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```
scripts.sh
#!/bin/bash
set -e
# > Normal build
g++ -02 -Wall -Wextra -std=c++11 -o $1.e $1.cpp
# > Debug build
q++ -fsanitize=address -fsanitize=undefined -D_GLIBCXX_DEBUG \
    -O2 -Wall -Wextra -std=c++11 -o $1.e $1.cpp
              -fvisibility=hidden
# Stack limit: -Wl,-stack_size -Wl,16000000 -Wl,-no_pie
# > Compare
./build.sh $1; ./build.sh $2; ./build.sh $3
while :: do
    $3.e > cmp.in; echo -n 0
    $1.e < cmp.in > progl.out; echo -n 1
    $2.e < cmp.in > prog2.out; echo -n 2
    diff progl.out prog2.out
    echo -n Y
done
                                                                                              2
template.h
#include <bits/stdc++.h>
using namespace std;
using 11 = int64_t;
using ull = uint64 t;
using ld = long double;
using cmpl = complex<double>;
#define IT iterator
#define rep(i, b, e) for (int i = int(b); i < int(e); i++)
#define repd(i, b, e) for (int i = int(b); i >= int(e); i --)
#define each(a, x) for (auto& a : x)
#define all(x)
                   (x).begin(), (x).end()
#define sz(x)
                    int((x).size())
#define gcd
#define popcount
                     __builtin_popcount
// unique_ptr without deallocation
template<typename T>
struct single_ptr {
   T* elem{0};
    single_ptr()
                                             {}
    single ptr(nullptr t)
                                             {}
    single ptr(T* v)
                              : elem(v)
                                             { }
    single_ptr(single_ptr&& r) : elem(r.elem) { r.elem = 0; }
    single_ptr& operator=(nullptr_t)
                                       { elem = 0; return *this; }
    single_ptr& operator=(single_ptr&& r) { elem = r.elem; r.elem = 0; return *this; }
    T* operator->() { return elem; }
    T& operator*() { return *elem; }
    operator bool() { return elem; }
};
math/fft.h
vector<cmpl> bases;
void initFft(int size) {
    bases.resize(size+1);
```

rep(i, 0, size+1) bases[i] = $exp(cmpl(0, 2*M_PI*i/size));$

```
template < bool inv>
void fft(vector<cmpl>::IT in, vector<cmpl>::IT out, int size, int step = 1) {
    if (size == 1) { *out = *in; return; }
    fft<inv>(in,
                                  size*2, step*2);
                     out,
   fft<inv>(in+step, out+size/2, size*2, step*2);
    rep(i, 0, size/2) {
        auto t = out[i], m = bases[(inv ? i : size-i)*step];
                     = t + out[i+size/2]*m;
        out[i+size/2] = t - out[i+size/2]*m;
math/mod inv.h
template<class T>
T modInv(T a, T b) {
   T u = 1, v = 0, x = 0, y = 1, m = b;
    while (a > 0) {
       T q = b / a, r = b % a;
       T m = x - u*q, n = y - v*q;
        b = a; a = r; x = u; y = v; u = m; v = n;
    return (b == 1 ? (x < 0 ? x+m : x) : 0);
                                                                                              5
math/montgomery.h
#include "mod inv.h"
constexpr 11 MG SHIFT = 32;
constexpr 11 MG MULT = 1LL << MG SHIFT;</pre>
constexpr 11 MG_MASK = MG_MULT - 1;
11 getMgInv(11 mod)
                        { return MG MULT - modInv(mod, MG MULT); }
11 mgShift(11 n, 11 mod) { return (n * MG_MULT) % mod; } // Precompute multipliers
11 redc(11 n, 11 mod, 11 mgInv) {
   11 quot = (n * mqInv) & MG_MASK;
   n = (n + quot*mod) >> MG_SHIFT;
   return (n >= mod ? n-mod : n);
// MOD < MG_MULT, gcd (MG_MULT, MOD) must be 1
// mgRedc(mgForm1 * mgForm2) = Montgomery-form product
// mgRedc(notMgForm1 * mgForm2) = normal number
                                                                                              6
structures/interval tree.h
struct IntervalTree {
   using T = int;
    static constexpr T T_IDENT = INT_MIN;
    // (+, max)
    \#define opModify(x, y) ((x)+(y))
    \#define opQuery(x, y) \max(x, y)
    #define opTimes(x, t) (x)
    // (max, max)
   // #define opModify(x, y) max(x, y)
   // #define opQuery(x, y) max(x, y)
   // #define opTimes(x, t) (x)
   // (+, +)
    // #define opModify(x, y) ((x)+(y))
   // #define opQuery(x, y) ((x)+(y))
    // #define opTimes(x, t) ((x)*(t))
```

```
struct Node {
        T val{0}, extra{0};
                                                                                                             void setNext(NodeP v) {
                                                                                                                 if (next) next->prev = nullptr;
    vector<Node> tree;
                                                                                                                next = move(v);
    int len;
                                                                                                                 if (next) next->prev = this;
    IntervalTree(int size) {
                                                                                                        };
        for (len = 1; len < size; len *= 2);</pre>
        tree.resize(len*2);
                                                                                                        NodeP root{nullptr};
                                                                                                        NodeP merge (NodeP 1, NodeP r) {
    T query (int vStart, int vFinish, int i, int begin, int end) {
                                                                                                            if (!1) return move(r);
        if (vFinish <= begin || end <= vStart) return T_IDENT;</pre>
                                                                                                             if (!r) return move(1);
       if (vStart <= begin && end <= vFinish) return tree[i].val;</pre>
                                                                                                             if (Cmp()(1->val, r->val)) swap(1, r);
        int mid = (begin + end) / 2;
        T tmp = opQuery(query(vStart, vFinish, i*2, begin, mid),
                                                                                                             1->setNext(r->moveChild());
                        query(vStart, vFinish, i*2+1, mid, end));
                                                                                                             r->setChild(move(1));
                                                                                                             return move(r);
        return opModify(tmp, opTimes(tree[i].extra, min(end, vFinish)-max(begin, vStart)));
                                                                                                        NodeP mergePairs (NodeP v) {
    void modify(int vStart, int vFinish, T val, int i, int begin, int end) {
                                                                                                             if (!v || !v->next) return v;
        if (vFinish <= begin || end <= vStart) return;</pre>
                                                                                                             NodeP v2 = v - moveNext(), v3 = v2 - moveNext();
                                                                                                             return merge(merge(move(v), move(v2)), mergePairs(move(v3)));
        if (vStart > begin || end > vFinish) {
            int mid = (begin + end) / 2;
            modify(vStart, vFinish, val, i*2, begin, mid);
                                                                                                        Node* push (const T& x) {
            modify(vStart, vFinish, val, i*2+1, mid, end);
                                                                                                             NodeP tmp (new Node (x));
                                                                                                             auto ret = &*tmp;
        } else {
            tree[i].extra = opModify(tree[i].extra, val);
                                                                                                             root = merge(move(root), move(tmp));
                                                                                                             return ret;
        if (i < len) tree[i].val = opModify(opQuery(tree[i\star2].val, tree[i\star2+1].val),
                                                                                                        void decrease(Node* v, T val) {
                                             opTimes(tree[i].extra, end-begin));
        else
                     tree[i].val = tree[i].extra;
                                                                                                             assert(!Cmp()(v->val, val));
                                                                                                             v->val = val;
         query (int begin, int end)
                                           { return query (begin, end, 1, 0, len); }
                                                                                                             auto prev = v->prev;
    void modify(int begin, int end, T val) { modify(begin, end, val, 1, 0, len); }
                                                                                                             if (!prev) return;
                                                                                                            NodeP uniq;
                                                                                                             if (&*v->prev->child == v) {
structures/pairing_heap.h
                                                                                                                 uniq = prev->moveChild();
                                                                                                                 prev->setChild(v->moveNext());
template < class T, class Cmp = less < T >>
                                                                                                             } else {
struct PHeap {
                                                                                                                 uniq = prev->moveNext();
    struct Node;
                                                                                                                 prev->setNext(v->moveNext());
    using NodeP = unique_ptr<Node>; // Or use single_ptr + bump allocator
    struct Node {
                                                                                                             root = merge(move(root), move(uniq));
       T val:
       NodeP child{nullptr}, next{nullptr};
       Node* prev{nullptr};
                                                                                                        bool
                                                                                                                  empty()
                                                                                                                                   { return !root; }
                                                                                                                                     return root->val; }
                                                                                                        const T& top()
       Node (T x = T()) { val = x; }
                                                                                                        void
                                                                                                                  merge(PHeap&& r) { root = merge(move(root), move(r.root)); r.root = nullptr; }
                                                                                                        void
                                                                                                                                  { root = mergePairs(root->moveChild()); }
       NodeP moveChild() {
                                                                                                     };
            if (child) child->prev = nullptr;
            return move (child):
                                                                                                     trees/centroid_decomp.h
       NodeP moveNext() {
                                                                                                     struct Vert {
            if (next) next->prev = nullptr;
                                                                                                        vector<Vert *> edges, cEdges;
            return move(next);
                                                                                                        vector<int> dists:
                                                                                                        Vert* cParent{nullptr};
                                                                                                        int cDepth{-1}, cSize{0}, cState{0};
       void setChild(NodeP v) {
                                                                                                    };
            if (child) child->prev = nullptr;
            child = move(v);
                                                                                                    void dfsSize(Vert* v, int depth) {
```

v->cDepth = depth;

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};

if (child) child->prev = this;

```
v->cSize = 1;
    v->cState = 0;
    each(e, v->edges) if (e->cState <= 1 && e->cDepth < depth) {</pre>
       dfsSize(e, depth);
       v->cSize += e->cSize;
void dfsDist(Vert* v, int dist) {
   v->dists.push_back(dist);
   v->cState = 1;
   each(e, v->edges) if (!e->cState) dfsDist(e, dist+1);
Vert* centroidDecomp(Vert* v, int depth, Vert* root = 0) {
    dfsSize(v, depth);
    int size = v->cSize;
    Vert *parent = 0, *heavy = 0;
    while (true) {
        int hSize = 0;
        each(e, v->edges) if (e != parent && e->cDepth == depth && hSize < e->cSize) {
           hSize = e->cSize;
           heavy = e;
       if (hSize <= size/2) break;</pre>
       parent = v; v = heavy;
   v->cParent = root;
    dfsDist(v, 0);
   v->cSize = size;
   v->cState = 2;
    each(e, v->edges) if (e->cDepth == depth)
       v->cEdges.push_back(centroidDecomp(e, depth+1, v));
    return v;
util/alloc.h
                                                                                               9
static char memPool[512*1024*1024];
static int memOffset;
void* operator new(size_t n) { memOffset += n; return &memPool[memOffset-n]; }
void operator delete(void*) {}
```