.bashrc	1	math/sieve.h	9	util/longest_inc_subseq.h	18
.vimrc	1	math/sieve_factors.h	9	util/max_rects.h	18
template.cpp	1	math/sieve_segmented.h	9	util/mo.h	18
various.h	1	structures/bitset_plus.h	10	util/parallel_binsearch.h	18
<pre>geometry/convex_hull.h</pre>	1	structures/fenwick_tree.h	10		18
<pre>geometry/convex_hull_dist.h</pre>	1	structures/fenwick_tree_2d.h	10		
<pre>geometry/convex_hull_sum.h</pre>	1	structures/find_union.h	10		
geometry/halfplanes.h	1	structures/hull_offline.h	10		
geometry/line2.h	2	structures/hull_online.h	10		
geometry/rmst.h	2	structures/max_queue.h	10		
geometry/segment2.h	2	structures/pairing_heap.h	10		
geometry/vec2.h	3	structures/rmq.h	11		
graphs/2sat.h	3	structures/segtree_config.h	11		
graphs/bellman_ineq.h	3	structures/segtree_general.h	11		
graphs/bridges_online.h	3	structures/segtree_persist.h	12		
graphs/dense_dfs.h	3	structures/segtree_point.h	12		
graphs/edmonds_karp.h	4	structures/treap.h	12		
graphs/gomory_hu.h	4	structures/wavelet_tree.h	13		
graphs/matroids.h	4	structures/ext/hash_table.h	13		
graphs/push_relabel.h	5	structures/ext/rope.h	13		
graphs/scc.h	5	structures/ext/tree.h	13		
graphs/turbo_matching.h	5	structures/ext/trie.h	13		
math/berlekamp_massey.h	5	text/aho_corasick.h	13		
math/bit_gauss.h	6	text/kmp.h	13		
math/bit_matrix.h	6	text/kmr.h	14		
math/crt.h	6	text/lcp.h	14		
math/discrete_logarithm.h	6	text/lyndon_factorization.h	14		
math/fft_complex.h	6	text/main_lorentz.h	14		
math/fft_mod.h	7	text/manacher.h	14		
math/fwht.h	7	text/min_rotation.h	14		
math/gauss.h	7	text/palindromic_tree.h	14		
math/matrix.h	7	text/suffix_array_linear.h	15		
math/miller_rabin.h	8	text/suffix_automaton.h	15		
math/modinv_precompute.h	8	text/suffix_tree.h	15		
math/modular.h	8	text/z_function.h	16		
math/modular64.h	8	trees/centroid_decomp.h	16		
math/montgomery.h	8	trees/heavylight_decomp.h	16		
math/nimber.h	8	trees/lca.h	16		
math/phi_large.h	9	trees/link_cut_tree.h	17		
math/phi_precompute.h	9	util/arc_interval_cover.h	17		
math/phi_prefix_sum.h	9	util/bit_hacks.h	17		
math/pi_large_precomp.h	9	util/bump_alloc.h	17		
math/pollard_rho.h	9	util/compress_vec.h	18		
math/polynomial_interp.h	9	util/inversion_vector.h	18		

```
ef12
.bashrc
build()(
  q++ $0 -o $1.e -DLOC -std=c++11
      -Wall -Wextra -Wfatal-errors -Wshadow \
      -Wlogical-op -Wconversion -Wfloat-equal
b() ( build $@ -02 )
d() ( build $@ -fsanitize=address, undefined \
              -D_GLIBCXX_DEBUG -q )
run()($1 $2 && echo start >&2 && time ./$2.e)
100()(
  set -e; $1 $2; $1 $3
  for ((;;)) {
    ./$3.e > gen.in
    time ./$2.e < gen.in > gen.out
cmp()(
  set -e; $1 $2; $1 $3; $1 $4
  for ((;;)) {
                             echo -n 0
    ./$4.e > gen.in;
    ./$2.e < gen.in > p1.out; echo -n 1
    ./$3.e < gen.in > p2.out; echo -n 2
    diff pl.out p2.out;
                             echo -n Y
# Other flags:
# -Wformat=2 -Wshift-overflow=2 -Wcast-qual
# -Wcast-align -Wduplicated-cond
# -D_GLIBCXX_DEBUG_PEDANTIC -D_FORTIFY SOURCE=2
# -fno-sanitize-recover -fstack-protector
                                        aaf7
.vimrc
se ai aw cin cul ic is nocp nohls nu sc scs
se bg=dark sw=4 ts=4 so=7 ttm=9
ca hash w !cpp -dD -P -fpreprocessed \|
  tr -d '[:space:]' \| md5sum \| cut -c-4
template.cpp
                                        b508
#include <bits/stdc++.h>
using namespace std;
using 11 = long long;
using Vi = vector<int>;
using Pii = pair<int,int>;
#define mp make_pair
#define pb push_back
#define x first
#define y second
#define rep(i,b,e) for(int i=(b); i<(e); i++)
#define each(a,x) for(auto& a : (x))
#define all(x)
                   (x).begin(),(x).end()
#define sz(x)
                   int((x).size())
int main() {
  cin.svnc with stdio(0); cin.tie(0);
```

```
cout << fixed << setprecision(18);</pre>
 return 0;
1 // 9974
// > Debug printer
#define tem template<class t,class u,class...w>
#define pri(x,y,z)tem auto operator<<(t&o,u a) \
 ->decltype(x,o) { o << z; return o << y; }
pri(a.print(), '}', '{'; a.print())
pri(a.y, ')', '(' << a.x << ", " << a.y)
pri(all(a), ']', '['; auto d="";
 for (auto i : a) (o << d << i, d = ", "))
void DD(...) {}
tem void DD(t s, u a, w... k) {
 for (int b=1; *s && *s - b*44; cerr << *s++)
   b += 2 / (*s*2 - 81);
 cerr << ": " << a << *s++; DD(s, k...);
} // fd6d
#ifdef LOC
#define deb(...) (DD("[,\b :] "#__VA_ARGS__, \
 __LINE__, __VA_ARGS__), cerr << endl)
#else
#define deb(...)
#endif
#define DBP(...) void print() { \
 DD(#__VA_ARGS__, __VA_ARGS__); } // 813f
// > Utils
// Return smallest k such that 2^k > n
// Undefined for n = 0!
int uplg(int n) { return 32-_builtin_clz(n); }
int uplq(ll n) { return 64- builtin clzll(n); }
// Compare with certain epsilon (branchless)
// Returns -1 if a < b; 1 if a > b; 0 if equal
// a and b are assumed equal if |a-b| <= eps</pre>
int cmp(double a, double b, double eps=1e-10) {
 return (a > b+eps) - (a+eps < b);
} // 81c1
various.h
                                         cbc4
// If math constants like M_PI are not found
// add this at the beginning of file
#define _USE_MATH_DEFINES
#pragma GCC optimize("Ofast,unroll-loops,
                      no-stack-protector")
#pragma GCC target("popcnt,avx,tune=native")
while (clock() < duration *CLOCKS PER SEC)
// Automatically implement operators:
// 1. != if == is defined
// 2. >, <= and >= if < is defined
using namespace rel ops;
// Mersenne twister for randomization.
```

```
mt19937 64 rnd(chrono::steady clock::now()
  .time since epoch().count());
// To shuffle randomly use:
shuffle(all(vec), rnd)
// To pick random integer from [A;B] use:
uniform int_distribution <> dist(A, B);
int value = dist(rnd);
// To pick random real number from [A;B] use:
uniform real distribution <> dist(A, B);
double value = dist(rnd);
geometry/convex hull.h
                                        66a8
#include "vec2.h"
// Translate points such that lower-left point
// is (0, 0). Returns old point location; O(n)
vec2 normPos(vector<vec2>€ points) {
 auto q = points[0].yxPair();
  each (p, points) q = min(q, p.yxPair());
 vec2 ret{q.y, q.x};
  each (p, points) p = p-ret;
 return ret:
} // 193b
// Find convex hull of points; time: O(n lq n)
// Points are returned counter-clockwise.
vector<vec2> convexHull(vector<vec2> points) {
 vec2 pivot = normPos(points);
  sort(all(points));
  vector<vec2> hull;
  each (p, points) {
    while (sz(hull) >= 2) {
      vec2 a = hull.back() - hull[sz(hull)-2];
      vec2 b = p - hull.back();
      if (a.cross(b) > 0) break;
      hull.pop_back();
    } // ad91
    hull.pb(p);
 } // 5908
  // Translate back, optional
  each (p, hull) p = p+pivot;
 return hull;
} // 62ed
geometry/convex hull dist.h 2859
#include "vec2.h"
// Check if p is inside convex polygon. Hull
// must be given in counter-clockwise order.
// Returns 2 if inside, 1 if on border,
// 0 if outside; time: O(n)
int insideHull(vector<vec2>& hull, vec2 p) {
 int ret = 1;
  rep(i, 0, sz(hull)) {
    auto v = hull[(i+1)%sz(hull)] - hull[i];
    auto t = v.cross(p-hull[i]);
    ret = min(ret, cmp(t, 0)); // For doubles
    //ret = min(ret, (t>0) - (t<0)); // Ints
  } // Od40
  return int(max(ret+1, 0));
                                                 #include "line2.h"
```

```
} // 1f39
#include "seament2.h"
// Get distance from point to hull; time: O(n)
double hullDist(vector<vec2>& hull, vec2 p) {
 if (insideHull(hull, p)) return 0;
 double ret = 1e30;
 rep(i, 0, sz(hull)) {
   seg2 seg{hull[(i+1)%sz(hull)], hull[i]};
   ret = min(ret, seg.distTo(p));
 } // f3be
 return ret:
} // a00c
// Compare distance from point to hull
// with sart(d2); time: O(n)
// -1 if smaller, 0 if equal, 1 if greater
int cmpHullDist(vector<vec2>€ hull,
               vec2 p, 11 d2) {
 if (insideHull(hull,p)) return (d2<0)-(d2>0);
 int ret = 1:
 rep(i, 0, sz(hull)) {
   seg2 seg{hull[(i+1)%sz(hull)], hull[i]};
   ret = min(ret, seg.cmpDistTo(p, d2));
 } // 28cb
 return ret;
} // 30f3
geometry/convex hull sum.h
#include "vec2.h"
// Get edge sequence for given polygon
// starting from lower-left vertex; time: O(n)
// Returns start position.
vec2 edgeSeg(vector<vec2> points,
            vector<vec2>& edges) {
 int i = 0, n = sz(points);
 rep(j, 0, n) {
   if (points[i].yxPair()>points[j].yxPair())
     i = j;
 } // 14e2
 rep(j, 0, n) edges.pb(points[(i+j+1)%n] -
                        points[(i+j)%n]);
 return points[i]:
} // 20e2
// Minkowski sum of given convex polygons.
// Vertices are required to be in
// counter-clockwise order; time: O(n+m)
vector<vec2> hullSum (vector<vec2> A,
                    vector<vec2> B) {
 vector\langle vec2 \rangle sum, e1, e2, es(sz(A) + sz(B));
 vec2 pivot = edgeSeg(A, e1) + edgeSeg(B, e2);
 merge(all(e1), all(e2), es.begin());
 sum.pb(pivot);
 each (e, es) sum.pb(sum.back() + e);
 sum.pop back();
 return sum;
} // f183
geometry/halfplanes.h
                                        78b5
#include "vec2.h"
```

```
// Intersect given halfplanes and output
// hull vertices to out.
// Returns 0 if intersection is empty,
// 1 if intersection is non-empty and bounded.
// 2 if intersection is unbounded.
// Output vertices are valid ONLY IF
// intersection is non-empty and bounded.
// Works only with floating point vec2/line2.
// CURRENTLY DOESN'T WORK FOR NON-EMPTY
// AND UNBOUNDED CASES!
int intersectHalfPlanes(vector<line2> lines,
                        vector<vec2>& out) {
  deque<line2> H:
  out.clear():
  if (sz(lines) <= 1) return 2;</pre>
  sort(all(lines), [](line2 a, line2 b) {
    int t = cmp(a.norm.angle(),b.norm.angle());
    return t ? t < 0 : cmp(a.off*b.norm.len(),</pre>
      b.off*a.norm.len()) < 0;
  }); // dfa1
  auto bad = [](line2 a, line2 b, line2 c) {
    if (cmp(a.norm.cross(c.norm), 0) <= 0)</pre>
      return false:
    vec2 p; assert(a.intersect(c, p));
    return b.side(p) <= 0;</pre>
  }; // c1e8
  each(e, lines) {
    if (!H.empty() &&
      !cmp(H.back().norm.angle(),
      e.norm.angle())) continue;
    while (sz(H) > 1 & bad(H[sz(H)-2])
      H.back(), e)) H.pop_back();
    while (sz(H) > 1 \&\& bad(e, H[0], H[1]))
     H.pop_front();
    H.pb(e);
  } // 5714
  while (sz(H) > 2 \& \& bad(H[sz(H)-2])
   H.back(), H[0])) H.pop_back();
  while (sz(H) > 2 && bad(H.back(),
    H[0], H[1])) H.pop_front();
  out.resize(sz(H));
  rep(i, 0, sz(H)) {
    auto a = H[i], b = H[(i+1) \cdot sz(H)];
    if (a.norm.cross(b.norm) <= 0)</pre>
      return cmp(a.off*b.norm.len(),
        -b.off*a.norm.len()) <= 0 ? 0 : 2;
    assert(a.intersect(b, out[i]));
  } // c550
  rep(i, 0, sz(H)) {
    auto a = out[i], b = out[(i+1)%sz(H)];
    if (H[i].norm.perp().cross(b-a) <= 0)</pre>
      return 0:
  } // 54b6
  return 1:
} // 019f
geometry/line2.h
                                          4bb7
```

#include "vec2.h"

```
// 2D line/halfplane structure
// PARTIALLY TESTED
// Base class of versions for ints and doubles
template<class T, class P, class S>
struct bline2 {
 // For lines: norm*point == off
 // For halfplanes: norm*point <= off
 // (i.e. normal vector points outside)
 P norm; // Normal vector [A; B]
 T off; // Offset (C parameter of equation)
 DBP (norm, off);
 // Line through 2 points; normal vector
  // points to the right of ab vector
  static S through(P a, P b) {
   return { (a-b).perp(), a.cross(b) };
 } // 9ac7
  // Parallel line through point
 static S parallel(P a, S b) {
   return { b.norm, b.norm.dot(a) };
 1 // 6a39
  // Perpendicular line through point
 static S perp(P a, S b) {
   return { b.norm.perp(), b.norm.cross(a) };
 } // 10a5
  // Distance from point to line
 double distTo(P a) {
   return fabs(norm.dot(a)-off) / norm.len();
 } // 64c9
}; // 3c15
// Version for integer coordinates (long long)
struct line2i : bline2<11, vec2i, line2i> {
 line2i() : bline2{{}, 0} {}
 line2i(vec2i n, 11 c) : bline2{n, c} {}
 // Returns 0 if point a lies on the line,
  // 1 if on side where normal vector points,
  // -1 if on the other side.
 int side(vec2i a) {
   11 d = norm.dot(a);
   return (d > off) - (d < off);</pre>
 } // e4ab
1: // ealb
// Version for double coordinates
// Requires cmp() from template
struct line2d : bline2<double, vec2d, line2d> {
 line2d() : bline2{{}, 0} {}
 line2d(vec2d n, double c) : bline2{n, c} {}
 // Returns 0 if point a lies on the line,
  // 1 if on side where normal vector points,
  // -1 if on the other side.
 int side(vec2d a) {
   return cmp(norm.dot(a), off);
 // Intersect this line with line a, returns
 // true on success (false if parallel).
  // Intersection point is saved to `out`.
```

```
bool intersect (line2d a, vec2d& out) {
   double d = norm.cross(a.norm);
   if (cmp(d, 0) == 0) return false;
   out = (norm*a.off-a.norm*off).perp() / d;
   return true:
 } // 1531
}; // 516b
using line2 = line2d;
geometry/rmst.h
                                         476a
#include "../structures/find union.h"
// Rectilinear Minimum Spanning Tree
// (MST in Manhattan metric); time: O(n lg n)
// Returns MST weight. Outputs spanning tree
// to G, vertex indices match point indices.
// Edge in G is pair (target, weight).
ll rmst (vector<Pii>€ points,
       vector<vector<Pii>>> G) {
 int n = sz(points);
 vector<pair<int, Pii>> edges;
 vector<Pii> close:
 Vi ord(n), merged(n);
 iota(all(ord), 0);
  function<void(int,int)> octant =
      [&] (int begin, int end) {
   if (begin+1 >= end) return;
   int mid = (begin+end) / 2;
   octant (begin, mid);
   octant (mid, end);
   int j = mid;
   Pii best = {INT MAX, -1};
   merged.clear();
   rep(i, begin, mid) {
     int v = ord[i];
     Pii p = points[v];
     while (j < end) {
       int e = ord[j];
       Pii q = points[e];
        if (q.x-q.y > p.x-p.y) break;
       best = min(best, make_pair(q.x+q.y, e));
       merged.pb(e);
        j++;
     ) // 8576
     if (best.y != -1) {
        int alt = best.x-p.x-p.y;
       if (alt < close[v].x)</pre>
          close[v] = {alt, best.y};
     } // 4208
     merged.pb(v);
   } // f3ff
   while (j < end) merged.pb(ord[j++]);</pre>
   copy(all(merged), ord.begin()+begin);
 }; // a4e1
  rep(i, 0, 4) {
   rep(j, 0, 2) {
     sort(all(ord), [&](int 1, int r) {
```

```
return points[1] < points[r];</pre>
      }); // fe33
      close.assign(n, {INT_MAX, -1});
      octant(0, n);
      rep(k, 0, n) {
       Pii p = close[k]:
       if (p.y != -1) edges.pb({p.x,{k,p.y}});
       points[k].x \star = -1;
     } // 1c1d
   1 // 9b38
   each (p, points) p = \{p.y, -p.x\};
 } // d06f
 11 sum = 0;
 FAU fau(n):
 sort(all(edges));
 G.assign(n, {});
 each(e, edges) if (fau.join(e.y.x, e.y.y)) {
   sum += e.x;
   G[e.y.x].pb({e.y.y, e.x});
   G[e.y.y].pb({e.y.x, e.x});
 } // b04a
 return sum:
} // f586
                                         6504
geometry/segment2.h
#include "vec2.h"
// 2D segment structure; NOT HEAVILY TESTED
// Base class of versions for ints and doubles
template < class P, class S> struct bseq2 {
 P a, b; // Endpoints
 // Distance from segment to point
 double distTo(P p) const {
   if ((p-a).dot(b-a) < 0) return (p-a).len();</pre>
   if ((p-b).dot(a-b) < 0) return (p-b).len();</pre>
   return double(abs((p-a).cross(b-a)))
                  / (b-a).len();
 } // 62a2
}; // 85bc
// Version for integer coordinates (long long)
struct seg2i : bseg2<vec2i, seg2i> {
 seg2i() {}
 seg2i(vec2i c, vec2i d) : bseg2{c, d} {}
  // Check if segment contains point p
 bool contains(vec2i p) {
   return (a-p).dot(b-p) <= 0 &&
           (a-p).cross(b-p) == 0;
 } // c598
 // Compare distance to p with sqrt(d2)
 // -1 if smaller, 0 if equal, 1 if greater
 int cmpDistTo(vec2i p, 11 d2) const {
   if ((p-a).dot(b-a) < 0) {
     11 1 = (p-a).len2();
      return (1 > d2) - (1 < d2);
   } // dla6
   if ((p-b).dot(a-b) < 0) {
     11 1 = (p-b).len2();
      return (1 > d2) - (1 < d2);
```

1 // 9e65

algolib

```
11 c = abs((p-a).cross(b-a));
    d2 = (b-a).len2();
    return (c*c > d2) - (c*c < d2);
 } // 726d
}; // 4df2
// Version for double coordinates
// Requires cmp() from template
struct seg2d : bseg2<vec2d, seg2d> {
  seg2d() {}
  seg2d(vec2d c, vec2d d) : bseg2{c, d} {}
  bool contains (vec2d p) {
    return cmp((a-p).dot(b-p), 0) <= 0 &&
           cmp((a-p).cross(b-p), 0) == 0;
  1 // b507
}; // 2036
using seg2 = seg2d;
geometry/vec2.h
                                         fbc2
// 2D point/vector structure; PARTIALLY TESTED
// Base class of versions for ints and doubles
template < class T, class S> struct bvec2 {
  тх, у;
  S operator+(S r) const {return{x+r.x,y+r.y};}
  S operator-(S r) const {return{x-r.x,y-r.y};}
  S operator*(T r) const { return {x*r, y*r}; }
  S operator/(T r) const { return {x/r, y/r}; }
  T dot(S r) const { return x*r.x+y*r.y; }
  T cross(S r) const { return x*r.y-y*r.x; }
  T len2()
               const { return x*x + y*y; }
  double len() const { return sqrt(len2()); }
  S perp()
               const { return {-y,x}; } //90deg
  pair<T, T> yxPair() const { return {y,x}; }
  double angle() const { //[0;2*PI] CCW from OX
    double a = atan2(y, x);
    return (a < 0 ? a+2*M PI : a);</pre>
 } // 7095
1; // 9a6b
// Version for integer coordinates (long long)
struct vec2i : bvec2<11, vec2i> {
  vec2i() : bvec2{0, 0} {}
  vec2i(11 a, 11 b) : bvec2{a, b} {}
  bool operator==(vec2i r) const {
    return x == r.x && y == r.y;
  } // 136e
  // Compare by angle, length if angles equal
  bool operator<(vec2i r) const {</pre>
   if (upper() != r.upper()) return upper();
    auto t = cross(r);
    return t > 0 || (!t && len2() < r.len2());</pre>
  } // d6ec
  bool upper() const {
    return v > 0 \mid | (v == 0 && x >= 0);
  } // ef96
1: // 06c6
```

```
// Version for double coordinates
// Requires cmp() from template
struct vec2d : bvec2<double, vec2d> {
 vec2d() : bvec2\{0, 0\} \{\}
  vec2d(double a, double b) : bvec2{a, b} {}
  vec2d unit() const { return *this/len(); }
  vec2d rotate(double a) const { // CCW
    return {x*cos(a) - y*sin(a),
            x*sin(a) + y*cos(a); // 1890
 } // 97e3
  bool operator==(vec2d r) const {
    return !cmp(x, r.x) && !cmp(y, r.y);
  } // 81cd
  // Compare by angle, length if angles equal
  bool operator<(vec2d r) const {</pre>
    int t = cmp(angle(), r.angle());
    return t < 0 || (!t && len2() <r.len2());</pre>
 } // 84fb
1; // 3c62
using vec2 = vec2d:
graphs/2sat.h
                                         024e
// 2-SAT solver; time: O(n+m), space: O(n+m)
// Variables are indexed from 1 and
// negative indices represent negations!
// Usage: SAT2 sat(variable_count);
// (add constraints...)
// bool solution_found = sat.solve();
// sat[i] = value of i-th variable, 0 or 1
            (also indexed from 1!)
// (internally: positive = i*2-1, neg. = i*2-2)
struct SAT2 : Vi {
  vector<Vi> G;
  Vi order, flags;
  // Init n variables, you can add more later
  SAT2 (int n = 0) : G(n*2) {}
  // Add new var and return its index
  int addVar() {
   G.resize(sz(G)+2); return sz(G)/2;
  } // 98f3
  // Add (i => j) constraint
  void imply(int i, int j) {
   i = max(i*2-1, -i*2-2);
    j = \max(j*2-1, -j*2-2);
   G[i].pb(j); G[j<sup>1</sup>].pb(i<sup>1</sup>);
  } // 7be6
  // Add (i v j) constraint
  void either(int i, int j) { imply(-i, j); }
  // Constraint at most one true variable
  void atMostOne(Vi& vars) {
    int x = addVar();
    each(i, vars) {
      int y = addVar();
      imply(x, y); imply(i, -x); imply(i, y);
      x = v;
    1 // 5228
```

```
} // 9760
 // Solve and save assignments in `values`
 bool solve() { // O(n+m), Kosaraju is used
   assign(sz(G)/2+1, -1);
   flags.assign(sz(G), 0);
   rep(i, 0, sz(G)) dfs(i);
   while (!order.empty()) {
     if (!propag(order.back()^1, 1)) return 0;
     order.pop_back();
   1 // 5594
   return 1;
 } // 1e58
 void dfs(int i) {
   if (flags[i]) return;
   flags[i] = 1;
   each(e, G[i]) dfs(e);
   order.pb(i);
 } // d076
 bool propag(int i, bool first) {
   if (!flags[i]) return 1;
   flags[i] = 0;
   if (at(i/2+1) >= 0) return first;
   at (i/2+1) = i&1;
   each(e, G[i]) if (!propag(e, 0)) return 0;
   return 1;
 } // 4c1b
1: // b60c
graphs/bellman ineq.h
                                        cd51
struct Ineq {
11 a, b, c; // a - b >= c
}; // 663a
// Solve system of inequalities of form a-b>=c
// using Bellman-Ford; time: O(n*m)
bool solveIneq(vector<Ineq>& edges,
              vector<ll>& vars) {
 rep(i, 0, sz(vars)) each(e, edges)
   vars[e.b] = min(vars[e.b], vars[e.a]-e.c);
 each (e, edges)
   if (vars[e.a]-e.c < vars[e.b]) return 0;</pre>
 return 1:
} // 241e
graphs/bridges online.h
                                        405b
// Dynamic 2-edge connectivity gueries
// Usage: Bridges bridges (vertex count);
// - bridges.addEdge(u, v); - add edge (u, v)
// - bridges.cc[v] = connected component ID
// - bridges.bi(v) = 2-edge connected comp ID
struct Bridges {
 vector<Vi> G; // Spanning forest
 Vi cc, size, par, bp, seen;
 int cnt{0};
  // Initialize structure for n vertices; O(n)
 Bridges (int n = 0) : G(n), cc(n), size(n, 1),
                      par(n, -1), bp(n, -1),
                       seen(n) {
   iota(all(cc), 0);
 } // ed70
```

```
// Add edge (u, v); time: amortized O(lg n)
  void addEdge(int u, int v) {
    if (cc[u] == cc[v]) {
      int r = lca(u, v);
      while ((v = root(v)) != r)
        v = bp[bi(v)] = par[v];
      while ((u = root(u)) != r)
        u = bp[bi(u)] = par[u];
    } else {
      G[u].pb(v); G[v].pb(u);
      if (size[cc[u]] > size[cc[v]]) swap(u,v);
      size[cc[v]] += size[cc[u]];
      dfs(u, v):
   } // abc7
 } // d31c
 // Get 2-edge connected component ID
 int bi(int v) { // amortized time: < O(lq n)</pre>
   return bp[v] == -1 ? v : bp[v] = bi(bp[v]);
 } // a8d0
 int root(int v) {
    return par[v] == -1 || bi(par[v]) != bi(v)
     ? v : par[v] = root(par[v]);
 1 // 2d27
 void dfs(int v, int p) {
    par[v] = p; cc[v] = cc[p];
    each(e, G[v]) if (e != p) dfs(e, v);
 ) // 3d81
 int lca(int u, int v) { // Don't use this!
    for (cnt++; ; swap(u, v)) if (u != -1) {
     if (seen[u = root(u)] == cnt) return u;
      seen[u] = cnt; u = par[u];
   } // afed
 } // 7f56
}; // bdf6
graphs/dense dfs.h
                                         4fbd
#include "../math/bit matrix.h"
// DFS over adjacency matrix; time: O(n^2/64)
// G = graph, V = not visited vertices masks
// UNTESTED
struct DenseDFS {
 BitMatrix G, V; // space: O(n^2/64)
 DenseDFS(int n = 0) : G(n, n), V(1, n) {
   reset():
 } // 79e4
  void reset() { each(x, V.M) x = -1; }
  void setVisited(int i) { V.set(0, i, 0); }
 bool isVisited(int i) { return !V(0, i); }
  // DFS step: func is called on each unvisited
  // neighbour of i. You need to manually call
  // setVisited(child) to mark it visited.
 template < class T > // Single step: O(n/64)
 void step(int i, T func) {
    ull* E = G.row(i);
    for (int w = 0; w < G.stride;) {</pre>
     ull x = E[w] & V.row(0)[w];
      if (x) func((w<<6) | builtin ctzll(x));</pre>
      else w++;
```

algolib

```
} // 4c0a
 } // f045
1: // 8edb
graphs/edmonds_karp.h
                                        d2ae
using flow_t = int;
constexpr flow t INF = 1e9+10;
// Edmonds-Karp algorithm for finding
// maximum flow in graph; time: O(V*E^2)
// NOT HEAVILY TESTED
struct MaxFlow {
  struct Edge {
   int dst. inv:
    flow_t flow, cap;
  }; // a53c
  vector<vector<Edge>> G;
  vector<flow t> add;
  Vi prev:
  // Initialize for n vertices
  MaxFlow(int n = 0) : G(n) {}
  // Add new vertex
  int addVert() {
   G.emplace_back(); return sz(G)-1;
  } // 907a
  // Add edge between u and v with capacity cap
  // and reverse capacity rcap
  void addEdge(int u, int v,
               flow_t cap, flow_t rcap = 0) {
   G[u].pb({ v, sz(G[v]), 0, cap });
   G[v].pb({u, sz(G[u])-1, 0, rcap });
  } // Of10
  // Compute maximum flow from src to dst.
  // Flow values can be found in edges.
  // vertices with `add` >= 0 belong to
  // cut component containing `s`.
  flow_t maxFlow(int src, int dst) {
   flow t f = 0;
    each (v, G) each (e, v) e.flow = 0;
      queue<int> Q;
     O.push(src);
     prev.assign(sz(G), -1);
     add.assign(sz(G), -1);
      add[src] = INF;
      while (!Q.empty()) {
       int i = 0.front();
        flow_t m = add[i];
       Q.pop();
       if (i == dst) {
          while (i != src) {
            auto& e = G[i][prev[i]];
            e.flow -= m;
           G[e.dst][e.inv].flow += m;
           i = e.dst;
          } // 35e6
          f += m;
          break:
```

```
} // 857e
        each(e, G[i]) if (add[e.dst] < 0) {
         if (e.flow < e.cap) {</pre>
           O.push(e.dst);
           prev[e.dst] = e.inv;
           add[e.dst] = min(m, e.cap-e.flow);
         } // 4cdb
       } // 1ea5
     } // bbb0
   } while (prev[dst] != -1);
   return f:
 1 // d492
 // Get if v belongs to cut component with src
 bool cutSide(int v) {
   return add[v] >= 0;
 } // 41e9
}; // afff
graphs/gomory_hu.h
                                        a520
#include "edmonds karp.h"
//#include "push relabel.h" // if you need
struct Edge {
 int a, b; // vertices
 flow_t w; // weight
}; // c331
// Build Gomory-Hu tree; time: O(n*maxflow)
// Gomory-Hu tree encodes minimum cuts between
// all pairs of vertices: mincut for u and v
// is equal to minimum on path from u and v
// in Gomory-Hu tree. n is vertex count.
// Returns vector of Gomory-Hu tree edges.
vector<Edge> gomoryHu (vector<Edge>& edges,
                     int n) {
 MaxFlow flow(n):
 each (e, edges) flow.addEdge (e.a,e.b,e.w,e.w);
  vector<Edge> ret(n-1);
 rep(i, 1, n) ret[i-1] = {i, 0, 0};
 rep(i, 1, n) {
   ret[i-1].w = flow.maxFlow(i, ret[i-1].b);
   rep(j, i+1, n)
     if (ret[j-1].b == ret[i-1].b &&
          flow.cutSide(j) ret[j-1].b = i;
 } // 5ae4
 return ret;
} // afdb
graphs/matroids.h
                                        55ef
// Find largest subset S of [n] such that
// S is independent in both matroid A and B.
// A and B are given by their oracles,
// see example implementations below.
// Returns vector V such that V[i] = 1 iff
// i-th element is included in found set;
// time: O(r^2*init + r^2*n*add),
// where r is max independent set,
// `init` is max time of oracles init
```

// and `add` is max time of oracles canAdd.

```
template<class T, class U>
vector<bool> intersectMatroids (T& A, U& B,
                               int n) {
 vector<bool> ans(n);
 bool ok = 1:
 A.init(ans);
 B.init(ans);
 rep(i, 0, n) if (A.canAdd(i) && B.canAdd(i))
   ans[i] = 1, A.init(ans), B.init(ans);
  while (ok) {
   vector<Vi> G(n):
   vector<bool> good(n);
   queue<int> que;
   Vi prev(n, -1);
   A.init(ans);
   B.init(ans);
   ok = 0:
   rep(i, 0, n) if (!ans[i]) {
     if (A.canAdd(i)) que.push(i), prev[i]=-2;
     good[i] = B.canAdd(i);
   } // 9581
   rep(i, 0, n) if (ans[i]) {
     ans[i] = 0;
     A.init(ans);
     B.init(ans);
     rep(j, 0, n) if (i != j && !ans[j]) {
       if (A.canAdd(j)) G[i].pb(j);
       if (B.canAdd(j)) G[j].pb(i);
     } // bd2a
     ans[i] = 1;
   } // bf3e
   while (!que.empty()) {
     int i = que.front();
     que.pop();
     if (good[i]) {
       ans[i] = 1;
        while (prev[i] >= 0) {
         ans[i = prev[i]] = 0;
         ans[i = prev[i]] = 1;
        } // 51c8
        ok = 1;
       break:
     } // 384b
     each(j, G[i]) if (prev[j] == -1)
       que.push(j), prev[j] = i;
   } // 6eb6
 } // e092
 return ans;
} // ae8e
// Matroid where each element has color
// and set is independent iff for each color c
// #{elements of color c} <= maxAllowed[c].
struct LimOracle {
 Vi color; // color[i] = color of i-th element
 Vi maxAllowed: // Limits for colors
```

```
// Init oracle for independent set S; O(n)
 void init(vector<bool>& S) {
   tmp = maxAllowed;
   rep(i, 0, sz(S)) tmp[color[i]] -= S[i];
 } // 4dfb
 // Check if S+{k} is independent; time: O(1)
 bool canAdd(int k) {
   return tmp[color[k]] > 0;
 } // e312
}; // 7b5d
// Graphic matroid - each element is edge.
// set is independent iff subgraph is acyclic.
struct GraphOracle {
 vector<Pii> elems; // Ground set: graph edges
 int n; // Number of vertices, indexed [0;n-1]
 Vi par:
 int find(int i) {
   return par[i] == -1 ? i
     : par[i] = find(par[i]);
 1 // b8b7
  // Init oracle for independent set S; ~O(n)
 void init(vector<bool>& S) {
   par.assign(n, -1);
   rep(i, 0, sz(S)) if (S[i])
      par[find(elems[i].x)] = find(elems[i].y);
 } // 1827
  // Check if S+{k} is independent; time: ~O(1)
 bool canAdd(int k) {
   return
      find(elems[k].x) != find(elems[k].y);
 } // 8ca4
}; // c506
// Co-graphic matroid - each element is edge,
// set is independent iff after removing edges
// from graph number of connected components
// doesn't change.
struct CographOracle {
 vector<Pii> elems; // Ground set: graph edges
 int n: // Number of vertices, indexed [0:n-1]
 vector<Vi> G;
 Vi pre, low;
 int cnt:
 int dfs(int v, int p) {
   pre[v] = low[v] = ++cnt;
   each(e, G[v]) if (e != p)
     low[v] = min(low[v], pre[e] ?: dfs(e,v));
   return low[v];
 } // 9d30
 // Init oracle for independent set S; O(n)
 void init(vector<bool>& S) {
   G.assign(n, {});
   pre.assign(n, 0);
   low.resize(n):
   cnt = 0;
   rep(i, 0, sz(S)) if (!S[i]) {
     Pii e = elems[i]:
     G[e.x].pb(e.v);
```

algolib

```
G[e.y].pb(e.x);
   } // 79a1
   rep(v, 0, n) if (!pre[v]) dfs(v, -1);
  } // 1200
  // Check if S+{k} is independent; time: O(1)
  bool canAdd(int k) {
   Pii e = elems[k]:
    return max(pre[e.x], pre[e.y])
      != max(low[e.x], low[e.y]);
 } // 2550
}; // a5cc
// Matroid equivalent to linear space with XOR
struct XorOracle {
  vector<ll> elems: // Ground set: numbers
  vector<11> base:
  // Init for independent set S: O(n+r^2)
  void init(vector<bool>& S) {
   base.assign(63, 0);
    rep(i, 0, sz(S)) if (S[i]) {
     ll e = elems[i];
     rep(j, 0, sz(base)) if ((e >> j) & 1) {
       if (!base[j]) {
         base[j] = e;
         break:
       } // 1df5
       e ^= base[i];
     } // 8495
   } // 655e
  } // b68c
  // Check if S+{k} is independent; time: O(r)
  bool canAdd(int k) {
   11 e = elems[k];
   rep(i, 0, sz(base)) if ((e >> i) & 1) {
     if (!base[i]) return 1;
     e ^= base[i];
   } // 49d1
   return 0;
 } // 66ff
}; // 4af3
graphs/push_relabel.h
                                        a9ca
using flow t = int;
constexpr flow_t INF = 1e9+10;
// Push-relabel algorithm with global relabel
// heuristic for finding maximum flow; O(V^3),
// but very fast in practice.
// Preflow is not converted to flow!
struct MaxFlow {
  struct Vert {
   int head{0}, cur{0}, label;
   flow_t excess;
  }; // 36c9
  struct Edge {
   int dst, nxt;
   flow t avail, cap;
  }; // 2782
  vector<Vert> V;
  vector<Edge> E;
  queue<int> que, bfs;
```

```
// Initialize for n vertices
MaxFlow(int n = 0) {
 V.assign(n, {});
 E.resize(2);
} // e1c2
// Add new vertex
int addVert() {
 V.emplace back();
 return sz(V)-1;
} // 4806
// Add edge between u and v with capacity cap
// and reverse capacity rcap
void addEdge(int u, int v,
             flow_t cap, flow_t rcap = 0) {
  E.pb({ v, V[u].head, 0, cap });
  E.pb({ u, V[v].head, 0, rcap });
  V[u].head = sz(E)-2;
  V[v].head = sz(E)-1;
} // 7c6e
void push(int v, int e) {
  flow_t f = min(V[v].excess, E[e].avail);
  E[e].avail -= f;
  E[e^1].avail += f;
  V[v].excess -= f;
  if ((V[E[e].dst].excess += f) == f)
    que.push(E[e].dst);
} // 12fd
// Compute maximum flow from src to dst
flow t maxFlow(int src, int dst) {
  each (v, V) v.excess = v.label = v.cur = 0;
  each (e, E) e.avail = max(e.cap, flow_t(0));
  int cnt, n = cnt = V[src].label = sz(V);
  V[src].excess = INF;
  for (int e = V[src].head; e; e = E[e].nxt)
   push (src, e);
  for (; !que.empty(); que.pop()) {
    if (cnt >= n/2) {
      each (v, V) v.label = n;
      V[dst1.label = 0;
      bfs.push(dst);
      cnt = 0;
      for (; !bfs.empty(); bfs.pop()) {
        auto& v = V[bfs.front()];
        for (int e=v.head; e; e = E[e].nxt) {
          int x = E[e].dst;
          if (E[e^1].avail &&
              V[x].label > v.label+1) {
            V[x].label = v.label+1;
           bfs.push(x);
         } // ce3d
       } // da4f
     } // 2f55
    } // 3f80
    int v = que.front(), &1 = V[v].label;
    if (v == dst) continue;
    while (V[v].excess && l < n) {
```

```
if (!V[v].cur) {
         1 = n;
         for (int e=V[v].head; e; e=E[e].nxt){
            if (E[e].avail)
             l = min(l, V[E[e].dst].label+1);
         } // c0f1
         V[v].cur = V[v].head;
         cnt++;
       } // 6825
        int e = V[v].cur;
        V[v].cur = E[e].nxt;
        if (E[e].avail &&
         l == V[E[e].dst].label+1) push(v, e);
     1 // 70b7
   } // ee36
   return V[dst].excess;
 1 // 7d37
 // Get if v belongs to cut component with src
 bool cutSide(int v) {
   return V[v].label >= sz(V);
 1 // 25f7
1: // e2d6
graphs/scc.h
                                        cea2
// Tarjan's SCC algorithm; time: O(n+m)
// Usage: SCC scc(graph);
// scc[v] = index of SCC for vertex v
// scc.comps[i] = vertices of i-th SCC
struct SCC : Vi {
 vector<Vi> comps;
 Vi S;
 int cnt{0};
 SCC() {}
 SCC(vector\langle Vi \rangle \& G) : Vi(sz(G),-1), S(sz(G)) {
   rep(i, 0, sz(G)) if (!S[i]) dfs(G, i);
 } // f0fa
 int dfs(vector<Vi>& G, int v) {
   int low = S[v] = ++cnt, t = -1;
   S.pb(v);
   each(e, G[v]) if (at(e) < 0)
     low = min(low, S[e] ?: dfs(G, e));
   if (low == S[v]) {
     comps.emplace_back();
     for (; t != v; S.pop_back()) {
       at (t = S.back()) = sz(comps) - 1;
        comps.back().pb(t);
     } // 9e74
   } // dcb5
   return low;
 } // 3257
}; // a055
                                        d400
graphs/turbo matching.h
// Find maximum bipartite matching; time: ?
// G must be bipartite graph!
```

// Returns matching size (edge count).

```
// match[v] = vert matched to v or -1
int matching (vector < Vi>& G, Vi& match) {
 vector<bool> seen:
 int n = 0, k = 1;
 match.assign(sz(G), -1);
  function<int(int)> dfs = [&](int i) {
    if (seen[i]) return 0;
    seen[i] = 1;
    each(e, G[i]) {
      if (match[e] < 0 || dfs(match[e])) {</pre>
        match[i] = e; match[e] = i;
       return 1:
     1 // 893d
    } // 9532
   return 0:
 }; // d332
  while (k) {
    seen.assign(sz(G), 0);
    k = 0:
    rep(i, 0, sz(G)) if (match[i] < 0)
     k += dfs(i);
   n += k;
 } // 1128
 return n:
} // 0d38
// Convert maximum matching to vertex cover
// time: O(n+m)
Vi vertexCover(vector<Vi>& G, Vi& match) {
 Vi ret, col(sz(G)), seen(sz(G));
  function<void(int, int)> dfs =
      [&] (int i, int c) {
   if (col[i]) return;
    col[i] = c+1;
    each(e, G[i]) dfs(e, !c);
 }; // 1f1b
  function<void(int)> aug = [&](int i) {
    if (seen[i] || col[i] != 1) return;
    seen[i] = 1;
    each(e, G[i]) seen[e] = 1, aug(match[e]);
 }; // 2465
  rep(i, 0, sz(G)) dfs(i, 0);
  rep(i, 0, sz(G)) if (match[i] < 0) aug(i);
  rep(i, 0, sz(G))
   if (seen[i] == col[i]-1) ret.pb(i);
 return ret:
} // 6f72
math/berlekamp massev.h
                                         c714
constexpr int MOD = 1e9+7;
11 modInv(11 a, 11 m) { // a^(-1) mod m
 if (a == 1) return 1;
 return ((a - modInv(m%a, a)) *m + 1) / a;
1 // c437
// Find shortest linear recurrence that matches
// given starting terms of recurrence; O(n^2)
// Returns vector C such that for each i >= |C|
// A[i] = sum A[i-j-1]*C[j] for j = 0..|C|-1
// UNTESTED
```

5

ll s = 1:

B[0] = C[0] = 1;

vector<ll> massev (vector<ll> € A) {

int n = sz(A), len = 0, k = 0;

vector<ll> B(n), C(n), tmp;

```
rep(i, 0, n) {
                                                 math/bit matrix.h
   11 d = 0;
   k++;
                                                 using ull = uint64 t;
    rep(j, 0, len+1)
     d = (d + C[j] * A[i-j]) % MOD;
                                                 // Matrix over Z 2 (bits and xor)
                                                 // UNTESTED and UNFINISHED
                                                 struct BitMatrix {
     11 q = d * modInv(s, MOD) % MOD;
                                                   vector<ull> M:
                                                   int rows, cols, stride;
     tmp = C;
                                                   BitMatrix(int n = 0, int m = 0) {
     rep(j, k, n)
       C[j] = (C[j] - q * B[j-k]) % MOD;
                                                     rows = n; cols = m;
                                                     stride = (m+63)/64;
     if (len*2 <= i) {</pre>
                                                    M.resize(n*stride);
       B.swap(tmp);
                                                   } // 7ef0
       len = i-len+1;
       s = d + (d < 0) * MOD;
                                                   ull* row(int i) { return &M[i*stride]; }
       k = 0;
     } // c350
                                                   bool operator()(int i, int j) {
   } // 79c7
                                                     return (row(i)[j/64] >> (j%64)) & 1;
  } // f70c
                                                   } // 28bd
                                                   void set(int i, int j, bool val) {
  C.resize(len+1);
                                                     ull \&w = row(i) [j/64], m = 1 << (j%64);
  C.erase(C.begin());
  each (x, C) x = (MOD - x) % MOD;
                                                     if (val) w |= m;
 return C:
                                                    else w &= ~m;
} // 4a08
                                                   } // e908
                                                 }; // 2192
math/bit gauss.h
                                        13eb
                                                 math/crt.h
constexpr int MAX COLS = 2048;
                                                 using Pll = pair<ll, 11>;
// Solve system of linear equations over Z 2
// time: O(n^2*m/W), where W is word size
                                                 ll egcd(ll a, ll b, ll& x, ll& y) {
// - A - extended matrix, rows are equations,
                                                  if (!a) return x=0, y=1, b;
        columns are variables.
                                                  11 d = egcd(b%a, a, y, x);
        m-th column is equation result
                                                   x = b/a*y;
        (A[i][i] - i-th row and i-th column)
                                                   return d;
// - ans - output for variables values
                                                 1 // 23c8
// - m - variable count
// Returns 0 if no solutions found, 1 if one,
                                                 // Chinese Remainder Theoerem; time: O(lq lcm)
// 2 if more than 1 solution exist.
                                                 // Solves x = a.x \pmod{a.y}, x = b.x \pmod{b.y}
int bitGauss (vector < bitset < MAX COLS >> & A,
                                                 // Returns pair (x mod lcm, lcm(a.v, b.v))
            vector<bool>& ans, int m) {
                                                 // or (-1, -1) if there's no solution.
 Vi col;
                                                 // WARNING: a.x and b.x are assumed to be
                                                 // in [0;a.y) and [0;b.y) respectively.
  ans.assign(m, 0);
                                                 // Works properly if lcm(a.y, b.y) < 2^63.
                                                 Pll crt(Pll a, Pll b) {
  rep(i, 0, sz(A)) {
   int c = int(A[i]. Find first());
                                                   if (a.v < b.v) swap(a, b);
   if (c >= m) {
                                                   ll x, y, q = \operatorname{egcd}(a.y, b.y, x, y);
     if (c == m) return 0;
                                                   11 c = b.x-a.x, d = b.y/q, p = a.y*d;
     continue:
                                                   if (c % g) return {-1, -1};
    } // a6bb
                                                   11 s = (a.x + c/q*x % d * a.y) % p;
                                                   return {s < 0 ? s+p : s, p};
    rep(k, i+1, sz(A)) if (A[k][c]) A[k]^=A[i];
                                                 } // 35a8
   swap(A[i], A[sz(col)]);
   col.pb(c);
                                                 math/discrete logarithm.h
  } // a953
                                                 #include "../modular.h"
  for (int i = sz(col); i--;) if (A[i][m]) {
   ans[col[i]] = 1;
                                                 // Baby-step giant-step algorithm; O(sgrt(p))
```

} // 4ca1

} // 996e

return sz(col) < m ? 2 : 1;</pre>

```
rep(k,0,i) if(A[k][col[i]]) A[k][m].flip();
                                            // Finds smallest x such that a^x = b \pmod{p}
                                             // or returns -1 if there's no solution.
                                             ll dlog(ll a, ll b, ll p) {
                                              int m = int(min(ll(sqrt(p))+2, p-1));
                                               unordered map<11, int> small;
                                               11 t = 1:
                                     73b9
                                               rep(i, 0, m) {
                                                int& k = small[t];
                                                if (!k) k = i+1;
                                                t = t*a % p;
                                              } // f1d0
                                              t = modInv(t, p);
                                               rep(i, 0, m) {
                                                int j = small[b];
                                                if (j) return i*m + j - 1;
                                                b = b * t % p;
                                              } // 533b
                                              return -1:
                                             } // 47fa
                                             math/fft complex.h
                                                                                      4311
                                             using dbl = double:
                                             using cmpl = complex<dbl>;
                                             // Default std::complex multiplication is slow.
                                             // You can use this to achieve small speedup.
                                             cmpl operator*(cmpl a, cmpl b) {
                                              dbl ax = real(a), ay = imag(a);
                                              dbl bx = real(b), by = imag(b);
                                              return {ax*bx-ay*by, ax*by+ay*bx};
                                            } // 3b78
                                    8a85
                                             cmpl operator*=(cmpl& a,cmpl b) {return a=a*b;}
                                             // Compute DFT over complex numbers; O(n lq n)
                                             // Input size must be power of 2!
                                             void fft(vector<cmpl>& a) {
                                               static vector<cmpl> w(2, 1);
                                              int n = sz(a);
                                               for (int k = sz(w); k < n; k *= 2) {
                                                 w.resize(n);
                                                 rep(i,0,k) w[k+i] = \exp(\text{cmpl}(0, M_PI*i/k));
                                              } // 92a9
                                               Vi rev(n):
                                               rep(i,0,n) rev[i] = (rev[i/2] | i*2*n) / 2;
                                               rep(i,0,n) if(i<rev[i]) swap(a[i],a[rev[i]]);
                                               for (int k = 1; k < n; k *= 2) {
                                                for (int i=0; i < n; i += k*2) rep(j,0,k) {
                                                   auto d = a[i+j+k] * w[j+k];
                                                   a[i+j+k] = a[i+j] - d;
                                                  a[i+j] += d;
                                                } // b389
                                              } // 84bf
                                             } // adf8
                                    53a9
                                             // Convolve complex-valued a and b,
                                             // store result in a; time: O(n lq n), 3x FFT
                                             void convolve(vector<cmpl>& a, vector<cmpl> b) {
                                             int len = sz(a) + sz(b) - 1;
```

```
int n = 1 \ll (32 - builtin clz(len));
 a.resize(n); b.resize(n);
 fft(a); fft(b);
 rep(i, 0, n) a[i] \star= b[i] / dbl(n);
  reverse (a.begin()+1, a.end());
 fft(a):
 a.resize(len);
} // 08e3
// Convolve real-valued a and b, returns result
// time: O(n lg n), 2x FFT
// Rounding to integers is safe as long as
// (max\_coeff^2) *n*log_2(n) < 9*10^14
// (in practice 10^16 or higher).
vector<dbl> convolve(vector<dbl>& a,
                     vector<dbl>& b) {
 int len = sz(a) + sz(b) - 1;
 int n = 1 << (32 - __builtin_clz(len));</pre>
 vector<cmpl> in(n), out(n);
 rep(i, 0, sz(a)) in[i].real(a[i]);
 rep(i, 0, sz(b)) in[i].imag(b[i]);
 fft(in);
 each(x, in) x \star = x;
  rep(i,0,n) out[i] = in[-i&(n-1)]-conj(in[i]);
  fft (out):
 vector<dbl> ret(len);
 rep(i, 0, len) ret[i] = imag(out[i]) / (n*4);
 return ret;
} // d1d3
constexpr 11 MOD = 1e9+7;
// High precision convolution of integer-valued
// a and b mod MOD; time: O(n lq n), 4x FFT
// Input is expected to be in range [0; MOD)!
// Rounding is safe if MOD*n*log 2(n) < 9*10^14
// (in practice 10^16 or higher).
vector<ll> convMod(vector<ll>& a,
                   vector<ll>& b) {
 vector<ll> ret(sz(a) + sz(b) - 1);
 int n = 1 << (32 - __builtin_clz(sz(ret)));</pre>
 11 cut = 11(sqrt(MOD))+1;
 vector<cmpl> c(n), d(n), g(n), f(n);
  rep(i, 0, sz(a))
   c[i] = {dbl(a[i]/cut), dbl(a[i]%cut)};
  rep(i, 0, sz(b))
   d[i] = {dbl(b[i]/cut), dbl(b[i]%cut)};
  fft(c); fft(d);
  rep(i, 0, n) {
   int j = -i & (n-1);
    f[j] = (c[i]+conj(c[j])) * d[i] / (n*2.0);
    q[j] =
      (c[i]-conj(c[j])) * d[i] / cmpl(0, n*2);
 } // e877
 fft(f); fft(q);
  rep(i, 0, sz(ret)) {
   11 t = llround(real(f[i])) % MOD * cut;
```

t += llround(imag(f[i]));

```
t = (t + llround(real(g[i]))) % MOD * cut;
   t = (t + llround(imag(g[i]))) % MOD;
    ret[i] = (t < 0 ? t+MOD : t);
  } // e75d
  return ret;
} // 513f
math/fft mod.h
                                         61d4
// Number Theoretic Tranform (NTT)
// For functions below you can choose 2 params:
// 1. M - prime modulus that MUST BE of form
         a*2^k+1, computation is done in Z M
// 2. R - generator of Z_M
// Modulus often seen on Codeforces:
// M = (119<<23)+1, R = 62; M is 998244353
// Parameters for 11 computation with CRT:
// M = (479 << 21) +1, R = 62; M is > 10^9
// M = (483<<21)+1, R = 62; M is > 10^9
11 modPow(11 a, 11 e, 11 m) {
 11 t = 1 % m;
  while (e) {
   if (e % 2) t = t*a % m;
   e /= 2; a = a*a % m;
  } // 66ca
  return t;
} // 1973
// Compute DFT over Z_M with generator R.
// Input size must be power of 2; O(n lg n)
// Input is expected to be in range [0;MOD)!
// dit == true <=> inverse transform * 2^n
                  (without normalization)
template<11 M, 11 R, bool dit>
void ntt(vector<ll>& a) {
  static vector<1l> w(2, 1);
  int n = sz(a):
  for (int k = sz(w); k < n; k *= 2) {
   w.resize(n, 1);
   11 c = modPow(R, M/2/k, M);
   if (dit) c = modPow(c, M-2, M);
    rep(i, k+1, k*2) w[i] = w[i-1]*c % M;
  } // 0d98
  for (int t = 1; t < n; t *= 2) {</pre>
    int k = (dit ? t : n/t/2);
    for (int i=0; i < n; i += k*2) rep(j,0,k) {
     ll &c = a[i+j], &d = a[i+j+k];
     ll e = w[j+k], f = d;
     d = (dit ? c - (f=f*e%M) : (c-f)*e % M);
     if (d < 0) d += M;
      if ((c += f) >= M) c -= M;
    } // e4a6
 } // 8d38
} // 01f5
// Convolve a and b mod M (R is generator),
// store result in a; time: O(n lg n), 3x NTT
// Input is expected to be in range [0;MOD)!
template<11 M = (119<<23)+1, 11 R = 62>
void convolve(vector<11>& a, vector<11> b) {
```

```
int len = sz(a) + sz(b) - 1;
   int n = 1 \ll (32 - builtin clz(len));
  ll t = modPow(n, M-2, M);
   a.resize(n); b.resize(n);
  ntt < M, R, 0 > (a); ntt < M, R, 0 > (b);
  rep(i, 0, n) a[i] = a[i] *b[i] % M * t % M;
  ntt<M,R,1>(a);
  a.resize(len);
 } // ec61
 ll egcd(ll a, ll b, ll& x, ll& y) {
  if (!a) return x=0, y=1, b;
  11 d = eqcd(b%a, a, y, x);
  x = b/a*v:
  return d:
 } // 23c8
 // Convolve a and b with 64-bit output,
 // store result in a; time: O(n lg n), 6x NTT
 // Input is expected to be non-negative!
 void convLong(vector<11>& a, vector<11> b) {
  const 11 M1 = (479 << 21) +1, M2 = (483 << 21) +1;
  const 11 MOD = M1*M2, R = 62;
  vector<11> c = a, d = b;
  each(k, a) k %= M1; each(k, b) k %= M1;
  each(k, c) k %= M2; each(k, d) k %= M2;
  convolve<M1, R>(a, b);
  convolve<M2, R>(c, d);
  11 x, y; egcd(M1, M2, x, y);
  rep(i, 0, sz(a)) {
    a[i] += (c[i]-a[i])*x % M2 * M1;
    if ((a[i] %= MOD) < 0) a[i] += MOD;</pre>
  } // add0
 } // fc1e
 math/fwht.h
                                          3e6f
 // Fast Walsh-Hadamard Transform; O(n lq n)
 // Input must be power of 2!
 // Uncommented version is for XOR.
 // OR version is equivalent to sum-over-subsets
 // (Zeta transform, inverse is Moebius).
 // AND version is same as sum-over-supersets.
 // TESTED ON RANDS
 template < bool inv, class T>
 void fwht(vector<T>& b) {
  for (int s = 1; s < sz(b); s *= 2) {
    for (int i = 0; i < sz(b); i += s*2) {
      rep(j, i, i+s) {
         auto &x = b[j], &y = b[j+s];
         tie(x, v) =
           mp(x+y, x-y);
                                           //XOR
         // inv ? mp(x-y, y) : mp(x+y, y); //AND
        // inv ? mp(x, y-x) : mp(x, x+y); //OR
      } // eea9
    } // a3d5
  } // 95ed
  // ONLY FOR XOR:
  if (inv) each(e, b) e /= sz(b);
} // 0779
// Compute convolution of a and b such that
```

```
// ans[i#i] += a[i]*b[i], where # is OR, AND
// or XOR, depending on FWHT version.
// Stores result in a; time: O(n lg n)
// Both arrays must be of same size = 2^n!
template<class T>
void bitConv(vector<T>& a, vector<T> b) {
 fwht<0>(a);
 fwht<0>(b):
 rep(i, 0, sz(a)) a[i] *= b[i];
 fwht<1>(a):
1 // 7b82
                                        7f0b
math/gauss.h
// Solve system of linear equations; O(n^2*m)
// - A - extended matrix, rows are equations,
        columns are variables.
        m-th column is equation result
        (A[i][j] - i-th row and j-th column)
// - ans - output for variables values
// - m - variable count
// Returns 0 if no solutions found, 1 if one,
// 2 if more than 1 solution exist.
int gauss (vector<vector<double>>& A,
         vector<double>& ans, int m) {
 Vi col:
  ans.assign(m, 0);
  rep(i, 0, sz(A)) {
   int c = 0:
    while (c <= m && !cmp(A[i][c], 0)) c++;</pre>
    // For Zp:
    //while (c <= m && !A[i][c].x) c++;
    if (c >= m) {
     if (c == m) return 0;
      continue:
   } // a6bb
    rep(k, i+1, sz(A)) {
      auto mult = A[k][c] / A[i][c];
      rep(j, 0, m+1) A[k][j] -= A[i][j]*mult;
    } // 8dd5
    swap(A[i], A[sz(col)]);
   col.pb(c):
 } // ea2c
  for (int i = sz(col); i--;) {
   ans [col[i]] = A[i][m] / A[i][col[i]];
    rep(k, 0, i)
      A[k][m] = ans[col[i]] * A[k][col[i]];
  } // 31b9
  return sz(col) < m ? 2 : 1;</pre>
1 // 0b76
math/matrix.h
                                         9bf7
#include "modular.h"
// UNTESTED
using Row = vector<Zp>;
using Matrix = vector<Row>;
// Create n x n identity matrix
Matrix ident(int n) {
```

```
Matrix ret(n, Row(n));
 rep(i, 0, n) ret[i][i] = 1;
 return ret:
} // ad1d
// Add matrices
Matrix& operator+= (Matrix& 1, const Matrix& r) {
 rep(i, 0, sz(l)) rep(k, 0, sz(l[0]))
   l[i][k] += r[i][k];
 return 1:
} // b6bf
Matrix operator+(Matrix 1, const Matrix& r) {
return 1 += r:
1 // d9b3
// Subtract matrices
Matrix& operator == (Matrix& 1, const Matrix& r) {
 rep(i, 0, sz(l)) rep(k, 0, sz(l[0]))
   l[i][k] = r[i][k];
 return 1:
} // 90a1
Matrix operator-(Matrix 1, const Matrix& r) {
 return 1 -= r;
} // dc4f
// Multiply matrices
Matrix operator* (const Matrix& 1,
                 const Matrix& r) {
 Matrix ret(sz(1), Row(sz(r[0])));
 rep(i, 0, sz(l)) rep(j, 0, sz(r[0]))
   rep(k, 0, sz(r))
      ret[i][j] += l[i][k] * r[k][j];
 return ret:
} // 52ca
Matrix& operator *= (Matrix& 1, const Matrix& r) {
 return 1 = 1*r;
} // da8a
// Square matrix power; time: O(n^3 * 1g e)
Matrix pow(Matrix a, ll e) {
 Matrix t = ident(sz(a));
 while (e) {
   if (e % 2) t *= a;
   e /= 2; a *= a;
 } // 4400
 return t;
} // 65ea
// Transpose matrix
Matrix transpose (const Matrix m) {
 Matrix ret(sz(m[0]), Row(sz(m)));
 rep(i, 0, sz(m)) rep(j, 0, sz(m[0]))
    ret[j][i] = m[i][j];
 return ret:
} // 5650
// Transform matrix to echelon form
// and compute its determinant sign and rank.
int echelon(Matrix& A, int& sign) { // O(n^3)
 int rank = 0;
 sign = 1;
 rep(c, 0, sz(A[0])) {
   if (rank >= sz(A)) break;
   rep(i, rank+1, sz(A)) if (A[i][c].x) {
      swap(A[i], A[rank]);
      sign *=-1;
```

```
break;
    } // f98a
    if (A[rank][c].x) {
      rep(i, rank+1, sz(A)) {
       auto mult = A[i][c] / A[rank][c];
        rep(j, 0, sz(A[0]))
          A[i][j] -= A[rank][j]*mult;
     1 // f519
     rank++;
   } // 4cd8
  1 // 36e9
  return rank;
1 // 6882
// Compute matrix rank; time: O(n^3)
#define rank rank
int rank (Matrix A) {
 int s; return echelon(A, s);
1 // c599
// Compute square matrix determinant; O(n^3)
Zp det (Matrix A) {
  int s; echelon(A, s);
  Zp ret = s:
  rep(i, 0, sz(A)) ret *= A[i][i];
  return ret:
1 // b252
// Invert square matrix if possible; O(n^3)
// Returns true if matrix is invertible.
bool invert (Matrix& A) {
  int s, n = sz(A);
  rep(i, 0, n) A[i].resize(n*2), A[i][n+i] = 1;
  echelon(A, s);
  for (int i = n; i--;) {
    if (!A[i][i].x) return 0;
    auto mult = A[i][i].inv();
   each(k, A[i]) k *= mult;
    rep(k, 0, i) rep(j, 0, n)
     A[k][n+j] -= A[i][n+j]*A[k][i];
  } // 1e97
  each (r, A) r.erase (r.begin(), r.begin()+n);
  return 1;
1 // 65b9
math/miller rabin.h
                                         4867
#include "modular64.h"
// Miller-Rabin primality test
// time O(k*lg^2 n), where k = number of bases
// Deterministic for p <= 10^9
// constexpr 11 BASES[] = {
// 336781006125, 9639812373923155
// }; // d41d
// Deterministic for p <= 2^64
constexpr 11 BASES[] = {
  2,325,9375,28178,450775,9780504,1795265022
}; // b8e0
bool isPrime(ll p) {
 if (p == 2) return true;
  if (p <= 1 || p%2 == 0) return false;
  11 d = p-1, times = 0;
```

```
while (d%2 == 0) d /= 2, times++;
 each (a, BASES) if (a%p) {
   // 11 a = rand() % (p-1) + 1;
   11 b = modPow(a%p, d, p);
   if (b == 1 || b == p-1) continue;
   rep(i, 1, times) {
     b = modMul(b, b, p);
     if (b == p-1) break;
   1 // 6061
   if (b != p-1) return false;
 1 // c7a4
 return true:
} // Ocdf
math/modinv precompute.h
                                       2882
constexpr 11 MOD = 234567899;
vector<11> modInv(MOD); // You can lower size
// Precompute modular inverses; time: O(MOD)
void initModInv() {
 modInv[1] = 1;
 rep(i, 2, sz(modInv)) modInv[i] =
   (MOD - (MOD/i) ★ modInv[MOD%i]) % MOD;
) // 22c1
math/modular.h
                                       5544
// Big prime number, about 2*10^9
constexpr int MOD = 15*(1<<27)+1;
11 modInv(11 a, 11 m) { // a^(-1) mod m
 if (a == 1) return 1:
 return ((a - modInv(m%a, a))*m + 1) / a;
} // c437
11 modPow(11 a, 11 e, 11 m) { // a^e mod m
 ll t = 1 % m;
 while (e) {
   if (e % 2) t = t*a % m;
   e /= 2; a = a*a % m;
 } // 66ca
 return t;
} // 1973
// Wrapper for modular arithmetic
struct Zp {
 11 x; // Contained value, in range [0; MOD-1]
 Zp() : x(0) {}
 Zp(11 a) : x(a\%MOD) { if (x < 0) x += MOD; }
 x = x d; return *this; } \
   Zp operator c(Zp r) const { \
     Zp \ t = *this; return \ t \ c##= r; \ // e986
 OP(+, +r.x - MOD*(x+r.x >= MOD));
 OP(-, -r.x + MOD*(x-r.x < 0));
 OP(*, *r.x % MOD);
 OP (/, *r.inv().x % MOD);
 // For composite modulus use modInv, not pow
 Zp inv() const { return pow(MOD-2); }
```

```
Zp pow(11 e) const{ return modPow(x,e,MOD); }
 void print() { cerr << x; } // For deb()</pre>
1: // 82fa
// Extended Euclidean Algorithm
ll egcd(ll a, ll b, ll& x, ll& y) {
 if (!a) return x=0, y=1, b;
 11 d = eqcd(b%a, a, y, x);
 x = b/a*v;
 return d:
1 // 23c8
                                        4b73
math/modular64.h
// Modular arithmetic for modulus < 2^62
11 modAdd(11 x, 11 y, 11 m) {
 x += v;
 return x < m ? x : x-m;
} // b653
11 modSub(11 x, 11 y, 11 m) {
 x -= v;
 return x >= 0 ? x : x+m;
1 // b073
// About 4x slower than normal modulo
ll modMul(ll a, ll b, ll m) {
 ll c = ll((long double) a * b / m);
 11 r = (a*b - c*m) % m;
 return r < 0 ? r+m : r;
} // 1815
ll modPow(11 x, 11 e, 11 m) {
 11 t = 1:
  while (e) {
    if (e \& 1) t = modMul(t, x, m);
   e >>= 1;
   x = modMul(x, x, m);
 } // bd61
 return t;
} // c8ba
math/montgomery.h
                                        a4ba
#include "modular.h"
// Montgomery modular multiplication
// MOD < MG_MULT, gcd (MG_MULT, MOD) must be 1
// Don't use if modulo is constexpr; UNTESTED
constexpr 11 MG_SHIFT = 32;
constexpr 11 MG MULT = 1LL << MG SHIFT;</pre>
constexpr 11 MG MASK = MG MULT - 1;
const 11 MG INV = MG MULT-modInv(MOD, MG MULT);
// Convert to Montgomery form
11 MG(11 x) { return (x*MG_MULT) % MOD; }
// Montgomery reduction
// redc(mg * mg) = Montgomery-form product
11 redc(11 x) {
 11 q = (x * MG_INV) & MG_MASK;
 x = (x + q*MOD) >> MG SHIFT;
 return (x >= MOD ? x-MOD : x);
} // d0f5
math/nimber.h
                                        474f
```

```
// Nimbers are defined as sizes of Nim heaps.
// Operations on nimbers are defined as:
// a+b = mex(\{a'+b : a' < a\} u \{a+b' : b' < b\})
// ab = mex(\{a'b+ab'+a'b' : a' < a, b' < b\})
// Nimbers smaller than M = 2^2 k form a field.
// Addition is equivalent to xor, meanwhile
// multiplication can be evaluated
// in O(1g^2 M) after precomputing.
using ull = uint64 t:
ull nbuf[64][64]; // Nim-products for 2^i * 2^j
// Multiply nimbers; time: O(1g^2 M)
// WARNING: Call initNimMul() before using.
ull nimMul(ull a, ull b) {
 ull ret = 0;
 for (ull s = a; s; s &= (s-1))
    for (ull t = b; t; t &= (t-1))
      ret ^= nbuf | builtin ctzll(s)1
                 [__builtin_ctzll(t)];
  return ret;
} // 25be
// Initialize nim-products lookup table
void initNimMul() {
  rep(i, 0, 64)
    nbuf[i][0] = nbuf[0][i] = 1ull << i;
  rep(b, 1, 64) rep(a, 1, b+1) {
    int i = 1 << (63 - __builtin_clzll(a));</pre>
    int j = 1 << (63 - __builtin_clzll(b));</pre>
    ull t = nbuf[a-i][b-j];
    if (i < j)
      t = nimMul(t, 1ull << i) << j;
      t = nimMul(t, 1ull << (i-1)) ^ (t << i);
    nbuf[a][b] = nbuf[b][a] = t;
 } // ca24
} // 1811
// Compute a^e under nim arithmetic; O(1g^3 M)
// WARNING: Call initNimMul() before using.
ull nimPow(ull a, ull e) {
 ull t = 1;
  while (e) {
    if (e % 2) t = nimMul(t, a);
    e /= 2; a = nimMul(a, a);
 } // da53
  return t;
} // c06c
// Compute inverse of a in 2^64 nim-field:
// time: 0(1a^3 M)
// WARNING: Call initNimMul() before using.
ull nimInv(ull a) {
 return nimPow(a, ull(-2));
} // c6d9
// If you need to multiply many nimbers by
// the same value you can use this to speedup.
// WARNING: Call initNimMul() before using.
struct NimMult (
 ull M[64] = \{0\};
  // Initialize lookup; time: O(lg^2 M)
  NimMult(ull a) {
    for (ull t=a; t; t &= (t-1)) rep(i, 0, 64)
```

```
M[i] ^= nbuf[ builtin ctzll(t)][i];
  } // ea88
  // Multiply by b; time: O(lq M)
  ull operator()(ull b) {
    ull ret = 0:
    for (ull t = b; t; t &= (t-1))
      ret ^= M[ builtin ctzll(t)];
    return ret;
  } // e480
}; // 1b80
                                         8703
math/phi large.h
#include "pollard_rho.h"
// Compute Euler's totient of large numbers
// time: O(n^(1/4)) \leftarrow factorization
ll phi(ll n) {
  each (p, factorize (n)) n = n / p.x * (p.x-1);
  return n:
} // 798e
                                         728b
math/phi precompute.h
Vi phi(1e7+1);
// Precompute Euler's totients; time: O(n lq n)
void calcPhi() {
  iota(all(phi), 0);
  rep(i, 2, sz(phi)) if (phi[i] == i)
    for (int j = i; j < sz(phi); j += i)</pre>
      phi[j] = phi[j] / i * (i-1);
} // 3c65
math/phi prefix sum.h
                                         a9e0
#include "phi_precompute.h"
vector<11> phiSum; // [k] = sum \ from \ 0 \ to \ k-1
// Precompute Euler's totient prefix sums
// for small values; time: O(n lg n)
void calcPhiSum() {
  calcPhi():
  phiSum.resize(sz(phi)+1);
  rep(i, 0, sz(phi))
    phiSum[i+1] = phiSum[i] + phi[i];
} // 3855
// Get prefix sum of phi(0) + ... + phi(n-1).
// WARNING: Call calcPhiSum first!
// For n > 4*10^9, answer will overflow.
// If you wish to get answer mod M use
// commented lines.
ll getPhiSum(ll n) { // time: O(n^{(2/3)})
  static unordered_map<11, 11> big;
  if (n < sz(phiSum)) return phiSum[n];</pre>
  if (big.count(--n)) return big[n];
  11 ret = n*(n+1)/2;
  // 11 ret = (n \% 2 ? n \% M * ((n+1)/2 % M)
                   : n/2%M * (n%M+1)) % M;
  for (11 s, i = 2; i \le n; i = s+1) {
   s = n / (n/i);
    ret -= (s-i+1) * getPhiSum(n/i+1);
```

```
// \text{ ret } -= (s-i+1) \% M * getPhiSum(n/i+1) \% M;
                                                    if (n <= 1) return;</pre>
 } // e792
                                                    if (isPrime(n)) out.pb(n);
                                                    else if (n^2 == 0) rho(out,2), rho(out,n/2);
 // \text{ ret = (ret %M + M) % M;}
                                                    else for (11 a = 2;; a++) {
 return big[n] = ret;
                                                      11 x = 2, y = 2, d = 1;
} // 820b
                                                      while (d == 1) {
                                                        x = modAdd(modMul(x, x, n), a, n);
                                                        y = modAdd(modMul(y, y, n), a, n);
math/pi large precomp.h
                                         7fc0
                                                        y = modAdd(modMul(y, y, n), a, n);
#include "sieve.h"
                                                        d = \underline{gcd(abs(x-y), n)};
                                                      } // 3378
// Count primes in given interval
                                                      if (d != n) {
// using precomputed table.
                                                        rho(out, d);
// Set MAX P to sgrt (MAX N) and run sieve()!
                                                        rho(out, n/d);
// Precomputed table will contain N BUCKETS
                                                        return:
// elements - check source size limit.
                                                     } // 60a2
                                                   1 // 9649
constexpr ll MAX N = 1e11+1;
                                                  } // c181
constexpr ll N BUCKETS = 10000;
constexpr ll BUCKET_SIZE = (MAX_N/N_BUCKETS)+1;
                                                  // Pollard's rho factorization algorithm
constexpr ll precomputed[] = {/* ... */};
                                                  // Las Vegas version; time: n^(1/4)
                                                  // Returns pairs (prime, power), sorted
ll sieveRange(ll from, ll to) {
                                                  vector<Factor> factorize(ll n) {
 bitset < BUCKET_SIZE > elems;
                                                   vector<Factor> ret:
 from = max(from, 2LL);
                                                   vector<ll> raw:
                                                    rho(raw, n);
 to = max(from, to);
                                                    sort(all(raw));
 each (p, primesList) {
   ll c = max((from+p-1) / p, 2LL);
                                                    each(f, raw) {
   for (11 i = c*p; i < to; i += p)</pre>
                                                      if (ret.emptv() | ret.back().x != f)
      elems.set(i-from);
                                                        ret.pb({ f, 1 });
 1 // a29f
 return to-from-elems.count();
                                                        ret.back().y++;
1 // c646
                                                   } // 2ab1
                                                   return ret;
// Run once on local computer to precompute
                                                  ) // 471c
// table. Takes about 10 minutes for n = 1e11.
// Sanity check (for default params):
                                                  math/polynomial interp.h
// 664579, 606028, 587253, 575795, ...
void localPrecompute() {
                                                  // Interpolates set of points (i, vec[i])
                                                  // and returns it evaluated at x; time: O(n)
 for (11 i = 0; i < MAX_N; i += BUCKET_SIZE) {</pre>
   11 to = min(i+BUCKET_SIZE, MAX_N);
                                                  template<class T>
   cout << sieveRange(i, to) << ',' << flush;</pre>
                                                  T polyExtend(vector<T>& vec, T x) {
 } // f6a7
                                                    int n = sz(vec);
 cout << endl;
                                                    vector<T> fac(n, 1), suf(n, 1);
} // 2b1e
                                                    rep(i, 1, n) fac[i] = fac[i-1] \star i;
// Count primes in [from; to) using table.
                                                    for (int i=n; --i;) suf[i-1] = suf[i]*(x-i);
// O(N_BUCKETS + BUCKET_SIZE*lg lg n + sgrt(n))
11 countPrimes(11 from, 11 to) {
                                                    T pref = 1, ret = 0;
 11 bFrom = from/BUCKET SIZE+1,
                                                    rep(i, 0, n) {
    bTo = to/BUCKET SIZE:
                                                     T d = fac[i] * fac[n-i-1] * ((n-i) %2*2-1);
  if (bFrom > bTo) return sieveRange(from, to);
                                                     ret += vec[i] * suf[i] * pref / d;
 11 ret = accumulate (precomputed+bFrom,
                                                     pref \star = x-i;
                      precomputed+bTo, 0);
                                                    } // 681d
  ret += sieveRange(from, bFrom*BUCKET SIZE);
                                                    return ret;
                                                  1 // dd92
 ret += sieveRange (bTo*BUCKET_SIZE, to);
 return ret;
} // cced
                                                  math/sieve.h
                                                  constexpr int MAX P = 1e6;
math/pollard rho.h
                                         0b74
                                                  bitset < MAX P+1> primes:
#include "modular64.h"
                                                  Vi primesList:
#include "miller rabin.h"
                                                  // Erathostenes sieve; time: O(n lg lg n)
using Factor = pair<11, int>;
                                                  void sieve() {
                                                   primes.set();
void rho(vector<11>& out, 11 n) {
                                                   primes.reset(0);
```

```
primes.reset(1);
  for (int i = 2; i*i <= MAX P; i++)
    if (primes[i])
      for (int j = i*i; j <= MAX_P; j += i)</pre>
        primes.reset(j);
  rep(i, 0, MAX P+1) if (primes[i])
    primesList.pb(i);
1 // d5ca
math/sieve factors.h
                                          312d
constexpr int MAX P = 1e6;
Vi factor (MAX P+1);
// Erathostenes sieve with saving smallest
// factor for each number; time: O(n lg lg n)
void sieve() {
  for (int i = 2; i*i <= MAX_P; i++)</pre>
    if (!factor[i])
      for (int j = i*i; j <= MAX_P; j += i)</pre>
        if (!factor[i])
          factor[j] = i;
  rep(i,0,MAX_P+1) if (!factor[i]) factor[i]=i;
1 // 82b6
// Factorize n <= MAX_P; time: O(lg n)</pre>
// Returns pairs (prime, power), sorted
vector < Pii > factorize (ll n) {
  vector<Pii> ret;
  while (n > 1) {
    int f = factor[n];
    if (ret.empty() | ret.back().x != f)
      ret.pb({ f, 1 });
      ret.back().y++;
    n /= f;
  } // 664c
  return ret;
} // bb65
math/sieve segmented.h
                                         849b
constexpr int MAX P = 1e9;
bitset<MAX_P/2+1> primes; // Only odd numbers
// Cache-friendly Erathostenes sieve
// ~1.5s on Intel Core i5 for MAX_P = 10^9
// Memory usage: MAX_P/16 bytes
void sieve() {
  constexpr int SEG_SIZE = 1<<18;</pre>
  int pSqrt = int(sqrt(MAX_P)+0.5);
  vector<Pii> dels;
  primes.set();
  primes.reset(0);
  for (int i = 3; i <= pSqrt; i += 2) {</pre>
    if (primes[i/2]) {
      for (i = i*i; i <= pSart; i += i*2)
        primes.reset(j/2);
      dels.pb(\{i, j/2\});
    } // 9e62
 } // ff49
```

54b5

3f3d

```
for (int seg = pSgrt/2;
                                                         T x = f(off, s[k]);
       seg <= sz(primes); seg += SEG SIZE) {
                                                         if (val > x) i=k, off=x;
    int lim = min(seq+SEG_SIZE, sz(primes));
                                                       } // de7f
    each(d, dels) for (;d.y < \lim; d.y += d.x)
                                                     } // 929c
     primes.reset(d.v);
                                                     return i+2:
                                                  } // 4be9
 } // 97ae
} // 6456
                                                 }; // 3ac1
bool isPrime(int x) {
                                                 structures/fenwick tree 2d.h 9f31
 return x == 2 \mid \mid (x \cdot 2 \cdot \xi \cdot primes[x/2]);
                                                 // Fenwick tree 2D (BIT tree 2D); space: O(n*m)
} // 422c
                                                 // Default version: prefix sums 2D
                                                 // Change s to hashmap for O(g lg^2 n) memory
structures/bitset plus.h
                                         6737
                                                 struct Fenwick2D {
                                                   using T = int;
// Undocumented std::bitset features:
                                                   static constexpr T ID = 0;
// - _Find_first() - returns first bit = 1 or N
                                                   T f(T a, T b) { return a+b; }
// - _Find_next(i) - returns first bit = 1
                    after i-th bit
                                                   vector<T> s:
                    or N if not found
                                                   int w, h;
// Bitwise operations for vector<bool>
                                                   Fenwick2D(int n = 0, int m = 0)
// UNTESTED
                                                     : s(n*m, ID), w(n), h(m) {}
#define OP(x) vector<bool>& operator x##=(
                                                   // A[i,j] = f(A[i,j], v); time: O(lg^2 n)
    vector<bool>& 1, const vector<bool>& r) { \
                                                   void modify(int i, int j, T v) {
  assert(sz(1) == sz(r));
                                                     for (; i < w; i |= i+1)
  auto a = 1.begin(); auto b = r.begin();
                                                       for (int k = j; k < h; k = k+1)
  while (a<1.end()) *a._M_p++ x##= *b._M_p++; \
                                                         s[i*h+k] = f(s[i*h+k], v);
  return 1; } // f164
                                                   } // d46b
OP (&) OP (|) OP (^)
                                                   // Query prefix; time: O(lg^2 n)
structures/fenwick tree.h
                                                   T query(int i, int j) {
                                         992b
                                                     T v = ID;
// Fenwick tree (BIT tree); space: O(n)
                                                     for (; i>0; i&=i-1)
// Default version: prefix sums
                                                       for (int k = j; k > 0; k \le k-1)
struct Fenwick {
                                                        v = f(v, s[i*h+k-h-1]);
  using T = int;
                                                     return v;
  static const T ID = 0;
                                                  } // 08cf
  T f(T a, T b) { return a+b; }
                                                 }; // e570
  vector<T> s;
                                                 structures/find union.h
                                                                                         b4de
  Fenwick(int n = 0) : s(n, ID) {}
                                                 // Disjoint set data structure; space: O(n)
                                                 // Operations work in amortized O(alfa(n))
  // A[i] = f(A[i], v); time: O(lg n)
  void modify(int i, T v) {
                                                 struct FAU {
   for (; i < sz(s); i |= i+1) s[i]=f(s[i],v);
                                                   Vi G:
                                                   FAU(int n = 0) : G(n, -1) {}
  } // a047
  // Get f(A[0], .., A[i-1]); time: O(lg n)
                                                   // Get size of set containing i
                                                   int size(int i) { return -G[find(i)]; }
  T query(int i) {
   T v = ID:
                                                   // Find representative of set containing i
    for (; i > 0; i &= i-1) v = f(v, s[i-1]);
                                                   int find(int i) {
   return v;
                                                     return G[i] < 0 ? i : G[i] = find(G[i]);</pre>
  1 // 9810
                                                   } // 5bc1
  // Find smallest i such that
                                                   // Union sets containing i and j
  // f(A[0],...,A[i-1]) >= val; time: O(lg n)
  // Prefixes must have non-descreasing values.
                                                   bool join(int i, int j) {
                                                     i = find(i); j = find(j);
  int lowerBound(T val) {
    if (val <= ID) return 0;</pre>
                                                     if (i == j) return 0;
    int i = -1, mask = 1;
                                                     if (G[i] > G[j]) swap(i, j);
    while (mask \leq sz(s)) mask \star= 2:
                                                     G[i] += G[j]; G[j] = i;
    T off = ID;
                                                     return 1;
                                                   } // c721
                                                 }; // 62a4
    while (mask /= 2) {
     int k = mask+i;
     if (k < sz(s)) {
                                                 structures/hull offline.h
                                                                                          3030
```

```
constexpr 11 INF = 2e18;
// constexpr double INF = 1e30;
// constexpr double EPS = 1e-9;
// MAX of linear functions; space: O(n)
// Use if you add lines in increasing `a` order
// Default uncommented version is for int64
struct Hull {
 using T = 11; // Or change to double
  struct Line {
   T a, b, end;
    T intersect (const Line& r) const {
      // Version for double:
      //if (r.a-a < EPS) return b>r.b?INF:-INF;
      //return (b-r.b) / (r.a-a);
      if (a==r.a) return b > r.b ? INF : -INF;
      11 u = b-r.b, d = r.a-a;
      return u/d + ((u^d) >= 0 || !(u^d));
   } // f27f
 }; // 10dc
  vector<Line> S;
  Hull() { S.pb({ 0, -INF, INF }); }
  // Insert f(x) = ax+b; time: amortized O(1)
  void push(T a, T b) {
   Line 1{a, b, INF};
    while (true) {
      T e = S.back().end=S.back().intersect(1);
      if (sz(S) < 2 | | S[sz(S)-2].end < e)
       break:
      S.pop_back();
   } // 044f
    S.pb(1);
 } // 978e
  // Query max(f(x)) for each f): time: O(lq n)
 T query (T x) {
    auto t = *upper_bound(all(S), x,
      [](int 1, const Line& r) {
        return 1 < r.end;</pre>
      }); // de77
    return t.a*x + t.b;
 } // b8de
1: // 1d64
structures/hull online.h
                                         2a7b
constexpr 11 INF = 2e18;
// MAX of linear functions online; space: O(n)
struct Hull {
 static bool modeQ; // Toggles operator< mode</pre>
  struct Line {
    mutable 11 a, b, end;
    ll intersect (const Line& r) const {
      if (a==r.a) return b > r.b ? INF : -INF;
      11 u = b-r.b, d = r.a-a;
      return u/d + ((u^d) >= 0 | | !(u^d));
   } // f27f
    bool operator<(const Line& r) const {</pre>
      return modeO ? end < r.end : a < r.a;</pre>
    1 // cfab
```

```
}; // 6046
  multiset < Line > S:
  Hull() { S.insert({ 0, -INF, INF }); }
  // Updates segment end
  bool update(multiset<Line>::iterator it) {
    auto cur = it++; cur->end = INF;
    if (it == S.end()) return false;
    cur->end = cur->intersect(*it):
    return cur->end >= it->end;
 } // 63b8
  // Insert f(x) = ax+b; time: O(lg n)
  void insert(ll a, ll b) {
    auto it = S.insert({ a, b, INF });
    while (update(it)) it = --S.erase(++it);
    rep(i, 0, 2)
      while (it != S.begin() && update(--it))
        update(it = --S.erase(++it));
 } // 4f69
  // Query max(f(x) for each f): time: O(lg n)
  ll query(ll x) {
    modeQ = 1;
    auto 1 = *S.upper_bound({ 0, 0, x });
    mode0 = 0:
    return 1.a*x + 1.b;
 } // 7533
}; // 037e
bool Hull::modeQ = false;
structures/max queue.h
                                        3e9e
// Queue with max query on contained elements
struct MaxOueue {
  using T = int;
  deque<T> 0, M;
  // Add v to the back; time: amortized O(1)
  void push(T v) {
    while (!M.empty() && M.back() < v)
      M.pop_back();
    M.pb(v); Q.pb(v);
  1 // 57a2
  // Pop from the front; time: O(1)
  } () gog biov
    if (M.front() == 0.front()) M.pop front();
    Q.pop_front();
  } // 101c
  // Get max element value; time: O(1)
 T max() const { return M.front(); }
}; // b6c4
structures/pairing heap.h
                                        b2a7
// Pairing heap implementation; space O(n)
// Elements are stored in vector for faster
// allocation. It's MINIMUM queue.
// Allows to merge heaps in O(1)
template < class T, class Cmp = less < T>>
struct PHeap {
  struct Node {
```

T val:

```
int child{-1}, next{-1}, prev{-1};
 Node (T x = T()) : val(x) \{\}
}; // 11ee
using Vnode = vector < Node>:
Vnode& M;
int root{-1};
int unlink(int& i) {
 if (i >= 0) M[i].prev = -1;
 int x = i; i = -1;
 return x:
} // d9f6
void link(int host, int& i, int val) {
 if (i >= 0) M[i].prev = -1;
 i = val;
 if (i >= 0) M[i].prev = host;
} // 47d5
int merge(int 1, int r) {
 if (1 < 0) return r;</pre>
 if (r < 0) return 1;</pre>
 if (Cmp()(M[1].val, M[r].val)) swap(l, r);
 link(1, M[1].next, unlink(M[r].child));
 link(r, M[r].child, 1);
 return r;
} // fc42
int mergePairs(int v) {
 if (v < 0 || M[v].next < 0) return v;</pre>
 int v2 = unlink(M[v].next);
 int v3 = unlink(M[v2].next);
 return merge (merge (v, v2), mergePairs (v3));
} // 2eea
// Initialize heap with given node storage
// Just declare 1 Vnode and pass it to heaps
PHeap(Vnode& mem) : M(mem) {}
// Add given key to heap, returns index; O(1)
int push (const T& x) {
 int index = sz(M);
 M.emplace back(x);
 root = merge(root, index);
  return index;
} // e744
// Change key of i to smaller value; O(1)
void decrease(int i, T val) {
  assert(!Cmp()(M[i].val, val));
 M[i].val = val;
  int prev = M[i].prev;
 if (prev < 0) return;</pre>
  auto& p = M[prev];
 link (prev. (p.child == i ? p.child
       : p.next), unlink(M[i].next));
  root = merge(root, i);
} // 1a67
```

```
bool empty() { return root < 0; }</pre>
 const T& top() { return M[root].val; }
 // Merge with other heap. Must use same vec.
 void merge(PHeap& r) { // time: 0(1)
   assert (&M == &r.M);
   root = merge(root, r.root); r.root = -1;
 } // 9623
 // Remove min element; time: O(lq n)
 void pop() {
   root = mergePairs (unlink (M[root].child));
 ) // 5b13
}; // 09f3
structures/rmg.h
                                        9649
// Range Minimum Query; space: O(n lg n)
struct RMO {
 using T = int:
 static constexpr T ID = INT_MAX;
 T f(T a, T b) { return min(a, b); }
 vector<vector<T>>> s;
 // Initialize RMQ structure; time: O(n lg n)
 RMO(const vector<T>& vec = {}) {
   s = \{vec\};
   for (int h = 1; h \le sz(vec); h *= 2) {
     s.emplace back();
     auto prev = s[sz(s)-2];
     rep(i, 0, sz(vec)-h*2+1)
       s.back().pb(f(prev[i], prev[i+h]));
   1 // b5ff
 } // cf67
 // Query f(s[b], ..., s[e-1]); time: O(1)
 T query(int b, int e) {
   if (b >= e) return ID;
   int k = 31 - __builtin_clz(e-b);
   return f(s[k][b], s[k][e - (1<<k)]);</pre>
 } // caaa
}; // 9b64
structures/segtree config.h 095b
// Segment tree configurations to be used
// in segtree general and segtree persistent.
// See comments in TREE_PLUS version
// to understand how to create custom ones.
// Capabilities notation: (update; query)
#if TREE_PLUS // (+; sum, max, max count)
 // time: O(lq n) [UNTESTED]
 using T = int; // Data type for update
                 // operations (lazy tag)
 const T ID = 0; // Neutral value for
                 // updates and lazy tags
 // This structure keeps aggregated data
 struct Agg {
   // Aggregated data: sum, max, max count
   // Default values should be neutral
   // values, i.e. "aggregate over empty set"
   T sum{0}, vMax{INT MIN}, nMax{0};
```

```
// Initialize as leaf (single value)
   void leaf() { sum = vMax = 0; nMax = 1; }
   // Combine data with aggregated data
   // from node to the right
   void merge(const Agg& r) {
     if (vMax < r.vMax) nMax = r.nMax;</pre>
     else if (vMax == r.vMax) nMax += r.nMax;
     vMax = max(vMax, r.vMax);
     sum += r.sum:
   } // 8850
   // Apply update provided in `x`:
   // - update aggregated data
   // - update lazy tag `lazy`
   // - `size` is amount of elements
   // - return 0 if update should branch
   // (to be used in "segement tree beats")
   // - if you change value of `x` changed
   // value will be passed to next node
   // to the right during updates
   bool apply (T& lazy, T& x, int size) {
     lazy += x;
     sum += x*size;
     vMax += x:
     return 1;
   } // 4858
 }; // 9bf5
#elif TREE_MAX // (max; max, max count)
 // time: O(lq n) [UNTESTED]
 using T = int;
 const T ID = INT_MIN;
 struct Agg {
   // Aggregated data: max value, max count
   T vMax{INT_MIN}, nMax{0};
   void leaf() { vMax = 0; nMax = 1; }
   void merge(const Agg& r) {
     if (vMax < r.vMax) nMax = r.nMax;</pre>
     else if (vMax == r.vMax) nMax += r.nMax;
     vMax = max(vMax, r.vMax);
   } // f56b
   bool apply (T& lazy, T& x, int size) {
     if (vMax <= x) nMax = size;</pre>
     lazy = max(lazy, x);
     vMax = max(vMax, x);
     return 1:
   } // 8bd5
 1: // 15b6
#elif TREE_SET // (=; sum, max, max count)
// time: O(lq n) [UNTESTED]
 // Set ID to some unused value.
 using T = int;
 const T ID = INT MIN;
 struct Agg {
   // Aggregated data: sum, max, max count
   T sum{0}, vMax{INT MIN}, nMax{0};
   void leaf() { sum = vMax = 0; nMax = 1; }
   void merge(const Agg& r) {
     if (vMax < r.vMax) nMax = r.nMax;</pre>
     else if (vMax == r.vMax) nMax += r.nMax;
     vMax = max(vMax, r.vMax);
```

```
sum += r.sum;
   } // 8850
   bool apply (T& lazy, T& x, int size) {
     lazv = x:
     sum = x*size;
     vMax = x;
     nMax = size;
     return 1;
   } // 845b
 1: // 7488
#elif TREE BEATS // (+, min; sum, max)
 // time: amortized O(lg n) if not using +
         amortized O(lg^2 n) if using +
 // Lazy tag is pair (add, min).
 // To add x: run update with {x, INT_MAX},
 // to min x: run update with {0, x}.
 // When both parts are provided addition
 // is applied first, then minimum.
 using T = Pii;
 const T ID = {0, INT_MAX};
 struct Agg {
   // Aggregated data: max value, max count,
                       second max value, sum
   int vMax{INT_MIN}, nMax{0}, max2{INT_MIN};
   int sum{0};
   void leaf() { sum = vMax = 0; nMax = 1; }
   void merge(const Agg& r) {
     if (r.vMax > vMax) {
       max2 = vMax;
       vMax = r.vMax;
       nMax = r.nMax;
     } else if (r.vMax == vMax) {
       nMax += r.nMax;
     } else if (r.vMax > max2) {
       max2 = r.vMax;
     } // b074
     max2 = max(max2, r.max2);
     sum += r.sum;
   } // 3124
   bool apply (T& lazy, T& x, int size) {
     if (max2 != INT_MIN && max2+x.x >= x.y)
       return 0:
     lazv.x += x.x;
     sum += x.x*size:
     vMax += x.x;
     if (max2 != INT MIN) max2 += x.x;
     if (x.v < vMax) {
       sum -= (vMax-x.y) * nMax;
       vMax = x.v;
     } // 7025
     lazy.y = vMax;
     return 1;
   } // fe0c
 1: // 2924
#endif
structures/segtree general.h 725a
// Highly configurable statically allocated
```

// (interval; interval) segment tree;

// space: O(n) [UNTESTED]

```
struct SegTree {
  // Choose/write configuration
  #include "seatree config.h"
  // Root node is 1, left is i*2, right i*2+1
  vector<Agg> agg; // Aggregated data for nodes
  vector<T> lazy; // Lazy tags for nodes
  int len{1};
                  // Number of leaves
  // Initialize tree for n elements; time: O(n)
  SegTree(int n = 0) {
    while (len < n) len *= 2;
    agg.resize(len*2);
   lazv.resize(len*2, ID);
   rep(i, 0, n) agg[len+i].leaf();
    for (int i = len; --i;)
      (agg[i] = agg[i*2]).merge(agg[i*2+1]);
  } // 4417
  void push(int i, int s) {
   if (lazy[i] != ID) {
      agg[i*2].apply(lazy[i*2], lazy[i], s/2);
     agg[i*2+1].apply(lazy[i*2+1],
                       lazy[i], s/2);
     lazy[i] = ID;
   } // 3ba9
  } // 5d19
  // Modify interval [vb;ve) with val; O(lq n)
  T update(int vb, int ve, T val, int i = 1,
          int b = 0, int e = -1) {
    if (e < 0) e = len;</pre>
   if (vb >= e || b >= ve) return val;
    if (b >= vb && e <= ve &&
       agg[i].apply(lazy[i], val, e-b))
     return val:
    int m = (b+e) / 2;
   push(i, e-b);
   val = update(vb, ve, val, i \star 2, b, m);
   val = update(vb, ve, val, i*2+1, m, e);
    (agg[i] = agg[i*2]).merge(agg[i*2+1]);
   return val:
  } // aa8e
  // Query interval [vb;ve); time: O(lg n)
  Agg guery(int vb, int ve, int i = 1,
           int b = 0, int e = -1) {
    if (e < 0) e = len;
   if (vb >= e || b >= ve) return {};
   if (b >= vb && e <= ve) return agg[i];</pre>
   int m = (b+e) / 2;
   push(i, e-b);
    Agg t = query(vb, ve, i*2, b, m);
   t.merge(query(vb, ve, i*2+1, m, e));
    return t;
 } // lale
1: // db5c
```

structures/segtree persist.h dcfc

```
// Highly configurable (interval; interval)
// persistent segment tree;
// space: O(queries lq n) [UNTESTED]
// First tree version number is 0.
```

```
struct SegTree {
 // Choose/write configuration
 #include "seatree config.h"
 vector<Agg> agg: // Aggregated data for nodes
 vector<T> lazv: // Lazv tags for nodes
 vector<bool> cow; // Copy children on push?
 Vi L. R:
                  // Children links
 int len{1};
                  // Number of leaves
 // Initialize tree for n elements; O(lq n)
 SegTree(int n = 0) {
   int k = 1:
   while (len < n) len *= 2, k++;
   agg.resize(k);
   lazy.resize(k, ID);
   cow.resize(k, 1);
   L.resize(k);
   R.resize(k);
   agg[--k].leaf();
   while (k--) {
     (agg[k] = agg[k+1]).merge(agg[k+1]);
     L[k] = R[k] = k+1;
   } // 211f
 } // 83cf
 // New version from version `i`; time: O(1)
 // First version number is 0.
 int fork(int i) {
   L.pb(L[i]); R.pb(R[i]); cow.pb(cow[i] = 1);
   agg.pb(agg[i]); lazy.pb(lazy[i]);
   return sz(L)-1;
 } // a21b
 void push(int i, int s, bool w) {
   bool has = (lazy[i] != ID);
   if ((has | | w) && cow[i]) {
     int a = fork(L[i]), b = fork(R[i]);
     L[i] = a; R[i] = b; cow[i] = 0;
   } // 1a3e
   if (has) {
     agg[L[i]].apply(lazy[L[i]],lazy[i],s/2);
     agg[R[i]].apply(lazy[R[i]],lazy[i],s/2);
     lazy[i] = ID;
   } // eca6
 } // 9f84
 // Modify interval [vb;ve) with val
 // in tree version `i`; time: O(lq n)
 T update(int i, int vb, int ve, T val,
          int b = 0, int e = -1) {
   if (e < 0) e = len;</pre>
   if (vb >= e || b >= ve) return val;
   if (b >= vb && e <= ve &&
       agg[i].apply(lazy[i], val, e-b))
     return val:
   int m = (b+e) / 2;
   push (i, e-b, 1);
   val = update(L[i], vb, ve, val, b, m);
   val = update(R[i], vb, ve, val, m, e);
    (agg[i] = agg[L[i]]).merge(agg[R[i]]);
   return val;
```

```
} // 776e
 // Ouerv interval [vb:ve)
 // in tree version `i`; time: O(lq n)
 Agg query (int i, int vb, int ve,
           int b = 0, int e = -1) {
   if (e < 0) e = len;
   if (vb >= e || b >= ve) return {};
   if (b >= vb && e <= ve) return agg[i];</pre>
   int m = (b+e) / 2;
   push(i, e-b, 0);
   Agg t = query(L[i], vb, ve, b, m);
   t.merge(query(R[i], vb, ve, m, e));
   return t:
 } // abf4
1: // 8a44
structures/segtree_point.h
// Segment tree (point, interval)
// Configure by modifying:
// - T - stored data type
// - ID - neutral element for guery operation
// - merge(a, b) - combine results
struct SegTree {
 using T = int;
 static constexpr T ID = INT MIN;
 static T merge(T a, T b) { return max(a,b); }
 vector<T> V:
 int len:
  // Initialize tree for n elements; time: O(n)
 SegTree(int n = 0, T def = ID) {
   for (len = 1; len < n; len *= 2);
   V.resize(len*2, ID);
   rep(i, 0, n) V[len+i] = def;
   for (int i = len; --i;)
     V[i] = merge(V[i*2], V[i*2+1]);
 1 // 99c8
  // Set element `i` to `val`; time: O(lq n)
 void set(int i, T val) {
   V[i += len] = val;
   while (i \neq 2)
     V[i] = merge(V[i*2], V[i*2+1]);
 } // ff1f
 // Ouery interval [b;e); time: O(lg n)
 T query(int b, int e) {
   b += len; e += len-1;
   if (b > e) return ID;
   if (b == e) return V[b];
   T \times = merge(V[b], V[e]);
   while (b/2 < e/2) {
     if (b\&1) x = merge(x, V[b^1]);
     if (e&1) x = merge(x, V[e^1]);
     b /= 2; e /= 2;
   1 // 737d
   return x;
 } // 2014
}; // 40d8
```

constexpr SegTree::T SegTree::ID;

```
structures/treap.h
```

```
bbb4
// "Set" of implicit keyed treaps; space: O(n)
// Nodes are keyed by their indices in array
// of all nodes. Treap key is key of its root.
// "Node x" means "node with key x".
// "Treap x" means "treap with key x".
// Kev -1 is "null".
// Put any additional data in Node struct.
struct Treap {
 struct Node {
   // E[0] = left child, <math>E[1] = right child
   // weight = node random weight (for treap)
   // size = subtree size, par = parent node
   int E[2] = \{-1, -1\}, weight{rand()};
   int size{1}, par{-1};
   bool flip{0}; // Is interval reversed?
 1: // c082
 vector<Node> G; // Array of all nodes
 // Initialize structure for n nodes
 // with keys 0, ..., n-1; time: O(n)
 // Each node is separate treap.
 // use join() to make sequence.
 Treap(int n = 0) : G(n) {}
 // Create new treap (a single node),
 // returns its key; time: O(1)
 int make() {
   G.emplace_back(); return sz(G)-1;
 } // 907a
 // Get size of node x subtree. x can be -1.
 int size(int x) { // time: 0(1)
   return (x \ge 0 ? G[x].size : 0);
 } // 81cf
 // Propagate down data (flip flag etc).
 // x can be -1; time: O(1)
 void push(int x) {
   if (x >= 0 && G[x].flip) {
     G[x].flip = 0;
      swap(G[x].E[0], G[x].E[1]);
     each(e, G[x].E) if (e>=0) G[e].flip ^= 1;
   } // + any other lazy operations
 } // ed19
 // Update aggregates of node x.
 // x can be -1; time: O(1)
 void update(int x) {
   if (x >= 0) {
     int& s = G[x].size = 1;
     G[x].par = -1;
     each (e, G[x].E) if (e >= 0) {
       s += G[e].size;
       G[e].par = x;
     } // f7a7
   } // + any other aggregates
 // Split treap x into treaps 1 and r
 // such that 1 contains first i elements
 // and r the remaining ones.
 // x, 1, r can be -1; time: ^{\circ}O(lg n)
```

void split(int x, int& l, int& r, int i) {

push(x): 1 = r = -1:

```
if (x < 0) return;
  int key = size(G[x].E[0]);
  if (i <= kev) {
   split(G[x].E[0], 1, G[x].E[0], i);
 } else {
   split(G[x].E[1], G[x].E[1], r, i-key-1);
   1 = x:
 } // fe19
 update(x);
} // 8211
// Join treaps 1 and r into one treap
// such that elements of 1 are before
// elements of r. Returns new treap.
// l. r and returned value can be -1.
int join(int 1, int r) { // time: ~O(lg n)
 push(1); push(r);
 if (1 < 0 || r < 0) return max(1, r);</pre>
  if (G[1].weight < G[r].weight) {</pre>
   G[1].E[1] = join(G[1].E[1], r);
   update(1);
   return 1:
 ) // 18c7
 G[r].E[0] = join(1, G[r].E[0]);
 update(r);
 return r;
1 // b559
// Find i-th node in treap x.
// Returns its key or -1 if not found.
// x can be -1; time: ~O(lq n)
int find(int x, int i) {
  while (x \ge 0) {
   push(x);
   int key = size(G[x].E[0]);
   if (kev == i) return x;
   x = G[x].E[key < i];
   if (key < i) i -= key+1;</pre>
  } // 054c
 return -1;
1 // 0b9b
// Get key of treap containing node x
// (key of treap root). x can be -1.
int root(int x) { // time: ~O(lq n)
 while (G[x].par \ge 0) x = G[x].par;
 return x;
} // be8b
// Get position of node x in its treap.
// x is assumed to NOT be -1; time: ~O(lq n)
int index(int x) {
  int p, i = size(G[x].E[G[x].flip]);
  while ((p = G[x].par) >= 0) {
   if (G[p].E[1] == x) i+=size(G[p].E[0])+1;
   if (G[p].flip) i = G[p].size-i-1;
   x = p;
 } // 3f81
 return i:
} // ddad
// Reverse interval [1:r) in treap x.
// Returns new key of treap; time: ~O(lq n)
```

```
int reverse(int x, int 1, int r) {
    int a, b, c;
    split(x, b, c, r);
    split(b, a, b, 1);
    if (b >= 0) G[b].flip ^= 1;
    return join(join(a, b), c);
 } // e418
1: // 6a6c
structures/wavelet tree.h
                                         69f4
// Wavelet tree ("merge-sort tree over values")
// Each node represent interval of values.
// seg[1]
              = original sequence
// seg[i]
              = subsequence with values
                represented by i-th node
// left[i][j] = how many values in seq[0:j)
                go to left subtree
struct WaveletTree {
  vector<Vi> seq, left;
  int len:
  // Build wavelet tree for sequence `elems`;
  // time and space: O((n+maxVal) log maxVal)
  // Values are expected to be in [0; maxVal).
  WaveletTree(const Vi& elems, int maxVal) {
    for (len = 1; len < maxVal; len *= 2);</pre>
    seq.resize(len*2);
    left.resize(len*2);
    seq[1] = elems;
    build(1, 0, len);
  } // a5e9
  void build(int i, int b, int e) {
    if (i >= len) return;
    int m = (b+e) / 2;
    left[i].pb(0);
    each(x, seq[i]) {
      left[i].pb(left[i].back() + (x < m));
      seq[i*2 + (x >= m)].pb(x);
    } // ac25
    build(i*2, b, m);
    build(i*2+1, m, e);
  } // 8153
  // Find k-th smallest element in [begin; end)
  // [begin;end); time: O(log maxVal)
  int kth(int begin, int end, int k, int i=1) {
    if (i >= len) return seg[i][0];
    int x = left[i][begin], y = left[i][end];
    if (k < y-x) return kth(x, y, k, i*2);
    return kth (begin-x, end-y, k-y+x, i*2+1);
  } // 7861
  // Count number of elements >= vb and < ve
  // in [begin;end); time: O(log maxVal)
  int count (int begin, int end, int vb, int ve,
            int i = 1, int b = 0, int e = -1) {
    if (e < 0) e = len;
    if (b >= ve || vb >= e) return 0;
    if (b >= vb && e <= ve) return end-begin;
    int m = (b+e) / 2;
    int x = left[i][begin], y = left[i][end];
    return count (x, y, vb, ve, i*2, b, m) +
      count (begin-x, end-y, vb, ve, i*2+1,m,e);
  } // 71cf
1: // dd48
```

```
structures/ext/hash table.h 2d30
#include <ext/pb ds/assoc container.hpp>
using namespace __gnu_pbds;
// gp_hash_table<K, V> = faster unordered_set
// Anti-anti-hash
const size_t HXOR = mt19937_64(time(0))();
template < class T> struct SafeHash {
 size t operator()(const T& x) const {
   return hash<T>()(x ^ T(HXOR));
}; // 7d0e
structures/ext/rope.h
                                       0.51f
#include <ext/rope>
using namespace __gnu_cxx;
// rope<T> = implicit cartesian tree
structures/ext/tree.h
                                       a3bc
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb ds/tree policy.hpp>
using namespace __gnu_pbds;
template < class T, class Cmp = less < T>>
using ordered_set = tree<</pre>
 T, null_type, Cmp, rb_tree_tag,
 tree order statistics node update
// Standard set functions and:
// t.order_of_key(key) - index of first >= key
// t.find_by_order(i) - find i-th element
// t1.join(t2) - assuming t1<>t2 merge t2 to t1
structures/ext/trie.h
                                       5cc2
#include <ext/pb ds/assoc container.hpp>
#include <ext/pb_ds/trie_policy.hpp>
using namespace __gnu_pbds;
using pref trie = trie<
 string, null type,
 trie string access traits. pat trie tag,
 trie_prefix_search_node_update
                                       697d
text/aho corasick.h
constexpr char AMIN = 'a'; // Smallest letter
constexpr int ALPHA = 26; // Alphabet size
// Aho-Corasick algorithm for linear-time
// multiple pattern matching.
// Add patterns using add(), then call build().
struct Aho {
 vector<array<int, ALPHA>> nxt{1};
 Vi suf = \{-1\}, accLink = \{-1\};
 vector<Vi> accept{1};
 // Add string with given ID to structure
  // Returns index of accepting node
 int add(const string& str, int id) {
   int i = 0;
   each(c, str) {
     if (!nxt[i][c-AMIN]) {
```

```
nxt[i][c-AMIN] = sz(nxt);
        nxt.pb({}); suf.pb(-1);
        accLink.pb(1); accept.pb({});
      } // 5ead
      i = nxt[i][c-AMIN];
    1 // ace9
    accept[i].pb(id);
    return i:
 } // 27c8
  // Build automata; time: O(V*ALPHA)
 void build() {
    queue<int> que:
    each(e, nxt[0]) if (e) {
      suf[e] = 0; que.push(e);
    } // c34d
    while (!que.empty()) {
      int i = que.front(), s = suf[i], j = 0;
      que.pop();
      each(e, nxt[i]) {
       if (e) que.push(e);
        (e ? suf[e] : e) = nxt[s][j++];
      } // 8521
      accLink[i] = (accept[s].empty() ?
          accLink[s] : s);
    } // 1e8a
 } // 2561
  // Append `c` to state `i`
 int next(int i, char c) {
    return nxt[i][c-AMIN];
 } // 6bb7
  // Call `f` for each pattern accepted
 // when in state `i` with its ID as argument.
  // Return true from `f` to terminate early.
  // Calls are in descreasing length order.
 template<class F> void accepted(int i, F f) {
   while (i != -1) {
      each(a, accept[i]) if (f(a)) return;
     i = accLink[i];
    } // c175
 } // 1f0d
}; // 2768
text/kmp.h
                                        5729
// Computes prefsuf array; time: O(n)
// ps[i] = max prefsuf of [0;i); ps[0] := -1
template < class T > Vi kmp (const T& str) {
 Vi ps; ps.pb(-1);
 each(x, str) {
    int k = ps.back();
    while (k \ge 0 \&\& str[k] != x) k = ps[k];
    ps.pb(k+1);
 } // 05aa
 return ps;
} // 8a6c
```

// Finds occurences of pat in vec; time: O(n)

pat.pb(-1); // SET TO SOME UNUSED CHARACTER

// Returns starting indices of matches.

Vi match (const T& str, T pat) {

pat.insert(pat.end(), all(str));

template<class T>

int n = sz(pat);

Vi ret, ps = kmp(pat);

rep(i, 0, sz(ps)) {

```
if (ps[i] == n) ret.pb(i-2*n-1);
  } // ale9
  return ret;
} // f986
text/kmr.h
                                         ee8c
// KMR algorithm for O(1) lexicographical
// comparison of substrings.
struct KMR {
  vector<Vi> ids;
  KMR() {}
  // Initialize structure; time: O(n lg^2 n)
  // You can change str type to Vi freely.
  KMR (const string& str) {
    ids.clear();
    ids.pb(Vi(all(str)));
    for (int h = 1; h \le sz(str); h *= 2) {
     vector<pair<Pii, int>> tmp;
      rep(j, 0, sz(str)) {
       int a = ids.back()[j], b = -1;
       if (j+h < sz(str)) b = ids.back()[j+h];
        tmp.pb({ {a, b}, j });
      1 // a210
      sort(all(tmp));
      ids.emplace_back(sz(tmp));
      int n = 0:
      rep(j, 0, sz(tmp)) {
       if (j > 0 && tmp[j-1].x != tmp[j].x)
        ids.back()[tmp[j].y] = n;
     } // bd2e
   } // 969a
  } // a40e
  // Get representative of [begin; end); 0(1)
  Pii get (int begin, int end) {
    if (begin >= end) return {0, 0};
    int k = 31 - builtin clz(end-begin);
    return {ids[k][begin], ids[k][end-(1<<k)]};</pre>
  } // 85f3
  // Compare [b1;e1) with [b2;e2); O(1)
  // Returns -1 if <, 0 if ==, 1 if >
  int cmp(int b1, int e1, int b2, int e2) {
   int 11 = e1-b1, 12 = e2-b2;
    int 1 = min(11, 12);
   Pii x = get (b1, b1+1), y = get (b2, b2+1);
    if (x == y) return (11 > 12) - (11 < 12);</pre>
    return (x > y) - (x < y);
  ) // bf42
  // Compute suffix array of string; O(n)
  Vi sufArrav() {
   Vi sufs(sz(ids.back()));
    rep(i, 0, sz(ids.back()))
     sufs[ids.back()[i]] = i;
    return sufs;
  1 // d98d
```

```
}; // 457e
text/lcp.h
                                        0c65
// Compute Longest Common Prefix array for
// given string and it's suffix array; O(n)
// In order to compute suffix array use kmr.h
// or suffix_array_linear.h
template<class T>
Vi lcpArrav(const T& str. const Vi& sufs) {
 int n = sz(str), k = 0;
 Vi pos(n), lcp(n-1);
 rep(i, 0, n) pos[sufs[i]] = i;
 rep(i, 0, n) {
   if (pos[i] < n-1) {
     int j = sufs[pos[i]+1];
      while (i+k < n && j+k < n &&
          str[i+k] == str[j+k]) k++;
     lcp[pos[i]] = k;
   } // 2cba
   if (k > 0) k--;
 1 // 8b22
 return lcp;
1 // d438
text/lyndon factorization.h 688c
// Compute Lyndon factorization for s; O(n)
// Word is simple iff it's stricly smaller
// than any of it's nontrivial suffixes.
// Lyndon factorization is division of string
// into non-increasing simple words.
// It is unique.
vector<string> duval(const string& s) {
 int n = sz(s), i = 0;
 vector<string> ret;
  while (i < n) {
    int j = i+1, k = i;
    while (j < n \&\& s[k] <= s[j])
     k = (s[k] < s[j] ? i : k+1), j++;
    while (i <= k)
      ret.pb(s.substr(i, j-k)), i += j-k;
 } // 3f17
 return ret;
} // 0e48
text/main lorentz.h
                                        9afb
#include "z function.h"
struct Sar {
 int begin, end, len;
}; // f012
// Main-Lorentz algorithm for finding
// all squares in given word; time: O(n lq n)
// Results are in compressed form:
// (b, e, 1) means that for each b <= i < e
// there is square at position i of size 21.
// Each square is present in only one interval.
vector < Sqr > lorentz (const string& s) {
 int n = sz(s):
 if (n <= 1) return {};</pre>
```

auto ans = lorentz(a);

each (p. lorentz (b))

```
ans.pb(\{p.begin+n/2, p.end+n/2, p.len\});
                                                  string ra(a.rbegin(), a.rend());
                                                  string rb(b.rbegin(), b.rend());
                                                  rep(j, 0, 2) {
                                                    Vi z1 = prefPref(ra), z2 = prefPref(b+a);
                                                    z1.pb(0); z2.pb(0);
                                                    rep(c, 0, sz(a)) {
                                                      int 1 = sz(a) - c;
                                                      int x = c - \min(1-1, z1[1]);
                                                      int y = c - max(1-z2[sz(b)+c], j);
                                                      if (x > v) continue;
                                                      if (j)
                                                        ans.pb(\{n-y-1*2, n-x-1*2+1, 1\});
                                                      6156
                                                        ans.pb(\{x, y+1, 1\});
                                                   } // 6c51
                                                   a.swap(rb);
                                                   b.swap(ra);
                                                 1 // b6b2
                                                  return ans;
                                                ) // 5567
                                                                                         8680
                                                text/manacher.h
                                                // Manacher algorithm; time: O(n)
                                                // Finds largest radiuses for palindromes:
                                                // r[2*i] = for center at i (single letter = 1)
                                                // r[2*i+1] = for center between i and i+1
                                                template < class T > Vi manacher (const T& str) {
                                                 int n = sz(str)*2, c = 0, e = 1;
                                                 Vi r(n, 1);
                                                  auto get = [&](int i) { return i%2 ? 0 :
                                                    (i \ge 0 \&\& i < n ? str[i/2] : i); }; // 3d98
                                                  rep(i, 0, n) {
                                                    if (i < e) r[i] = min(r[c*2-i], e-i);</pre>
                                                    while (\text{get}(i-r[i]) == \text{get}(i+r[i])) r[i]++;
                                                    if (i+r[i] > e) c = i, e = i+r[i]-1;
                                                 } // Of87
                                                  rep(i, 0, n) r[i] /= 2;
                                                 return r;
                                                } // a300
                                                text/min rotation.h
                                                                                         e4d6
                                                // Find lexicographically smallest
                                                // rotation of s; time: O(n)
                                                // Returns index where shifted word starts.
                                                // You can use std::rotate to get the word:
                                                // rotate(s.begin(), v.begin()+minRotation(v),
                                                          v.end());
                                                int minRotation(string s) {
                                                 int a = 0, n = sz(s); s += s;
                                                  rep(b, 0, n) rep(i, 0, n) {
                                                   if (a+i == b || s[a+i] < s[b+i]) {</pre>
                                                     b += max(0, i-1); break;
                                                    } // 865b
auto a = s.substr(0, n/2), b = s.substr(n/2);
                                                    if (s[a+i] > s[b+i]) {
                                                     a = b; break;
                                                    1 // 7628
```

```
return a;
} // 9ed8
text/palindromic tree.h
                                        8d2d
constexpr int ALPHA = 26; // Set alphabet size
// Tree of all palindromes in string,
// constructed online by appending letters.
// space: O(n*ALPHA); time: O(n)
// Code marked with [EXT] is extension for
// calculating minimal palindrome partition
// in O(n lg n). Can also be modified for
// similar dynamic programmings.
struct PalTree {
 Vi txt; // Text for which tree is built
 // Node 0 = empty palindrome (root of even)
 // Node 1 = "-1" palindrome (root of odd)
 Vi len{0, -1}; // Lengths of palindromes
 Vi link{1, 0}; // Suffix palindrome links
 // Edges to next palindromes
 vector<array<int, ALPHA>> to{ {}, {} };
 int last{0}; // Current node (max suffix pal)
 Vi diff{0, 0}; // len[i]-len[link[i]] [EXT]
 Vi slink{0, 0}; // Serial links
                                         [EXT]
 Vi series {0, 0}; // Series DP answer
                                         [EXT]
 Vi ans{0};
                  // DP answer for prefix[EXT]
 int ext(int i) {
   while (len[i]+2 > sz(txt) ||
           txt[sz(txt)-len[i]-2] != txt.back())
     i = link[i]:
   return i;
 1 // d442
 // Append letter from [0; ALPHA]; time: O(1)
 // (or O(lq n) if [EXT] is enabled)
 void add(int x) {
   txt.pb(x);
   last = ext(last);
   if (!to[last][x]) {
     len.pb(len[last]+2);
     link.pb(to[ext(link[last])][x]);
     to[last][x] = sz(to);
     to.emplace_back();
     diff.pb(len.back() - len[link.back()]);
     slink.pb(diff.back() == diff[link.back()]
       ? slink[link.back()] : link.back());
      series.pb(0);
     // [/EXT]
   } // Oadb
   last = to[last][x];
   ans.pb(INT_MAX);
   for (int i=last; len[i] > 0; i=slink[i]) {
     series[i] = ans[sz(ans) - len[slink[i]]
                    - diff[i] - 1];
     if (diff[i] == diff[link[i]])
       series[i] = min(series[i],
                       series[link[i]]);
```

} // 40be

```
// If you want only even palindromes
     // set ans only for sz(txt) %2 == 0
     ans.back() = min(ans.back(), series[i]+1);
   } // ab3b
   // [/EXT]
 } // 909a
}; // b3a7
text/suffix array linear.h 1341
#include "../util/radix sort.h"
// KS algorithm for suffix array; time: O(n)
// Input values are assumed to be in [1;k]
Vi sufArray(Vi str, int k) {
 int n = sz(str);
 Vi suf(n):
  str.resize(n+15);
  if (n < 15) {
   iota(all(suf), 0);
   rep(j, 0, n) countSort(suf,
     [&](int i) { return str[i+n-j-1]; }, k);
   return suf:
  } // 5fcf
  // Compute triples codes
  Vi tmp, code(n+2);
  rep(i, 0, n) if (i % 3) tmp.pb(i);
  rep(j, 0, 3) countSort(tmp,
   [&](int i) { return str[i-j+2]; }, k);
  int mc = 0, j = -1;
  each(i, tmp) {
   code[i] = mc += (j == -1)
       str[i] != str[j] ||
       str[i+1] != str[j+1] ||
       str[i+2] != str[j+2]);
    j = i;
  } // bfdc
  // Compute suffix array of 2/3
  tmp.clear():
  for (int i=1; i < n; i += 3) tmp.pb(code[i]);</pre>
  tmp.pb(0);
  for (int i=2; i < n; i += 3) tmp.pb(code[i]);</pre>
  tmp = sufArray(move(tmp), mc);
  // Compute partial suffix arrays
  Vi third;
  int th = (n+4) / 3;
  if (n%3 == 1) third.pb(n-1);
  rep(i, 1, sz(tmp)) {
   int e = tmp[i];
   tmp[i-1] = (e 
   code[tmp[i-1]] = i;
   if (e < th) third.pb(e \times 3);
  } // f9f1
  tmp.pop_back();
  countSort (third,
    [&] (int i) { return str[i]; }, k);
  // Merge suffix arrays
```

```
merge(all(third), all(tmp), suf.begin(),
    [&] (int 1, int r) {
      while (1%3 == 0 | 1 | r%3 == 0) {
        if (str[1] != str[r])
          return str[1] < str[r];</pre>
       1++: r++:
     } // 2f8a
     return code[1] < code[r];</pre>
   }); // 4cb3
 return suf:
} // 9165
// KS algorithm for suffix array; time: O(n)
Vi sufArray(const string& str) {
return sufArray(Vi(all(str)), 255);
} // 593f
text/suffix automaton.h
                                        d00d
constexpr char AMIN = 'a': // Smallest letter
constexpr int ALPHA = 26; // Set alphabet size
// Suffix automaton - minimal DFA that
// recognizes all suffixes of given string
// (and encodes all substrings);
// space: O(n*ALPHA); time: O(n)
// Paths from root are equivalent to substrings
// Extensions:
// - [OCC] - count occurences of substrings
// - [PATHS] - count paths from node
struct SufDFA {
 // State v represents endpos-equivalence
 // class that contains words of all lengths
 // between link[len[v]]+1 and len[v].
  // len[v] = longest word of equivalence class
 // link[v] = link to state of longest suffix
              in other equivalence class
  // to[v][c] = automaton edge c from v
 Vi len{0}, link{-1};
  vector<array<int, ALPHA>> to{ {} };
 int last{0}; // Current node (whole word)
 vector<Vi> inSufs; // [OCC] Suffix-link tree
 Vi cnt{O};
                   // [OCC] Occurence count
 vector<11> paths; // [PATHS] Out-path count
 SufDFA() {}
  // Build suffix automaton for given string
  // and compute extended stuff; time: O(n)
 SufDFA (const string& s) {
   each(c, s) add(c);
   finish();
 } // ec2e
  // Append letter to the back
  void add(char c) {
   int v = last, x = c-AMIN;
   last = sz(len);
   len.pb(len[v]+1);
   link.pb(0):
   to.pb({});
    cnt.pb(1); // [OCC]
    while (v != -1 \&\& !to[v][x]) {
     to[v][x] = last;
```

```
v = link[v];
  } // 4cfc
  if (v != -1) {
    int q = to[v][x]:
    if (len[v]+1 == len[q]) {
      link[last] = q;
    } else {
      len.pb(len[v]+1);
      link.pb(link[q]);
      to.pb(to[q]);
      cnt.pb(0); // [OCC]
      link[last] = link[q] = sz(len)-1;
      while (v != -1 \&\& to[v][x] == q) {
        to[v][x] = link[q];
       v = link[v];
      } // 784f
    } // 90aa
 } // af69
} // 345a
// Compute some additional stuff (offline)
void finish() {
  inSufs.resize(sz(len));
  rep(i, 1, sz(link)) inSufs[link[i]].pb(i);
  dfsSufs(0);
  // [/occ]
  // [PATHS]
  paths.assign(sz(len), 0);
  dfs(0);
  // [/PATHS]
} // 3f75
// Only for [OCC]
void dfsSufs(int v) {
  each(e, inSufs[v]) {
    dfsSufs(e);
    cnt[v] += cnt[e];
  } // 2469
} // 0c60
// Only for [PATHS]
void dfs(int v) {
  if (paths[v]) return;
  paths[v] = 1;
  each(e, to[v]) if (e) {
    dfs(e);
    paths[v] += paths[e];
  } // 22b3
} // d004
// Go using edge `c` from state `i`.
// Returns 0 if edge doesn't exist.
int next(int i, char c) {
  return to[i][c-AMIN];
} // c363
// Get lexicographically k-th substring
// of represented string; time: O(|substr|)
// Empty string has index 0.
// Requires [PATHS] extension.
string lex(ll k) {
  string s:
  int v = 0;
```

```
while (k--) rep(i, 0, ALPHA) {
      int e = to[v][i];
      if (e) {
       if (k < paths[e]) {</pre>
         s.pb(char(AMIN+i));
         v = e;
         break;
       } // f307
       k -= paths[e];
     1 // 29be
    } // 4600
    return s;
 } // e4af
1: // 7135
text/suffix tree.h
                                        d261
// Ukkonen's algorithm for online suffix tree
// construction; space: O(n*ALPHA); time: O(n)
// Real tree nodes are called dedicated nodes.
// "Nodes" lying on compressed edges are called
// implicit nodes and are represented
// as pairs (lower node, label index).
// Labels are represented as intervals [L:R)
// which refer to substrings [L;R) of txt.
// Leaves have labels of form [L:infinity].
// use getR to get current right endpoint.
// Suffix links are valid only for internal
// nodes (non-leaves).
struct SufTree {
 Vi txt; // Text for which tree is built
 // to[v][c] = edge with label starting with c
               from node v
 vector<array<int, ALPHA>> to{ {} };
 Vi L{0}, R{0}; // Parent edge label endpoints
 Vi par{0};  // Parent link
 Vi link{0}; // Suffix link
 Pii cur{0, 0}; // Current state
  // Get current right end of node label
 int getR(int i) { return min(R[i],sz(txt)); }
 // Follow edge `e` of implicit node `s`.
 // Returns (-1, -1) if there is no edge.
 Pii next (Pii s, int e) {
   if (s.v < getR(s.x))
     return txt[s.y] == e ? mp(s.x, s.y+1)
                          : mp(-1, -1);
    e = to[s.x][e];
    return e ? mp(e, L[e]+1) : mp(-1, -1);
 ) // f430
  // Create dedicated node for implicit node
  // and all its suffixes
 int split(Pii s) {
   if (s.y == R[s.x]) return s.x;
    int t = sz(to); to.pb({});
    to[t][txt[s.y]] = s.x;
    L.pb(L[s.x]);
    R.pb(L[s.x] = s.y);
    par.pb(par[s.x]);
    par[s.x] = to[par[t]][txt[L[t]]] = t;
    link.pb(-1);
```

int v = link[par[t]], l = L[t] + !par[t];

while (1 < R[t]) {

```
v = to[v][txt[1]];
     1 += getR(v) - L[v];
   1 // 0393
   v = split(\{v, getR(v)-l+R[t]\});
   link[t] = v;
   return t;
  } // 10bb
  // Append letter from [0; ALPHA] to the back
  void add(int x) { // amoritzed time: 0(1)
   Pii t; txt.pb(x);
    while ((t = next(cur, x)).x == -1) {
     int m = split(cur);
     to[m][x] = sz(to);
     to.pb({});
     par.pb(m);
     L.pb(sz(txt)-1);
     R.pb(INT_MAX);
     link.pb(-1);
     cur = {link[m], getR(link[m])};
     if (!m) return;
   } // 60c2
   cur = t;
 } // 6f4e
}; // dbfb
```

text/z_function.h

0466

4554

```
// Computes Z function array; time: O(n)

// zf[i] = max common prefix of str and str[i:]

template<class T> Vi prefPref(const T& str) {
  int n = sz(str), b = 0, e = 1;
  Vi zf(n);
  rep(i, 1, n) {
   if (i < e) zf[i] = min(zf[i-b], e-i);
   while (i+zf[i] < n &&
      str[zf[i]] == str[i+zf[i]]) zf[i]++;
   if (i+zf[i] > e) b = i, e = i+zf[i];
  } // e906
  zf[0] = n;
  return zf;
} // b88d
```

trees/centroid_decomp.h

// size[v] = size of centroid subtree of v
// subtree[v] = list of vertices
// in centroid subtree of v
// dists[v] = distances from v to vertices
// in its centroid subtree
// (in the order of subtree[v])

// neigh[v] = neighbours of v
// in its centroid subtree
// dir[v][i] = index of centroid neighbour

that is first vertex on path from centroid v to i-th vertex #

int p = -1, s = dfs(G, v, -1);
bool ok = 1;
while (ok) {
 ok = 0;
 each(e, G[v]) {
 if (e != p && par[e] == -2 &&
 size[e] > s/2) {
 p = v; v = e; ok = 1;
 break;

break;
} // 81f3
} // 3c10
} // 8770

par[v] = -1;
size[v] = s;
depth[v] = d;

of centroid subtree

: child(sz(G)), ind(sz(G)), dists(sz(G)),

subtree(sz(G)), neigh(sz(G)),

dir(sz(G)), par(sz(G), -2),

depth(sz(G)), size(sz(G)) {

int dfs(vector<Vi>& G, int v, int p) {

size[v] += dfs(G, e, v);

void layer(vector<Vi>& G, int v,

ind[v].pb(sz(subtree[c]));

dir[c].pb(sz(neigh[c])-1);

layer(G, e, v, c, d+1);

if (v == c) neigh[c].pb(e);

int decomp(vector<Vi>& G, int v, int d) {

each (e, G[v]) if (e != p && par[e] == -2)

int p, int c, int d) {

each(e, G[v]) if (e != p && par[e] == -2) {

(-1 for centroid)

vector<Vi> child, ind, dists, subtree,

neigh, dir;

Vi par, depth, size;

CentroidTree() {}

1 // 026c

} // 2277

size[v] = 1;

return size[v];

subtree[c].pb(v);

dists[c].pb(d);

} // dc82

} // 37ee

} // 4b61

}; // 9332

int root; // Root centroid

CentroidTree (vector<Vi>€ G)

root = decomp(G, 0, 0);

layer(G, v, -1, v, 0);
each(e, G[v]) if (par[e] == -2) {
 int j = decomp(G, e, d+1);
 child[v].pb(j);
 par[j] = v;
} // 70b5
return v;

trees/heavylight_decomp.h

#include "../structures/segtree_point.h"

9f55

```
// Heavy-Light Decomposition of tree
// with subtree query support; space: O(n)
struct HLD {
 // Subtree of v = [pos[v]; pos[v] + size[v])
 // Chain with v = [chBegin[v]; chEnd[v])
 Vi par;
             // Vertex parent
 Vi size:
             // Vertex subtree size
 Vi depth; // Vertex distance to root
 Vi pos:
             // Vertex position in "HLD" order
 Vi chBegin; // Begin of chain with vertex
 Vi chEnd; // End of chain with vertex
 Vi order; // "HLD" preorder of vertices
 SegTree tree: // Verts are in HLD order
 HLD() {}
 // Initialize structure for tree G
 // and given root; time: O(n lg n)
 // MODIFIES ORDER OF EDGES IN G!
 HLD (vector<Vi>& G, int root)
     : par(sz(G)), size(sz(G)),
        depth(sz(G)), pos(sz(G)),
        chBegin(sz(G)), chEnd(sz(G)) {
   dfs(G, root, -1);
   decomp(G, root, -1, 0);
   tree = {sz(order)};
 } // 8263
 void dfs(vector<Vi>& G, int v, int p) {
   par[v] = p;
   size[v] = 1;
   depth[v] = p < 0 ? 0 : depth[p]+1;
   int& fs = G[v][0];
   if (fs == p) swap(fs, G[v].back());
   each(e, G[v]) if (e != p) {
     dfs(G, e, v);
     size[v] += size[e];
     if (size[e] > size[fs]) swap(e, fs);
   } // 9872
 } // 12fe
 void decomp(vector<Vi>& G,
             int v, int p, int chb) {
   pos[v] = sz(order);
   chBegin[v] = chb;
   chEnd[v] = pos[v]+1;
   order.pb(v);
   each(e, G[v]) if (e != p) {
     if (e == G[v][0]) {
        decomp(G, e, v, chb);
        chEnd[v] = chEnd[e];
     } else {
        decomp(G, e, v, sz(order));
     } // c84a
   } // f707
 } // eb89
 // Get root of chain containing v
 int chRoot(int v) {return order[chBegin[v]];}
  // Level Ancestor Ouerv; time: O(lg n)
```

int lag(int v, int level) {

```
while (true) {
     int k = pos[v] - depth[v] + level;
     if (k >= chBegin[v]) return order[k];
     v = par[chRoot(v)];
   1 // 8c18
 } // 675e
 // Lowest Common Ancestor; time: O(lg n)
 int lca(int a, int b) {
   while (chBegin[a] != chBegin[b]) {
     int ha = chRoot(a), hb = chRoot(b);
     if (depth[ha] > depth[hb]) a = par[ha];
     else b = par[hb];
   1 // 5620
   return depth[a] < depth[b] ? a : b;</pre>
 } // c168
 // Call func (chBegin, chEnd) on each path
 // segment; time: O(lq n * time of func)
 template<class T>
 void iterPath(int a, int b, T func) {
   while (chBegin[a] != chBegin[b]) {
      int ha = chRoot(a), hb = chRoot(b);
     if (depth[ha] > depth[hb]) {
       func(chBegin[a], pos[a]+1);
       a = par[ha];
     } else {
       func(chBegin[b], pos[b]+1);
       b = par[hb];
     } // f9a5
   } // 563c
   if (pos[a] > pos[b]) swap(a, b);
   // Remove +1 from pos[a]+1 for vertices
    // queries (with +1 -> edges).
   func(pos[a]+1, pos[b]+1);
 } // 17e5
  // Query path between a and b; O(1g^2 n)
 SegTree::T queryPath(int a, int b) {
   auto ret = SegTree::ID;
   iterPath(a, b, [&](int i, int j) {
     ret = SegTree::merge(ret,
          tree.query(i, j));
   }); // 482d
   return ret:
 } // add0
 // Query subtree of v; time: O(lg n)
 SegTree::T guerySubtree(int v) {
   return tree.query(pos[v], pos[v]+size[v]);
 } // 23db
}; // a566
trees/lca.h
                                        4a1d
// LAQ and LCA using jump pointers
// space: 0(n lq n)
struct LCA {
 vector<Vi> jumps;
 Vi level, pre, post:
 int cnt{0}, depth;
 LCA() {}
 // Initialize structure for tree G
```

```
// and root r; time: O(n lg n)
  LCA(vector<Vi>& G, int root)
      : jumps(sz(G)), level(sz(G)),
       pre(sz(G)), post(sz(G)) {
    dfs(G, root, root);
    depth = int(log2(sz(G))) + 2;
    rep(j, 0, depth) each(v, jumps)
     v.pb(jumps[v[j]][j]);
  } // d6ce
  void dfs(vector<Vi>& G, int v, int p) {
   level[v] = p == v ? 0 : level[p]+1;
    jumps[v].pb(p);
   pre[v] = ++cnt;
   each(e, G[v]) if (e != p) dfs(G, e, v);
   post[v] = ++cnt;
  } // e286
  // Check if a is ancestor of b; time: O(1)
  bool isAncestor(int a, int b) {
    return pre[a] <= pre[b] &&
           post[b] <= post[a];</pre>
  } // 5514
  // Lowest Common Ancestor; time: O(lq n)
  int operator()(int a, int b) {
   for (int j = depth; j--;)
     if (!isAncestor(jumps[a][j], b))
       a = jumps[a][j];
    return isAncestor(a, b) ? a : jumps[a][0];
  } // 27d8
  // Level Ancestor Query; time: O(lq n)
  int lag(int a, int lvl) {
   for (int j = depth; j--;)
     if (lvl <= level[jumps[a][j]])</pre>
       a = jumps[a][j];
   return a;
  } // 75b3
  // Get distance from a to b; time: O(lg n)
  int distance(int a, int b) {
    return level[a] + level[b] -
           level[operator()(a, b)]*2;
 } // 07e0
}; // 8076
trees/link cut tree.h
                                         6bd6
constexpr int INF = 1e9;
// Link/cut tree; space: O(n)
// Represents forest of (un)rooted trees.
struct LinkCutTree {
  vector<array<int, 2>> child;
  Vi par, prev, flip, size;
  // Initialize structure for n vertices; O(n)
  // At first there's no edges.
  LinkCutTree(int n = 0)
     : child(n, \{-1, -1\}), par(n, -1),
       prev(n, -1), flip(n, -1), size(n, 1) {}
  void push(int x) {
   if (x >= 0 && flip[x]) {
      flip[x] = 0;
      swap(child[x][0], child[x][1]);
```

```
each(e, child[x]) if (e>=0) flip[e] ^= 1;
 } // + any other lazy path operations
} // bae2
void update(int x) {
 if (x >= 0) {
    size[x] = 1;
    each(e, child[x]) if (e \geq= 0)
      size[x] += size[e];
 } // + any other path aggregates
} // 8ec0
void auxLink(int p, int i, int ch) {
  child[p][i] = ch;
  if (ch >= 0) par[ch] = p;
  update(p);
} // 0a9a
void rot(int p, int i) {
  int x = child[p][i], g = par[x] = par[p];
  if (g \ge 0) child[g][child[g][1] == p] = x;
  auxLink(p, i, child[x][!i]);
  auxLink(x, !i, p);
  swap(prev[x], prev[p]);
  update(g);
} // 4c76
void splay(int x) {
  while (par[x] >= 0) {
    int p = par[x], q = par[p];
    push(g); push(p); push(x);
    bool f = (child[p][1] == x);
    if (q >= 0) {
      if (child[g][f] == p) { // zig-zig
        rot(g, f); rot(p, f);
      } else { // zig-zag
        rot(p, f); rot(g, !f);
      } // 2ebb
    } else { // zig
      rot (p, f);
    } // f8a2
  } // 446b
  push(x);
1 // 55a7
// After this operation x becomes the end
// of preferred path starting in root;
void access(int x) { // amortized O(lq n)
  while (true) {
    splay(x);
    int p = prev[x];
    if (p < 0) break;
    prev[x] = -1;
    splav(p);
    int r = child[p][1];
    if (r \ge 0) swap(par[r], prev[r]);
    auxLink(p, 1, x);
 1 // 2b87
} // 30be
// Make x root of its tree; amortized O(lg n)
void makeRoot(int x) {
  access(x):
  int& l = child[x][0];
```

```
if (1 >= 0) {
     swap(par[1], prev[1]);
     flip[1] ^= 1;
     update(1);
     1 = -1:
     update(x);
   } // 0064
 1 // b246
 // Find root of tree containing x
 int find(int x) { // time: amortized O(lq n)
   access(x);
   while (child[x][0] >= 0)
     push(x = child[x][0]);
   splay(x);
   return x:
 } // d78d
 // Add edge x-y; time: amortized O(lg n)
 // Root of tree containing y becomes
 // root of new tree.
 void link(int x, int y) {
   makeRoot(x); prev[x] = y;
 } // fb4f
 // Remove edge x-y; time: amortized O(lg n)
 // x and y become roots of new trees!
 void cut(int x, int y) {
   makeRoot(x); access(v);
   par[x] = child[y][0] = -1;
   update(y);
 } // 1908
 // Get distance between x and v,
 // returns INF if x and y there's no path.
  // This operation makes x root of the tree!
 int dist(int x, int y) { // amortized O(lg n)
   makeRoot(x);
   if (find(y) != x) return INF;
   access(v);
   int t = child[y][0];
   return t >= 0 ? size[t] : 0;
 } // ae69
); // 4480
util/arc interval cover.h
                                        7507
using dbl = double;
// Find size of smallest set of points
// such that each arc contains at least one
// of them; time: O(n lq n)
int arcCover(vector<pair<dbl, dbl>>& inters,
            dbl wrap) {
 int n = sz(inters);
 rep(i, 0, n) {
   auto& e = inters[i];
   e.x = fmod(e.x, wrap);
   e.v = fmod(e.v, wrap);
   if (e.x < 0) e.x += wrap, e.y += wrap;
   if (e.x > e.v) e.x += wrap;
   inters.pb({e.x+wrap, e.y+wrap});
 } // b87d
 Vi nxt(n);
 deque<dbl> que:
```

```
dbl r = wrap*4;
  sort(all(inters));
  for (int i = n*2-1; i--;) {
    r = min(r, inters[i].v);
    que.push_front(inters[i].x);
    while (!que.empty() && que.back() > r)
     que.pop back();
    if (i < n) nxt[i] = i+sz(que);</pre>
 } // 5e6c
 int a = 0, b = 0;
 do {
    a = nxt[a] % n;
   b = nxt[nxt[b]%n] % n;
 } while (a != b);
 int ans = 0;
 while (b < a+n) {
   b += nxt[b%n] - b%n;
   ans++:
 } // 7350
 return ans;
1 // 7871
util/bit hacks.h
                                        599a
// __builtin_popcount - count number of 1 bits
// __builtin_clz - count most significant 0s
// __builtin_ctz - count least significant Os
// __builtin_ffs - like ctz, but indexed from 1
                  returns 0 for 0
// For 11 version add 11 to name
using ull = uint64_t;
#define T64(s.up)
 for (ull i=0; i<64; i+=s*2)
   for (ull j = i; j < i+s; j++) {
     ull \ a = (M[j] >> s) \& up;
     ull \ b = (M[j+s] \& up) << s;
     M[j] = (M[j] \& up) | b;
     M[j+s] = (M[j+s] & (up << s)) | a; 
    } // a290
// Transpose 64x64 bit matrix
void transpose64(array<ull, 64>& M) {
 T64(2, 0x3333333333333333);
 T64(4, 0xF0F0F0F0F0F0F0F);
 T64(8, 0xFF00FF00FF00FF);
 T64 (16, 0xFFFF0000FFFF);
 T64 (32, OxFFFFFFFLL);
} // 6889
// Lexicographically next mask with same
// amount of ones.
int nextSubset(int v) {
 int t = v | (v - 1);
 return (t + 1) | (((~t & -~t) - 1) >>
      (__builtin_ctz(v) + 1));
} // 4c0c
                                        09f9
util/bump alloc.h
// Allocator, which doesn't free memory.
```

```
char mem[400<<20]; // Set memory limit</pre>
size t nMem;
void* operator new(size t n) {
 nMem += n; return &mem[nMem-n];
} // fba6
void operator delete(void*) {}
util/compress vec.h
                                        bc5d
// Compress integers to range [0;n) while
// preserving their order; time: O(n lg n)
// Returns mapping: compressed -> original
Vi compressVec(vector<int*>& vec) {
  sort (all (vec),
    [](int* l, int* r) { return *l < *r; });
  Vi old;
  each (e, vec) {
   if (old.empty() || old.back() != *e)
     old.pb(\stare);
    \star e = sz(old)-1;
  } // 7eb0
  return old:
} // 2b60
util/inversion vector.h
                                        0.1 + 9
// Get inversion vector for sequence of
// numbers in [0;n); ret[i] = count of numbers
// smaller than perm[i] to the left; O(n lg n)
Vi encodeInversions (Vi perm) {
 Vi odd, ret(sz(perm));
  int cont = 1;
  while (cont) {
   odd.assign(sz(perm)+1, 0);
    cont = 0:
    rep(i, 0, sz(perm)) {
     if (perm[i] % 2) odd[perm[i]]++;
      else ret[i] += odd[perm[i]+1];
     cont += perm[i] /= 2;
   } // 4ed0
  } // a4f0
  return ret;
} // c2e1
// Count inversions in sequence of numbers
// in [0;n); time: O(n lg n)
11 countInversions(Vi perm) {
 ll ret = 0, cont = 1;
 Vi odd;
  while (cont) {
    odd.assign(sz(perm)+1, 0);
    cont = 0;
    rep(i, 0, sz(perm)) {
     if (perm[i] % 2) odd[perm[i]]++;
      else ret += odd[perm[i]+1];
     cont += perm[i] /= 2;
   } // 916f
  } // c9b5
  return ret:
} // laaf
util/longest inc subseq.h
                                         0bd1 | } // 0fb9
```

```
// Longest Increasing Subsequence; O(n lg n)
int lis(const Vi& seq) {
 Vi dp(sz(seg), INT_MAX);
 each(c, seq) *lower_bound(all(dp), c) = c;
 return int(lower_bound(all(dp), INT_MAX)
            - dp.begin());
} // d0e9
util/max rects.h
                                         2a16
struct MaxRect {
 // begin = first column of rectangle
 // end = first column after rectangle
 // hei = height of rectangle
 // touch = columns of height hei inside
 int begin, end, hei;
 Vi touch; // sorted increasing
}; // 41fe
// Given consecutive column heights find
// all inclusion-wise maximal rectangles
// contained in "drawing" of columns; time O(n)
vector<MaxRect> getMaxRects(Vi hei) {
 hei.insert(hei.begin(), -1);
 hei.pb(-1);
 Vi reach(sz(hei), sz(hei)-1);
 vector < MaxRect > ans;
 for (int i = sz(hei)-1; --i;) {
   int j = i+1, k = i;
   while (hei[j] > hei[i]) j = reach[j];
   reach[i] = j;
   while (hei[k] > hei[i-1]) {
     ans.pb({ i-1, 0, hei[k], {} });
     auto& rect = ans.back();
     while (hei[k] == rect.hei) {
       rect.touch.pb(k-1);
       k = reach[k];
     } // 6e7e
     rect.end = k-1;
   } // e03f
 } // 2796
 return ans;
} // 0e49
util/mo.h
                                         caeb
// Modified MO's queries sorting algorithm,
// slightly better results than standard.
// Allows to process q queries in O(n*sqrt(q))
struct Query {
 int begin, end;
}; // b76d
// Get point index on Hilbert curve
11 hilbert(int x, int y, int s, ll c = 0) {
 if (s <= 1) return c;</pre>
 s /= 2; c \star = 4;
 if (v < s)
   return hilbert (x \in (s-1), y, s, c+(x>=s)+1);
   return hilbert (2*s-y-1, s-x-1, s, c);
 return hilbert (v-s, x-s, s, c+3);
```

```
// Get good order of gueries; time: O(n lg n)
Vi moOrder(vector<Query>& queries, int maxN) {
 int s = 1;
 while (s < maxN) s \star= 2;
 vector<11> ord;
 each (q, queries)
   ord.pb(hilbert(q.begin, q.end, s));
 Vi ret(sz(ord));
 iota(all(ret), 0);
 sort(all(ret), [&](int 1, int r) {
   return ord[1] < ord[r];</pre>
 }); // 9aea
 return ret:
} // ecec
util/parallel binsearch.h
// Run `count` binary searches on [begin; end),
// `cmp` arguments:
// 1) vector<Pii>& - pairs (value, index)
     which are queries if value of index is
     greater or equal to value,
     sorted by value
// 2) vector<bool>& - true at index i means
     value of i-th query is >= queried value
// Returns vector of found values.
// Time: O((n+c) lg n), where c is cmp time.
template<class T>
Vi multiBS(int begin, int end, int count, T cmp) {
 vector<Pii> ranges(count, {begin, end});
 vector<Pii> queries(count);
 vector<bool> answers(count);
 rep(i,0,count) queries[i]={(begin+end)/2,i};
  for (int k = uplg(end-begin); k > 0; k--) {
   int last = 0, j = 0;
   cmp(queries, answers);
   rep(i, 0, sz(queries)) {
     Pii &q = queries[i], &r = ranges[q.y];
     if (q.x != last) last = q.x, j = i;
      (answers[i] ? r.x : r.y) = q.x;
     q.x = (r.x+r.y) / 2;
     if (!answers[i])
        swap(queries[i], queries[j++]);
   } // dd99
 } // 7151
 Vi ret;
 each (p, ranges) ret.pb(p.x);
 return ret;
} // 3f84
util/radix sort.h
                                         6fb4
// Stable countingsort; time: O(k+sz(vec))
// See example usage in radixSort for pairs.
template<class F>
void countSort(Vi& vec, F key, int k) {
 static Vi buf, cnt;
 vec.swap(buf);
```

```
vec.resize(sz(buf));
 cnt.assign(k+1, 0);
 each (e, buf) cnt [key (e)]++;
  rep(i, 1, k+1) cnt[i] += cnt[i-1];
  for (int i = sz(vec)-1; i >= 0; i--)
    vec[--cnt[key(buf[i])]] = buf[i];
} // cc6f
// Compute order of elems, k is max key; O(n)
Vi radixSort(const vector<Pii>& elems, int k) {
 Vi order(sz(elems));
 iota(all(order), 0);
 countSort (order,
    [&] (int i) { return elems[i].y; }, k);
 countSort (order,
    [&] (int i) { return elems[i].x; }, k);
 return order:
} // e8f6
```