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```
.bashrc
                                          ef12
                                                  #define pri(x,y,z)tem auto operator<<(t&o,u a) \
                                                    ->decltype(x,o) { o << z; return o << y; }
build()(
 g++ $0 -o $1.e -DLOC -std=c++11
                                                  pri(a.print(), '}', '{'; a.print())
      -Wall -Wextra -Wfatal-errors -Wshadow \
                                                  pri(a.y, ')', '(' << a.x << ", " << a.y)
      -Wlogical-op -Wconversion -Wfloat-equal
                                                  pri(all(a), ']', '['; auto d="";
                                                  for (auto i : a) (o << d << i, d = ", "))
b() ( build $@ -02 )
                                                  void DD(...) {}
d() ( build $@ -fsanitize=address, undefined \
                                                  tem void DD(ts, ua, w...k) {
              -D_GLIBCXX_DEBUG -q )
                                                   for (int b=1; *s && *s - b*44; cerr << *s++)
                                                   b += 2 / (*s*2 - 81);
run()($1 $2 && echo start >&2 && time ./$2.e)
                                                   cerr << ": " << a << *s++; DD(s, k...);
100()(
                                                  } // fd6d
  set -e; $1 $2; $1 $3
                                                  #ifdef LOC
  for ((;;)) {
                                                  #define deb(...) (DD("[,\b :] "#__VA_ARGS__, \
    ./$3.e > gen.in
                                                   __LINE__, __VA_ARGS__), cerr << endl)
    time ./$2.e < gen.in > gen.out
                                                  #else
                                                  #define deb(...)
                                                  #endif
cmp()(
                                                  #define DBP(...) void print() { \
  set -e; $1 $2; $1 $3; $1 $4
                                                   DD (# VA ARGS , VA ARGS ); } // 813f
  for ((;;)) {
    ./$4.e > gen.in;
                              echo -n 0
                                                  // > Utils
    ./$2.e < gen.in > p1.out; echo -n 1
                                                  // Return smallest k such that 2^k > n
    ./$3.e < gen.in > p2.out; echo -n 2
                                                  // Undefined for n = 0!
    diff pl.out p2.out;
                              echo -n Y
                                                  int uplg(int n) { return 32- builtin clz(n); }
                                                  int uplg(ll n) { return 64-__builtin_clzll(n); }
                                                  // Compare with certain epsilon (branchless)
# Other flags:
                                                  // Returns -1 if a < b: 1 if a > b: 0 if equal
# -Wformat=2 -Wshift-overflow=2 -Wcast-qual
                                                  // a and b are assumed equal if |a-b| <= eps
# -Wcast-align -Wduplicated-cond
                                                  int cmp(double a, double b, double eps=1e-9) {
# -D GLIBCXX DEBUG PEDANTIC -D FORTIFY SOURCE=2
                                                   return (a > b + eps) - (a + eps < b);
# -fno-sanitize-recover -fstack-protector
                                                  } // 81c1
                                          8b2d
.vimrc
                                                  various.h
se ai aw cin cul ic is nocp nohls nu sc scs
                                                  // If math constants like M_PI are not found
se bg=dark sw=4 ts=4 so=7 ttm=9
                                                  // add this at the beginning of file
                                                  #define _USE_MATH_DEFINES
vn _ :w !cpp -dD -P -fpreprocessed \|
 tr -d '[:space:]' \| md5sum \| cut -c-4 <CR>
                                                  // Pragmas
                                                  #pragma GCC optimize("Ofast, unroll-loops,
                                          8fcc
template.cpp
                                                                        no-stack-protector")
                                                  #pragma GCC target("popcnt,avx,tune=native")
#include <bits/stdc++.h>
using namespace std;
                                                  // Clock
                                                  while (clock() < duration*CLOCKS PER SEC)
using 11 = long long;
using Vi = vector<int>;
                                                  // Automatically implement operators:
using Pii = pair<int,int>;
                                                  // 1. != if == is defined
                                                  // 2. >, <= and >= if < is defined
#define mp make pair
                                                  using namespace rel_ops;
#define pb push back
#define x first
                                                  // Mersenne twister for randomization.
#define v second
                                                  mt19937_64 rnd (chrono::steady_clock::now()
                                                   .time_since_epoch().count());
#define rep(i,b,e) for(int i=(b); i<(e); i++)
#define each (a, x) for (auto \& a : (x))
                                                  // To shuffle randomly use:
#define all(x)
                   (x).begin(),(x).end()
                                                  shuffle(all(vec), rnd)
#define sz(x)
                   int((x).size())
                                                  // To pick random integer from [A;B] use:
int main() {
                                                  uniform_int_distribution <> dist(A, B);
 cin.sync_with_stdio(0); cin.tie(0);
                                                  int value = dist(rnd);
 cout << fixed << setprecision(18);</pre>
                                                  // To pick random real number from [A;B] use:
 // Don't call destructors:
                                                  uniform_real_distribution  dist(A, B);
 cout << flush; _Exit(0);</pre>
                                                  double value = dist(rnd);
} // 4799
                                                  geometry/convex hull.h
// > Debug printer
                                                  #include "vec2.h"
#define tem template < class t, class u, class...w>
```

```
// Translate points such that lower-left point
       // is (0, 0). Returns old point location; O(n)
       vec2 normPos(vector<vec2>& points) {
        auto q = points[0].yx();
        each (p, points) q = min(q, p.yx());
        vec2 ret{q.y, q.x};
        each (p, points) p = p-ret;
        return ret;
       } // ee96
       // Find convex hull of points; time: O(n lg n)
       // Points are returned counter-clockwise,
       // first point is the lowest-left.
       vector<vec2> convexHull (vector<vec2> points) {
        vec2 pivot = normPos(points);
        sort(all(points));
        vector<vec2> hull;
        each (p, points) {
          while (sz(hull) >= 2) {
           vec2 a = hull.back() - hull[sz(hull)-2];
           vec2 b = p - hull.back();
           if (a.cross(b) > 0) break;
           hull.pop_back();
          } // ad91
         hull.pb(p);
        } // 5908
        // Translate back, optional
        each (p, hull) p = p+pivot;
        return hull:
       } // 62ed
       // Find point p that minimizes dot product p*q.
       // Returns point index in hull; time: O(lq n)
       // If multiple points have same dot product
       // one with smallest index is returned.
       // Points are expected to be in the same order
cbc4
       // as output from convexHull function.
       int minDot (const vector < vec2> € hull, vec2 q) {
        auto search = [&] (int b, int e, vec2 p) {
          while (b+1 < e) {
           int m = (b+e) / 2;
           (p.dot(hull[m-1]) > p.dot(hull[m])
            ? b : e) = m;
          1 // 184c
          return b;
        }; // 62e8
        int m = search(0, sz(hull), \{0, -1\});
        int i = search(0, m, q);
        int j = search(m, sz(hull), q);
        return q.dot(hull[i]) > q.dot(hull[j])
         ? j : i;
       } // 4599
       geometry/convex hull dist.h 2859
        #include "vec2.h"
       // Check if p is inside convex polygon. Hull
       // must be given in counter-clockwise order.
       // Returns 2 if inside, 1 if on border,
       // 0 if outside; time: O(n)
       int insideHull(vector<vec2>& hull, vec2 p) {
        int ret = 1:
        rep(i, 0, sz(hull)) {
          auto v = hull[(i+1)%sz(hull)] - hull[i];
          auto t = v.cross(p-hull[i]);
4a8e
          ret = min(ret, cmp(t, 0)); // For doubles
          //ret = min(ret, (t>0) - (t<0)); // Ints
```

} // Od40

```
return int (max (ret+1, 0));
} // 1f39
#include "segment2.h"
// Get distance from point to hull; time: O(n)
double hullDist (vector<vec2>& hull, vec2 p) {
 if (insideHull(hull, p)) return 0;
 double ret = 1e30;
 rep(i, 0, sz(hull)) {
  seg2 seg{hull[(i+1)%sz(hull)], hull[i]};
  ret = min(ret, seg.distTo(p));
 } // f3be
 return ret;
} // a00c
// Compare distance from point to hull
// with sqrt(d2); time: O(n)
// -1 if smaller, 0 if equal, 1 if greater
int cmpHullDist(vector<vec2>& hull,
          vec2 p, 11 d2) {
 if (insideHull(hull,p)) return (d2<0)-(d2>0);
 int ret = 1:
 rep(i, 0, sz(hull)) {
  seg2 seg{hull[(i+1)%sz(hull)], hull[i]};
  ret = min(ret, seg.cmpDistTo(p, d2));
 } // 28cb
 return ret;
} // 30f3
geometry/convex_hull sum.h
                                          7f53
#include "vec2.h"
// Get edge sequence for given polygon
// starting from lower-left vertex; time: O(n)
// Returns start position.
vec2 edgeSeq(vector<vec2> points,
        vector<vec2>& edges) {
 int i = 0, n = sz(points);
 rep(j, 0, n)
  if (points[i].yx() > points[j].yx()) i = j;
 rep(j, 0, n) edges.pb(points[(i+j+1)%n] -
               points[(i+j)%n]);
 return points[i];
} // 3aa7
// Minkowski sum of given convex polygons.
// Vertices are required to be in
// counter-clockwise order; time: O(n+m)
vector<vec2> hullSum (vector<vec2> A,
             vector<vec2> B) {
 vector<vec2> sum, e1, e2, es(sz(A) + sz(B));
 vec2 pivot = edgeSeg(A, e1) + edgeSeg(B, e2);
 merge(all(e1), all(e2), es.begin());
 sum.pb(pivot);
 each (e, es) sum.pb (sum.back() + e);
 sum.pop_back();
 return sum;
} // f183
                                          356a
geometry/halfplanes.h
#include "vec2.h"
#include "line2.h"
// Intersect halfplanes given by `lines`
// and output hull vertices to 'out'
// in counter-clockwise order. Returns true
// if intersection is non-empty and bounded.
// Unbounded cases are not supported.
// add bounding-box if necessary. Works only
// with floating point vec2/line2; O(n lg n)
```

bool intersectHalfplanes (vector<line2> in,

sort(all(in), [](line2 a, line2 b) {

return (a.v.angleCmp(b.v) ?:

int a = 0, b = 0, n = sz(in);

vector<line2> dq(n+5);

out.resize(n+5);

dq[0] = in[0];

vector<vec2>& out) {

a.c\*b.v.len() - b.c\*a.v.len()) < 0;

// PARTIALLY TESTED

}); // 82fb

```
rep(i, 1, n+1) {
  if (i == n) in.pb(dq[a]);
  if (!in[i].v.angleCmp(in[i-1].v)) continue;
  while (a < b && in[i].side(out[b-1]) > 0)
   h--:
  while (i!=n && a < b && in[i].side(out[a])>0)
  if (in[i].intersect(dq[b], out[b]))
   dq[++b] = in[i];
 1 // b9ba
 out.resize(b):
 out.erase(out.begin(), out.begin()+a);
 return b-a > 2;
} // f334
geometry/line2.h
                                          92.07
#include "vec2.h"
// 2D line/halfplane structure
// PARTIALLY TESTED
// Base class of versions for ints and doubles
template<class T, class P, class S>
struct bline2 {
// For lines: v * point == c
 // For halfplanes: v * point <= c
 // (i.e. normal vector points outside)
P v: // Normal vector [A: B]
T c; // Offset (C parameter of equation)
 DBP (v, c);
 // Line through 2 points; normal vector
 // points to the right of ab vector
 static S through (Pa, Pb) {
  return { (a-b).perp(), a.cross(b) };
 // Parallel line through point
 static S parallel (P a, S b) {
  return { b.v. b.v.dot(a) };
 } // 8e1c
 // Perpendicular line through point
 static S perp (Pa, Sb) {
  return { b.v.perp(), b.v.cross(a) };
 } // 7b75
 // Distance from point to line
 double distTo(P a) {
  return fabs (v.dot(a)-c) / v.len();
1 // 79e6
}; // ee4f
// Version for integer coordinates (long long)
struct line2i : bline2<11, vec2i, line2i> {
line2i(): bline2{{}, 0} {}
line2i (vec2i a, 11 b) : bline2{a, b} {}
 // Returns 0 if point a lies on the line,
// 1 if on side where normal vector points,
```

```
int side(vec2i a) {
  11 d = v.dot(a);
  return (d > c) - (d < c);
} // 18a7
1: // fc9c
// Version for double coordinates
// Requires cmp() from template
struct line2d : bline2<double, vec2d, line2d> {
line2d() : bline2{{}, 0} {}
line2d(vec2d a, double b) : bline2{a, b} {}
 // Returns 0 if point a lies on the line,
 // 1 if on side where normal vector points,
 // -1 if on the other side.
 int side(vec2d a) { return cmp(v.dot(a),c); }
 // Intersect this line with line a, returns
 // true on success (false if parallel).
 // Intersection point is saved to `out`.
 bool intersect (line2d a, vec2d& out) {
  double d = v.cross(a.v);
  if (!cmp(d, 0)) return 0;
  out = (v*a.c - a.v*c).perp() / d;
  return 1;
} // 2e68
}; // ab54
using line2 = line2d;
geometry/rmst.h
                                           476a
#include "../structures/find union.h"
// Rectilinear Minimum Spanning Tree
// (MST in Manhattan metric); time: O(n lq n)
// Returns MST weight. Outputs spanning tree
// to G, vertex indices match point indices.
// Edge in G is pair (target, weight).
ll rmst (vector < Pii > & points.
     vector<vector<Pii>>> G) {
 int n = sz(points);
 vector<pair<int, Pii>> edges;
 vector<Pii> close;
 Vi ord(n), merged(n);
 iota(all(ord), 0);
 function<void(int,int)> octant =
   [&] (int begin, int end) {
  if (begin+1 >= end) return;
  int mid = (begin+end) / 2;
  octant (begin, mid);
  octant (mid, end);
  int i = mid:
  Pii best = {INT MAX, -1};
  merged.clear():
  rep(i, begin, mid) {
   int v = ord[i];
   Pii p = points[v];
    while (j < end) {
     int e = ord[j];
     Pii q = points[e];
     if (q.x-q.y > p.x-p.y) break;
     best = min(best, make_pair(q.x+q.y, e));
     merged.pb(e);
     j++;
   } // 8576
   if (best.v != -1) {
    int alt = best.x-p.x-p.y;
```

// -1 if on the other side.

```
close[v] = {alt, best.y};
   } // 4208
   merged.pb(v);
  } // f3ff
  while (j < end) merged.pb(ord[j++]);</pre>
  copy(all(merged), ord.begin()+begin);
 }; // a4e1
 rep(i, 0, 4) {
  rep(j, 0, 2) {
   sort(all(ord), [&](int l, int r) {
     return points[l] < points[r];</pre>
    }); // fe33
    close.assign(n, {INT_MAX, -1});
    octant(0, n);
    rep(k, 0, n) {
    Pii p = close[k];
     if (p.y != -1) edges.pb(\{p.x, \{k, p.y\}\});
     points[k].x \star = -1;
   } // 1c1d
  1 // 9b38
  each (p, points) p = \{p.y, -p.x\};
 } // d06f
 11 sum = 0;
 FAU fau(n);
 sort(all(edges));
 G.assign(n, {});
 each (e, edges) if (fau. join (e.y.x, e.y.y)) {
  sum += e.x;
  G[e.y.x].pb({e.y.y, e.x});
  G[e.y.y].pb({e.y.x, e.x});
 } // b04a
return sum;
1 // f586
geometry/segment2.h
                                            6504
#include "vec2.h"
// 2D segment structure; NOT HEAVILY TESTED
// Base class of versions for ints and doubles
template < class P, class S> struct bseq2 {
Pa, b; // Endpoints
 // Distance from segment to point
 double distTo(P p) const {
  if ((p-a).dot(b-a) < 0) return (p-a).len();</pre>
  if ((p-b).dot(a-b) < 0) return (p-b).len();</pre>
  return double (abs ((p-a).cross (b-a)))
           / (b-a).len();
1 // 62a2
}; // 85bc
// Version for integer coordinates (long long)
struct seg2i : bseg2<vec2i, seg2i> {
 seq2i() {}
 seq2i(vec2i c, vec2i d) : bseq2{c, d} {}
 // Check if segment contains point p
 bool contains (vec2i p) {
  return (a-p).dot(b-p) <= 0 &&
       (a-p).cross(b-p) == 0;
 // Compare distance to p with sqrt(d2)
 // -1 if smaller, 0 if equal, 1 if greater
 int cmpDistTo(vec2i p, 11 d2) const {
  if ((p-a).dot(b-a) < 0) {
   11 1 = (p-a).len2();
```

if (alt < close[v1.x)</pre>

```
return (1 > d2) - (1 < d2);
  } // dla6
  if ((p-b).dot(a-b) < 0) {
   ll 1 = (p-b).len2();
    return (1 > d2) - (1 < d2);
  1 // 9e65
  11 c = abs((p-a).cross(b-a));
  d2 \neq (b-a).len2();
  return (c*c > d2) - (c*c < d2);
 } // 726d
}; // 4df2
// Version for double coordinates
// Requires cmp() from template
struct seg2d: bseg2<vec2d, seg2d> {
 seq2d() {}
 seg2d(vec2d c, vec2d d) : bseg2{c, d} {}
 bool contains (vec2d p) {
  return cmp((a-p).dot(b-p), 0) <= 0 &&
       cmp((a-p).cross(b-p), 0) == 0;
 1 // b507
}; // 2036
using seg2 = seg2d;
geometry/vec2.h
                                            6e47
// 2D point/vector structure; PARTIALLY TESTED
// Base class of versions for ints and doubles
template < class T, class S> struct bvec2 {
Tx, v;
 S operator+(S r) const {return{x+r.x,y+r.y};}
 S operator-(S r) const {return{x-r.x,y-r.y};}
 S operator*(T r) const { return {x*r, y*r}; }
 S operator/(T r) const { return {x/r, y/r}; }
 T dot(S r) const { return x*r.x + y*r.y; }
 T cross(S r) const { return x*r.y - y*r.x; }
 T len2() const { return x*x + y*y; }
 double len() const { return hypot(x, y); }
 S perp() const { return {-y,x}; } // CCW
 pair<T, T> yx() const { return {y, x}; }
 double angle() const { //[0;2*PI] CCW from OX
  double a = atan2(y, x);
  return (a < 0 ? a+2*M_PI : a);</pre>
 } // 7095
1: // 17ed
// Version for integer coordinates (long long)
struct vec2i : bvec2<11, vec2i> {
 vec2i() : bvec2{0, 0} {}
 vec2i(11 a, 11 b) : bvec2{a, b} {}
 bool upper() const { return (y ?: x) >= 0; }
 int angleCmp(vec2i r) const {
  11 c = cross(r);
  return r.upper() -upper() ?: (c<0) - (c>0);
 } // b35f
 // Compare by angle, length if angles equal
 bool operator<(vec2i r) const {</pre>
  return (angleCmp(r) ?:
       len2() - r.len2()) < 0;
 1 // 6f78
 bool operator==(vec2i r) const {
  return x == r.x && v == r.v;
 } // 136e
}; // d3f4
```

```
// Version for double coordinates
// Requires cmp() from template
struct vec2d : bvec2<double, vec2d> {
 vec2d() : bvec2{0, 0} {}
 vec2d(double a, double b) : bvec2{a, b} {}
 bool upper () const {
  return (cmp(y, 0) ?: cmp(x, 0)) >= 0;
 } // 086c
 int angleCmp(vec2d r) const {
  return r.upper() - upper() ?:
       cmp(0, cross(r));
 } // 12f3
 // Compare by angle, length if angles equal
 bool operator<(vec2d r) const {</pre>
  return (angleCmp(r) ?:
        cmp(len2(), r.len2())) < 0;
 bool operator==(vec2d r) const {
  return !cmp(x, r.x) && !cmp(v, r.v);
 } // 81cd
 vec2d unit() const { return *this / len(); }
 vec2d rotate (double a) const { // CCW
  return {x*cos(a) - y*sin(a),
       x*sin(a) + y*cos(a); // 1890
 } // 97e3
}; // 08e9
using vec2 = vec2d;
graphs/2sat.h
                                           2443
// 2-SAT solver; time: O(n+m), space: O(n+m)
// Variables are indexed from 1 and
// negative indices represent negations!
// Usage: SAT2 sat(variable_count);
// (add constraints...)
// bool solution_found = sat.solve();
// sat[i] = value of i-th variable, 0 or 1
            (also indexed from 1!)
// (internally: positive = i*2-1, neg. = i*2-2)
struct SAT2 : Vi {
 vector<Vi>G;
 Vi order, flags;
 // Init n variables, you can add more later
 SAT2 (int n = 0) : G(n*2) {}
 // Add new var and return its index
 int addVar() {
  G.resize(sz(G)+2); return sz(G)/2;
 // Add (i => j) constraint
 void imply(int i, int j) {
  i = i*2 ^i >> 31;
  j = j*2 ^ j >> 31;
  G[--i].pb(--j); G[j^1].pb(i^1);
 // Add (i v j) constraint
 void either(int i, int j) { imply(-i, j); }
 // Constraint at most one true variable
 void atMostOne(Vi& vars) {
  int v, x = addVar();
  each(i, vars) {
   imply(x, y = addVar());
    imply(i, -x); imply(i, x = y);
  } // 24aa
```

```
1 // 3ed7
 // Solve and save assignments in `values`
 bool solve() { // O(n+m), Kosaraju is used
  assign(sz(G)/2+1, -1);
  flags.assign(sz(G), 0);
  rep(i, 0, sz(G)) dfs(i);
  while (!order.empty()) {
   if (!propag(order.back()^1, 1)) return 0;
   order.pop_back();
  } // 5594
  return 1;
 } // 1e58
 void dfs(int i) {
  if (flags[i]) return;
  flags[i] = 1;
  each (e, G[i]) dfs (e);
  order.pb(i);
 } // d076
 bool propag(int i, bool first) {
  if (!flags[i]) return 1;
  flags[i] = 0;
  if (at (i/2+1) >= 0) return first;
  at (i/2+1) = i & 1;
  each (e, G[i]) if (!propag(e, 0)) return 0;
  return 1:
} // 4c1b
}; // d74c
graphs/bellman ineq.h
                                           cd51
struct Inea {
11 a, b, c; // a - b >= c
1; // 663a
// Solve system of inequalities of form a-b>=c
// using Bellman-Ford; time: O(n*m)
bool solveIneq(vector<Ineq>₺ edges,
         vector<ll>& vars) {
 rep(i, 0, sz(vars)) each(e, edges)
  vars[e.b] = min(vars[e.b], vars[e.a]-e.c);
 each (e, edges)
  if (vars[e.a]-e.c < vars[e.b]) return 0;</pre>
 return 1;
} // 241e
graphs/biconnected.h
                                           2b9e
// Biconnected components; time: O(n+m)
// Usage: Biconnected bi(graph);
// bi[v] = indices of components containing v
// bi.verts[i] = vertices of i-th component
// bi.edges[i] = edges of i-th component
// Bridges <=> components with 2 vertices
// Articulation points <=> vertices that belong
                           to > 1 component
// Isolated vertex <=> empty component list
struct Biconnected : vector<Vi> {
 vector<Vi> verts:
 vector<vector<Pii>>> edges;
 vector<Pii>S;
 Biconnected() {}
 Biconnected (vector < Vi>& G) : S(sz(G)) {
  resize(sz(G));
  rep(i, 0, sz(G)) S[i].x ?: dfs(G, i, -1);
  rep(c, 0, sz(verts)) each(v, verts[c])
   at (v) .pb(c);
 } // cfce
 int dfs(vector<Vi>& G, int v, int p) {
```

```
int low = S[v].x = sz(S)-1;
  S.pb(\{v, -1\});
  each(e, G[v]) if (e != p) {
   if (S[e].x < S[v].x) S.pb({v, e});
   low = min(low, S[e].x ?: dfs(G, e, v));
  } // 446d
  if (p+1 && low >= S[p].x) {
   verts.pb({p}); edges.pb({});
   rep(i, S[v].x, sz(S)) {
     if (S[i].y == -1)
      verts.back().pb(S[i].x);
      edges.back().pb(S[i]);
   } // 4fab
   S.resize(S[v].x);
  1 // 6d66
  return low:
} // 7fcc
}; // 4fa4
graphs/boski matching.h
                                           dbd2
// Bosek's algorithm for partially online
// bipartite maximum matching - white vertices
// are fixed, black vertices are added
// one by one; time: O(E*sqrt(V))
// Usage: Matching match(num_white);
// match[v] = index of black vertex matched to
              white vertex v or -1 if unmatched
// match.add(indices of white neighbours);
// Black vertices are indexed in order they
// were added, the first black vertex is 0.
struct Matching : Vi {
vector<Vi> adj;
 Vi rank, low, pos, vis, seen;
 int k{0};
 // Initialize structure for n white vertices
 Matching(int n = 0): Vi(n, -1), rank(n) {}
 // Add new black vertex with its neighbours
 // given by `vec`. Returns true if maximum
 // matching is increased by 1.
 bool add(Vi vec) {
  adj.pb (move (vec));
  low.pb(0); pos.pb(0); vis.pb(0);
  if (!adi.back().emptv()) {
   int i = k;
    seen.clear();
    if (dfs(sz(adj)-1, ++k-i)) return 1;
    each (v. seen) each (e. adi[v])
     if (rank[e] < 1e9 && vis[at(e)] < k)</pre>
      goto nxt:
    each (v, seen) each (w, adj[v])
     rank[w] = low[v] = 1e9;
  } // 6aec
  return 0;
 } // d2a7
 bool dfs(int v, int g) {
  if (vis[v] < k) vis[v] = k, seen.pb(v);
  while (low[v] < g) {</pre>
   int e = adj[v][pos[v]];
   if (at(e) != v && low[v] == rank[e]) {
     rank[e]++;
     if (at (e) == -1 | | dfs(at (e), rank[e]))
      return at (e) = v, 1;
   } else if (++pos[v] == sz(adj[v])) {
```

```
pos[v] = 0; low[v] ++;
   } // e532
  } // 3d88
  return 0;
 } // 8561
}; // aac1
graphs/bridges online.h
                                           4124
// Dynamic 2-edge connectivity gueries
// Usage: Bridges bridges (vertex count);
// - bridges.addEdge(u, v); - add edge (u, v)
// - bridges.cc[v] = connected component ID
// - bridges.bi(v) = 2-edge connected comp ID
struct Bridges {
 vector<Vi>G; // Spanning forest
 Vi cc, size, par, bp, seen;
 int cnt{0};
 // Initialize structure for n vertices: O(n)
 Bridges (int n = 0): G(n), cc(n), size(n, 1),
               par(n, -1), bp(n, -1),
               seen(n) {
  iota(all(cc), 0);
 1 // ed70
 // Add edge (u, v); time: amortized O(lg n)
 void addEdge(int u, int v) {
  if (cc[u] == cc[v]) {
   int r = lca(u, v);
    for (int x : \{u, v\})
     while ((x = root(x)) != r)
      x = bp[bi(x)] = par[x];
  } else {
    G[u].pb(v); G[v].pb(u);
    if (size[cc[u]] > size[cc[v]]) swap(u,v);
    size[cc[v]] += size[cc[u]];
   dfs(u, v);
  } // abc7
 } // a6fd
 // Get 2-edge connected component ID
 int bi(int v) { // amortized time: < O(lq n)</pre>
  return bp[v] + 1 ? bp[v] = bi(bp[v]) : v;
 1 // 3206
 int root(int v) {
  return par [v] == -1 || bi (par [v]) != bi (v)
   ? v : par[v] = root(par[v]);
 1 // 2d27
 void dfs(int v, int p) {
  cc[v] = cc[par[v] = p];
  each(e, G[v]) if (e != p) dfs(e, v);
 } // 85f5
 int lca(int u, int v) { // Don't use this!
  for (cnt++;; swap(u, v)) if (u != -1) {
   if (seen[u = root(u)] == cnt) return u;
    seen[u] = cnt; u = par[u];
  } // afed
} // 7f56
}; // bd70
graphs/dense_dfs.h
                                           4fbd
#include "../math/bit matrix.h"
// DFS over bit-packed adjacency matrix
// G = NxN adjacency matrix of graph
       G(i,j) \iff (i,j) \text{ is edge}
// V = 1xN matrix containing unvisited vertices
       V(0,i) \iff i-th \text{ vertex is not visited}
// Total DFS time: O(n^2/64)
```

```
reset();
 } // 79e4
 // Mark all vertices as unvisited
 void reset() { each(x, V.M) x = -1; }
 // Get/set visited flag for i-th vertex
 void setVisited(int i) { V.set(0, i, 0); }
 bool isVisited(int i) { return !V(0, i); }
 // DFS step: func is called on each unvisited
 // neighbour of i. You need to manually call
 // setVisited(child) to mark it visited
 // or this function will call the callback
 // with the same vertex again.
 template<class T>
 void step(int i, T func) {
  ull \star E = G.row(i);
  for (int w = 0; w < G.stride;) {</pre>
   ull x = E[w] & V.row(0)[w];
   if (x) func((w<<6) | builtin ctzll(x));</pre>
  } // 4c0a
 } // f045
}; // 8edb
graphs/dominators.h
                                            aec6
// Tarjan's algorithm for finding dominators
// in directed graph; time: O(m log n)
// Returns array of immediate dominators idom.
// idom[root] = root
// idom[v] = -1 if v is unreachable from root
Vi dominators (const vector < Vi>& G, int root) {
 int n = sz(G):
 vector<Vi> in(n), bucket(n);
 Vi pre (n, -1), anc (n, -1), par (n), best (n);
 Vi ord, idom(n, -1), sdom(n, n), rdom(n);
 function<void(int,int) > dfs =
  [&] (int v, int p) {
   if (pre[v] == -1) {
     par[v] = p;
     pre[v] = sz(ord);
     ord.pb(v);
     each(e, G[v]) in[e].pb(v), dfs(e, v);
   } // 1182
  }; // ffd2
 function<Pii(int)> find = [&](int v) {
  if (anc[v] == -1) return mp(best[v], v);
  int b: tie(b, anc[v]) = find(anc[v]);
  if (sdom[b] < sdom[best[v]]) best[v] = b;</pre>
  return mp (best[v], anc[v]);
 }; // c07b
 rdom[root] = idom[root] = root;
 iota(all(best), 0);
 dfs(root, -1);
 rep(i, 0, sz(ord)) {
  int v = ord[sz(ord)-i-1], b = pre[v];
  each(e, in[v])
   b = min(b, pre[e] < pre[v] ? pre[e] :</pre>
           sdom[find(e).x]);
  each (u, bucket [v]) rdom[u] = find(u).x;
  sdom[v] = b;
  anc[v] = par[v];
```

struct DenseDFS {

BitMatrix G, V; // space: O(n^2/64)

// Initialize structure for n vertices
DenseDFS(int n = 0) : G(n, n), V(1, n) {

```
bucket[ord[sdom[v]]].pb(v);
 } // 54f4
 each (v, ord) idom [v] = (rdom[v] == v ?
  ord[sdom[v]] : idom[rdom[v]]);
 return idom:
} // 0656
graphs/edmonds karp.h
                                           e8cc
using flow t = int:
constexpr flow_t INF = 1e9+10;
// Edmonds-Karp algorithm for finding
// maximum flow in graph; time: O(V*E^2)
// NOT HEAVILY TESTED
struct MaxFlow {
 struct Edge {
  int dst. inv:
  flow_t flow, cap;
 }; // a53c
 vector<vector<Edge>> G;
 vector<flow_t> add;
 Vi prev;
 // Initialize for n vertices
 MaxFlow(int n = 0) : G(n) {}
 // Add new vertex
 int addVert() {
  G.emplace_back(); return sz(G)-1;
 } // 907a
 // Add edge between u and v with capacity cap
 // and reverse capacity rcap
 void addEdge(int u, int v,
          flow_t cap, flow_t rcap = 0) {
  G[u].pb({v, sz(G[v]), 0, cap});
  G[v].pb({u, sz(G[u])-1, 0, rcap});
 } // Of10
 // Compute maximum flow from src to dst.
 // Flow values can be found in edges.
 // vertices with `add` >= 0 belong to
 // cut component containing `s`.
 flow_t maxFlow(int src, int dst) {
  flow ti, m, f = 0;
  each (v, G) each (e, v) e.flow = 0;
  queue<int> 0:
  O.push (src);
  prev.assign(sz(G), -1);
  add.assign(sz(G), -1);
  add[src] = INF;
  while (!Q.empty()) {
   m = add[i = Q.front()];
   Q.pop();
    if (i == dst) {
     while (i != src) {
      auto& e = G[i][prev[i]];
      e.flow -= m:
      G[i = e.dst][e.inv].flow += m;
     } // 1f86
     f += m;
     goto nxt;
    } // 43a2
    each (e, G[i])
     if (add[e.dst] < 0 && e.flow < e.cap) {</pre>
      Q.push(e.dst);
```

prev[e.dst] = e.inv;

```
add[e.dst] = min(m, e.cap-e.flow);
     } // 4cdb
  } // 887e
  return f:
 } // cec0
 // Get if v belongs to cut component with src
bool cutSide(int v) {
  return add[v] >= 0;
} // 41e9
}; // 8673
graphs/gomory hu.h
                                          a520
#include "edmonds karp.h"
//#include "push relabel.h" // if you need
struct Edge {
int a, b; // vertices
flow_t w; // weight
1: // c331
// Build Gomory-Hu tree; time: O(n*maxflow)
// Gomory-Hu tree encodes minimum cuts between
// all pairs of vertices: mincut for u and v
// is equal to minimum on path from u and v
// in Gomory-Hu tree. n is vertex count.
// Returns vector of Gomory-Hu tree edges.
vector<Edge> gomoryHu (vector<Edge>& edges,
              int n) {
 MaxFlow flow(n):
 each (e, edges) flow.addEdge (e.a, e.b, e.w, e.w);
 vector<Edge> ret(n-1);
 rep(i, 1, n) ret[i-1] = \{i, 0, 0\};
 rep(i, 1, n) {
  ret[i-1].w = flow.maxFlow(i, ret[i-1].b);
  rep(j, i+1, n)
   if (ret[j-1].b == ret[i-1].b &&
      flow.cutSide(j)) ret[j-1].b = i;
 } // 5ae4
 return ret;
} // afdb
                                          1f40
graphs/kth shortest.h
constexpr 11 INF = 1e18;
// Eppstein's k-th shortest path algorithm;
// time and space: O((m+k) log (m+k))
struct Eppstein {
 using T = 11; // Type for edge weights
 using Edge = pair<int, T>;
 struct Node {
  int E[2] = \{\}, s\{0\};
  Edge x:
 }; // 013b
 T shortest; // Shortest path length
 priority queue<pair<T, int>> 0;
 vector<Node> P{1};
 // Initialize shortest path structure for
 // weighted graph G, source s and target t;
 // time: O(m log m)
 Eppstein (vector<vector<Edge>>& G,
      int s, int t) {
  int n = sz(G);
  vector<vector<Edge>> H(n);
  rep(i,0,n) each(e,G[i]) H[e.x].pb({i,e.y});
```

```
Vi ord, par(n, -1);
  vector<T> d(n, -INF);
  Q.push(\{d[t] = 0, t\});
  while (!Q.empty()) {
    auto v = Q.top();
    () qoq.0
    if (d[v.y] == v.x) {
     ord.pb(v.v);
     each (e, H[v.y]) if (v.x-e.y > d[e.x]) {
      Q.push(\{d[e.x] = v.x-e.y, e.x\});
      par[e.x] = v.y;
     } // 5895
   } // 1b62
  } // la6d
   if ((shortest = -d[s]) >= INF) return;
  h.resize(n);
  each (v. ord) {
    int p = par[v];
    if (p+1) h[v] = h[p];
    each (e, G[v]) if (d[e.x] > -INF) {
     T k = e.v - d[e.x] + d[v];
     if (k | | e.x != p)
      h[v] = push(h[v], \{e.x, k\});
      p = -1;
    } // 5e05
  } // 31b9
  P[0].x.x = s;
  0.push({0, 0});
 } // e00e
 int push(int t, Edge x) {
  P.pb(P[t1);
  if (!P[t = sz(P)-1].s || P[t].x.y >= x.y)
    swap(x, P[t].x);
  if (P[t1.s) {
    int i = P[t].E[0], j = P[t].E[1];
    int d = P[il.s > P[il.s;
    int k = push(d ? j : i, x);
   P[t].E[d] = k; // Don't inline k!
  } // 10e1
  P[t].s++;
  return t;
 } // a2dc
 // Get next shortest path length.
 // the first call returns shortest path.
 // Returns -1 if there's no more paths;
 // time: O(\log k), where k is total count
 // of nextPath calls.
 ll nextPath() {
  if (Q.empty()) return -1;
  auto v = Q.top();
  Q.pop();
  for (int i : P[v.y].E) if (i)
    Q.push({v.x-P[i].x.y+P[v.y].x.y, i});
  int t = h[P[v.y].x.x];
  if (t) Q.push({ v.x - P[t].x.y, t });
  return shortest - v.x;
 } // 08af
}; // 5326
graphs/matroids.h
                                           55ef
// Find largest subset S of [n] such that
```

// S is independent in both matroid A and B.

// A and B are given by their oracles,

// see example implementations below.

```
// Returns vector V such that V[i] = 1 iff
// i-th element is included in found set;
// time: O(r^2*init + r^2*n*add).
// where r is max independent set,
// `init` is max time of oracles init
// and `add` is max time of oracles canAdd.
template < class T, class U>
vector<bool> intersectMatroids (T& A, U& B,
                    int n) {
 vector<bool> ans(n);
bool ok = 1:
 A.init(ans);
 B.init (ans);
 rep(i, 0, n) if (A.canAdd(i) && B.canAdd(i))
  ans[i] = 1, A.init(ans), B.init(ans);
 while (ok) {
  vector<Vi>G(n);
  vector<bool> good(n);
  queue<int> que;
  Vi prev(n, -1);
  A.init(ans);
  B.init(ans);
  ok = 0;
  rep(i, 0, n) if (!ans[i]) {
   if (A.canAdd(i)) que.push(i), prev[i]=-2;
   good[i] = B.canAdd(i);
  } // 9581
  rep(i, 0, n) if (ans[i]) {
   ans[i] = 0;
   A.init(ans);
   B.init(ans);
   rep(i, 0, n) if (i != i && !ans[i]) {
    if (A.canAdd(j)) G[i].pb(j);
    if (B.canAdd(j)) G[j].pb(i);
   1 // bd2a
   ans[i] = 1;
  1 // bf3e
  while (!que.emptv()) {
   int i = que.front();
   que.pop();
   if (good[i]) {
    ans[i] = 1;
     while (prev[i] >= 0) {
      ans[i = prev[i] = 0;
     ans[i = prev[i]] = 1;
    } // 51c8
    ok = 1:
    break:
   } // 384b
   each(j, G[i]) if (prev[j] == -1)
    que.push(j), prev[j] = i;
  } // 6eb6
 1 // e092
 return ans:
} // ae8e
// Matroid where each element has color
// and set is independent iff for each color c
// #{elements of color c} <= maxAllowed[c].</pre>
struct LimOracle {
Vi color; // color[i] = color of i-th element
Vi maxAllowed; // Limits for colors
 // Init oracle for independent set S; O(n)
```

```
void init(vector<bool>& S) {
  tmp = maxAllowed;
  rep(i, 0, sz(S)) tmp[color[i]] -= S[i];
 } // 4dfb
 // Check if S+{k} is independent; time: O(1)
 bool canAdd(int k) {
 return tmp[color[k]] > 0;
} // e312
}; // 7b5d
// Graphic matroid - each element is edge,
// set is independent iff subgraph is acyclic.
struct GraphOracle {
vector<Pii> elems; // Ground set: graph edges
 int n: // Number of vertices, indexed [0:n-1]
 Vi par;
 int find(int i) {
  return par[i] == -1 ? i
     : par[i] = find(par[i]);
 } // b8b7
 // Init oracle for independent set S: ~O(n)
 void init(vector<bool>& S) {
  par.assign(n, -1);
  rep(i, 0, sz(S)) if (S[i])
   par[find(elems[i].x)] = find(elems[i].v);
 // Check if S+{k} is independent; time: ~O(1)
 bool canAdd(int k) {
   find(elems[k].x) != find(elems[k].y);
1 // 8ca4
}; // c506
// Co-graphic matroid - each element is edge,
// set is independent iff after removing edges
// from graph number of connected components
// doesn't change.
struct CographOracle {
vector<Pii> elems; // Ground set: graph edges
 int n: // Number of vertices, indexed [0:n-1]
 vector<Vi>G:
 Vi pre, low;
 int cnt:
 int dfs(int v, int p) {
  pre[v] = low[v] = ++cnt;
  each (e, G[v]) if (e != p)
   low[v] = min(low[v], pre[e] ?: dfs(e,v));
  return low[v];
 1 // 9d30
 // Init oracle for independent set S: O(n)
 void init(vector<bool>& S) {
  G.assign(n, {});
  pre.assign(n, 0);
  low.resize(n);
  cnt = 0:
  rep(i, 0, sz(S)) if (!S[i]) {
   Pii e = elems[i];
   G[e.x].pb(e.y);
   G[e.y].pb(e.x);
  } // 79a1
  rep(v, 0, n) if (!pre[v]) dfs(v, -1);
 } // 1200
 // Check if S+{k} is independent; time: O(1)
 bool canAdd(int k) {
  Pii e = elems[k]:
  return max(pre[e.x], pre[e.y])
```

```
!= max(low[e.x], low[e.y]);
} // 2550
}; // a5cc
// Matroid equivalent to linear space with XOR
struct XorOracle {
vector<11> elems; // Ground set: numbers
 vector<11> base:
 // Init for independent set S; O(n+r^2)
 void init(vector<bool>& S) {
  base.assign(63, 0);
  rep(i, 0, sz(S)) if (S[i]) {
   ll e = elems[i];
   rep(j, 0, sz(base)) if ((e >> j) & 1) {
    if (!base[j]) {
      base[j] = e;
      break:
     } // 1df5
     e ^= base[i];
   } // 8495
  } // 655e
 1 // b68c
 // Check if S+{k} is independent; time: O(r)
 bool canAdd(int k) {
  11 e = elems[k];
  rep(i, 0, sz(base)) if ((e >> i) & 1) {
   if (!base[i]) return 1;
   e ^= base[i];
  1 // 49d1
  return 0;
} // 66ff
1: // 4af3
graphs/push relabel.h
                                          2a0c
using flow t = int;
constexpr flow_t INF = 1e9+10;
// Push-relabel algorithm for maximum flow:
// O(V^2*sqrt(E)), but very fast in practice.
// Preflow is not converted to flow!
// UNTESTED
struct MaxFlow {
 struct Edge {
  int to, inv;
  flow t rem, cap;
 }; // bc77
 vector<basic_string<Edge>> G;
 vector<flow t> extra;
 Vi hei, arc, prv, nxt, act, bot;
 queue<int> 0:
 int n, high, cut, work;
 // Initialize for n vertices
 MaxFlow(int k = 0) : G(k) {}
 // Add new vertex
 int addVert() {
  G.emplace back();
  return sz(G)-1;
 } // 907a
 // Add edge between u and v with
 // capacity cap and reverse capacity rcap
 void addEdge(int u, int v,
         flow_t cap, flow_t rcap = 0) {
  G[u].pb({ v, sz(G[v]), 0, cap });
  G[v].pb({u, sz(G[u])-1, 0, rcap});
 } // Of10
 void raise(int v, int h) {
```

```
if (hei[v] < n)</pre>
  prv[nxt[prv[v]] = nxt[v]] = prv[v];
 if ((hei[v] = h) < n) {</pre>
  if (extra[v] > 0) {
   bot[v] = act[h], act[h] = v;
   high = max(high, h);
  } // Oae9
  cut = max(cut, h);
  nxt[v] = nxt[prv[v] = h += n];
  prv[nxt[nxt[h] = v]] = v;
 } // 9bcf
} // 1c35
void global(int t) {
hei.assign(n, n);
 act.assign(n, -1);
 iota(all(prv), 0);
 iota(all(nxt), 0);
 hei[t] = high = cut = work = 0;
 for (Q.push(t); !Q.empty(); Q.pop()) {
  int v = Q.front();
  each (e, G[v])
    if (hei[e.to]==n && G[e.to][e.inv].rem)
     Q.push(e.to), raise(e.to, hei[v]+1);
} // 4edc
} // d78f
void push(int v, Edge& e) {
 auto f = min(extra[v], e.rem);
 if (f > 0) {
  if (!extra[e.to]) {
   bot[e.to] = act[hei[e.to]];
    act[hei[e.to]] = e.to;
  } // 9d90
  e.rem -= f; G[e.to][e.inv].rem += f;
  extra[v] -= f; extra[e.to] += f;
1 // a86a
} // 94aa
void discharge(int v) {
 int h = n;
 auto go = [&] (int a, int b) {
  rep(i, a, b) {
    auto& e = G[v][i];
    if (e.rem) {
     if (hei[v] == hei[e.to]+1) {
      push (v, e);
      if (extra[v] <= 0)</pre>
        return arc[v] = i, 0;
     } else h = min(h, hei[e.to]+1);
   } // 8adf
  } // 6369
  return 1:
 }; // 0671
 if (go(arc[v], sz(G[v])) && go(0, arc[v])){
  int k = hei[v] + n;
  if (nxt[k] == prv[k]) {
   rep(j, k, cut+n+1)
     while (nxt[j] < n) raise(nxt[j], n);</pre>
    cut = k-n-1;
  } else raise(v, h), work++;
} // dcb2
} // 4d2f
// Compute maximum flow from src to dst
flow t maxFlow(int src, int dst) {
 extra.assign(n = sz(G), 0);
 hei.assign(n, 0);
 arc.assign(n, 0);
```

```
prv.resize(n*2);
  nxt.resize(n*2);
  act.resize(n);
  bot.resize(n);
  each (v, G) each (e, v) e.rem = e.cap;
  extra[dst] = -(extra[src] = INF);
  each (e, G[src]) push (src, e);
  global(dst);
  for (; high; high--)
   while (act[high] != -1) {
     int v = act[high];
     act[high] = bot[v];
     if (hei[v] == high) {
      discharge(v);
      if (work > 4*n) global(dst);
     } // 21cf
   } // b0c8
  return extra[dst] + INF;
 } // 8e2f
 // Get if v belongs to cut component with src
 bool cutSide(int v) { return hei[v] >= n; }
}; // 44ea
graphs/scc.h
// Tarjan's SCC algorithm; time: O(n+m)
// Usage: SCC scc(graph);
// scc[v] = index of SCC for vertex v
// scc.comps[i] = vertices of i-th SCC
// Components are in reversed topological order
struct SCC : Vi {
 vector<Vi>comps:
 Vi S;
 SCC() {}
 SCC(vector\langle \text{Vi} \rangle \& \text{G}): Vi(sz(G),-1), S(sz(G)) {
  rep(i, 0, sz(G)) if (!S[i]) dfs(G, i);
 } // f0fa
 int dfs(vector<Vi>& G, int v) {
  int low = S[v] = sz(S);
  S.pb(v);
  each (e, G[v]) if (at (e) < 0)
   low = min(low, S[e] ?: dfs(G, e));
  if (low == S[v]) {
   comps.pb({});
   rep(i, S[v], sz(S)) {
     at (S[i]) = sz(comps)-1;
     comps.back().pb(S[i]);
   } // 8ed0
   S.resize(S[v]);
  } // ecc7
  return low:
 } // f3c6
}; // 215e
graphs/turbo matching.h
                                           d400
// Find maximum bipartite matching; time: ?
// G must be bipartite graph!
// Returns matching size (edge count).
// match[v] = vert matched to v or -1
int matching(vector<Vi>& G, Vi& match) {
 vector<bool> seen:
 int n = 0, k = 1;
```

match.assign(sz(G), -1);

function<int(int)> dfs = [&](int i) {

```
if (seen[i]) return 0;
                                                         if (cur < sla[j])</pre>
   seen[i] = 1;
                                                          sla[j] = cur, prv[j] = b;
   each(e, G[i]) {
                                                         if (sla[j] < d) d = sla[j], c = j;</pre>
   if (match[e] < 0 || dfs(match[e])) {</pre>
                                                        } // 6717
                                                        rep(j, 0, m+1) {
     match[i] = e; match[e] = i;
                                                         if (vis[j]) x[R[j]] += d, y[j] -= d;
     return 1:
   } // 893d
                                                         else sla[j] -= d;
  } // 9532
                                                       } // 8bb3
  return 0;
                                                      } // 01c6
 }; // d332
                                                      while (b-m) c = b, R[c] = R[b = prv[b]];
                                                     } // 71f5
 while (k) {
  seen.assign(sz(G), 0);
                                                     rep(j, 0, m) if (R[j]+1) L[R[j]] = j;
                                                     R.resize(m);
  rep(i, 0, sz(G)) if (match[i] < 0)
                                                     return -y[m];
   k += dfs(i);
                                                    } // 349d
  n += k;
                                                    math/berlekamp massey.h
                                                                                               7d12
 } // 1128
 return n:
                                                    constexpr int MOD = 998244353;
} // 0d38
                                                    ll modInv(ll a, ll m) { // a^{(-1)} \mod m
// Convert maximum matching to vertex cover
                                                    if (a == 1) return 1:
// time: O(n+m)
                                                    return ((a - modInv(m%a, a)) *m + 1) / a;
Vi vertexCover (vector < Vi>& G, Vi& match) {
                                                   } // c437
Vi ret, col(sz(G)), seen(sz(G));
                                                    // Find shortest linear recurrence that matches
 function<void(int, int)> dfs =
                                                   // given starting terms of recurrence; O(n^2)
   [&] (int i, int c) {
                                                    // Returns vector C such that for each i >= |C|
  if (col[i]) return;
                                                    // A[i] = sum A[i-j-1]*C[j] for j = 0..|C|-1
  col[i] = c+1;
                                                    vector<ll> massey (vector<ll>& A) {
  each (e, G[i]) dfs (e, !c);
                                                    if (A.empty()) return {};
 }; // 1f1b
                                                     int n = sz(A), len = 0, k = 0;
                                                     11 s = 1:
 function<void(int) > aug = [&](int i) {
                                                     vector<11> B(n), C(n), tmp;
  if (seen[i] | col[i] != 1) return;
                                                     B[0] = C[0] = 1;
  seen[i] = 1;
  each (e, G[i]) seen [e] = 1, aug (match [e]);
                                                     rep(i, 0, n) {
 1: // 2465
                                                      11 d = 0;
                                                      k++;
 rep(i, 0, sz(G)) dfs(i, 0);
                                                      rep(j, 0, len+1)
 rep(i, 0, sz(G)) if (match[i] < 0) aug(i);
                                                       d = (d + C[j] * A[i-j]) % MOD;
 rep(i, 0, sz(G))
  if (seen[i] == col[i]-1) ret.pb(i);
 return ret;
                                                       11 q = d ★ modInv(s, MOD) % MOD;
} // 6f72
                                                       tmp = C:
graphs/weighted matching.h
                                           8264
                                                        rep(j, k, n)
                                                        C[j] = (C[j] - q * B[j-k]) % MOD;
// Minimum cost bipartite matching; O(n^2*m)
                                                       if (len*2 <= i) {</pre>
// Input is n x m cost matrix, where n <= m.
                                                         B.swap(tmp);
// Returns matching weight.
// L[i] = right vertex matched to i-th left
                                                         len = i-len+1;
                                                         s = d + (d < 0) * MOD;
// R[i] = left vertex matched to i-th right
                                                         k = 0;
11 hungarian (const vector < vector < ll>> & cost.
                                                       } // c350
        Vi& L, Vi& R) {
 if (cost.empty())
                                                      } // 79c7
  return L.clear(), R.clear(), 0;
                                                     } // f70c
 int b, c = 0, n = sz(cost), m = sz(cost[0]);
                                                     C.resize(len+1);
 assert (n <= m);
                                                     C.erase(C.begin());
 vector<11> x(n), y(m+1);
                                                     each (x, C) x = (MOD - x) % MOD;
                                                     return C:
 L.assign(n, -1);
                                                    } // 20ce
 R.assign(m+1, -1);
 rep(i, 0, n) {
                                                   math/bit_gauss.h
                                                                                               13eb
  vector<11> sla(m, INT64_MAX);
                                                    constexpr int MAX COLS = 2048;
  Vi vis (m+1), prv(m, -1);
  for (R[b = m] = i; R[b] + 1; b = c) {
                                                    // Solve system of linear equations over Z_2
   int a = R[b];
                                                    // time: O(n^2*m/W), where W is word size
    11 d = INT64_MAX;
                                                    // - A - extended matrix, rows are equations,
    vis[b] = 1:
                                                             columns are variables.
    rep(j, 0, m) if (!vis[j]) {
                                                             m-th column is equation result
```

(A[i][j] - i-th row and j-th column)

ll cur = cost[a][j] - x[a] - y[j];

```
// - ans - output for variables values
// - m - variable count
// Returns 0 if no solutions found, 1 if one,
// 2 if more than 1 solution exist.
int bitGauss (vector<bitset<MAX COLS>>& A,
        vector<bool>& ans, int m) {
 Vi col;
 ans.assign(m, 0);
 rep(i, 0, sz(A)) {
  int c = int(A[i]._Find_first());
  if (c >= m) {
    if (c == m) return 0;
    continue;
  } // a6bb
  rep(k, i+1, sz(A)) if (A[k][c]) A[k]^=A[i];
  swap(A[i], A[sz(col)]);
  col.pb(c);
 } // a953
 for (int i = sz(col); i--;) if (A[i][m]) {
  ans [col[i]] = 1;
  rep(k,0,i) if(A[k][col[i]]) A[k][m].flip();
 } // 4ca1
 return sz(col) < m ? 2 : 1;</pre>
} // 996e
math/bit matrix.h
                                           2e3f
using ull = uint64 t;
// Matrix over Z 2 (bits and xor)
// TODO: arithmetic operations
struct BitMatrix {
 vector<ull> M:
 int rows, cols, stride;
 // Create matrix with n rows and m columns
 BitMatrix(int n = 0, int m = 0) {
  rows = n; cols = m;
  stride = (m+63)/64;
  M.resize(n*stride);
 } // 7ef0
 // Get pointer to bit-packed data of i-th row
 ull* row(int i) { return &M[i*stride]; }
 // Get value in i-th row and j-th column
 bool operator()(int i, int j) {
  return (row(i)[j/64] >> (j%64)) & 1;
 } // 28bd
 // Set value in i-th row and j-th column
 void set(int i, int j, bool val) {
  ull \&w = row(i)[j/64], m = 1ull << (j%64);
  if (val) w |= m;
  else w &= ~m;
 } // 98a8
}; // 4df7
math/crt.h
                                           8a85
using Pll = pair<11, 11>;
11 egcd(11 a, 11 b, 11& x, 11& y) {
 if (!a) return x=0, y=1, b;
 11 d = eqcd(b%a, a, y, x);
 x = b/a*v;
 return d;
} // 23c8
// Chinese Remainder Theoerem; time: O(lg lcm)
// Solves x = a.x \pmod{a.y}, x = b.x \pmod{b.y}
// Returns pair (x mod lcm, lcm(a.y, b.y))
```

```
// or (-1, -1) if there's no solution.
// WARNING: a.x and b.x are assumed to be
// in [0;a.y) and [0;b.y) respectively.
// Works properly if lcm(a.y, b.y) < 2^63.
Pll crt (Pll a, Pll b) {
 if (a.y < b.y) swap(a, b);</pre>
 11 x, y, g = egcd(a.y, b.y, x, y);
 11 c = b.x-a.x, d = b.y/g, p = a.y*d;
 if (c % g) return {-1, -1};
 11 s = (a.x + c/q*x % d * a.v) % p;
 return {s < 0 ? s+p : s, p};
} // 35a8
math/fft complex.h
                                            31ee
using dbl = double;
using cmpl = complex<dbl>;
// Default std::complex multiplication is slow.
// You can use this to achieve small speedup.
cmpl operator*(cmpl a, cmpl b) {
 dbl ax = real(a), ay = imag(a);
 dbl bx = real(b), by = imag(b);
 return {ax*bx-ay*by, ax*by+ay*bx};
} // 3b78
cmpl operator*=(cmpl& a, cmpl b) {return a=a*b;}
// Compute DFT over complex numbers; O(n lq n)
// Input size must be power of 2!
void fft (vector<cmpl>& a) {
 static vector<cmpl> w(2, 1);
 int n = sz(a);
 for (int k = sz(w); k < n; k *= 2) {
  w.resize(n);
  rep(i,0,k) w[k+i] = \exp(\text{cmpl}(0, M_PI*i/k));
 } // 92a9
 Vi rev(n);
 rep(i,0,n) rev[i] = (rev[i/2] | i*2*n) / 2;
 rep(i,0,n) if(i<rev[i]) swap(a[i],a[rev[i]]);
 for (int k = 1; k < n; k *= 2) {
  for (int i=0; i < n; i += k*2) rep(j, 0, k) {
    auto d = a[i+j+k] * w[j+k];
    a[i+j+k] = a[i+j] - d;
    a[i+j] += d;
  } // b389
 } // 84bf
} // adf8
// Convolve complex-valued a and b,
// store result in a; time: O(n lq n), 3x FFT
void convolve(vector<cmpl>& a, vector<cmpl> b) {
 int len = \max(sz(a) + sz(b) - 1, 0);
 int n = 1 << (32 - __builtin_clz(len));</pre>
 a.resize(n); b.resize(n);
 fft(a); fft(b);
 rep(i, 0, n) a[i] *= b[i] / dbl(n);
 reverse (a.begin()+1, a.end());
 fft(a);
 a.resize(len);
1 // 7987
// Convolve real-valued a and b, returns result
// time: O(n lq n), 2x FFT
// Rounding to integers is safe as long as
// (max coeff<sup>2</sup>) *n*log_2(n) < 9*10<sup>14</sup>
// (in practice 10^16 or higher).
vector<dbl> convolve (vector<dbl>& a,
              vector<dbl>& b) {
 int len = \max(sz(a) + sz(b) - 1, 0);
```

```
int n = 1 << (32 - __builtin_clz(len));</pre>
 vector<cmpl> in(n), out(n);
 rep(i, 0, sz(a)) in[i].real(a[i]);
 rep(i, 0, sz(b)) in[i].imag(b[i]);
 each(x, in) x \star = x;
 rep(i,0,n) out[i] = in[-i&(n-1)]-conj(in[i]);
 fft (out):
 vector<dbl> ret(len);
 rep(i, 0, len) ret[i] = imag(out[i]) / (n*4);
 return ret:
} // 19ed
constexpr 11 MOD = 1e9+7:
// High precision convolution of integer-valued
// a and b mod MOD; time: O(n lq n), 4x FFT
// Input is expected to be in range [0;MOD)!
// Rounding is safe if MOD*n*log_2(n) < 9*10^14
// (in practice 10^16 or higher).
vector<11> convMod(vector<11>& a.
            vector<11>& b) {
 vector<11> ret(sz(a) + sz(b) - 1);
 int n = 1 << (32 - __builtin_clz(sz(ret)));</pre>
 11 cut = 11 (sqrt (MOD))+1;
 vector<cmpl> c(n), d(n), g(n), f(n);
 rep(i, 0, sz(a))
  c[i] = {dbl(a[i]/cut), dbl(a[i]%cut)};
 rep(i, 0, sz(b))
  d[i] = {dbl(b[i]/cut), dbl(b[i]%cut)};
 fft(c); fft(d);
 rep(i, 0, n) {
  int j = -i & (n-1);
  f[j] = (c[i] + conj(c[j])) * d[i] / (n*2.0);
  a[j] =
   (c[i]-conj(c[j])) * d[i] / cmpl(0, n*2);
 1 // e877
 fft(f); fft(a);
 rep(i, 0, sz(ret)) {
  11 t = llround(real(f[i])) % MOD * cut;
  t += llround(imag(f[i]));
  t = (t + llround(real(g[i]))) % MOD * cut;
  t = (t + llround(imag(g[i]))) % MOD;
  ret[i] = (t < 0 ? t + MOD : t);
 } // e75d
 return ret:
} // 513f
math/fft mod.h
                                           17aa
// Number Theoretic Tranform (NTT)
// For functions below you can choose 2 params:
// 1. M - prime modulus that MUST BE of form
         a*2^k+1, computation is done in Z M
// 2. R - generator of Z M
// Modulus often seen on Codeforces:
// M = (119<<23)+1, R = 62; M is 998244353
// Parameters for 11 computation with CRT:
//M = (479 << 21) + 1, R = 62; M is > 10^9
// M = (483 << 21) + 1, R = 62; M is > 10^9
11 modPow(11 a, 11 e, 11 m) {
11 t = 1 % m;
 while (e) {
  if (e % 2) t = t*a % m;
```

```
e /= 2; a = a*a % m;
 } // 66ca
 return t:
1 // 1973
// Compute DFT over Z_M with generator R.
// Input size must be power of 2; O(n lq n)
// Input is expected to be in range [0; MOD)!
// dit == true <=> inverse transform * 2^n
                    (without normalization)
template<11 M, 11 R, bool dit>
void ntt(vector<ll>& a) {
 static vector<11> w(2, 1);
 int n = sz(a):
 for (int k = sz(w); k < n; k *= 2) {
  w.resize(n, 1);
  11 c = modPow(R, M/2/k, M);
  if (dit) c = modPow(c, M-2, M);
   rep(i, k+1, k*2) w[i] = w[i-1]*c % M;
 1 // 0d98
 for (int t = 1; t < n; t *= 2) {
  int k = (dit ? t : n/t/2);
  for (int i=0; i < n; i += k*2) rep(j,0,k) {
    11 \&c = a[i+j], \&d = a[i+j+k];
    ll e = w[j+k], f = d;
    d = (dit ? c - (f=f*e%M) : (c-f)*e%M);
    if (d < 0) d += M;
    if ((c += f) >= M) c -= M;
  } // e4a6
} // 8d38
} // 01f5
// Convolve a and b mod M (R is generator),
// store result in a; time: O(n lg n), 3x NTT
// Input is expected to be in range [0;MOD)!
template<11 M = (119<<23)+1, 11 R = 62>
void convolve(vector<11>& a, vector<11> b) {
 int len = \max(sz(a) + sz(b) - 1, 0);
 int n = 1 << (32 - __builtin_clz(len));</pre>
 ll t = modPow(n, M-2, M);
 a.resize(n); b.resize(n);
 ntt < M, R, 0 > (a); ntt < M, R, 0 > (b);
 rep(i, 0, n) a[i] = a[i] *b[i] % M * t % M;
 ntt<M,R,1>(a);
 a.resize(len);
1 // 4b4d
ll egcd(ll a, ll b, ll& x, ll& y) {
if (!a) return x=0, y=1, b;
11 d = egcd(b%a, a, y, x);
x = b/a*v;
return d:
} // 23c8
// Convolve a and b with 64-bit output,
// store result in a; time: O(n lg n), 6x NTT
// Input is expected to be non-negative!
void convLong(vector<11>& a, vector<11> b) {
 const 11 M1 = (479 << 21) +1, M2 = (483 << 21) +1;
 const 11 MX = M1 * M2, R = 62;
 vector<11> c = a, d = b;
 each(k, a) k %= M1; each(k, b) k %= M1;
 each(k, c) k %= M2; each(k, d) k %= M2;
 convolve<M1, R>(a, b);
 convolve<M2, R>(c, d);
 11 x, y; egcd (M1, M2, x, y);
 rep(i, 0, sz(a)) {
```

```
if ((a[i] %= MX) < 0) a[i] += MX;</pre>
} // 2279
} // ef93
math/fwht.h
                                           3e6f
// Fast Walsh-Hadamard Transform; O(n lg n)
// Input must be power of 2!
// Uncommented version is for XOR.
// OR version is equivalent to sum-over-subsets
// (Zeta transform, inverse is Moebius).
// AND version is same as sum-over-supersets.
// TESTED ON RANDS
template < bool inv. class T>
void fwht (vector<T>& b) {
 for (int s = 1; s < sz(b); s *= 2) {
  for (int i = 0; i < sz(b); i += s*2) {
    rep(j, i, i+s) {
     auto &x = b[j], &y = b[j+s];
     tie(x, y) =
      mp(x+y, x-y);
                                //XOR
     // inv ? mp(x-y, y) : mp(x+y, y); //AND
     // inv ? mp(x, y-x) : mp(x, x+y); //OR
    } // eea9
  1 // a3d5
 1 // 95ed
 // ONLY FOR XOR:
 if (inv) each(e, b) e /= sz(b);
1 // 0779
// Compute convolution of a and b such that
// ans[i#i] += a[i]*b[i], where # is OR, AND
// or XOR, depending on FWHT version.
// Stores result in a; time: O(n lg n)
// Both arrays must be of same size = 2^n!
template<class T>
void bitConv(vector<T>& a, vector<T> b) {
 fwht<0>(a);
 fwht<0>(b):
 rep(i, 0, sz(a)) a[i] *= b[i];
 fwht<1>(a);
} // 7b82
math/gauss.h
                                           7f0b
// Solve system of linear equations; O(n^2*m)
// - A - extended matrix, rows are equations,
         columns are variables.
         m-th column is equation result
         (A[i][j] - i-th row and j-th column)
// - ans - output for variables values
// - m - variable count
// Returns 0 if no solutions found, 1 if one,
// 2 if more than 1 solution exist.
int gauss (vector < vector < double >> & A.
      vector<double>& ans, int m) {
 Vi col;
 ans.assign(m, 0);
 rep(i, 0, sz(A)) {
  int c = 0;
  while (c <= m && !cmp(A[i][c], 0)) c++;</pre>
  // For Zp:
  //while (c <= m && !A[i][c].x) c++;
  if (c >= m) {
    if (c == m) return 0;
    continue;
  } // a6bb
  rep(k, i+1, sz(A)) {
```

a[i] += (c[i]-a[i]) \*x % M2 \* M1;

```
auto mult = A[k][c] / A[i][c];
   rep(j, 0, m+1) A[k][j] -= A[i][j] *mult;
  } // 8dd5
  swap(A[i], A[sz(col)]);
  col.pb(c);
 } // ea2c
 for (int i = sz(col); i--;) {
  ans [col[i]] = A[i][m] / A[i][col[i]];
  rep(k, 0, i)
   A[k][m] = ans[col[i]] * A[k][col[i]];
 } // 31b9
 return sz(col) < m ? 2 : 1;</pre>
} // Ob76
                                            9bf7
math/matrix.h
#include "modular.h"
using Row = vector<Zp>;
using Matrix = vector<Row>;
// Create n x n identity matrix
Matrix ident(int n) {
Matrix ret(n, Row(n));
 rep(i, 0, n) ret[i][i] = 1;
 return ret;
1 // adld
// Add matrices
Matrix& operator+= (Matrix& 1, const Matrix& r) {
 rep(i, 0, sz(l)) rep(k, 0, sz(l[0]))
  l[i][k] += r[i][k];
 return 1;
1 // b6bf
Matrix operator+ (Matrix 1, const Matrix& r) {
 return 1 += r;
} // d9b3
// Subtract matrices
Matrix& operator -= (Matrix& 1, const Matrix& r) {
 rep(i, 0, sz(l)) rep(k, 0, sz(l[0]))
  l[i][k] = r[i][k];
 return 1;
} // 90a1
Matrix operator- (Matrix 1, const Matrix& r) {
 return 1 -= r;
1 // dc4f
// Multiply matrices
Matrix operator* (const Matrix& 1,
           const Matrix& r) {
 Matrix ret(sz(1), Row(sz(r[01)));
 rep(i, 0, sz(l)) rep(j, 0, sz(r[0]))
  rep(k, 0, sz(r))
   ret[i][j] += l[i][k] * r[k][j];
 return ret;
Matrix& operator *= (Matrix& 1, const Matrix& r) {
 return 1 = 1*r;
1 // da8a
// Square matrix power; time: O(n^3 * 1g e)
Matrix pow (Matrix a, ll e) {
 Matrix t = ident(sz(a));
 while (e) {
  if (e % 2) t *= a;
  e /= 2; a *= a;
 } // 4400
 return t;
} // 65ea
```

```
// Transpose matrix
Matrix transpose (const Matrix & m) {
Matrix ret(sz(m[0]), Row(sz(m)));
 rep(i, 0, sz(m)) rep(j, 0, sz(m[0]))
 ret[i][i] = m[i][i];
 return ret:
} // 5650
// Transform matrix to echelon form
// and compute its determinant sign and rank.
int echelon (Matrix& A, int& sign) { // O(n^3)
int rank = 0;
 sign = 1:
 rep(c, 0, sz(A[0])) {
  if (rank >= sz(A)) break;
  rep(i, rank+1, sz(A)) if (A[i][c].x) {
   swap(A[i], A[rank]);
    sign *=-1;
   break:
  } // f98a
  if (A[rank][c].x) {
   rep(i, rank+1, sz(A)) {
     auto mult = A[i][c] / A[rank][c];
     rep(j, 0, sz(A[0]))
      A[i][j] -= A[rank][j] * mult;
   } // f519
   rank++;
  } // 4cd8
 } // 36e9
 return rank:
} // 6882
// Compute matrix rank; time: O(n^3)
#define rank rank_
int rank(Matrix A) {
int s; return echelon(A, s);
// Compute square matrix determinant; O(n^3)
Zp det (Matrix A) {
int s; echelon (A, s);
 Zp ret = s:
 rep(i, 0, sz(A)) ret \star= A[i][i];
return ret:
} // b252
// Invert square matrix if possible; O(n^3)
// Returns true if matrix is invertible.
bool invert (Matrix& A) {
 int s, n = sz(A);
 rep(i, 0, n) A[i].resize(n*2), A[i][n+i] = 1;
 echelon(A, s);
 for (int i = n; i--;) {
  if (!A[i][i].x) return 0;
  auto mult = A[i][i].inv();
  each(k, A[i]) k *= mult;
  rep(k, 0, i) rep(j, 0, n)
   A[k][n+j] -= A[i][n+j]*A[k][i];
 1 // 1e97
 each (r, A) r.erase (r.begin(), r.begin()+n);
 return 1:
1 // 65b9
math/miller rabin.h
                                           7005
#include "modular64.h"
// Miller-Rabin primality test
// time O(k*lg^2 n), where k = number of bases
// Deterministic for p <= 10^9
// constexpr 11 BASES[] = {
```

```
336781006125, 9639812373923155
// }; // d41d
// Deterministic for p <= 2^64
constexpr 11 BASES[] = {
2,325,9375,28178,450775,9780504,1795265022
}; // b8e0
bool isPrime(ll p) {
if (p <= 2) return p == 2;
 if (p%2 == 0) return 0;
 11 d = p-1, t = 0;
 while (d%2 == 0) d /= 2, t++;
 each(a, BASES) if (a%p) {
  // 11 a = rand() % (p-1) + 1;
  11 b = modPow(a%p, d, p);
  if (b == 1 \mid | b == p-1) continue:
  rep(i, 1, t)
   if ((b = modMul(b, b, p)) == p-1) break;
  if (b != p-1) return 0;
 } // 9342
 return 1;
} // bec2
math/modiny precompute.h
                                           2882
constexpr 11 MOD = 234567899;
vector<ll> modInv(MOD); // You can lower size
// Precompute modular inverses; time: O(MOD)
void initModInv() {
modInv[1] = 1;
 rep(i, 2, sz(modInv)) modInv[i] =
  (MOD - (MOD/i) * modInv[MOD%i]) % MOD;
} // 22c1
math/modular.h
                                           71e5
// Modulus often seen on Codeforces:
constexpr int MOD = 998244353;
// Some big prime: 15*(1<<27)+1 ~ 2*10^9
11 modInv(11 a, 11 m) { // a^(-1) mod m
if (a == 1) return 1;
return ((a - modInv(m%a, a))*m + 1) / a;
} // c437
11 modPow(11 a, 11 e, 11 m) { // a^e mod m
11 t = 1 % m;
 while (e) {
  if (e % 2) t = t*a % m;
  e /= 2; a = a*a % m;
 1 // 66ca
 return t;
1 // 1973
// Wrapper for modular arithmetic
struct Zp {
11 x: // Contained value, in range [0:MOD-1]
 Zp() : x(0) \{ \}
 Zp(11 a) : x(a\%MOD) { if (x < 0) x += MOD; }
 #define OP(c,d) Zp& operator c##=(Zp r) {
      x = x d; return *this; } \
    Zp operator c(Zp r) const { \
      Zp t = *this; return t c##= r; } // e986
 OP(+, +r.x - MOD*(x+r.x >= MOD));
 OP (-, -r.x + MOD*(x-r.x < 0));
 OP(*, *r.x % MOD);
 OP(/, *r.inv().x % MOD);
 Zp operator-()
  const { Zp t; t.x = MOD-x; return t; }
```

```
8
 // For composite modulus use modInv, not pow
 Zp inv() const { return pow(MOD-2); }
 Zp pow(ll e) const{ return modPow(x,e,MOD); }
 void print() { cerr << x; } // For deb()</pre>
1: // 407f
// Extended Euclidean Algorithm
ll egcd(ll a, ll b, ll& x, ll& y) {
 if (!a) return x=0, y=1, b;
 11 d = egcd(b%a, a, y, x);
 x = b/a*v;
 return d;
1 // 23c8
math/modular64.h
                                            4b73
// Modular arithmetic for modulus < 2^62
11 modAdd(11 x, 11 v, 11 m) {
x += v;
 return x < m ? x : x-m;
1 // b653
11 modSub(11 x, 11 v, 11 m) {
x -= y;
 return x \ge 0 ? x : x+m;
1 // b073
// About 4x slower than normal modulo
ll modMul(ll a, ll b, ll m) {
 11 c = 11 ((long double) a * b / m);
 11 r = (a*b - c*m) % m;
 return r < 0 ? r+m : r;
} // 1815
11 modPow(11 x, 11 e, 11 m) {
11 t = 1;
 while (e) {
  if (e \& 1) t = modMul(t, x, m);
  e >>= 1;
  x = modMul(x, x, m);
 } // bd61
 return t;
} // c8ba
math/modular generator.h
                                            845b
#include "modular.h" // modPow
// Get unique prime factors of n; O(sqrt n)
vector<ll> factorize(11 n) {
 vector<11> fac;
 for (ll i = 2; i*i <= n; i++) {
  if (n\%i == 0) {
    while (n\%i == 0) n /= i;
    fac.pb(i);
  } // 6069
 1 // a0cc
 if (n > 1) fac.pb(n);
 return fac;
1 // 4a2a
// Find smallest primitive root mod n:
// time: O(sqrt(n) + q*log^2 n)
// Returns -1 if generator doesn't exist.
// For n \le 10^7 smallest generator is \le 115.
// You can use faster factorization algorithm
// to get rid of sgrt(n). [UNTESTED]
ll generator(11 n) {
 if (n \le 1 \mid | (n > 4 \&\& n%4 == 0)) return -1;
 vector<ll> fac = factorize(n);
```

if (sz(fac) > (fac[0] == 2)+1) return -1;

} // f83f

}\_// 7a97

```
math/montgomery.h
                                                                                                a4ba
 11 phi = n:
 each (p, fac) phi = phi / p \star (p-1);
                                                    #include "modular.h" // modInv
 fac = factorize (phi);
                                                    // Montgomery modular multiplication
 for (ll q = 1;; q++) if (__qcd(q, n) == 1) {
                                                    // MOD < MG MULT, gcd (MG MULT, MOD) must be 1
  each (f, fac) if (modPow(q, phi/f, n) == 1)
                                                    // Don't use if modulo is constexpr: UNTESTED
   goto nxt;
  return a:
                                                    constexpr 11 MG_SHIFT = 32;
                                                    constexpr ll MG MULT = 1LL << MG SHIFT;</pre>
  nxt::
 } // db24
                                                    constexpr 11 MG MASK = MG MULT - 1;
                                                    const 11 MG_INV = MG_MULT-modInv(MOD, MG_MULT);
} // 7641
                                                    // Convert to Montgomery form
math/modular log.h
                                           ac62
                                                    11 MG(11 x) { return (x*MG MULT) % MOD; }
#include "modular.h" // modInv
                                                    // Montgomery reduction
// Baby-step giant-step algorithm; O(sqrt(p))
                                                    // redc(mg * mg) = Montgomery-form product
// Finds smallest x such that a^x = b \pmod{p}
                                                    ll redc(ll x) {
// or returns -1 if there's no solution.
                                                    11 g = (x * MG INV) & MG MASK;
ll dlog(ll a, ll b, ll p) {
                                                     x = (x + q*MOD) >> MG_SHIFT;
 int m = int (min(ll(sqrt(p))+2, p-1));
                                                     return (x >= MOD ? x-MOD : x);
 unordered_map<11, int> small;
                                                    } // d0f5
 11 t = 1:
                                                    math/nimber.h
                                                                                                474f
 rep(i, 0, m) {
                                                    // Nimbers are defined as sizes of Nim heaps.
  int& k = small[t];
                                                    // Operations on nimbers are defined as:
  if (!k) k = i+1;
                                                    // a+b = mex(\{a'+b : a' < a\} u \{a+b' : b' < b\})
  t = t*a % p;
                                                    // ab = mex(\{a'b+ab'+a'b' : a' < a, b' < b\})
 } // f1d0
                                                    // Nimbers smaller than M = 2^2 k form a field.
 t = modInv(t, p);
                                                    // Addition is equivalent to xor, meanwhile
                                                    // multiplication can be evaluated
 rep(i, 0, m) {
                                                    // in O(lg^2 M) after precomputing.
  int j = small[b];
  if (j) return i*ll(m) + j - 1;
                                                    using ull = uint64 t;
  b = b * t % p;
                                                    ull nbuf[64][64]; // Nim-products for 2^i * 2^j
 } // c7ed
                                                    // Multiply nimbers; time: O(la^2 M)
 return -1:
                                                    // WARNING: Call initNimMul() before using.
} // 5c26
                                                    ull nimMul(ull a, ull b) {
                                                    ull ret = 0:
math/modular sgrt.h
                                           db16
                                                     for (ull s = a; s; s &= (s-1))
#include "modular.h" // modPow
                                                      for (ull t = b; t; t &= (t-1))
                                                       ret ^= nbuf[__builtin_ctzll(s)]
// Tonelli-Shanks algorithm for modular sqrt
                                                               [ builtin ctzll(t)];
// modulo prime; O(lq^2 p), O(lq p) for most p
                                                     return ret:
// Returns -1 if root doesn't exists or else
                                                    } // 25be
// returns square root x (the other one is -x).
11 modSgrt(11 a, 11 p) {
                                                    // Initialize nim-products lookup table
                                                    void initNimMul() {
 if (a < 0) a += p;
                                                     rep(i, 0, 64)
 if (a <= 1) return a;</pre>
                                                      nbuf[i][0] = nbuf[0][i] = 1ull << i;
 if (modPow(a, p/2, p) != 1) return -1;
                                                     rep (b, 1, 64) rep (a, 1, b+1) {
 if (p%4 == 3) return modPow(a, p/4+1, p);
                                                      int i = 1 << (63 - __builtin_clzll(a));</pre>
                                                      int j = 1 << (63 - __builtin_clzll(b));</pre>
 11 s = p-1, n = 2;
                                                      ull t = nbuf[a-i][b-i];
 int r = 0, j;
                                                      if (i < j)
 while (s%2 == 0) s /= 2, r++;
                                                       t = nimMul(t, 1ull << i) << i;
 while (modPow(n, p/2, p) != p-1) n++;
                                                       t = nimMul(t, 1ull << (i-1))^ (t << i);
 ll x = modPow(a, (s+1)/2, p);
                                                      nbuf[a][b] = nbuf[b][a] = t;
 11 b = modPow(a, s, p), q = modPow(n, s, p);
                                                    } // ca24
 for (:: r = i) {
                                                   } // 1811
  11 t = b;
  for (j = 0; j < r && t != 1; j++)
                                                    // Compute a^e under nim arithmetic; O(lg^3 M)
   t = t * t % p;
                                                    // WARNING: Call initNimMul() before using.
                                                   ull nimPow(ull a, ull e) {
  if (!i) return x;
  ll gs = modPow(g, 1LL \ll (r-j-1), p);
                                                     ull t = 1:
                                                     while (e) {
  q = qs*qs % p;
                                                      if (e % 2) t = nimMul(t, a);
  x = x*gs % p;
  b = b*g % p;
                                                      e /= 2; a = nimMul(a, a);
```

} // da53

return t;

```
1 // c06c
// Compute inverse of a in 2^64 nim-field;
// time: 0(1g^3 M)
// WARNING: Call initNimMul() before using.
ull nimInv(ull a) {
return nimPow(a, ull(-2));
1 // c6d9
// If you need to multiply many nimbers by
// the same value you can use this to speedup.
// WARNING: Call initNimMul() before using.
struct NimMult {
ull M[64] = \{0\};
 // Initialize lookup; time: O(lg^2 M)
 NimMult(ull a) {
  for (ull t=a; t; t &= (t-1)) rep(i, 0, 64)
   M[i] ^= nbuf[ builtin ctzll(t)][i];
 } // ea88
 // Multiply by b; time: O(lq M)
 ull operator() (ull b) {
  ull ret = 0:
  for (ull t = b; t; t &= (t-1))
   ret ^= M[ builtin ctzll(t)];
  return ret;
 } // e480
}; // 1b80
math/phi large.h
                                           8703
#include "pollard rho.h"
// Compute Euler's totient of large numbers
// time: O(n^(1/4)) \leftarrow factorization
ll phi(ll n) {
each (p, factorize (n)) n = n / p.x * (p.x-1);
return n;
1 // 798e
math/phi precompute.h
                                           728b
Vi phi(1e7+1);
// Precompute Euler's totients; time: O(n lg n)
void calcPhi() {
iota(all(phi), 0);
 rep(i, 2, sz(phi)) if (phi[i] == i)
  for (int j = i; j < sz(phi); j += i)</pre>
   phi[j] = phi[j] / i * (i-1);
1 // 3c65
math/phi prefix sum.h
                                           a9e0
#include "phi precompute.h"
vector<11> phiSum; // [k] = sum \ from \ 0 \ to \ k-1
// Precompute Euler's totient prefix sums
// for small values; time: O(n lg n)
void calcPhiSum() {
 calcPhi();
 phiSum.resize(sz(phi)+1);
 rep(i, 0, sz(phi))
 phiSum[i+1] = phiSum[i] + phi[i];
// Get prefix sum of phi(0) + ... + phi(n-1).
// WARNING: Call calcPhiSum first!
// For n > 4*10^9, answer will overflow.
// If you wish to get answer mod M use
// commented lines.
11 getPhiSum(11 n) { // time: O(n^{2/3})
 static unordered map<11, 11> big;
 if (n < sz(phiSum)) return phiSum[n];</pre>
```

```
if (big.count(--n)) return big[n];
 11 ret = n*(n+1)/2;
 // 11 ret = (n%2 ? n%M * ((n+1)/2 % M)
                   : n/2%M * (n%M+1)) % M;
 for (11 s, i = 2; i \le n; i = s+1) {
  s = n / (n/i);
  ret -= (s-i+1) * getPhiSum(n/i+1);
  // ret -= (s-i+1) %M * getPhiSum(n/i+1) % M;
 } // e792
 // ret = (ret %M + M) % M;
 return big[n] = ret;
1 // 820b
math/pi large.h
                                            fcbd
constexpr int MAX P = 1e7;
vector<ll> pis, prl;
// Precompute prime counting function
// for small values; time: O(n lq lq n)
void initPi() {
 pis.assign (MAX_P+1, 1);
 pis[0] = pis[1] = 0;
 for (int i = 2; i*i <= MAX P; i++)
  if (pis[i])
    for (int j = i*i; j <= MAX_P; j += i)</pre>
    pis[j] = 0;
 rep(i, 1, sz(pis)) {
  if (pis[i]) prl.pb(i);
  pis[i] += pis[i-1];
 } // 0672
1 // 6d92
11 partial(11 x, 11 a) {
 static vector<unordered map<11, 11>> big;
 big.resize(sz(prl));
 if (!a) return (x+1) / 2:
 if (big[a].count(x)) return big[a][x];
 ll ret = partial(x, a-1)
  - partial (x / prl[a], a-1);
 return big[a][x] = ret;
1 // 774f
// Count number of primes <= x;
// \text{ time: } O(n^{(2/3)} * log(n)^{(1/3)})
// Set MAX P to be > sgrt(x) and call initPi
// before using!
ll pi(ll x) {
 static unordered_map<11, 11> big;
 if (x < sz(pis)) return pis[x];</pre>
 if (big.count(x)) return big[x];
 11 a = 0:
 while (prl[a]*prl[a]*prl[a]*prl[a] < x) a++;</pre>
 11 ret = 0, b = --a;
 while (++b < sz(prl) && prl[b]*prl[b] < x) {</pre>
  11 w = x / prl[b];
  ret -= pi(w);
  for (ll j = b; prl[j]*prl[j] <= w; j++)</pre>
    ret -= pi(w / prl[j]) - j;
 1 // a584
 ret += partial (x, a) + (b+a-1)*(b-a)/2;
 return big[x] = ret;
} // eald
math/pi large precomp.h
                                            7fc0
#include "sieve.h"
```

```
// Count primes in given interval
// using precomputed table.
// Set MAX_P to sqrt(MAX_N) and run sieve()!
// Precomputed table will contain N_BUCKETS
// elements - check source size limit.
constexpr 11 MAX N = 1e11+1;
constexpr 11 N_BUCKETS = 10000;
constexpr 11 BUCKET SIZE = (MAX N/N BUCKETS)+1;
constexpr ll precomputed[] = {/* ... */};
ll sieveRange(ll from, ll to) {
bitset < BUCKET_SIZE > elems;
 from = max(from, 2LL);
 to = max(from, to);
 each (p, primesList) {
  ll c = max((from+p-1) / p, 2LL);
  for (ll i = c*p; i < to; i += p)</pre>
   elems.set(i-from);
 } // a29f
 return to-from-elems.count();
// Run once on local computer to precompute
// table. Takes about 10 minutes for n = 1e11.
// Sanity check (for default params):
// 664579, 606028, 587253, 575795, ...
void localPrecompute() {
 for (11 i = 0; i < MAX N; i += BUCKET SIZE) {
  11 to = min(i+BUCKET SIZE, MAX N);
  cout << sieveRange(i, to) << ',' << flush;
 } // f6a7
 cout << endl;
} // 2b1e
// Count primes in [from; to) using table.
// O(N_BUCKETS + BUCKET_SIZE*lg lg n + sqrt(n))
ll countPrimes (ll from, ll to) {
11 bFrom = from/BUCKET SIZE+1,
   bTo = to/BUCKET SIZE;
 if (bFrom > bTo) return sieveRange(from, to);
 11 ret = accumulate (precomputed+bFrom,
              precomputed+bTo, 0);
 ret += sieveRange(from, bFrom*BUCKET SIZE);
 ret += sieveRange (bTo*BUCKET_SIZE, to);
 return ret:
} // cced
math/pollard_rho.h
                                           ef01
#include "modular64.h"
#include "miller_rabin.h"
using Factor = pair<11, int>;
void rho(vector<11>& out, 11 n) {
 if (n <= 1) return;</pre>
 if (isPrime(n)) out.pb(n);
 else if (n%2 == 0) rho(out,2), rho(out,n/2);
 else for (ll a = 2;; a++) {
  11 x = 2, y = 2, d = 1;
  while (d == 1) {
   x = modAdd (modMul(x, x, n), a, n);
   y = modAdd (modMul(y, y, n), a, n);
   y = modAdd(modMul(y, y, n), a, n);
   d = \underline{gcd(abs(x-y), n)};
  1 // 3378
  if (d != n) return rho(out,d), rho(out, n/d);
 } // 047e
} // ba89
// Pollard's rho factorization algorithm
// Las Vegas version; time: n^(1/4)
```

```
// Returns pairs (prime, power), sorted
vector<Factor> factorize(ll n) {
vector<Factor> ret;
 vector<11> raw;
 rho(raw, n);
 sort (all (raw));
 each(f, raw) {
  if (ret.empty() | ret.back().x != f)
   ret.pb({ f, 1 });
   ret.back().y++;
 } // 2ab1
 return ret;
} // 471c
math/polynomial.h
                                           c486
#include "modular.h"
#include "fft mod.h"
using Poly = vector<Zp>;
// Cut off trailing zeroes; time: O(n)
void norm(Poly& P) {
while (!P.empty() && !P.back().x)
  P.pop_back();
} // 8a8a
// Evaluate polynomial at x; time: O(n)
Zp eval (const Poly& P, Zp x) {
 Zp n = 0, y = 1;
 each (a, P) n += a*y, y *= x;
 return n;
} // d865
// Add polynomial; time: O(n)
Poly& operator+= (Poly& 1, const Poly& r) {
1.resize(max(sz(1), sz(r)));
 rep(i, 0, sz(r)) l[i] += r[i];
 norm(1);
 return 1;
} // 656e
Poly operator+ (Poly 1, const Poly& r) {
return 1 += r;
} // d9b3
// Subtract polynomial; time: O(n)
Poly& operator = (Poly& 1, const Poly& r) {
1.resize(max(sz(1), sz(r)));
 rep(i, 0, sz(r)) l[i] -= r[i];
 norm(1);
 return 1;
} // c68b
Poly operator-(Poly 1, const Poly& r) {
return 1 -= r:
// Multiply by polynomial; time: O(n lg n)
Polv& operator *= (Polv& 1, const Polv& r) {
if (min(sz(1), sz(r)) < 50) {
  // Naive multiplication
  Polv P(sz(1)+sz(r));
  rep(i, 0, sz(l)) rep(j, 0, sz(r))
   P[i+j] += l[i]*r[j];
  l.swap(P);
 } else {
  // FFT multiplication
  vector<ll> a, b;
  each(k, l) a.pb(k.x);
  each (k, r) b.pb (k.x);
  // Choose appropriate convolution method,
  // see fft_mod.h and fft_complex.h
```

```
convolve<MOD, 62>(a, b);
  l.assign(all(a));
 } // f730
 norm(1);
 return 1;
} // 28de
Poly operator* (Poly 1, const Poly& r) {
return 1 *= r;
} // 2de3
// Derivate polynomial; time: O(n)
Poly derivate (Poly P) {
if (!P.empty()) {
  rep(i, 1, sz(P)) P[i-1] = P[i] * i;
  P.pop_back();
} // bd78
 return P;
} // c6c5
// Integrate polynomial; time: O(n)
Poly integrate (Poly P) {
if (!P.empty()) {
  P.pb(0);
  for (int i = sz(P); --i;) P[i] = P[i-1]/i;
  P[0] = 0;
 } // eec1
 return P;
} // e2f3
// Compute inverse series mod x^n; O(n lq n)
Polv invert (const Polv& P, int n) {
 assert(!P.empty() && P[0].x != 0);
Poly tmp, ret = \{P[0].inv()\};
 for (int i = 1; i < n; i *= 2) {
  tmp.clear();
  rep(j, 0, min(i*2, sz(P))) tmp.pb(-P[j]);
  tmp *= ret:
  tmp[0] += 2;
  ret *= tmp;
  ret.resize(i*2);
 } // 139b
 ret.resize(n);
return ret;
} // 4d3e
// Floor division by polynomial; O(n lg n)
Poly operator/(Poly 1, Poly r) {
norm(1); norm(r);
 int d = sz(1) - sz(r) + 1;
 if (d <= 0) return {};</pre>
 reverse (all(1));
 reverse (all(r));
 l.resize(d);
 l \star = invert(r, d);
 l.resize(d);
 reverse (all(1));
 return 1;
} // d4a4
Poly& operator/=(Poly& 1, const Poly& r) {
return 1 = 1/r;
} // e12e
// Compute modulo by polynomial; O(n lg n)
Poly operator% (const Poly& 1, const Poly& r) {
return 1 - r*(1/r);
} // 4fc8
Poly& operator%=(Poly& 1, const Poly& r) {
return 1 -= r*(1/r);
} // 80bb
```

```
// time: O(n lg^2 n)
Poly eval (const Poly P, Poly points) {
 int len = 1;
 while (len < sz(points)) len *= 2;
 vector<Poly> tree(len*2, {1});
 rep(i, 0, sz(points))
  tree[len+i] = \{-points[i], 1\};
 for (int i = len; --i;)
  tree[i] = tree[i\star2] \star tree[i\star2+1];
 tree[0] = P;
 rep(i, 1, len*2)
  tree[i] = tree[i/2] % tree[i];
 rep(i, 0, sz(points)) {
  auto& vec = tree[len+i];
  points[i] = vec.empty() ? 0 : vec[0];
 } // c1c2
 return points;
} // 69b0
// Given n points (x, f(x)) compute n-1-degree
// polynomial f that passes through them;
// time: O(n lg^2 n)
// For O(n^2) version see polynomial interp.h.
Poly interpolate (const vector < pair < Zp, Zp>>& P) {
 while (len < sz(P)) len *= 2;
 vector<Poly> mult(len*2, {1}), tree(len*2);
 rep(i, 0, sz(P))
  mult[len+i] = \{-P[i].x, 1\};
 for (int i = len; --i;)
  mult[i] = mult[i*2] * mult[i*2+1];
 tree[0] = derivate(mult[1]);
 rep(i, 1, len*2)
  tree[i] = tree[i/2] % mult[i];
 rep(i, 0, sz(P))
  tree[len+i][0] = P[i].y / tree[len+i][0];
 for (int i = len: --i:)
  tree[i] = tree[i*2]*mult[i*2+1]
       + mult[i*2]*tree[i*2+1];
 return tree[1];
} // b706
math/polynomial interp.h
                                            a4cc
// Interpolate set of points (i, vec[i])
// and return it evaluated at x; time: O(n)
template<class T>
T polyExtend (vector < T > & vec, T x) {
 int n = sz(vec);
 vector<T> fac(n, 1), suf(n, 1);
 rep(i, 1, n) fac[i] = fac[i-1] \star i;
 for (int i=n; --i;) suf[i-1] = suf[i] * (x-i);
 T pref = 1, ret = 0;
 rep(i, 0, n) {
  T d = fac[i] * fac[n-i-1] * ((n-i) *2*2-1);
  ret += vec[i] * suf[i] * pref / d;
  pref *= x-i;
 } // 681d
 return ret;
} // dd92
// Given n points (x, f(x)) compute n-1-degree
// polynomial f that passes through them;
// time: O(n^2)
```

// Evaluate polynomial P in given points;

```
// For O(n lg^2 n) version see polynomial.h
template<class T>
vector<T> polyInterp (vector<pair<T, T>> P) {
 int n = sz(P);
 vector<T> ret(n), tmp(n);
 T last = 0:
 tmp[0] = 1;
 rep(k, 0, n-1) rep(i, k+1, n)
  P[i].y = (P[i].y-P[k].y) / (P[i].x-P[k].x);
 rep(k, 0, n) rep(i, 0, n) {
  ret[i] += P[k].y \star tmp[i];
  swap(last, tmp[i]);
  tmp[i] = last * P[k].x;
 } // af1c
 return ret;
1 // 7c2c
                                           3f3d
math/sieve.h
constexpr int MAX_P = 1e6;
bitset<MAX_P+1> primes;
Vi primesList;
// Erathostenes sieve; time: O(n lg lg n)
void sieve() {
 primes.set();
 primes.reset(0);
 primes.reset (1);
 for (int i = 2; i*i <= MAX_P; i++)</pre>
  if (primes[i])
   for (int j = i*i; j <= MAX_P; j += i)</pre>
     primes.reset(j);
 rep(i, 0, MAX_P+1) if (primes[i])
  primesList.pb(i);
} // d5ca
                                           312d
math/sieve factors.h
constexpr int MAX P = 1e6;
Vi factor (MAX_P+1);
// Erathostenes sieve with saving smallest
// factor for each number; time: O(n lg lg n)
void sieve() {
 for (int i = 2; i*i <= MAX P; i++)
  if (!factor[i])
   for (int i = i*i; i <= MAX P; i += i)</pre>
     if (!factor[j])
      factor[i] = i;
 rep(i, 0, MAX_P+1) if (!factor[i]) factor[i]=i;
1 // 82b6
// Factorize n <= MAX_P; time: O(lq n)</pre>
// Returns pairs (prime, power), sorted
vector<Pii> factorize(ll n) {
 vector<Pii> ret;
 while (n > 1) {
  int f = factor[n];
  if (ret.empty() || ret.back().x != f)
   ret.pb({ f, 1 });
  else
   ret.back().y++;
  n /= f;
 } // 664c
 return ret;
1 // bb65
math/sieve segmented.h
                                           849b
constexpr int MAX P = 1e9;
```

```
bitset<MAX_P/2+1> primes; // Only odd numbers
// Cache-friendly Erathostenes sieve
// ~1.5s on Intel Core i5 for MAX_P = 10^9
// Memory usage: MAX_P/16 bytes
void sieve() {
 constexpr int SEG SIZE = 1<<18;</pre>
 int pSqrt = int (sqrt (MAX_P)+0.5);
 vector<Pii> dels;
 primes.set();
 primes.reset(0);
 for (int i = 3; i <= pSqrt; i += 2) {</pre>
  if (primes[i/2]) {
   int j;
    for (j = i*i; j <= pSqrt; j += i*2)</pre>
     primes.reset(j/2);
    dels.pb(\{i, j/2\});
  } // 9e62
} // ff49
 for (int seg = pSgrt/2;
    seq <= sz(primes); seq += SEG_SIZE) {</pre>
  int lim = min(seg+SEG SIZE, sz(primes));
  each (d, dels) for (;d.y < lim; d.y += d.x)
   primes.reset(d.y);
} // 97ae
} // 6456
bool isPrime(int x) {
return x == 2 \mid \mid (x \cdot 2 \cdot 6 \cdot primes[x/2]);
1 // 422c
structures/bitset plus.h
                                            6737
// Undocumented std::bitset features:
// - Find first() - returns first bit = 1 or N
// - _Find_next(i) - returns first bit = 1
                      after i-th bit
                      or N if not found
// Bitwise operations for vector<bool>
// UNTESTED
#define OP(x) vector<bool>& operator x##=(
   vector<bool>& 1, const vector<bool>& r) {
  assert(sz(1) == sz(r));
  auto a = 1.begin(); auto b = r.begin();
  while (a<1.end()) *a._M_p++ x##= *b._M_p++; \
  return 1: } // f164
OP (&) OP (|) OP (^)
structures/fenwick tree.h
                                           b467
// Fenwick tree (BIT tree); space: O(n)
// Default version: prefix sums
struct Fenwick {
 using T = int;
 T ID = 0:
 T f (T a, T b) { return a+b; }
 vector<T> s;
 Fenwick(int n = 0) : s(n, ID) {}
 // A[i] = f(A[i], v); time: O(lg n)
 void modify(int i, T v) {
  for (; i < sz(s); i |= i+1) s[i]=f(s[i],v);
 } // a047
 // Get f(A[0], ..., A[i-1]); time: O(lg n)
 T query(int i) {
  T v = ID;
  for (; i > 0; i \le i - 1) v = f(v, s[i-1]);
  return v;
 } // 9810
```

```
// Find smallest i such that
 // f(A[0],...,A[i-1]) >= val; time: O(lg n)
 // Prefixes must have non-descreasing values.
 int lowerBound(T val) {
  if (val <= ID) return 0;</pre>
  int i = -1, mask = 1;
  while (mask \leq sz(s)) mask \star= 2;
  T \circ ff = TD:
  while (mask /= 2) {
   int k = mask+i;
   if (k < sz(s)) {
    T x = f(off, s[k]);
     if (val > x) i=k, off=x;
   } // de7f
  } // 929c
  return i+2;
} // 4be9
}; // 1470
structures/fenwick tree 2d.h 4945
// Fenwick tree 2D (BIT tree 2D); space: O(n*m)
// Default version: prefix sums 2D
// Change s to hashmap for O(q lg^2 n) memory
struct Fenwick2D {
using T = int;
 T ID = 0:
 T f (T a, T b) { return a+b; }
 vector<T> s;
 int w, h;
 Fenwick2D (int n = 0, int m = 0)
 : s(n*m, ID), w(n), h(m) {}
 // A[i,j] = f(A[i,j], v); time: O(1g^2 n)
 void modify(int i, int j, T v) {
  for (; i < w; i |= i+1)
   for (int k = j; k < h; k = k+1)
     s[i*h+k] = f(s[i*h+k], v);
 } // d46b
 // Query prefix; time: O(lg^2 n)
 T query (int i, int j) {
  T v = ID;
  for (; i>0; i&=i-1)
   for (int k = j; k > 0; k &= k-1)
     v = f(v, s[i*h+k-h-1]);
  return v;
} // 08cf
}; // 36b4
structures/find union.h
                                           b4de
// Disjoint set data structure; space: O(n)
// Operations work in amortized O(alfa(n))
struct FAU {
 Vi G;
 FAU(int n = 0) : G(n, -1) {}
 // Get size of set containing i
 int size(int i) { return -G[find(i)]; }
 // Find representative of set containing i
 int find(int i) {
  return G[i] < 0 ? i : G[i] = find(G[i]);</pre>
 } // 5bc1
 // Union sets containing i and j
 bool join(int i, int j) {
  i = find(i); j = find(j);
  if (i == j) return 0;
```

```
if (G[i] > G[j]) swap(i, j);
  G[i] += G[j]; G[j] = i;
  return 1;
} // c721
}; // 62a4
structures/hull offline.h
                                           3030
constexpr 11 INF = 2e18;
// constexpr double INF = 1e30;
// constexpr double EPS = 1e-9;
// MAX of linear functions; space: O(n)
// Use if you add lines in increasing `a` order
// Default uncommented version is for int64
struct Hull {
 using T = 11; // Or change to double
 struct Line {
  Ta, b, end:
  T intersect (const Line& r) const {
    // Version for double:
    //if (r.a-a < EPS) return b>r.b?INF:-INF;
    //return (b-r.b) / (r.a-a);
    if (a==r.a) return b > r.b ? INF : -INF;
    11 u = b-r.b, d = r.a-a;
    return u/d + ((u^d) >= 0 || !(u%d));
  } // f27f
 }; // 10dc
 vector<Line> S:
 Hull() { S.pb({ 0, -INF, INF }); }
 // Insert f(x) = ax+b; time: amortized O(1)
 void push(T a, T b) {
  Line 1{a, b, INF};
  while (true) {
   T e = S.back().end=S.back().intersect(1);
   if (sz(S) < 2 \mid \mid S[sz(S)-2].end < e)
    break:
   S.pop_back();
  } // 044f
  S.pb(1);
 } // 978e
 // Query max(f(x) for each f): time: O(lg n)
 T query (T x) {
  auto t = *upper_bound(all(S), x,
   [](int l, const Line& r) {
     return 1 < r.end;</pre>
   }); // de77
  return t.a*x + t.b;
} // b8de
}; // 1d64
structures/hull online.h
                                           2a7b
constexpr 11 INF = 2e18:
// MAX of linear functions online; space: O(n)
struct Hull {
 static bool modeQ; // Toggles operator< mode</pre>
 struct Line (
  mutable 11 a, b, end;
  ll intersect (const Line& r) const {
   if (a==r.a) return b > r.b ? INF : -INF;
   11 u = b-r.b, d = r.a-a;
   return u/d + ((u^d) >= 0 || !(u^d));
  } // f27f
  bool operator < (const Line& r) const {
```

return modeQ ? end < r.end : a < r.a;</pre>

```
} // cfab
 }; // 6046
 multiset<Line> S;
 Hull() { S.insert({ 0, -INF, INF }); }
 // Updates segment end
 bool update(multiset<Line>::iterator it) {
  auto cur = it++; cur->end = INF;
  if (it == S.end()) return false;
  cur->end = cur->intersect(*it);
  return cur->end >= it->end;
 } // 63b8
 // Insert f(x) = ax+b; time: O(lq n)
 void insert(ll a, ll b) {
  auto it = S.insert({ a, b, INF });
  while (update(it)) it = --S.erase(++it);
  rep(i, 0, 2)
   while (it != S.begin() && update(--it))
     update(it = --S.erase(++it));
 } // 4f69
 // Ouerv max(f(x) for each f): time: O(lg n)
 11 query(11 x) {
  mode0 = 1;
  auto l = *S.upper_bound({ 0, 0, x });
  mode0 = 0;
  return 1.a*x + 1.b;
 } // 7533
}; // 037e
bool Hull::mode() = false;
structures/max queue.h
                                           3e9e
// Queue with max query on contained elements
struct MaxOueue {
 using T = int:
 deque<T> Q, M;
 // Add v to the back; time: amortized O(1)
 void push(T v) {
  while (!M.empty() && M.back() < v)</pre>
   M.pop_back();
  M.pb(v); O.pb(v);
 1 // 57a2
 // Pop from the front; time: O(1)
 void pop() {
  if (M.front() == Q.front()) M.pop_front();
  Q.pop_front();
 } // 101c
 // Get max element value; time: O(1)
 T max() const { return M.front(); }
}; // b6c4
structures/pairing heap.h
                                          b2a7
// Pairing heap implementation; space O(n)
// Elements are stored in vector for faster
// allocation. It's MINIMUM queue.
// Allows to merge heaps in O(1)
template < class T, class Cmp = less < T>>
struct PHeap {
 struct Node {
  T val:
  int child{-1}, next{-1}, prev{-1};
  Node (T x = T()) : val(x) \{\}
 }; // 11ee
 using Vnode = vector < Node>;
 Vnode& M;
```

```
int root{-1};
 int unlink(int& i) {
  if (i >= 0) M[i].prev = -1;
  int x = i; i = -1;
  return x:
 } // d9f6
 void link(int host, int& i, int val) {
  if (i >= 0) M[i].prev = -1;
  i = val;
  if (i >= 0) M[i].prev = host;
 } // 47d5
 int merge(int 1, int r) {
  if (1 < 0) return r;
  if (r < 0) return 1;</pre>
  if (Cmp()(M[1].val, M[r].val)) swap(1, r);
  link(1, M[1].next, unlink(M[r].child));
  link(r, M[r].child, 1);
  return r:
 } // fc42
 int mergePairs(int v) {
  if (v < 0 | | M[v].next < 0) return v;</pre>
  int v2 = unlink(M[v].next);
  int v3 = unlink (M[v2].next);
  return merge(merge(v, v2), mergePairs(v3));
 } // 2eea
 // Initialize heap with given node storage
 // Just declare 1 Vnode and pass it to heaps
PHeap(Vnode& mem) : M(mem) {}
 // Add given key to heap, returns index; O(1)
 int push (const T& x) {
  int index = sz(M);
  M.emplace back(x);
  root = merge(root, index);
  return index:
 } // e744
 // Change key of i to smaller value; O(1)
 void decrease(int i, T val) {
  assert (!Cmp()(M[i].val, val));
  M[i].val = val:
  int prev = M[i].prev;
  if (prev < 0) return;
  auto& p = M[prev];
  link (prev, (p.child == i ? p.child
         : p.next), unlink(M[i].next));
  root = merge(root, i);
 } // 1a67
 bool empty() { return root < 0; }</pre>
 const T& top() { return M[root].val; }
 // Merge with other heap. Must use same vec.
 void merge(PHeap& r) { // time: O(1)
  assert (&M == &r.M);
  root = merge (root, r.root); r.root = -1;
 1 // 9623
 // Remove min element; time: O(lg n)
 void pop() {
  root = mergePairs (unlink (M[root].child));
} // 5b13
}; // 09f3
```

```
structures/rmg.h
                                          4551
// Range Minimum Query; space: O(n lg n)
struct RMQ {
using T = int;
 T ID = INT_MAX;
 Tf(Ta, Tb) { return min(a, b); }
 vector<vector<T>>> s;
 // Initialize RMO structure; time: O(n lq n)
 RMQ (const vector<T>& vec = {}) {
  s = \{vec\};
  for (int h = 1; h <= sz(vec); h *= 2) {
   s.emplace back();
   auto& prev = s[sz(s)-2];
   rep(i, 0, sz(vec)-h*2+1)
    s.back().pb(f(prev[i], prev[i+h]));
 1 // cf67
 // Query f(s[b], ..., s[e-1]); time: O(1)
 T query (int b, int e) {
  if (b >= e) return ID;
  int k = 31 - __builtin_clz(e-b);
  return f(s[k][b], s[k][e - (1<<k)]);
} // caaa
}; // e694
structures/segtree config.h 7ef8
// Segment tree configurations to be used
// in segtree_general and segtree_persistent.
// See comments in TREE PLUS version
// to understand how to create custom ones.
// Capabilities notation: (update; query)
#if TREE_PLUS // (+; sum, max, max count)
 // time: O(lq n) [UNTESTED]
 using T = int; // Data type for update
           // operations (lazy tag)
           // Neutral value for
           // updates and lazv tags
 // This structure keeps aggregated data
 struct Agg {
  // Aggregated data: sum, max, max count
  // Default values should be neutral
  // values, i.e. "aggregate over empty set"
  T sum{0}, vMax{INT_MIN}, nMax{0};
  // Initialize as leaf (single value)
  void leaf() { sum = vMax = 0; nMax = 1; }
  // Combine data with aggregated data
  // from node to the right
  void merge (const Agg& r) {
   if (vMax < r.vMax) nMax = r.nMax;</pre>
   else if (vMax == r.vMax) nMax += r.nMax;
    vMax = max(vMax, r.vMax);
    sum += r.sum;
  1 // 8850
  // Apply update provided in `x`:
  // - update aggregated data
  // - update lazy tag `lazy`
  // - 'size' is amount of elements
  // - return 0 if update should branch
      (to be used in "segement tree beats")
  // - if you change value of `x` changed
      value will be passed to next node
  // to the right during updates
  bool apply (T& lazy, T& x, int size) {
   lazy += x;
```

```
sum += x*size:
   vMax += x;
   return 1:
 } // 4858
}; // 9bf5
#elif TREE_MAX // (max; max, max count)
// time: O(lg n) [UNTESTED]
using T = int;
T ID = INT MIN;
struct Agg {
  // Aggregated data: max value, max count
  T vMax{INT_MIN}, nMax{0};
  void leaf() { vMax = 0; nMax = 1; }
  void merge(const Agg& r) {
   if (vMax < r.vMax) nMax = r.nMax;</pre>
   else if (vMax == r.vMax) nMax += r.nMax;
   vMax = max(vMax, r.vMax);
  } // f56b
  bool apply (T& lazy, T& x, int size) {
   if (vMax <= x) nMax = size;</pre>
   lazy = max(lazy, x);
   vMax = max (vMax, x);
   return 1;
 } // 8bd5
}; // 15b6
#elif TREE SET // (=; sum, max, max count)
// time: O(lq n) [UNTESTED]
// Set ID to some unused value.
using T = int;
T ID = INT MIN:
struct Agg {
  // Aggregated data: sum, max, max count
  T sum{0}, vMax{INT MIN}, nMax{0};
  void leaf() { sum = vMax = 0; nMax = 1; }
  void merge(const Agg& r) {
   if (vMax < r.vMax) nMax = r.nMax;</pre>
   else if (vMax == r.vMax) nMax += r.nMax;
   vMax = max(vMax, r.vMax);
   sum += r.sum;
  1 // 8850
  bool apply (T& lazy, T& x, int size) {
   lazv = x;
   sum = x*size:
   vMax = x;
   nMax = size:
   return 1:
 1 // 845b
}; // 7488
#elif TREE_BEATS // (+, min; sum, max)
// time: amortized O(lg n) if not using +
          amortized O(lg^2 n) if using +
// Lazy tag is pair (add, min).
// To add x: run update with {x, INT MAX},
// to min x: run update with \{0, x\}.
// When both parts are provided addition
// is applied first, then minimum.
using T = Pii;
T ID = \{0, INT_MAX\};
struct Agg {
  // Aggregated data: max value, max count,
                       second max value, sum
  int vMax{INT_MIN}, nMax{0}, max2{INT_MIN};
  int sum{0};
  void leaf() { sum = vMax = 0; nMax = 1; }
```

12

max2 = vMax:

void merge(const Agg& r) {

if (r.vMax > vMax) {

```
13
```

```
int m = (b+e) / 2;
     vMax = r.vMax;
                                                     push(i, e-b);
     nMax = r.nMax;
                                                     val = update(vb, ve, val, i*2, b, m);
   } else if (r.vMax == vMax) {
                                                     val = update(vb, ve, val, i*2+1, m, e);
    nMax += r.nMax;
                                                      (agg[i] = agg[i*2]).merge(agg[i*2+1]);
   } else if (r.vMax > max2) {
                                                     return val;
    max2 = r.vMax;
                                                    } // aa8e
   } // b074
   max2 = max(max2, r.max2);
                                                    // Query interval [vb;ve); time: O(lg n)
                                                    Agg query (int vb, int ve, int i = 1,
   sum += r.sum;
                                                          int b = 0, int e = -1) {
  } // 3124
                                                     if (e < 0) e = len;</pre>
  bool apply (T& lazy, T& x, int size) {
                                                     if (vb >= e || b >= ve) return {};
   if (max2 != INT_MIN && max2+x.x >= x.y)
                                                     if (b >= vb && e <= ve) return agg[i];</pre>
    return 0;
                                                     int m = (b+e) / 2;
   lazy.x += x.x;
                                                     push(i, e-b);
   sum += x.x*size;
                                                     Agg t = query (vb, ve, i*2, b, m);
   vMax += x.x;
                                                     t.merge(query(vb, ve, i*2+1, m, e));
   if (\max 2 != INT MIN) \max 2 += x.x;
                                                     return t:
   if (x.y < vMax) {
                                                    } // lale
    sum -= (vMax-x.y) * nMax;
                                                   }; // db5c
    vMax = x.y;
                                                   structures/segtree persist.h dcfc
   } // 7025
   lazy.y = vMax;
                                                   // Highly configurable (interval; interval)
   return 1;
                                                   // persistent segment tree;
  } // fe0c
                                                   // space: O(queries lg n) [UNTESTED]
 1: // 2924
                                                   // First tree version number is 0.
#endif
                                                   struct SegTree {
                                                    // Choose/write configuration
structures/segtree general.h 725a
                                                    #include "segtree config.h"
                                                    vector<Agg> agg; // Aggregated data for nodes
// Highly configurable statically allocated
                                                    vector<T> lazy; // Lazy tags for nodes
// (interval; interval) segment tree;
                                                    vector<bool> cow; // Copy children on push?
// space: O(n) [UNTESTED]
struct SegTree {
                                                                 // Children links
                                                    Vi L, R;
 // Choose/write configuration
                                                    int len{1};
                                                                // Number of leaves
 #include "seatree config.h"
                                                    // Initialize tree for n elements; O(lq n)
 // Root node is 1, left is i*2, right i*2+1
                                                    SegTree(int n = 0) {
 vector<Agg> agg; // Aggregated data for nodes
                                                     int k = 1;
 vector<T> lazy; // Lazy tags for nodes
                                                     while (len < n) len *= 2, k++;
 int len{1}; // Number of leaves
                                                     agg.resize(k);
 // Initialize tree for n elements; time: O(n)
                                                      lazv.resize(k, ID);
 SegTree(int n = 0) {
                                                      cow.resize(k, 1);
  while (len < n) len *= 2;
                                                      L.resize(k);
  agg.resize(len*2);
                                                     R.resize(k);
                                                     agg[--k].leaf();
  lazy.resize(len*2, ID);
  rep(i, 0, n) agg[len+i].leaf();
                                                      while (k--) {
  for (int i = len; --i;)
                                                       (agg[k] = agg[k+1]).merge(agg[k+1]);
    (agg[i] = agg[i*2]).merge(agg[i*2+1]);
                                                      L[k] = R[k] = k+1;
                                                     } // 211f
 void push(int i, int s) {
                                                    } // 83cf
  if (lazv[i] != ID) {
                                                    // New version from version `i`; time: O(1)
   agg[i*2].apply(lazy[i*2], lazy[i], s/2);
                                                    // First version number is 0.
   agg[i*2+1].apply(lazy[i*2+1],
                                                    int fork(int i) {
               lazy[i], s/2);
                                                     L.pb(L[i]); R.pb(R[i]); cow.pb(cow[i] = 1);
   lazv[i] = ID;
                                                     agg.pb(agg[i]); lazy.pb(lazy[i]);
  } // 3ba9
                                                     return sz(L)-1;
 1 // 5d19
                                                    1 // a21b
 // Modify interval [vb;ve) with val; O(lq n)
                                                    void push(int i, int s, bool w) {
 T update (int vb, int ve, T val, int i = 1,
                                                     bool has = (lazy[i] != ID);
       int b = 0, int e = -1) {
                                                     if ((has || w) && cow[i]) {
  if (e < 0) e = len;
                                                      int a = fork(L[i]), b = fork(R[i]);
  if (vb >= e | | b >= ve) return val;
                                                      L[i] = a; R[i] = b; cow[i] = 0;
  if (b >= vb && e <= ve &&
                                                     } // 1a3e
```

agg[i].apply(lazy[i], val, e-b))

return val;

```
if (has) {
   agg[L[i]].apply(lazy[L[i]],lazy[i],s/2);
    agg[R[i]].apply(lazy[R[i]],lazy[i],s/2);
   lazy[i] = ID;
  } // eca6
 } // 9f84
 // Modify interval [vb;ve) with val
 // in tree version `i`; time: O(lq n)
 T update(int i, int vb, int ve, T val,
       int b = 0, int e = -1) {
  if (e < 0) e = len;
  if (vb >= e || b >= ve) return val;
  if (b >= vb && e <= ve &&
     agg[i].apply(lazy[i], val, e-b))
    return val;
  int m = (b+e) / 2;
  push(i, e-b, 1);
  val = update(L[i], vb, ve, val, b, m);
  val = update(R[i], vb, ve, val, m, e);
  (agg[i] = agg[L[i]]).merge(agg[R[i]]);
  return val;
 1 // 776e
 // Query interval [vb;ve)
 // in tree version `i`; time: O(lq n)
 Agg query (int i, int vb, int ve,
        int b = 0, int e = -1) {
  if (e < 0) e = len;
  if (vb >= e | | b >= ve) return {};
  if (b >= vb && e <= ve) return agg[i]:
  int m = (b+e) / 2;
  push(i, e-b, 0);
  Agg t = query (L[i], vb, ve, b, m);
  t.merge(query(R[i], vb, ve, m, e));
  return t;
} // abf4
}; // 8a44
structures/segtree point.h
                                           2b0f
// Segment tree (point, interval)
// Configure by modifying:
// - T - stored data type
// - ID - neutral element for query operation
// - f(a, b) - combine results
struct SegTree {
using T = int;
 T ID = INT MIN;
 T f (T a, T b) { return max(a,b); }
 vector<T> V;
 int len:
 // Initialize tree for n elements; time: O(n)
 SegTree (int n = 0, T def = 0) {
  for (len = 1; len < n; len *= 2);
  V.resize(len*2, ID);
  rep(i, 0, n) V[len+i] = def;
  for (int i = len; --i;)
   V[i] = f(V[i*2], V[i*2+1]);
 } // 459e
 // Set element `i` to `val`; time: O(lg n)
 void set(int i, T val) {
  V[i += len] = val;
  while (i \neq 2)
   V[i] = f(V[i*2], V[i*2+1]);
 } // 4bcd
 // Query interval [b;e); time: O(lg n)
```

```
T query (int b, int e) {
  b += len; e += len-1;
  if (b > e) return ID;
  if (b == e) return V[b];
  T x = f(V[b], V[e]);
  while (b/2 < e/2) {
   if (^{\circ}b_{\bullet}^{\bullet}1) x = f(x, V[b^{\circ}1]);
   if (e&1) x = f(x, V[e^1]);
   b /= 2; e /= 2;
  } // 444a
  return x;
 } // de36
1: // d571
structures/treap.h
                                           bbb4
// "Set" of implicit keyed treaps; space: O(n)
// Nodes are keyed by their indices in array
// of all nodes. Treap key is key of its root.
// "Node x" means "node with key x".
// "Treap x" means "treap with key x".
// Kev -1 is "null".
// Put any additional data in Node struct.
struct Treap {
 struct Node {
  // E[0] = left child, <math>E[1] = right child
  // weight = node random weight (for treap)
  // size = subtree size, par = parent node
  int E[2] = \{-1, -1\}, weight {rand()};
  int size{1}, par{-1};
  bool flip{0}; // Is interval reversed?
 }; // c082
 vector<Node> G; // Array of all nodes
 // Initialize structure for n nodes
 // with keys 0, ..., n-1; time: O(n)
 // Each node is separate treap,
 // use join() to make sequence.
 Treap(int n = 0) : G(n) {}
 // Create new treap (a single node),
 // returns its key; time: O(1)
 int make() {
  G.emplace back(); return sz(G)-1;
 1 // 907a
 // Get size of node x subtree. x can be -1.
 int size(int x) { // time: O(1)
  return (x \ge 0 ? G[x].size : 0);
 } // 81cf
 // Propagate down data (flip flag etc).
 // x can be -1; time: O(1)
 void push(int x) {
  if (x >= 0 && G[x].flip) {
   G[x].flip = 0:
    swap (G[x].E[0], G[x].E[1]);
    each (e, G[x].E) if (e>=0) G[e].flip ^= 1;
  } // + any other lazy operations
 } // ed19
 // Update aggregates of node x.
 // x can be -1; time: O(1)
 void update(int x) {
  if (x >= 0) {
   int& s = G[x].size = 1;
   G[x].par = -1;
   each(e, G[x].E) if (e >= 0) {
     s += G[e].size;
     G[e].par = x;
    } // f7a7
```

```
} // + any other aggregates
// Split treap x into treaps 1 and r
// such that 1 contains first i elements
// and r the remaining ones.
// x, l, r can be -1; time: ^{\circ}O(\lg n)
void split(int x, int& l, int& r, int i) {
push (x); l = r = -1;
 if (x < 0) return;
 int key = size(G[x].E[0]);
 if (i <= key) {
  split(G[x].E[0], 1, G[x].E[0], i);
  split(G[x].E[1], G[x].E[1], r, i-key-1);
  1 = x;
} // fe19
 update(x);
} // 8211
// Join treaps 1 and r into one treap
// such that elements of 1 are before
// elements of r. Returns new treap.
// 1, r and returned value can be -1.
int join(int 1, int r) { // time: ~O(lq n)
push(1); push(r);
 if (1 < 0 | | r < 0) return max(1, r);</pre>
 if (G[1].weight < G[r].weight) {</pre>
  G[1].E[1] = join(G[1].E[1], r);
  update(1);
  return 1;
 1 // 18c7
 G[r].E[0] = join(1, G[r].E[0]);
update(r);
return r:
} // b559
// Find i-th node in treap x.
// Returns its kev or -1 if not found.
// x can be -1; time: ~O(lq n)
int find(int x, int i) {
 while (x \ge 0) {
  push(x);
  int key = size(G[x].E[0]);
  if (key == i) return x;
  x = G[x].E[key < i];
  if (key < i) i -= key+1;</pre>
1 // 054c
 return -1;
1 // 0b9b
// Get key of treap containing node x
// (key of treap root). x can be -1.
int root(int x) { // time: ~O(lq n)
while (G[x].par \ge 0) x = G[x].par;
return x;
} // be8b
// Get position of node x in its treap.
// x is assumed to NOT be -1; time: ~O(lq n)
int index(int x) {
int p, i = size(G[x].E[G[x].flip]);
 while ((p = G[x].par) >= 0) {
  if (G[p].E[1] == x) i+=size(G[p].E[0])+1;
  if (G[p].flip) i = G[p].size-i-1;
  x = p;
} // 3f81
 return i;
} // ddad
```

```
// Reverse interval [1;r) in treap x.
 // Returns new key of treap; time: ~O(lg n)
 int reverse(int x, int 1, int r) {
  int a, b, c;
  split(x, b, c, r);
  split (b, a, b, 1);
  if (b >= 0) G[b].flip ^= 1;
  return join(join(a, b), c);
} // e418
}; // 6a6c
structures/wavelet tree.h
// Wavelet tree ("merge-sort tree over values")
// Each node represent interval of values.
// seg[1]
             = original sequence
// seg[i]
              = subsequence with values
                represented by i-th node
// left[i][j] = how many values in seq[0:j)
                go to left subtree
struct WaveletTree {
vector<Vi> seq, left;
int len;
 // Build wavelet tree for sequence `elems`;
 // time and space: O((n+maxVal) log maxVal)
 // Values are expected to be in [0; maxVal).
 WaveletTree (const Vi& elems, int maxVal) {
  for (len = 1; len < maxVal; len *= 2);</pre>
  seq.resize(len*2);
  left.resize(len*2);
  seq[1] = elems;
  build(1, 0, len);
 } // a5e9
 void build(int i, int b, int e) {
  if (i >= len) return;
  int m = (b+e) / 2;
  left[i].pb(0);
  each(x, seq[i]) {
   left[i].pb(left[i].back() + (x < m));
   seq[i*2 + (x >= m)].pb(x);
  } // ac25
  build(i*2, b, m);
  build(i*2+1, m, e);
 } // 8153
 // Find k-th smallest element in [begin; end)
 // [begin;end); time: O(log maxVal)
 int kth(int begin, int end, int k, int i=1) {
  if (i >= len) return seg[i][0];
  int x = left[i][begin], y = left[i][end];
  if (k < y-x) return kth(x, y, k, i*2);
  return kth (begin-x, end-y, k-y+x, i*2+1);
 // Count number of elements >= vb and < ve
 // in [begin;end); time: O(log maxVal)
 int count (int begin, int end, int vb, int ve,
        int i = 1, int b = 0, int e = -1) {
  if (e < 0) e = len;</pre>
  if (b >= ve | | vb >= e) return 0;
  if (b >= vb && e <= ve) return end-begin;
  int m = (b+e) / 2;
  int x = left[i][begin], y = left[i][end];
  return count (x, y, vb, ve, i*2, b, m) +
   count (begin-x, end-y, vb, ve, i*2+1, m, e);
} // 71cf
}; // dd48
```

```
structures/ext/hash table.h 2d30
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
// gp_hash_table<K, V> = faster unordered_set
// Anti-anti-hash
const size_t HXOR = mt19937_64(time(0))();
template < class T > struct SafeHash {
size_t operator() (const T& x) const {
 return hash<T>() (x ^ T(HXOR));
} // 3a78
}; // 7d0e
structures/ext/rope.h
                                         051f
#include <ext/rope>
using namespace __qnu_cxx;
// rope<T> = implicit cartesian tree
structures/ext/tree.h
                                         a3bc
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb ds/tree policy.hpp>
using namespace __gnu_pbds;
template < class T, class Cmp = less < T>>
using ordered set = tree<
T, null_type, Cmp, rb_tree_tag,
tree_order_statistics_node_update
// Standard set functions and:
// t.order_of_key(key) - index of first >= key
// t.find_by_order(i) - find i-th element
// t1.join(t2) - assuming t1<>t2 merge t2 to t1
structures/ext/trie.h
                                         5cc2
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb ds/trie policy.hpp>
using namespace __gnu_pbds;
using pref_trie = trie<</pre>
string, null type,
 trie_string_access_traits , pat_trie_tag,
trie_prefix_search_node_update
text/aho corasick.h
                                         697d
constexpr char AMIN = 'a'; // Smallest letter
constexpr int ALPHA = 26; // Alphabet size
// Aho-Corasick algorithm for linear-time
// multiple pattern matching.
// Add patterns using add(), then call build().
struct Aho {
 vector<arrav<int, ALPHA>> nxt{1};
 Vi suf = \{-1\}, accLink = \{-1\};
 vector<Vi> accept{1};
 // Add string with given ID to structure
 // Returns index of accepting node
 int add(const string& str, int id) {
  int i = 0:
  each(c, str) {
   if (!nxt[i][c-AMIN]) {
     nxt[i][c-AMIN] = sz(nxt);
     nxt.pb({}); suf.pb(-1);
     accLink.pb(1); accept.pb({});
   } // 5ead
   i = nxt[i][c-AMIN];
  } // ace9
  accept[i].pb(id);
  return i;
                                                  KMR() {}
```

```
1 // 27c8
 // Build automata; time: O(V*ALPHA)
 void build() {
  queue<int> que;
  each(e, nxt[0]) if (e) {
   suf[e] = 0; que.push(e);
  } // c34d
  while (!que.emptv()) {
   int i = que.front(), s = suf[i], j = 0;
    que.pop();
    each(e, nxt[i]) {
     if (e) que.push(e);
     (e ? suf[e] : e) = nxt[s][j++];
    } // 8521
    accLink[i] = (accept[s].empty() ?
      accLink[s] : s);
  } // 1e8a
 1 // 2561
 // Append `c` to state `i`
 int next(int i, char c) {
  return nxt[i][c-AMIN];
 } // 6bb7
 // Call `f` for each pattern accepted
 // when in state `i` with its ID as argument.
 // Return true from `f` to terminate early.
 // Calls are in descreasing length order.
 template<class F> void accepted(int i, F f) {
  while (i !=-1) {
   each(a, accept[i]) if (f(a)) return;
   i = accLink[i];
  } // c175
 } // 1f0d
1: // 2768
text/kmp.h
                                           5729
// Computes prefsuf array; time: O(n)
// ps[i] = max prefsuf of [0;i); ps[0] := -1
template < class T > Vi kmp (const T& str) {
 Vi ps; ps.pb(-1);
 each(x, str) {
  int k = ps.back();
  while (k \ge 0 \& \& str[k] != x) k = ps[k];
  ps.pb(k+1);
 } // 05aa
 return ps;
1 // 8a6c
// Finds occurences of pat in vec; time: O(n)
// Returns starting indices of matches.
template<class T>
Vi match (const T& str, T pat) {
 int n = sz(pat);
 pat.pb(-1); // SET TO SOME UNUSED CHARACTER
 pat.insert(pat.end(), all(str));
 Vi ret, ps = kmp(pat);
 rep(i, 0, sz(ps)) {
 if (ps[i] == n) ret.pb(i-2*n-1);
 } // ale9
 return ret:
} // f986
text/kmr.h
                                          ee8c
// KMR algorithm for O(1) lexicographical
// comparison of substrings.
struct KMR {
 vector<Vi>ids;
```

```
if (k > 0) k--;
                                                                                                      text/manacher.h
                                                                                                                                                8680
                                                                                                                                                           return i:
 // Initialize structure; time: O(n lg^2 n)
                                                   } // 8b22
                                                                                                                                                          } // d442
                                                                                                      // Manacher algorithm; time: O(n)
 // You can change str type to Vi freely.
                                                    return lcp;
                                                                                                      // Finds largest radiuses for palindromes:
                                                                                                                                                          // Append letter from [0; ALPHA); time: O(1)
 KMR (const string& str) {
                                                  } // d438
                                                                                                     // r[2*i] = for center at i (single letter = 1)
                                                                                                                                                          // (or O(lg n) if [EXT] is enabled)
  ids.clear();
                                                                                                      // r[2*i+1] = for center between i and i+1
                                                                                                                                                          void add(int x) {
  ids.pb(Vi(all(str)));
                                                   text/lvndon factorization.h 688c
                                                                                                      template < class T > Vi manacher (const T& str) {
                                                                                                                                                           txt.pb(x);
  for (int h = 1; h <= sz(str); h *= 2) {
                                                                                                      int n = sz(str) *2, c = 0, e = 1;
                                                                                                                                                           last = ext(last);
                                                   // Compute Lyndon factorization for s; O(n)
   vector<pair<Pii, int>> tmp;
                                                   // Word is simple iff it's stricly smaller
                                                                                                       Vi r(n, 1);
                                                                                                                                                           if (!to[last][x]) {
                                                                                                       auto get = [&] (int i) { return i%2 ? 0 :
                                                   // than any of it's nontrivial suffixes.
                                                                                                                                                            len.pb(len[last]+2);
   rep(j, 0, sz(str)) {
                                                   // Lyndon factorization is division of string
                                                                                                        (i \ge 0 \&\& i < n ? str[i/2] : i); }; // 3d98
     int a = ids.back()[j], b = -1;
                                                                                                                                                            link.pb(to[ext(link[last])][x]);
                                                   // into non-increasing simple words.
     if (j+h < sz(str)) b = ids.back()[j+h];
                                                                                                                                                            to[last][x] = sz(to);
                                                   // It is unique.
                                                                                                        if (i < e) r[i] = min(r[c*2-i], e-i);
     tmp.pb({ {a, b}, j });
                                                                                                                                                            to.emplace_back();
                                                   vector<string> duval(const string& s) {
   } // a210
                                                                                                        while (get(i-r[i]) == get(i+r[i])) r[i]++;
                                                    int n = sz(s), i = 0;
                                                                                                        if (i+r[i] > e) c = i, e = i+r[i]-1;
    sort(all(tmp));
                                                                                                                                                            diff.pb(len.back() - len[link.back()]);
                                                    vector<string> ret:
                                                                                                       } // Of87
   ids.emplace_back(sz(tmp));
                                                                                                                                                            slink.pb(diff.back() == diff[link.back()]
                                                    while (i < n) {
                                                     int i = i+1, k = i;
                                                                                                       rep(i, 0, n) r[i] /= 2;
                                                                                                                                                             ? slink[link.back()] : link.back());
    int n = 0;
                                                                                                      return r:
                                                                                                                                                            series.pb(0):
                                                     while (j < n \&\& s[k] <= s[j])
    rep(j, 0, sz(tmp)) {
                                                      k = (s[k] < s[j] ? i : k+1), j++;
                                                                                                      } // a300
                                                                                                                                                            // [/EXT]
     if (j > 0 \&\& tmp[j-1].x != tmp[j].x)
                                                                                                                                                           } // 0adb
                                                     while (i <= k)
                                                                                                      text/min rotation.h
                                                                                                                                                e4d6
                                                      ret.pb(s.substr(i, j-k)), i += j-k;
                                                                                                                                                           last = to[last][x];
     ids.back()[tmp[j].y] = n;
                                                    } // 3f17
                                                                                                      // Find lexicographically smallest
   } // bd2e
                                                                                                                                                           // [EXT]
                                                                                                     // rotation of s; time: O(n)
                                                   return ret:
  } // 969a
                                                                                                                                                           ans.pb(INT MAX);
                                                   } // 0e48
                                                                                                      // Returns index where shifted word starts.
 } // a40e
                                                                                                                                                           for (int i=last; len[i] > 0; i=slink[i]) {
                                                                                                      // You can use std::rotate to get the word:
                                                                                                                                                            series[i] = ans[sz(ans) - len[slink[i]]
 // Get representative of [begin; end); O(1)
                                                   text/main lorentz.h
                                                                                              9afb
                                                                                                     // rotate(s.begin(), s.begin()+minRotation(s),
                                                                                                                                                                      - diff[i] - 1];
 Pii get (int begin, int end) {
                                                                                                               s.end()):
                                                                                                                                                            if (diff[i] == diff[link[i]])
                                                   #include "z_function.h"
  if (begin >= end) return {0, 0};
                                                                                                     int minRotation(string s) {
                                                                                                                                                              series[i] = min(series[i],
  int k = 31 - builtin clz(end-begin);
                                                                                                      int a = 0, n = sz(s); s += s;
                                                   struct Sgr {
                                                                                                                                                                        series[link[i]]);
  return {ids[k][begin], ids[k][end-(1<<k)]};</pre>
                                                                                                      rep(b, 0, n) rep(i, 0, n) {
                                                   int begin, end, len;
                                                                                                                                                            // If you want only even palindromes
                                                                                                        if (a+i == b | | s[a+i] < s[b+i]) {</pre>
                                                   }; // f012
                                                                                                                                                            // set ans only for sz(txt) %2 == 0
                                                                                                         b += max(0, i-1); break;
 // Compare [b1;e1) with [b2;e2); O(1)
                                                                                                                                                            ans.back() = min(ans.back(), series[i]+1);
                                                   // Main-Lorentz algorithm for finding
                                                                                                        } // 865b
 // Returns -1 if <, 0 if ==, 1 if >
                                                                                                                                                          } // ab3b
                                                   // all squares in given word; time: O(n lq n)
                                                                                                        if (s[a+i] > s[b+i]) {
 int cmp(int b1, int e1, int b2, int e2) {
                                                                                                                                                          // [/EXT]
                                                   // Results are in compressed form:
                                                                                                         a = b; break;
  int 11 = e1-b1, 12 = e2-b2;
                                                                                                                                                         1 // 909a
                                                   // (b, e, 1) means that for each b <= i < e
                                                                                                        ] // 7628
                                                                                                                                                        }; // b3a7
  int 1 = min(11, 12);
                                                   // there is square at position i of size 21.
                                                                                                      } // 40be
  Pii x = get(b1, b1+1), y = get(b2, b2+1);
                                                   // Each square is present in only one interval.
                                                                                                      return a;
                                                                                                                                                        text/suffix array linear.h
                                                                                                                                                                                                   1341
                                                   vector<Sqr> lorentz(const string& s) {
  if (x == v) return (11 > 12) - (11 < 12):
                                                                                                     } // 9ed8
                                                    int n = sz(s);
                                                                                                                                                         #include "../util/radix sort.h"
  return (x > y) - (x < y);
                                                                                                                                                8d2d
                                                                                                      text/palindromic tree.h
                                                    if (n <= 1) return {};</pre>
 } // bf42
                                                                                                                                                         // KS algorithm for suffix array; time: O(n)
                                                    auto a = s.substr(0, n/2), b = s.substr(n/2);
                                                                                                      constexpr int ALPHA = 26; // Set alphabet size
                                                                                                                                                         // Input values are assumed to be in [1;k]
 // Compute suffix array of string; O(n)
                                                    auto ans = lorentz(a);
                                                                                                                                                        Vi sufArray(Vi str, int k) {
 Vi sufArray() {
                                                                                                      // Tree of all palindromes in string,
                                                    each (p, lorentz (b))
                                                                                                                                                         int n = sz(str);
  Vi sufs(sz(ids.back()));
                                                                                                      // constructed online by appending letters.
                                                     ans.pb(\{p.begin+n/2, p.end+n/2, p.len\});
                                                                                                                                                          Vi suf(n);
  rep(i, 0, sz(ids.back()))
                                                                                                      // space: O(n*ALPHA); time: O(n)
                                                                                                                                                          str.resize(n+15);
   sufs[ids.back()[i]] = i;
                                                    string ra(a.rbegin(), a.rend());
                                                                                                      // Code marked with [EXT] is extension for
  return sufs;
                                                    string rb(b.rbegin(), b.rend());
                                                                                                      // calculating minimal palindrome partition
                                                                                                                                                          if (n < 15) {
 } // d98d
                                                                                                      // in O(n lg n). Can also be modified for
                                                                                                                                                           iota(all(suf), 0);
                                                    rep(j, 0, 2) {
}; // 457e
                                                                                                      // similar dynamic programmings.
                                                                                                                                                           rep(j, 0, n) countSort(suf,
                                                     Vi z1 = prefPref(ra), z2 = prefPref(b+a);
                                                                                                                                                            [&] (int i) { return str[i+n-j-1]; }, k);
                                                                                                      struct PalTree {
                                                     z1.pb(0); z2.pb(0);
text/lcp.h
                                           0c65
                                                                                                      Vi txt: // Text for which tree is built
                                                                                                                                                           return suf:
                                                     rep(c, 0, sz(a)) {
                                                                                                                                                          } // 5fcf
// Compute Longest Common Prefix array for
                                                                                                      // Node 0 = empty palindrome (root of even)
                                                       int l = sz(a) - c;
// given string and it's suffix array; O(n)
                                                                                                       // Node 1 = "-1" palindrome (root of odd)
                                                                                                                                                          // Compute triples codes
                                                       int x = c - \min(1-1, z1[1]);
// In order to compute suffix array use kmr.h
                                                                                                      Vi len (0, -1): // Lengths of palindromes
                                                                                                                                                         Vi tmp, code (n+2);
                                                       int y = c - max(1-z2[sz(b)+c], j);
// or suffix_array_linear.h
                                                                                                      Vi link{1, 0}; // Suffix palindrome links
                                                                                                                                                          rep(i, 0, n) if (i % 3) tmp.pb(i);
                                                       if (x > y) continue;
template<class T>
                                                                                                       // Edges to next palindromes
                                                                                                                                                          rep(j, 0, 3) countSort(tmp,
Vi lcpArray (const T& str, const Vi& sufs) {
                                                                                                       vector<array<int, ALPHA>> to{ {}, {} };
                                                                                                                                                           [&] (int i) { return str[i-j+2]; }, k);
 int n = sz(str), k = 0;
                                                        ans.pb(\{n-y-1*2, n-x-1*2+1, 1\});
                                                                                                       int last{0}; // Current node (max suffix pal)
 Vi pos(n), lcp(n-1);
                                                                                                                                                          int mc = 0, j = -1;
                                                                                                       Vi diff{0, 0}; // len[i]-len[link[i]] [EXT]
 rep(i, 0, n) pos[sufs[i]] = i;
                                                        ans.pb(\{x, y+1, 1\});
                                                                                                       Vi slink{0, 0}; // Serial links
                                                                                                                                               [EXT]
                                                                                                                                                          each(i, tmp) {
 rep(i, 0, n) {
                                                     } // 6c51
                                                                                                       Vi series {0, 0}; // Series DP answer
                                                                                                                                               [EXT]
                                                                                                                                                           code[i] = mc += (j == -1)
  if (pos[i] < n-1) {
                                                                                                       Vi ans{0};
                                                                                                                    // DP answer for prefix[EXT]
                                                                                                                                                              str[i] != str[j] ||
                                                     a.swap(rb);
   int j = sufs[pos[i]+1];
                                                     b.swap(ra);
                                                                                                                                                              str[i+1] != str[j+1] ||
   while (i+k < n && j+k < n &&
                                                                                                       int ext(int i) {
                                                    } // b6b2
                                                                                                                                                              str[i+2] != str[j+2]);
      str[i+k] == str[j+k]) k++;
                                                                                                        while (len[i]+2 > sz(txt) ||
                                                                                                                                                           j = i;
    lcp[pos[i]] = k;
                                                    return ans;
                                                                                                             txt[sz(txt)-len[i]-2] != txt.back())
                                                                                                                                                          } // bfdc
  } // 2cba
                                                   } // 5567
                                                                                                         i = link[i];
```

tmp.clear();

// Compute suffix array of 2/3

for (int i=1; i < n; i += 3) tmp.pb(code[i]);</pre>

```
tmp.pb(0);
                                                     finish();
 for (int i=2; i < n; i += 3) tmp.pb(code[i]);</pre>
                                                    } // ec2e
 tmp = sufArray (move (tmp), mc);
                                                    // Append letter to the back
 // Compute partial suffix arrays
                                                    void add(char c) {
                                                     int v = last, x = c-AMIN;
 Vi third;
                                                     last = sz(len);
 int th = (n+4) / 3;
 if (n%3 == 1) third.pb(n-1);
                                                     len.pb(len[v]+1);
                                                     link.pb(0);
 rep(i, 1, sz(tmp)) {
                                                     to.pb({});
  int e = tmp[i];
                                                     cnt.pb(1); // [OCC]
  tmp[i-1] = (e 
  code[tmp[i-1]] = i;
                                                     while (v != -1 && !to[v][x]) {
  if (e < th) third.pb(e*3);
                                                      to[v][x] = last;
 } // f9f1
                                                      v = link[v];
                                                     } // 4cfc
 tmp.pop_back();
                                                     if ( \lor != -1 )  {
 countSort (third,
  [&] (int i) { return str[i]; }, k);
                                                      int q = to[v][x];
                                                      if (len[v]+1 == len[q]) {
 // Merge suffix arravs
                                                       link[last] = q;
 merge(all(third), all(tmp), suf.begin(),
                                                      } else {
  [&] (int 1, int r) {
                                                        len.pb(len[v]+1);
    while (1%3 == 0 | | r%3 == 0) {
                                                        link.pb(link[q]);
     if (str[1] != str[r])
                                                        to.pb(to[q]);
      return str[1] < str[r];</pre>
                                                        cnt.pb(0); // [OCC]
     1++; r++;
                                                        link[last] = link[q] = sz(len)-1;
   } // 2f8a
                                                        while (v != -1 \&\& to[v][x] == q) {
    return code[1] < code[r];</pre>
                                                        to[v][x] = link[q];
  1): // 4cb3
                                                         v = link[v];
                                                       1 // 784f
 return suf:
                                                      } // 90aa
} // 9165
                                                     } // af69
// KS algorithm for suffix array; time: O(n)
                                                   } // 345a
Vi sufArrav(const string& str) {
 return sufArray(Vi(all(str)), 255);
                                                    // Compute some additional stuff (offline)
1 // 593f
                                                    void finish() {
text/suffix automaton.h
                                           d00d
                                                     inSufs.resize(sz(len));
                                                     rep(i, 1, sz(link)) inSufs[link[i]].pb(i);
constexpr char AMIN = 'a'; // Smallest letter
                                                     dfsSufs(0):
constexpr int ALPHA = 26; // Set alphabet size
// Suffix automaton - minimal DFA that
                                                     // [PATHS]
// recognizes all suffixes of given string
                                                     paths.assign(sz(len), 0);
// (and encodes all substrings);
                                                     dfs(0);
// space: O(n*ALPHA); time: O(n)
                                                     // [/PATHS]
// Paths from root are equivalent to substrings
                                                    1 // 3f75
// Extensions:
                                                    // Only for [OCC]
// - [OCC] - count occurences of substrings
                                                    void dfsSufs(int v) {
// - [PATHS] - count paths from node
                                                     each(e, inSufs[v]) {
struct SufDFA {
 // State v represents endpos-equivalence
                                                      dfsSufs(e);
                                                      cnt[v] += cnt[e];
 // class that contains words of all lengths
                                                     } // 2469
 // between link[len[v]]+1 and len[v].
                                                   } // 0c60
 // len[v] = longest word of equivalence class
 // link[v] = link to state of longest suffix
                                                    // Only for [PATHS]
              in other equivalence class
                                                    void dfs(int v) {
 // to[v][c] = automaton edge c from v
                                                     if (paths[v]) return;
 Vi len{0}, link{-1};
                                                     paths[v] = 1;
 vector<array<int, ALPHA>> to{ {} };
                                                     each (e, to[v]) if (e) {
 int last{0}; // Current node (whole word)
                                                      dfs(e);
                                                      paths[v] += paths[e];
 vector<Vi>inSufs; // [OCC] Suffix-link tree
                                                     } // 22b3
 Vi cnt{0};
                // [OCC] Occurence count
                                                    } // d004
 vector<ll> paths; // [PATHS] Out-path count
                                                    // Go using edge `c` from state `i`.
 SufDFA() {}
                                                    // Returns 0 if edge doesn't exist.
 // Build suffix automaton for given string
```

// and compute extended stuff; time: O(n)

SufDFA (const string& s) {

each(c, s) add(c);

```
return to[i][c-AMIN];
 } // c363
 // Get lexicographically k-th substring
 // of represented string; time: O(|substr|)
 // Empty string has index 0.
 // Requires [PATHS] extension.
 string lex(ll k) {
  string s;
  int v = 0;
  while (k--) rep(i, 0, ALPHA) {
   int e = to[v][i];
   if (e) {
     if (k < paths[e]) {</pre>
      s.pb(char(AMIN+i));
      v = e;
      break;
     } // f307
     k -= paths[e];
   } // 29be
  } // 4600
  return s;
} // e4af
}; // 7135
text/suffix tree.h
                                           40a4
constexpr int ALPHA = 26;
// Ukkonen's algorithm for online suffix tree
// construction; space: O(n*ALPHA); time: O(n)
// Real tree nodes are called dedicated nodes.
// "Nodes" lying on compressed edges are called
// implicit nodes and are represented
// as pairs (lower node, label index).
// Labels are represented as intervals [L;R)
// which refer to substrings [L;R) of txt.
// Leaves have labels of form [L:infinity].
// use getR to get current right endpoint.
// Suffix links are valid only for internal
// nodes (non-leaves).
struct SufTree {
Vi txt; // Text for which tree is built
// to[v][c] = edge with label starting with c
               from node v
 vector<array<int, ALPHA>> to{ {} };
 Vi L{0}, R{0}; // Parent edge label endpoints
Vi par{0};  // Parent link
Vi link{0};  // Suffix link
 Pii cur{0, 0}; // Current state
 // Get current right end of node label
 int getR(int i) { return min(R[i],sz(txt)); }
 // Follow edge 'e' of implicit node 's'.
 // Returns (-1, -1) if there is no edge.
 Pii next (Pii s, int e) {
  if (s.y < getR(s.x))</pre>
   return txt[s.v] == e ? mp(s.x, s.v+1)
                 : mp(-1, -1);
  e = to[s.x][e];
  return e ? mp (e, L[e]+1) : mp (-1, -1);
 1 // f430
 // Create dedicated node for implicit node
 // and all its suffixes
 int split (Pii s) {
  if (s.y == R[s.x]) return s.x;
  int t = sz(to); to.pb({});
  to[t][txt[s.y]] = s.x;
```

int next(int i, char c) {

```
L.pb(L[s.x]);
  R.pb(L[s.x] = s.y);
  par.pb(par[s.x]);
  par[s.x] = to[par[t]][txt[L[t]]] = t;
  link.pb(-1);
  int v = link[par[t]], l = L[t] + !par[t];
  while (1 < R[t]) {</pre>
   v = to[v][txt[1]];
   1 += getR(v) - L[v];
  } // 0393
  v = split(\{v, getR(v)-l+R[t]\});
  link[t] = v;
  return t;
 1 // 10bb
 // Append letter from [0;ALPHA) to the back
 void add(int x) { // amortized time: 0(1)
  Pii t; txt.pb(x);
  while ((t = next(cur, x)).x == -1) {
   int m = split(cur);
    to[m][x] = sz(to);
    to.pb({});
    par.pb(m);
    L.pb(sz(txt)-1);
    R.pb(INT MAX);
    link.pb(-1);
    cur = {link[m], getR(link[m])};
    if (!m) return;
  } // 60c2
  cur = t;
 } // 6f4e
1: // dbfb
text/z function.h
                                           0466
// Computes Z function array; time: O(n)
// zf[i] = max common prefix of str and str[i:]
template < class T> Vi prefPref (const T& str) {
 int n = sz(str), b = 0, e = 1;
 Vi zf(n):
 rep(i, 1, n) {
  if (i < e) zf[i] = min(zf[i-b], e-i);</pre>
  while (i+zf[i] < n &&
    str[zf[i]] == str[i+zf[i]]) zf[i]++;
  if (i+zf[i] > e) b = i, e = i+zf[i];
 } // e906
 zf[0] = n;
 return zf:
} // b88d
                                           5247
trees/centroid decomp.h
// Centroid decomposition; space: O(n lq n)
struct CentroidTree {
 // child[v] = children of v in centroid tree
 // par[v] = parent of v in centroid tree
              (-1 for root)
 // depth[v] = depth of v in centroid tree
                (0 for root)
 // ind[v][i] = index of vertex v in i-th
                centroid subtree from root
 // size[v] = size of centroid subtree of v
 // subtree[v] = list of vertices
                 in centroid subtree of v
 // dists[v] = distances from v to vertices
               in its centroid subtree
                (in the order of subtree[v])
 // neigh[v] = neighbours of v
               in its centroid subtree
 // dir[v][i] = index of centroid neighbour
```

```
that is first vertex on path
                 from centroid v to i-th vertex
                 of centroid subtree
                 (-1 for centroid)
 vector<Vi> child, ind, dists, subtree,
        neigh, dir;
 Vi par, depth, size;
 int root; // Root centroid
 CentroidTree() {}
 CentroidTree (vector<Vi>& G)
   : child(sz(G)), ind(sz(G)), dists(sz(G)),
     subtree(sz(G)), neigh(sz(G)),
     dir(sz(G)), par(sz(G), -2),
     depth(sz(G)), size(sz(G)) {
  root = decomp(G, 0, 0);
 1 // 026c
 void dfs(vector<Vi>& G, int v, int p) {
  size[v] = 1;
  each (e, G[v]) if (e != p && par[e] == -2)
   dfs(G, e, v), size[v] += size[e];
 } // bbed
 void layer (vector < Vi>& G, int v,
        int p, int c, int d) {
  ind[v].pb(sz(subtree[c]));
  subtree[c].pb(v);
  dists[c].pb(d);
  dir[c].pb(sz(neigh[c])-1);
  each (e, G[v]) if (e != p && par[e] == -2) {
   if (v == c) neigh[c].pb(e);
   layer(G, e, v, c, d+1);
  } // dc82
 } // 37ee
 int decomp(vector<Vi>& G, int v, int d) {
  dfs(G, v, -1);
  int p = -1, s = size[v];
 loop:
  each (e, G[v]) {
   if (e != p && par[e] == -2 &&
      size[e] > s/2) {
     p = v; v = e; goto loop;
   } // e0a5
  } // 3533
  par[v] = -1;
  size[v] = s;
  depth[v] = d;
  layer(G, v, -1, v, 0);
  each (e, G[v]) if (par[e] == -2) {
   int j = decomp(G, e, d+1);
   child[v].pb(j);
   par[j] = v;
  } // 70b5
  return v;
 } // 217c
}; // 71d6
                                           ac92
trees/centroid offline.h
```

## // Helper for offline centroid decomposition // Usage: CentroidDecomp(G); // Constructor calls method `process` // for each centroid subtree. struct CentroidDecomp { vector<Vi>& G; // Reference to target graph

vector<bool> on; // Is vertex enabled?

Vi size: // Used internally

```
// Run centroid decomposition for graph g
CentroidDecomp (vector < Vi>& q)
   : G(q), on(sz(q), 1), size(sz(q)) {
  decomp(0);
 } // 8677
 // Compute subtree sizes for subtree rooted
 // at v, ignoring p and disabled vertices
 void computeSize(int v, int p) {
  size[v] = 1;
  each (e, G[v]) if (e != p && on[e])
   computeSize(e, v), size[v] += size[e];
 } // 1c0d
 void decomp(int v) {
  computeSize(v, -1);
  int p = -1, s = size[v];
 loop:
  each(e, G[v]) {
   if (e != p && on[e] && size[e] > s/2) {
    p = v; v = e; goto loop;
   } // e0a5
  } // f31d
  process(v);
  on[v] = 0;
  each (e, G[v]) if (on[e]) decomp (e);
 } // f170
 // Process current centroid subtree:
 // - v is centroid
 // - boundary vertices have on[x] = 0
 // Formally: Let H be subgraph induced
 // on vertices such that on [v] = 1.
 // Then current centroid subtree is
 // connected component of H that contains v
 // and v is its centroid.
 void process(int v) {
  // Do your stuff here...
) // d41d
}; // a923
                                          9739
trees/heavylight decomp.h
#include "../structures/segtree point.h"
// Heavy-Light Decomposition of tree
// with subtree query support; space: O(n)
struct HLD {
// Subtree of v = [pos[v]; pos[v] + size[v])
 // Chain with v = [chBegin[v]; chEnd[v])
 Vi par; // Vertex parent
 Vi size; // Vertex subtree size
 Vi depth; // Vertex distance to root
 Vi pos; // Vertex position in "HLD" order
 Vi chBegin: // Begin of chain with vertex
 Vi chEnd; // End of chain with vertex
 Vi order: // "HLD" preorder of vertices
 SegTree tree; // Verts are in HLD order
 HLD() {}
 // Initialize structure for tree G
 // and given root; time: O(n la n)
 // MODIFIES ORDER OF EDGES IN G!
 HLD(vector<Vi>& G, int root)
   : par(sz(G)), size(sz(G)),
     depth(sz(G)), pos(sz(G)),
     chBegin(sz(G)), chEnd(sz(G)) {
  dfs(G, root, -1);
  decomp(G, root, -1, 0);
  tree = {sz(order)};
 1 // 8263
```

```
void dfs(vector<Vi>& G, int v, int p) {
 par[v] = p;
 size[v] = 1;
 depth[v] = p < 0 ? 0 : depth[p]+1;
 int& fs = G[v][0];
 if (fs == p) swap(fs, G[v].back());
 each(e, G[v]) if (e != p) {
  dfs(G, e, v);
   size[v] += size[e];
   if (size[e] > size[fs]) swap(e, fs);
 } // 9872
} // 12fe
void decomp(vector<Vi>& G,
        int v, int p, int chb) {
 pos[v] = sz(order);
 chBegin[v] = chb;
 chEnd[v] = pos[v]+1;
 order.pb(v);
 each(e, G[v]) if (e != p) {
  if (e == G[v][0]) {
    decomp (G, e, v, chb);
    chEnd[v] = chEnd[e];
   } else {
    decomp(G, e, v, sz(order));
  } // c84a
 } // f707
} // eb89
// Get root of chain containing v
int chRoot(int v) {return order[chBegin[v]];}
// Level Ancestor Query; time: O(lq n)
int lag(int v, int level) {
 while (true) {
   int k = pos[v] - depth[v] + level;
   if (k >= chBegin[v]) return order[k];
   v = par[chRoot(v)];
 1 // 8c18
} // 675e
// Lowest Common Ancestor; time: O(lq n)
int lca(int a, int b) {
 while (chBegin[a] != chBegin[b]) {
   int ha = chRoot(a), hb = chRoot(b);
   if (depth[ha] > depth[hb]) a = par[ha];
   else b = par[hb];
 } // 5620
 return depth[a] < depth[b] ? a : b;</pre>
} // c168
// Call func(chBegin, chEnd) on each path
// seament; time: O(la n * time of func)
template<class T>
void iterPath(int a, int b, T func) {
 while (chBegin[a] != chBegin[b]) {
   int ha = chRoot(a), hb = chRoot(b);
   if (depth[ha] > depth[hb]) {
    func(chBegin[a], pos[a]+1);
    a = par[ha];
   } else {
    func(chBegin[b], pos[b]+1);
    b = par[hb];
  1 // f9a5
 1 // 563c
 if (pos[a] > pos[b]) swap(a, b);
 // Remove +1 from pos[a]+1 for vertices
  // queries (with +1 -> edges).
 func (pos[a]+1, pos[b]+1);
```

```
1 // 17e5
 // Query path between a and b; O(1g^2 n)
 SegTree:: T queryPath (int a, int b) {
  auto ret = tree.ID;
  iterPath(a, b, [&](int i, int j) {
   ret = tree.f(ret, tree.query(i, j));
  }); // 1113
  return ret;
 } // 1bc9
 // Query subtree of v; time: O(lg n)
 SegTree::T querySubtree(int v) {
 return tree.query(pos[v], pos[v]+size[v]);
} // 23db
1: // a062
trees/lca.h
                                           294f
// LAQ and LCA using jump pointers
// space: O(n lg n)
struct LCA {
 vector<Vi>jumps;
 Vi level, pre, post;
 int cnt{0}, depth;
 LCA() {}
 // Initialize structure for tree G
 // and root r; time: O(n lg n)
 LCA (vector<Vi>& G, int root)
   : jumps(sz(G)), level(sz(G)),
     pre(sz(G)), post(sz(G)) {
  dfs(G, root, root);
  depth = int(log2(sz(G))) + 2;
  rep(j, 0, depth) each(v, jumps)
   v.pb(jumps[v[j]][j]);
 1 // d6ce
 void dfs(vector<Vi>& G, int v, int p) {
  level[v] = p == v ? 0 : level[p]+1;
  jumps[v].pb(p);
  pre[v] = ++cnt;
  each(e, G[v]) if (e != p) dfs(G, e, v);
  post[v] = ++cnt;
 } // e286
 // Check if a is ancestor of b; time: O(1)
 bool isAncestor(int a, int b) {
  return pre[a] <= pre[b] &&
       post[b] <= post[a];</pre>
 1 // 5514
 // Lowest Common Ancestor; time: O(lg n)
 int operator()(int a, int b) {
  for (int j = depth; j--;)
   if (!isAncestor(jumps[a][j], b))
     a = jumps[a][j];
  return isAncestor(a, b) ? a : jumps[a][0];
 } // 27d8
 // Level Ancestor Query; time: O(lg n)
 int lag(int a, int lvl) {
  for (int j = depth; j--;)
   if (lvl <= level[jumps[a][j]])</pre>
     a = jumps[a][j];
  return a:
 } // 75b3
 // Get distance from a to b; time: O(lg n)
 int distance(int a, int b) {
  return level[a] + level[b] -
       level[operator()(a, b)]*2;
```

```
1 // 07e0
 // Get k-th vertex on path from a to b,
 // a is 0, b is last; time: O(lg n)
 // Returns -1 if k > distance(a, b)
 int kthVertex(int a, int b, int k) {
  int c = operator()(a, b);
  if (level[a]-k >= level[c])
   return lag(a, level[a]-k);
  k += level[c] *2 - level[a];
  return (k > level[b] ? -1 : laq(b, k));
 } // 46c9
}; // 2254
trees/lca linear.h
                                            7aa5
// LAO and LCA using jump pointers
// with linear memory; space: O(n)
struct LCA {
 Vi par, jmp, depth, pre, post;
 int cnt{0};
 LCA() {}
 // Initialize structure for tree G
 // and root v; time: O(n lg n)
 LCA (vector < Vi>& G, int v)
    : par(sz(G), -1), imp(sz(G), v),
     depth(sz(G)), pre(sz(G)), post(sz(G)) {
  dfs(G, v);
 } // 94cf
 void dfs (vector<Vi>& G, int v) {
  int j = jmp[v], k = jmp[j], x =
   depth[v]+depth[k] == depth[j]*2 ? k : v;
  pre[v] = ++cnt;
  each(e, G[v]) if (!pre[e]) {
   par[e] = v; jmp[e] = x;
   depth[e] = depth[v]+1;
   dfs(G, e);
  } // b123
  post[v] = ++cnt;
 } // 3280
 // Level Ancestor Ouerv; time: O(lq n)
 int lag(int v, int d) {
  while (depth[v] > d)
   v = depth[jmp[v]] < d ? par[v] : jmp[v];</pre>
  return v;
 } // f509
 // Lowest Common Ancestor; time: O(lq n)
 int operator()(int a, int b) {
  if (depth[a] > depth[b]) swap(a, b);
  b = lag(b, depth[a]);
  while (a != b) {
   if (jmp[a] == jmp[b])
     a = par[a], b = par[b];
     a = jmp[a], b = jmp[b];
  } // fe08
  return a:
 // Check if a is ancestor of b; time: O(1)
 bool isAncestor(int a, int b) {
  return pre[a] <= pre[b] &&
       post[b] <= post[a];</pre>
 // Get distance from a to b; time: O(lg n)
 int distance(int a, int b) {
  return depth[a] + depth[b] -
```

```
depth[operator()(a, b)]*2;
 1 // a340
 // Get k-th vertex on path from a to b,
 // a is 0, b is last; time: O(lq n)
 // Returns -1 if k > distance(a, b)
 int kthVertex(int a, int b, int k) {
  int c = operator()(a, b);
  if (depth[a]-k >= depth[c])
   return lag(a, depth[a]-k);
  k += depth[c] *2 - depth[a];
  return (k > depth[b] ? -1 : laq(b, k));
 } // 34ed
}; // a221
trees/link cut tree.h
                                            6bd6
constexpr int INF = 1e9:
// Link/cut tree; space: O(n)
// Represents forest of (un)rooted trees.
struct LinkCutTree {
vector<array<int, 2>> child;
 Vi par, prev, flip, size;
 // Initialize structure for n vertices; O(n)
 // At first there's no edges.
 LinkCutTree(int n = 0)
   : child(n, {-1, -1}), par(n, -1),
     prev(n, -1), flip(n, -1), size(n, 1) {}
 void push(int x) {
  if (x >= 0 && flip[x]) {
   flip[x] = 0;
    swap(child[x][0], child[x][1]);
    each (e, child[x]) if (e>=0) flip[e] ^= 1;
  } // + any other lazy path operations
 } // bae2
 void update(int x) {
  if (x >= 0) {
   size[x] = 1;
    each (e, child[x]) if (e >= 0)
     size[x] += size[e];
  } // + any other path aggregates
 } // 8ec0
 void auxLink(int p, int i, int ch) {
  child[p][i] = ch;
  if (ch \ge 0) par[ch] = p;
  update(p);
 } // 0a9a
 void rot(int p, int i) {
  int x = child[p][i], g = par[x] = par[p];
  if (q \ge 0) child [q] [child [q] [1] == p] = x;
  auxLink(p, i, child[x][!i]);
  auxLink(x, !i, p);
  swap(prev[x], prev[p]);
  update(q);
 1 // 4c76
 void splay(int x) {
  while (par[x] >= 0) {
   int p = par[x], g = par[p];
    push(q); push(p); push(x);
    bool f = (child[p][1] == x);
    if (a >= 0) {
     if (child[g][f] == p) { // zig-zig
      rot (g, f); rot (p, f);
     } else { // zig-zag
      rot (p, f); rot (g, !f);
     } // 2ebb
```

```
} else { // zig
     rot (p, f);
   } // f8a2
  } // 446b
  push(x);
 } // 55a7
 // After this operation x becomes the end
 // of preferred path starting in root;
 void access(int x) { // amortized O(lg n)
  while (true) {
   splay(x);
    int p = prev[x];
   if (p < 0) break:
    prev[x] = -1;
    splay(p);
    int r = child[p][1];
   if (r \ge 0) swap(par[r], prev[r]);
   auxLink(p, 1, x);
  } // 2b87
 } // 30be
 // Make x root of its tree; amortized O(lq n)
 void makeRoot(int x) {
  access(x);
  int& l = child[x][0];
  if (1 >= 0) {
    swap(par[1], prev[1]);
    flip[1] ^= 1;
    update(1);
   1 = -1:
   update(x);
  } // 0064
 } // b246
 // Find root of tree containing x
 int find(int x) { // time: amortized O(lq n)
  access(x):
  while (child[x][0] >= 0)
   push(x = child[x][0]);
  splay(x);
  return x;
 } // d78d
 // Add edge x-y; time: amortized O(lg n)
 // Root of tree containing y becomes
 // root of new tree.
 void link(int x, int v) {
 makeRoot(x); prev[x] = y;
 } // fb4f
 // Remove edge x-v; time: amortized O(lg n)
 // x and v become roots of new trees!
 void cut(int x, int y) {
  makeRoot(x); access(y);
  par[x] = child[y][0] = -1;
  update(y);
 } // 1908
 // Get distance between x and y,
 // returns INF if x and y there's no path.
 // This operation makes x root of the tree!
 int dist(int x, int y) { // amortized O(lg n)
  makeRoot(x);
  if (find(y) != x) return INF;
  access(y);
  int t = child[y][0];
  return t >= 0 ? size[t] : 0;
 } // ae69
}; // 4480
```

```
util/arc interval cover.h
                                          7507
using dbl = double;
// Find size of smallest set of points
// such that each arc contains at least one
// of them; time: O(n lg n)
int arcCover(vector<pair<dbl, dbl>>& inters,
        dbl wrap) {
 int n = sz(inters);
 rep(i, 0, n) {
  auto& e = inters[i];
  e.x = fmod(e.x, wrap);
  e.y = fmod(e.y, wrap);
  if (e.x < 0) e.x += wrap, e.y += wrap;</pre>
  if (e.x > e.y) e.x += wrap;
  inters.pb({e.x+wrap, e.y+wrap});
 } // b87d
 Vi nxt(n);
 deque<dbl> que:
 dbl r = wrap*4;
 sort(all(inters));
 for (int i = n*2-1; i--;) {
  r = min(r, inters[i].y);
  que.push front(inters[i].x);
  while (!que.empty() && que.back() > r)
   que.pop back();
  if (i < n) nxt[i] = i+sz(que);</pre>
 1 // 5e6c
 int a = 0, b = 0;
 do {
  a = nxt[a] % n;
  b = nxt[nxt[b]%n]%n;
 } while (a != b);
 int ans = 0;
 while (b < a+n) {
  b += nxt [b%n] - b%n;
  ans++;
 } // 7350
 return ans;
) // 7871
util/bit hacks.h
                                          599a
// __builtin_popcount - count number of 1 bits
// builtin clz - count most significant 0s
// builtin ctz - count least significant Os
// __builtin_ffs - like ctz, but indexed from 1
                   returns 0 for 0
// For 11 version add 11 to name
using ull = uint64_t;
#define T64(s.up)
 for (ull i=0; i<64; i+=s*2)
    for (ull j = i; j < i+s; j++) {
      ull \ a = (M[j] >> s) \& up;
      ull \ b = (M[j+s] \& up) << s;
      M[j] = (M[j] \& up) / b;
      M[j+s] = (M[j+s] & (up << s)) | a; 
    } // a290
// Transpose 64x64 bit matrix
void transpose64 (arrav<ull, 64>& M) {
 T64(1, 0x555555555555555);
 T64(4, 0xF0F0F0F0F0F0F0F);
 T64(8, 0xFF00FF00FF00FF);
 T64 (16, 0xFFFF0000FFFF);
```

```
T64 (32, OxFFFFFFFFLL);
} // 6889
// Lexicographically next mask with same
// amount of ones.
int nextSubset(int v) {
 int t = v | (v - 1);
 return (t + 1) | (((~t & -~t) - 1) >>
    ( builtin ctz(v) + 1));
} // 4c0c
                                           09f9
util/bump alloc.h
// Allocator, which doesn't free memory.
char mem[400<<20]; // Set memory limit</pre>
size_t nMem;
void* operator new(size_t n) {
nMem += n; return &mem[nMem-n];
} // fba6
void operator delete(void*) {}
util/compress vec.h
                                           bc5d
// Compress integers to range [0;n) while
// preserving their order; time: O(n lg n)
// Returns mapping: compressed -> original
Vi compressVec(vector<int*>& vec) {
 sort (all (vec).
  [](int* l, int* r) { return *l < *r; });
 Vi old;
 each (e, vec) {
  if (old.emptv() | old.back() != *e)
   old.pb(\stare);
  *e = sz(old) -1;
 1 // 7eb0
 return old;
} // 2b60
util/inversion vector.h
                                           0.1 + 9
// Get inversion vector for sequence of
// numbers in [0;n); ret[i] = count of numbers
// greater than perm[i] to the left; O(n lg n)
Vi encodeInversions (Vi perm) {
 Vi odd, ret(sz(perm));
 int cont = 1;
 while (cont) {
  odd.assign(sz(perm)+1, 0);
  cont = 0;
  rep(i, 0, sz(perm)) {
   if (perm[i] % 2) odd[perm[i]]++;
   else ret[i] += odd[perm[i]+1];
   cont += perm[i] /= 2;
  } // 4ed0
 } // a4f0
 return ret:
} // c2e1
// Count inversions in sequence of numbers
// in [0:n); time: O(n lq n)
11 countInversions(Vi perm) {
 11 \text{ ret} = 0, cont = 1;
 Vi odd:
 while (cont) {
  odd.assign(sz(perm)+1, 0);
  cont = 0:
  rep(i, 0, sz(perm)) {
   if (perm[i] % 2) odd[perm[i]]++;
   else ret += odd[perm[i]+1];
```

```
cont += perm[i] /= 2;
  } // 916f
 } // c9b5
return ret;
} // laaf
util/longest inc subseq.h
                                          0bd1
// Longest Increasing Subsequence; O(n lg n)
int lis(const Vi& seg) {
Vi dp(sz(seq), INT_MAX);
 each (c, seq) *lower_bound(all(dp), c) = c;
 return int(lower_bound(all(dp), INT_MAX)
        - dp.begin());
} // d0e9
util/max rects.h
                                          2a16
struct MaxRect {
// begin = first column of rectangle
// end = first column after rectangle
// hei = height of rectangle
// touch = columns of height hei inside
 int begin, end, hei;
Vi touch; // sorted increasing
}; // 41fe
// Given consecutive column heights find
// all inclusion-wise maximal rectangles
// contained in "drawing" of columns; time O(n)
vector<MaxRect> getMaxRects(Vi hei) {
hei.insert (hei.begin(), -1);
 hei.pb(-1);
 Vi reach (sz (hei), sz (hei)-1);
 vector < MaxRect > ans;
 for (int i = sz(hei)-1; --i;) {
  int j = i+1, k = i;
  while (hei[j] > hei[i]) j = reach[j];
  reach[i] = j;
  while (hei[k] > hei[i-1]) {
   ans.pb({ i-1, 0, hei[k], {} });
    auto& rect = ans.back();
    while (hei[k] == rect.hei) {
     rect.touch.pb(k-1);
     k = reach[k];
   } // 6e7e
   rect.end = k-1;
  } // e03f
} // 2796
return ans:
} // Oe49
util/mo.h
// Modified MO's queries sorting algorithm,
// slightly better results than standard.
// Allows to process q queries in O(n*sqrt(q))
struct Query {
int begin, end;
1; // b76d
// Get point index on Hilbert curve
11 hilbert(int x, int y, int s, 11 c = 0) {
if (s <= 1) return c;</pre>
 s /= 2; c *= 4;
 if (y < s)
  return hilbert (x&(s-1), y, s, c+(x>=s)+1);
 if (x < s)
  return hilbert (2*s-y-1, s-x-1, s, c);
 return hilbert (y-s, x-s, s, c+3);
```

```
1 // Ofb9
// Get good order of queries; time: O(n lg n)
Vi moOrder (vector<Query> € queries, int maxN) {
int s = 1:
 while (s < maxN) s \star= 2;
 vector<11> ord;
 each (q, queries)
  ord.pb(hilbert(q.begin, q.end, s));
 Vi ret(sz(ord));
 iota(all(ret), 0);
 sort(all(ret), [&](int l, int r) {
  return ord[1] < ord[r];</pre>
 }); // 9aea
return ret;
} // ecec
util/parallel binsearch.h
                                           bc5d
// Run `n` binary searches on [b;e] parallely.
// `cmp` should be lambda with arguments:
// 1) vector<Pii>& - pairs (v, i)
      which are queries if value for index i
      is greater or equal to v;
     pairs are sorted by v
// 2) vector<bool>& - output vector,
     set true at index i if value
      for i-th query is >= queried value
// Returns vector of found values;
// time: O((n+c) lg range), where c is cmp time
template<class T>
Vi multiBS(int b, int e, int n, T cmp) {
 vector<Pii> que(n), rng(n, {b, e});
 vector<bool> ans(n);
 rep(i, 0, n) que[i] = \{(b+e)/2, i\};
 for (int k = 32-__builtin_clz(e-b); k--;) {
  int last = 0, j = 0;
  cmp (que, ans);
  rep(i, 0, sz(que)) {
   Pii &q = que[i], &r = rng[q.y];
   if (q.x != last) last = q.x, j = i;
    (ans[i] ? r.x : r.y) = q.x;
   q.x = (r.x+r.y) / 2;
   if (!ans[i]) swap(que[i], que[j++]);
  } // 6c4e
 } // 622c
 each (p, rng) ret.pb(p.x);
 return ret;
} // lad7
util/radix sort.h
                                           6fb4
// Stable countingsort; time: O(k+sz(vec))
// See example usage in radixSort for pairs.
template<class F>
void countSort(Vi& vec, F key, int k) {
 static Vi buf, cnt;
 vec.swap(buf);
 vec.resize(sz(buf));
 cnt.assign(k+1, 0);
 each (e, buf) cnt[key(e)]++;
 rep(i, 1, k+1) cnt[i] += cnt[i-1];
 for (int i = sz(vec)-1; i >= 0; i--)
  vec[--cnt[key(buf[i])]] = buf[i];
} // cc6f
// Compute order of elems, k is max key; O(n)
```

Vi radixSort (const vector < Pii> € elems, int k) {

```
Vi order(sz(elems));
iota(all(order), 0);
countSort(order,
    [5](int i) { return elems[i].y; }, k);
countSort(order,
    [5](int i) { return elems[i].x; }, k);
return order;
} // e8f6
```