)) {
       int a = ids.back()[j], b = -1;
       if (j+h < sz(str)) b = ids.back()[j+h];
       tmp.pb({ {a, b}, j });
     } // a210
     sort(all(tmp));
     ids.emplace_back(sz(tmp));
     int n = 0:
     rep(j, 0, sz(tmp)) {
       if (j > 0 \&\& tmp[j-1].x != tmp[j].x)
       ids.back()[tmp[j].v] = n;
     } // bd2e
   } // 969a
 } // a40e
 // Get representative of [begin; end); 0(1)
 Pii get (int begin, int end) {
   if (begin >= end) return {0, 0};
   int k = 31 - builtin clz(end-begin);
   return {ids[k][begin], ids[k][end-(1<<k)]};</pre>
 } // 85f3
 // Compare [b1;e1) with [b2;e2); O(1)
 // Returns -1 if <, 0 if ==, 1 if >
 int cmp(int b1, int e1, int b2, int e2) {
   int 11 = e1-b1, 12 = e2-b2;
   int 1 = \min(11, 12);
   Pii x = get(b1, b1+1), y = get(b2, b2+1);
   if (x == y) return (11 > 12) - (11 < 12);
   return (x > y) - (x < y);
 } // bf42
  // Compute suffix array of string; O(n)
 Vi sufArrav() {
   Vi sufs(sz(ids.back()));
   rep(i, 0, sz(ids.back()))
     sufs[ids.back()[i]] = i;
   return sufs:
 } // d98d
}; // 457e
                                         0c65
text/lcp.h
// Compute Longest Common Prefix array for
// given string and it's suffix array; O(n)
// In order to compute suffix array use kmr.h
// or suffix_array_linear.h
template<class T>
Vi lcpArray(const T& str, const Vi& sufs) {
 int n = sz(str), k = 0;
 Vi pos(n), lcp(n-1);
 rep(i, 0, n) pos[sufs[i]] = i;
 rep(i, 0, n) {
   if (pos[i] < n-1) {</pre>
     int j = sufs[pos[i]+1];
```

```
while (i+k < n && j+k < n &&
         str[i+k] == str[j+k]) k++;
     lcp[pos[i]] = k;
   } // 2cba
   if (k > 0) k--;
 } // 8b22
 return lcp;
} // d438
text/lvndon factorization.h 688c
// Compute Lyndon factorization for s: O(n)
// Word is simple iff it's stricly smaller
// than any of it's nontrivial suffixes.
// Lyndon factorization is division of string
// into non-increasing simple words.
// It is unique.
vector<string> duval(const string& s) {
 int n = sz(s), i = 0;
 vector<string> ret:
 while (i < n) {
   int j = i+1, k = i;
   while (j < n && s[k] <= s[j])
     k = (s[k] < s[j] ? i : k+1), j++;
   while (i \le k)
     ret.pb(s.substr(i, j-k)), i \leftarrow j-k;
 } // 3f17
 return ret:
} // 0e48
text/main lorentz.h
                                          9afh
#include "z_function.h"
struct Sqr {
 int begin, end, len;
}; // f012
// Main-Lorentz algorithm for finding
// all squares in given word; time: O(n lg n)
// Results are in compressed form:
// (b, e, 1) means that for each b <= i < e
// there is square at position i of size 21.
// Each square is present in only one interval.
vector<Sqr> lorentz(const string& s) {
 int n = sz(s);
 if (n <= 1) return {};</pre>
 auto a = s.substr(0, n/2), b = s.substr(n/2);
 auto ans = lorentz(a);
 each (p, lorentz (b))
   ans.pb(\{p.begin+n/2, p.end+n/2, p.len\});
 string ra(a.rbegin(), a.rend());
 string rb(b.rbegin(), b.rend());
 rep(j, 0, 2) {
   Vi z1 = prefPref(ra), z2 = prefPref(b+a);
   z1.pb(0); z2.pb(0);
   rep(c, 0, sz(a)) {
     int 1 = sz(a) - c;
     int x = c - \min(1-1, z1[11);
     int y = c - max(1-z2[sz(b)+c], j);
     if (x > y) continue;
        ans.pb(\{n-y-1*2, n-x-1*2+1, 1\});
     else
        ans.pb(\{x, y+1, 1\});
   } // 6c51
   a.swap(rb);
   b.swap(ra);
```

```
1 // b6b2
 return ans:
} // 5567
text/manacher.h
                                         8680
// Manacher algorithm; time: O(n)
// Finds largest radiuses for palindromes:
// r[2*i] = for center at i (single letter = 1)
// r[2*i+1] = for center between i and i+1
template < class T > Vi manacher (const T& str) {
 int n = sz(str) \star 2, c = 0, e = 1;
 Vi r(n, 1);
 auto get = [&](int i) { return i%2 ? 0 :
   (i \ge 0 \&\& i < n ? str[i/2] : i); }; // 3d98
 rep(i, 0, n) {
   if (i < e) r[i] = min(r[c*2-i], e-i);
   while (get(i-r[i]) == get(i+r[i])) r[i]++;
   if (i+r[i] > e) c = i, e = i+r[i]-1;
 } // Of87
 rep(i, 0, n) r[i] /= 2;
 return r:
} // a300
text/min rotation.h
                                         e4d6
// Find lexicographically smallest
// rotation of s; time: O(n)
// Returns index where shifted word starts.
// You can use std::rotate to get the word:
// rotate(s.begin(), s.begin()+minRotation(s),
         s.end());
int minRotation(string s) {
 int a = 0, n = sz(s); s += s;
 rep(b, 0, n) rep(i, 0, n) {
   if (a+i == b || s[a+i] < s[b+i]) {
     b += max(0, i-1); break;
   } // 865b
   if (s[a+i] > s[b+i]) {
     a = b; break;
   } // 7628
 } // 40be
 return a;
} // 9ed8
                                         8d2d
text/palindromic tree.h
constexpr int ALPHA = 26; // Set alphabet size
// Tree of all palindromes in string,
// constructed online by appending letters.
// space: O(n*ALPHA); time: O(n)
// Code marked with [EXT] is extension for
// calculating minimal palindrome partition
// in O(n lq n). Can also be modified for
// similar dynamic programmings.
struct PalTree {
 Vi txt; // Text for which tree is built
 // Node 0 = empty palindrome (root of even)
 // Node 1 = "-1" palindrome (root of odd)
 Vi len{0, -1}; // Lengths of palindromes
 Vi link{1, 0}; // Suffix palindrome links
 // Edges to next palindromes
 vector<array<int, ALPHA>> to{ {}, {} };
 int last{0}; // Current node (max suffix pal)
 Vi diff{0, 0}; // len[i]-len[link[i]] [EXT]
 Vi slink{0, 0}; // Serial links
                                          [EXT]
 Vi series {0, 0}; // Series DP answer
                                         [EXT]
 Vi ans{0};
                  // DP answer for prefix[EXT]
```

```
int ext(int i) {
    while (len[i]+2 > sz(txt) ||
          txt[sz(txt)-len[i]-2] != txt.back())
     i = link[i];
    return i;
  ) // d442
  // Append letter from [0;ALPHA); time: O(1)
  // (or O(lg n) if [EXT] is enabled)
  void add(int x) {
   txt.pb(x);
   last = ext(last);
    if (!to[last][x]) {
     len.pb(len[last]+2);
     link.pb(to[ext(link[last])][x]);
     to[last][x] = sz(to);
     to.emplace_back();
     diff.pb(len.back() - len[link.back()]);
     slink.pb(diff.back() == diff[link.back()]
       ? slink[link.back()] : link.back());
     series.pb(0);
     // [/EXT]
    } // Oadb
    last = to[last][x];
    // [EXT]
    ans.pb(INT_MAX);
    for (int i=last; len[i] > 0; i=slink[i]) {
     series[i] = ans[sz(ans) - len[slink[i]]
                     - diff[i] - 11:
     if (diff[i] == diff[link[i]])
       series[i] = min(series[i],
                       series[link[i]]);
     // If you want only even palindromes
     // set ans only for sz(txt) %2 == 0
     ans.back() = min(ans.back(), series[i]+1);
   } // ab3b
    // [/EXT1
 } // 909a
1: // b3a7
                                         1341
```

text/suffix array linear.h

```
#include "../util/radix sort.h"
// KS algorithm for suffix array; time: O(n)
// Input values are assumed to be in [1:k]
Vi sufArray(Vi str, int k) {
  int n = sz(str);
  Vi suf(n);
  str.resize(n+15);
  if (n < 15) {
    iota(all(suf), 0);
    rep(j, 0, n) countSort(suf,
      [&] (int i) { return str[i+n-j-1]; }, k);
    return suf;
  } // 5fcf
  // Compute triples codes
  Vi tmp, code(n+2);
  rep(i, 0, n) if (i % 3) tmp.pb(i);
  rep(j, 0, 3) countSort(tmp,
   [&] (int i) { return str[i-j+2]; }, k);
  int mc = 0, j = -1;
  each(i, tmp) {
    code[i] = mc += (j == -1)
```

str[i] != str[j] ||

```
str[i+1] != str[j+1] ||
       str[i+2] != str[j+2]);
   j = i;
 } // bfdc
 // Compute suffix array of 2/3
 tmp.clear();
 for (int i=1; i < n; i += 3) tmp.pb(code[i]);</pre>
 tmp.pb(0);
 for (int i=2; i < n; i += 3) tmp.pb(code[i]);</pre>
 tmp = sufArray(move(tmp), mc);
 // Compute partial suffix arrays
 Vi third;
 int th = (n+4) / 3;
 if (n%3 == 1) third.pb(n-1);
 rep(i, 1, sz(tmp)) {
   int e = tmp[i];
   tmp[i-1] = (e 
   code[tmp[i-1]] = i;
   if (e < th) third.pb(e*3);
 } // f9f1
 tmp.pop_back();
 countSort (third,
   [&] (int i) { return str[i]; }, k);
 // Merge suffix arrays
 merge(all(third), all(tmp), suf.begin(),
   [&] (int 1, int r) {
     while (1%3 == 0 || r%3 == 0) {
       if (str[l] != str[r])
         return str[l] < str[r];</pre>
       l++: r++:
     } // 2f8a
     return code[1] < code[r];</pre>
   }); // 4cb3
 return suf;
} // 9165
// KS algorithm for suffix array; time: O(n)
Vi sufArrav(const string& str) {
 return sufArray(Vi(all(str)), 255);
} // 593f
                                         d00d
constexpr char AMIN = 'a'; // Smallest letter
```

text/suffix automaton.h

```
constexpr int ALPHA = 26; // Set alphabet size
// Suffix automaton - minimal DFA that
// recognizes all suffixes of given string
// (and encodes all substrings);
// space: O(n*ALPHA); time: O(n)
// Paths from root are equivalent to substrings
// Extensions:
// - [OCC] - count occurences of substrings
// - [PATHS] - count paths from node
struct SufDFA {
 // State v represents endpos-equivalence
 // class that contains words of all lengths
 // between link[len[v]]+1 and len[v].
 // len[v] = longest word of equivalence class
 // link[v] = link to state of longest suffix
              in other equivalence class
 // to [v][c] = automaton edge c from v
 Vi len{0}, link{-1};
 vector<array<int, ALPHA>> to{ {} };
 int last{0}; // Current node (whole word)
 vector<Vi> inSufs; // [OCC] Suffix-link tree
```

// [OCC] Occurence count

Vi cnt{0};

```
vector<11> paths; // [PATHS] Out-path count
SufDFA() {}
// Build suffix automaton for given string
// and compute extended stuff; time: O(n)
SufDFA(const string& s) {
 each(c, s) add(c);
  finish();
} // ec2e
// Append letter to the back
void add(char c) {
 int v = last, x = c-AMIN;
 last = sz(len);
  len.pb(len[v]+1);
  link.pb(0);
  to.pb({});
  cnt.pb(1); // [OCC]
  while (v != -1 \&\& !to[v][x]) {
   to[v][x] = last;
    v = link[v];
  } // 4cfc
  if ( \lor != -1 )  {
    int q = to[v][x];
    if (len[v]+1 == len[q]) {
      link[last] = q;
      len.pb(len[v]+1);
      link.pb(link[a]);
      to.pb(to[q]);
      cnt.pb(0); // [OCC]
      link[last] = link[q] = sz(len)-1;
      while (v != -1 &   to[v][x] == q) {
       to[v][x] = link[q];
       v = link[v];
      } // 784f
    } // 90aa
 } // af69
1 // 345a
// Compute some additional stuff (offline)
void finish() {
  inSufs.resize(sz(len));
  rep(i, 1, sz(link)) inSufs[link[i]].pb(i);
  dfsSufs(0);
  // [PATHS]
  paths.assign(sz(len), 0);
 dfs(0);
  // [/PATHS]
} // 3f75
// Only for [OCC]
void dfsSufs(int v) {
  each(e, inSufs[v]) {
    dfsSufs(e);
    cnt[v] += cnt[e];
 } // 2469
} // 0c60
// Only for [PATHS]
void dfs(int v) {
  if (paths[v]) return;
  paths[v] = 1;
  each(e, to[v]) if (e) {
    dfs(e);
    paths[v] += paths[e];
```

} // 22b3

```
} // d004
 // Go using edge `c` from state `i`.
 // Returns 0 if edge doesn't exist.
 int next(int i, char c) {
   return to[i][c-AMIN];
 } // c363
 // Get lexicographically k-th substring
 // of represented string; time: O(|substr|)
 // Empty string has index 0.
 // Requires [PATHS] extension.
 string lex(ll k) {
   string s;
   int v = 0;
   while (k--) rep(i, 0, ALPHA) {
     int e = to[v][i];
     if (e) {
       if (k < paths[e]) {</pre>
         s.pb(char(AMIN+i));
         v = e;
         break;
       } // f307
       k -= paths[e];
     } // 29be
   } // 4600
   return s;
 } // e4af
}; // 7135
```

text/suffix tree.h

int split(Pii s) {

```
40a4
constexpr int ALPHA = 26;
// Ukkonen's algorithm for online suffix tree
// construction; space: O(n*ALPHA); time: O(n)
// Real tree nodes are called dedicated nodes.
// "Nodes" lying on compressed edges are called
// implicit nodes and are represented
// as pairs (lower node, label index).
// Labels are represented as intervals [L;R)
// which refer to substrings [L;R) of txt.
// Leaves have labels of form [L; infinity),
// use getR to get current right endpoint.
// Suffix links are valid only for internal
// nodes (non-leaves).
struct SufTree {
 Vi txt; // Text for which tree is built
 // to[v][c] = edge with label starting with c
               from node v
 vector<array<int, ALPHA>> to{ {} };
 Vi L{0}, R{0}; // Parent edge label endpoints
              // Parent link
 Vi par{0};
 Vi link{0}: // Suffix link
 Pii cur{0, 0}; // Current state
 // Get current right end of node label
 int getR(int i) { return min(R[i],sz(txt)); }
 // Follow edge `e` of implicit node `s`.
 // Returns (-1, -1) if there is no edge.
 Pii next (Pii s, int e) {
   if (s.y < qetR(s.x))
     return txt[s.y] == e ? mp(s.x, s.y+1)
                           : mp(-1, -1);
   e = to[s.xl[e]:
   return e ? mp(e, L[e]+1) : mp(-1, -1);
 } // f430
 // Create dedicated node for implicit node
 // and all its suffixes
```

```
if (s.y == R[s.x]) return s.x;
    int t = sz(to); to.pb({});
    to[t][txt[s.y]] = s.x;
    L.pb(L[s.x]);
   R.pb(L[s.x] = s.y);
   par.pb(par[s.x]);
    par[s.x] = to[par[t]][txt[L[t]]] = t;
    link.pb(-1);
    int v = link[par[t]], l = L[t] + !par[t];
    while (1 < R[t]) {</pre>
     v = to[v][txt[1]];
     1 += getR(v) - L[v];
   } // 0393
                                                   CentroidTree() {}
   v = split(\{v, getR(v)-l+R[t]\});
   link[t] = v;
    return t;
  } // 10bb
  // Append letter from [0; ALPHA) to the back
  void add(int x) { // amoritzed time: 0(1)
   Pii t; txt.pb(x);
                                                   } // 026c
    while ((t = next(cur, x)).x == -1) {
     int m = split(cur);
                                                     size[v] = 1;
     to[m][x] = sz(to);
     to.pb({});
     par.pb(m);
                                                   } // bbed
     L.pb(sz(txt)-1);
     R.pb(INT MAX);
     link.pb(-1);
     cur = {link[m], getR(link[m])};
     if (!m) return;
   } // 60c2
                                                     dists[c].pb(d);
   cur = t;
 } // 6f4e
1: // dbfb
text/z function.h
                                         0466
                                                    1 // dc82
                                                   } // 37ee
// Computes Z function array; time: O(n)
// zf[i] = max common prefix of str and str[i:]
template < class T > Vi prefPref (const T& str) {
                                                     dfs(G, v, -1);
 int n = sz(str), b = 0, e = 1;
  Vi zf(n);
                                                   loop:
  rep(i, 1, n) {
                                                     each(e, G[v]) {
   if (i < e) zf[i] = min(zf[i-b], e-i);</pre>
   while (i+zf[i] < n &&
     str[zf[i]] == str[i+zf[i]]) zf[i]++;
   if (i+zf[i] > e) b = i, e = i+zf[i];
                                                       } // e0a5
  } // e906
                                                     } // 3533
  zf[0] = n;
                                                     par[v] = -1;
  return zf;
                                                     size[v] = s;
} // b88d
                                                     depth[v] = d;
trees/centroid decomp.h
                                         5247
// Centroid decomposition; space: O(n lg n)
// UNTESTED
struct CentroidTree {
                                                       par[j] = v;
  // child[v] = children of v in centroid tree
                                                     } // 70b5
  // par[v] = parent of v in centroid tree
              (-1 for root)
                                                     return v;
                                                   } // 217c
  // depth[v] = depth of v in centroid tree
                                                 }; // 71d6
                (0 for root)
  // ind[v][i] = index of vertex v in i-th
                centroid subtree from root
  // size[v] = size of centroid subtree of v
```

// subtree[v] = list of vertices

// dists[v] = distances from v to vertices

in centroid subtree of v

```
in its centroid subtree
               (in the order of subtree[v])
 // neigh[v] = neighbours of v
               in its centroid subtree
 // dir[v][i] = index of centroid neighbour
                that is first vertex on path
                from centroid v to i-th vertex
                of centroid subtree
                (-1 for centroid)
 vector<Vi> child, ind, dists, subtree,
            neigh, dir;
 Vi par, depth, size;
 int root; // Root centroid
 CentroidTree (vector<Vi>& G)
     : child(sz(G)), ind(sz(G)), dists(sz(G)),
       subtree(sz(G)), neigh(sz(G)),
       dir(sz(G)), par(sz(G), -2),
       depth(sz(G)), size(sz(G)) {
   root = decomp(G, 0, 0);
 void dfs(vector<Vi>& G, int v, int p) {
   each(e, G[v]) if (e != p && par[e] == -2)
     dfs(G, e, v), size[v] += size[e];
 void layer(vector<Vi>& G, int v,
            int p, int c, int d) {
   ind[v1.pb(sz(subtree[c1));
   subtree[c].pb(v);
   dir[c].pb(sz(neigh[c])-1);
   each(e, G[v]) if (e != p && par[e] == -2) {
     if (v == c) neigh[c].pb(e);
     layer(G, e, v, c, d+1);
 int decomp(vector<Vi>& G, int v, int d) {
   int p = -1, s = size[v];
     if (e != p && par[e] == -2 &&
         size[e] > s/2) {
       p = v; v = e; goto loop;
   layer(G, v, -1, v, 0);
   each (e, G[v]) if (par[e] == -2) {
     int j = decomp(G, e, d+1);
     child[v].pb(j);
                                         ac92
trees/centroid offline.h
// Helper for offline centroid decomposition
// Usage: CentroidDecomp(G);
// Constructor calls method `process`
```

// for each centroid subtree.

```
struct CentroidDecomp {
 vector<Vi>← G; // Reference to target graph
 vector<bool> on; // Is vertex enabled?
 Vi size; // Used internally
  // Run centroid decomposition for graph g
 CentroidDecomp(vector<Vi>& g)
     : G(q), on(sz(q), 1), size(sz(q)) {
   decomp(0);
 } // 8677
 // Compute subtree sizes for subtree rooted
 // at v, ignoring p and disabled vertices
 void computeSize(int v, int p) {
   size[v] = 1;
   each(e, G[v]) if (e != p && on[e])
     computeSize(e, v), size[v] += size[e];
 } // 1c0d
 void decomp(int v) {
   computeSize(v, -1);
   int p = -1, s = size[v];
   each(e, G[v]) {
     if (e != p && on[e] && size[e] > s/2) {
       p = v; v = e; goto loop;
     } // e0a5
   } // f31d
   process(v);
   on[v] = 0;
   each(e, G[v]) if (on[e]) decomp(e);
 } // f170
 // Process current centroid subtree:
 // - v is centroid
 // - boundary vertices have on[x] = 0
 // Formally: Let H be subgraph induced
 // on vertices such that on[v] = 1.
 // Then current centroid subtree is
 // connected component of H that contains v
 // and v is its centroid.
 void process(int v) {
   // Do your stuff here...
 } // d41d
}; // a923
                                         9739
trees/heavylight decomp.h
#include "../structures/segtree_point.h"
// Heavy-Light Decomposition of tree
// with subtree query support; space: O(n)
struct HLD {
 // Subtree of v = [pos[v]; pos[v]+size[v])
 // Chain with v = [chBegin[v]; chEnd[v])
 Vi par;
             // Vertex parent
 Vi size:
             // Vertex subtree size
 Vi depth; // Vertex distance to root
             // Vertex position in "HLD" order
 Vi pos:
 Vi chBegin; // Begin of chain with vertex
 Vi chEnd; // End of chain with vertex
 Vi order; // "HLD" preorder of vertices
 SegTree tree; // Verts are in HLD order
 HLD() {}
 // Initialize structure for tree G
 // and given root; time: O(n lg n)
 // MODIFIES ORDER OF EDGES IN G!
 HLD (vector<Vi>& G, int root)
     : par(sz(G)), size(sz(G)),
       depth(sz(G)), pos(sz(G)),
       chBegin(sz(G)), chEnd(sz(G)) {
```

```
dfs(G, root, -1);
  decomp(G, root, -1, 0);
  tree = {sz(order)};
1 // 8263
void dfs(vector<Vi>& G, int v, int p) {
  par[v] = p;
  size[v] = 1;
  depth[v] = p < 0 ? 0 : depth[p]+1;
  int& fs = G[v][0];
  if (fs == p) swap(fs, G[v].back());
  each(e, G[v]) if (e != p) {
    dfs(G, e, v);
    size[v] += size[e];
    if (size[e] > size[fs]) swap(e, fs);
  } // 9872
} // 12fe
void decomp(vector<Vi>& G,
            int v, int p, int chb) {
  pos[v] = sz(order);
  chBegin[v] = chb;
  chEnd[v] = pos[v]+1;
  order.pb(v);
  each(e, G[v]) if (e != p) {
    if (e == G[v][0]) {
      decomp(G, e, v, chb);
      chEnd[v] = chEnd[e];
    } else {
      decomp(G, e, v, sz(order));
    } // c84a
  } // f707
} // eb89
// Get root of chain containing v
int chRoot(int v) {return order[chBeqin[v]];}
// Level Ancestor Query; time: O(lq n)
int lag(int v, int level) {
  while (true) {
    int k = pos[v] - depth[v] + level;
    if (k >= chBegin[v]) return order[k];
    v = par[chRoot(v)];
  } // 8c18
} // 675e
// Lowest Common Ancestor; time: O(lq n)
int lca(int a, int b) {
  while (chBegin[a] != chBegin[b]) {
    int ha = chRoot(a), hb = chRoot(b);
    if (depth[ha] > depth[hb]) a = par[ha];
    else b = par[hb];
  1 // 5620
  return depth[a] < depth[b] ? a : b;</pre>
} // c168
// Call func(chBegin, chEnd) on each path
// segment; time: O(lq n * time of func)
template<class T>
void iterPath(int a, int b, T func) {
  while (chBegin[a] != chBegin[b]) {
    int ha = chRoot(a), hb = chRoot(b);
    if (depth[ha] > depth[hb]) {
      func(chBegin[a], pos[a]+1);
      a = par[ha];
    } else {
      func(chBegin[b], pos[b]+1);
      b = par[hb];
    } // f9a5
  } // 563c
```

```
// queries (with +1 -> edges).
    func (pos[a]+1, pos[b]+1);
  } // 17e5
  // Query path between a and b; O(lg^2 n)
  SegTree:: T queryPath(int a, int b) {
    auto ret = tree.ID;
   iterPath(a, b, [&](int i, int j) {
     ret = tree.f(ret, tree.query(i, j));
    }); // 1113
    return ret:
  } // 1bc9
  // Query subtree of v; time: O(lg n)
  SegTree::T querySubtree(int v) {
   return tree.query(pos[v], pos[v]+size[v]);
 } // 23db
1: // a062
trees/lca.h
                                          294f
// LAQ and LCA using jump pointers
// space: O(n lg n)
struct LCA {
  vector<Vi> jumps;
  Vi level, pre, post;
  int cnt{0}, depth;
  LCA() {}
  // Initialize structure for tree G
  // and root r; time: O(n lq n)
  LCA(vector<Vi>& G, int root)
      : jumps(sz(G)), level(sz(G)),
        pre(sz(G)), post(sz(G)) {
    dfs(G, root, root);
    depth = int(log2(sz(G))) + 2;
    rep(j, 0, depth) each(v, jumps)
      v.pb(jumps[v[j]][j]);
  } // d6ce
  void dfs(vector<Vi>& G, int v, int p) {
   level[v] = p == v ? 0 : level[p]+1;
    jumps[v].pb(p);
    pre[v] = ++cnt;
    each (e, G[v]) if (e != p) dfs(G, e, v);
   post[v] = ++cnt;
  } // e286
  // Check if a is ancestor of b; time: O(1)
  bool isAncestor(int a, int b) {
    return pre[a] <= pre[b] &&
           post[b] <= post[a];</pre>
  // Lowest Common Ancestor; time: O(lq n)
  int operator()(int a, int b) {
    for (int j = depth; j--;)
      if (!isAncestor(jumps[a][j], b))
       a = jumps[a][j];
    return isAncestor(a, b) ? a : jumps[a][0];
  } // 27d8
  // Level Ancestor Query; time: O(lg n)
  int lag(int a, int lvl) {
    for (int j = depth; j--;)
     if (lvl <= level[jumps[a][j]])</pre>
       a = jumps[a][j];
    return a;
 } // 75b3
```

if (pos[a] > pos[b]) swap(a, b);

// Remove +1 from pos[a]+1 for vertices

```
// Get distance from a to b; time: O(lg n)
 int distance(int a, int b) {
   return level[a] + level[b] -
          level[operator()(a, b)]*2;
 } // 07e0
  // Get k-th vertex on path from a to b,
 // a is 0, b is last; time: 0(lq n)
  // Returns -1 if k > distance(a, b)
 int kthVertex(int a, int b, int k) {
   int c = operator()(a, b);
   if (level[a]-k >= level[c])
     return lag(a, level[a]-k);
    k \leftarrow level[c] \times 2 - level[a];
   return (k > level[b] ? -1 : lag(b, k));
 } // 46c9
}; // 2254
trees/lca linear.h
                                          7aa5
// LAO and LCA using jump pointers
// with linear memory; space: O(n)
// UNTESTED
struct LCA {
 Vi par, jmp, depth, pre, post;
 int cnt{0};
  // Initialize structure for tree G
  // and root v; time: O(n lg n)
 LCA (vector < Vi>& G, int v)
      : par(sz(G), -1), jmp(sz(G), v),
        depth(sz(G)), pre(sz(G)), post(sz(G)) {
   dfs(G, v):
 } // 94cf
  void dfs(vector<Vi>& G, int v) {
   int j = jmp[v], k = jmp[j], x =
     depth[v]+depth[k] == depth[j]*2 ? k : v;
    pre[v] = ++cnt;
    each(e, G[v]) if (!pre[e]) {
     par[e] = v; imp[e] = x;
     depth[e] = depth[v]+1;
     dfs(G, e);
    } // b123
   post[v] = ++cnt;
  1 // 3280
  // Level Ancestor Ouery; time: O(lq n)
 int lag(int v, int d) {
    while (depth[v] > d)
     v = depth[jmp[v]] < d ? par[v] : jmp[v];
   return v;
 } // f509
  // Lowest Common Ancestor; time: O(lq n)
  int operator()(int a, int b) {
   if (depth[a] > depth[b]) swap(a, b);
   b = laq(b, depth[a]);
    while (a != b) {
     if (jmp[a] == jmp[b])
        a = par[a], b = par[b];
       a = jmp[a], b = jmp[b];
   } // fe08
   return a;
 } // 25ff
  // Check if a is ancestor of b; time: O(1)
 bool isAncestor(int a, int b) {
```

```
return pre[a] <= pre[b] &&
          post[b] <= post[a];</pre>
 } // 5514
 // Get distance from a to b; time: O(lg n)
 int distance(int a, int b) {
   return depth[a] + depth[b] -
          depth[operator()(a, b)]*2;
 } // a340
 // Get k-th vertex on path from a to b,
 // a is 0, b is last; time: O(lg n)
 // Returns -1 if k > distance(a, b)
 int kthVertex(int a, int b, int k) {
   int c = operator()(a, b);
   if (depth[a]-k >= depth[c])
     return laq(a, depth[a]-k);
   k += depth[c] *2 - depth[a];
   return (k > depth[b] ? -1 : laq(b, k));
} // 34ed
}; // a221
trees/link cut tree.h
                                          6bd6
constexpr int INF = 1e9;
// Link/cut tree; space: O(n)
// Represents forest of (un)rooted trees.
struct LinkCutTree {
 vector<array<int, 2>> child;
 Vi par, prev, flip, size;
 // Initialize structure for n vertices; O(n)
  // At first there's no edges.
 LinkCutTree(int n = 0)
     : child(n, \{-1, -1\}), par(n, -1),
       prev(n, -1), flip(n, -1), size(n, 1) {}
 void push(int x) {
   if (x >= 0 && flip[x]) {
     flip[x] = 0;
     swap(child[x][0], child[x][1]);
     each(e, child[x]) if (e>=0) flip[e] ^= 1;
   } // + any other lazy path operations
 } // bae2
 void update(int x) {
   if (x >= 0) {
     size[x] = 1;
     each(e, child[x]) if (e \geq= 0)
       size[x] += size[e];
   } // + any other path aggregates
  } // 8ec0
 void auxLink(int p, int i, int ch) {
   child[p][i] = ch;
   if (ch \ge 0) par[ch] = p;
   update(p);
 } // 0a9a
 void rot(int p, int i) {
   int x = child[p][i], g = par[x] = par[p];
   if (g \ge 0) child[g][child[g][1] == p] = x;
   auxLink(p, i, child[x][!i]);
   auxLink(x, !i, p);
   swap(prev[x], prev[p]);
   update(g);
 } // 4c76
 void splay(int x) {
   while (par[x] >= 0) {
     int p = par[x], g = par[p];
     push(g); push(p); push(x);
     bool f = (child[p][1] == x);
```

```
if (q >= 0) {
      if (child[g][f] == p) { // zig-zig
        rot(q, f); rot(p, f);
      } else { // zig-zag
        rot(p, f); rot(g, !f);
      } // 2ebb
    } else { // zig
      rot (p, f);
    } // f8a2
  } // 446b
  push(x);
} // 55a7
// After this operation x becomes the end
// of preferred path starting in root;
void access(int x) { // amortized O(lg n)
  while (true) {
    splay(x);
    int p = prev[x];
    if (p < 0) break;
    prev[x] = -1;
    splay(p);
    int r = child[p][1];
    if (r \ge 0) swap(par[r], prev[r]);
    auxLink(p, 1, x);
  } // 2b87
} // 30be
// Make x root of its tree; amortized O(lq n)
void makeRoot(int x) {
  access(x):
  int& 1 = child[x][0];
  if (1 >= 0) {
    swap(par[1], prev[1]);
    flip[1] ^= 1;
    update(1):
    1 = -1;
    update(x);
  } // 0064
} // b246
// Find root of tree containing x
int find(int x) { // time: amortized O(lq n)
  access(x);
  while (child[x][0] >= 0)
    push(x = child[x][0]);
  splay(x);
  return x;
1 // d78d
// Add edge x-y; time: amortized O(lg n)
// Root of tree containing y becomes
// root of new tree.
void link(int x, int y) {
  makeRoot(x); prev[x] = y;
} // fb4f
// Remove edge x-y; time: amortized O(lg n)
// x and y become roots of new trees!
void cut(int x, int y) {
  makeRoot(x); access(y);
  par[x] = child[y][0] = -1;
  update(y);
} // 1908
// Get distance between x and y,
// returns INF if x and y there's no path.
// This operation makes x root of the tree!
int dist(int x, int y) { // amortized O(lq n)
  makeRoot(x);
```

```
if (find(y) != x) return INF;
    access(y);
    int t = child[y][0];
    return t >= 0 ? size[t] : 0;
 } // ae69
}; // 4480
util/arc interval cover.h
                                         7507
using dbl = double:
// Find size of smallest set of points
// such that each arc contains at least one
// of them; time: O(n lq n)
int arcCover(vector<pair<dbl, dbl>>& inters,
            dbl wrap) {
  int n = sz(inters);
  rep(i, 0, n) {
   auto& e = inters[i];
   e.x = fmod(e.x, wrap);
   e.y = fmod(e.y, wrap);
   if (e.x < 0) e.x += wrap, e.y += wrap;</pre>
   if (e.x > e.y) e.x += wrap;
   inters.pb({e.x+wrap, e.y+wrap});
  } // b87d
 Vi nxt(n);
  deque<dbl> que;
  dbl r = wrap*4;
  sort (all (inters));
  for (int i = n*2-1; i--:) {
   r = min(r, inters[i].y);
   que.push front(inters[i].x);
   while (!que.empty() && que.back() > r)
     que.pop_back();
   if (i < n) nxt[i] = i+sz(que);</pre>
  } // 5e6c
  int a = 0, b = 0;
  do {
   a = nxt[a] % n;
   b = nxt[nxt[b]%n] % n;
  } while (a != b);
  int ans = 0;
  while (b < a+n) {
   b += nxt[b%n] - b%n;
   ans++:
  } // 7350
  return ans;
} // 7871
util/bit hacks.h
                                         599a
// builtin popcount - count number of 1 bits
// builtin clz - count most significant 0s
// builtin ctz - count least significant 0s
// __builtin_ffs - like ctz, but indexed from 1
                returns 0 for 0
// For 11 version add 11 to name
using ull = uint64 t:
#define T64(s,up)
 for (ull i=0; i<64; i+=s*2)
    for (ull j = i; j < i+s; j++) {
     ull \ a = (M[j] >> s) \& up;
      ull\ b = (M[j+s] \& up) << s;
     M[j] = (M[j] \& up) | b;
     M[j+s] = (M[j+s] & (up << s)) | a; 
    } // a290
// Transpose 64x64 bit matrix
```

```
void transpose64 (arrav<ull, 64>& M) {
 T64(1, 0x55555555555555);
 T64(4, OxFOFOFOFOFOFOF);
 T64(8, OxFF00FF00FF00FF);
 T64 (16. 0xFFFF0000FFFF);
 T64 (32, OxFFFFFFFLL);
} // 6889
// Lexicographically next mask with same
// amount of ones.
int nextSubset(int v) {
 int t = v | (v - 1);
 return (t + 1) | (((~t & -~t) - 1) >>
      (\underline{\phantom{a}}builtin_ctz(v) + 1));
} // 4c0c
util/bump_alloc.h
                                         09f9
// Allocator, which doesn't free memory.
char mem[400<<20]; // Set memory limit</pre>
size t nMem;
void* operator new(size t n) {
 nMem += n; return &mem[nMem-n];
} // fba6
void operator delete(void*) {}
                                         bc5d
util/compress vec.h
// Compress integers to range [0;n) while
// preserving their order; time: O(n lg n)
// Returns mapping: compressed -> original
Vi compressVec(vector<int*>& vec) {
 sort (all (vec),
   [](int* 1, int* r) { return *1 < *r; });
 Vi old;
 each (e, vec) {
   if (old.empty() || old.back() != *e)
     old.pb(\stare);
   \star e = sz(old)-1;
 } // 7eb0
 return old:
} // 2b60
util/inversion vector.h
                                         0.1 + 9
// Get inversion vector for sequence of
// numbers in [0;n); ret[i] = count of numbers
// greater than perm[i] to the left; O(n lq n)
Vi encodeInversions (Vi perm) {
 Vi odd, ret(sz(perm));
 int cont = 1;
  while (cont) {
   odd.assign(sz(perm)+1, 0);
    cont = 0;
   rep(i, 0, sz(perm)) {
     if (perm[i] % 2) odd[perm[i]]++;
     else ret[i] += odd[perm[i]+1];
     cont += perm[i] /= 2;
   } // 4ed0
 } // a4f0
 return ret;
} // c2e1
// Count inversions in sequence of numbers
// in [0;n); time: O(n lq n)
11 countInversions(Vi perm) {
 11 ret = 0, cont = 1;
 Vi odd;
```

while (cont) {

```
odd.assign(sz(perm)+1, 0);
   cont = 0;
   rep(i, 0, sz(perm)) {
     if (perm[i] % 2) odd[perm[i]]++;
     else ret += odd[perm[i]+1];
     cont += perm[i] /= 2;
   } // 916f
 } // c9b5
 return ret;
} // laaf
util/longest_inc_subseq.h
                                         0bd1
// Longest Increasing Subsequence; O(n lq n)
int lis(const Vi& seq) {
 Vi dp(sz(seg), INT MAX);
 each(c, seg) *lower bound(all(dp), c) = c;
 return int (lower bound (all (dp), INT MAX)
            - dp.begin());
} // d0e9
util/max rects.h
                                         2a16
struct MaxRect (
 // begin = first column of rectangle
 // end = first column after rectangle
 // hei = height of rectangle
 // touch = columns of height hei inside
 int begin, end, hei;
 Vi touch; // sorted increasing
}; // 41fe
// Given consecutive column heights find
// all inclusion-wise maximal rectangles
// contained in "drawing" of columns; time O(n)
vector < MaxRect > getMaxRects (Vi hei) {
 hei.insert(hei.begin(), -1);
 hei.pb(-1);
 Vi reach(sz(hei), sz(hei)-1);
 vector<MaxRect> ans;
 for (int i = sz(hei)-1; --i;) {
   int j = i+1, k = i;
   while (hei[j] > hei[i]) j = reach[j];
   reach[i] = j;
    while (hei[k] > hei[i-1]) {
     ans.pb(\{ i-1, 0, hei[k], \{\} \});
     auto& rect = ans.back();
     while (hei[k] == rect.hei) {
       rect.touch.pb(k-1);
       k = reach[k];
     } // 6e7e
     rect.end = k-1;
   } // e03f
 } // 2796
 return ans;
} // 0e49
util/mo.h
                                         caeb
// Modified MO's queries sorting algorithm,
// slightly better results than standard.
// Allows to process q queries in O(n*sqrt(q))
struct Query {
int begin, end:
1; // b76d
// Get point index on Hilbert curve
11 hilbert(int x, int y, int s, ll c = 0) {
if (s <= 1) return c;
 s /= 2; c *= 4;
```

```
if (y < s)
    return hilbert (x \in (s-1), y, s, c+(x>=s)+1);
 if (x < s)
    return hilbert (2*s-y-1, s-x-1, s, c);
 return hilbert (y-s, x-s, s, c+3);
} // Ofb9
// Get good order of queries; time: O(n lq n)
Vi moOrder(vector<Ouery>€ queries, int maxN) {
 int s = 1;
 while (s < maxN) s \star= 2;
 vector<11> ord;
 each (q, queries)
   ord.pb(hilbert(g.begin, g.end, s));
 Vi ret(sz(ord));
 iota(all(ret), 0);
 sort(all(ret), [&](int l, int r) {
   return ord[1] < ord[r];</pre>
 }); // 9aea
 return ret;
} // ecec
util/parallel binsearch.h
                                         bc5d
// Run `n` binary searches on [b;e) parallely.
// `cmp` should be lambda with arguments:
// 1) vector<Pii>& - pairs (v, i)
    which are queries if value for index i
     is greater or equal to v;
     pairs are sorted by v
// 2) vector<bool>& - output vector,
     set true at index i if value
      for i-th query is >= queried value
// Returns vector of found values:
// time: O((n+c) lg range), where c is cmp time
template<class T>
Vi multiBS(int b, int e, int n, T cmp) {
 vector<Pii> que(n), rng(n, {b, e});
 vector<bool> ans(n);
  rep(i, 0, n) que[i] = \{(b+e)/2, i\};
 for (int k = 32-__builtin_clz(e-b); k--;) {
   int last = 0, j = 0;
    cmp(que, ans);
    rep(i, 0, sz(que)) {
     Pii &q = que[i], &r = rng[q.y];
      if (q.x != last) last = q.x, j = i;
      (ans[i] ? r.x : r.y) = q.x;
      q.x = (r.x+r.y) / 2;
      if (!ans[i]) swap(que[i], que[j++]);
   } // 6c4e
 } // 622c
 Vi ret;
 each (p, rng) ret.pb(p.x);
 return ret;
} // lad7
util/radix sort.h
                                          6fb4
// Stable countingsort; time: O(k+sz(vec))
// See example usage in radixSort for pairs.
template<class F>
void countSort(Vi& vec, F key, int k) {
 static Vi buf, cnt;
 vec.swap(buf);
 vec.resize(sz(buf));
 cnt.assign(k+1, 0);
```

each (e, buf) cnt [key (e)]++;

rep(i, 1, k+1) cnt[i] += cnt[i-1];

```
for (int i = sz(vec)-1; i >= 0; i--)
   vec[--cnt[key(buf[i])]] = buf[i];
} // cc6f
// Compute order of elems, k is max key; O(n)
Vi radixSort (const vector < Pii>& elems, int k) {
 Vi order(sz(elems));
 iota(all(order), 0);
 countSort(order,
   [&](int i) { return elems[i].y; }, k);
  countSort(order,
   [&] (int i) { return elems[i].x; }, k);
 return order;
} // e8f6
```