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scripts.sh1

```
#!/bin/bash
set -e

# > Build
g++ -Wall -Wextra -Wshadow -Wformat=2 -Wfloat-equal -Wconversion -pedantic \
    -Wlogical-op -O2 -std=c++11 -o $1.e $1.cpp

# Debug flags: -fsanitize=address -fsanitize=undefined -D_FORTIFY_SOURCE=2 \
#              -D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC

# Mac fix:      -fvisibility=hidden
# Stack limit: -Wl,-stack_size -Wl,16000000 -Wl,-no_pie

# > Compare
./build.sh $1; ./build.sh $2; ./build.sh $3

while ;; do
    $3.e > cmp.in; echo -n 0
    $1.e < cmp.in > prog1.out; echo -n 1
    $2.e < cmp.in > prog2.out; echo -n 2
    diff prog1.out prog2.out
    echo -n Y
done
```

template.h2

```
#include <bits/stdc++.h>
using namespace std;

using ll    = int64_t;
using ull   = uint64_t;
using ld    = long double;
using cmpl  = complex<double>;

#define IT iterator

#define rep(i, b, e)   for (int i = int(b); i < int(e); i++)
#define repd(i, b, e) for (int i = int(b); i >= int(e); i--)
#define each(a, x)     for (auto& a : x)
#define all(x)         (x).begin(), (x).end()
#define sz(x)          int((x).size())

#define gcd             __gcd
#define popcount        __builtin_popcount
```

math/bellman\_inequalities.h3

```
struct Constraint {
    ll a, b, limit; // a - b >= limit
};

bool solveIneq(vector<Constraint>& edges, vector<ll>& vars) {
    rep(i, 0, sz(vars)) each(e, edges) vars[e.b] = min(vars[e.b], vars[e.a] - e.limit);
    each(e, edges) if (vars[e.a] - e.limit < vars[e.b]) return false;
    return true;
}
```

math/fft.h4

```
vector<cmpl> bases;

void initFft(int size) {
    bases.resize(size+1);
    rep(i, 0, size+1) bases[i] = exp(cmpl(0, 2*M_PI*i/size));
}

template<bool inv>
void fft(vector<cmpl>::IT in, vector<cmpl>::IT out, int size, int step = 1) {
    if (size == 1) { *out = *in; return; }
```

```
    fft<inv>(in, out, size/2, step*2);
    fft<inv>(in+step, out+size/2, size/2, step*2);

    rep(i, 0, size/2) {
        auto t = out[i], m = bases[(inv ? i : size-i)*step];
        out[i] = t + out[i+size/2]*m;
        out[i+size/2] = t - out[i+size/2]*m;
    }
}

template<bool inv>
vector<cmpl> fft(vector<cmpl>& in) {
    vector<cmpl> out(sz(in));
    fft<inv>(in.begin(), out.begin(), sz(in));
    if (inv) each(x, out) x /= sz(in);
    return out;
}
```

math/mod\_inv.h5

```
template<class T>
T modInv(T a, T b) {
    T u = 1, v = 0, x = 0, y = 1, m = b;

    while (a > 0) {
        T q = b / a, r = b % a;
        T m = x - u*q, n = y - v*q;
        b = a; a = r; x = u; y = v; u = m; v = n;
    }
    return (b == 1 ? (x < 0 ? x+m : x) : 0);
}
```

math/montgomery.h6

```
#include "mod_inv.h"

constexpr ll MG_SHIFT = 32;
constexpr ll MG_MULT  = 1LL << MG_SHIFT;
constexpr ll MG_MASK  = MG_MULT - 1;

ll getMgInv(ll mod) { return MG_MULT - modInv(mod, MG_MULT); }
ll mgShift(ll n, ll mod) { return (n * MG_MULT) % mod; } // Precompute multipliers

ll redc(ll n, ll mod, ll mgInv) {
    ll quot = (n * mgInv) & MG_MASK;
    n = (n + quot*mod) >> MG_SHIFT;
    return (n >= mod ? n-mod : n);
}

// MOD < MG_MULT, gcd(MG_MULT, MOD) must be 1
// mgRedc(mgForm1 * mgForm2) = Montgomery-form product
// mgRedc(notMgForm1 * mgForm2) = normal number
```

math/sieve.h7

```
constexpr int MAX_P = 1000000;

vector<int> primes(MAX_P+1);

void sieve() {
    primes[0] = 0;
    primes[1] = 1;

    for (int i = 2; i*i <= MAX_P; i++) {
        if (primes[i]) continue;
        for (int j = i*i; j <= MAX_P; j += i) if (!primes[j]) primes[j] = i;
    }

    rep(i, 2, MAX_P+1) if (!primes[i]) primes[i] = i;
}
```

structures/interval\_tree.h8

```

struct IntervalTree {
    using T = int;

    // (+, max)
    static constexpr T T_IDENT = INT_MIN;
    #define opModify(x, y) ((x)+(y))
    #define opQuery(x, y)  max(x, y)
    #define opTimes(x, t)  (x)

    // (max, max)
    // static constexpr T T_IDENT = INT_MIN;
    // #define opModify(x, y) max(x, y)
    // #define opQuery(x, y)  max(x, y)
    // #define opTimes(x, t)  (x)

    // (+, +)
    // static constexpr T T_IDENT = 0;
    // #define opModify(x, y) ((x)+(y))
    // #define opQuery(x, y)  ((x)+(y))
    // #define opTimes(x, t)  ((x)*(t))

    // (=, max)
    // static constexpr T T_IDENT = INT_MIN;
    // #define opQuery(x, y)  max(x, y)
    // #define opTimes(x, t)  (x)

    struct Node {
        T val{0}, extra{0};
        int nEqual{1}; // EXTENSION: MIN/MAX ELEMENT COUNT
        bool current{false}; // EXTENSION: (=, ?) TREE
    };

    vector<Node> tree;
    int len;

    IntervalTree(int size) {
        for (len = 1; len < size; len *= 2);
        tree.resize(len*2);

        // EXTENSION: MIN/MAX ELEMENT COUNT
        repd(i, len-1, 0) tree[i].nEqual = tree[i*2].nEqual + tree[i*2+1].nEqual;
    }

    // WITHOUT MIN/MAX ELEMENT COUNT
    T query(int vStart, int vFinish, int i = 1, int begin = 0, int end = -1) {
        if (end < 0) end = len;
        // push(i, begin, end); // EXTENSION: (=, ?) TREE

        if (vStart >= vFinish || vFinish <= begin || end <= vStart) return T_IDENT;
        if (vStart <= begin && end <= vFinish) return tree[i].val;

        int mid = (begin + end) / 2;
        T tmp = opQuery(query(vStart, vFinish, i*2, begin, mid),
                        query(vStart, vFinish, i*2+1, mid, end));

        // return tmp; // EXTENSION: (=, ?) TREE -> USE THIS INSTEAD OF FOLLOWING LINE
        return opModify(tmp, opTimes(tree[i].extra, min(end, vFinish)-max(begin, vStart)));
    }

    // EXTENSION: MIN/MAX ELEMENT COUNT -> USE THIS INSTEAD OF ABOVE
    T query2(int vStart, int vFinish, int& count, int i = 1, int begin = 0, int end = -1) {
        if (end < 0) end = len;
        if (vStart >= vFinish || vFinish <= begin || end <= vStart) return T_IDENT;
        // push(i, begin, end); // EXTENSION: (=, ?) TREE

        if (vStart <= begin && end <= vFinish) {
            count = tree[i].nEqual;
            return tree[i].val;
        }
    }

```

```

    int eq1 = 0, eq2 = 0, mid = (begin + end) / 2;
    T v1 = query2(vStart, vFinish, eq1, i*2, begin, mid);
    T v2 = query2(vStart, vFinish, eq2, i*2+1, mid, end);
    T tmp = opQuery(v1, v2);

    count = (v1 == tmp ? eq1 : 0) + (v2 == tmp ? eq2 : 0);
    // return tmp; // EXTENSION: (=, ?) TREE -> USE THIS INSTEAD OF FOLLOWING LINE
    return opModify(tmp, opTimes(tree[i].extra, min(end, vFinish)-max(begin, vStart)));
}

// FOR NON-(=, ?) TREE
void modify(int vStart, int vFinish, T val, int i = 1, int begin = 0, int end = -1) {
    if (end < 0) end = len;
    if (vFinish <= begin || end <= vStart) return;

    if (vStart > begin || end > vFinish) {
        int mid = (begin + end) / 2;
        modify(vStart, vFinish, val, i*2, begin, mid);
        modify(vStart, vFinish, val, i*2+1, mid, end);
    } else {
        tree[i].extra = opModify(tree[i].extra, val);
    }

    if (i < len) tree[i].val = opModify(opQuery(tree[i*2].val, tree[i*2+1].val),
                                        opTimes(tree[i].extra, end-begin));
    else tree[i].val = tree[i].extra;

    // EXTENSION: MIN/MAX ELEMENT COUNT
    tree[i].nEqual = (i >= len);
    if (i < len) {
        T tmp = opQuery(tree[i*2].val, tree[i*2+1].val);
        if (tmp == tree[i*2].val) tree[i].nEqual += tree[i*2].nEqual;
        if (tmp == tree[i*2+1].val) tree[i].nEqual += tree[i*2+1].nEqual;
    }
}

// EXTENSION: (=, ?) TREE -> USE THIS INSTEAD OF ABOVE
void modify2(int vStart, int vFinish, T val, int i = 1, int begin = 0, int end = -1) {
    if (end < 0) end = len;
    if (vFinish <= begin || end <= vStart) return;
    push(i, begin, end);

    if (vStart > begin || end > vFinish) {
        int mid = (begin + end) / 2;
        modify2(vStart, vFinish, val, i*2, begin, mid);
        modify2(vStart, vFinish, val, i*2+1, mid, end);
    } else {
        tree[i].extra = val;
        tree[i].val = opTimes(val, end-begin);
        tree[i].current = true;
        tree[i].nEqual = end-begin; // EXTENSION: MIN/MAX ELEMENT COUNT
        return;
    }

    if (i < len) tree[i].val = opQuery(tree[i*2].val, tree[i*2+1].val);

    // EXTENSION: MIN/MAX ELEMENT COUNT
    tree[i].nEqual = (i >= len);
    if (i < len) {
        T tmp = opQuery(tree[i*2].val, tree[i*2+1].val);
        if (tmp == tree[i*2].val) tree[i].nEqual += tree[i*2].nEqual;
        if (tmp == tree[i*2+1].val) tree[i].nEqual += tree[i*2+1].nEqual;
    }
}

// EXTENSION: (=, ?) TREE
void push(int i, int begin, int end) {
    if (!tree[i].current || i >= len) return;
    tree[i*2].val = tree[i*2+1].val = opTimes(tree[i].extra, (end-begin)/2);
    tree[i*2].extra = tree[i*2+1].extra = tree[i].extra;
    tree[i*2].current = tree[i*2+1].current = true;
}

```

```

tree[i].current    = false;

// EXTENSION: MIN/MAX ELEMENT COUNT
tree[i*2].nEqual = tree[i*2+1].nEqual = (end-begin)/2;
}
};

```

## structures/pairing\_heap.h

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```

template<class T, class Cmp = less<T>>
struct PHeap {
    struct Node;
    using NodeP = unique_ptr<Node>; // Or use single_ptr + bump allocator

    struct Node {
        T val;
        NodeP child{nullptr}, next{nullptr};
        Node* prev{nullptr};

        Node(T x = T()) { val = x; }

        NodeP moveChild() {
            if (child) child->prev = nullptr;
            return move(child);
        }

        NodeP moveNext() {
            if (next) next->prev = nullptr;
            return move(next);
        }

        void setChild(NodeP v) {
            if (child) child->prev = nullptr;
            child = move(v);
            if (child) child->prev = this;
        }

        void setNext(NodeP v) {
            if (next) next->prev = nullptr;
            next = move(v);
            if (next) next->prev = this;
        }
    };

    NodeP root{nullptr};

    NodeP merge(NodeP l, NodeP r) {
        if (!l) return move(r);
        if (!r) return move(l);

        if (Cmp()(l->val, r->val)) swap(l, r);

        l->setNext(r->moveChild());
        r->setChild(move(l));
        return move(r);
    }

    NodeP mergePairs(NodeP v) {
        if (!v || !v->next) return v;
        NodeP v2 = v->moveNext(), v3 = v2->moveNext();
        return merge(merge(move(v), move(v2)), mergePairs(move(v3)));
    }

    Node* push(const T& x) {
        NodeP tmp(new Node(x));
        auto ret = &*tmp;
        root = merge(move(root), move(tmp));
        return ret;
    }

    void decrease(Node* v, T val) {

```

```

assert(!Cmp()(v->val, val));
v->val = val;

    auto prev = v->prev;
    if (!prev) return;
    NodeP uniq;

    if (&*v->prev->child == v) {
        uniq = prev->moveChild();
        prev->setChild(v->moveNext());
    } else {
        uniq = prev->moveNext();
        prev->setNext(v->moveNext());
    }

    root = merge(move(root), move(uniq));
}

bool    empty()           { return !root; }
const T& top()            { return root->val; }
void    merge(PHeap&& r)  { root = merge(move(root), move(r.root)); r.root = nullptr; }
void    pop()             { root = mergePairs(root->moveChild()); }
};

```

## trees/centroid\_decomp.h

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```

struct Vert {
    vector<Vert*> edges, cEdges;
    vector<int> dists;
    Vert* cParent{nullptr};
    int cDepth{-1}, cSize{0}, cState{0};
};

void dfsSize(Vert* v, int depth) {
    v->cDepth = depth;
    v->cSize = 1;
    v->cState = 0;

    each(e, v->edges) if (e->cState <= 1 && e->cDepth < depth) {
        dfsSize(e, depth);
        v->cSize += e->cSize;
    }
}

void dfsDist(Vert* v, int dist) {
    v->dists.push_back(dist);
    v->cState = 1;
    each(e, v->edges) if (!e->cState) dfsDist(e, dist+1);
}

Vert* centroidDecomp(Vert* v, int depth, Vert* root = 0) {
    dfsSize(v, depth);

    int size = v->cSize;
    Vert *parent = 0, *heavy = 0;

    while (true) {
        int hSize = 0;

        each(e, v->edges) if (e != parent && e->cDepth == depth && hSize < e->cSize) {
            hSize = e->cSize;
            heavy = e;
        }

        if (hSize <= size/2) break;
        parent = v; v = heavy;
    }

    v->cParent = root;
    dfsDist(v, 0);
    v->cSize = size;

```

```

v->cState = 2;

each(e, v->edges) if (e->cDepth == depth) {
    v->cEdges.push_back(centroidDecomp(e, depth+1, v));
}
return v;
}

```

## util/alloc.h

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```

char memPool[512*1024*1024];
int memOffset;

void* operator new(size_t n) { memOffset += n; return &memPool[memOffset-n]; }
void operator delete(void*) {}

// unique_ptr without deallocation
template<typename T>
struct single_ptr {
    T* elem{0};

    single_ptr() {}
    single_ptr(nullptr_t) {}
    single_ptr(T* v) : elem(v) {}
    single_ptr(single_ptr&& r) : elem(r.elem) { r.elem = 0; }

    single_ptr& operator=(nullptr_t) { elem = 0; return *this; }
    single_ptr& operator=(single_ptr&& r) { elem = r.elem; r.elem = 0; return *this; }

    T* operator->() { return elem; }
    T& operator*() { return *elem; }
    operator bool() { return elem; }
};

```