vreg

December 6, 2023

0.1 Background and Motivation

The purpose of autonomously adjusting reference voltage (AARV) is to mitigate rapid voltage change (RVC), without affecting the utility's control of steady-state voltage or the DER's steady-state reactive power. AARV may be used with a volt-watt function that mitigates steady-state overvoltage, but otherwise AARV does not regulate steady-state voltage.

Page 39 of IEEE 1547-2018 says: The DER shall be capable of autonomously adjusting reference voltage (VRef) with VRef being equal to the low pass filtered measured voltage. The time constant shall be adjustable at least over the range of 300 s to 5000 s. The voltage-reactive power Volt-Var curve characteristic shall be adjusted autonomously as VRef changes. The approval of the Area EPS operator shall be required for the DER to autonomously adjust the reference voltage. Implementation of the autonomous VRef adjustability and the associated time constant shall be specified by the Area EPS operator.

References:

- 2019 Conference Paper: https://doi.org/10.1109/PVSC40753.2019.8981277
- 2023 Conference Paper: https://doi.org/10.1109/PESGM52003.2023.10252317

Run the following cell to define support functions using Numpy and Matplotlib

```
[14]: import sys
      import os
      import matplotlib.pyplot as plt
      import numpy as np
      import math
      # convert center, deadband, slope, and q limits into a table of V and Q points.
      # the function returns two arrays for the V and Q points
            the arrays have sentinel elements below V1 and above V4, so they are 6_{\square}
       ⇔elements long (not 4)
            the sentinel elements clarify that constant extrapolation is used outside,
        \hookrightarrow the range [V1..V4]
      def set_characteristic (center=1.0, deadband=0.0, slope=22.0, qmax=0.44,__
        \rightarrowqmin=-0.44, qbias=0.0):
        if qbias > qmax:
          qbias = qmax
        elif qbias < qmin:</pre>
          qbias = qmin
```

```
Q1 = qmax
 Q2 = qbias
 Q3 = qbias
 Q4 = qmin
 V2 = center - 0.5 * deadband
 V3 = center + 0.5 * deadband
 V1 = V2 - (Q1 - Q2) / slope
 V4 = V3 - (Q4 - Q3) / slope
 VL = V1 - 0.01
 VH = V4 + 0.01
 vtable = np.array ([VL, V1, V2, V3, V4, VH])
 qtable = np.array ([Q1, Q1, Q2, Q3, Q4, Q4])
 return vtable, qtable
# This function plots a volt-var characteristic, and returns the VQ points.
# (Tabular display is not needed in this notebook.)
def show_characteristic (label, center, deadband, slope, qmax, qmin, qbias=0):
 vtable, qtable = set_characteristic (center, deadband, slope, qmax, qmin, u
 ⊶qbias)
  # bounds for plotting the horizontal axis
 vmin = vtable[0]-0.01
 vmax = vtable[-1]+0.01
 # evaluate the characteristic over 500 equal voltage intervals
 v = np.linspace (vmin, vmax, 501)
  # interpolating Q using the numpy library function
 q = np.interp (v, vtable, qtable)
  # create the plot
 fig, ax = plt.subplots(1, 1, figsize=(6,4), tight_layout=True)
 fig.suptitle ('{:s} volt-var characteristic'.format (label))
 ax.plot (vtable, qtable, marker='o', color='blue', label='Points and
 ⇔Sentinels')
 ax.plot (v, q, color='red', label='Interpolated')
 ax.grid ()
 ax.set_xlabel ('V [pu]')
 ax.set_ylabel ('Q [pu]')
 ax.set_xlim (vmin, vmax)
 ax.legend ()
 plt.show ()
 return vtable, qtable
\# This function calculates V and dV at the POC from the formula
# in clause 5.1.2 of IEEE 1547.2-2023
# All input and output in per-unit
```

```
def get_voltage (rpu, xpu, dP, dQ, vsrcpu):
    a1 = vsrcpu*vsrcpu + rpu*dP + xpu*dQ
    a2 = xpu*dP - rpu*dQ
    d = math.sqrt (a1*a1 + a2*a2) / vsrcpu / vsrcpu - 1.0
    vpu = vsrcpu + d
    return vpu, d

# use the current directory as default location for the "save plot" buttons
# optimize the graphic export for LaTex and PDF
plt.rcParams['savefig.directory'] = os.getcwd()
plt.rcParams['savefig.pad_inches'] = 0.05
plt.rcParams['savefig.dpi'] = 300.0
plt.rcParams['savefig.bbox'] = 'tight'
# invoke the Jupyter support for Matplotlib graphics
%matplotlib widget
```

0.2 Global Variables

Run the following cell to define and test variables for:

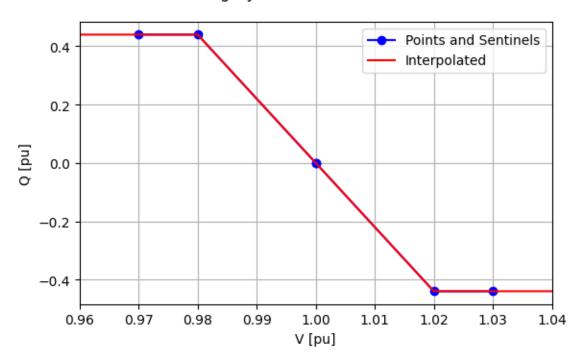
- A category B volt-var characteristic with maximum allowed slope and zero deadband.
- A 6-MW battery energy storage system (BESS) for testing the AARV response to system conditions.

```
[15]: # GLOBAL variables for the Nantucket BESS example; only the volt-var parameters
                        ⇔will change in the notebook examples
                      SBASE = 6.0e6
                      VBASE = 13200.0
                      ZBASE = VBASE*VBASE/SBASE
                      RPU = 1.210 / ZBASE # 1.744
                      XPU = 2.8339 / ZBASE # 2.6797
                      DP = 6.0e6 / SBASE
                      DQ = 0.0 / SBASE
                      VSRC = 1.0
                      vpoc, d = get_voltage (RPU, XPU, DP, DQ, VSRC)
                      print ('Nantucket BESS example for dP=\{:.3f\}, dQ=\{:.3f\}, R=\{:.3f\}, X=\{:.3f\} pu:\sqcup
                           Solution Street, Stre
                      # pseudo-code from OpenDSS
                       \#Verr = Vpu - Vreg
                       #Vreg = Vreg + Verr * IncRef
                      \#Qtarg = -K * (V - Vreg) + Qbias \# differs from OpenDSS in that it does not_{\sqcup}
                           \rightarrow iterate
                      \#Q = Qlast + (Q - Qlast) * IncOL
                      # plot the default characteristic used for AARV examples
```

```
vtable, qtable = show_characteristic ('AARV Category B', center=1, deadband=0, uselope=22, qmax=0.44, qmin=-0.44)
```

Nantucket BESS example for dP=1.000, dQ=0.000, R=0.042, X=0.098 pu: Vpoc=1.0462, dV=0.0462 pu

AARV Category B volt-var characteristic



0.3 AARV Test from 1547.1-2020

Clause 5.14.5 of IEEE 1547.1-2020 describes a test for AARV. In all other tests, AARV is to be disabled. Four AARV tests are described, at the time constant values Tref = 300s and 5000s, each of those with source voltage steps to (V1+V2)/2 and (V3+V4)/2. Before each voltage step, the steady-state reactive power, Q, should be zero at V=Vref.

The voltage steps result in step changes of Q to 0.5*Q1 and 0.5*Q4, respectively, with some delay from the open-loop response. These new Q values should follow an exponential decay back to zero, governed by Tref = 300s or 5000s. The test criteria specifies that after one time constant, Tref, the value of Q should be less than 10% of Q1 or Q4, respectively. However, the expected value of Q, following an exponential decay from the stepped value, is Q = 0.5*Q1*exp(-Tref/Tref) = 0.1839*Q1 or 0.1839*Q4. The evaluation criteria at 1*Tref should be 20% instead of 10% of Q1 or Q4. Note: at 2*Tref, the expected value of Q is 0.0677*Q1 or 0.0677*Q4.

Tref is defined as the time constant for AARV reference voltage. On the other hand, Tresponse is defined as an open-loop response time, which is converted to an exponential time constant in the code below. Furthermore, the simulation is run at a constant time step, dt, so both time constants may be implemented as constant decrement factors. If the real controller operates at a constant

sample interval, it may also use constant decrement factors to save the time of repeatedly evaluating the exponential functions.

Passing this test verifies implementation of Tref, but not the impact of AARV on a system with grid impedance.

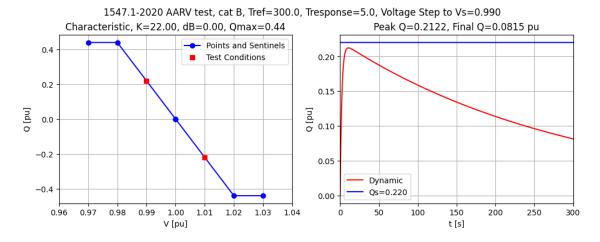
The first example simulates one AARV test, for the step to (V1+V2)/2, and category B with maximum allowed slope and no deadband. The steady-state value of Q at this voltage would be 0.22 pu, but it only reaches 0.2122 pu due to the open-loop response time constant. The value of Q at Tref is 0.0815 pu, which is 18.52% of Q1. (Due to the open-loop response, this is higher than the static expected value of 18.39% at t=Tref). The next three examples show AARV tests for category A (maximum slope), and for category B with minimum and maximum allowed *Tresponse* values.

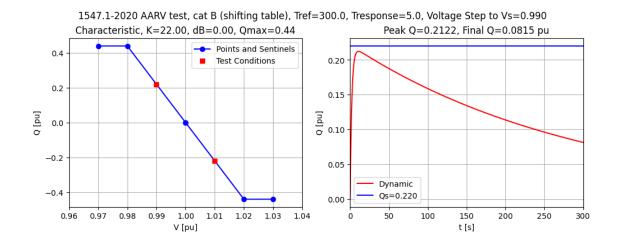
```
[23]: def show_aarv_test (tag, Vreg, dB, K, Qmax, Qmin, Tref, Tresponse, dt,_
       ⇔bShiftTable=True):
        TauOL = Tresponse / 2.3026
        IncRef = 1.0 - math.exp(-dt/Tref)
        IncOL = 1.0 - math.exp(-dt/TauOL)
        vtable, qtable = set characteristic (Vreg, dB, K, Qmax, Qmin)
        vtest = [(vtable[1]+vtable[2])/2.0, (vtable[3]+vtable[4])/2.0]
        qtest = np.interp (vtest, vtable, qtable)
        tmax = 1.0 * Tref
        t = np.linspace (0, tmax, int(tmax / dt) + 1)
        npts = len(t)
        v0 = (vtable[1]+vtable[2])/2.0
        q0 = np.interp(v0, vtable, qtable)
        q = np.zeros(npts)
        vset = 1.0
        vref = 1.0
        qpeak = 0.0
        #print ('
                               Vpu
                                       Vreq
                                                 Verr
                                                         Otara
        if bShiftTable: # this approach resets the V1..V4 points each time Vrefu
       ⇔changes
          for i in range(1, npts):
            verr = v0 - vref
            vref = vref + verr * IncRef
            vtable, qtable = set_characteristic (center=vref, deadband=dB, slope=K,_u

¬qmax=Qmax, qmin=Qmin)
            qtarg = np.interp (v0, vtable, qtable)
            q[i] = q[i-1] + (qtarg - q[i-1]) * IncOL
            if abs(q[i]) > qpeak:
              qpeak = abs(q[i])
        else: # this approach modifies the voltage entry point
          for i in range(1, npts):
            verr = v0 - vref
```

```
vref = vref + verr * IncRef
              qtarg = np.interp (v0 + (vset - vref), vtable, qtable)
              q[i] = q[i-1] + (qtarg - q[i-1]) * IncOL
              if abs(q[i]) > qpeak:
                   qpeak = abs(q[i])
         #print ('{:8.3f} {:8.5f} {:8.5f} {:8.5f} {:8.5f}'.format (t[i], v0,
  \neg vref, verr, qtarg, q[i])
# print ('\{:d\} test points, IncRef=\{:.6f\}, IncOL=\{:.6f\}, Qpeak=\{:.3f\}, Qend=\{:.6f\}, IncOL=\{:.6f\}, Qend=\{:.6f\}, Qend=\{:.6
  \hookrightarrow 3f}'.format (npts, IncRef, IncOL, qpeak, q[-1]))
    fig, ax = plt.subplots(1, 2, sharex = 'col', figsize=(10,4),
   fig.suptitle ('1547.1-2020 AARV test, {:s}, Tref={:.1f}, Tresponse={:.1f},
   →Voltage Step to Vs={:.3f}'.format (tag, Tref, Tresponse, v0))
    ax[0].set_title ('Characteristic, K={:.2f}, dB={:.2f}, Qmax={:.2f}'.formatu
   \hookrightarrow (K, dB, Qmax))
    # remove any shift of vtable, qtable that might have been done while,
   \hookrightarrow simulating the test
    vtable, qtable = set_characteristic (Vreg, dB, K, Qmax, Qmin)
    ax[0].plot (vtable, qtable, marker='o', color='blue', label='Points and
   ⇔Sentinels')
    ax[0].plot (vtest, qtest, color='red', marker='s', linestyle='None',
   ⇔label='Test Conditions')
    ax[0].set xlabel ('V [pu]')
    ax[0].set xlim (vtable[0]-0.01, vtable[-1]+0.01)
    ax[0].legend()
    ax[1].set_title ('Peak Q={:.4f}, Final Q={:.4f} pu'.format (qpeak, q[-1]))
    ax[1].plot (t, q, color='red', label='Dynamic')
    ax[1].plot (t, q0*np.ones(npts), color='blue', label='Qs={:.3f}'.format(q0))
    ax[1].set_xlabel ('t [s]')
    ax[1].set_xlim(t[0], t[-1])
    for i in range(2):
         ax[1].legend()
         ax[i].grid()
         ax[i].set_ylabel ('Q [pu]')
    plt.show()
show_aarv_test ('cat B', Vreg=1, dB=0, K=22, Qmax=0.44, Qmin=-0.44, Tref=300, U
   →Tresponse=5, dt=0.1) # for most aggressive category B
```

```
show_aarv_test ('cat B (shifting table)', Vreg=1, dB=0, K=22, Qmax=0.44, U \( \to \Q\text{Qmin}=-0.44, \text{Tref}=300, \text{Tresponse}=5, \text{dt}=0.1, \text{bShiftTable}=\text{True}) \( # for most_U \) \( \text{aggressive category } B \) \( \text{show_aarv_test ('cat A', Vreg=1, dB=0, K=12.5, Qmax=0.25, Qmin=-0.25, Tref=300, U \) \( \text{Tresponse}=10, \text{dt}=0.1) \( # for most aggressive category A \) \( \text{show_aarv_test ('cat B fast', Vreg=1, dB=0, K=22, Qmax=0.44, Qmin=-0.44, U \) \( \text{Tref}=300, \text{Tresponse} = 1, \text{dt}=0.1) \( # category B with lowest Tresponse \) \( \text{show_aarv_test ('cat B slow', Vreg=1, dB=0, K=22, Qmax=0.44, Qmin=-0.44, U \) \( \text{Tref}=300, \text{Tresponse} = 90, \text{dt}=0.1) \( # category B with highest Tresponse \)
```





1547.1-2020 AARV test, cat A, Tref=300.0, Tresponse=10.0, Voltage Step to Vs=0.990 Characteristic, K=12.50, dB=0.00, Qmax=0.25 Peak Q=0.1174, Final Q=0.0467 pu --- Points and Sentinels 0.12 Test Conditions 0.2 0.10 0.1 0.08 o.06 0.0 0.04 -0.10.02 -0.2 Dynamic Qs=0.125 0.00

t [s]

0.96

0.97

0.98

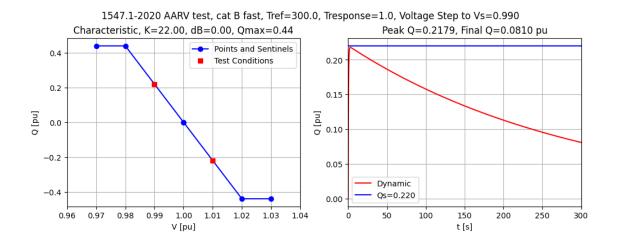
1.00

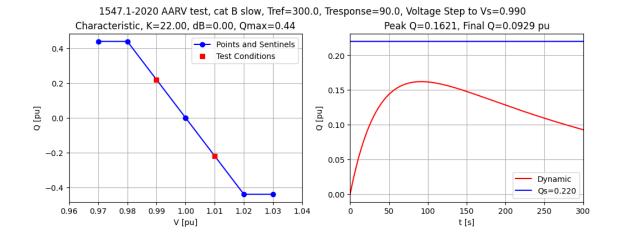
V [pu]

1.01

1.02

1.03

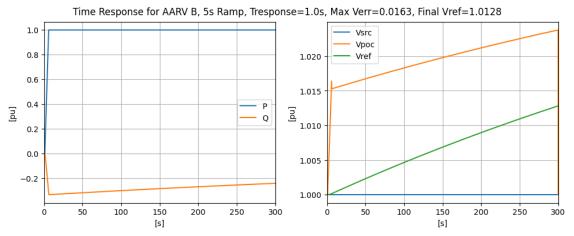


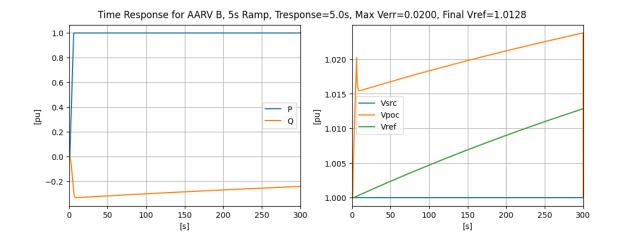


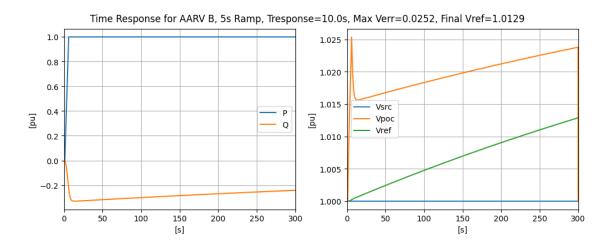
0.4 AARV Response to Storage Power-On Ramping

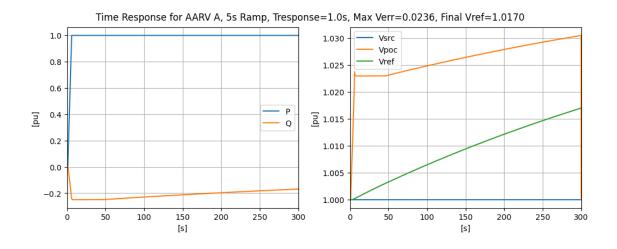
```
[24]: def show_bess_test (tag, Vreg, dB, K, Qmax, Qmin, Tref, Tresponse, dt=0.1,
       →numTrefs=1, RampTime=5, bShiftTable=False):
        TauOL = Tresponse / 2.3026
        if Tref > 0.0:
          IncRef = 1.0 - math.exp(-dt/Tref)
          tmax = numTrefs * Tref
        else:
          IncRef = 0.0
          tmax = 300.0
        IncOL = 1.0 - math.exp(-dt/TauOL)
        vtable, qtable = set_characteristic (Vreg, dB, K, Qmax, Qmin)
        t = np.linspace (0, tmax, int(tmax / dt) + 1)
        npts = len(t)
        vsrc = np.ones(npts)
        vpoc = np.ones(npts)
        pstart = 1.0
        pend = pstart + RampTime
        p = np.interp(t, [0.0, pstart, pend, t[-1]], [0.0, 0.0, DP, DP])
        q = np.zeros(npts)
        vref = np.ones(npts)
        verr = np.zeros(npts)
        # this approach resets the V1..V4 points each time Vref changes
        for i in range(npts-1):
          vpoc[i], d = get_voltage (RPU, XPU, p[i], q[i], vsrc[i])
          verr[i] = vpoc[i] - vref[i]
          vref[i+1] = vref[i] + verr[i] * IncRef
          if bShiftTable: # this approach resets the V1..V4 points each time Vrefu
       \hookrightarrow changes
            vtable, qtable = set_characteristic (vref[i], deadband=dB, slope=K,_u
       ⇒qmax=Qmax, qmin=Qmin)
            qtarg = np.interp (vpoc[i], vtable, qtable)
          else: # this approach modifies the voltage entry point
            qtarg = np.interp (Vreg + verr[i], vtable, qtable)
          q[i+1] = q[i] + (qtarg - q[i]) * IncOL
        fig, ax = plt.subplots(1, 2, sharex = 'col', figsize=(10,4),
       ⇔constrained_layout=True)
        fig.suptitle ('Time Response for {:s}, Max Verr={:.4f}, Final Vref={:.4f}'.
       →format (tag, np.max(verr), vref[-1]))
        ax[0].plot (t, p, label='P')
        ax[0].plot(t, q, label='Q')
        ax[1].plot (t, vsrc, label='Vsrc')
        ax[1].plot (t, vpoc, label='Vpoc')
```

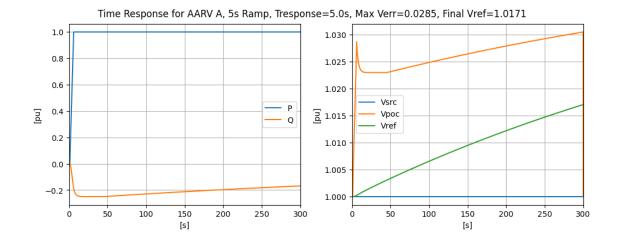
```
ax[1].plot (t, vref, label='Vref')
  #ax[1].plot (t, verr, label='Verr')
  for i in range(2):
    ax[i].set_ylabel ('[pu]')
    ax[i].set_xlabel ('[s]')
    ax[i].set_xlim (t[0], t[-1])
    ax[i].legend()
    ax[i].grid()
 plt.show()
for tr in [1.0, 5.0, 10.0]:
  tag = 'AARV B, 5s Ramp, Tresponse={:.1f}s'.format (tr)
  show_bess_test (tag, Vreg=1, dB=0, K=22, Qmax=0.44, Qmin=-0.44, Tref=300, U
 →Tresponse=tr, dt=0.1, numTrefs=1.0, RampTime=5.0)
for tr in [1.0, 5.0, 10.0]:
  tag = 'AARV A, 5s Ramp, Tresponse={:.1f}s'.format (tr)
  show_bess_test (tag, Vreg=1, dB=0, K=12.5, Qmax=0.25, Qmin=-0.25, Tref=300, __
 →Tresponse=tr, dt=0.1, numTrefs=1.0, RampTime=5.0)
#show bess test ('5s Ramp, No Volt-Var', Vreq=1, dB=0, K=22, Qmax=0, Qmin=0, U
 \neg Tref=300, Tresponse=5, dt=0.1, numTrefs=1.0, RampTime=5.0, bShiftTable=True)
#show bess test ('5s Ramp, No Volt-Var', Vreq=1, dB=0, K=22, Qmax=0, Qmin=0, | |
 ⇔Tref=300, Tresponse=5, dt=0.1, numTrefs=1.0, RampTime=5.0, bShiftTable=False)
#show_bess_test ('Q decay', Vreq=1, dB=0, K=22, Qmax=0.44, Qmin=-0.44, __
 \hookrightarrow Tref=300, Tresponse=5, dt=0.1, numTrefs=10.0, RampTime=5.0, bShiftTable=True)
#show_bess_test ('Q decay', Vreg=1, dB=0, K=22, Qmax=0.44, Qmin=-0.44, __
 \hookrightarrow Tref=300, Tresponse=5, dt=0.1, numTrefs=10.0, RampTime=5.0,
 \hookrightarrow bShiftTable=False)
```

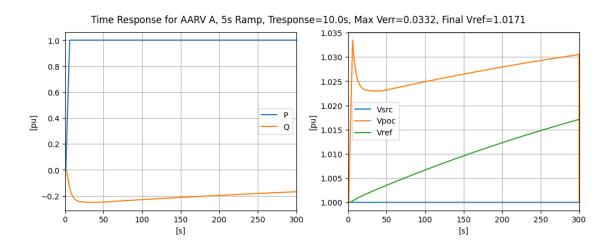










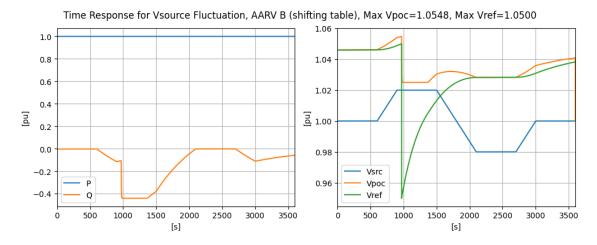


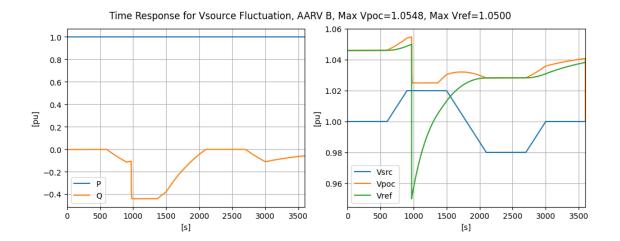
0.5 AARV Response to Grid Voltage Fluctuations

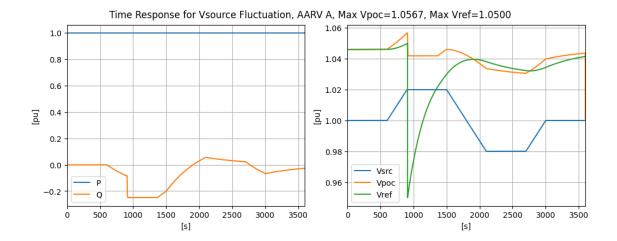
```
vsrc = np.interp (t, [0.0, 2*Tref, 3*Tref, 5*Tref, 7*Tref, 9*Tref, 10*Tref,
 \hookrightarrowt [-1]],
                       [1.0, 1.0, 1.02, 1.02, 0.98, 0.98, 1.0,
 →0])
  vpoc = np.ones(npts)
 p = DP * np.ones(npts)
 q = np.zeros(npts)
 vref = Vref * np.ones(npts)
 verr = np.zeros(npts)
  for i in range(npts-1):
    vpoc[i], d = get_voltage (RPU, XPU, p[i], q[i], vsrc[i])
    verr[i] = vpoc[i] - vref[i]
    vref[i+1] = vref[i] + verr[i] * IncRef
    if vref[i+1] > 1.05:
      vref[i+1] = 0.95
    if bShiftTable: # this approach resets the V1..V4 points each time Vrefu
 \hookrightarrow changes
      vtable, qtable = set_characteristic (vref[i], deadband=dB, slope=K,_u
 →qmax=Qmax, qmin=Qmin)
      qtarg = np.interp (vpoc[i], vtable, qtable)
    else: # this approach modifies the voltage entry point
      qtarg = np.interp (Vreg + verr[i], vtable, qtable)
    q[i+1] = q[i] + (qtarg - q[i]) * IncOL
 fig, ax = plt.subplots(1, 2, sharex = 'col', figsize=(10,4),__
 ⇔constrained_layout=True)
 fig.suptitle ('Time Response for {:s}, Max Vpoc={:.4f}, Max Vref={:.4f}'.

→format (tag, np.max(vpoc), np.max(vref)))
  ax[0].plot (t, p, label='P')
  ax[0].plot(t, q, label='Q')
  ax[1].plot (t, vsrc, label='Vsrc')
  ax[1].plot (t, vpoc, label='Vpoc')
  ax[1].plot (t, vref, label='Vref')
  #ax[1].plot (t, verr, label='Verr')
  for i in range(2):
    ax[i].set ylabel ('[pu]')
    ax[i].set_xlabel ('[s]')
    ax[i].set_xlim(t[0], t[-1])
    ax[i].legend()
    ax[i].grid()
 plt.show()
show_vsrc_test ('Vsource Fluctuation, AARV B (shifting table)', Vreg=1, dB=0, __
 →K=22, Qmax=0.44, Qmin=-0.44, Tref=300, Tresponse=5, dt=0.1, Vref=1.0459,
 ⇒bShiftTable=True)
```

show_vsrc_test ('Vsource Fluctuation, AARV B', Vreg=1, dB=0, K=22, Qmax=0.44, Gmin=-0.44, Tref=300, Tresponse=5, dt=0.1, Vref=1.0459, bShiftTable=False) show_vsrc_test ('Vsource Fluctuation, AARV A', Vreg=1, dB=0, K=12.5, Qmax=0.25, Gmin=-0.25, Tref=300, Tresponse=5, dt=0.1, Vref=1.0459)

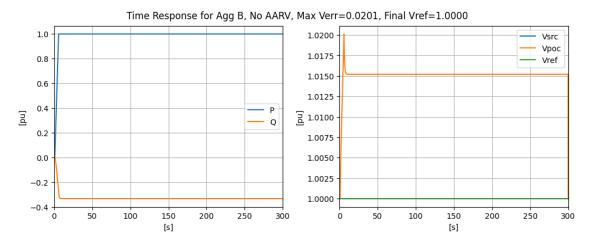


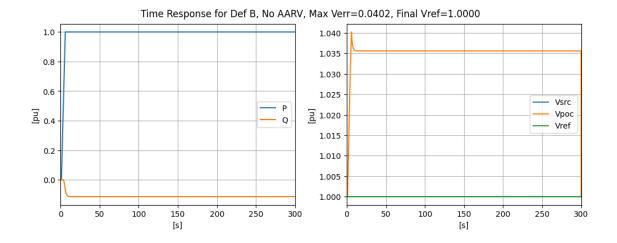


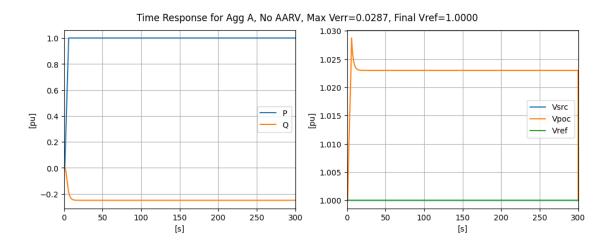


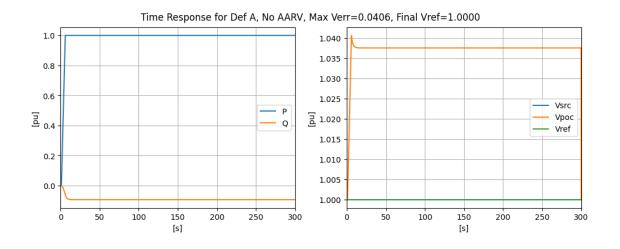
0.6 Volt-Var Response to Storage Power-On Ramping

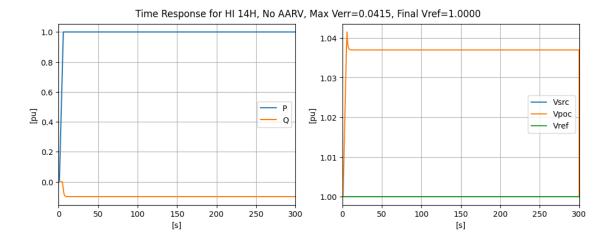
```
[26]: show_bess_test ('Agg B, No AARV', Vreg=1, dB=0, K=22, Qmax=0.44, Qmin=-0.44, Uref=0, Tresponse=5)
show_bess_test ('Def B, No AARV', Vreg=1, dB=0.04, K=22.0/3.0, Qmax=0.44, Uref=0, Tresponse=5)
show_bess_test ('Agg A, No AARV', Vreg=1, dB=0, K=12.5, Qmax=0.25, Qmin=-0.25, Uref=0, Tresponse=5)
show_bess_test ('Def A, No AARV', Vreg=1, dB=0, K=2.50, Qmax=0.25, Qmin=-0.25, Uref=0, Tresponse=5)
show_bess_test ('HI 14H, No AARV', Vreg=1, dB=0.06, K=43.0/3.0, Qmax=0.44, Uref=0, Tresponse=5)
```



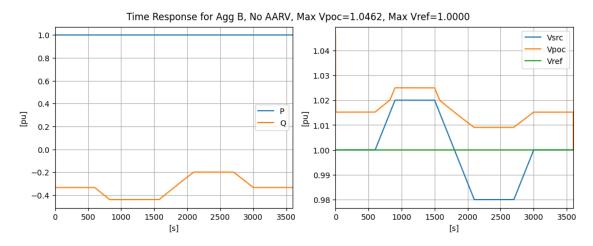


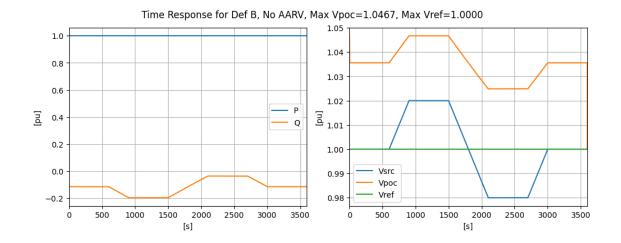


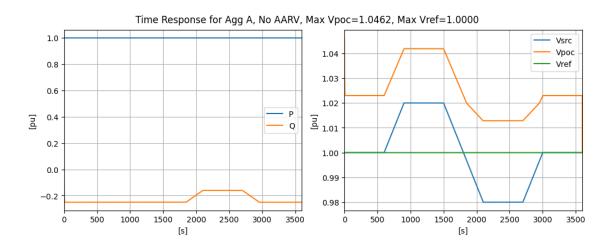


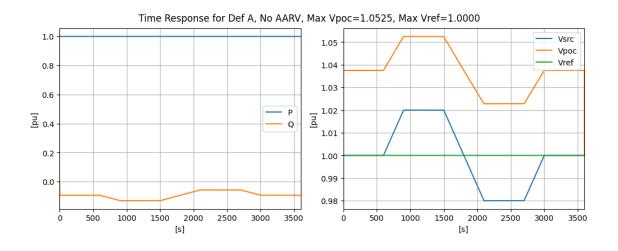


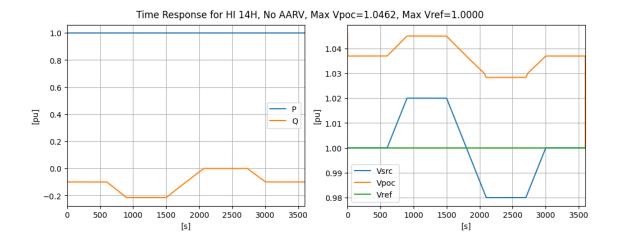
0.7 Volt-Var Response to Grid Voltage Fluctuations











[]: