

Homework

Saturday, February 12, 2022 3:18 PM

Precedence of operators

$$9 + 5 * 2$$

$$(9 + 5) * 2 \text{ or } 9 + (5 * 2) ?$$

Homework:

a) Build a grammar for arithmetic expressions (+, -, *, ÷)

Solution

$$\begin{array}{l} +, - \\ *, / \end{array} \quad \begin{array}{l} \downarrow \text{precedence} \\ + \end{array}$$

Since we have $n=2$ levels of precedence, we need $n+1$ Nonterminals for the grammar:

- | | |
|---------------|--|
| 1. piece | } from lowest to highest level of precedence |
| 2. term | |
| 3. expression | |

To define the grammar, we will use the productions:

1. expression \rightarrow expression + term | expression - term | term
2. term \rightarrow term / piece | term * piece | piece
3. piece \rightarrow digit
4. digit \rightarrow 0 | 1 | 2 | 3 | ... | 9

Note: it is current_nonterminal, operator, higher-precedence_nonterminal since current_nonterminal (+, -, /, *) are left associative, and thus they are similar to lists that associate to the left: list \rightarrow list + digit.

b) Build the grammar for the statements (propositions) missing in example 2, prop.

Example 2: Sequence of statements (propositions) separated by ; that are inside blocks of begin and end.

Solution: consider: (if, if else, while, for, do while, switch)

block \rightarrow begin props_opt end

props_opt \rightarrow list_props | ϵ

list_props \rightarrow list_props ; prop | prop ;

prop \rightarrow if (expr) stmt ;
 | if (expr) stmt ; else stmt ;
 | while (expr) stmt ;
 | do stmt ; while (expr) ;
 | switch (id) case (digit) stmt ; default stmt ;
 | for (expr) stmt ;

stmt \rightarrow id = expr ; | expr ; | ϵ ;

expr \rightarrow expr + term ; | expr - term ; | term ;

term \rightarrow term / piece ; | term * piece ; | piece ;

piece \rightarrow digit ;

digit \rightarrow 0 | 1 | 2 | 3 | ... | 9