

# Homework

Saturday, February 12, 2022 3:18 PM

Precedence of operators

$$9 + 5 * 2$$

$$(9 + 5) * 2 \text{ or } 9 + (5 * 2) ?$$

Homework:

a) Build a grammar for arithmetic expressions (+, -, \*, ÷)

Solution

+ , -  
\* , /      ↓ precedence

Since we have  $n=2$  levels of precedence, we need  $n+1$  Nonterminals for the grammar:

- |               |  |
|---------------|--|
| 1. piece      | } from lowest to highest level of precedence |
| 2. term       |  |
| 3. expression |  |

To define the grammar, we will use the productions:

1.  $\text{expression} \rightarrow \text{expression} + \text{term} \mid \text{expression} - \text{term} \mid \text{term}$
2.  $\text{term} \rightarrow \text{term} / \text{piece} \mid \text{term} * \text{piece} \mid \text{piece}$
3.  $\text{piece} \rightarrow \text{digit}$
4.  $\text{digit} \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid \infty$

Note: it is current\_nonterminal, operator, higher-precedence\_nonterminal since current\_nonterminal (+, -, /, \*) are left associative, and thus they are similar to lists that associate to the left:  $\text{list} \rightarrow \text{list} + \text{digit}$ .

b) Build the grammar for the statements (propositions) missing in example 2, prop.

Example 2: Sequence of statements (propositions) separated by ; that are inside blocks of begin and end.

Solution: consider: (if, if else, while, for, do while, switch)

$\text{block} \rightarrow \text{begin props\_opt end}$

$\text{props\_opt} \rightarrow \text{list\_props} \mid \epsilon$

$\text{list\_props} \rightarrow \text{list\_props} ; \text{prop} \mid \text{prop}$

$\text{prop} \rightarrow \text{if}(\text{expr}) \text{ stmt};$   
            $\mid \text{if}(\text{expr}) \text{ stmt}; \text{else stmt};$   
            $\mid \text{while}(\text{expr}) \text{ stmt};$   
            $\mid \text{do stmt}; \text{while}(\text{expr});$   
            $\mid \text{switch}(\text{id}) \text{ case}(\text{digit}) \text{ stmt}; \text{default stmt};$   
            $\mid \text{for}(\text{expr}) \text{ stmt}$

$\text{stmt} \rightarrow \text{id} = \text{expr} \mid \text{expr} \mid \epsilon$

$\text{expr} \rightarrow \text{expr} + \text{term} \mid \text{expr} - \text{term} \mid \text{term}$

$\text{term} \rightarrow \text{term} / \text{piece} \mid \text{term} * \text{piece} \mid \text{piece}$

$\text{piece} \rightarrow \text{digit}$

$\text{digit} \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid \infty$