

Defects in materials

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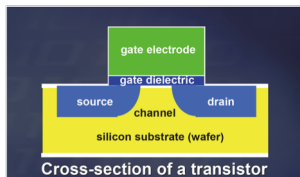
- Motivation.
- Computational methods.
- Defects in oxides.
 - Why are defects challenging?
 - Defects in high- κ dielectric – HfO_2 .
 - Defects in technologically important material – TiO_2 .
 - Defects for quantum computing.

■ Motivation.

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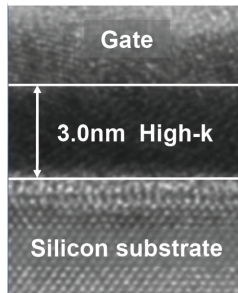
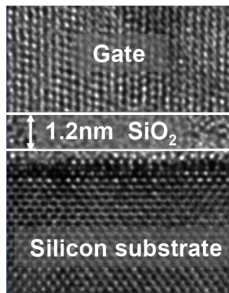
Motivation – High- κ dielectric material HfO_2

- Moore's law about size of transistor.
- HfO_2 has replaced SiO_2 in today's MOSFET devices.



$$\kappa_{\text{SiO}_2} \approx 3.9$$

$$\kappa_{\text{HfO}_2} \approx 16 - 17$$



¹<http://www.intel.com/technology/45nm/index.htm>

- High defect density.
- Charge trapping by defects in the interfacial layer or oxide – threshold voltage instability¹.
- Oxygen-related defects – vacancy² (V_O) or interstitials (I_O) major cause.
- Study the stability of point defects – V_O .

¹G. Ribes et. al., IEEE Trans. Device Mater. Reliab. **5**, 5 (2005).

²K. Shiraishi et. al., Jpn. J. Appl. Phys., Part 2 **43** L1413 (2004); H. Park et. al., IEEE Electron Device Lett. **29**, 54 (2008).

- Photovoltaic material in solar cells¹.
- Photocatalytic material – hydrolysis of water².
- Memresistive switches for non-volatile memory³.
- Oxygen vacancies are believed to play a very important role in all these applications.

¹B. O'Regan and M. Grätzel, Nature (London) **353**, 737 (1991).

²A. Fujishima and K. Honda, Nature (London) **238**, 37 (1972).

³J. J. Yang, M. D. Pickett, X. Li, D. A. A. Ohlberg, D. R. Stewart, and R. S. Williams, Nature Nanotechnology **3**, 429 (2008).

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Methods – Ground-state properties

Properties that are intrinsic to a system with all its electrons in equilibrium.



- Density functional theory is the “standard model” for understanding **ground-state** properties.
- Total energy is a functional of the charge density.
- Kohn-Sham formulation: Map the interacting many-electron problem to non-interacting electrons moving in a self-consistent field.

$$\left(-\frac{\nabla^2}{2} + V_{\text{ionic}}(\mathbf{r}) + V_{\text{Hartree}}(\mathbf{r}) + V_{\text{xc}}(\mathbf{r}) \right) \psi(\mathbf{r}) = \epsilon \psi(\mathbf{r})$$



Local density approximation
Generalized gradient approximation

Methods – Excited-state properties

Spectroscopic properties that involve experiments creating an excited particle above the ground state.

- Concept and formalism of the **interacting particle Green's function** (G).
- Many-body perturbation theory is the “standard model” for understanding **excited-state** properties.

$$G^{-1} = G_0^{-1} + \Sigma$$

- GW approximation to the self-energy (Σ).


$$\Sigma = \text{diagram} = iGW$$

$$W = \varepsilon^{-1} v$$

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Why are defects challenging?

- Potentially strong electron-electron correlations.
 - Can be open-shell systems.
 - Multiple localized, interacting electrons.
- Lattice relaxation effects.
- Screening from the host.
 - Mimicking the system by isolated cluster may be incorrect.
- Experiments often involve excited-state properties (deep level transient spectroscopy or optical absorption etc.)
- Computational difficulty – isolated defect.

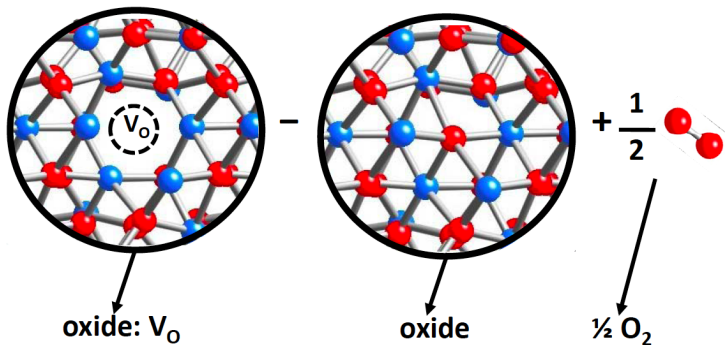
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High- κ dielectric materials – Definitions

Formation energy of an oxygen-vacancy:

$$E^f[\vec{R}] = E[\vec{R}] - E_{\text{ref}} + \frac{1}{2}E_{\text{O}_2}$$

Example: V_{O}



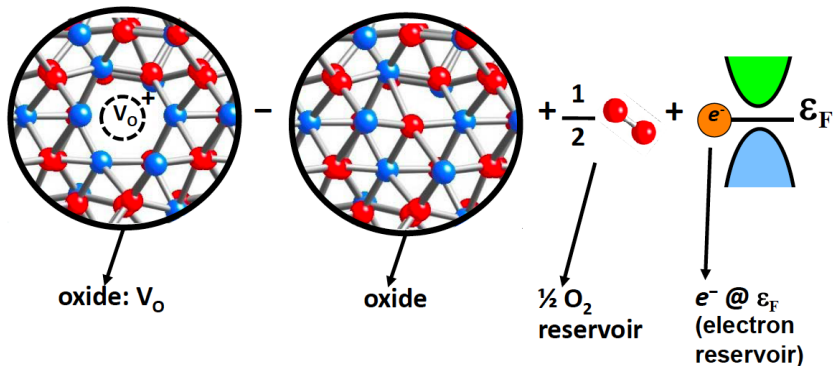
From slides by C. G. Van de Walle

High- κ dielectric materials – Definitions

Formation energy of an oxygen-vacancy:

$$E_q^f[\vec{R}_q](E_F) = E_q[\vec{R}_q] - E_{\text{ref}} + \frac{1}{2}E_{\text{O}_2} + q(E_F + E_v)$$

Example: V_O



Formation energy of an oxygen-related defect in hafnia :

$$E_q^f[\vec{R}_q](E_F) = E_q[\vec{R}_q] - E_{\text{HfO}_2} - n_O \mu_O + q(E_F + E_v)$$

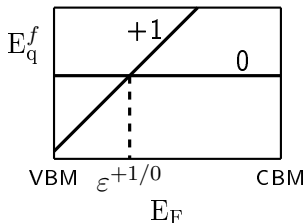
where μ_O is the oxygen chemical potential.

Formation energy of an oxygen-related defect in hafnia :

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Charge transition level : $\varepsilon^{q/q-1} = \text{Fermi energy where defect } q \rightarrow q-1$.



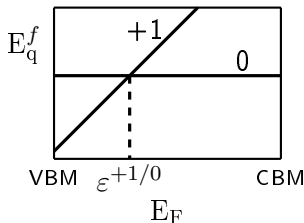
Formation energy of an oxygen-related defect in hafnia :

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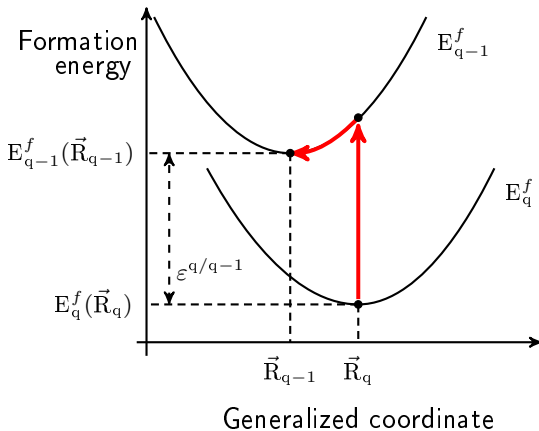
Charge transition level : $\varepsilon^{q/q-1}$ = Fermi energy where defect $q \rightarrow q-1$.

$$= E_{q-1}^f[\vec{R}_{q-1}](E_F = 0) - E_q^f[\vec{R}_q](E_F = 0)$$



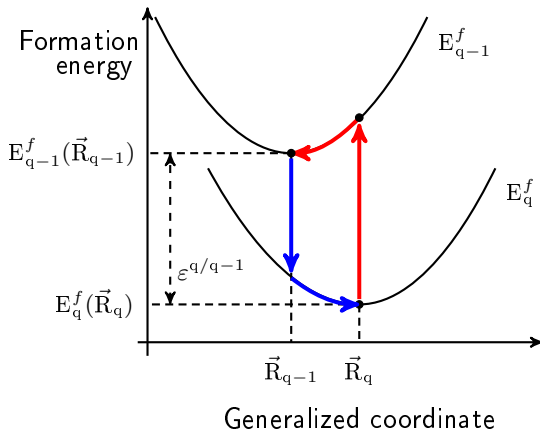
High- κ dielectric materials – Methodology

DFT + GW methodology.



M. Hedström, A. Schindlmayr, G. Schwarz, and M. Scheffler, Phys. Rev. Lett. **97**, 226401 (2006); P. Rinke, A. Janotti, M. Scheffler, and C. G. Van de Walle, Phys. Rev. Lett. **102**, 026402 (2009); M. Jain, J. R. Chelikowsky and S. G. Louie, Phys. Rev. Lett. **107**, 216803 (2011).

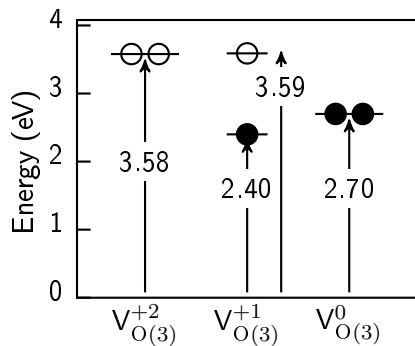
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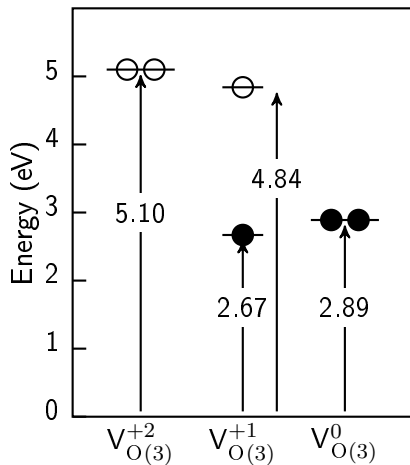
M. Hedström, A. Schindlmayr, G. Schwarz, and M. Scheffler, Phys. Rev. Lett. **97**, 226401 (2006); P. Rinke, A. Janotti, M. Scheffler, and C. G. Van de Walle, Phys. Rev. Lett. **102**, 026402 (2009); M. Jain, J. R. Chelikowsky and S. G. Louie, Phys. Rev. Lett. **107**, 216803 (2011).

- Three fold coordinated ($V_{O(3)}$) and four fold coordinated ($V_{O(4)}$) vacancies in charge states $\{0, +1, +2\}$
- 96 atom super cells.
- Norm conserving pseudopotentials - Hf $5s^25p^65d^26s^2$ and O $2s^22p^4$.
- 250 Ry energy cutoff for wavefunctions.
- PBE functional for structural energies.
- 'One shot' GW done within generalized plasmon pole model done with BerkeleyGW.
- Bulk structural parameters and band gap (6.00 eV) in good agreement with experiment.
- SIESTA for large supercells to get electrostatic corrections.

PBE and quasiparticle level diagram - $V_{O(3)}$



PBE

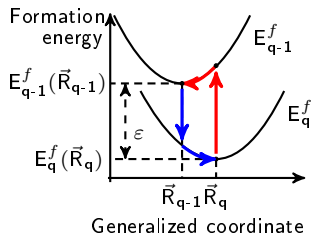


GW

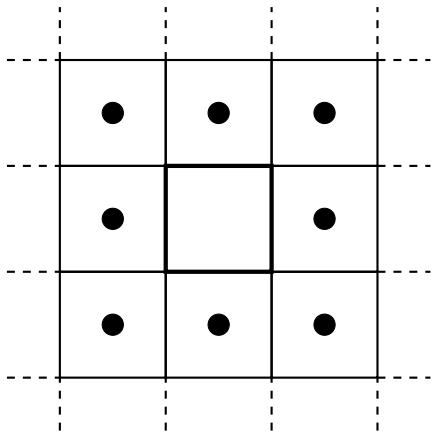
Electrostatic corrections - $V_{O(3)}$

GW charge transition
levels (eV)

$\epsilon^{+2/+1}$	4.50
$\epsilon^{+2/+1}$	3.42
$\epsilon^{+1/0}$	3.55
$\epsilon^{+1/0}$	4.33

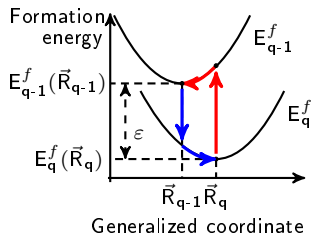


Electrostatic corrections - $V_{O(3)}$



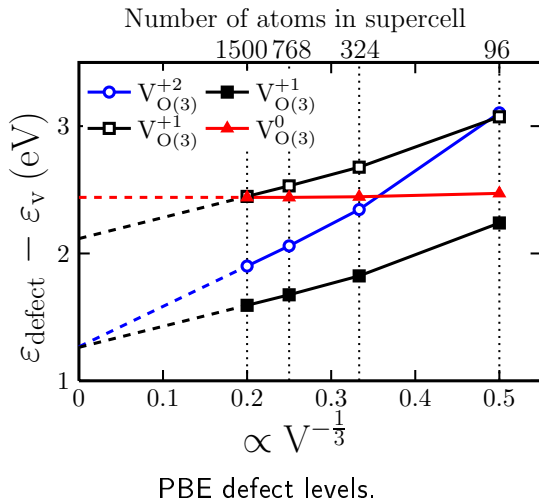
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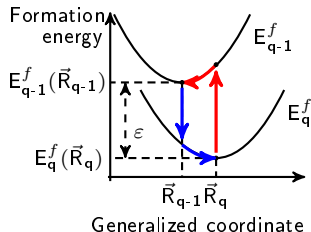
S. Lany and A. Zunger, Phys. Rev. B **81** 113201 (2010)

Electrostatic corrections - $V_{O(3)}$

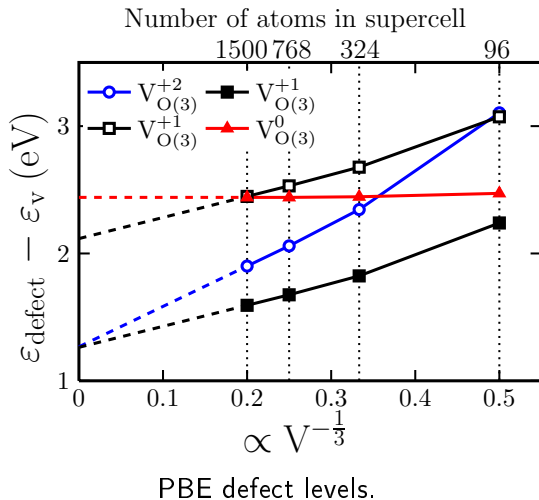


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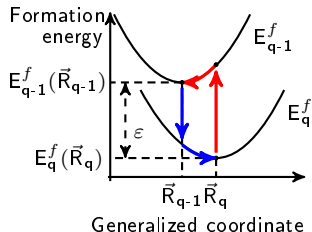


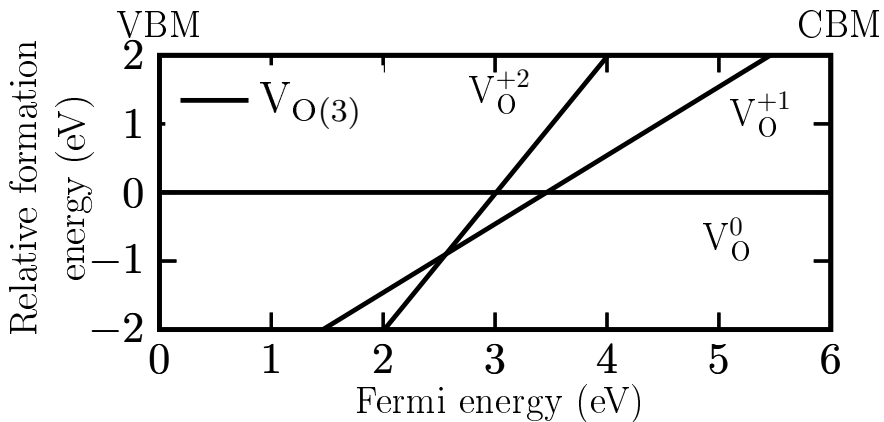
Electrostatic corrections - $V_{O(3)}$

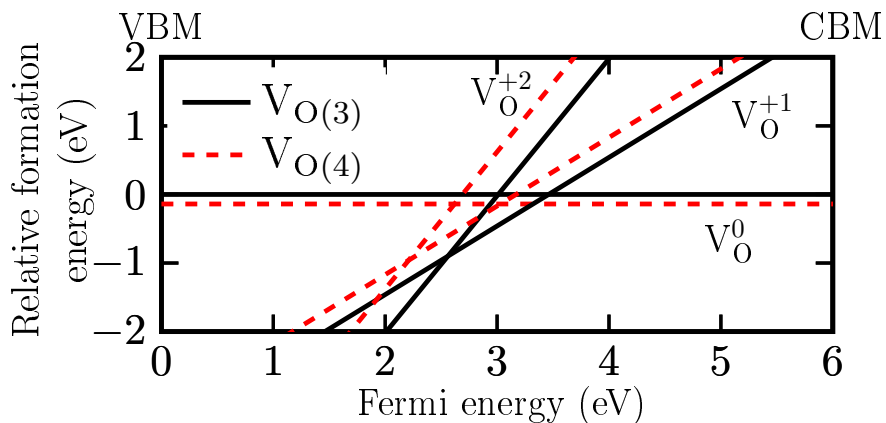


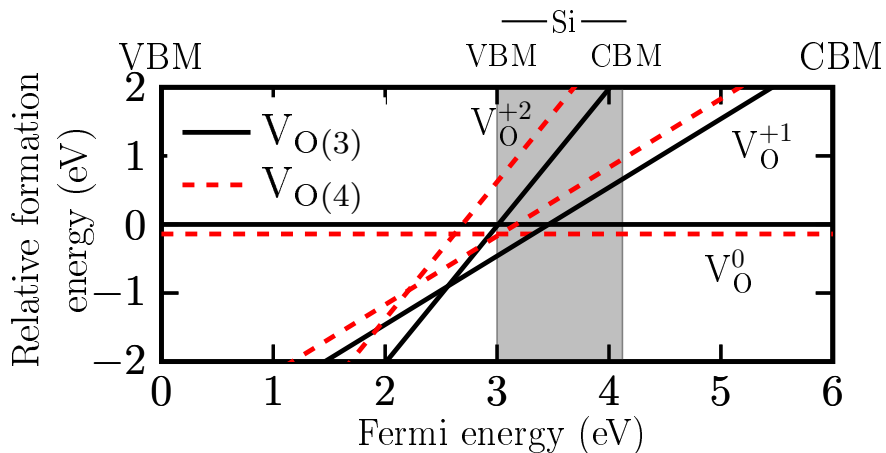
GW charge transition levels (eV)

	w/o cor.	with cor.
$\epsilon^{+2/+1}$	4.50	2.66
$\epsilon^{+2/+1}$	3.42	2.45
$\epsilon^{+1/0}$	3.55	3.55
$\epsilon^{+1/0}$	4.33	3.36

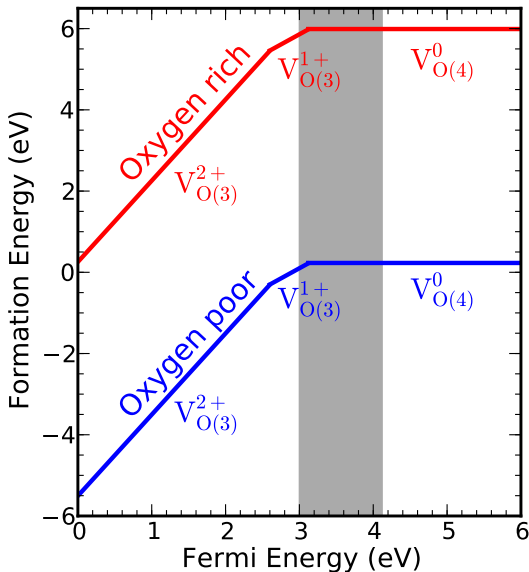








High- κ dielectric materials – Formation energy of vacancies



¹M. Jain, J. R. Chelikowsky and S. G. Louie, Phys. Rev. Lett. **107**, 216803 (2011).

U, defect charging energy, is defined as the energy of the reaction:



$$\begin{aligned} U &= E_{+2}^f(\vec{R}_{+2}) + E_0^f(\vec{R}_0) - 2E_{+1}^f(\vec{R}_{+1}) \\ &= -\varepsilon^{+2/+1} + \varepsilon^{+1/0} \end{aligned}$$

Comparison with previous studies

All values are in eV.

	$V_{O(3)}$			$V_{O(4)}$		
	$\epsilon^{+2/+1}$	$\epsilon^{+1/0}$	U	$\epsilon^{+2/+1}$	$\epsilon^{+1/0}$	U
GGA	2.74	2.69	-0.05	2.38	2.41	-0.03
HSE ¹	3.93	4.42	0.49	—	—	—
PBE0 ²	3.7	4.1	0.4	—	—	—
GW ³ (24 atoms)	4.00	3.10	-0.90	3.22	2.43	-0.79
GW ⁴ (96 atoms)	2.56	3.46	0.90	2.21	3.03	0.82

¹J.L. Lyons, A. Janotti and C.G. Van de Walle, Microelectronic Engineering **88**, 1452 (2011).

²P. Broqvist and A. Pasquarello, Appl. Phys. Lett. **89**, 262904 (2006).

³E.-A. Choi, and K. J. Chang, Appl. Phys. Lett., **94**, 122901 (2009).

⁴M. Jain, J. R. Chelikowsky and S. G. Louie, Phys. Rev. Lett. **107**, 216803 (2011).

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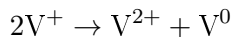
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U, defect charging energy, is defined as the energy of the reaction:



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$$U_{\text{elec}} \geq 0 \text{ and } U_{\text{relax}} \leq 0$$



	U_{elec}	U_{relax}	U
$V_{O(3)}$	2.24	-1.33	0.90
$V_{O(4)}$	2.13	-1.35	0.81

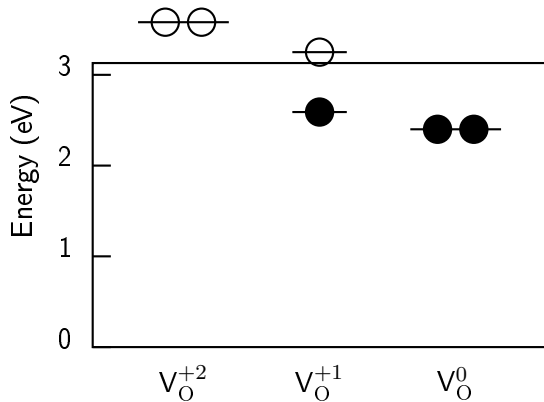
- DFT+GW method for calculating the stability of oxygen vacancies.
- *Qualitative* agreement with previous hybrid functional calculations on the vacancies.
- *Quantitative* disagreement with previous hybrid functional calculations - vacancies near a Si/HfO₂ interface.

	DFT+GW	HSE
V _O	+1,0	+2,+1

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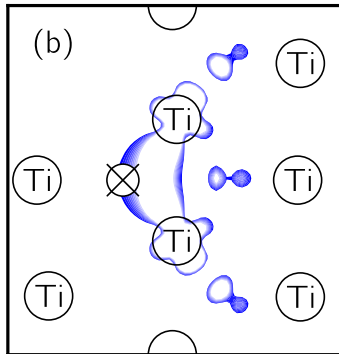
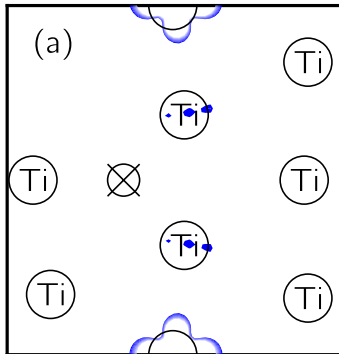
- Oxygen vacancies (V_O) in rutile in charge states $\{0, +1, +2\}$
- 72 atom super cells.
- 200 Ry energy cutoff for wavefunctions.
- HSE functional for structural energies.
- 'One shot' GW done within generalized plasmon pole model done with BerkeleyGW.
- Bulk structural parameters and band gap (3.13 eV) in good agreement with experiment.

Schematic quasiparticle level diagram - V_O



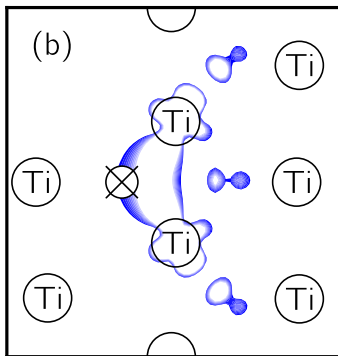
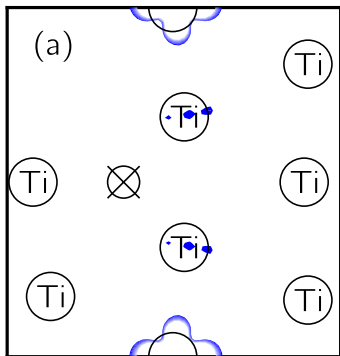
Polaron formation – V_O^{+1}

Relaxation of the atoms : Two minima



Polaron formation – V_O^{+1}

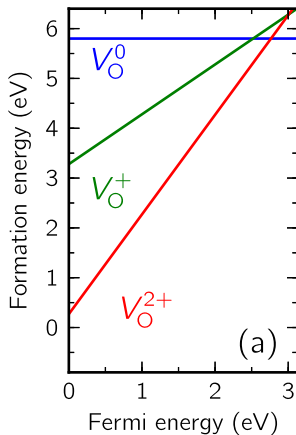
Relaxation of the atoms : Two minima



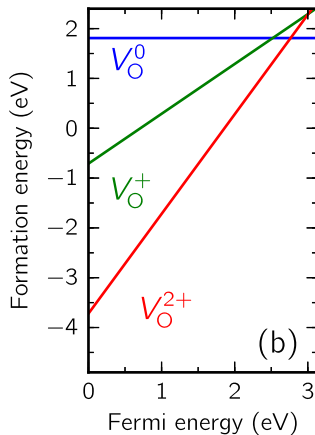
- A state in the gap – polaron.
- $V_O^{+1} \rightarrow V_O^{+2} + \text{polaron}$.
- Lower in energy by 1.2 eV.
- Not relevant for charge transition level

- A state in the gap – defect state.
- Charge density on the defect site.
- Local minima.
- Relevant for charge transition level

TiO₂ – Formation energy of vacancies



Oxygen rich



Titanium rich

Comparison with previous studies

All values are in eV.

	V_O		
	$\epsilon^{+2/+1}$	$\epsilon^{+1/0}$	U
GGA ¹	2.0	2.0	0
HSE ²	3.8	3.1	-0.7
GW ³	3.01	2.56	-0.45

Negative U defect.

¹H. Iddir, S. Ogut, P. Zapol, and N. D. Browning, Phys. Rev. B **75**, 073203 (2007). (value from plot)

²A. Janotti, J. B. Varley, P. Rinke, N. Umezawa, G. Kresse, and C. G. Van de Walle, Phys. Rev. B **81** 085212 (2010). (value from plot)

³A. Malashevich, M. Jain and S. G. Louie, Phys. Rev. B **89**, 075205, (2014).

- DFT+GW method for calculating the stability of oxygen vacancies.
- Negative U defect.
- *Qualitative* agreement with previous hybrid functional calculations.
- *Quantitative* disagreement with previous hybrid functional calculations.

	DFT+GW	HSE
V _O	+2,0	+2

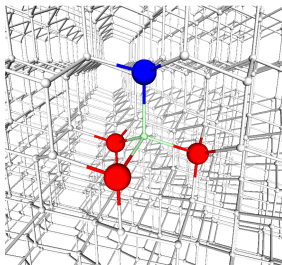
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Defects for spin-qubit applications

- Room temperature individually addressable spin systems in the solid-state for quantum computing.

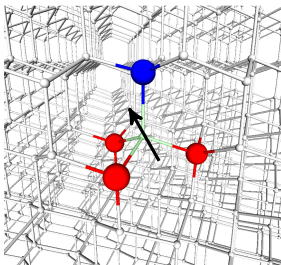
Defects for spin-qubit applications

- Room temperature individually addressable spin systems in the solid-state for quantum computing.
- NV^- center in diamond is the leading candidate.



Defects for spin-qubit applications

- Room temperature individually addressable spin systems in the solid-state for quantum computing.
- NV^- center in diamond is the leading candidate.



- Possible room-temperature qubit with long coherence time ($\sim 1\text{ms}$) for quantum computing.
- High sensitivity, high-spatial resolution magnetometry.

NV⁻ center in diamond – Motivation

Optical initialization at room-temperature provides initial spin pure state for spin-qubit operation.

Notation : $^{2S+1} \Lambda$

Λ : Irreducible representation of the orbital symmetry

S : Total Spin

NV⁻ center in diamond – Motivation

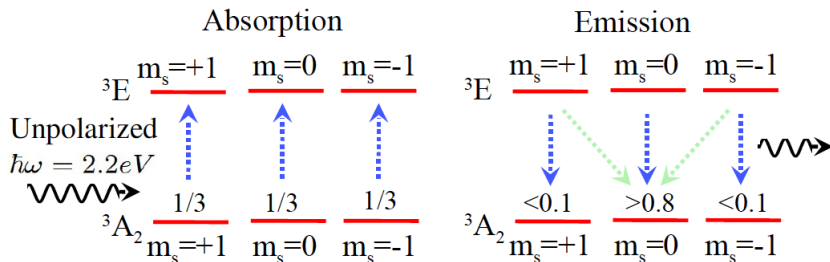
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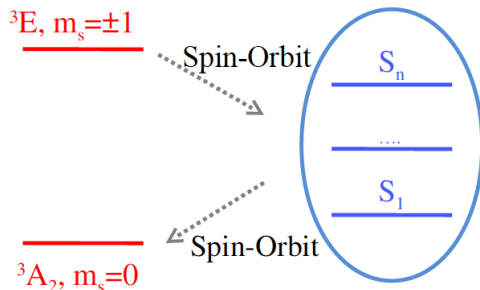
S : Total Spin

At Room Temperature



Degenerate mixed ground state un-entangled spin pure state

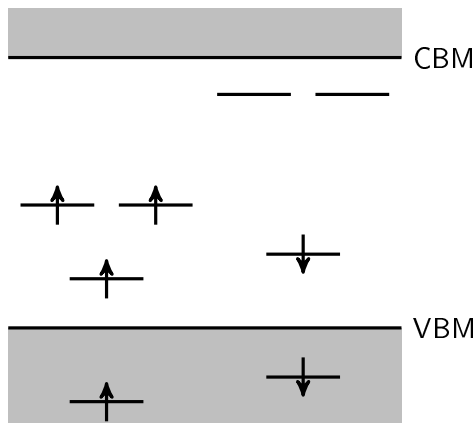
NV⁻ center in diamond – Unsolved problem



- Identification of singlet-level structure.
- Effective optical initialization path between the two triplet levels.

NV⁻ center in diamond – Single particle levels

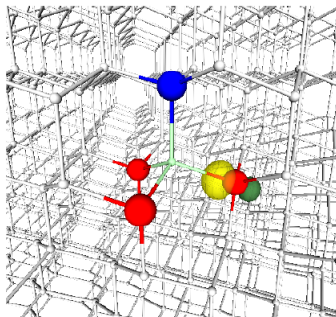
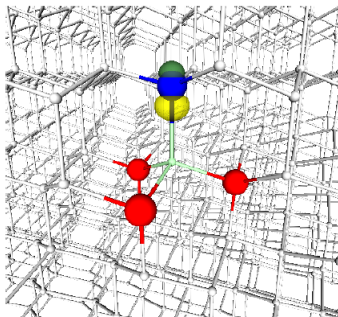
NV⁻ is a deep level center in a band gap of diamond with multiple localized, interacting electrons.



- Open-shell problem¹.
- Correlation due to degenerate ground-states.

¹J. Lischner, J. Deslippe, M. Jain and S. G. Louie, Phys. Rev. Lett. **109**, 036406 (2012)

NV⁻ center in diamond – Dangling orbitals



● N
● C
● V

8 dangling spin-orbitals
in and near band-gap of
diamond



Good basis for low energy
excitations.

NV⁻ center in diamond – Extended Hubbard model

$$\hat{H} = \sum_{i,\sigma} E_i n_{i\sigma} + \sum_{i \neq j, \sigma} t_{i,j} c_{i,\sigma}^\dagger c_{j,\sigma} \\ + \sum_i U n_{i,\uparrow} n_{i,\downarrow} + \sum_{i \neq j, \sigma, \sigma'} V n_{i,\sigma} n_{j,\sigma'}$$

i, j : Atomic sites (C or N)

σ, σ' : Spin direction

E_i : On-site energy

$t_{i,j}$: Hopping integral

U : On-site Coulomb repulsion

V : Nearest neighbor

Coulomb repulsion

Effective Coulomb
interaction parameters

Strong electron-electron
correlation

Screening from diamond

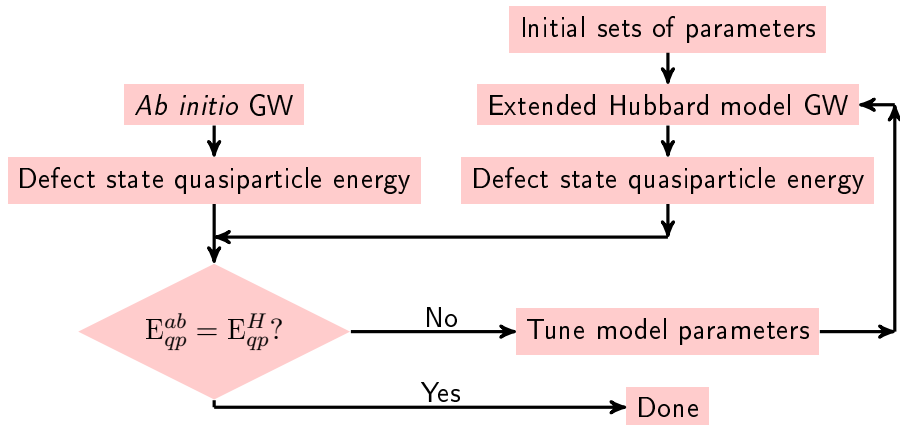
Geometry dependent
parameter sets

Large structural relaxation

Hindered by the difficulty in getting physically grounded model parameters.

NV⁻ center in diamond – Model parameters from GW

Use *ab initio* GW to get model parameters, incorporating realistic electron-electron interactions.



NV⁻ center in diamond – Model parameters from GW

- $U/t > 3 \rightarrow$ strongly correlated system.
- Reasonable values of parameters.
- Geometry dependent parameters.

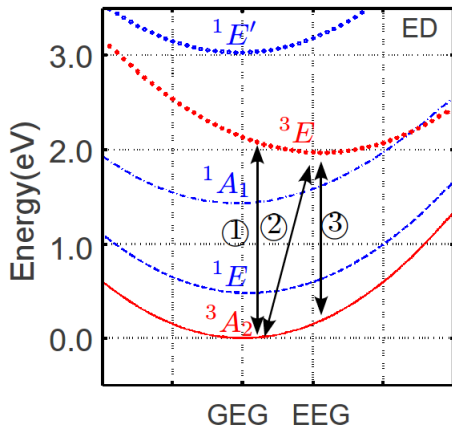
All parameters are in eV.

	$E_C - E_N$	t_{NC}	t_{CC}	U	V
Ground-state	2.56	-0.68	-1.03	3.43	0.83
Excited-state	2.86	-0.75	-0.90	3.45	0.67

NV⁻ center in diamond – Level diagram

Level diagram¹ from exact diagonalization of model Hamiltonian
– all many-electron correlation effects within our Hilbert space.

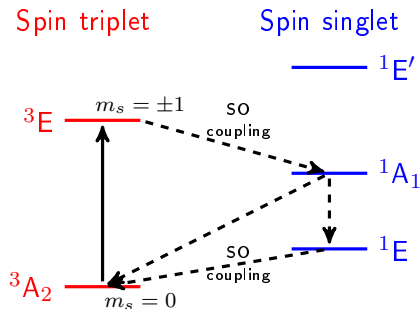
All energies in eV.



	Theory	Exp
$\textcircled{1}$	2.1	2.2
$\textcircled{2}$	2.0	1.945
$\textcircled{3}$	1.8	1.8
τ_{rad}^{3E}	20ns	13ns
τ_{nonrad}^{3E}	30ns	50ns

¹S. Choi, M. Jain and S. G. Louie, Phys. Rev. B **86**, 041202 (2012)

NV⁻ center in diamond – Proposed optical pathway¹



Qualitatively and quantitatively consistent with available experimental data.

¹S. Choi, M. Jain and S. G. Louie, Phys. Rev. B **86**, 041202 (2012)

- Constructed extended Hubbard Hamiltonian from *ab initio* GW calculations.
- Through exact diagonalization, many-electron effects strongly affect the energy level diagram qualitatively and quantitatively.
- Computed ground- and excited-state energy surfaces and transition rates between them provided a consistent picture with experiments.
- Proposed an optical initialization pathway in which inter-system crossing plays a crucial role.

- *Ab initio* methods to understand and predict properties of defects in materials.
- Oxygen vacancies in high- κ material – HfO_2 and photocatalytic material – TiO_2 .
- NV^- center in diamond for quantum computing application.

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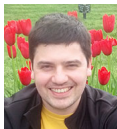
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