$$\frac{5.)}{A \in \mathbb{Z}_{n}}$$
 is invertible  $z = 3 \gcd(n, olef(A)) = 1$ 

$$A = \begin{pmatrix} a_{11} & - & a_{1m} \\ a_{11} & - & a_{1m} \end{pmatrix} \in \mathbb{Z}_m$$

It holds 
$$A = \begin{cases} b_{11} - b_{11} \\ b_{11} - b_{11} \end{cases} = \frac{acl_{1}(A)}{det(A)}$$

$$= \sum_{j=1}^{n} \frac{1}{\operatorname{det}(A)} \stackrel{\sim}{\alpha_{j}} (\operatorname{mod} m)$$

lost equivolence: see next home noch <=> ==1

$$M = \begin{pmatrix} 7 & 1 \\ 9 & 2 \end{pmatrix} \in \mathbb{Z}_{26}^{2\times 2}$$

with a.) Mis revertible.

$$A^{-1} = \frac{1}{\det(A)} \begin{pmatrix} d - b \\ -c & a \end{pmatrix} \quad A = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$

$$\Rightarrow k = \frac{26.4 + 1}{5} = \frac{25.4 + 5}{5} = 27$$

21.17 = 21.73 +21.4 = --

$$\frac{4.1}{4.1}$$
  $\alpha_{1}$   $C = A.m. m(m_{1}, m_{2}, m_{3})$   $A = \begin{pmatrix} 1.11 \\ 1.10 \\ 10.1 \end{pmatrix} \in \mathbb{Z}_{2}$ 

$$\frac{4. b.}{E S. a.} = 3 \quad \gcd(m, def(4)) = 1$$

$$def(A) = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & 0 \end{vmatrix} = 1 \cdot \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix} + 1 \begin{vmatrix} 1 & 1 \\ 1 & 0 \end{vmatrix}$$

$$= 1 + 1 + 1 = 1 \quad (mod 2)$$

$$= 3 \quad \gcd(2, 1) = 1 = 3 \quad A \quad is \quad \text{in vertible}$$

$$= 1 + 1 + 1 = 1 \quad (mod 2)$$

$$\begin{pmatrix}
1 & 1 & 1 & 1 & 0 & 0 \\
1 & 1 & 0 & 0 & 1 & 0
\end{pmatrix}
\xrightarrow{R_2 + R_3}
\begin{pmatrix}
1 & 0 & 1 & 0 & 0 & 1 \\
0 & 1 & 0 & 0 & 1
\end{pmatrix}
\xrightarrow{R_2 + R_3}
\begin{pmatrix}
1 & 0 & 1 & 0 & 0 & 1 \\
0 & 1 & 0 & 1 & 0 & 1
\end{pmatrix}$$

E6.) a.) It of possible keys

substitution off e. Kees are given

es permitations over symbol elphabet E.

151= m

=> n! per un te Hous, i.e., u! kees

bi) effine ciphers with 26 symbols he alphobet c; = a. m; +b (mod 26)

m; = a (c; -b) (mod 26)

=> a' hos to exist for decryption before: a' exists, if gcd (a, 26) = 1

Perm.  $M_3 = M_4 \circ M_2 , m; -> m_{M_2}(M_4(i)) = m_{M_3}(i)$