
Preamble

Figures and tables in this document are often accompanied by a link to the Jupyter Notebook that generated them. These notebooks contain more information than can be conveyed in just the caption. These links look like, e.g: [2021-12-06__local_HH_dV_shape](#). To visit these links, in the digital version of this document, just click them. In the paper version, convert them to an URL as follows: https://tfiers.github.io/phd/nb/2021-12-06__local_HH_dV_shape.html.

Introduction

- Problem statement
- Opportunity of voltage imaging, core idea of inverting the causal ‘presynaptic spike \rightarrow postsynaptic PSP’ relation
- Overview of thesis



Figure 1: **The causal link between neural connectivity and activity.** On the left, a cartoon of a synaptic connection. The axon of presynaptic neuron M (in blue) impinges on postsynaptic neuron N (in brown). The electrode icons indicate that their membrane voltages are recorded (shown on the right). A succesful spike in neuron M will elicit a small but precisely-timed voltage bump in neuron N (the postsynaptic potential, PSP). There is thus a causal relationship between 1) the existence of a connection $M \rightarrow N$ and 2) both neurons' membrane voltages. This causal relationship (black arrow) is exploited to perform network inference from voltage recordings (green arrow).

Drawings adapted from Purves et al.'s "Neuroscience" textbook, 6th edition, 2018.

1.1 Connectomics

- Motivation
- Ground-truth connectomics: tracing of electron microscopy and fluorescent injection imaging
- Necessity of connection *inference*
- Mention ‘invasive’ connection testing (stimulate one cell, record possible neighbours)
- Limitations of ‘connectomics’, and of inferred vs ‘actual’ connectomics.
Terminology, e.g. ‘functional connectomics’

1.2 Voltage imaging

- Technologies (from dyes to GEVIs)
- Specs: cell yield, tissue depth, recording duration, SNR, species
- ..and growth of these over time, and comparison with calcium imaging.
To extrapolate how these might advance in the future
- Comparison with other recording techniques: ephys, calcium imaging, (and briefly mention coarser methods)

1.3 Network inference

- Working with events/spikes only, versus working with continuous signals; or a hybrid as here.
- Overview of the spikes-only methods
- The connectomics competition, and the findings about the best methods
- Mention other application domains, like gene regulatory networks
- Conclusion: connection inference by spikes is poor (Ila Fiete etc), and Vm imaging offers unique advantage (causality)

Simulation details

In this chapter, we describe our experimental setup: the neuron model we simulate, its inputs, and how we simulate voltage imaging.

2.1 The AdEx neuron

We choose to simulate the ‘AdEx’ point neuron model, or the ‘adaptive exponential integrate-and-fire’ neuron [BG05], with conductance-based synaptic currents. The AdEx neuron is a leaky-integrate-and-fire (LIF) neuron model, with two additions. First, the full upstroke of each spike is simulated, as an exponential runoff. Second, an extra dynamic variable is added: the adaptation current. This current allows the simulation of many non-linear effects of real neurons, like spike-rate adaptation and post-inhibitory rebound.

The AdEx model consists of two differential equations ((1) and (2)), and a discontinuous update after a spike is generated (3). One equation simulates the membrane voltage V , and one the adaptation current w :

$$C \frac{dV}{dt} = -g_L(V - E_L) + g_L \Delta_T \exp\left(\frac{V - V_T}{\Delta_T}\right) - I_{\text{syn}} - w \quad (1)$$

$$\tau_w \frac{dw}{dt} = a(V - E_L) - w \quad (2)$$

Parameters are described in [table 1](#).

The first term of equation (1) is the restorative force pulling the voltage back to the resting (or leak) potential E_L . The second, exponential term is what generates the spike upstrokes. It is practically zero over most of the sub-threshold regime, and only becomes large (and then very large) near the firing threshold. (This firing threshold is characterised further on).

I_{syn} is the synaptic current, explained in [section 2.4](#). We use the sign convention of inter alia Dayan & Abbott¹ where membrane currents are defined as positive when positive charges flow *out* of the cell. I.e.



Figure 2: A linear-plus-exponential model (red) fit to data from a cortical pyramidal neuron (black), from [Bad+08]

¹ [DA01], ch. 5.3, p. 162

a positive I_{syn} decreases the membrane voltage (itself defined as the electric potential inside minus outside the cell).

The adaptation current w decays exponentially to zero on its own ($-w$ in equation (2)), and is influenced by voltage deviations from equilibrium: for $a > 0$, w acts on V in the opposite direction of the deviation, and for $a < 0$, w acts in the same direction. Izhikevich calls the former a resonant current, and the latter an amplifying one.²

² [Izh07], section 5.2.4. Note the different notation used; see the translation in table 2.

Name	Description	Value
V	Membrane voltage	(in mV)
w	Adaptation current	(in pA)
C	Membrane capacitance	104 pF
g_L	Input / leak conductance	4.3 nS
E_L	Resting / leak potential	−65 mV
Δ_T	Threshold slope factor	0.8 mV
V_T	Location of minimum of $\frac{dV}{dt}$	−52 mV
τ_w	Time constant of adaptation current	88 ms
a	Sensitivity of adaptation current to V	−0.8 nS
θ	Spike definition threshold	40 mV
V_r	Reset voltage after spike	−53 mV
b	Adaptation current bump after spike	65 pA

Table 1: Quantities and parameters of the AdEx neuron, equations (1) to (3). Values are from a model fit to a cortical regular spiking (RS) neuron, from [Nau+08]. By defining the location of $\frac{dV}{dt}$'s minimum, V_T also co-determines the location of the firing threshold.

In this chapter, we will analyse $\frac{dV}{dt}$ as a function of V , i.e. analyse it as a dynamical system: will the voltage increase or decrease at the current voltage? For conciseness, we call this function $F(V)$. I.e. $F(V) = \frac{dV}{dt}$ = the right-hand-side of equation (1) here, scaled by $1/C$. We'll mostly analyse F in the absence of synaptic and adaptation currents, i.e. for I_{syn} and w both zero. Figure 2 shows the $F(V)$ curve for an AdEx neuron fit to a real neuron. Figure 5 compares the $F(V)$ curve of an AdEx neuron with that of another two-dimensional neuron model, the Izhikevich neuron.

In addition to the two differential equations, the AdEx model also consists of an instantaneous reset condition. When the membrane voltage V reaches a certain threshold θ , a spike is recorded, V is reset, and w is increased:

$$\begin{aligned} \text{if } V > \theta \text{ then: } V &\leftarrow V_r \\ w &\leftarrow w + b \end{aligned} \quad (3)$$

This bump of the adaptation current is what provides the spike rate adaptation: the more spikes the neuron has recently fired, the higher the adaptation current w and the more it drives down the voltage (equation (1)), away from the firing threshold.

For a full description of the different firing patterns that the AdEx neuron can exhibit, for different parameter values (i.e, a characterisa-

tion of its bifurcations), see [Nau+08], “Firing Patterns in the Adaptive Exponential Integrate-and-Fire Model”. For an even fuller description, including a derivation of two-dimensional neuron models from higher-dimensional, Hodgkin-Huxley-like models, see Eugene Izhikevich’s book, *Dynamical Systems in Neuroscience: The Geometry of Excitability and Bursting* [Izh07].

In terms of parameter choice, we choose to simulate a cortical regular spiking (RS) neuron, i.e. a ‘standard’ excitatory neuron that does not display e.g. bursting or fast-spiking behaviour. We take our parameter values from [Nau+08]³, where they fitted an AdEx model to recordings from real cortical RS neurons injected with different step currents. Parameter values are listed in table 1.

³ Section 6, and Table 1, row 3

Examples of the signals V and w that this model generates are given later, in figure 10 and figure 13.

Analysis

Where are the fixed points of the dynamical system $\frac{dV}{dt} = F(V)$? I.e, where is $F = 0$? Like other neuron models, there are two fixed points: a stable one at the leak potential E_L , and an unstable one at the instantaneous firing threshold (which we’ll call E_T).

We see in equation (1) (for $I_{\text{syn}} = 0$ and $w = 0$) that the leak potential E_L is indeed a fixed point – or rather lies very close to one: the exponential term is negligibly small at $V = E_L$. The second fixed point has no straightforward expression. The exact solutions for F ’s roots need the so called Lambert W or ‘product logarithm’ functions W_0 and W_{-1} (see figure 3). The roots are found at:

$$V = E_L - \Delta_T W_k \left(-\exp \left(\frac{E_L - V_T}{\Delta_T} \right) \right) \quad (4)$$

..where $k = 0$ gives the resting potential, and $k = -1$ the instantaneous firing threshold.⁴ For our cortical RS neuron, this gives us an instantaneous threshold of $E_T = -49.6$ mV.

Also of interest – especially when comparing with the Izhikevich neuron later – is the slope of AdEx’s $F(V)$, i.e. its derivative with respect to V :

$$\begin{aligned} \frac{dF}{dV} &= \frac{d}{dV} \left(-g_L(V - E_L) + g_L \Delta_T \exp \left(\frac{V - V_T}{\Delta_T} \right) \right) \\ &= -g_L + g_L \exp \left(\frac{V - V_T}{\Delta_T} \right) \end{aligned} \quad (5)$$

This derivative is zero at $V = V_T$. I.e, unlike what is suggested by the ‘ T ’ subscript, and the name ‘effective threshold potential’ given to it in the AdEx literature[BG05; Nau+08], V_T is not the instantaneous threshold potential (it is not a zero of F), but rather the minimum of F (it is the zero of $\frac{dF}{dV}$).

From equation (5), we also calculate the slope of F at its two roots. At $V = E_L$, the slope (also known as the leak or input conductance



Figure 3: The Lambert W functions for real numbers.

⁴ Here too we see that the true resting potential is almost identical to E_L : W_0 passes through zero, and its argument is ≈ 0 , because the exponential’s argument is negative. For W_{-1} however, figure 3 shows that the second term is not negligible around 0.

here) is $-g_L$, plus a negligibly small exponential term. The negative sign shows that this is a stable fixed point: in a linearization of F around this point, at voltages below the resting potential, F (i.e. $\frac{dV}{dt}$) is positive and thus V will increase. At voltages above E_L , F is negative and V will decrease. Small deviations on either side of the resting potential will thus decay back to this resting potential.

At the firing threshold $V = E_T$ (i.e. the second solution to equation (4)), the slope is:

$$g_L \left(\exp \left(\frac{E_T - V_T}{\Delta_T} \right) - 1 \right) \quad (6)$$

..which is positive (as $E_T > V_T$), indicating that this is an unstable fixed point: a small deviation of the voltage above E_T will blow up to infinity (i.e, a spike is generated).

2.2 Alternative neuron models

Why did we choose the AdEx model to simulate neuron voltages? In short, because it strikes a good balance between realism and complexity. We briefly consider here two alternative neuron models: the simple leaky-integrate-and-fire (LIF) neuron, and the more complex Hodgkin-Huxley (HH) neuron. In the next section, we go into more depth on a third alternative, the very similar Izhikevich neuron.

A simpler model than AdEx would be the well-known LIF neuron:

$$C \frac{dV}{dt} = -g_L(V - E_L) - I_{\text{syn}}$$

if $V > \theta$, then: $V \leftarrow V_r$

As is apparent from comparing this with equations (1) and (3), the AdEx model is an extension of the LIF model. The LIF neuron lacks a simulation of the upstroke of spikes (the exponential term in equation (1)), and the slower time-scale adaptation current (equation (2)), which allows the simulation of many qualitatively different real neuron types. It is especially this first addition, the full upstroke simulation, that seems relevant in generating realistic voltage traces.

Would this thesis have been very different had we used LIF neurons instead? Probably not, though it might depend on the mean voltage level of the simulated neuron: if it is well below the firing threshold, both LIF and AdEx are linear (the exponential term is negligible), and they behave quasi identically. When a spike is generated in the AdEx model, the exponential feedback makes the upstroke very fast, and thus not many timesteps in the simulation are spent on it, versus the linear regime.

On the other hand, when the neuron would continuously teeter just below its firing threshold, the LIF and AdEx models do not behave

similarly. LIF's $F(V)$ curve is still fully linear, while AdEx's is not, and AdEx will behave more like a real neuron – see [figure 2](#).

Another well-known alternative neuron model is the class of Hodgkin-Huxley (HH)-like neurons. These models simulate the full trajectory of a spike: both its upstroke and its downstroke. Unfortunately they also have many free parameters. They also take a bit longer to simulate, being higher dimensional (having more differential equations), and containing many more exponential terms, which take the brunt of the time when numerically evaluating a differential expression.



Figure 4: Neuron models as dynamical systems: a comparison of the $F(V)$ curves of the Izhikevich and AdEx neurons. ‘Experimental’ is an AdEx neuron fit to a cortical pyramidal neuron (using data from [Bad+08]). The Izhikevich neuron’s parameters were chosen to match the fixed points and the leak conductance. Arrows indicate whether the voltage will increase or decrease (1D flow field). $\rightarrow \bullet \leftarrow$ is a stable fixed point (resting potential), $\leftarrow \circ \rightarrow$ is an unstable fixed point (spike threshold). $\dot{V} \equiv \frac{dV}{dt}$.

2.3 The Izhikevich neuron

Another alternative neuron model is the Izhikevich neuron, which is exceedingly similar to the AdEx neuron. These are the Izhikevich equations, using the same symbols as used before (in equations (1) to (3)):

$$C \frac{dV}{dt} = k(V - E_L)(V - E_T) - I_{\text{syn}} - w \quad (7)$$

$$\tau_w \frac{dw}{dt} = a(V - E_L) - w \quad (8)$$

$$\text{if } V > \theta, \text{ then:} \quad (9)$$

$$V \leftarrow V_r$$

$$w \leftarrow w + \Delta w$$

We have introduced two new parameters not present in the AdEx equations: the steepness of the parabola, k ; and E_T , the instantaneous firing threshold (the firing threshold in the absence of any synaptic or adaptation currents).

The only difference with AdEx is in equation (7), where the $F(V)$ curve is not made by a linear plus exponential term, as in AdEx; but rather by a quadratic (a parabola). Its two zeros (the fixed points) are readily apparent, as E_L and E_T .

Correspondences with AdEx

In Izhikevich’s book⁵, different names are used for the same quanti-

⁵ [Izh07], section 5.2.4, equations 5.7 & 5.8

ties:

$$C \frac{dv}{dt} = k(v - v_r)(v - v_t) - u + I \quad (10)$$

$$\frac{du}{dt} = a(b(v - v_r) - u) \quad (11)$$

$$\text{if } v > v_{\text{peak}}, \text{ then:} \quad (12)$$

$$v \leftarrow c$$

$$u \leftarrow u + d$$

Table 2 compares both notation conventions.

AdEx	Izh	Description	Units
V	v	Membrane voltage	V
w	u	Adaptation current	A
τ_w	$1/a$	Time constant of adaptation current	s
E_L	v_r	Resting / leak potential	V
V_r	c	Reset voltage after spike	V
a	b	Sensitivity of adapt. current to V	S
b	d	Adaptation current bump after spike	A

Table 2: **Translating between Izhikevich and AdEx.** Different symbols used for the same quantities, in [BG05] and in most of this thesis ('AdEx'), and in [Izh07] ('Izh'). Membrane capacitance C (in farad) is the same in both notations.

Beside these straightforward correspondences, there are some parameters in either model that have no direct equivalent in the other: k and v_t in Izhikevich, and g_L , Δ_T , and V_T in AdEx. For those, we'll look at the shape of Izhikevich's $F(V)$, as we've done for the AdEx neuron before.

First, the AdEx parameter g_L . This is the input conductance, a.k.a. the leak conductance, and the slope of $F(V)$ around the leak potential. We can find this same conductance for the Izhikevich neuron by taking the derivative with respect to v of the right hand side of equation (10), at $w = 0$, $I_{\text{syn}} = 0$, and $v = v_r$. We find:

$$\left. \frac{d}{dv} (k(v - v_r)(v - v_t)) \right|_{v=v_r} = k(v_r - v_t) \quad (13)$$

(this value is negative: the leak potential is a stable fixed point. This corresponds to equation (1), where we find ' $-g_L$ '). Thus, our first nontrivial correspondence:

$$g_L = k(v_t - v_r) \quad (14)$$

We've seen that V_T is the minimum of AdEx's F . The minimum of Izhikevich's F is easily found as the average of the parabola's two zeros. I.e, V_T corresponds to $(v_r + v_t)/2$.

Finally, Δ_T co-determines the slope of AdEx's F at the firing threshold (equation (6)). Given that Izhikevich's F is a parabola, with

slopes equal in magnitude at both roots, we already know the firing threshold slope: it is the same as the leak conductance, equation (14). Here, the AdEx model is more expressive than Izhikevich's: the slope of $\frac{dV}{dt}$ at the firing threshold can be independently tweaked from the leak conductance; in Izhikevich these two are clung together by the form of the quadratic equation.

Comparison with AdEx

The Izhikevich and AdEx models are very similar. Their phase spaces are topologically identical: the adaptive current equation is identical (up to a renaming of the variables); and the $F(V)$ -graph has the same shape, with two fixed points: a stable fixed point at the resting potential, and an unstable one at the firing threshold (figure 4).

They differ in the exact shape: Izhikevich's $F(V)$ is a parabola, while AdEx is the more realistic 'linear subthreshold, and then transitioning to an exponential' (see figures 2 and 4). As a result, Izhikevich neurons have an unrealistically slow spike upstroke, examples of which can be seen in figure 5.

A second issue is Izhikevich's subthreshold nonlinearity. The effects of this can be seen in figure 6. Positive input currents produce stronger responses than equally large negative input currents. This is explained by the quadratic $\frac{dV}{dt}$ shape: positive deviations are attenuated less, and negative deviations more, than a linear neuron would. Real and AdEx neurons do not suffer this asymmetry.



Figure 5: **Two neuron models behave differently for (near) identical parameters and input.**

The AdEx neuron's parameters are from [Nau+08], for a cortical regular spiking neuron. The Izhikevich neuron's parameters are copied from the AdEx neuron wherever they correspond directly. The other parameters are chosen so both models have the same resting and threshold potentials, and the same leak conductance, using the correspondences found earlier in this section. Both models receive EI-balanced synaptic input from 6500 Poisson spike trains with lognormal firing rates. The AdEx neuron was given stronger inputs ($\Delta g_{\text{exc}} = 12.2$ pS) than the Izhikevich neuron ($\Delta g_{\text{exc}} = 4$ pS), so as to obtain the same number of output spikes. (In both cases, $\Delta g_{\text{inh}} = 4 \Delta g_{\text{exc}}$). For more details, see 2023-06-23__Vm_traces_AdEx_Izh__Brian.

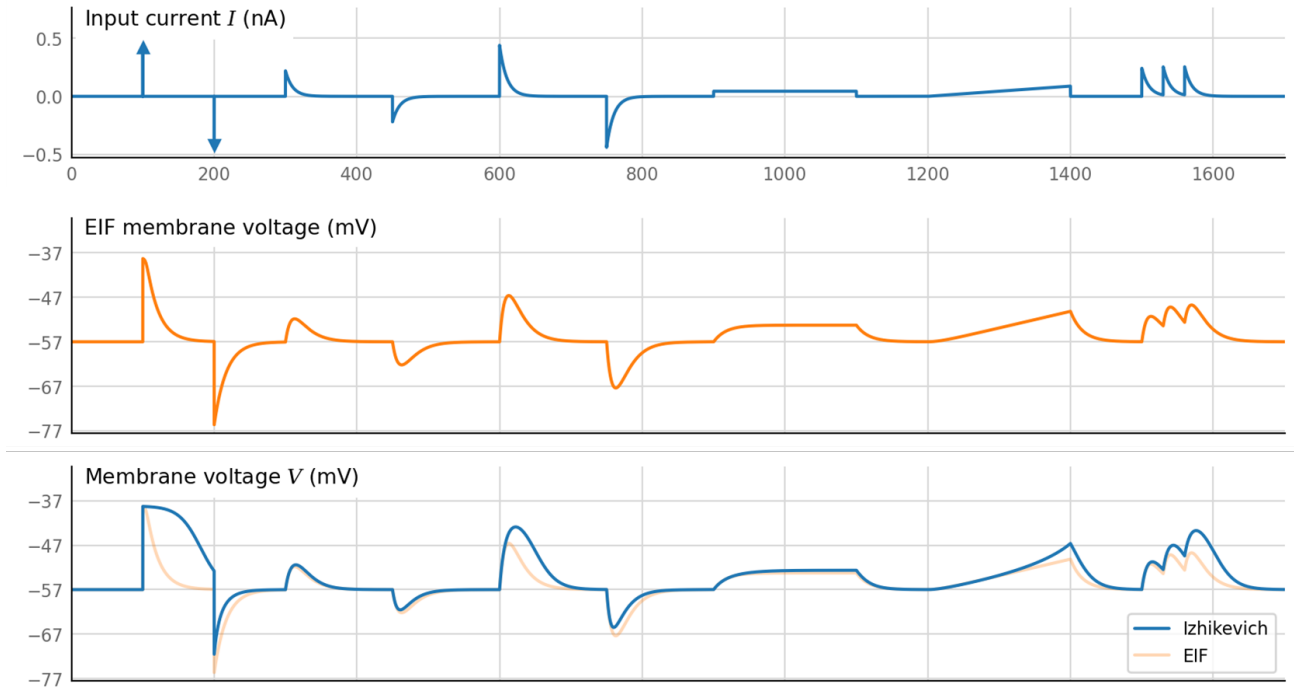


Figure 6: **The nonlinear response of Izhikevich neurons to sub-threshold input currents.**

'EIF' stands for exponential integrate-and-fire; it has the same $\frac{dV}{dt}$ as an AdEx neuron. Adaptation currents are negligibly small for both models in this test scenario.

This nonlinearity is not visible for small voltage deviations, which is what the postsynaptic potentials we are interested in in this thesis tend to be. There is however an effect of the neuron's average voltage: if this voltage is constantly on the higher side, then inputs – both negative and positive – will cause larger responses than if the median voltage was lower.

2.4 Synapse model

One as of yet unexplained term in our neuron model, equation (1), is the synaptic current I_{syn} . This is the following sum over all input synapses i of the neuron:

$$I_{\text{syn}} = \sum_i g_i (V - E_i) \quad (15)$$

where V is the global membrane voltage of the neuron, E_i is the reversal potential of that synapse, and g_i is the local synaptic conductance, which is modulated by presynaptic spikes.

For an excitatory synapse, $V < E_i$, making $g_i(V - E_i)$ negative, increasing the membrane voltage according to the sign convention for I_{syn} in equation (1).

We simulate the synaptic conductances g_i as exponentially decaying signals (with time constant τ_g), and bump them up instantaneously on arrival of a presynaptic spike:

$$\frac{dg_i}{dt} = -g_i/\tau_g \quad (16)$$

On incoming presynaptic spike:

$$g_i \leftarrow g_i + \Delta g_i \quad (17)$$

Note that these are not the so called alpha-synapses. Those are two dimensional and also have an exponential rise, instead of just an exponential decay. (For an infinitely fast rise though, these models are of course the same). Simulating a full alpha synapse might increase the realism of our voltage traces, for a small simulation cost. We did not try this however. Foremost because alpha synapses fit to real data often have very fast rise times that are almost indistinguishable from instantaneous jumps.

For efficiency, we give all our excitatory synapses the same reversal potential, E_{exc} . Idem for the inhibitory synapses, with E_{inh} . This allows us to factor the synaptic current sum (equation (15)) as follows:

$$I_{\text{syn}} = (V - E_{\text{exc}}) \sum_{\text{exc } i} g_i + (V - E_{\text{inh}}) \sum_{\text{inh } i} g_i \quad (18)$$

The sums of conductance signals $g_i(t)$ can also be simplified. Say that the values of g_i at $t = 0$ are G_i . The solution to equation (16) (at least in the time until a new presynaptic spike arrives) is then

$$g_i(t) = G_i e^{-t/\tau_g} \quad (19)$$

With this, and when all synapses have the same time constant τ_g , the two sums in equation (18) can be factored as follows:⁶

$$\sum_i g_i(t) = \sum_i \left(G_i e^{-t/\tau_g} \right) = \left(\sum_i G_i \right) e^{-t/\tau_g} \quad (20)$$



Figure 7: Example synaptic conductance trace $g_1(t)$, with a single incoming spike at $t = 20$ ms.



Figure 8: Another example trace $g_2(t)$, with spikes at $t = 10$ ms and 30 ms, and a smaller Δg .

⁶ This is only valid in the time before any new spikes arrive. But the ‘summability’ still holds after a new spike. To see this, the given reasoning can be repeated, but simply with different values for the G_i (all decayed by an amount $e^{-t_{\text{spike}}/\tau_g}$, and one increased by a bump Δg_i), and then redefining t_{spike} to be $t = 0$.

This means that we need to only keep track of two conductance signals: g_{exc} and g_{inh} , each the sum of all excitatory or all inhibitory synaptic conductances.

Our synaptic current sum then becomes simply:

$$I_{\text{syn}} = (V - E_{\text{exc}}) g_{\text{exc}} + (V - E_{\text{inh}}) g_{\text{inh}}, \quad (21)$$

and we only need to simulate two differential equations, instead of one for every synapse:

$$\begin{aligned} \frac{dg_{\text{exc}}}{dt} &= -g_{\text{exc}}/\tau_g \\ \frac{dg_{\text{inh}}}{dt} &= -g_{\text{inh}}/\tau_g, \end{aligned} \quad (22)$$

where on arrival of a spike at synapse i either g_{exc} or g_{inh} is instantaneously increased by a value Δg_i , depending on whether that synapse is excitatory or inhibitory.

We choose an excitatory reversal potential of $E_{\text{exc}} = 0$ mV, an inhibitory one of $E_{\text{inh}} = -80$ mV, and a time constant for the synaptic conductance decay of $\tau_g = 7$ ms. These values are rather arbitrary, but in line with other simulation studies (e.g. [Bre+07]).



Figure 9: A third synaptic conductance trace $g_3(t)$, with three input spikes at the same times and strengths as in figures 7 and 8. This signal is simulated independently, but turns out to be equal to the sum of the two others: $g_3(t) \equiv g_1(t) + g_2(t)$.

2.5 Model summary

Combining [equations \(1\) to \(3\)](#) with [equations \(21\) and \(22\)](#), our complete AdEx point neuron with conductance-based synaptic current is:

$$C \frac{dV}{dt} = -g_L(V - E_L) + g_L \Delta_T \exp\left(\frac{V - V_T}{\Delta_T}\right) - \underbrace{g_{\text{exc}}(V - E_{\text{exc}}) - g_{\text{inh}}(V - E_{\text{inh}})}_{-I_{\text{syn}}} - w$$

$$\tau_w \frac{dw}{dt} = a(V - E_L) - w$$

$$\tau_g \frac{dg_{\text{exc}}}{dt} = -g_{\text{exc}}$$

$$\tau_g \frac{dg_{\text{inh}}}{dt} = -g_{\text{inh}}$$

$$\begin{aligned} \text{When } V > \theta: \quad & V \leftarrow V_r \\ & w \leftarrow w + b \end{aligned}$$

$$\begin{aligned} \text{On input spike at..} \\ \text{exc. synapse } i: \quad & g_{\text{exc}} \leftarrow g_{\text{exc}} + \Delta g_i \\ \text{inh. synapse } j: \quad & g_{\text{inh}} \leftarrow g_{\text{inh}} + \Delta g_j \end{aligned}$$

We solve these equations numerically using first-order (Euler) integration, with a timestep Δt of 0.1 ms. This timestep is sufficiently small with respect to the different time constants in the model⁷. See [section 2.9](#) below for more details on the numeric implementation.

[Figure 10](#) shows the impulse response of this model, using a single spike, coming from either an excitatory or an inhibitory input neuron. The PSP bump is visible in the second panel from the bottom ('membrane voltage, V '). Note its tiny size, of about 0.04 mV. Our task will be to detect this tiny signal, in a sea of voltage imaging noise and PSP bumps of other input neurons.

Note also that, even though the inhibitory input is four times as strong as the excitatory one, its synaptic current and PSP bumps are not larger. (In fact, they are a smidge smaller). This is due to the fact that the neuron's resting potential (at -65 mV) lies closer to the inhibitory reversal potential ($E_{\text{inh}} = -80$ mV) than the excitatory one ($E_{\text{exc}} = 0$ mV), making the inhibitory term of the synaptic current I_{syn} weaker than the excitatory term (equation (21)).

Excitatory input spike



Inhibitory input spike



Synaptic conductances



Synaptic current, $-I_{\text{syn}}$



Membrane voltage, V



Adaptation current, w



Figure 10: **Impulse response of the conductance-based AdEx neuron.** Overlay of two independent simulations, each using a single spike arriving at $t = 10$ ms, with synaptic weight of either $\Delta g_{\text{exc}} = 14$ pS, or $\Delta g_{\text{inh}} = 56$ pS. Parameters as in [table 1](#), with $E_{\text{exc}} = 0$ mV, $E_{\text{inh}} = -80$ mV and $\tau_g = 7$ ms. For the inhibitory impulse response, $g_{\text{exc}}(t) \equiv 0$, and for the excitatory impulse response, $g_{\text{inh}}(t) \equiv 0$ (neither is shown). More details at [2023-09-05__Inhibitory_impulse_response_PSP](#).

⁷ $\tau_g = 7$ ms,
 $\tau_w = 88$ ms,
 $C/g_L = 24.2$ ms.

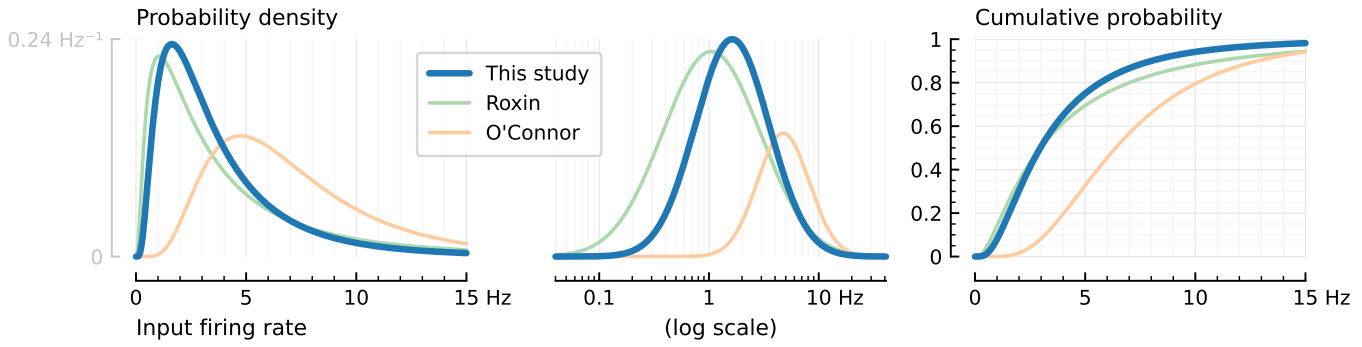


Figure 11: **Input spike trains are given log-normally distributed firing rates.**

The distribution used in our simulations is shown in bold. It has mean $\mu_x = 4$ Hz and variance of the underlying Gaussian $\sigma^2 = 0.6$. The two light distributions are from the literature. Note that the Roxin et al. distribution is slightly more heavy tailed than this study's: it has both more low firing and more high firing neurons.

2.6 Input in the N-to-1 setup

In our simplest experimental setup, we simulate just one AdEx neuron. Its input is provided by an array of N Poisson neurons, i.e. they each generate spike trains according to a Poisson process. We call this the 'N-to-1' setup.

Log-normal Poisson spiketrains

The firing rates of real neurons often follow a long-tailed distribution: most neurons do not fire much at all, while a few fire a lot. We recapitulate this in the firing rates of our Poisson input neurons, by drawing their firing rates from a log-normal distribution. We look to the literature for realistic parameters for this distribution, namely to the modelling paper of Roxin et al. [Rox+11], and the experimental sources it cites [HDZ08; OCo+10].

Log-normal distributions are usually parametrized with μ and σ : the location and scale of the underlying normal distribution, i.e. after log-transforming the input domain. In the above sources however, the mean μ_x of the data distribution itself is given. We can find μ , if σ is known, as $\mu = \ln(\mu_x) - \sigma^2/2$.

Roxin et al. use a mean rate μ_x of 5 Hz and a variance of the logarithm of the rate $\sigma^2 = 1.04$ in their figure 2. Hromádka et al. [HDZ08] recorded neurons in the auditory cortex of awake rats during acoustic stimulation. They find a mean firing rate μ_x of 6.2 Hz and a median of 2.4 Hz; no numeric variances are given. O'Connor et al. [OCo+10] recorded neurons in the barrel (whisker) cortex of behaving mice. Ensembled over all layers of the cortex they recorded from, they report $\mu_x = 7.4$ Hz, $\sigma_x = 12.6$ Hz, a median of 1.5 Hz, and an interquartile range of 9.5 Hz. This corresponds to a Gaussian variance of $\sigma^2 = \ln(1 + \sigma_x^2/\mu_x^2) = 0.30$. The Roxin and O'Connor

distributions are also shown in [figure 11](#).

Given these data, we choose our parameters μ and σ so that the distribution lies roughly halfway O'Connor's and Roxin's, while making sure our firing rates are rather low than high: as our idea for connection inference rests on the number of spikes that can be used to calculate spike-triggered averages (see [chapter 3](#)), we don't want to overestimate the number of available input spikes and obtain overly optimistic results.

Our log-normal distribution has a median of 2.96 Hz, very close to Roxin's 2.97 Hz. O'Connor's has 6.4 Hz, which is markedly different from the median of 1.5 Hz they reported (hinting that their data distribution might not be log-normal).

Synaptic weights

We choose to simulate EI-balanced input, where we simulate four times as many excitatory as inhibitory input spiketrains; but with the inhibitory inputs four times as strong as the excitatory inputs.

I.e. if our total number of input spiketrains is $N = 6500$, we have $N_{\text{exc}} = 5200$ excitatory inputs, and $N_{\text{inh}} = 1300$ inhibitory inputs. In the N-to-1-setup, we give every input of the same type the same synaptic weight. I.e. in the model summary ([section 2.5](#)), $\forall i : \Delta g_i = \Delta g_{\text{exc}}$ and $\forall j : \Delta g_j = \Delta g_{\text{inh}}$. If we would thus choose $\Delta g_{\text{exc}} = 10$ pS, then, for 4:1 EI-balanced input, Δg_{inh} would be 40 pS.

To choose a value Δg_{exc} for the excitatory input strength, we look at the desired output firing rate of our one simulated neuron. We want it to spike at a realistic, average rate. Thus, we try for it to have the same output firing rate as the mean input firing rate: $\mu_x = 4$ Hz. This rate is achieved by testing a range of different input drives Δg_{exc} : see [figure 12](#). For $N = 6500$ inputs, we find an average output firing rate of 4.0 Hz at $\Delta g_{\text{exc}} = 15$ pS (and thus $\Delta g_{\text{inh}} = 60$ pS).

Two asides on [figure 12](#). First, from the bottom panel, we see that the AdEx model, with parameters for a cortical RS (regular spiking) neuron, is a so called 'Type I' neuron:⁸ the firing rate can be made arbitrarily low, and there is no discontinuous jump from 0 Hz to some minimum firing rate.

Second, why does the output activity level increase for increasing excitatory input, if the inhibitory input becomes stronger by the same amount? The answer lies in the synaptic reversal potentials, which are $E_{\text{exc}} = 0$ mV and $E_{\text{inh}} = -80$ mV. The median membrane voltage (top panel in [figure 12](#)), at about -60 mV, lies closer to the inhibitory reversal potential than the excitatory potential, making the inhibitory term of the synaptic current I_{syn} weaker than the excitatory term (equation (21)).

The fact that this EI-balanced input leads to a net-excitatory effect can also be seen in [figure 13](#): the signal $g_{\text{exc}} - g_{\text{inh}}$ hovers around zero,



Figure 12: **Activity level of the output neuron in the N-to-1 setup, for increasing input strength Δg_{exc} .**

With $N = 6500$ EI-balanced inputs, and $\Delta g_{\text{inh}} = 4 \cdot \Delta g_{\text{exc}}$.

The blue line is the average over 10 different simulations (black dots), each with a different random seed for the input spike train generation.

Increasing input first heightens the voltage level without increasing the firing rate, and later heightens the firing rate without increasing the voltage level further.

V_m = membrane voltage V .

Source: 2023-08-05__AdEx_Nto1_we_sweep.

⁸ <https://neurondynamics.epfl.ch/online/Ch4.S4.html>



Figure 13: **Signals generated by the neuron model, for 6500 EI-balanced input spiketrains.**

Example extract from the signal traces of the conductance-based AdEx neuron. N-to-1 setup, with $\Delta g_{\text{exc}} = 15$ pS, and Poisson inputs with lognormally distributed firing rates. Neuron parameters for a cortical regular spiking neuron.

Note that the synaptic current signal $-I_{\text{syn}}$ is very similar to the difference of the excitatory and inhibitory synaptic conductances, as long as the membrane voltage V does not vary too much; on a spike (here at $t \approx 680$ ms), I_{syn} spikes as well.

Also note that the neuron spikes at a time when the inhibitory input randomly falls below the excitatory input, for a certain time. Spikes are 'fluctuation driven' in this input regime.

$g_e \equiv g_{\text{exc}}$ and $g_i \equiv g_{\text{inh}}$.

The V and $-I_{\text{syn}}$ signals are cut-off by the plot boundaries at the spike time.

Source: [2023-07-26__AdEx_Nto1_we_I_syn](#).

but the signal I_{syn} — even though it has largely the same shape — is nowhere near zero.

Later, we will compare the performance of a connection-detection algorithm across different numbers of inputs N . We choose the approximately evenly log-spaced sequence

$$N \in [10, 20, 45, 100, 200, 400, 800, 1600, 3200, 6500].$$

For each of these N , we want the output firing rate to be the same, namely 4 Hz. To find the synaptic strengths Δg_{exc} that accomplish this, we perform an iterative search.⁹ As an initial guess, it would make sense for the required input strength to scale inversely proportional to the number of inputs. We find however that there is a slight deviation from this linear expectation (figure 14): the less inputs, the less strong each input should be to reach the same output firing rate, compared to a linear extrapolation from our finding of $\Delta g_{\text{exc}} = 15$ pS for $N = 6500$. E.g. the linear expectation for $N = 10$ would be $\Delta g_{\text{exc}} = 9.75$ nS ($= 15 \text{ pS} \cdot 6500/10$), but we find we need only $\Delta g_{\text{exc}} = 2.83$ nS to reach an output firing rate of 4 Hz.

⁹ We use SciPy's `root_scalar` function, which uses 'Brent's method', which is like bisection but has faster convergence. We seed the algorithm with the bracket $[w_0/4, w_0 \cdot 4]$, where w_0 is the initial linear guess for Δg_{exc} . In about 8 iterations, we come within 0.01 Hz of the desired 4 Hz.



2.7 Spike ceiling

Our neuron model (section 2.5) consists of 1) a set of continuous differential equations, and 2) a discontinuous, instantaneous jump (namely whenever the membrane voltage V crosses the spike-definition threshold θ). Because we simulate our model using a discrete and finite timestep, this discontinuity introduces variability in the height of our spikes: the simulated voltage will never exactly equal the threshold θ in a given timestep, but will be either somewhere below it (where it will become the simulated spike height), or above it (in which case a spike is defined and the voltage is reset). This variability, or jitter, in the height of spikes can be seen in figure 15 (orange trace).

Real neurons generally do not show such variability: their spike heights are quite consistent (remarkably so). To make our simulated voltage traces look more realistic, we set the voltage to a fixed height at spike events. We call this modification "spike ceiling". It is illustrated in figure 15 (blue trace).

This spike ceiling is a common technique. In Izhikevich's book for example, the same technique is applied (there it is called "spike padding"): see listing 1. There is one difference however. Izhikevich's code pads the spikes during the simulation, and overwrites the spike height of the previous timestep, before the threshold crossing. We ceil our spikes after the simulation has fully run. We ceil the voltage one timestep later than Izhikevich: after the threshold

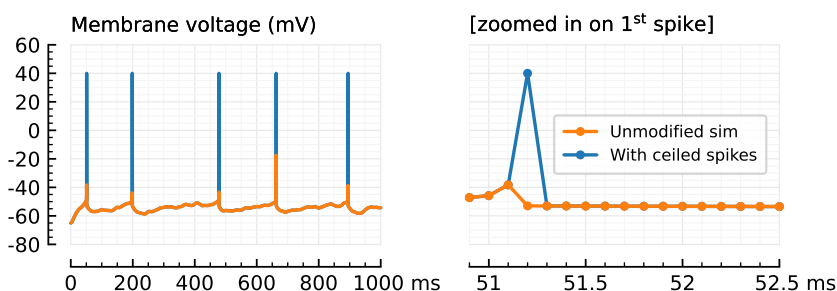


Figure 15: Example voltage trace, before (orange) and after (blue) spikes are ceiled.

Source: 2023-09-05__ceil_spikes.

Figure 14: Finding the right input strength in the N-to-1 setup, for different numbers of inputs N .

Δg_{exc} is the synaptic conductance increase per incoming spike from an excitatory input. For each N , the right Δg_{exc} value — namely the one for which the output neuron fires at 4 Hz — was found using an iterative search procedure. For every Δg_{exc} value evaluated, ten different 10-second simulations were run (each with a different random seed for the input spiketrain generation). The average output firing rate of these ten simulations was taken, and compared with the goal firing rate of 4 Hz. Δg_{exc} was then adjusted until the simulated firing rate was sufficiently close. In every case, Δg_{inh} was four times Δg_{exc} . Source: 2023-08-05__AdEx_Nto1_we_sweep.

crossing; i.e. the timestep where the voltage was previously reset to V_r . This difference in approach is merely a personal aesthetic preference, and was not found to yield any difference in network inference performance in an informal test.

The act of spike ceiling in itself does have an effect on network inference performance. This is shown later, in [section 3.1](#).

```

1 for i = 1:n-1           % forward Euler method
2   v(i+1) = v(i)+tau*(k*(v(i)-vr)*(v(i)-vt)-u(i)+I(i))/C;
3   u(i+1) = u(i)+tau*a*(b*(v(i)-vr)-u(i));
4   if v(i+1) >= vpeak    % a spike is fired!
5     v(i) = vpeak;      % padding the spike amplitude
6     v(i+1) = c;        % membrane voltage reset
7     u(i+1) = u(i)+d;    % recovery variable update
8   end;
9 end;

```

Listing 1: Matlab code simulating the Izhikevich neuron. Lines pertinent to spike ceiling/padding are highlighted. Source: Eugene Izhikevich's 2007 book, *Dynamical Systems in Neuroscience: The Geometry of Excitability and Bursting*, section 8.4.1 ("Simple Model of Choice"), p. 274

2.8 Voltage imaging

The signals detected by a light microscope in a voltage imaging setup are not the same as the real membrane voltage traces of which they are a reflection.

We model this lossy transformation by simply adding Gaussian noise to our simulated membrane voltage. As in the voltage imaging literature, we quantify the amount of this noise by a 'spike-SNR' measure (spike signal-to-noise ratio). This is defined as the height of an average spike relative to the standard deviation of the noise:

$$\text{spike-SNR} = \frac{\text{spike height}}{\sigma_{\text{noise}}} \quad (23)$$

In other words, if we call our output signal y , and with V_i the voltage samples resulting from the numeric integration of equation (1), we have:

$$y_i = V_i + \varepsilon_i \quad (24)$$

$$\varepsilon_i \sim \mathcal{N}(0, \sigma_{\text{noise}})$$

A typical but conservative level of noise in voltage imaging recordings has a spike-SNR of 10. If we take as spike height the spike detection threshold minus the leak potential ($\theta - E_L$, see [table 1](#)), we obtain a σ_{noise} of 10.5 mV.

A more realistic model of the voltage imaging-transformation would also incorporate the exponential decay over time of the SNR (with a



Figure 16: Simulated voltage trace (same as in [figure 5](#), right), without and with 'voltage imaging' (VI) noise added ($\sigma_{\text{noise}} = 10.5$ mV).

time constant of about 10 minutes), and the short-term ‘smearing in time’ of voltage indicators. The latter could be done by passing the voltage signal through a linear filter with some non-instantaneous impulse response.

2.9 Software implementation

To numerically simulate the model described in this chapter, different software implementations have been used throughout my PhD.

Software	Language	Model	Time (seconds)	
			Compilation	Simulation
Brian2	Cython + Python	full	61	11
		merged	86	11
	C++	full	15	6.5
		merged	18	0.35
own	Julia	full	0.68	0.036

{to expand a bit}

Table 3: Time taken to simulate 10 seconds of the N-to-1 experiment with $N = 6500$ Poisson inputs, and one conductance-based AdEx neuron. In the ‘merged’ models, only 200 Poisson spiketrains are independently simulated (instead of all 6500, as in the ‘full’ model). All other inputs are replaced by two single Poisson inputs (one excitatory and one inhibitory), with an equivalent effect. (That is, we use Brian’s ‘[PoissonInput](#)’).

For details, see [2023-07-10__AdEx_Nto1_Brian_speedtest](#) (Cython), [2023-08-02__speedtest_brian_standalone_AdEx_Nto1](#) (C++), and [2023-08-09__Poisson_cquantile_upperbound](#) (Julia).

Spike-triggered averaging

As shown in [figure 1](#), our idea for connection inference rests on the causal ‘presynaptic spike’ \rightarrow ‘postsynaptic voltage bump’ link. I.e. we want to know for which neuron pairs a spike in one is reliably followed by such a bump in the other. The problem is that these bumps (the postsynaptic potentials or PSPs) are minute, and are easily drowned out by (1) other PSPs, (2) postsynaptic spikes, and (3) voltage imaging noise.

So, as is often done in neuroscience, we take the *average* over many instantiations, so as to hopefully find a signal in the noise. Specifically, we take spike-triggered averages, or **STAs**, of neurons’ voltage traces. If there is a connection from neuron ‘M’ to neuron ‘N’, then an STA of neuron N’s voltage imaging signal, based on neuron M’s spikes, would hopefully show the PSP.

To use this idea for an actual connection test, we look specifically at the height of an STA, and compare it to a distribution of STA heights that we’d expect were the two neurons not connected. This is illustrated in [figure 18](#).

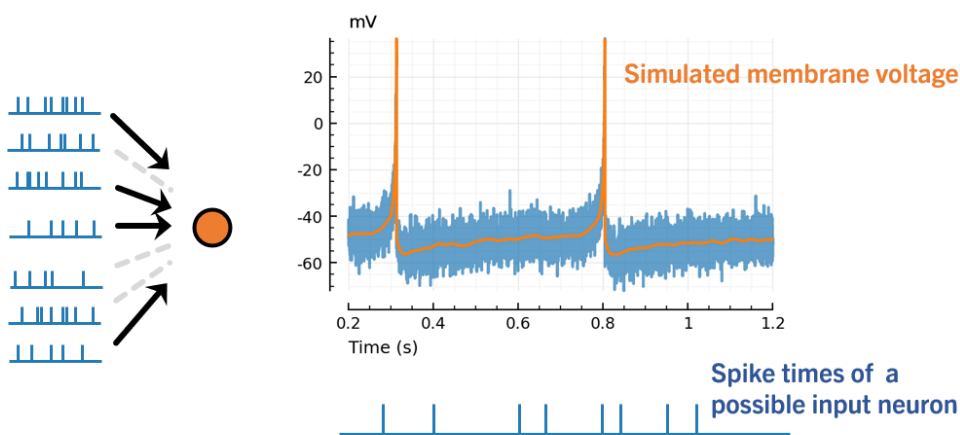


Figure 17: **The ‘N-to-1’ problem.**

Left: A neuron N (orange circle), and the spike trains of other neurons in the network (blue). Some of these other neurons impinge directly on N (black arrows), while others are not (directly) connected (dashed gray lines). Given only neuron N ’s voltage signal and the other neurons’ spiketrains, we want to detect the direct inputs, while rejecting the not-directly-connected spiketrains.

Right: The simulated membrane voltage of the impinged-upon neuron (orange), and the same signal with Gaussian noise added, to simulate a voltage imaging signal (blue). Underneath the plot, one of the possible input spiketrains, time-aligned to the voltage signal. This alignment is used later to extract spike-triggered windows from the voltage signal.

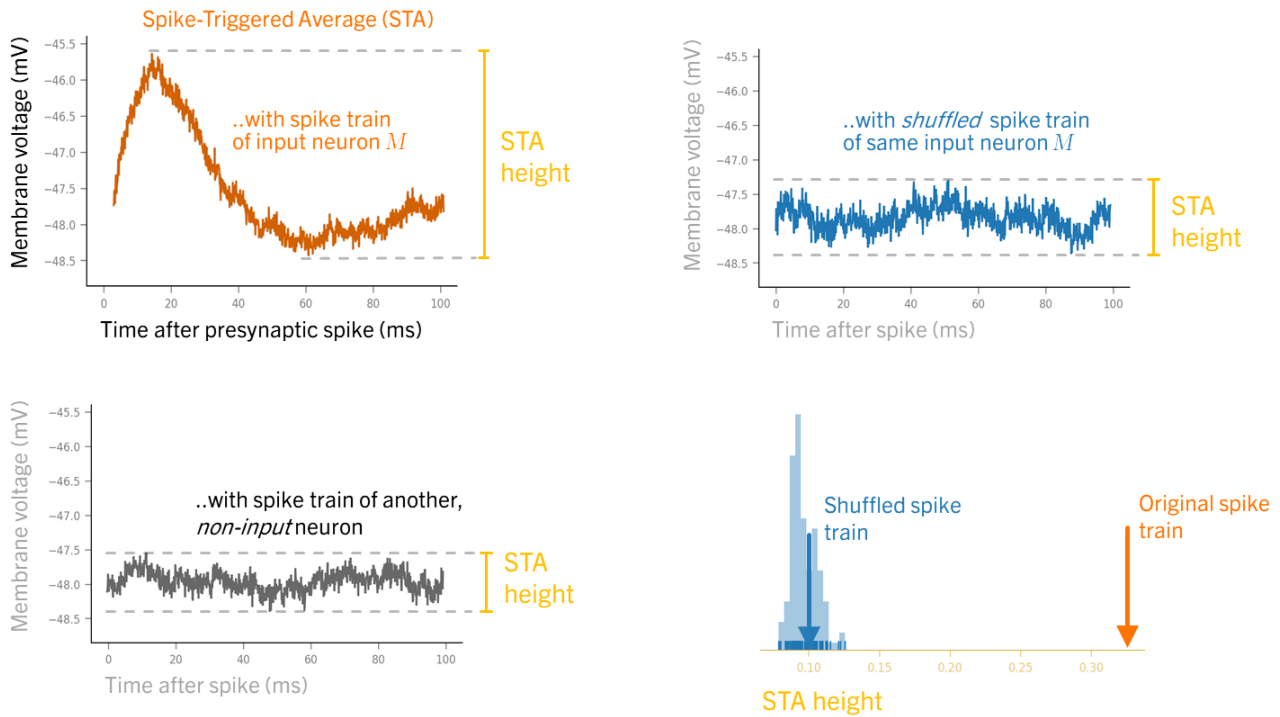


Figure 18: **A simple connection test: STA height with shuffle control.**

The spikes of a possible input neuron are aligned to the voltage trace of the neuron of interest N , as in figure 17. For every such spike, a 100-ms long window is cut out of the voltage of N . The average of all these windows is called the spike-triggered average (STA).

Left: Two example STAs of neuron N 's membrane voltage: one for an actually connected input neuron, M (top, orange); and one for a non-input neuron (below, gray). Given an STA signal x , we will use its height $h = \max(x) - \min(x)$ (also known as 'peak-to-peak' or 'ptp') to test whether two neurons are connected.

Right: An STA of N 's membrane voltage using a shuffled version of M 's spike times (which is made by randomly permuting the inter-spike-intervals of M). This 'shuffled STA height' provides a control for the STA height connection test statistic: "what do we expect the STA height to be if there is *no* connection $M \rightarrow N$ ". By calculating different such shuffles, we obtain a null-distribution for the STA height test statistic. And by comparing the real STA height to this distribution, we can calculate a p -value. Here, the real STA is larger than all shuffle controls, of which there are 100. So $p < 0.01$, and at $\alpha = 0.05$, we conclude there is indeed a connection $M \rightarrow N$.

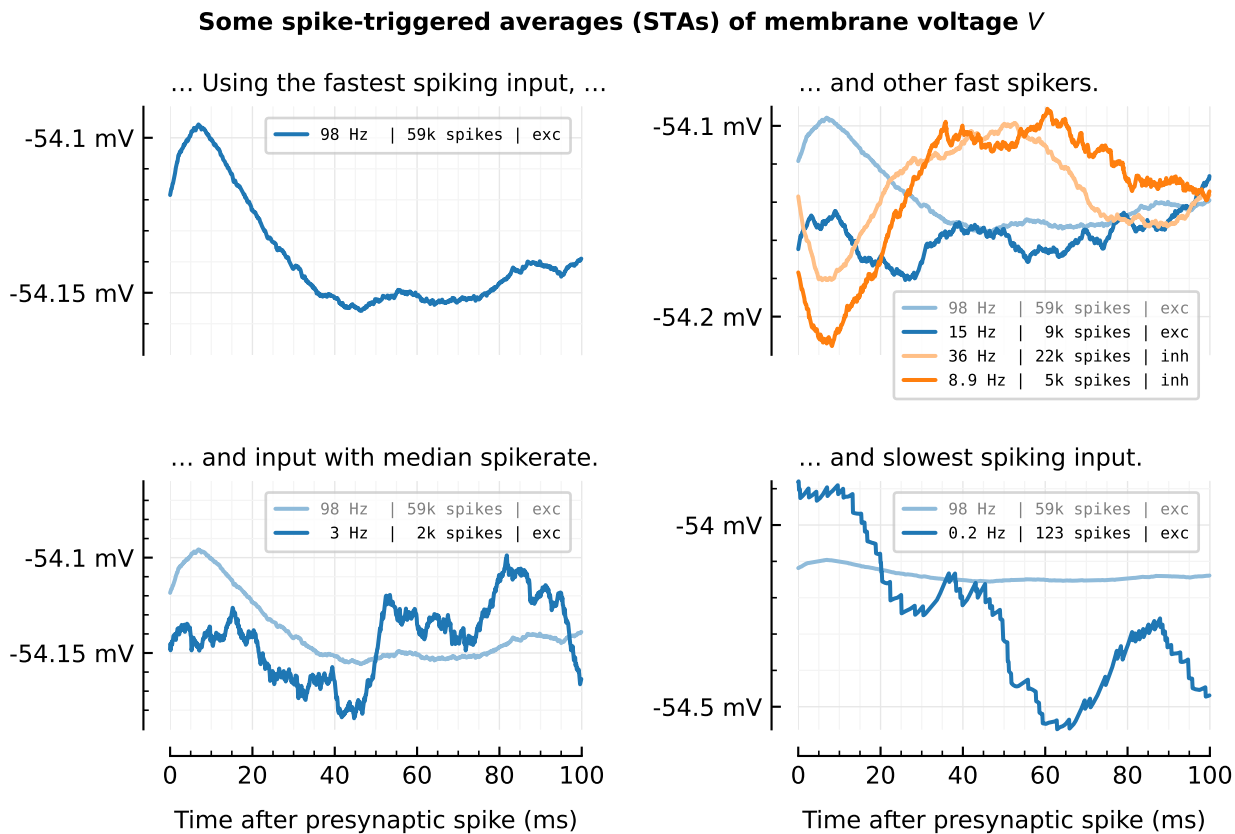


Figure 19: **Example STAs in the 10' simulation with 6500 inputs.**

Note that every panel has a different y-axis (voltage) scale. The STA of the most active input is repeated in every panel (in faded blue), to allow a visual scale comparison nonetheless.

The inset legends indicate with how many presynaptic spikes the STA was calculated, and whether the input was an excitatory or inhibitory one.

The top right panel shows STAs of the 1st and 100th fastest spiking inputs, both within the excitatory inputs (blue shades), and within the inhibitory inputs (orange shades).

Source: [2023-09-13__Clippin_and_Ceilin](#).

3.1 Ceiling and clipping

As explained in [section 2.7](#), we modify our simulated voltage trace so that spikes have a consistent height. This modification has an effect on STAs, as is illustrated in [figure 20](#): the blue trace is the signal without spike ceiling, the orange one with spike ceiling. Their corresponding STAs are shown on the right. Note that the orange STA (made with ceiled spikes) is much noisier than the blue STA (from the unmodified voltage trace).

This suggests a relatively easy intervention to drastically de-noise STAs, and presumably increase their effectiveness for network inference: namely to remove the spikes from the signal.

We tried this ‘spike clipping’ and it indeed drastically denoised the STA; see the green signal and STA in [figure 20](#). We show that this decreased noise in the STA does indeed lead to an increase in network inference performance, by running a connection detection test without and with this spike clipping. The results are shown in [figure 21](#): detection performance increases from an AUC of 0.56 for the non-clipped voltage trace, to an AUC of 0.79 for the voltage trace with clipped spikes.



Figure 20: Example voltage traces and corresponding STAs, where the only difference is the height of spikes. In blue, the unmodified simulated voltage trace. In orange, the same, but with ceiled spikes (as in [section 2.7](#)). In green, the same as orange, but with the spikes clipped again after the ceiling (as explained in this section).

Source: [2023-09-13__Clippin_and_Ceilin](#).

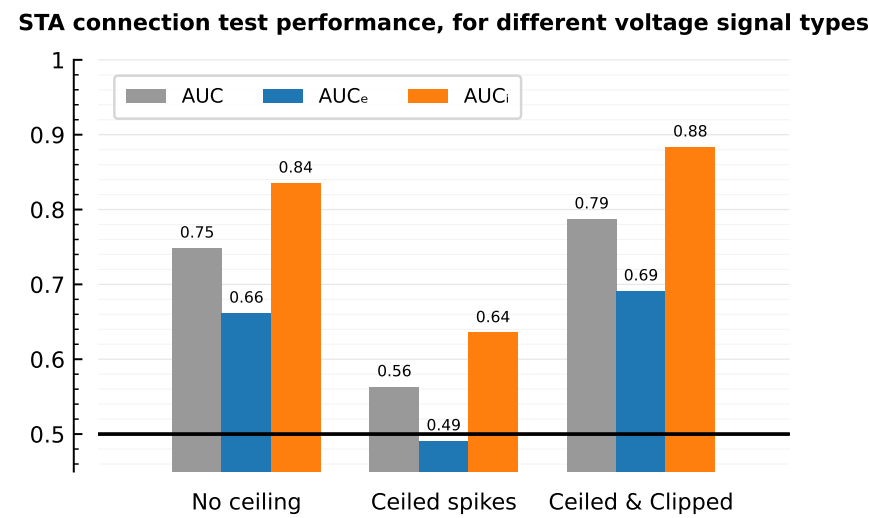


Figure 21: Connection detection performance for the three types of handling spikes shown in figure 20: not modifying them; ceiling them; and clipping them.
Source: [2023-09-13__Clippin_and_Ceilin.](#)

3.2 Performance quantification

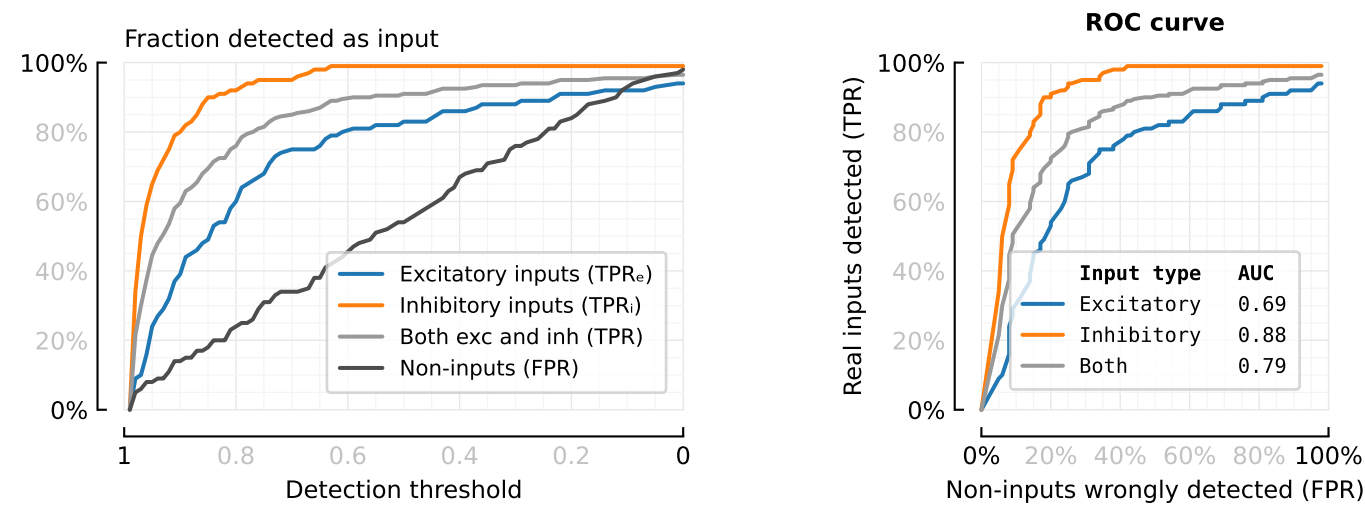


Figure 22: .
Source: [2023-09-13__Clippin_and_Ceilin.](#)

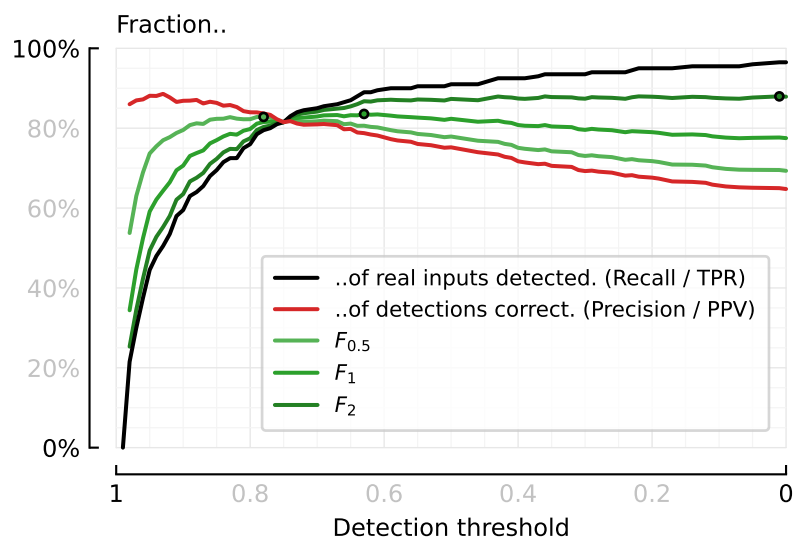


Figure 23: .

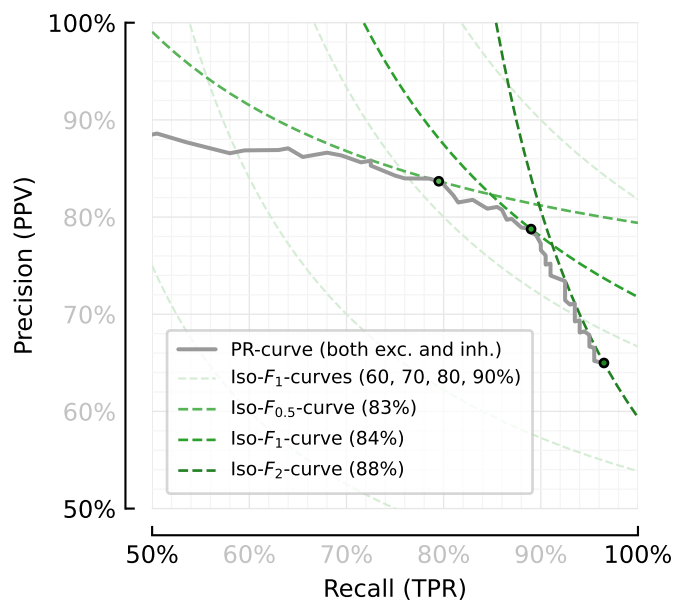


Figure 24: .

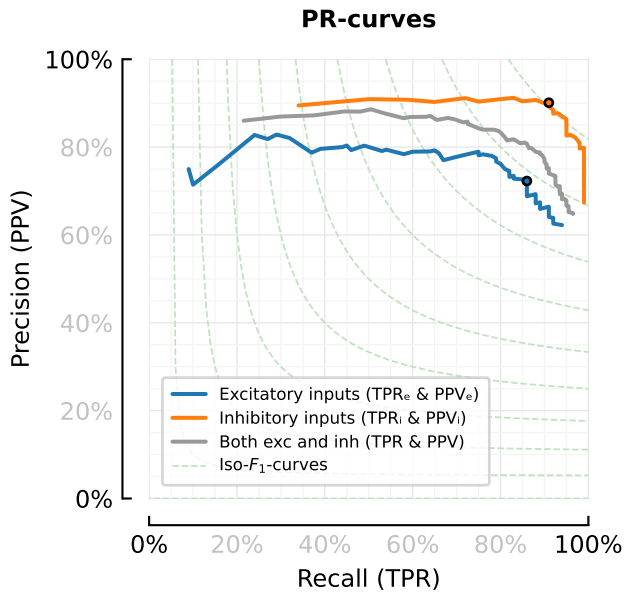
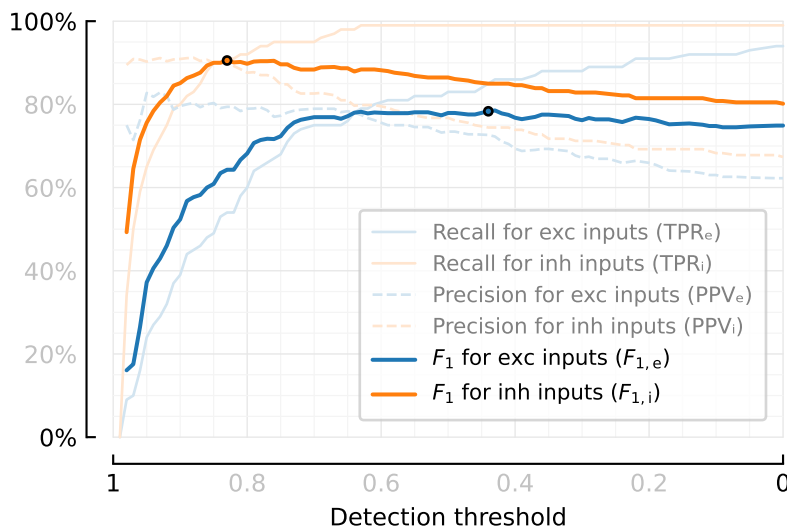
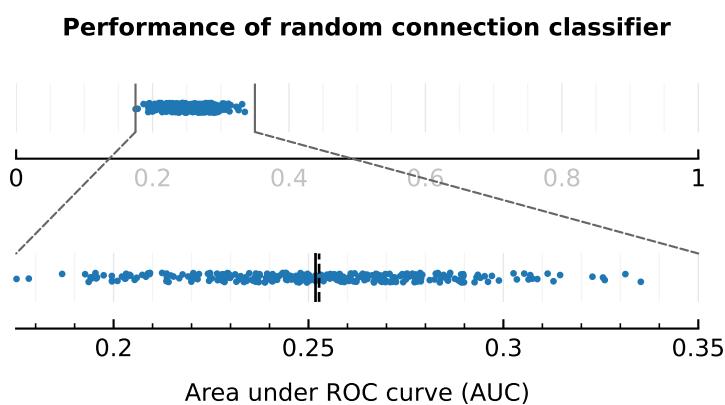


Figure 25: .

Figure 26: **Excitatory and inhibitory inputs reach $\max F_1$ at different thresholds.**

But for simplicity, whenever we use $\max F_1$ to evaluate a classifier, we will use only one threshold for both types of inputs, which will be a compromise between these two thresholds.

Figure 27: **Randomly classifying connections yields a chance level $AUC < 0.5$.**

300 random test results, and their performance as connection detector, quantified as area under their ROC curves. Solid black line is the mean, dashed line is the median.

In every of the 300 simulations, every connection (100 exc, 100 inh, and 100 unconnecteds) was assigned a random 't-value' uniformly between -1 and 1 ; and then the classification threshold was swept over these t-values.

3.3 Recording duration & noise

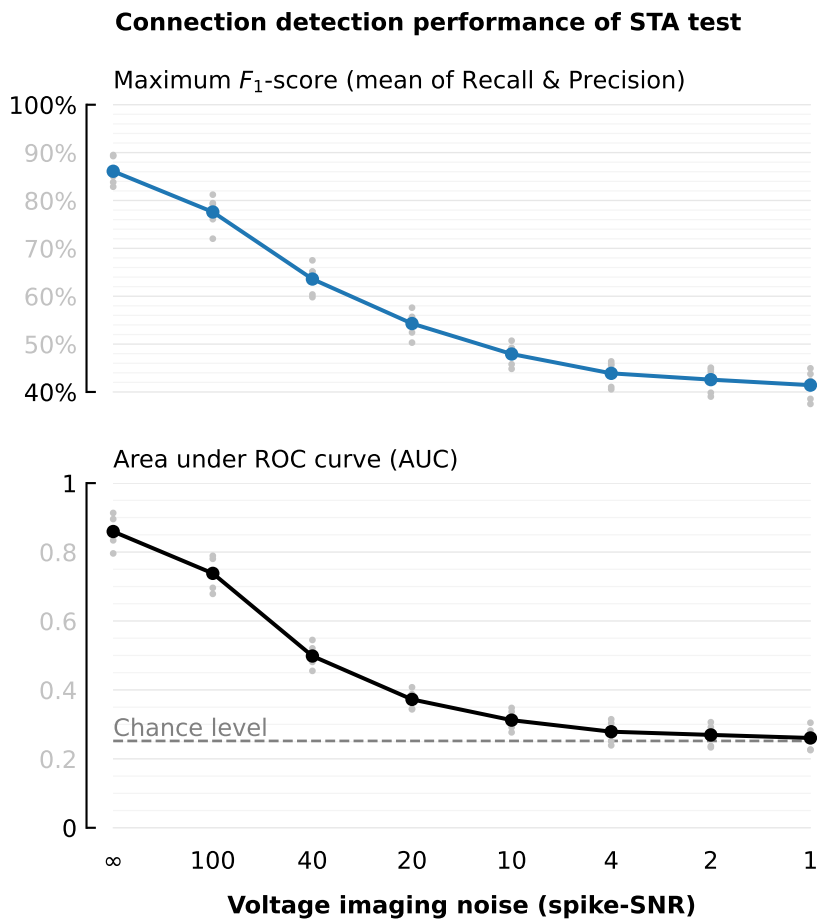


Figure 28: **Performance drops to chance level for noisier signals.**

All simulations were 10 minutes long. Signal-to-noise (SNR) values on the x-axis are approximately (but not exactly) log-spaced. An SNR of ' ∞ ' corresponds to no noise (i.e. the voltage signal straight out of the simulation, without any noise added). For every SNR value, five different simulations were run (gray dots), each with a different RNG seed for input firing rate and spiketrain generation. The mean performances of these five simulations are plotted with larger dots and are line-connected. Only the 100 highest-firing excitatory and inhibitory inputs were tested. An additional 100 unconnected spiketrains were generated and tested, with similar firing rates as those 200 high-firing real inputs. AUC chance level determined as in [figure 27](#).

Source: [2023-09-20__STA_comntest_for_diff_recording_quality_n_durations](#).

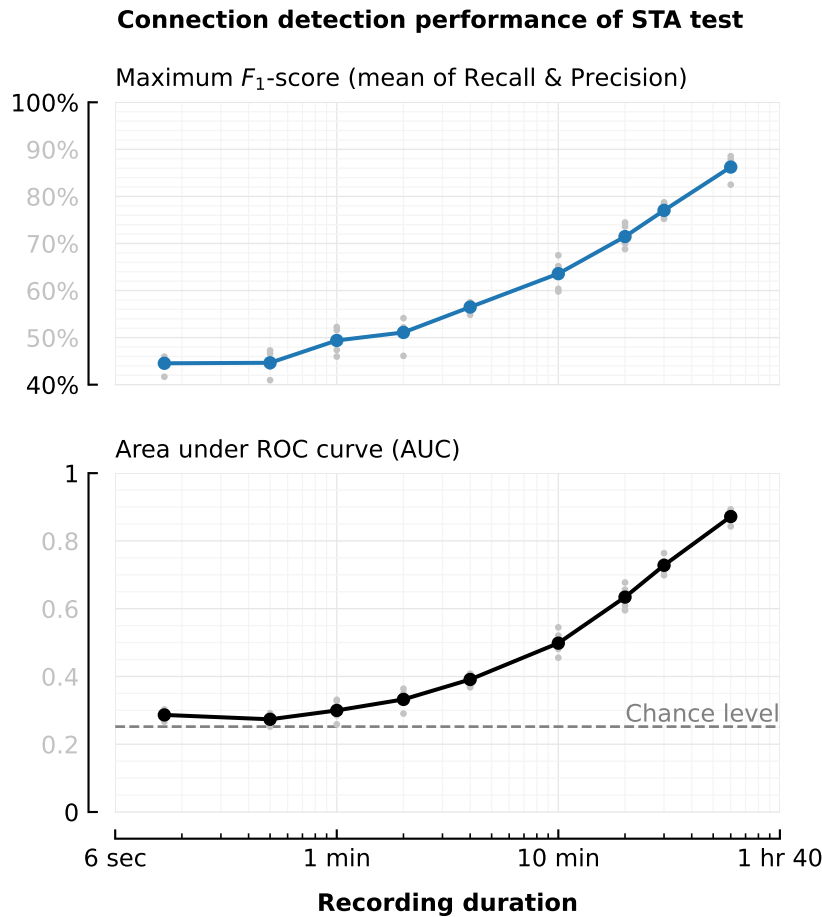


Figure 29: **Longer recordings allow more accurate connection inference.**

All simulations had a voltage imaging noise level (spike-SNR) of 40.

The simulation ('recording') durations are on a logarithmic axis. (The first two data points are at 10 and 30 seconds; the last one is at 1 hour).

For more, see [figure 28's](#) caption.

3.4 Computational cost of STA test

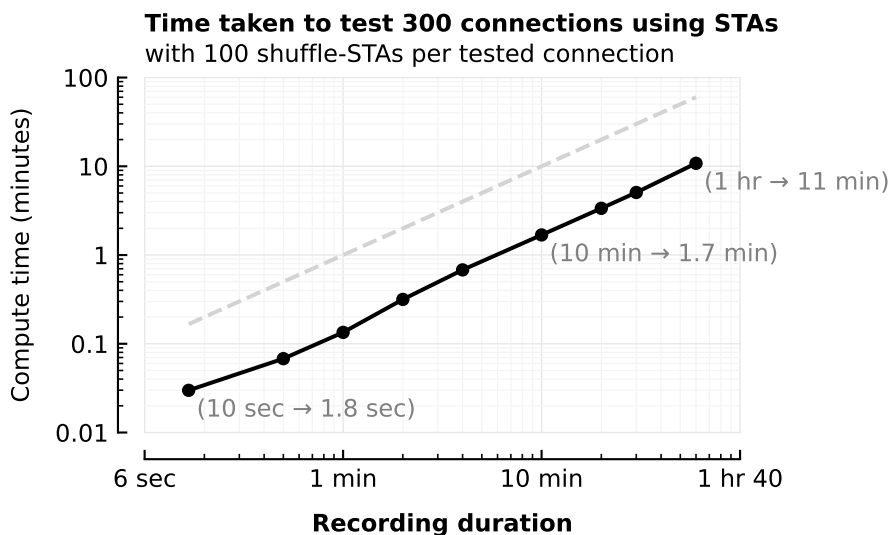


Figure 30: **Test time scales linearly with voltage signal duration.**

Simulation timestep ('sample time') of 0.1 ms. STA length of 20 ms; i.e. 200 samples. The chosen inputs to test (300 high firing trains) have a median firing rate of 16 Hz. i.e. at a simulation duration of 10 seconds, there are about 160 presynaptic spikes per tested connection. There are 101 times that many STAs to calculate per connection: once for the real spiketrain, and a 100 times for shuffles of it. For a 10 second simulation, there are thus about 16k STAs to calculate per connection. For 10 minutes: 967k STAs. For 1 hour: 5.8M STAs.

Black dots are the means over five simulations per duration. Compute time for individual simulations is shown in grey.

New connection inference methods

4.1 STA Template correlation

- Idea for the two-pass test
- Template examples. Both ideal and template found with first-pass (STA height-only)
- Performance for different N , & comparison with previous method

4.2 Linear regression of the upstroke

- Non-STA method: concatenated individual windows as (X, y)
- Examples of pooled windows, and fits
- Mention the problem of unknown transmission delays
- Performance for different N , & comparison with previous methods

4.3 Fitting a full STA model

- Model design
- Iterative model fitting
- Problem of overfitting, and parameter-constraints to solve it
- An advantage: fit parameters (like transmission delay and time constants) are biologically meaningful
- Performance for different N , & comparison with previous methods

4.4 Clustering, & Hierarchical model fitting

- (Time-permitting)

4.5 Zhou/Cai's 'Spike-triggered regression'

- (Time-permitting)

4.6 Computational cost

- Timings of each method, extrapolation for larger number of tested connections

4.7 Summary

- Conclusions of the N-to-1 experiment
- Leadup to the network experiments: what we could not yet test (the problem of indirect connections, as e.g. identified in the connectomics challenge)

Network model

- Network connectivity, E/I balance, raster plots
- Too many possible connections to test them all → Subsampling
- Performance of last chapter's methods
- If time: experiment with a network that is less densely connected than our current fully-random one. Why? To better examine the effect of indirect connections / colliders (For the current connectivity, there are too many of those. But in a more realistic, 'localized' network, there are less, and so it seems easier to isolate and examine their effect).

Discussion

6.1 Summary & conclusions

..

6.2 Future work

- Test on real data
- Direct comparison with spikes-only methods
- More complexity in the testing setup: different transmission delays and time constants per synapse / neuron, plus:
- Short term synaptic plasticity. Bursting. Oscillations.
- Simulate different brain areas (different cell types and connectivity patterns). Simulate the same area, but in different states (up vs down, e.g.)
- New connection test method to try: something deep learning-based (we have infinite training data, given our simulation)

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