


Monad Transformers



Background: abstracting over effects

works with any effect



```
add :: Monad m => m Int -> m Int -> m Int
add mx my = do
  x <- mx
  y <- my
  return (x + y)
```

IO

```
>>> add readIO readIO
```

5

7

12

Failure

```
>>> add (Just 3) (Just 4)
Just 7
```

```
>>> add (Just 3) Nothing
Nothing
```

Nondeterminism

```
>>> add [10, 20] [1, 3, 5]
[11, 13, 15, 21, 23, 25]
```

tracing, state, exceptions, ...

Monads and effects

Monads help us to **structure** effects:

- write effect logic once (in Monad instance)
- sequence effectful code (with bind/do-notation)
- abstract over a variety of effects

What if we need more than one effect?

Monad transformers help us to **combine** effects:

- write *interaction logic* once (in MonadTrans instance)
- use multiple effects by *layering* monad transformers

Monad transformer

Monad (t m) =>

```
class MonadTrans t where  
  lift :: Monad m => m a -> t m a
```

return for m

return for t m

`lift . return <==> return`

lift distributes over bind

`lift (m >>= f) <==> lift m >>= (lift . f)`

Maybe monad transformer

```
data MaybeT m a = MaybeT { runMaybeT :: m (Maybe a) }
```


Equivalent to:

```
data MaybeT m a = MaybeT (m (Maybe a))  
runMaybeT :: MaybeT m a -> m (Maybe a)  
runMaybeT (MaybeT x) = x
```

Maybe monad transformer

```
data MaybeT m a = MaybeT { runMaybeT :: m (Maybe a) }
```

```
instance Monad m => Monad (MaybeT m) where
    return = MaybeT . return . Just
    x >>= f = MaybeT $ do may <- runMaybeT x
                        case may of
                            Nothing -> return Nothing
                            Just a -> runMaybeT (f a)
```

do-block in m! 

```
instance MonadTrans MaybeT where
    lift m = MaybeT (m >>= return . Just)
```

Maybe monad transformer

```
data MaybeT m a = MaybeT { runMaybeT :: m (Maybe a) }
```

```
instance Monad m => MonadPlus (MaybeT m) where
    mzero      = MaybeT (return Nothing)
    mplus x y = MaybeT $ do may <- runMaybeT x
                           case may of
                               Just _   -> return may
                               Nothing -> runMaybeT y
```



State monad transformer

```
data StateT s m a = StateT (s -> m (a, s))
```

Recall original state monad:

```
data State s a = State (s -> (a, s))
```

```
instance Monad (State s) where
  return x = State (\s -> (x, s))
  State c >>= f = State $ \s ->
    let (x, t) = c s
    in State d = f x
    in d t
```


State monad transformer

```
data StateT s m a = StateT (s -> m (a, s))
```

Recall original state monad:

```
data State s a = State (s -> (a, s))
```

```
instance Monad m => Monad (StateT s m) where  
  return x = StateT (\s -> return (x, s))  
  StateT c >>= f = StateT $ \s -> do  
    (x, t) <- c s  
    let StateT d = f x  
    return (d t)
```

do-block in m!



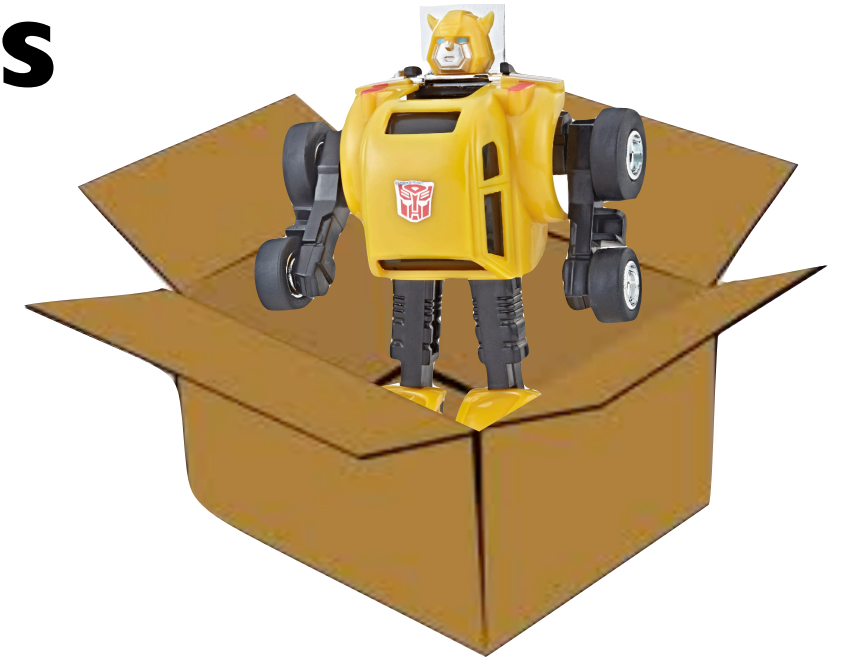
Other monad transformers

Box-like monads:

MaybeT (m (Maybe a))

ListT (m [a])

ExceptT (m (Either e a))



Computation-like monads:

	<i>Original</i>	<i>Transformer</i>
<i>Writer</i>	Writer (a, w)	WriterT (m (a, w))
<i>Reader</i>	Reader (r -> a)	ReaderT (r -> m a)
<i>State</i>	State (s -> (a, s))	StateT (s -> m (a, s))

Identity monad

A trivial monad – useful base of a monad transformer stack

```
data Identity a = Identity { runIdentity :: a }
```

```
instance Monad Identity where  
    return = Identity  
    Identity x >>= f = f x
```

```
    Maybe a    <~>    MaybeT Identity a  
    Writer w a  <~>    WriterT w Identity a  
    State s a   <~>    StateT s Identity a  
    ...
```

Ordering monad transformers

The order that you layer effects matters!

`StateT s (MaybeT Identity) a`

corresponds to: `s -> Maybe (a, s)`

`MaybeT (StateT s Identity) a`

corresponds to: `s -> (Maybe a, s)`

 *new state even if
computation fails!*

(Semi-) automatic lifting

Some type classes to ease or automate lifting in deep stacks

Lift an IO action through all monad transformers:

```
class Monad m => MonadIO m where  
  liftIO :: IO a -> m a
```

“Primitives” that automate lifting:

check out the “mtl” library!

```
class Monad m => MonadState s m | m -> s where  
  get :: m s  
  put :: s -> m ()
```

```
class Monad m => MonadError e m | m -> e where  
  throwError :: e -> m a  
  catchError :: m a -> (e -> m a) -> m a
```

(KitchenSink.hs)

