

For the jupyter notebook we use this octave kernel: https://github.com/Calysto/octave_kernel

```
pip install octave_kernel
cd <root of the project>
jupyter notebook
```

```
In [1]: format longE

# setup the path to include the 'utils' directory
directory = pwd
addpath(genpath(directory))
```

```
directory = /home/thodkatz/repos/personal/math-optimization
```

```
In [2]: is_backtracking_wolfe_weak = 1;
is_wolfe_strong = 2;
is_backtracking_armijo = 3;
is_none = 4;
```

```
In [ ]: # define rosenbrock function

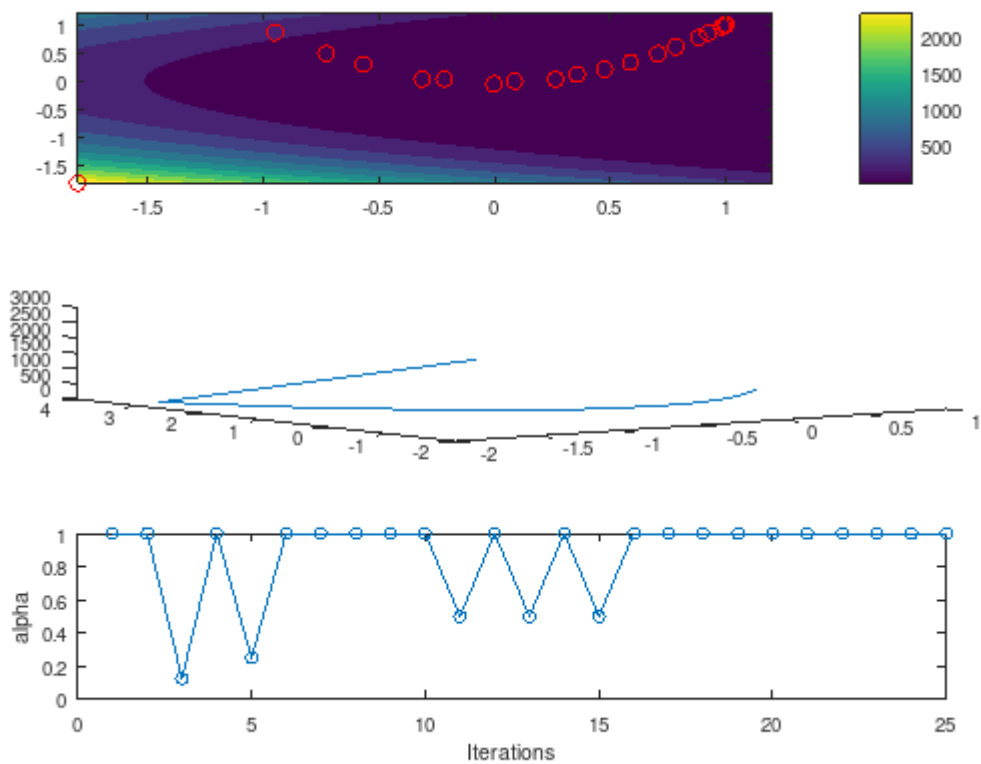
function f = rosen_sym()
    syms x y
    f = 100*(y-x^2)^2 + (1-x)^2;
end
```

```
In [53]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
[xmin, fmin] = newton(rosen_sym, [-1.8, -1.8]', is_backtracking_wolfe_weak, search_x,
```

```
STARTED Line search using newton
ENDED Line search using newton
xmin =
```

```
9.999999999816411e-01
9.999999999576280e-01
```

```
fmin = 3.534107889272943e-21
```

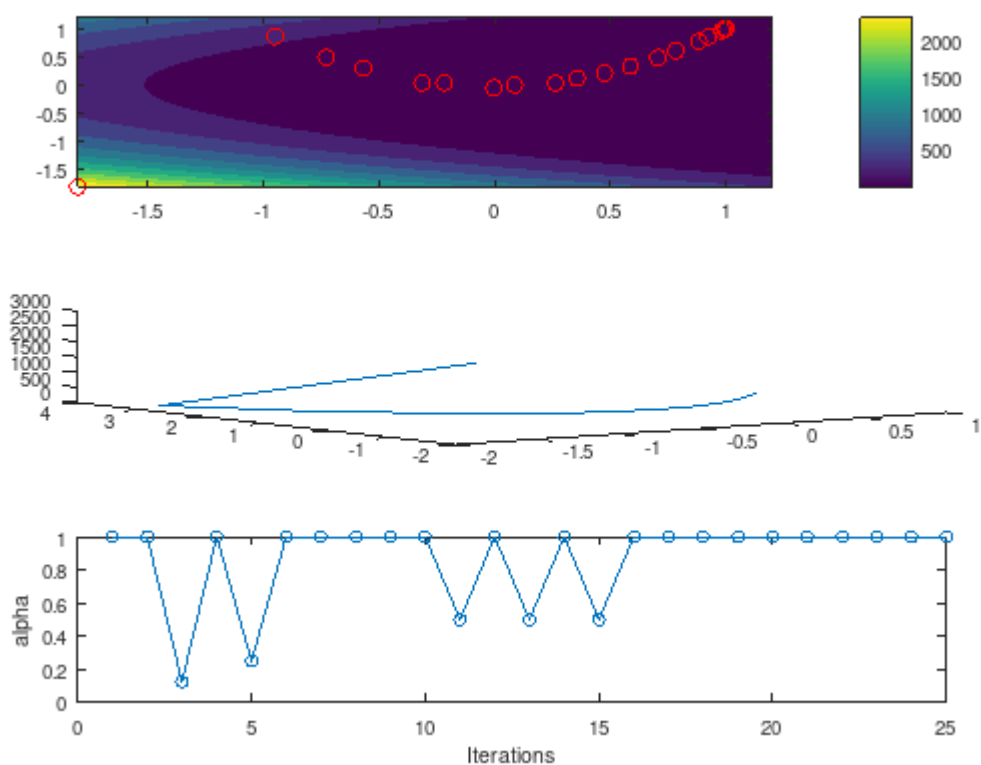


```
In [54]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
[xmin, fmin] = newton(rosen_sym, [-1.8,-1.8]', is_backtracking_armijo, search_x, sear
```

```
STARTED Line search using newton
ENDED Line search using newton
xmin =
```

```
9.999999999816411e-01
9.999999999576280e-01
```

```
fmin = 3.534107889272943e-21
```

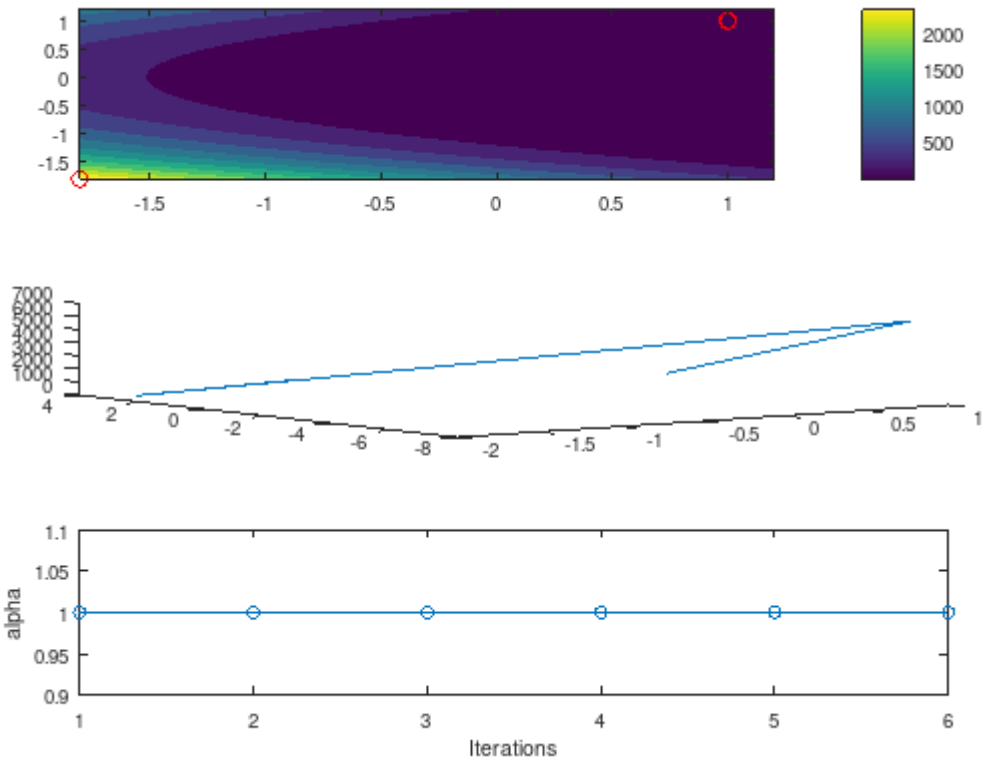


```
In [55]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
[xmin, fmin] = newton(rosen_sym, [-1.8,-1.8]', is_none, search_x, search_y);
```

STARTED Line search using newton
 ENDED Line search using newton
 xmin =

```
9.99999999999759e-01
9.99999999999519e-01
```

fmin = 5.816493321323984e-28

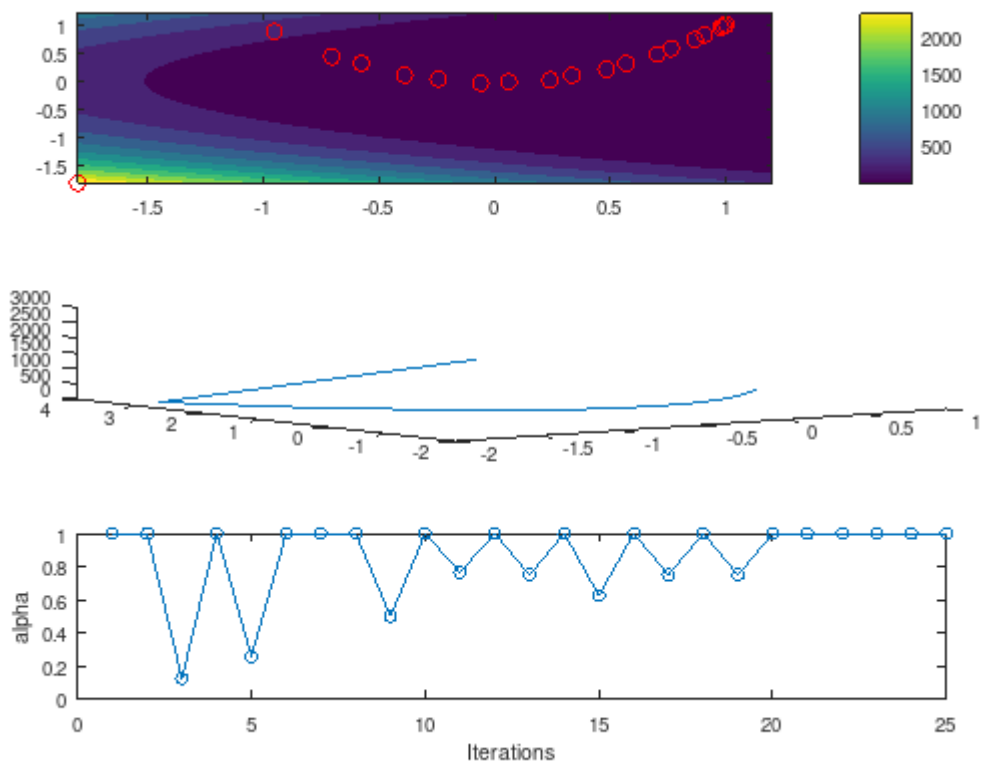


```
In [56]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = newton(rosen_sym, [-1.8,-1.8]', is_wolfe_strong, search_x, search_y, c
```

STARTED Line search using newton
 ENDED Line search using newton
 xmin =

```
9.9999999998532665e-01
9.999999996432530e-01
```

fmin = 4.219657651944829e-19

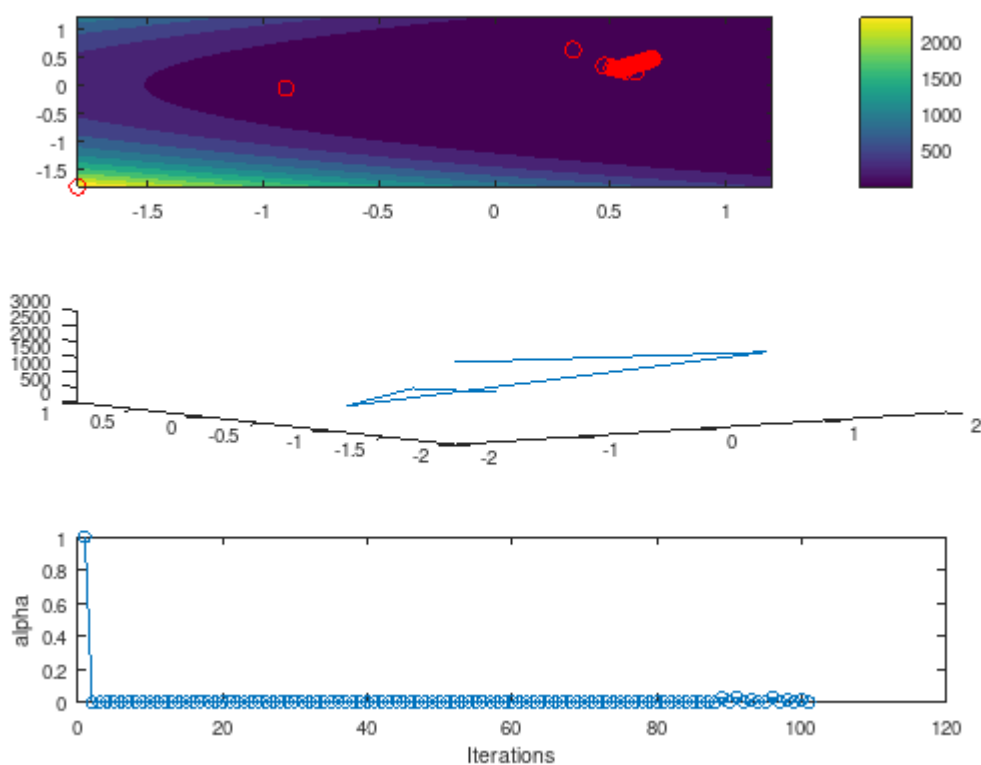


```
In [57]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
[xmin, fmin] = steepest_descent(rosen_sym, [-1.8,-1.8]', is_backtracking_wolfe_weak,
```

```
STARTED Line search using steepest descent
ENDED Line search using steepest descent
xmin =
```

```
6.830308556342202e-01
4.645442633745788e-01
```

```
fmin = 1.008642102262281e-01
```



```
In [61]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
[xmin, fmin] = steepest_descent(rosen_sym, [-1.8,-1.8]', is_backtracking_armijo, sear
```

STARTED Line search using steepest descent

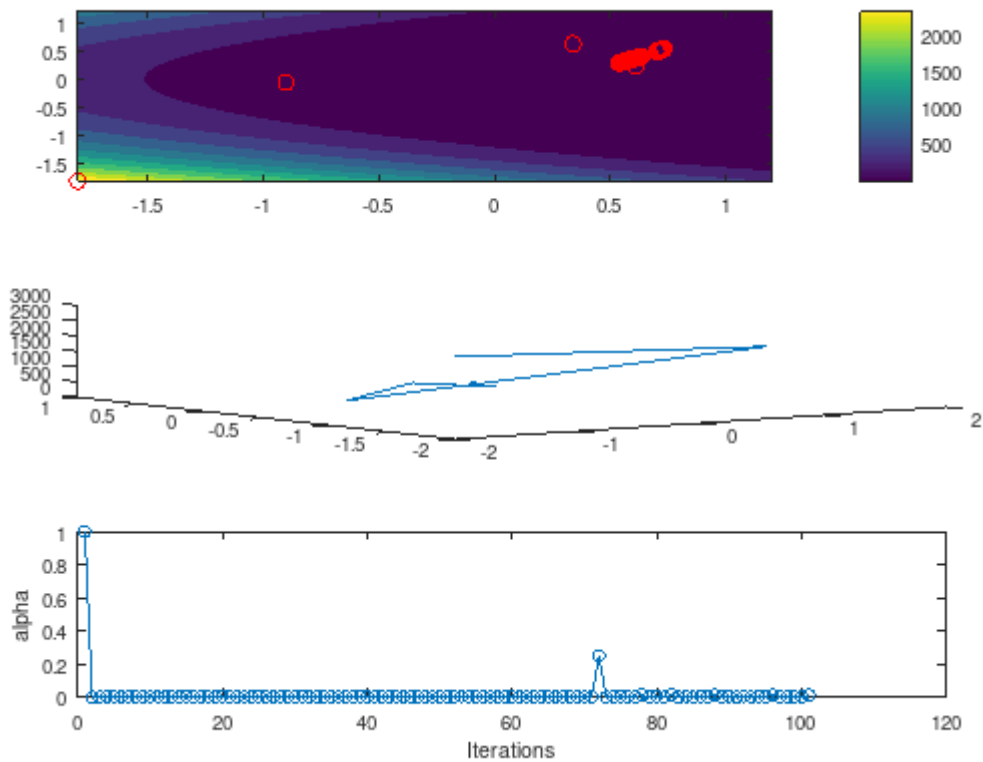
ENDED Line search using steepest descent

xmin =

7.314832480328027e-01

5.367666412124249e-01

fmin = 7.238987188855434e-02



```
In [62]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
[xmin, fmin] = steepest_descent(rosen_sym, [-1.8,-1.8]', is_none, search_x, search_y)
```

STARTED Line search using steepest descent

error: Failed to converge. Inf value reached

error: called from

steepest_descent at line 45 column 13

```
In [63]: search_x = -1.8:0.1:1.2;
search_y = -1.8:0.1:1.2;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = steepest_descent(rosen_sym, [-1.8,-1.8]', is_wolfe_strong, search_x, s
```

STARTED Line search using steepest descent

error: Failed to converge. Inf value reached

error: called from

steepest_descent at line 45 column 13

```

function f = f1_sym()
    syms x y
    f = x^2 + 4*y^2 + 2*x*y;
end

```

```

In [65]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
[xmin, fmin] = newton(f1_sym, [-3,-3]', is_backtracking_wolfe_weak, search_x, search_

```

```

STARTED Line search using newton
ENDED Line search using newton
xmin =

```

```

-1.332267629550188e-15
8.881784197001252e-16

```

```

fmin = 2.563797941968288e-30
xmin =

```

```

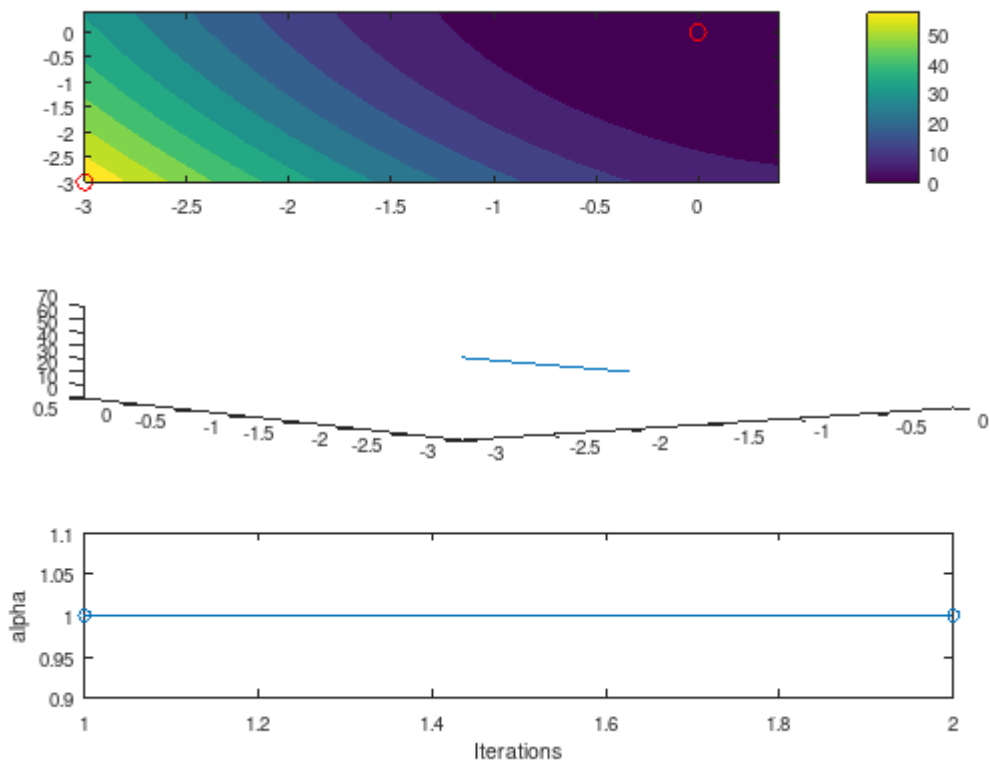
-1.332267629550188e-15
8.881784197001252e-16

```

```

fmin = 2.563797941968288e-30

```



```

In [66]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
[xmin, fmin] = newton(f1_sym, [-3,-3]', is_backtracking_armijo, search_x, search_y)

```

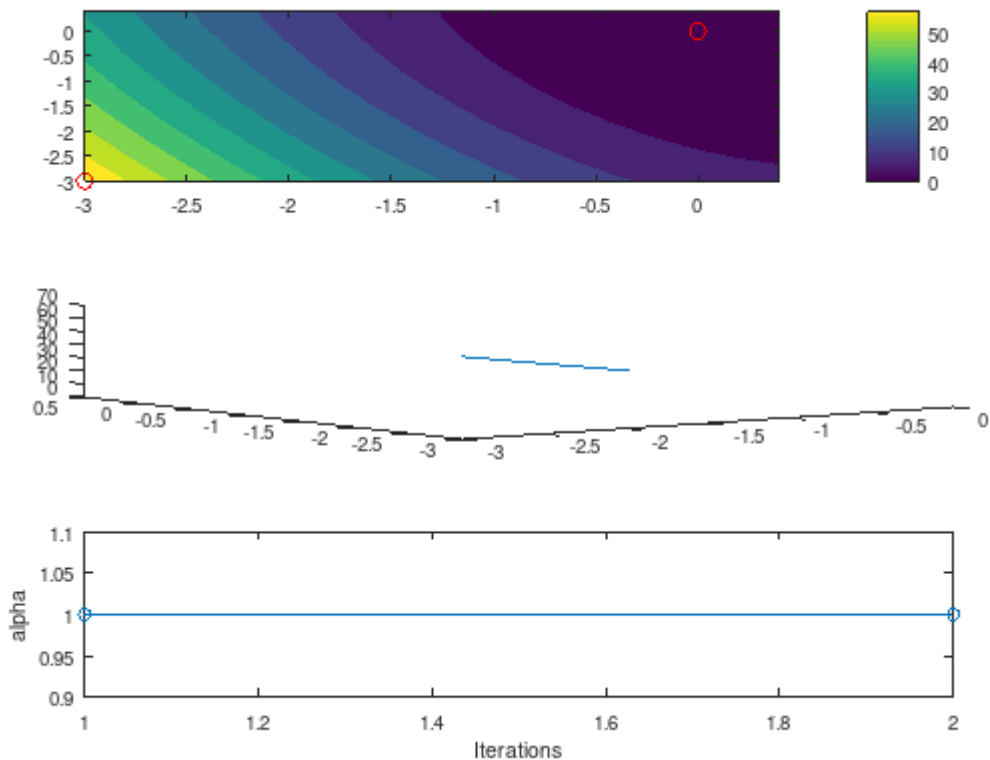
STARTED Line search using newton
 ENDED Line search using newton
 xmin =

-1.332267629550188e-15
 8.881784197001252e-16

fmin = 2.563797941968288e-30
 xmin =

-1.332267629550188e-15
 8.881784197001252e-16

fmin = 2.563797941968288e-30



```
In [67]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
[xmin, fmin] = newton(f1_sym, [-3,-3]', is_none, search_x, search_y)
```

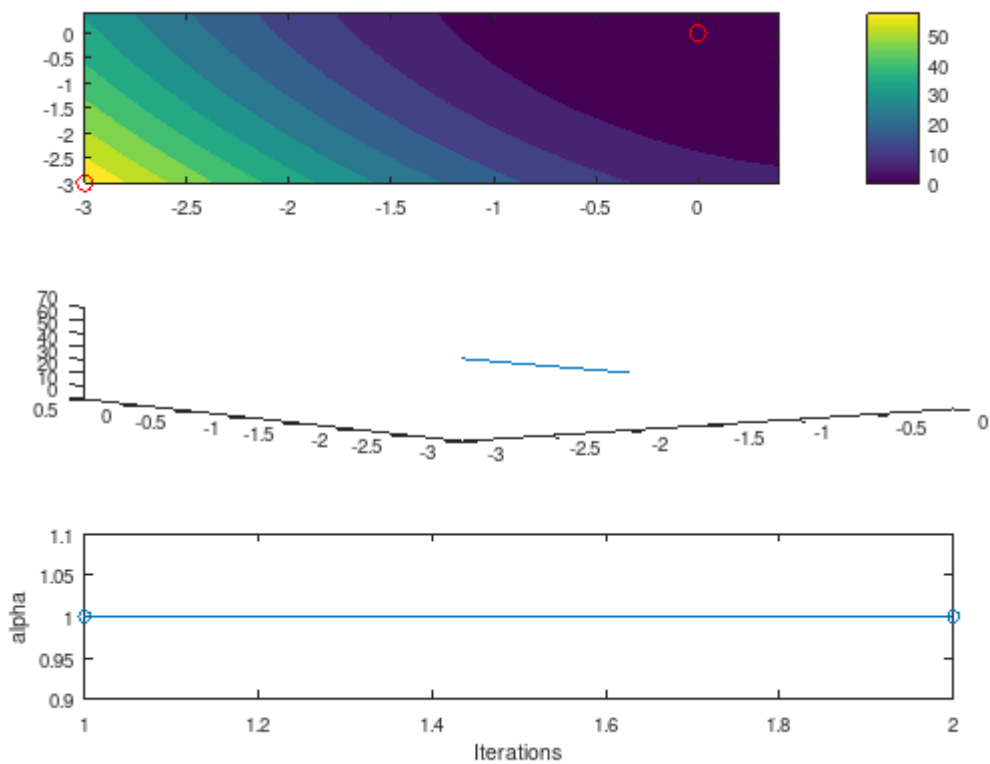
STARTED Line search using newton
 ENDED Line search using newton
 xmin =

-1.332267629550188e-15
 8.881784197001252e-16

fmin = 2.563797941968288e-30
 xmin =

-1.332267629550188e-15
 8.881784197001252e-16

fmin = 2.563797941968288e-30



```
In [68]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = newton(f1_sym, [-3,-3]', is_wolfe_strong, search_x, search_y, c, rho)
```

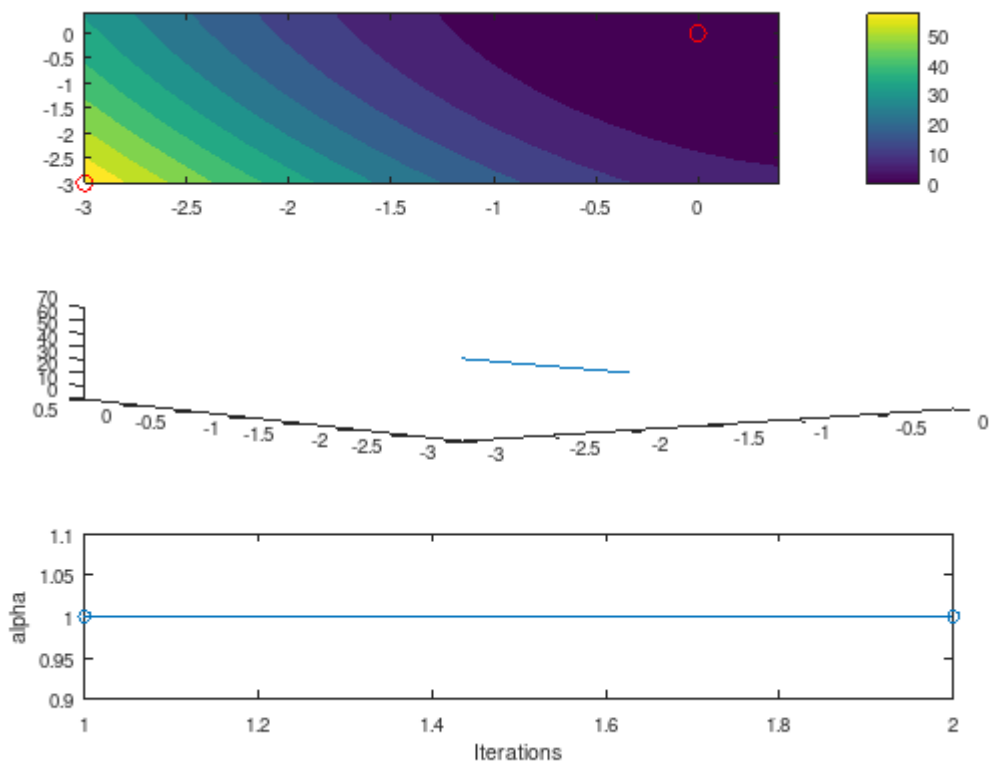
```
STARTED Line search using newton
ENDED Line search using newton
xmin =
```

```
-1.332267629550188e-15
8.881784197001252e-16
```

```
fmin = 2.563797941968288e-30
xmin =
```

```
-1.332267629550188e-15
8.881784197001252e-16
```

```
fmin = 2.563797941968288e-30
```

```
In [5]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
[xmin, fmin] = steepest_descent(f1_sym, [-3,-3]', is_backtracking_wolfe_weak, search_
```

Symbolic pkg v3.1.1: Python communication link active, SymPy v1.11.1.

STARTED Line search using steepest descent

ENDED Line search using steepest descent

xmin =

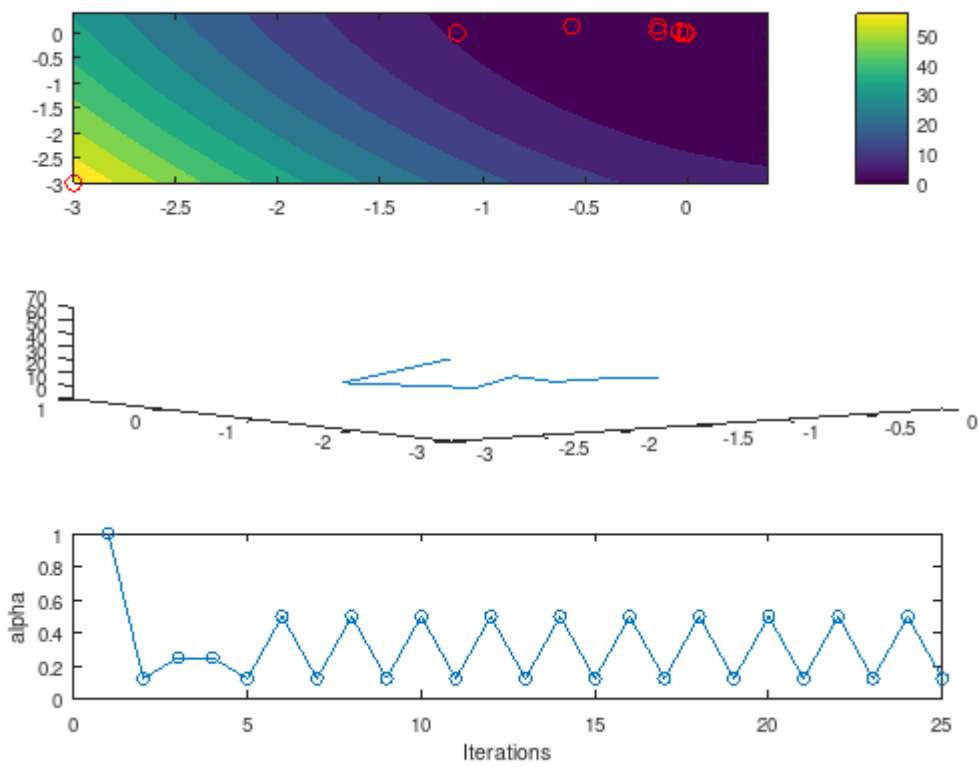
```
-5.364418029785156e-07
1.341104507446289e-07
```

fmin = 2.158273559871304e-13

xmin =

```
-5.364418029785156e-07
1.341104507446289e-07
```

fmin = 2.158273559871304e-13



```
In [70]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
[xmin, fmin] = steepest_descent(f1_sym, [-3,-3]', is_backtracking_armijo, search_x, s
```

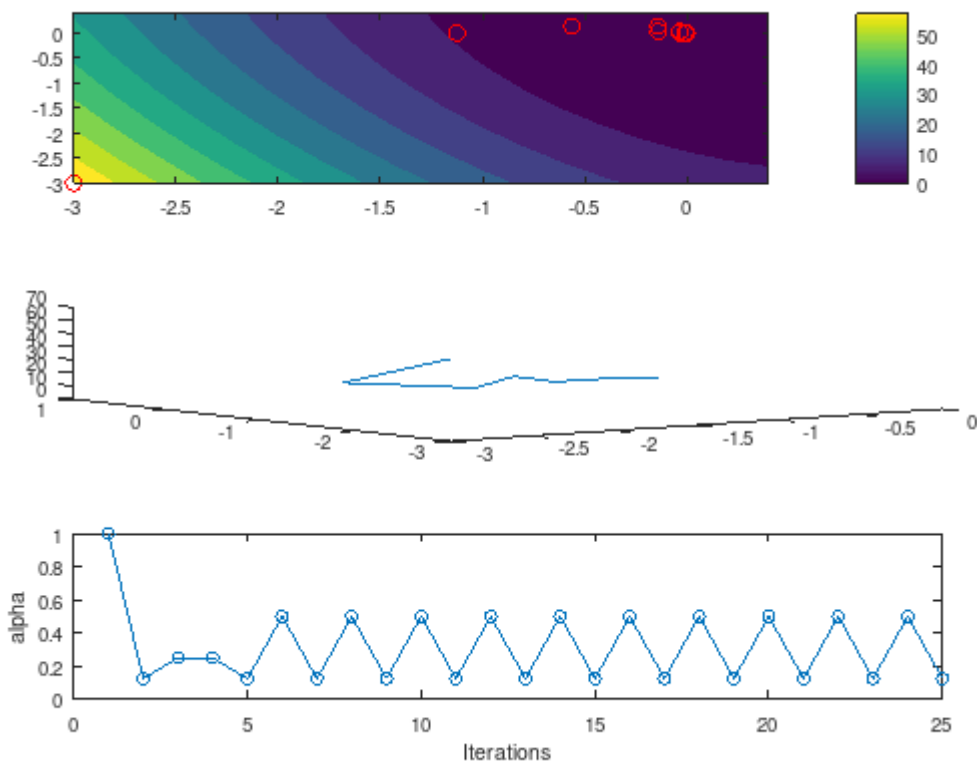
```
STARTED Line search using steepest descent
ENDED Line search using steepest descent
xmin =
```

```
-5.364418029785156e-07
1.341104507446289e-07
```

```
fmin = 2.158273559871304e-13
xmin =
```

```
-5.364418029785156e-07
1.341104507446289e-07
```

```
fmin = 2.158273559871304e-13
```



```
In [71]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
[xmin, fmin] = steepest_descent(f1_sym, [-3,-3]', is_none, search_x, search_y);
```

STARTED Line search using steepest descent
 ENDED Line search using steepest descent
 xmin =

-1.406335921346234e+88
 -4.644812019489721e+88

fmin = 1.013392274910718e+178
 error: set: "cameraviewangle" must be finite
 error: called from
 plot3 at line 371 column 10
 plot_line_search1 at line 41 column 9
 steepest_descent at line 65 column 5

Inline plot failed, consider trying another graphics toolkit

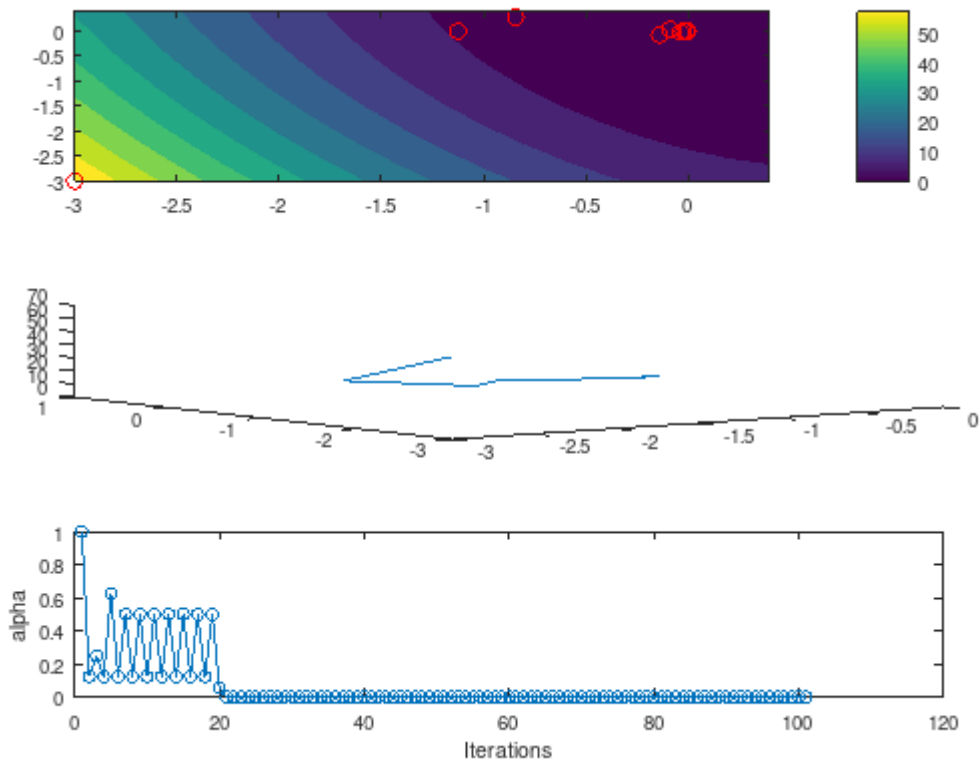
error: set: "cameraviewangle" must be finite
 error: called from
 _make_figures>safe_print at line 125 column 7
 _make_figures at line 49 column 13

```
In [6]: search_x = -3:0.2:0.4;
search_y = -3:0.2:0.4;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = steepest_descent(f1_sym, [-3,-3]', is_wolfe_strong, search_x, search_y)
```

STARTED Line search using steepest descent
 ENDED Line search using steepest descent
 xmin =

-6.383952198571882e-06
 -5.914933985905300e-07

fmin = 4.970643460070100e-11



In [7]: `% f(x,y) = (x + 2y - 7)^2 + (2x + y - 5)^2 -- fmin = 0 at x = 1, y = 3 -- Search doma`

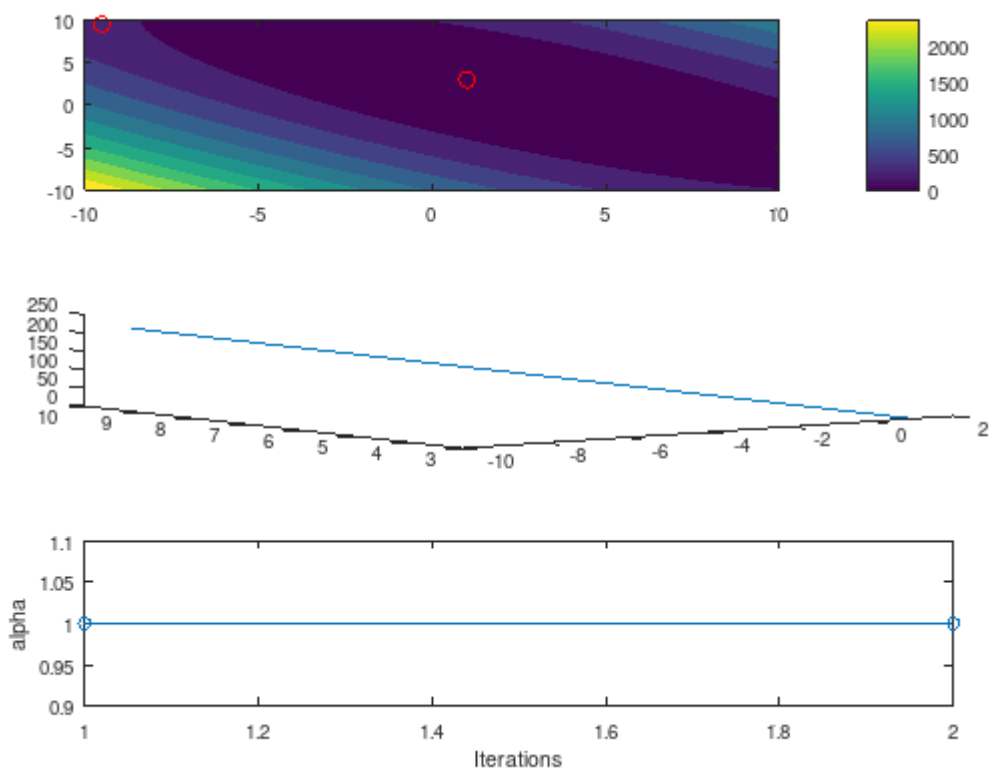
```
function f = f2_sym()
    syms x y
    f = (x+2*y-7)^2 + (2*x + y - 5)^2;
end
```

In [8]: `search_x = -10:0.5:10;
search_y = -10:0.5:10;
[xmin, fmin] = newton(f2_sym, [-9.5,9.5]', is_backtracking_wolfe_weak, search_x, sear`

STARTED Line search using newton
 ENDED Line search using newton
 xmin =

1.000000000000000e+00
 3.000000000000000e+00

fmin = 0

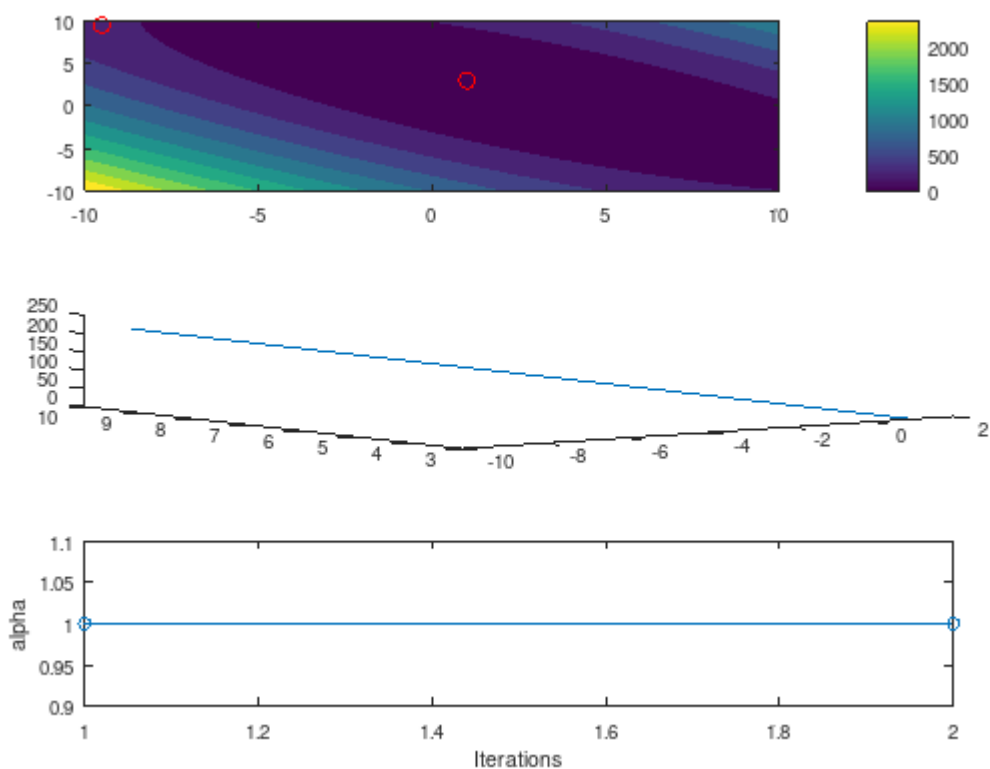


```
In [9]: search_x = -10:0.5:10;
search_y = -10:0.5:10;
[xmin, fmin] = newton(f2_sym, [-9.5,9.5]', is_backtracking_armijo, search_x, search_y
```

```
STARTED Line search using newton
ENDED Line search using newton
xmin =
```

```
1.0000000000000000e+00
3.0000000000000000e+00
```

```
fmin =          0
```



```
In [10]: search_x = -10:0.5:10;
search_y = -10:0.5:10;
[xmin, fmin] = newton(f2_sym, [-9.5,9.5]', is_none, search_x, search_y);
```

STARTED Line search using newton

ENDED Line search using newton

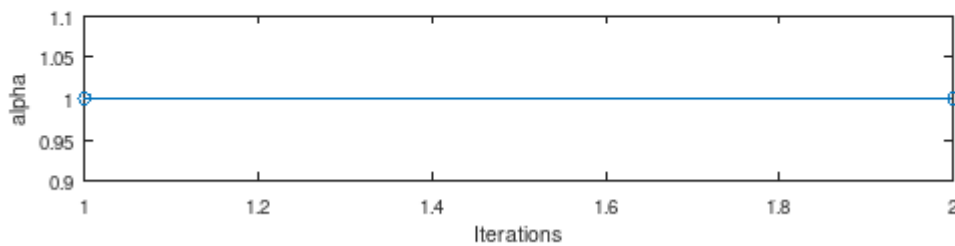
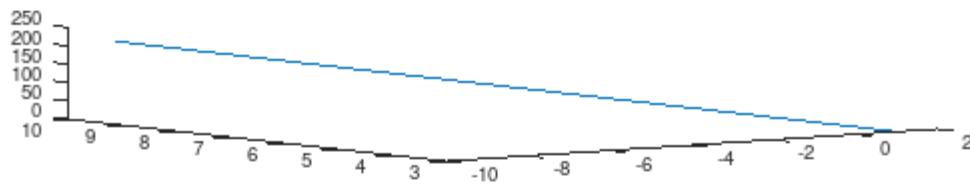
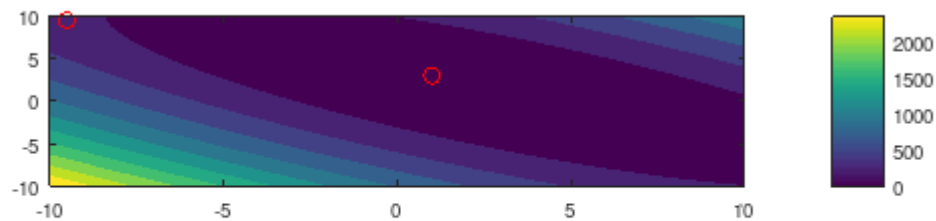
xmin =

1.0000000000000000e+00

3.0000000000000000e+00

fmin =

0



```
In [11]: search_x = -10:0.5:10;
search_y = -10:0.5:10;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = newton(f2_sym, [-9.5,9.5]', is_wolfe_strong, search_x, search_y, c, rh
```

STARTED Line search using newton

ENDED Line search using newton

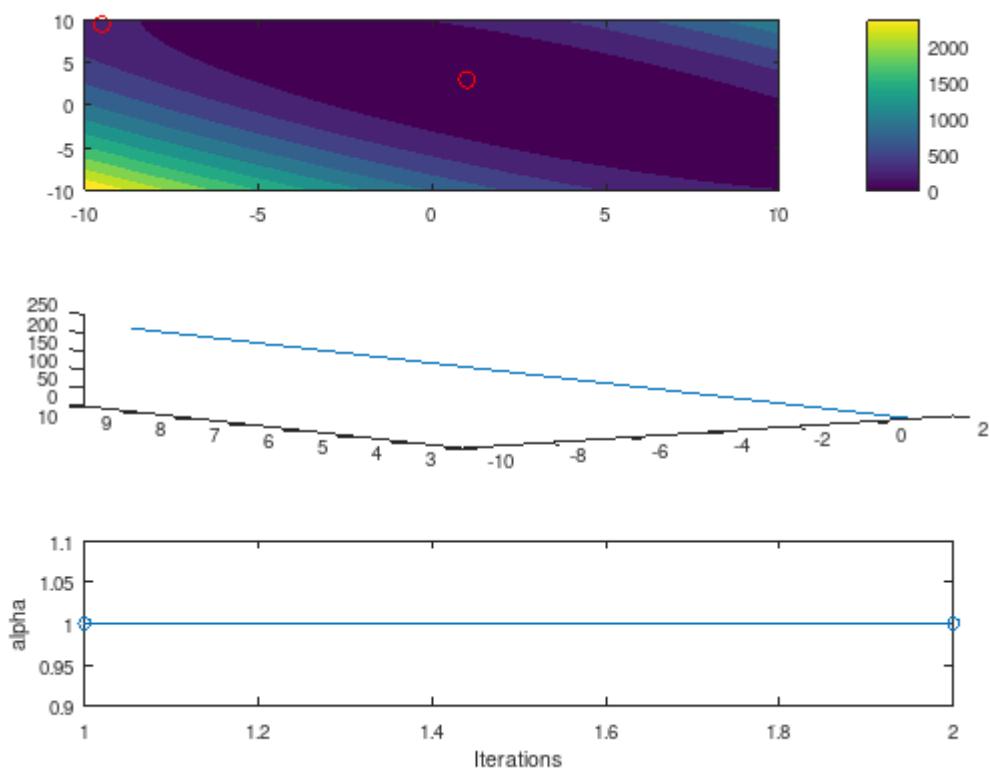
xmin =

1.0000000000000000e+00

3.0000000000000000e+00

fmin =

0

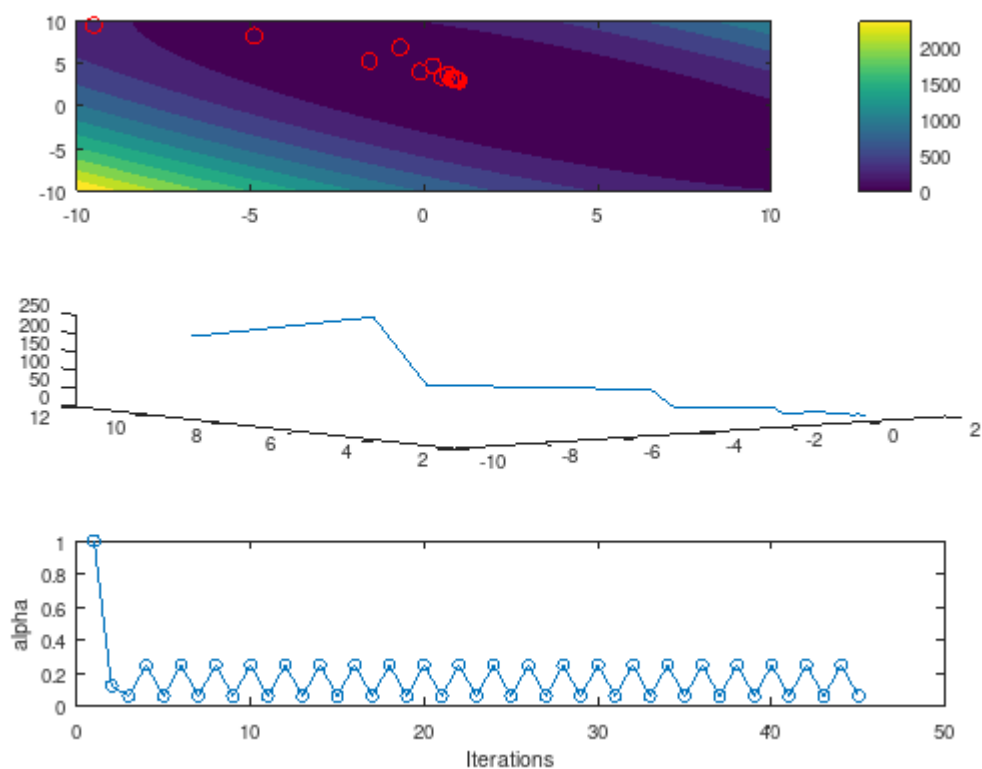


```
In [12]: search_x = -10:0.5:10;
search_y = -10:0.5:10;
[xmin, fmin] = steepest_descent(f2_sym, [-9.5,9.5]', is_backtracking_wolfe_weak, sear
```

```
STARTED Line search using steepest descent
ENDED Line search using steepest descent
xmin =
```

```
9.999998299014621e-01
3.0000000152050948e+00
```

```
fmin = 5.335586537193396e-14
```

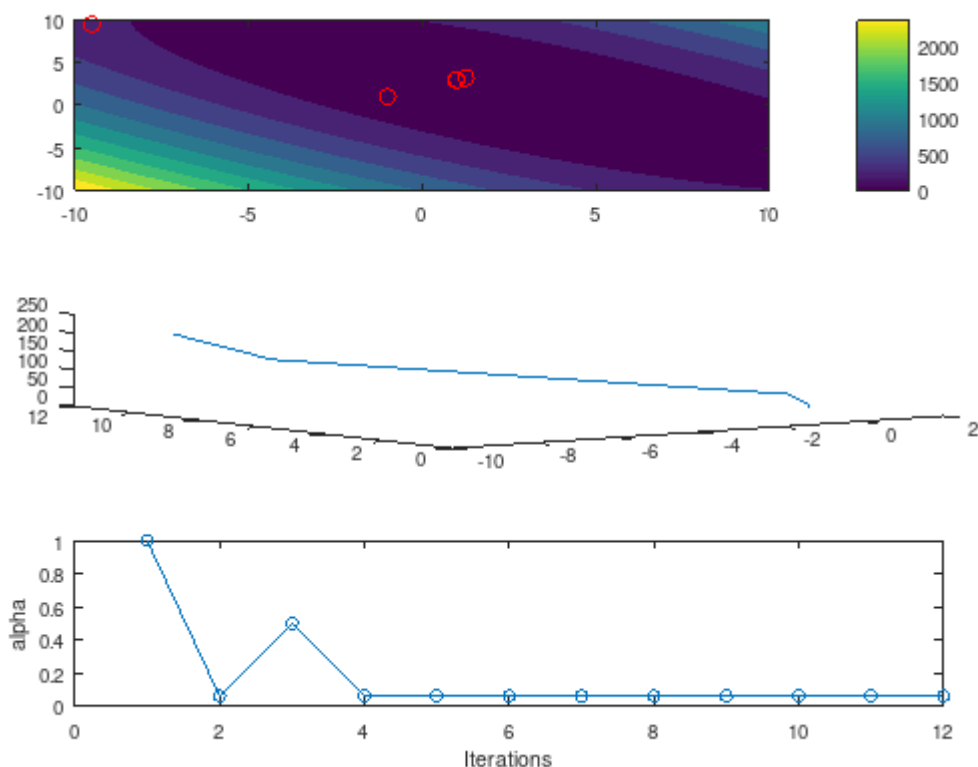


```
In [13]: search_x = -10:0.5:10;
search_y = -10:0.5:10;
[xmin, fmin] = steepest_descent(f2_sym, [-9.5,9.5]', is_backtracking_armijo, search_x
```

STARTED Line search using steepest descent
 ENDED Line search using steepest descent
 xmin =

1.000000014901161e+00
 3.000000014901161e+00

fmin = 3.996802888650564e-15



```
In [14]: search_x = -10:0.5:10;
search_y = -10:0.5:10;
[xmin, fmin] = steepest_descent(f2_sym, [-9.5,9.5]', is_none, search_x, search_y);
```

STARTED Line search using steepest descent
 ENDED Line search using steepest descent
 xmin =

-2.217798745561569e+123
 -2.217798745561569e+123

fmin = 8.853536296466041e+247
 error: set: "cameraviewangle" must be finite
 error: called from
 plot3 at line 371 column 10
 plot_line_search1 at line 41 column 9
 steepest_descent at line 65 column 5

Inline plot failed, consider trying another graphics toolkit

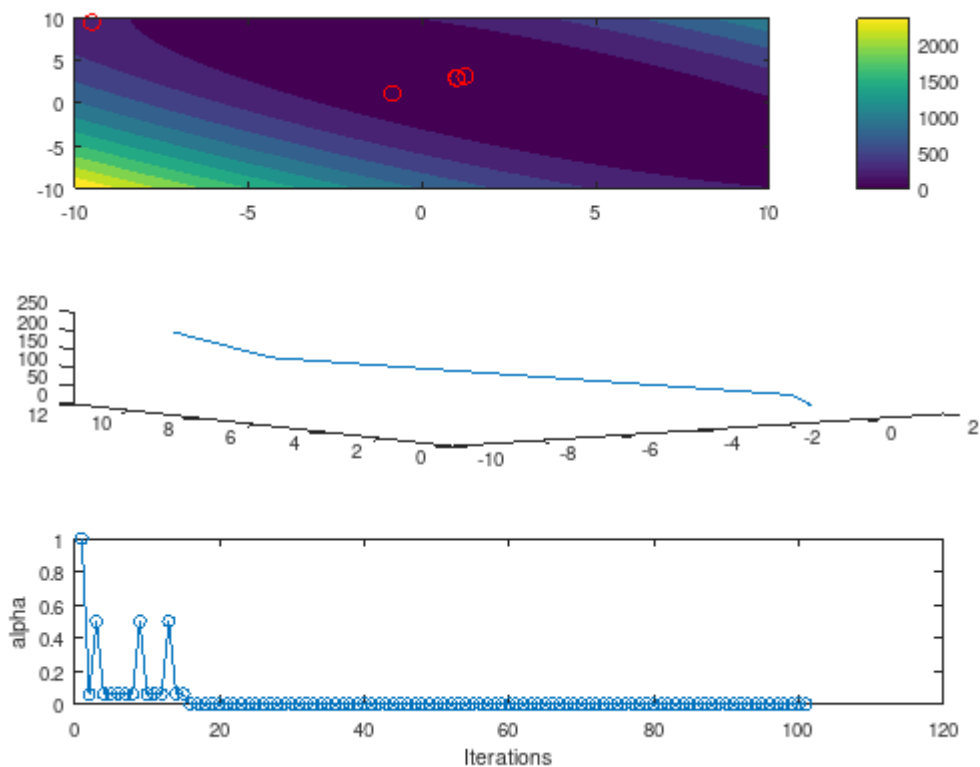
error: set: "cameraviewangle" must be finite
 error: called from
 _make_figures>safe_print at line 125 column 7
 _make_figures at line 49 column 13


```
In [15]: search_x = -10:0.5:10;
search_y = -10:0.5:10;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = steepest_descent(f2_sym, [-9.5,9.5]', is_wolfe_strong, search_x, search_y)
```

STARTED Line search using steepest descent
 ENDED Line search using steepest descent
 xmin =

9.999999381765151e-01
 2.999999934833218e+00

fmin = 7.257496400782470e-14



```
In [16]: % f(x,y) = 5x^4 + 6y^4 - 6x^2 + 2xy + 5y^2 +15x - 7y + 13 -- fmin = -6.4931 at x = -1

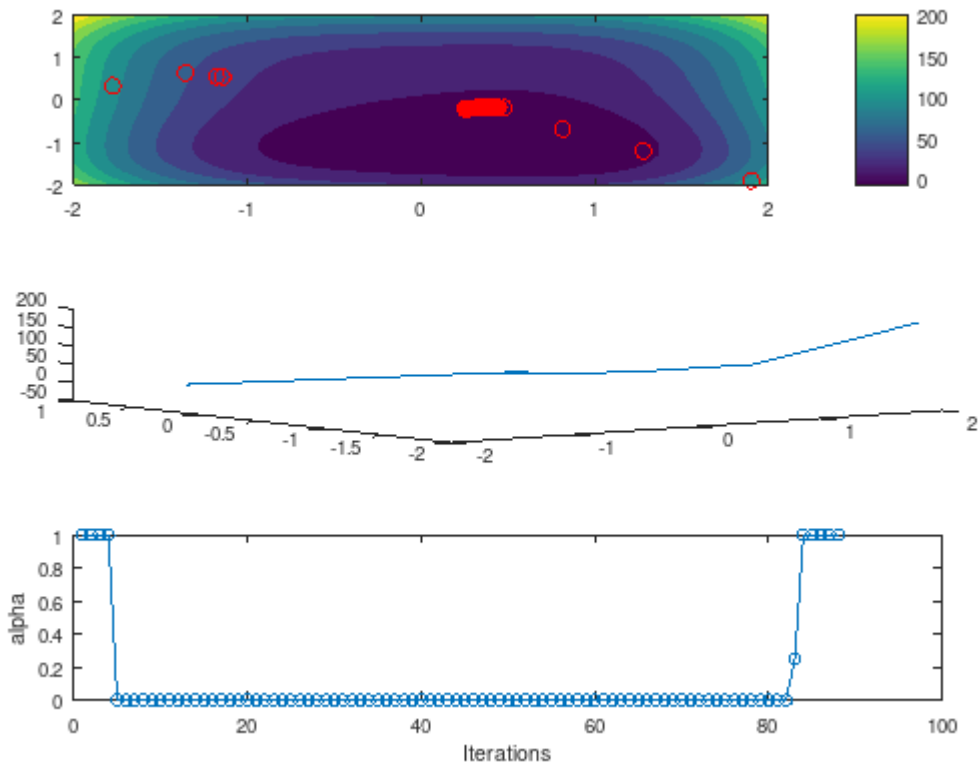
function f = f3_sym()
    syms x y
    f = 5*x^4 + 6*y^4 - 6*x^2 + 2*x*y + 5*y^2 + 15*x - 7*y + 13;
end
```

```
In [18]: search_x = -2:0.1:2;
search_y = -2:0.1:2;
[xmin, fmin] = newton(f3_sym, [1.9,-1.9]', is_backtracking_wolfe_weak, search_x, search_y)
```

STARTED Line search using newton
ENDED Line search using newton
xmin =

-1.142054928372278e+00
5.433724812053312e-01

fmin = -6.496118935491067e+00

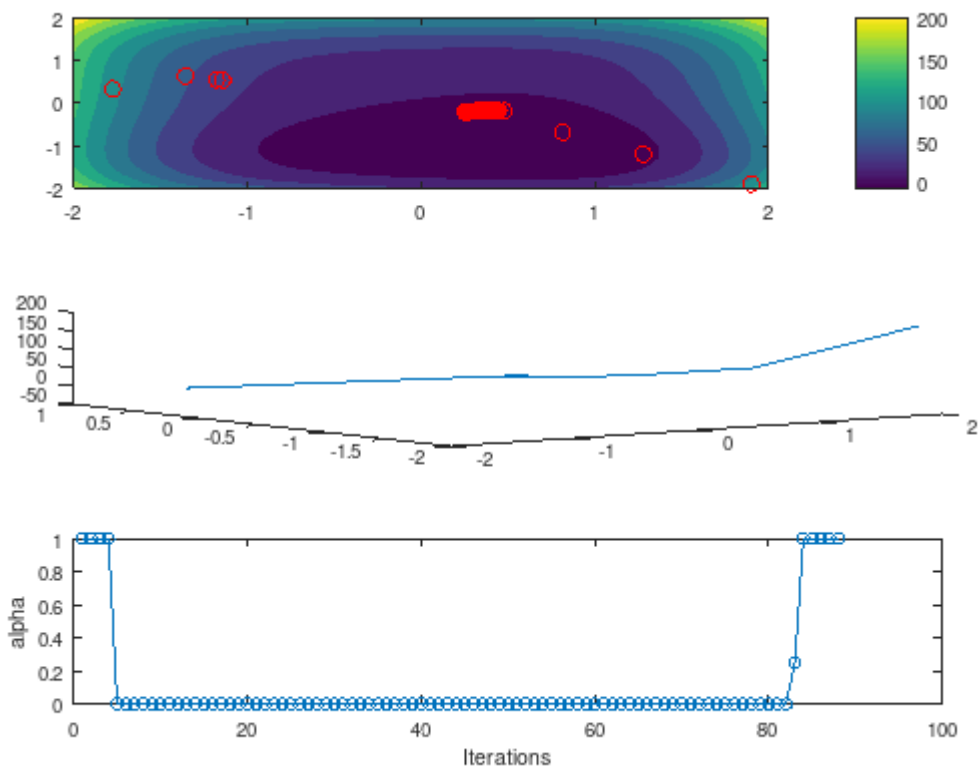


```
In [19]: search_x = -2:0.1:2;  
search_y = -2:0.1:2;  
[xmin, fmin] = newton(f3_sym, [1.9, -1.9]', is_backtracking_armijo, search_x, search_y
```

STARTED Line search using newton
ENDED Line search using newton
xmin =

-1.142054928372278e+00
5.433724812053312e-01

fmin = -6.496118935491067e+00

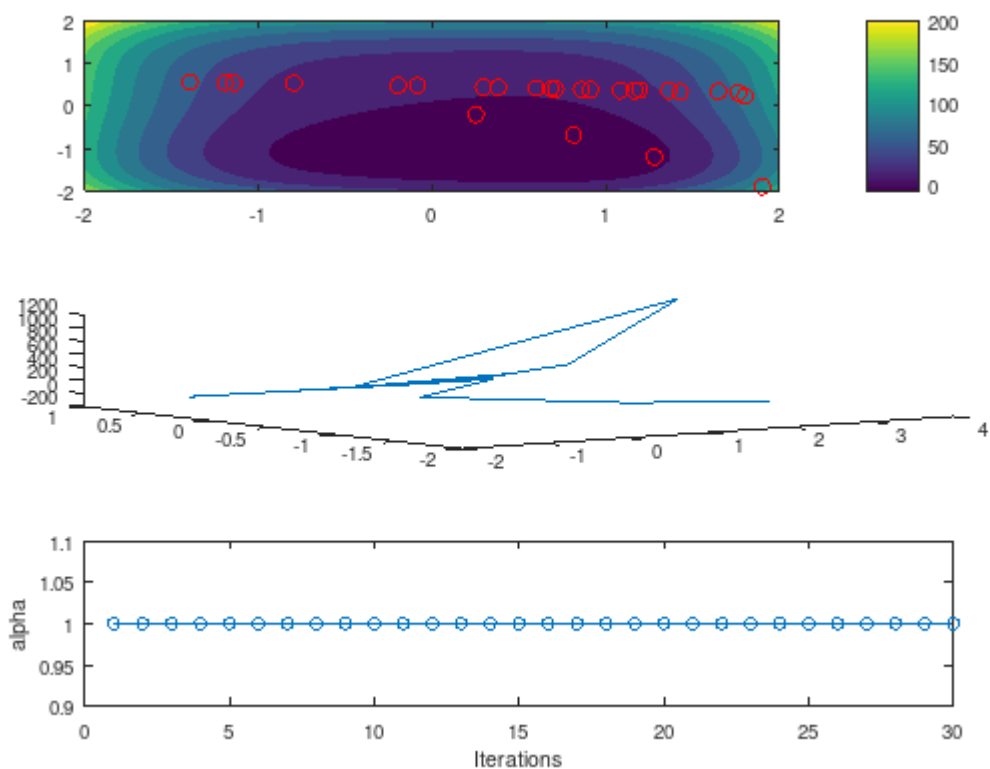


```
In [20]: search_x = -2:0.1:2;
search_y = -2:0.1:2;
[xmin, fmin] = newton(f3_sym, [1.9, -1.9]', is_none, search_x, search_y);
```

```
STARTED Line search using newton
ENDED Line search using newton
xmin =
```

```
-1.142054928396837e+00
5.433724812070151e-01
```

```
fmin = -6.496118935491067e+00
```

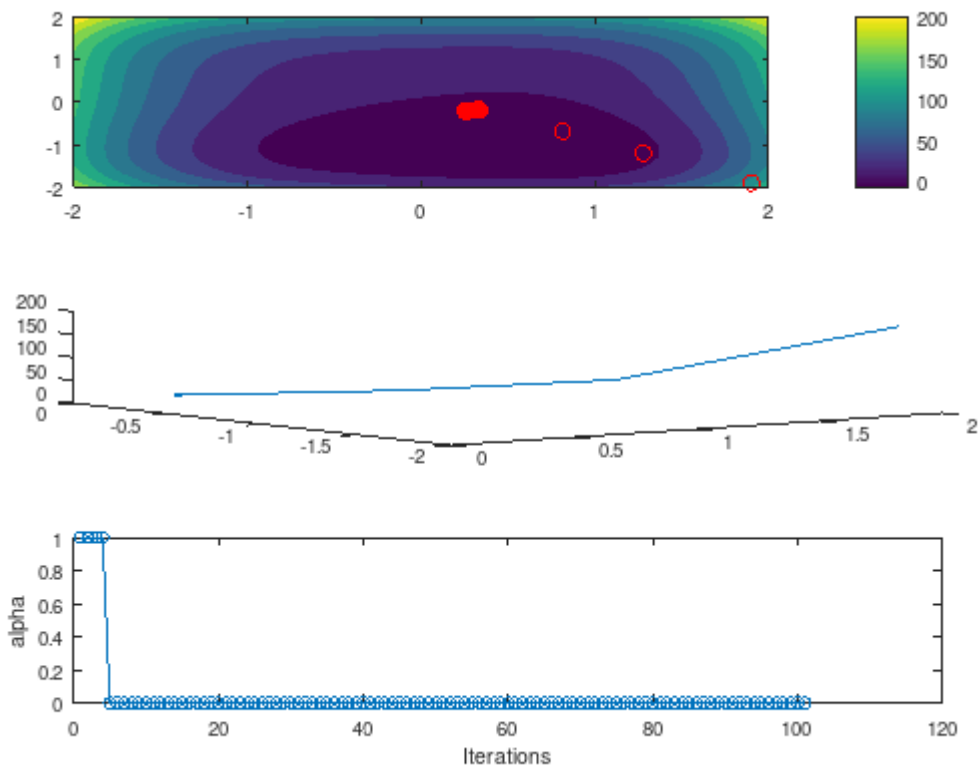


```
In [21]: search_x = -2:0.1:2;
search_y = -2:0.1:2;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = newton(f3_sym, [1.9,-1.9]', is_wolfe_strong, search_x, search_y, c, rh
```

STARTED Line search using newton
 ENDED Line search using newton
 xmin =

3.370260384521531e-01
 -1.856908054665151e-01

fmin = 1.879259020424283e+01

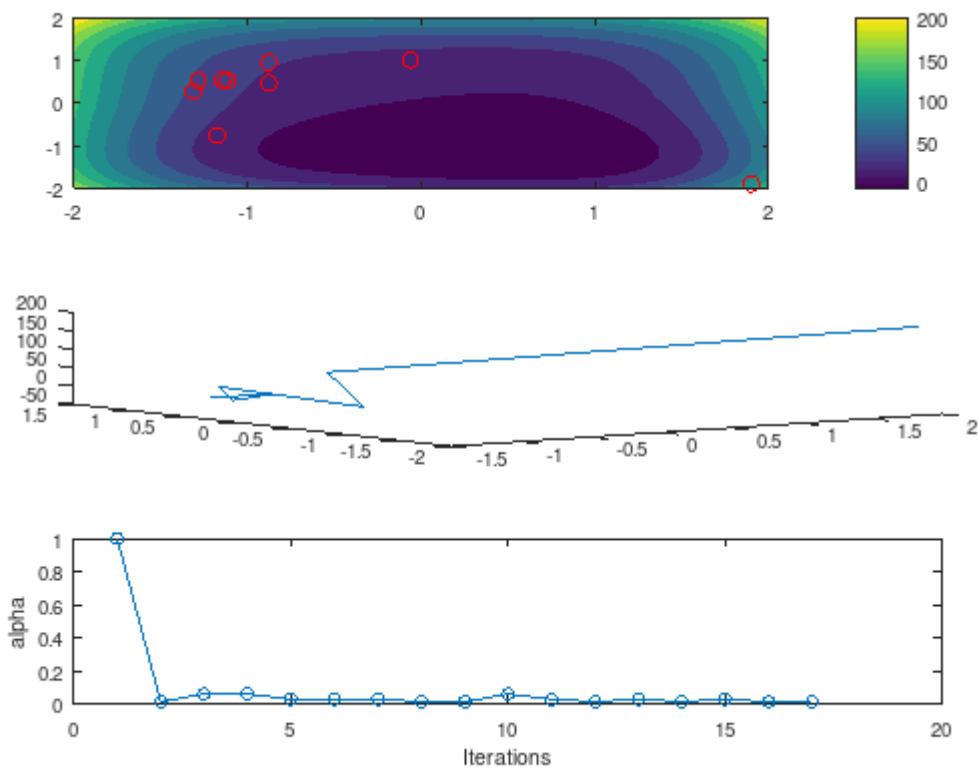


```
In [22]: search_x = -2:0.1:2;
search_y = -2:0.1:2;
[xmin, fmin] = steepest_descent(f3_sym, [1.9,-1.9]', is_backtracking_wolfe_weak, sear
```

STARTED Line search using steepest descent
 ENDED Line search using steepest descent
 xmin =

-1.142054930103962e+00
 5.433724860137114e-01

fmin = -6.496118935491067e+00

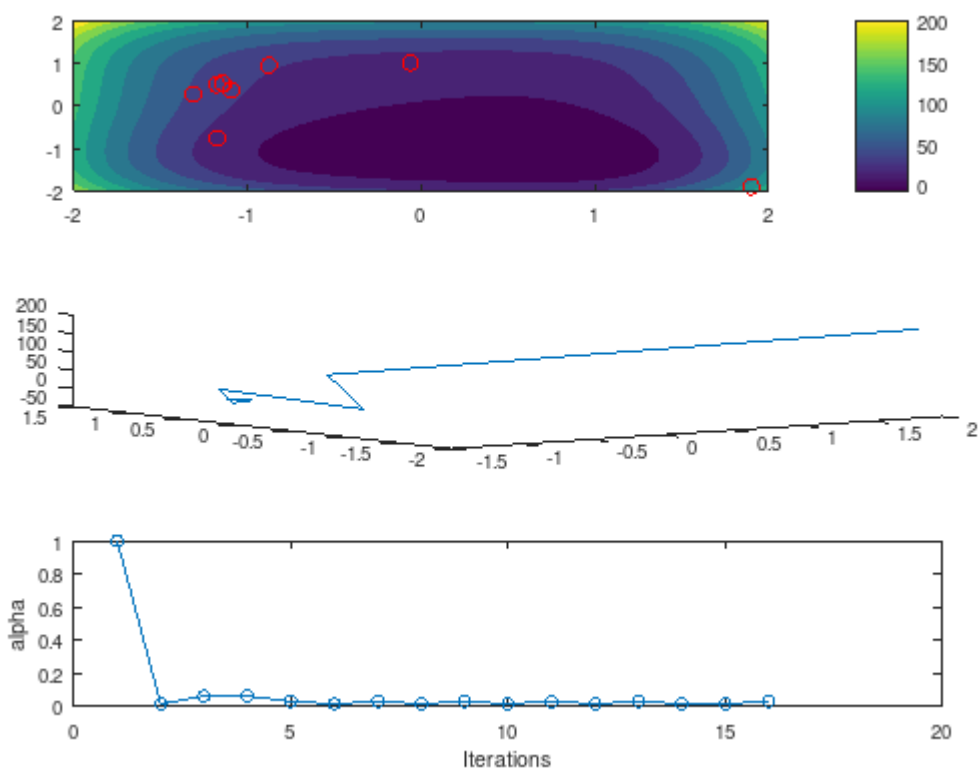


```
In [23]: search_x = -2:0.1:2;
search_y = -2:0.1:2;
[xmin, fmin] = steepest_descent(f3_sym, [1.9, -1.9]', is_backtracking_armijo, search_x
```

STARTED Line search using steepest descent
 ENDED Line search using steepest descent
 xmin =

-1.142054921038707e+00
 5.433724802876779e-01

fmin = -6.496118935491065e+00



```
In [25]: search_x = -2:0.1:2;
search_y = -2:0.1:2;
[xmin, fmin] = steepest_descent(f3_sym, [1.9,-1.9]', is_none, search_x, search_y);
```

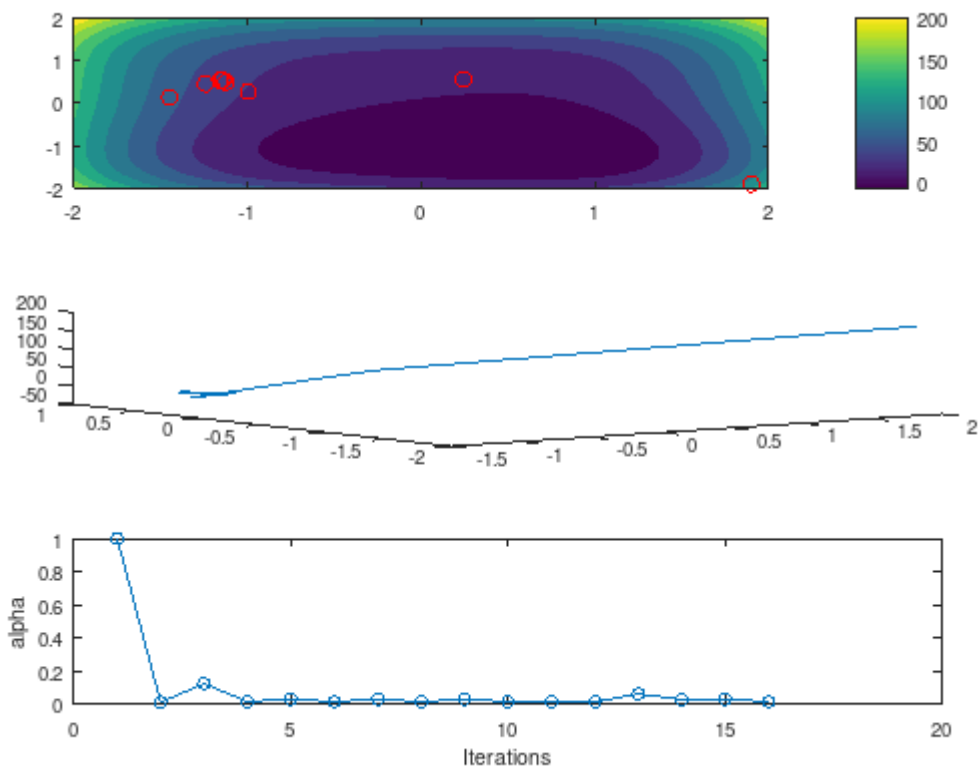
STARTED Line search using steepest descent
error: Failed to converge. Inf value reached
error: called from
steepest_descent at line 45 column 13

```
In [26]: search_x = -2:0.1:2;
search_y = -2:0.1:2;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = steepest_descent(f3_sym, [1.9,-1.9]', is_wolfe_strong, search_x, search_y);
```

STARTED Line search using steepest descent
ENDED Line search using steepest descent
xmin =

-1.142054917024262e+00
5.433724830420348e-01

fmin = -6.496118935491062e+00



```
In [7]: % f(x,y) = (x^2)^(y^2 + 1) + (y^2)^(x^2+1) -- fmin = 0 at x = 0, y = 0 Search domain:

function f = f4_sym()
    syms x y
    f = (x^2)^(y^2 + 1) + (y^2)^(x^2 + 1);
end
```

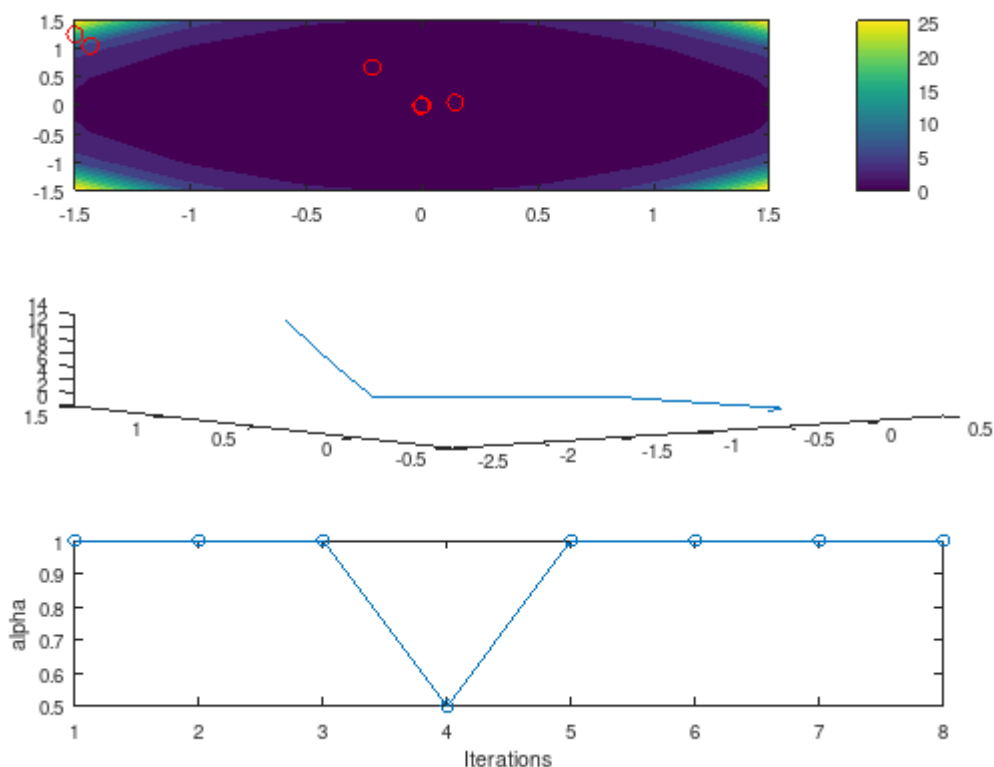
```
In [8]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
[xmin, fmin] = newton(f4_sym, [-1.5,1.25]', is_backtracking_wolfe_weak, search_x, sea
```

Symbolic pkg v3.1.1: Python communication link active, SymPy v1.11.1.
 STARTED Line search using newton
 ENDED Line search using newton
 xmin =

-4.898290906457485e-13

-1.411519028897868e-12

fmin = 2.232318506983620e-24



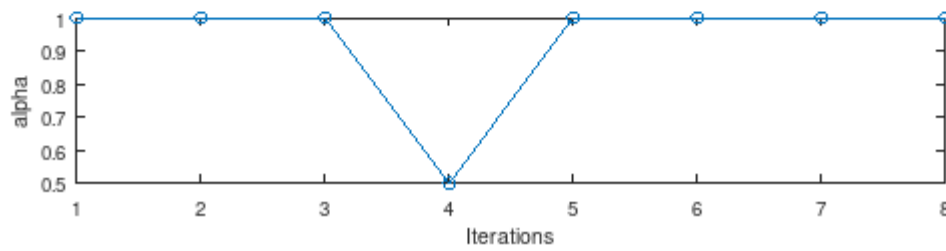
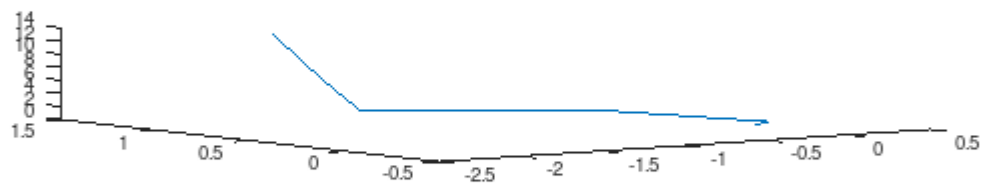
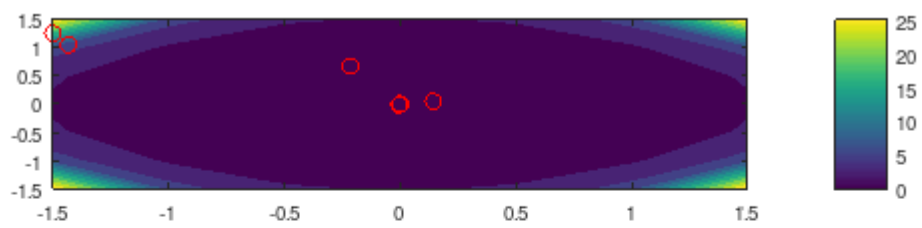
```
In [9]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
[xmin, fmin] = newton(f4_sym, [-1.5,1.25]', is_backtracking_armijo, search_x, search_
```

STARTED Line search using newton
 ENDED Line search using newton
 xmin =

-4.898290906457485e-13

-1.411519028897868e-12

fmin = 2.232318506983620e-24



```
In [10]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
[xmin, fmin] = newton(f4_sym, [-1.5,1.25]', is_none, search_x, search_y);
```


STARTED Line search using newton
warning: matrix singular to machine precision
warning: called from
 linsolve at line 113 column 7
 newton at line 60 column 12

warning: matrix singular to machine precision
warning: called from
 linsolve at line 113 column 7
 newton at line 60 column 12

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warning: matrix singular to machine precision
warning: called from
 linsolve at line 113 column 7

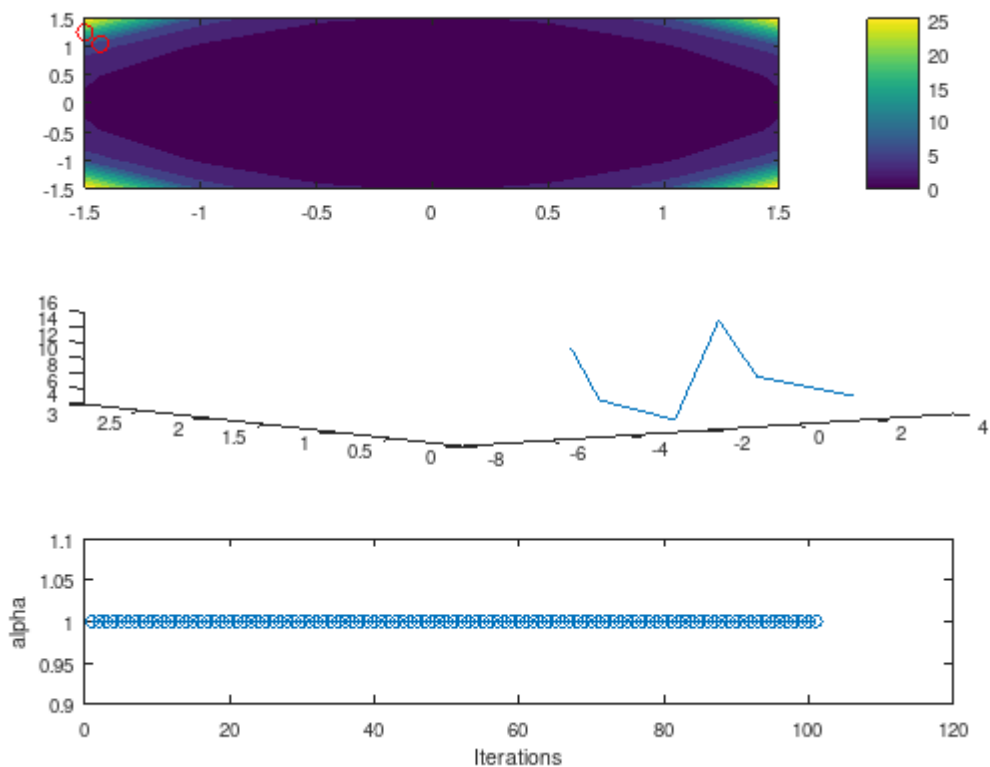
```
warning: matrix singular to machine precision
warning: called from
    linsolve at line 113 column 7
    newton at line 60 column 12
```

```
warning: matrix singular to machine precision
warning: called from
    linsolve at line 113 column 7
    newton at line 60 column 12
```

```
ENDED Line search using newton
xmin =
```

```
NaN
NaN
```

```
fmin = NaN
```



```
In [ ]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = newton(f4_sym, [-1.5,1.25]', is_wolfe_strong, search_x, search_y, c, r
```

```
In [12]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
[xmin, fmin] = steepest_descent(f4_sym, [-1.5,1.25]', is_backtracking_wolfe_weak, sea
```


STARTED Line search using steepest descent

Traceback (most recent call last):

```
File "<stdin>", line 31, in octoutput
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2871, in pretty
    return pp.doprint(expr)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 66, in doprint
    return self._print(expr).render(**self._settings)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 1933, in _print_Add
    pforms.append(self._print(term))
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2011, in _print_Mul
    a = [self._print(ai) for ai in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2011, in <listcomp>
    a = [self._print(ai) for ai in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2107, in _print_Rational
    result = self._print_numer_denom(expr.p, expr.q)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2093, in _print_numer_denom
    return prettyForm(str(p))
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_max_str_digits() to increase the limit
```

During handling of the above exception, another exception occurred:

Traceback (most recent call last):

```
File "<stdin>", line 2, in <module>
File "<stdin>", line 12, in octoutput_drv
File "<stdin>", line 34, in octoutput
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/core/_print_helpers.py", line 29, in __str__
    return sstr(self, order=None)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 1000, in sstr
    s = p.doprint(expr)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 292, in doprint
    return self._str(self._print(expr))
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 56, in _print_Add
    t = self._print(term)
```

```

y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 366, in _print_Mul
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 366, in <listcomp>
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 37, in parenthesize
    return self._print(item)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 681, in _print_Integer
    return str(expr.p)
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_m
ax_str_digits() to increase the limit
error: Python exception: ValueError: Exceeds the limit (4300) for integer string conv
ersion; use sys.set_int_max_str_digits() to increase the limit
    occurred while copying variables from Python.
    Try "sympref reset" and repeat your command?
    (consider filing an issue at https://github.com/cbm755/octsympy/issues)
error: called from
    pycall_sympy__ at line 192 column 5
    subs at line 269 column 5
    sym2fun at line 3 column 9
    steepest_descent>@<anonymous> at line 37 column 14
    backtracking_wolfe_weak>armijo_condition at line 26 column 7
    backtracking_wolfe_weak at line 8 column 58
    step_size at line 12 column 14
    steepest_descent at line 55 column 14

```

```

In [13]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
[xmin, fmin] = steepest_descent(f4_sym, [-1.5,1.25]', is_backtracking_armijo, search_

```

STARTED Line search using steepest descent

Traceback (most recent call last):

```
File "<stdin>", line 31, in octoutput
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2871, in pretty
    return pp.doprint(expr)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 66, in doprint
    return self._print(expr).render(**self._settings)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 1933, in _print_Add
    pforms.append(self._print(term))
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2011, in _print_Mul
    a = [self._print(ai) for ai in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2011, in <listcomp>
    a = [self._print(ai) for ai in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2107, in _print_Rational
    result = self._print_numer_denom(expr.p, expr.q)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2093, in _print_numer_denom
    return prettyForm(str(p))
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_max_str_digits() to increase the limit
```

During handling of the above exception, another exception occurred:

Traceback (most recent call last):

```
File "<stdin>", line 2, in <module>
File "<stdin>", line 12, in octoutput_drv
File "<stdin>", line 34, in octoutput
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/core/_print_helpers.py", line 29, in __str__
    return sstr(self, order=None)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 1000, in sstr
    s = p.doprint(expr)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 292, in doprint
    return self._str(self._print(expr))
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 56, in _print_Add
    t = self._print(term)
```

```

y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 366, in _print_Mul
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 366, in <listcomp>
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 37, in parenthesize
    return self._print(item)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 681, in _print_Integer
    return str(expr.p)
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_m
ax_str_digits() to increase the limit
error: Python exception: ValueError: Exceeds the limit (4300) for integer string conv
ersion; use sys.set_int_max_str_digits() to increase the limit
    occurred while copying variables from Python.
    Try "sympref reset" and repeat your command?
    (consider filing an issue at https://github.com/cbm755/octsympy/issues)
error: called from
    pycall_sympy__ at line 192 column 5
    subs at line 269 column 5
    sym2fun at line 3 column 9
    steepest_descent>@<anonymous> at line 37 column 14
    backtracking_armijo>armijo_condition at line 19 column 7
    backtracking_armijo at line 6 column 11
    step_size at line 7 column 14
    steepest_descent at line 55 column 14

```

```

In [14]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
[xmin, fmin] = steepest_descent(f4_sym, [-1.5,1.25]', is_none, search_x, search_y);

```

STARTED Line search using steepest descent

Traceback (most recent call last):

```
File "<stdin>", line 31, in octoutput
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 2871, in pretty
    return pp.doprint(expr)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 66, in doprint
    return self._print(expr).render(**self._settings)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 764, in _print_MatrixBase
    D = self._print_matrix_contents(e)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 702, in _print_matrix_contents
    Ms[i, j] = self._print(M[i, j])
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 1933, in _print_Add
    pforms.append(self._print(term))
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 2011, in _print_Mul
    a = [self._print(ai) for ai in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 2011, in <listcomp>
    a = [self._print(ai) for ai in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 2107, in _print_Rational
    result = self._print_numer_denom(expr.p, expr.q)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pre
ty.py", line 2093, in __print_numer_denom
    return prettyForm(str(p))
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_m
ax_str_digits() to increase the limit
```

During handling of the above exception, another exception occurred:

Traceback (most recent call last):

```
File "<stdin>", line 2, in <module>
File "<stdin>", line 12, in octoutput_drv
File "<stdin>", line 34, in octoutput
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/matrices/matrices.p
y", line 852, in __str__
    return "Matrix(%s)" % str(self.tolist())
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/core/_print_helpers.
py", line 29, in __str__
    return sstr(self, order=None)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
```

```

ne 1000, in sstr
    s = p.doprint(expr)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 292, in doprint
    return self._str(self._print(expr))
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 56, in _print_Add
    t = self._print(term)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 366, in _print_Mul
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 366, in <listcomp>
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 37, in parenthesize
    return self._print(item)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 681, in _print_Integer
    return str(expr.p)
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_max_str_digits() to increase the limit
error: Python exception: ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_max_str_digits() to increase the limit
    occurred while copying variables from Python.
    Try "sympref reset" and repeat your command?
    (consider filing an issue at https://github.com/cbm755/octsympy/issues)
error: called from
    pycall_sympy__ at line 192 column 5
    subs at line 269 column 5
    multidim_grad at line 31 column 9
    steepest_descent>@<anonymous> at line 38 column 19
    steepest_descent at line 48 column 12

```

```

In [15]: search_x = -1.5:0.5:1.5;
search_y = -1.5:0.5:1.5;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = steepest_descent(f4_sym, [-1.5,1.25]', is_wolfe_strong, search_x, sear

```

```

STARTED Line search using steepest descent
Traceback (most recent call last):
  File "<stdin>", line 31, in octoutput
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2871, in pretty
    return pp.doprint(expr)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 66, in doprint
    return self._print(expr).render(**self._settings)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 1933, in _print_Add
    pforms.append(self._print(term))
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2011, in _print_Mul
    a = [self._print(ai) for ai in a]
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2011, in <listcomp>
    a = [self._print(ai) for ai in a]
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2107, in _print_Rational
    result = self._print_numer_denom(expr.p, expr.q)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/pretty/pretty.py", line 2093, in _print_numer_denom
    return prettyForm(str(p))
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_max_str_digits() to increase the limit

```

During handling of the above exception, another exception occurred:

```

Traceback (most recent call last):
  File "<stdin>", line 2, in <module>
  File "<stdin>", line 12, in octoutput_drv
  File "<stdin>", line 34, in octoutput
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/core/_print_helpers.py", line 29, in __str__
    return sstr(self, order=None)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 372, in __call__
    return self._wrapped__(*args, **kwargs)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", line 1000, in sstr
    s = p.doprint(expr)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 292, in doprint
    return self._str(self._print(expr))
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.py", line 331, in _print
    return printmethod(expr, **kwargs)
  File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li

```

```

t = self._print(term)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 366, in _print_Mul
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 366, in <listcomp>
    a_str = [self.parenthesize(x, prec, strict=False) for x in a]
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 37, in parenthesize
    return self._print(item)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/printer.p
y", line 331, in _print
    return printmethod(expr, **kwargs)
File "/home/thodkatz/.local/lib/python3.10/site-packages/sympy/printing/str.py", li
ne 681, in _print_Integer
    return str(expr.p)
ValueError: Exceeds the limit (4300) for integer string conversion; use sys.set_int_m
ax_str_digits() to increase the limit
error: Python exception: ValueError: Exceeds the limit (4300) for integer string conv
ersion; use sys.set_int_max_str_digits() to increase the limit
occurred while copying variables from Python.
Try "sympref reset" and repeat your command?
(consider filing an issue at https://github.com/cbm755/octsympy/issues)
error: called from
    pycall_sympy__ at line 192 column 5
    subs at line 269 column 5
    sym2fun at line 3 column 9
    steepest_descent>@<anonymous> at line 37 column 14
    wolfe_strong at line 16 column 13
    step_size at line 21 column 14
    steepest_descent at line 55 column 14

```

```

In [3]: % f(x,y,z)=(x^2+y^3-z^4)^2+(2*x*y*z)^2+(2*x*y-3*y*z+x*z)^2 -init x=y=z=10-obj =0.0000

function f = f5_sym()
    syms x y z
    f = (x^2 + y^3 - z^4)^2 + (2*x*y*z)^2 + (2*x*y-3*y*z+x*z)^2;
end

```

```

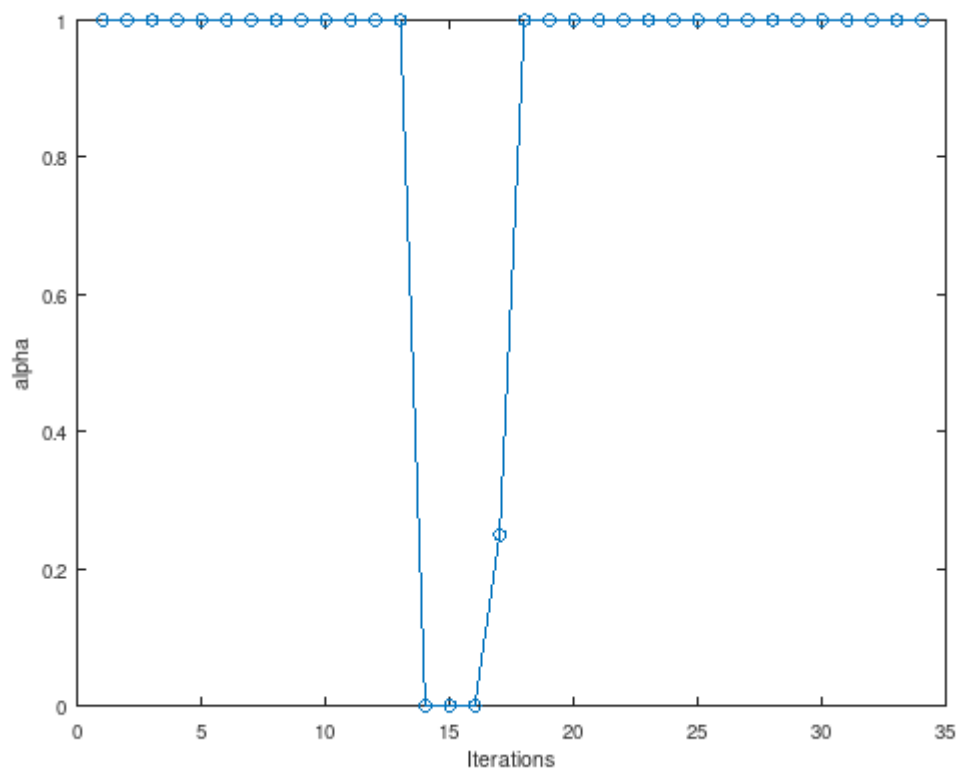
In [4]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = newton(f5_sym, [10,10,10]', is_backtracking_wolfe_weak, search_x, sear

```

Symbolic pkg v3.1.1: Python communication link active, SymPy v1.11.1.
STARTED Line search using newton
ENDED Line search using newton
xmin =

-2.126482159228893e-05
-7.097574255828430e-06
9.006911588552714e-02

fmin = 4.331130112795951e-09

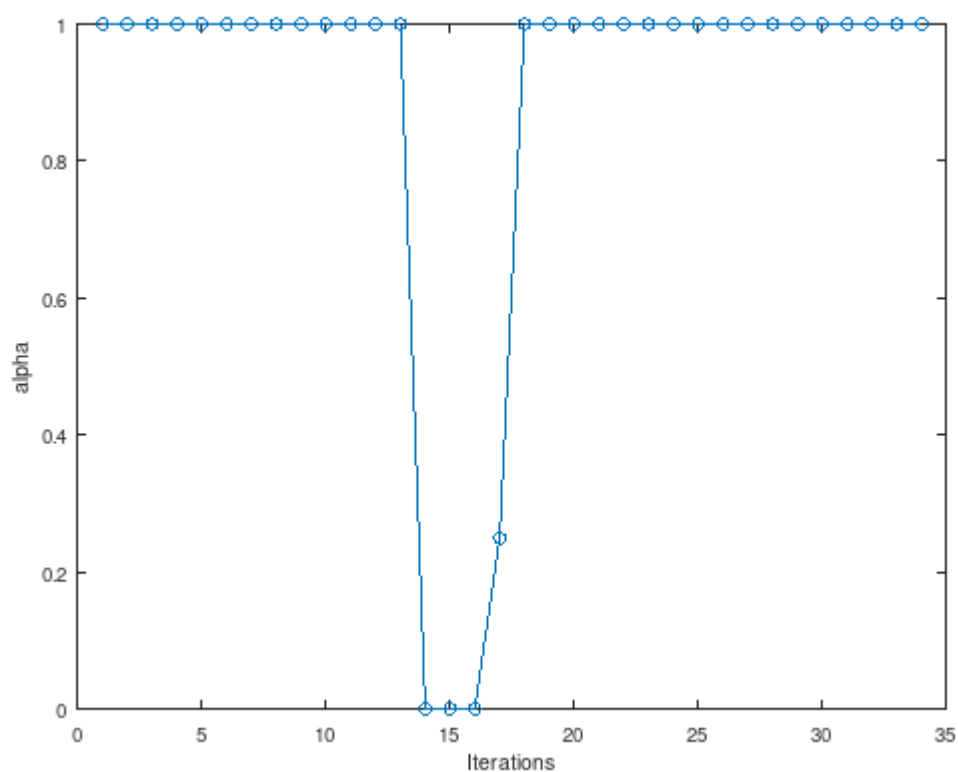


```
In [5]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = newton(f5_sym, [10,10,10]', is_backtracking_armijo, search_x, search_y
```

```
STARTED Line search using newton
ENDED Line search using newton
xmin =
```

```
-2.126482159228893e-05
-7.097574255828430e-06
9.006911588552714e-02
```

```
fmin = 4.331130112795951e-09
```

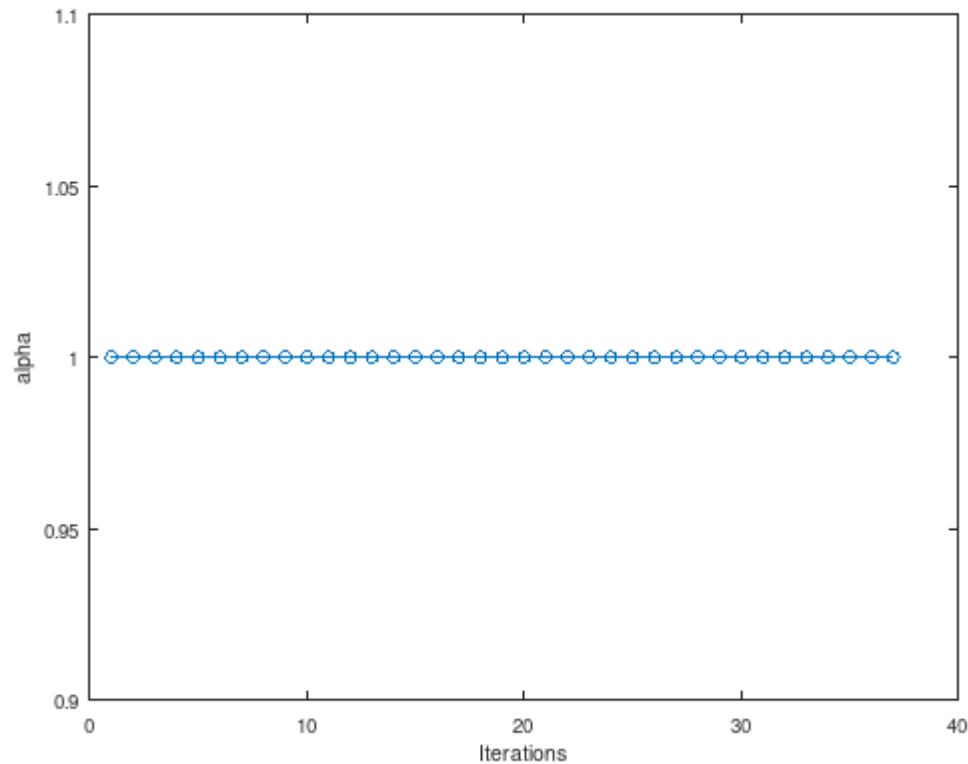


```
In [6]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = newton(f5_sym, [10,10,10]', is_none, search_x, search_y);
```

STARTED Line search using newton
 ENDED Line search using newton
 xmin =

```
2.525601052449970e-04
3.792558884054644e-02
1.684963639464687e-04
```

fmin = 2.982697279570769e-09

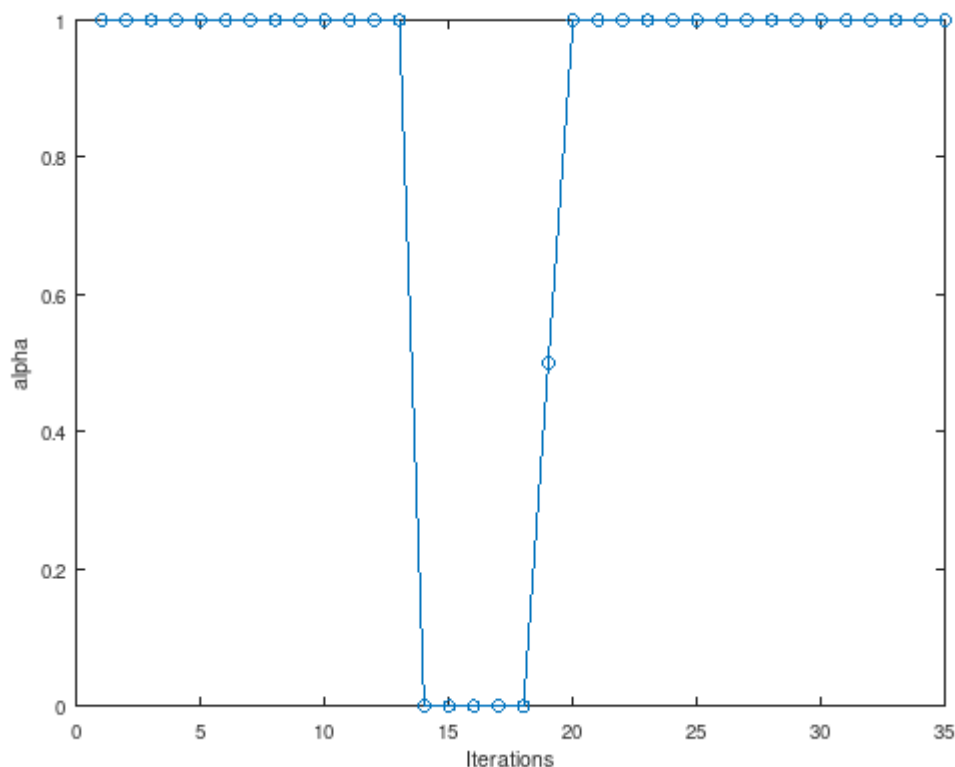


```
In [7]: search_x = -1:1:1;
search_y = -1:1:1;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = newton(f5_sym, [10,10,10]', is_wolfe_strong, search_x, search_y, c, rh
```

STARTED Line search using newton
 ENDED Line search using newton
 xmin =

```
2.167392528313391e-03
-2.296477871401249e-03
3.761317198771993e-03
```

fmin = 6.032867139200067e-10



```
In [8]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = steepest_descent(f5_sym, [10,10,10]', is_backtracking_wolfe_weak, sear
```

STARTED Line search using steepest descent
error: Failed to converge. Inf value reached
error: called from
 steepest_descent at line 45 column 13

```
In [9]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = steepest_descent(f5_sym, [10,10,10]', is_backtracking_armijo, search_x
```

STARTED Line search using steepest descent
error: Failed to converge. Inf value reached
error: called from
 steepest_descent at line 45 column 13

```
In [10]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = steepest_descent(f5_sym, [10,10,10]', is_none, search_x, search_y);
```

STARTED Line search using steepest descent
error: Failed to converge. Inf value reached
error: called from
 steepest_descent at line 45 column 13

```
In [11]: search_x = -1:1:1;
search_y = -1:1:1;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = steepest_descent(f5_sym, [10,10,10]', is_wolfe_strong, search_x, searc
```

STARTED Line search using steepest descent
 error: Failed to converge. Inf value reached
 error: called from
 steepest_descent at line 45 column 13

```
In [21]: % f(x,y,z,k)=(x-1)^2+ (x-y)^2 + (y-z)^2 + (z-k)^2 -init x=y=z=k=0.1 -obj =1.13719e-10

function f = f6_sym()
    syms x y z k
    f = (x-1)^2 + (x-sqrt(y))^2 + (y-sqrt(z))^2 + (z-sqrt(k))^2;
end
```

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = newton(f6_sym, [0.1,0.1,0.1,0.1]', is_backtracking_wolfe_weak, search_x,
```

STARTED Line search using newton

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = newton(f6_sym, [0.1,0.1,0.1,0.1]', is_backtracking_armijo, search_x, s
```

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = newton(f6_sym, [0.1,0.1,0.1,0.1]', is_none, search_x, search_y);
```

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = newton(f6_sym, [0.1,0.1,0.1,0.1]', is_wolfe_strong, search_x, search_y
```

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = steepest_descent(f6_sym, [0.1,0.1,0.1,0.1]', is_backtracking_wolfe_wea
```

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = steepest_descent(f6_sym, [0.1,0.1,0.1,0.1]', is_backtracking_armijo, s
```

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
[xmin, fmin] = steepest_descent(f6_sym, [0.1,0.1,0.1,0.1]', is_none, search_x, search
```

```
In [ ]: search_x = -1:1:1;
search_y = -1:1:1;
c = [1e-4 0.9];
rho = 2;
[xmin, fmin] = steepest_descent(f6_sym, [0.1,0.1,0.1,0.1]', is_wolfe_strong, search_x
```