Phonon Related Phenomena in Materials

Umesh V. Waghmare
Theoretical Sciences Unit
also at Centre for Computational Materials Science
Jawaharlal Nehru Centre for Advanced Scientific Research,
Bangalore 560 064

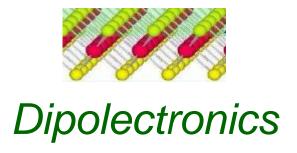
http://www.jncasr.ac.in/waghmare http://www.jncasr.ac.in/ccms waghmare_AT_jncasr.ac.in

Funded by Dept of Sci. and Tech., Dept of Atomic Energy Govt of India

Why Phonons?

- Fingerprint of a material: Raman, IR spectra
- Thermodynamic stability: vibrational entropy T, soft modes
- Properties: elastic, dielectric, piezoelectric, etc (couple with fields)
- Structural Transitions: instabilities of a structure $w \rightarrow 0$
- Phonons coupled with electrons, spin, exciton, polarons; e.g. superconductivity

Emergence of Ferroelectricity at a Metal-Semiconductor Transition in a 1T Monolayer of MoS₂



Sharmila N Shirodkar, Anjali Singh & UVW

Theoretical Sciences Unit

J Nehru Centre for Advanced Scientific Research, Bangalore 560 064 www.jncasr.ac.in/waghmare

JNCASR

Funding from DST and DAE, Government of India

Collaborators

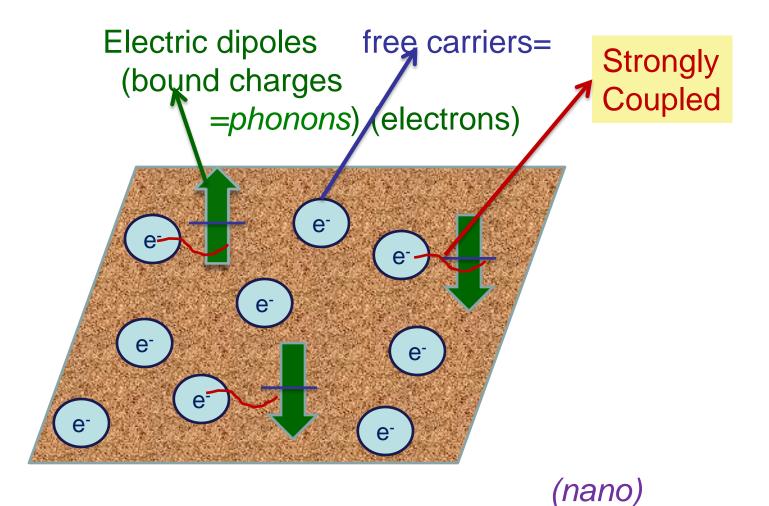
- Sharmila N Shirodkar (JNCASR)
- Anjali Singh (JNCASR)

Experiments and Stimulating Collaborations:

- CNR Rao and Group (JNCASR)
- Ajay K Sood and Group (IISc)

Take-Home Message: 1T MoS₂

Ferroelectric Semiconductor

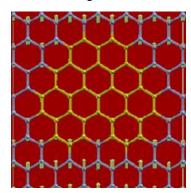


Propose new class of devices: Dipolectronics

S N Shirodkar and U V Waghmare, Phys Rev Lett. 112, 157601 (2014).

2-D Nano-materials

- Graphene: High mobility, Low on/off ratio
- BN: A good insulator, too low mobility
- $C_x(BN)_{1-x}$: Domains of BN vs disorder VRH conduction



MoS₂: Intermediate gap, good on/off ratio

Holds promise for nano-electronic applications

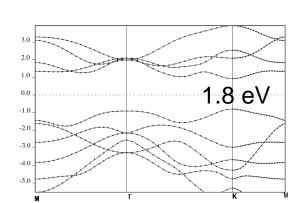
Massive Dirac Fermionic nature Spin split bands

FET: Kis et al, Nature Nano 6, 107601 (2011)

FET based Sensors:

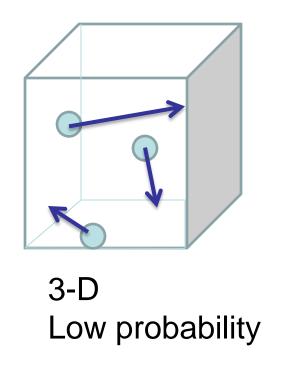
Rao, Dravid, UVW et al ACS Nano (2013)

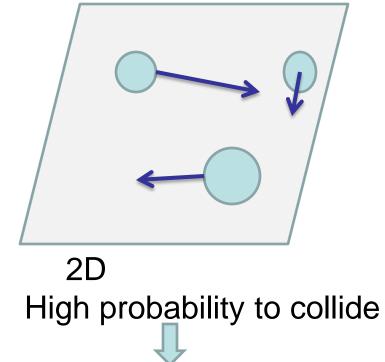
Frontier: Rao, Maitra and UVW, CPL (2014)



Electron-phonon Coupling

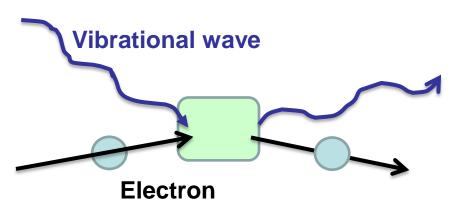
Low Dimensionality:





- Coupling between degrees of freedom is more readily possible
- Such coupling can have more drastic consequences
- Sensitivity to external Fields:
 As long as the symmetry allows it!

Electron-phonon Coupling

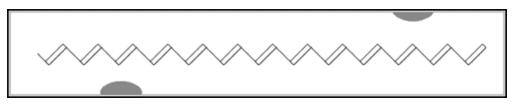


Examples in Low-dimensional Systems

Bredas et al, Acc Chem Res 18, 305 (1985)

Polarons:

Conducting Polymers



www.nobelprize.org

Z X Shen et al, Phys Rev Lett 110, 265502 (2013).

Quasi-1D cuprates:

"Our results indicate that the lattice degrees of freedom are fully integrated into the electronic behavior in low-dimensional systems."

Electron-Phonon Coupling (EPC) in Graphene

EPC results in changes in phonon frequencies

with doping:

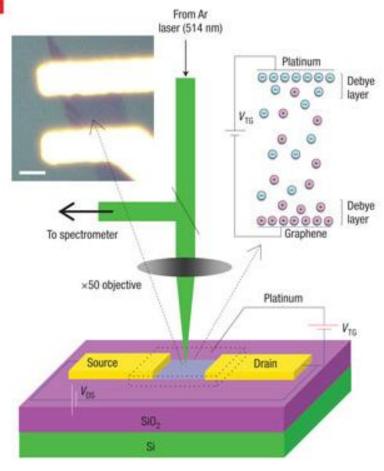
key to use of Raman for characterization of devices

Sood et al, Nat Nanotech. (2008).

Electric Field Effect Tuning of EPC in graphene:

Gate voltage changes w of G-band

Pinczuk et al, Phys Rev Lett. (2008).

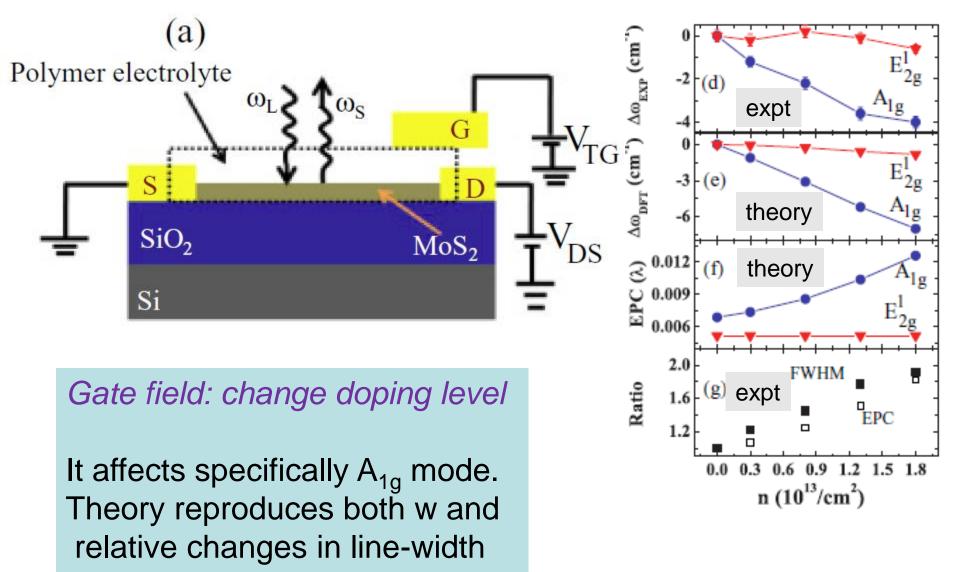


Breakdown of Born-Oppenheimer Approximation!

Motion of e and phonon can not be decoupled

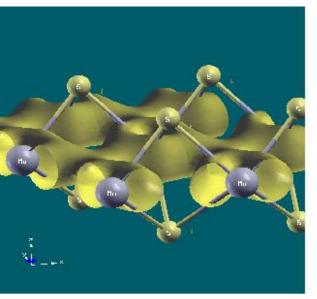
Pisana et al, Nat Mat. (2007).

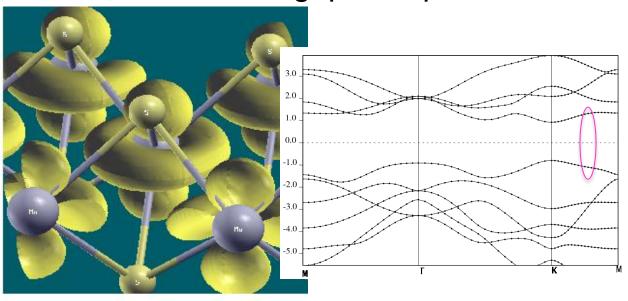
Electron-Phonon Coupling (EPC) in MoS₂

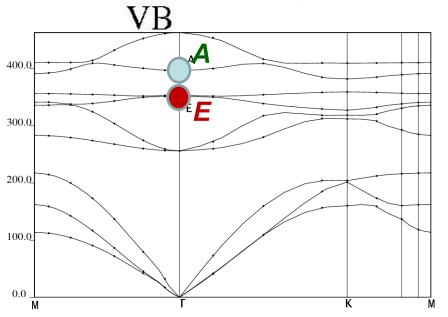


Chakraborty, Bera, Muthu, Bhowmick, Waghmare and Sood, Phys Rev B 85, *R* 161403 (2012) Editor's Suggestion.

Large Coupling of A_{1g} Mode with Electrons States on the two sides of band gap at K-point







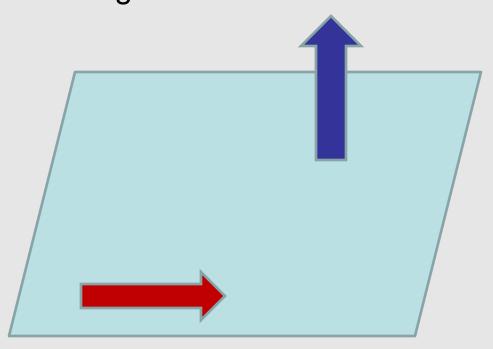
CB Sood et al, Phys Rev B 85, R 161403 (12

CB: Full symmetry of the system (A_{1g} representation) only $< A_{1q} | \Delta V(A_{1q}) | A_{1q} > \neq 0!$

Symmetry dependent phonon renormalization

Raman: Characterization of FET

So far, effect of \perp electric field on 2-D materials has been investigated.



What if the field is *in-plane*?

- → Metallic 2-D materials will just conduct!
- → Semiconducting ones may do something interesting!

Tunability of Electron-phonon Coupling with In-plane Electric Field

→ Electro-resistance, polarons

A generic property of the 2-D materials

Tuning EPC with Electric Field

Electron-phonon coupling matrix element

$$\lambda_{qv} = \frac{2}{\hbar \omega_{qv} N(\epsilon_f)} \sum_{k} \sum_{mn} |g_{k+q,k}^{qv,ij}|^2 \times \delta(\epsilon_{k+q,i} - \epsilon_f)$$

$$\times \delta(\epsilon_{k,j} - \epsilon_f).$$
Density of States

 E_{\perp} changes doping, ϵ_{F} , the occupation numbers: DoS

We show that the *in-plane E* changes the matrix element (for q=0):

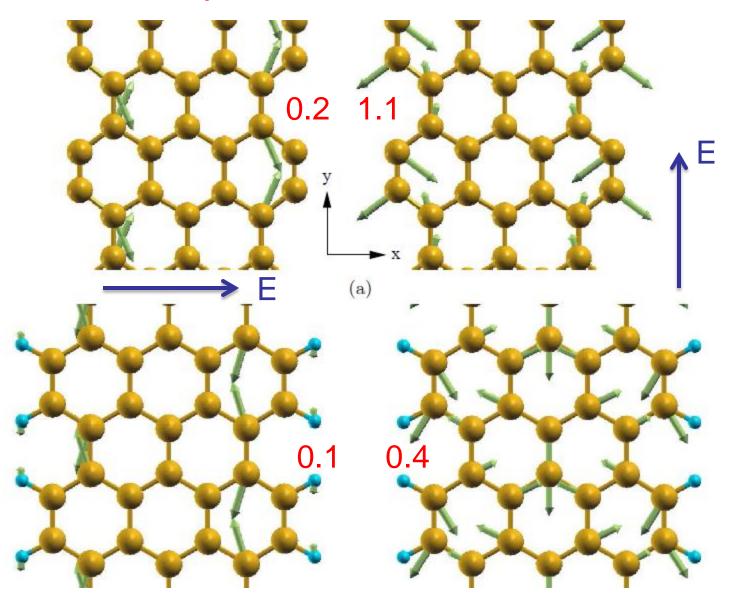
$$g_{k+q,k}^{qv,ij} = \left(\frac{\hbar}{2M\omega_{qv}}\right)^{\frac{1}{2}} \langle \underline{\psi_{k+q,i}} | \Delta V_{qv} | \underline{\psi_{k,j}} \rangle,$$
 Expand series in E

$$\langle k, m\sigma | \nabla_{\mathbf{R}_n} V_{el-i} | k, n\sigma \rangle + E Z_{n,\alpha,\beta}(k,n) \delta_{m,n}$$
 Force

Tunability Parameter

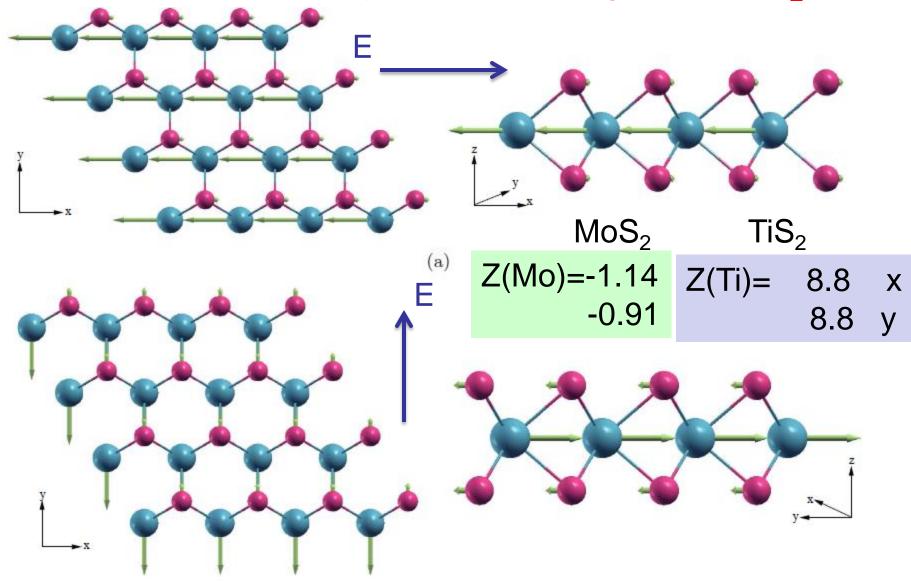
CHARGE: Force on an atom by E

Graphene Nano-ribbons



States localized on edges, force felt by the ions there!

EPC(E): Dynamical Charges in MoS₂

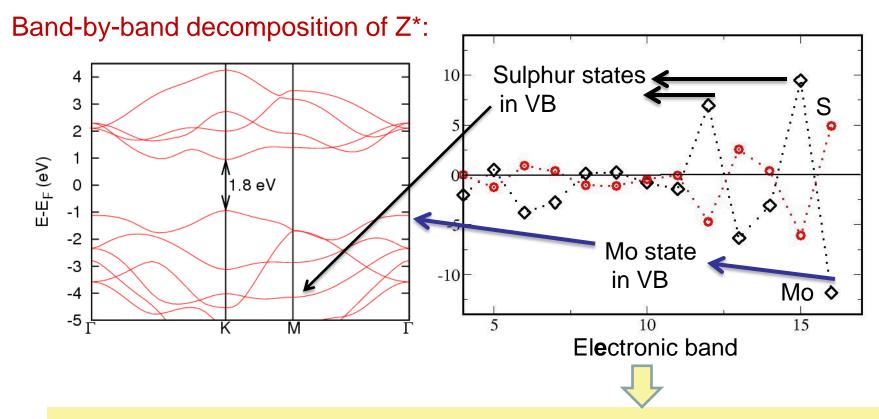


Anomaly: even the sign of charge is counter-intuitive!

Tunability of EPC (MoS₂) with in-plane electric field

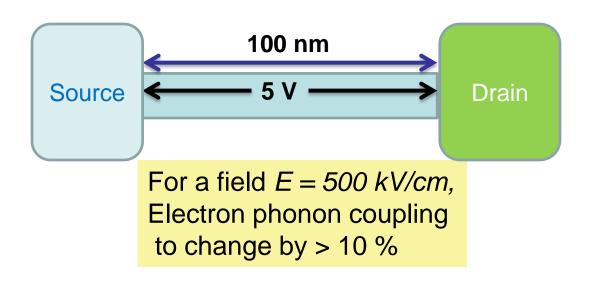
Anomalous dynamical charges:

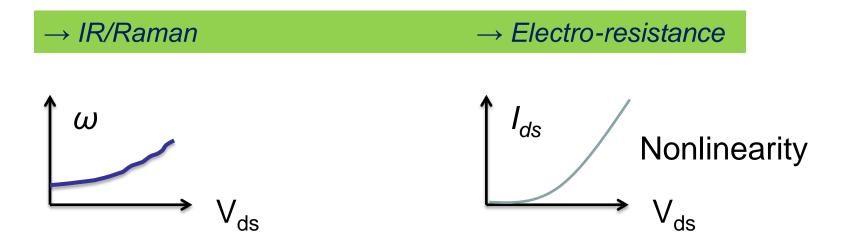
 $Z^*(Mo) = -0.8$ to -1.0, depending on the method used $Z^*(S) = 0.4$ to 0.5!



Coupling of top of the valence and bottom of the conduction e states with *Phonons* most tunable with electric field!

Predictions for experiments (MoS₂)





So far, we find in 2H MoS₂:

- Strong electron phonon coupling (EPC)
- Strong dependence of EPC on electric field
- Highly anomalous dynamical charges
 Waghmare, Kandpal, Spaldin and Seshadri, PRB (2003).
 - ► Tendency of a material to turn metallic
 - ► Tendency to be ferroelectric

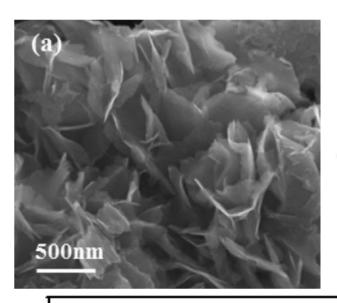
The usual 2H form of MoS₂:

not a good candidate (is non-centrosymmetric, but P=0, because of other symmetries)

► Is there a metallic state in *the s*tructural neighborhood?

Prof. Rao's experiments gave us a hint!

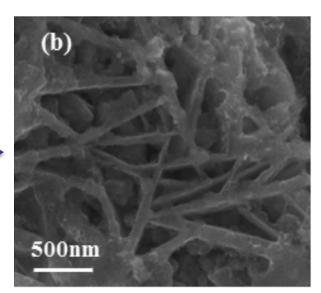
Ironing out MoS₂ or MoSe₂

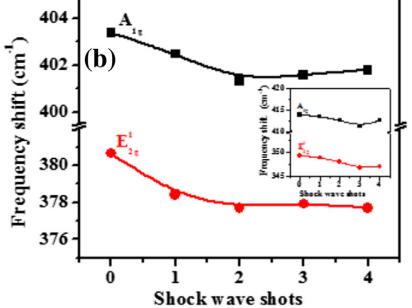


MoSe₂

High T
Shock Waves

Reduction in d (interplaner spacing)





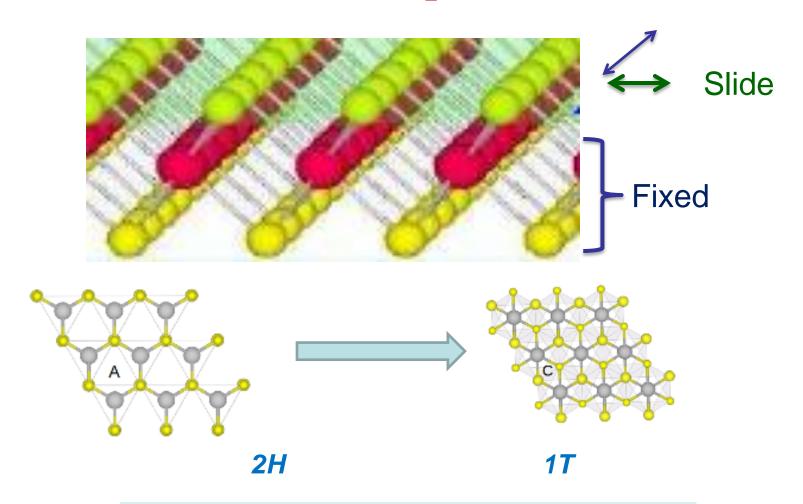
CNR Rao et al, Chem Phys Lett 582, 105 (2013)

Two-stage mechanism:

- (i) Flattening of sheets through shear+uniaxial strains
- (ii) Mainly compression along caxis

SHEAR STRAIN within a Monolayer

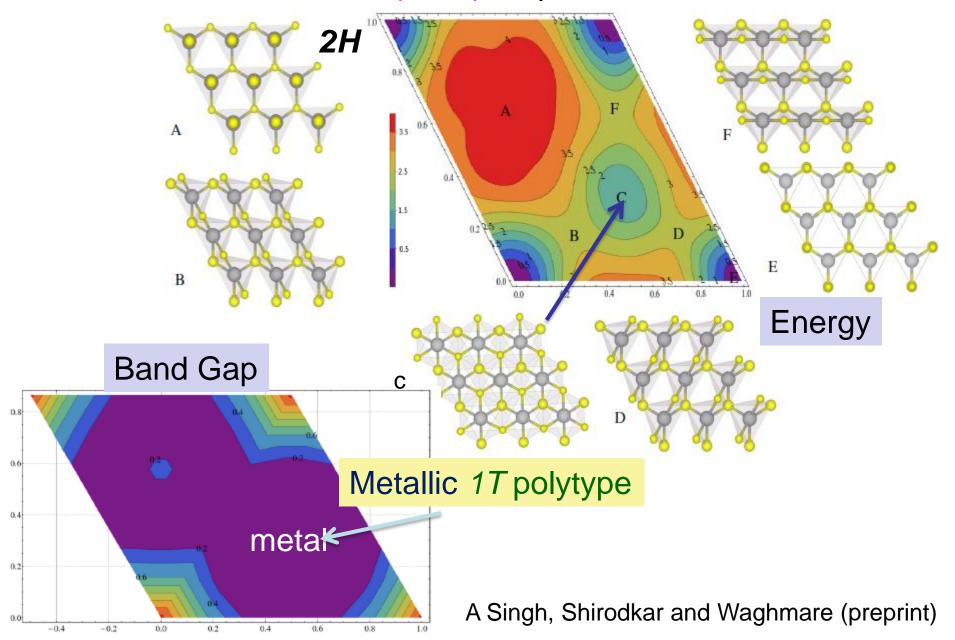
Shearing MX₂ sheets

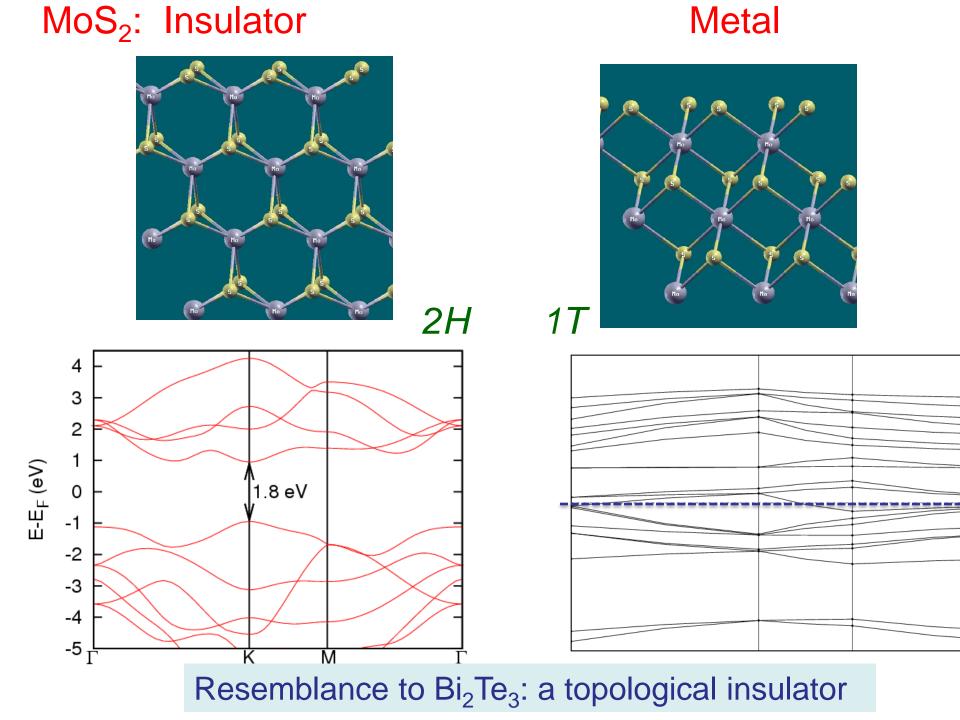


What is the energetics? How does the band-gap change?

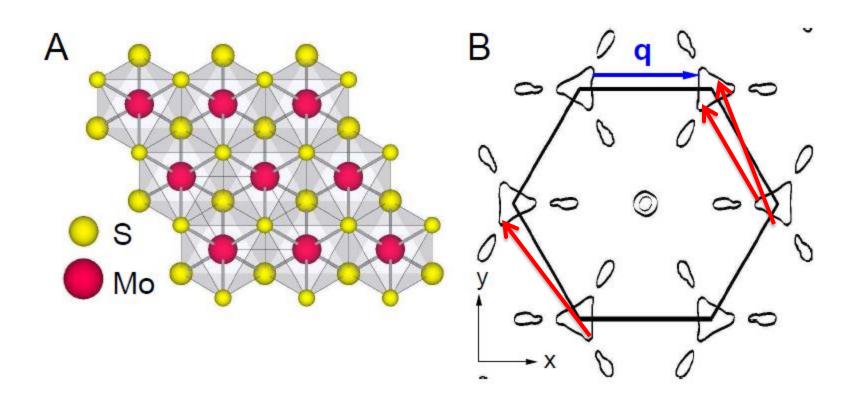
MoS₂ monolayer:

Generalized shear strain (SLIP) response





Structure of the 17 Polymorph of MoS₂



- Structure is Centro-symmetric
- Fermi surface is weakly nested by q-vectors that form an equilateral triangle centred at K

"Average nesting" by K: instability

Charge Density WaveLattice Wave: Phonon

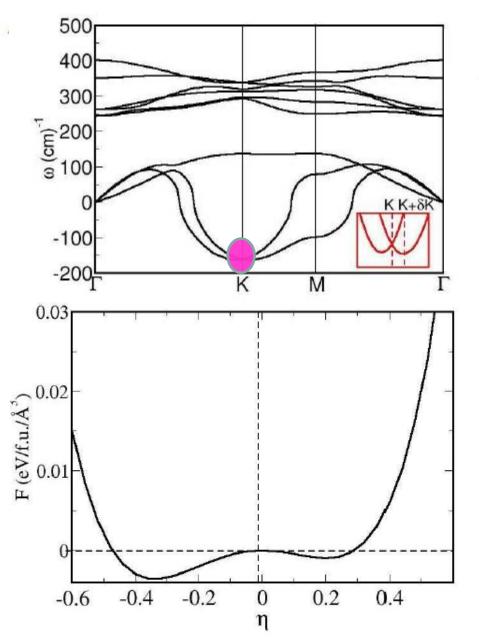
Fermi Surface Nesting:

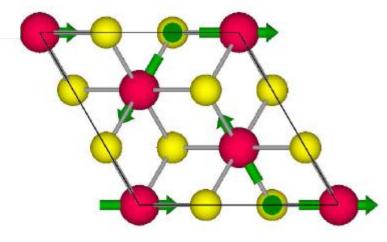
Many electronic states on the Fermi-surface can be scattered by a phonon with nesting wave vector to other states on the Fermi-surface

Structure is unstable:

Perturbation with that phonon drives the structure to lower energy!

Cell-tripling Structural Instability



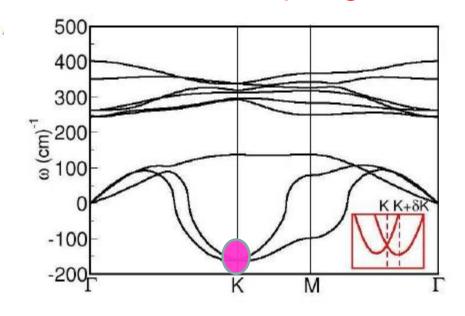


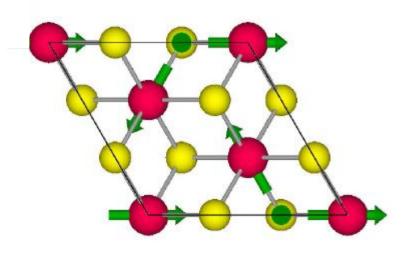
Strongest instability at *K*:

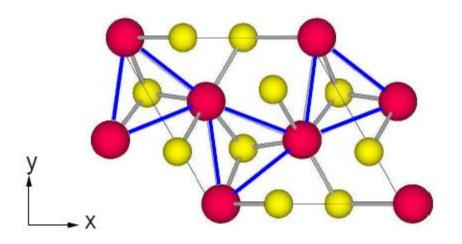
distortion of the structure leads to lower energy "stable" structure

Mo-trimerization

Cell-tripling Structural Instability



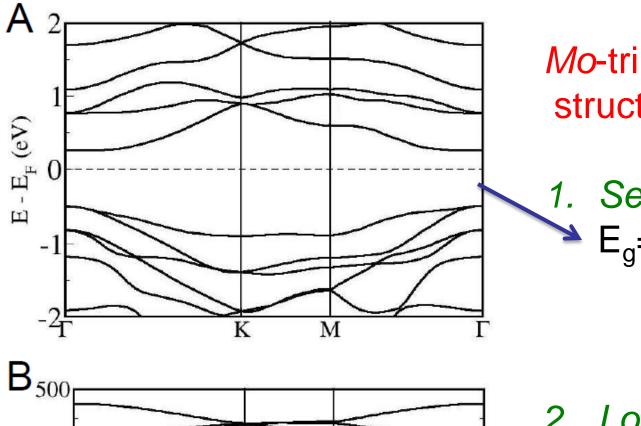




Strongest instability at *K*

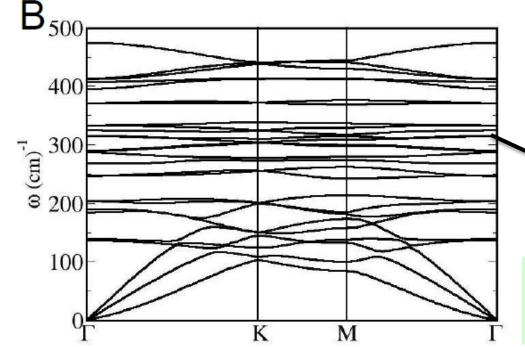
Leads to Mo-trimerization

What happens to Electronic Structure?



Mo-trimerized structure (*d1T*):

Semiconducting
 E_g=0.7 eV

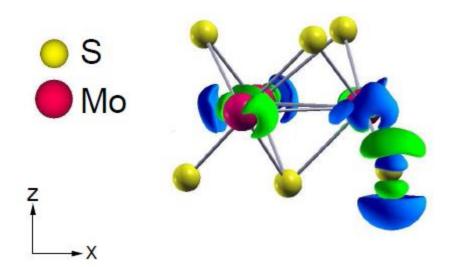


2. Locally stable:

 phonon dispersion
 Raman Sign A_{1g}
 mode at 321 cm⁻¹

What happens to inversion symmetry?

Broken inversion symmetry: Difference density d1T-c1T



K: zone boundary point periodic modulation

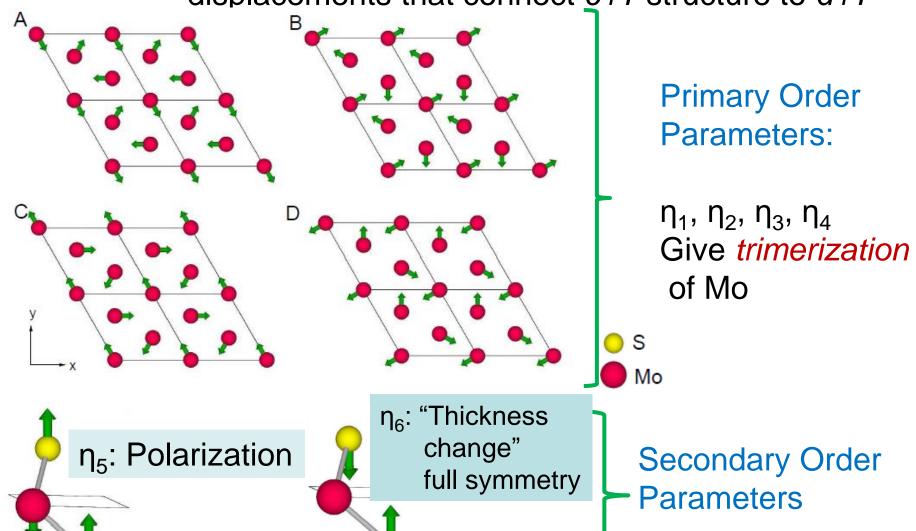
Can *not* give a uniform polarization

Berry phase calculation: P=0.28 µC/cm²

Puzzle: Where does the polarization come from?

Symmetry Analysis: Landau Theory

Order Parameters: Symmetry invariant subspace of atomic displacements that connect <u>c1T</u> structure to <u>d1T</u>



Landau Theory: Free Energy of Structural Distortions

$$\begin{split} F &= g_{12} \; (\eta_1^2 + \eta_2^2 + \eta_3^2 + \eta_4^2) + g_{22} \; \eta_5^2 \\ &+ g_{13} \; (\eta_1^3 - 3 \; \eta_1 \; \eta_2^2 + \eta_3^3 - 3 \; \eta_3 \; \eta_4^2) + g_{23} \; \eta_5 (\eta_1^2 + \eta_2^2 - \eta_3^2 - \eta_4^2) \\ &+ g_{14} \; [(\eta_1^2 + \eta_2^2)^2 + (\eta_2^2 + \eta_3^2)^2 + (\eta_3^2 + \eta_4^2)^2 + (\eta_4^2 + \eta_1^2)^2 + (\eta_3^2 + \eta_1^2)^2 + (\eta_4^2 + \eta_2^2)^2 \\ &- 2\eta_1^4 - 2\eta_2^4 - 2\eta_3^4 - 2\eta_4^4] \\ &+ g_{24} \; [(\eta_1^2 + \eta_2^2)^2 + (\eta_3^2 + \eta_4^2)^2] \end{split}$$
 Cubic term: 1st order transition

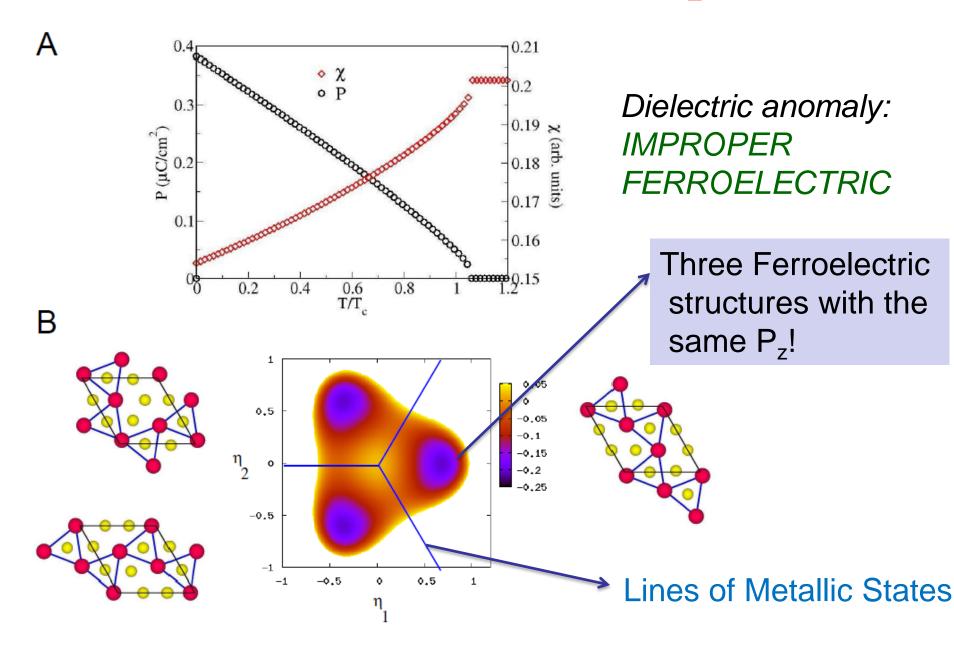
$$+ g_{34} \eta_5(\eta_1^3 - 3 \eta_1 \eta_2^2 + \eta_3^3 - 3 \eta_3 \eta_4^2)$$
 - Nonlinear Coupling

+
$$g_{44} \eta_5^2 (\eta_1^2 + \eta_2^2 + \eta_3^2 + \eta_4^2) + g_{54} \eta_5^4$$
.

Polarization induced as a *quadratic* function of Mo-trimerization:

P
$$\alpha$$
 $\eta_5 = -\frac{g_{23}}{2g_{22}}\eta_1^2$

Ferroelectricity in MoS₂



Our first-principles theoretical prediction:

17-MoS₂ (with no electrodes):

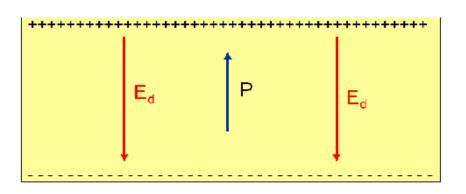
The world's thinnest known ferroelectric!

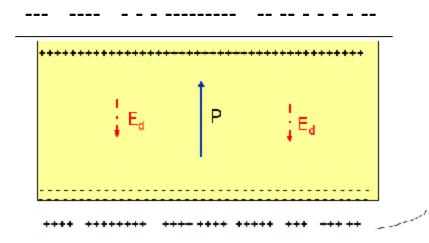
~ 0.6 nm

Other World Records (with electrodes):

1.0 nm: Polymer [PVDF] Bune et al, Nature 391, 874 (1998)

1.2 nm: PbTiO₃ Fong et al, Science 304, 1650 (2004).





1T MoS₂: 2D Ferroelectric Semiconductor

Electric dipole perpendicular to plane: Bound charges, phonons

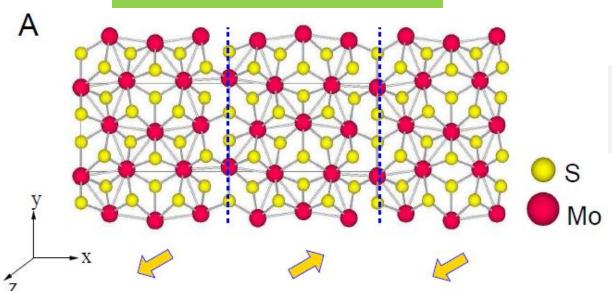
Electrical transport in-plane: Free carriers

The two are strongly coupled!

Can we exploit this to make novel devices?

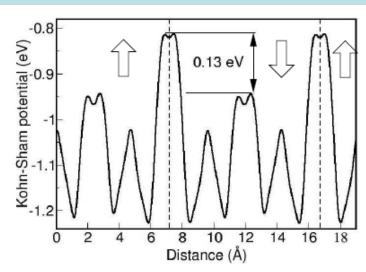
Ferroelectric Domains





Domain Wall Energy of 7.7 mJ/m²

Potential Energy Barrier at Domain Wall

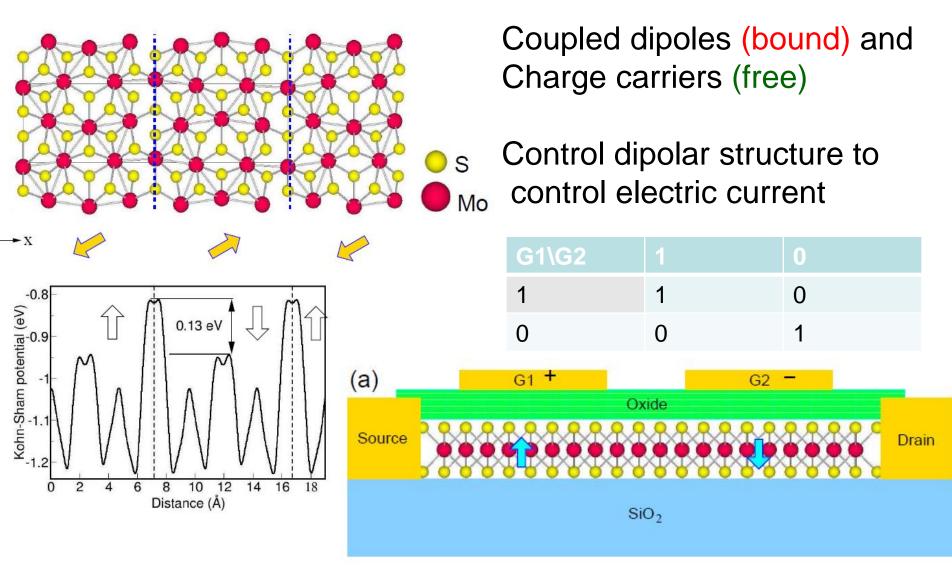


Domain Wall Energy Barrier of 0.13 eV:

Polarization switching:

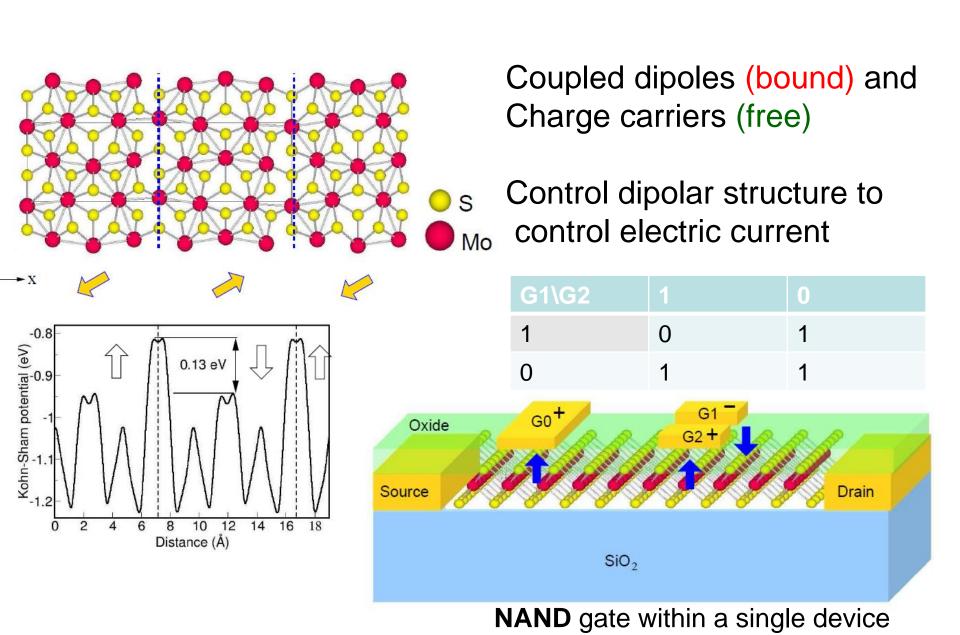
Consequences to transport

Dipolectronic Devices based on MoS₂

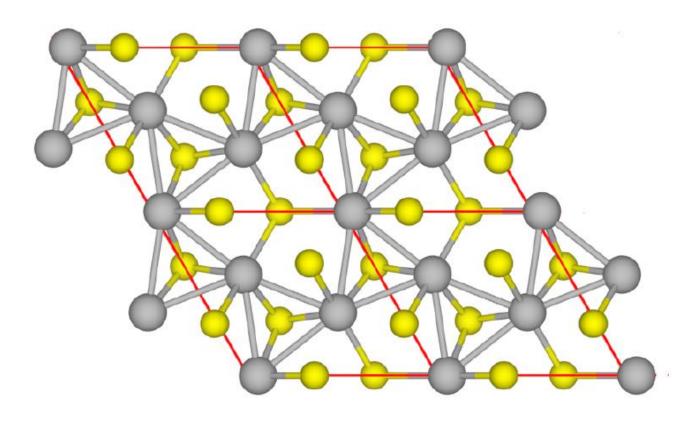


XNOR gate within a single device

Dipolectronic Devices based on MoS₂



Symmetry Analysis, Ferroelectricity are generic to 1T polytype of (Mo,W)(S,Se)₂



Polarization ~ 0.25-0.28 µC/cm²

But only MoS₂ has the stable domains and is usable!

Summary

Strong electron-phonon coupling and its tunability with Electric Field: generic to 2-D nanomaterials

Theoretical Demonstration of

Emergence of 2-D ferroelectricity at an MIT

in 1T-(Mo,W)(Se,S)₂

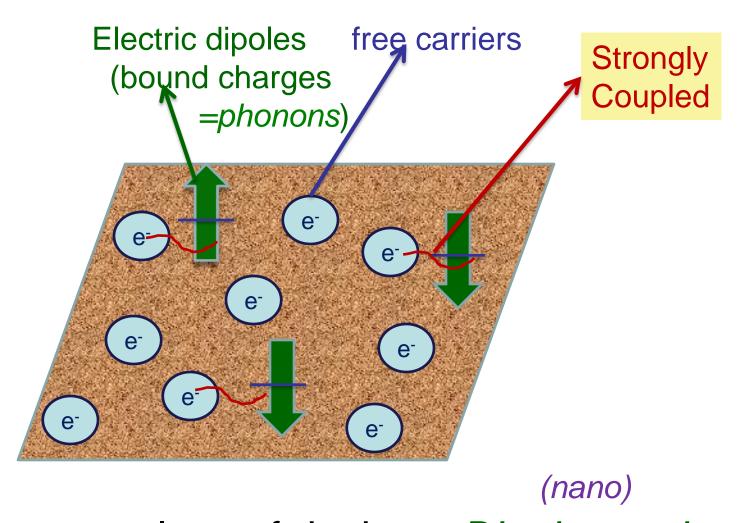
Origin: electron-phonon coupling



Dipolelectronic Devices

Take-Home Message: 1T MoS₂

Ferroelectric Semiconductor



Propose new class of devices: Dipolectronics

Why Phonons?

- Fingerprint of a material: Raman, IR spectra
- Thermodynamic stability: vibrational entropy T, soft modes
- Properties: elastic, dielectric, piezoelectric, etc (couple with fields)
- Structural Transitions: instabilities of a structure $w \rightarrow 0$
- Phonons coupled with electrons, spin, exciton, polarons; e.g. superconductivity

SiC

SiC: a promising technological material both as a bulk and at nano-scale

(see a review by Melinon et al, Nature Materials 6, 479 (2007)).

Bulk SiC: mechanical hardness, optical properties (large band gap), bio-compatibility, high-temperature stability, chemical inertness, shock resistant, high refractive index

Stacking (eg. ABCAB...) of crystal planes (polytypes) tune properties

1950: Shockley predicted SiC would replace Si

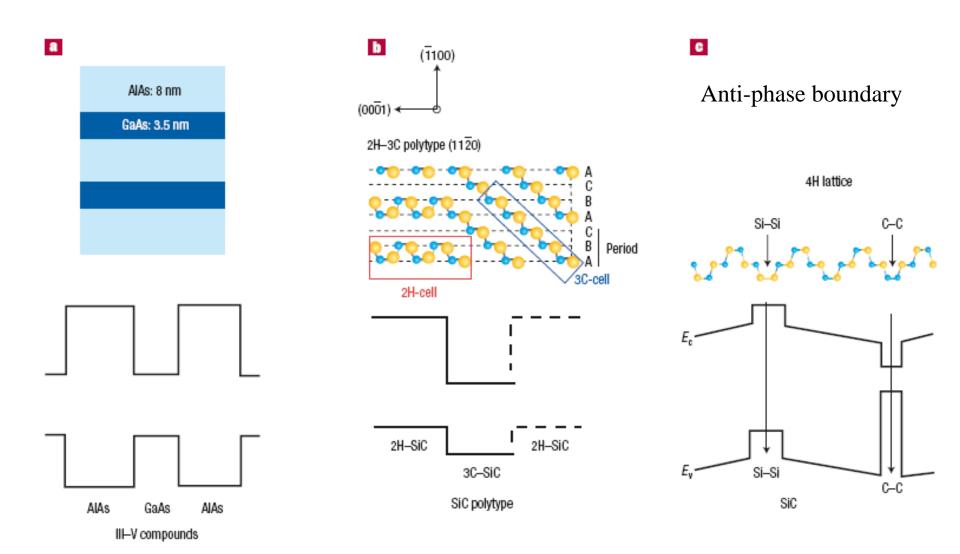
Many applications from power electronics to catalysis

Nano-form of SiC: Atomic engineering of nano-structures to tune properties

Clusters,

Nano-wires, nano-tubes,

43



(From Nature Mat. 6, 479 (2007)).

Ultrahigh-quality silicon carbide single crystals

Daisuke Nakamura¹, Itaru Gunjishima¹, Satoshi Yamaguchi¹, Tadashi Ito¹, Atsuto Okamoto¹, Hiroyuki Kondo², Shoichi Onda² & Kazumasa Takatori¹

¹Toyota Central R&D Laboratories, Inc., Nagakute, Aichi, 480-1192, Japan
²Research Laboratories, DENSO Corporation, 500-1, Nissin, Aichi, 470-0111, Japan

Silicon carbide (SiC) has a range of useful physical, mechanical and electronic properties that make it a promising material for next-generation electronic devices1,2. Careful consideration of the thermal conditions³⁻⁶ in which SiC {0001} is grown has resulted in improvements in crystal diameter and quality: the quantity of macroscopic defects such as hollow core dislocations (micropipes)⁷⁻⁹, inclusions, small-angle boundaries and longrange lattice warp has been reduced^{10,11}. But some macroscopic defects (about 1-10 cm⁻²) and a large density of elementary dislocations (~10⁴ cm⁻²), such as edge, basal plane and screw dislocations, remain within the crystal, and have so far prevented the realization of high-efficiency, reliable electronic devices in SiC (refs 12-16). Here we report a method, inspired by the dislocation structure of SiC grown perpendicular to the c-axis (a-face growth)¹⁷, to reduce the number of dislocations in SiC single crystals by two to three orders of magnitude, rendering them virtually dislocation-free. These substrates will promote the development of high-power SiC devices and reduce energy losses of the resulting electrical systems.

Nature 430, 1010 (2004)

Developed a method for making SiC crystals/wafers that have two to three orders of magnitude lower density of dislocations.

Repeated A-Face (RAF) growth:

At each stage, the crystal is carefully rotated so that the solidifying compound crystallises on the best, least-blemished face.

News Report on BBC

Last Updated: Wednesday, 25 August, 2004, 17:28 GMT 18:28 UK

Door open for silicon replacement

A replacement for the use of pure silicon in electronics has come a step closer, the journal Nature reports.

Silicon chips can malfunction at high temperatures, often from the heat generated in their own circuitry.

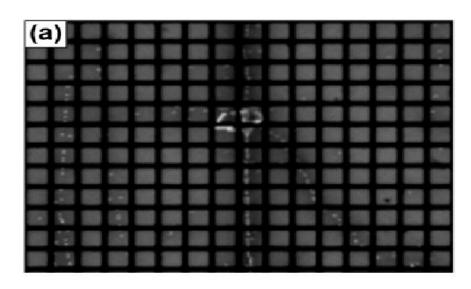
But Japanese experts have now overcome the flaws that plague crystals of silicon carbide, a hard compound that is more robust in hot conditions.

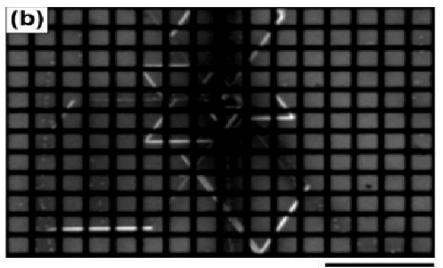
This material could now fulfil its potential as a replacement for pure silicon in manufacturing processes. Silicon carbide (SiC) could be used to make electronic devices that can operate at high power, in fierce heat or at lethal doses of radiation.

If the breakthrough can be carried forward commercially, it could spawn a wide range of improved devices, including electronics that work in red-hot jet engines, better wireless communications and radar, as well as improving smart devices that optimise performance in cars.

Problem: Stacking fault expansion in SiC

Ha, Skowronski, Sumakeris, Paisley and Das, Phy. Rev. Lett. 92, 175504 (2004)





SCALE

100 µm

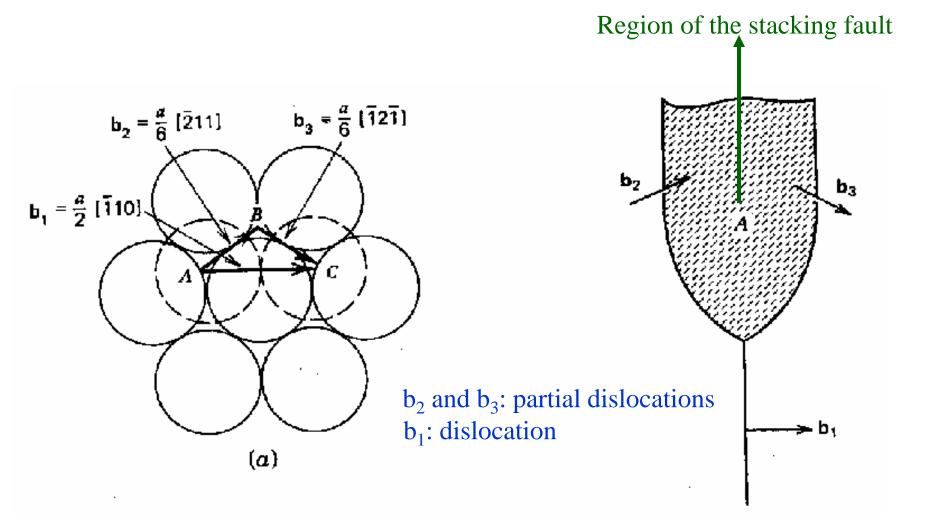
OEM showing development of rhombic stacking faults in the basal plane of 4H-SiC when used in p-i-n diode

- (a) Virgin diode
- (b) Diode after 5 minutes of biasing at 50 A/cm²
- ▶ Degraded performance:
 ∆V changes by up to 1 V!

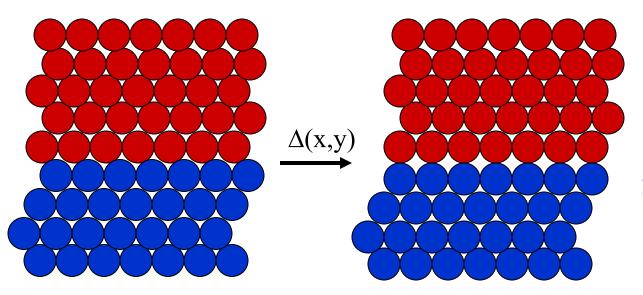
Fundamental Problem

Origin of this phenomenon needs to be understood.

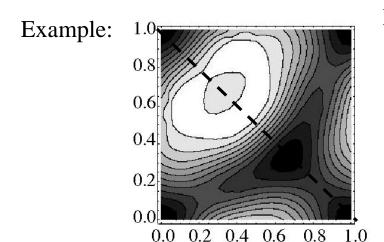
Stacking Faults

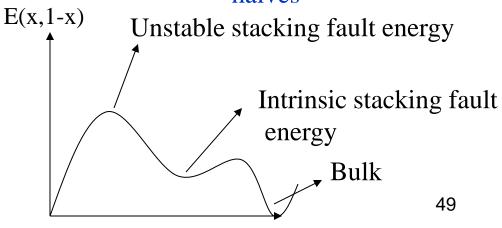


Generalized Stacking Fault Energy Surface γ-surface: E(x,y)



- 1. Energy required to slip one half of a crystal with respect to the other by $x*a_1+y*a_2$
- 2. Exhibits periodicity of the unit cell (a_1,a_2) in the plane separating the two halves





Stacking fault expansion (T≠0): Statistical Thermodynamics

$$F = E + F_{config} + F_{vib}$$

Free energy of a crystal has 3 components:

- (a) Internal energy: Total energy from DFT
- (b) Configurational entropy: Obtain from the DFT γ-surface

Approximate energy basins in the γ -surface with

$$E(x,y) = E_o + K((x-x_o)^2 + (y-y_o)^2),$$
 Free energy is then,
$$F_{conf} = -k_B T Log(\frac{K}{2\pi k_B T})$$

(c) Vibrational entropy: Obtain from phonons using DFT

$$F_{vib} = +k_B T \sum_{ig} Log(2sinh(\frac{\hbar\omega_{iq}}{2k_b T}))$$

(a) Gives very low SFE (1 mJ/m²) (earlier first-principles works).

The y surface of 4H-SiC

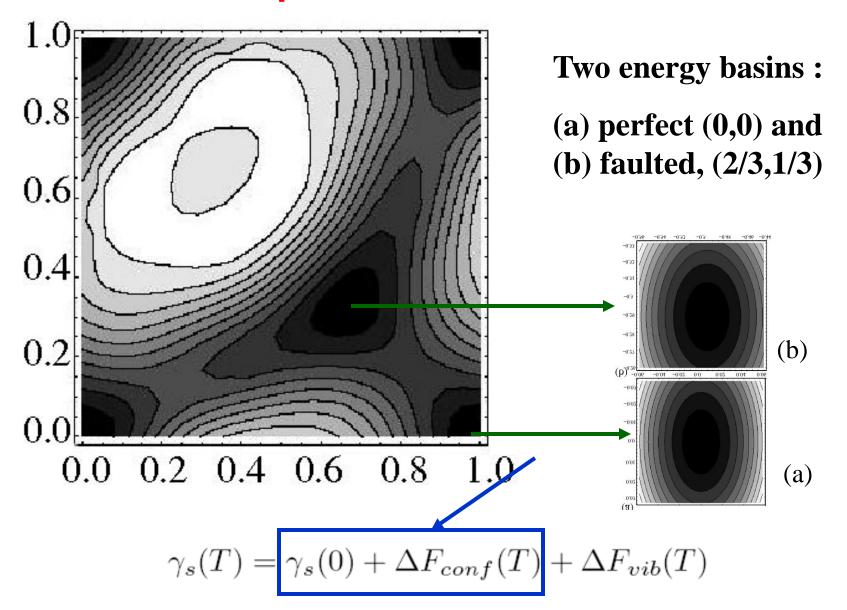
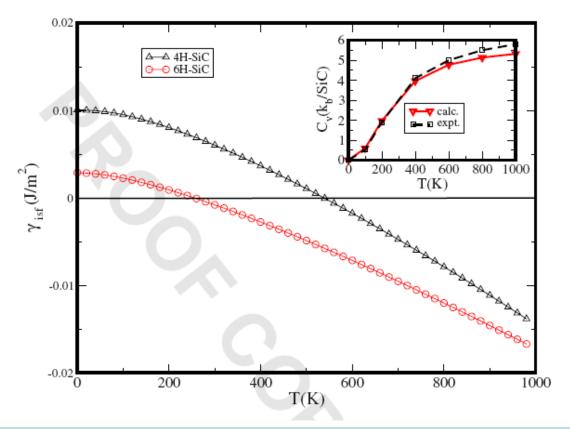


TABLE I. Calculated and experimental estimates of intrinsic (γ_{isf}) and unstable (γ_{us}) stacking fault energies for the slip in glide plane.

System	γ_{isf} (calculated) $({ m mJ/m^2})$	γ_{isf} (experimental) $({ m mJ/m^2})$	γ_{us} (J/m^2)
Si	46.9	69 (Refs. 26 and 27)	1.7
C	250	279 (Refs. 27 and 28)	5.5
Ge	48.5		1.6
3 <i>C</i> -SiC	10.1		2.8
4H-SiC	9.1	14.7 ± 2.5 (Ref. 11)	2.9
6H-SiC	2.6	2.5 ± 0.9 (Ref. 12)	2.9

Ref. Thomas, Pandey and Waghmare, Phys Rev B (Rapid Comm), 77, 121203 (08)

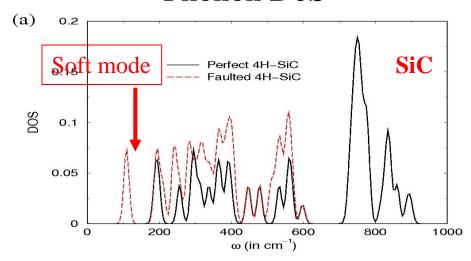
Stacking fault energy of 4H-SiC

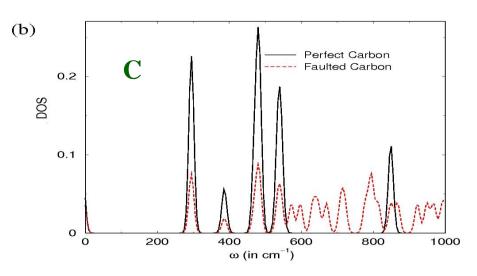


- (1) Vibrational contribution to ∆F/T of (0.2×10-3 J/m²K) dominates over the configurational contribution of (0.27×10-5 J/m²K).
- (2) $\gamma s(T) < 0$ for T > 60 K
- ▶ the faulted structure stabilized, yielding the observed stacking fault expansion.

Origin of Observed Stacking Fault Expansion in 4H-SiC

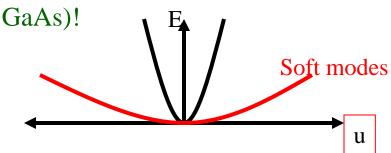
Phonon DoS





Soft modes at 107.3, 107.4, 109.9 and 110.0 cm⁻¹ in faulted 4H-structure of SiC

No such modes in Carbon (or Si, Ge,

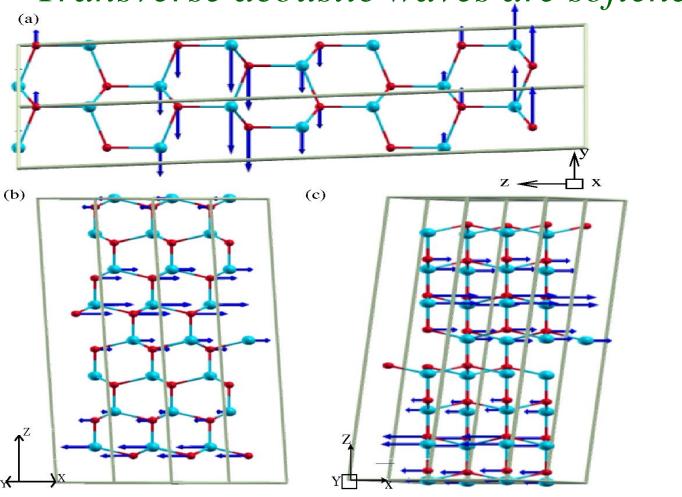


Soft modes: greater entropy

Soft phonon modes commonly responsible for structural phase transitions in solids. Here, we discover them in the context of stacking fault expansion.

Soft modes: Shear straining

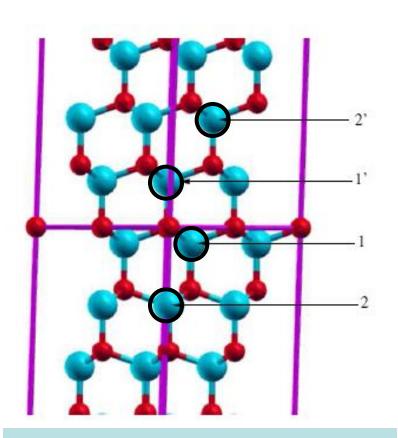
Transverse acoustic waves are softened



Prediction to be verified experimentally: Shear waves will be slown down.

Can we stop the stacking fault expansion in SiC?

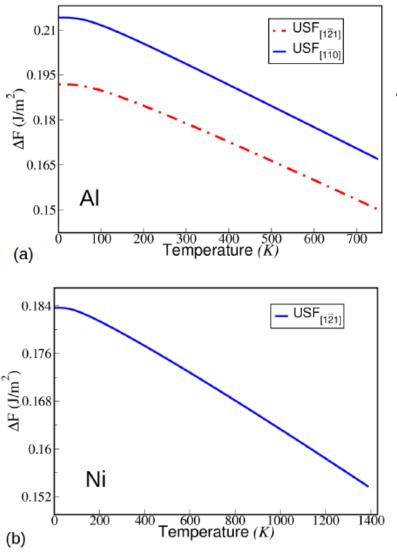
► Through suitable substitutional doping to arrest it!



V and Cr doping in SiC results in higher SF energies, while also giving a DMS!

			P				<u> </u>	
	${\rm TM}$	N	${\bf Fault}$	Energy	(meV)	J (meV)	γ_{sf} (r	nJ/m^2)
			(y/n)	$_{\mathrm{FM}}$	AFM		FM	$_{ m AFM}$
6H	Cr	1	У	34.0	194.7	-160.7	16.6	35.5
			\mathbf{n}	0.0	121.8	-121.8		
	Cr	2	\mathbf{y}	253.2	261.1	-7.9	2.3	6.2
			\mathbf{n}	245.2	248.3	-3.1		
	Cr	3	\mathbf{y}	279.2	279.3	-0.1	24.9	24.6
			\mathbf{n}	228.0	228.7	-0.7		
	${ m Mn}$	1	\mathbf{y}	0.0	57.1	-57.1	-62.1	-8.4
			\mathbf{n}	127.4	74.3	53.1		
	Mn	2	У	335.0	335.0	0.0	18.8	17.2
			\mathbf{n}	296.5	299.6	-3.1		
	${ m Mn}$	3	\mathbf{y}	358.1	357.6	0.5	29.2	28.0
			\mathbf{n}	298.1	300.1	-2.0		
	V	1	у	38.0	_	_	18.5	_
			\mathbf{n}	0.0	_	_		
	V	2	\mathbf{y}	372.5	377.7	-5.2	15.8	12.3
			\mathbf{n}	340.0	352.5	-12.5		
	V	3	\mathbf{y}	387.5	399.7	-12.2	20.2	22.2
			\mathbf{n}	346.1	354.0	-7.9		

Unstable Stacking Fault Energies in Metals



Energy release rate for nucleation of dislocations

20-25 % reduction as T increases to $0.8 T_m$

In Cu, the configuration is unstable!

Enhanced ductility

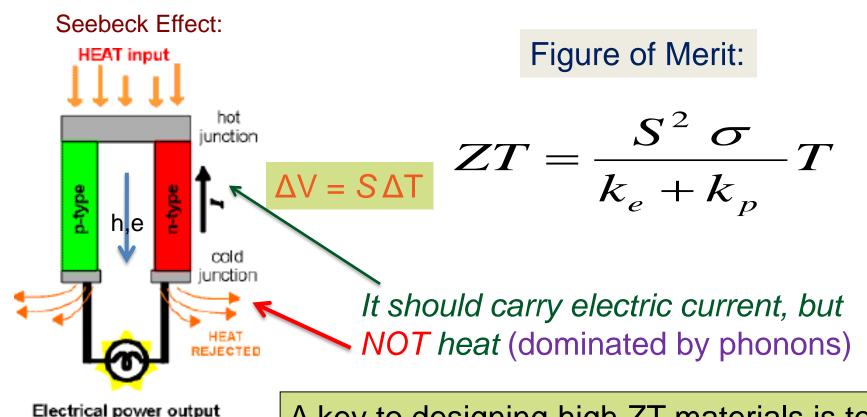
57

Why Phonons?

- Fingerprint of a material: Raman, IR spectra
- Thermodynamic stability: vibrational entropy T, soft modes
- Properties: elastic, dielectric, piezoelectric, etc (couple with fields)
- Structural Transitions: instabilities of a structure $w \rightarrow 0$
- Phonons coupled with electrons, spin, exciton, polarons; e.g. superconductivity

Thermoelectrics and energy conversion

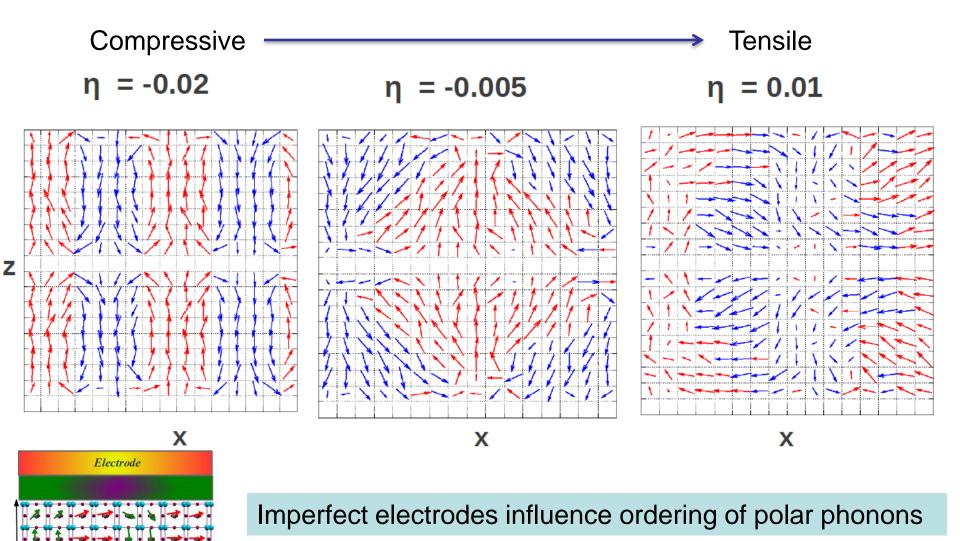
Directly convert thermal energy to electrical energy Environmentally friendly, No moving parts (except for a fan)



A key to designing high ZT materials is to manipulate transport of phonons and electrons: low k

Properties of Ferroelectric Domains

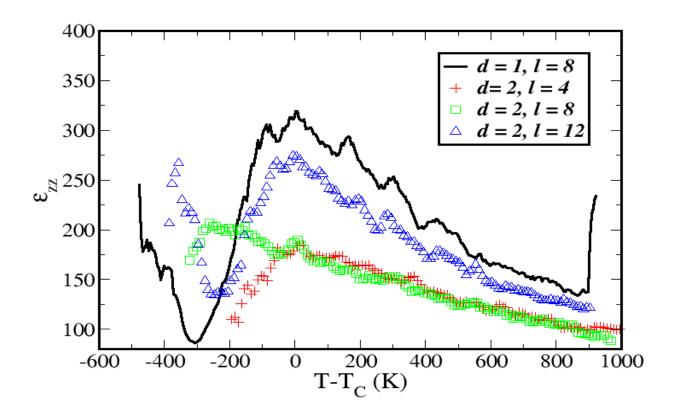
Strain Engineering of Domain Structure in epitaxial PbTiO₃



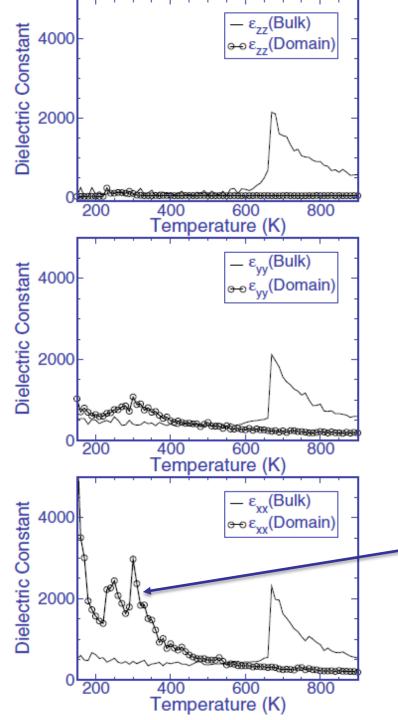
Electrode

Kouser, Nishimatsu, Waghmare, Phys. Rev. B **88**, 064102 (2013); PRB Kaleidoscope, Aug (2013)

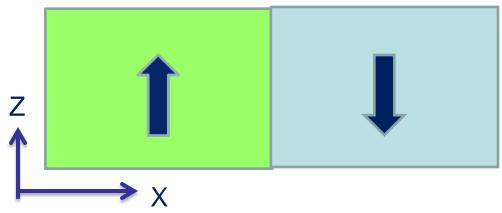
Diffuse Dielectric Response of Domain Structure (PbTiO₃)



Ordering to inhomogeneous phase leads to a diffuse dielectric response across the transition



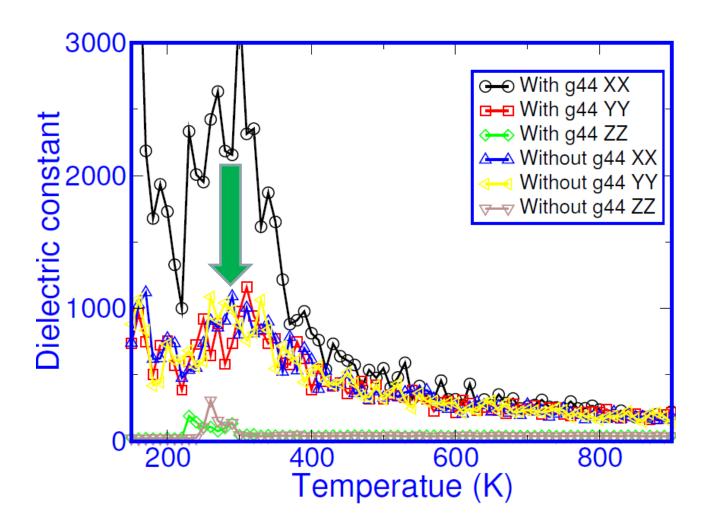
Dielectric Response of a 180° Ferroelectric Domain in PbTiO₃



Enhanced Dielectric Response In the direction perpendicular to the domain wall!

Why xx component?

Corroboration of the phen. Theory from MD



Strain-phonon coupling: dielectric response of a domain wall

Collaborators

Sharmila N Shirodkar Anjali Singh Tiju Thomas Summayya Kouser T Nishimatsu

D Pandey (BHU)

Thank you!