## Euclidean Geometry: An Introduction to Mathematical Work

Math 3600

Fall 2016

## Polygons

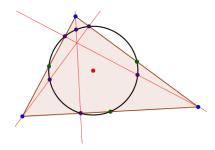
Now it is time to extend our venue to *polygons* with an arbitrary number of sides.

**Definition.** Let n be a natural number. An n-gon is a figure consisting of n points  $A_1, A_2, \ldots, A_n$ , prescribed in order and called vertices, and the n line segments, called sides,  $A_1A_2, A_2A_3, \ldots, A_{n-1}A_n, A_nA_1$ . A polygon is an n-gon where n has not been specified.

**5.1 Problem.** Suppose that *A*, *B*, *C* are three consecutive vertices of a polygon. If at the vertex *B* we extend one of the two sides through *B* to a ray, then we create a new angle, called an *exterior angle* to the polygon at *B*.

This construction has a choice in it. In principle, this could be a problem. Describe the problem, then state and prove a theorem that resolves the issue.

- **5.2 Conjecture.** The exterior angles of a pentagon, one choice made at each vertex, add up to four right angles.
- **5.3 Question.** What is the sum of the exterior angles of a hexagon? What about a general n-gon? Can you find a way to build on our understanding from small values of n, to general values of n?



Note: Commonly used terminology includes the following: 3-gon = triangle, 4-gon = quadrilateral, 5-gon = pentagon, 6-gon = hexagon.