#### Section 4: Cross-seasonal models & Lincoln estimates

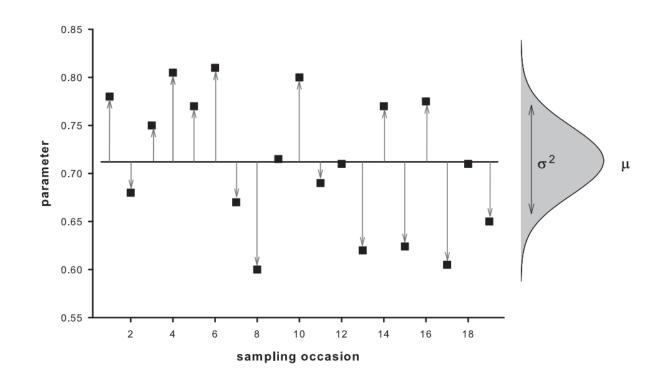
#### Model

 $marr \sim multinomial(rel, p)$ 

logit(
$$\mathbf{S}$$
) =  $\mu_S + \varepsilon_{S,t}$   
logit( $\mathbf{f}$ ) =  $\mu_f + \varepsilon_{f,t}$ 

#### **Priors**

 $\varepsilon_{S,t} \sim \text{Normal}(0, \sigma_S^2)$   $\varepsilon_{f,t} \sim \text{Normal}(0, \sigma_f^2)$   $\sigma_S \sim \text{Gamma}(1,1)$  $\sigma_f \sim \text{Gamma}(1,1)$ 

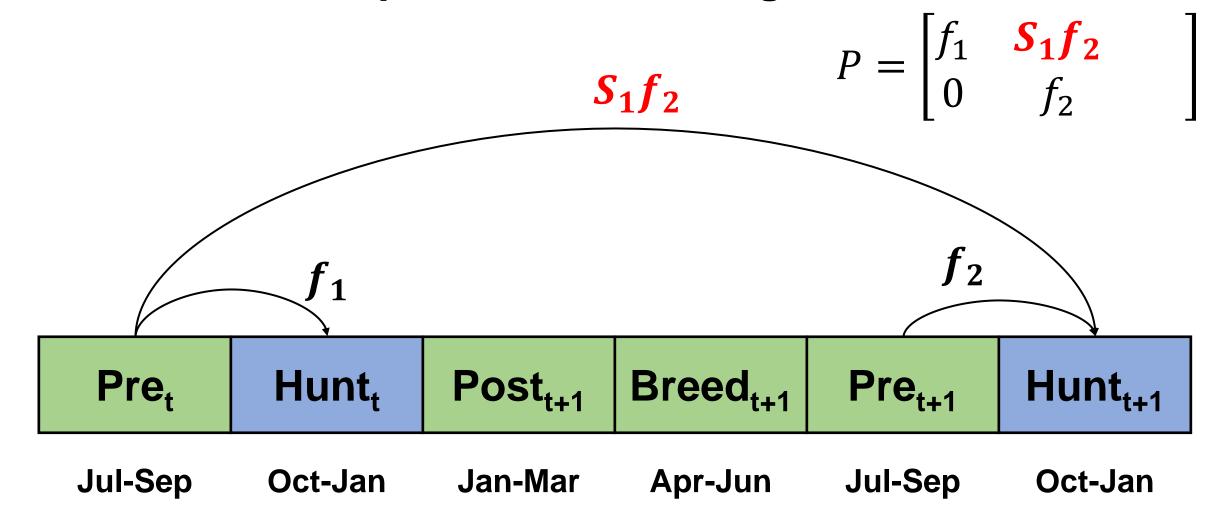


### **Cross-seasonal models**

## Models based on pre-season banding

$$P = \begin{bmatrix} f_1 & S_1 f_2 & S_1 S_2 f_3 & S_1 S_2 S_3 f_4 & S_1 S_2 S_3 S_4 f_5 & 1 - \sum_{j=1}^{n} P_{1,1:5} \\ 0 & f_2 & S_2 f_3 & S_2 S_3 f_4 & S_2 S_3 S_4 f_5 & 1 - \sum_{j=1}^{n} P_{2,1:5} \\ 0 & 0 & f_3 & S_3 f_4 & S_3 S_4 f_5 & 1 - \sum_{j=1}^{n} P_{3,1:5} \\ 0 & 0 & 0 & f_4 & S_4 f_5 & 1 - \sum_{j=1}^{n} P_{4,1:5} \\ 0 & 0 & 0 & 0 & f_5 & 1 - \sum_{j=1}^{n} P_{5,1:5} \end{bmatrix}$$

## Models based on pre-season banding

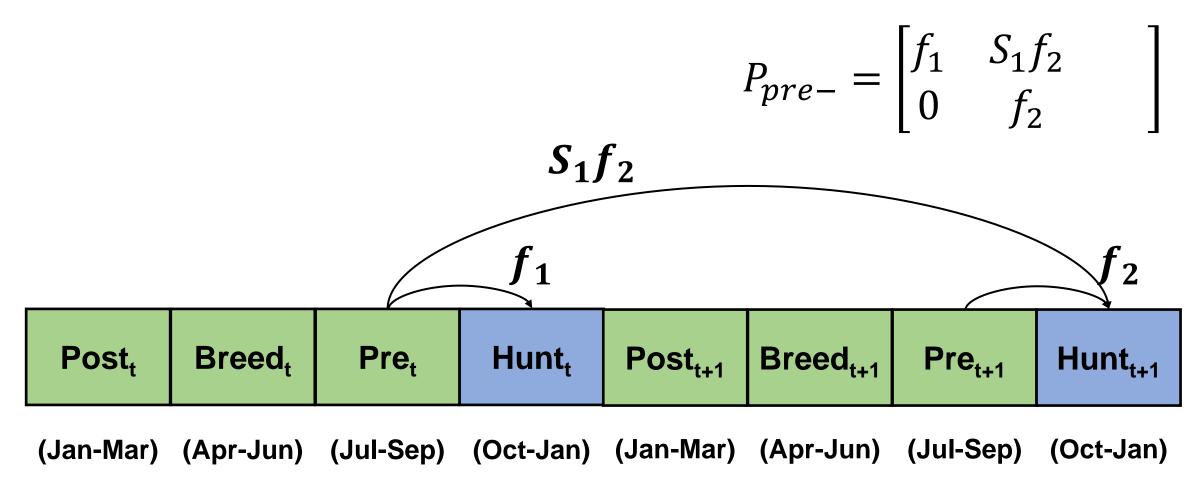


$$P_{pre-} = \begin{bmatrix} f_1 & \mathbf{S_1 f_2} \\ 0 & f_2 \end{bmatrix}$$

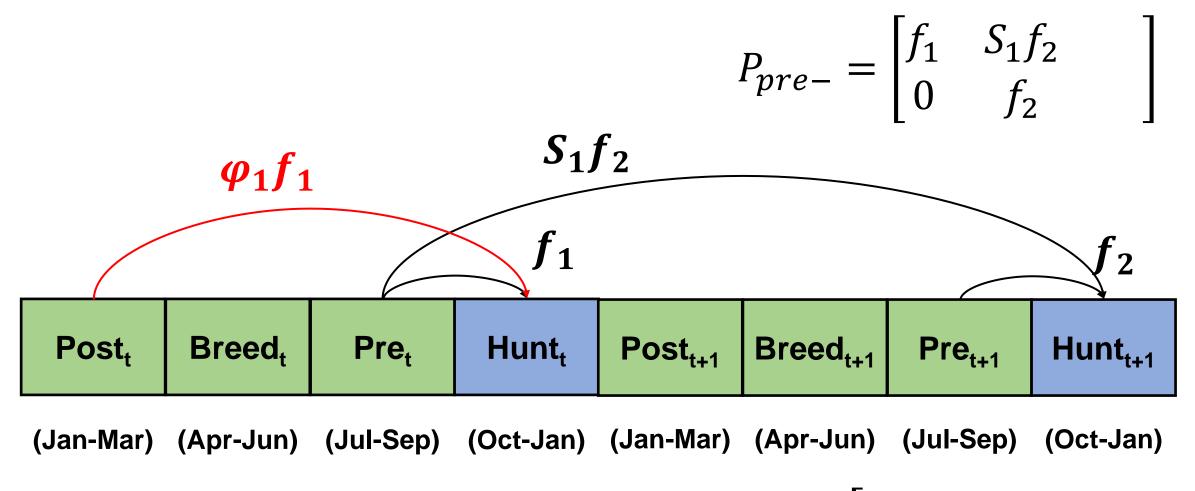
$$\mathbf{S_1 f_2}$$

$$\mathbf{Post_t} \quad \mathbf{Breed_t} \quad \mathbf{Pre_t} \quad \mathbf{Hunt_t} \quad \mathbf{Post_{t+1}} \quad \mathbf{Breed_{t+1}} \quad \mathbf{Pre_{t+1}} \quad \mathbf{Hunt_{t+1}}$$

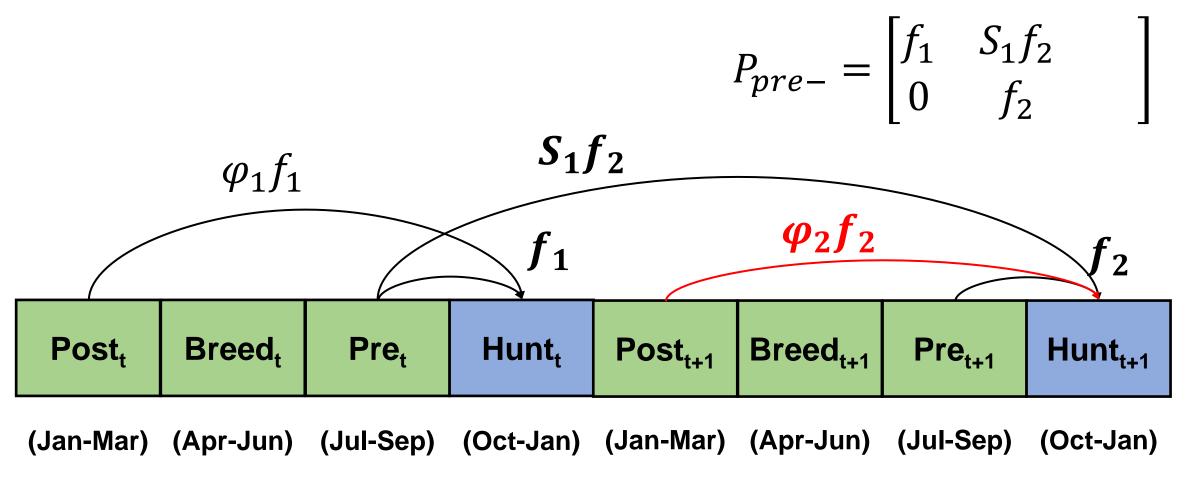
$$(Jan-Mar) \quad (Apr-Jun) \quad (Jul-Sep) \quad (Oct-Jan) \quad (Jan-Mar) \quad (Apr-Jun) \quad (Jul-Sep) \quad (Oct-Jan)$$



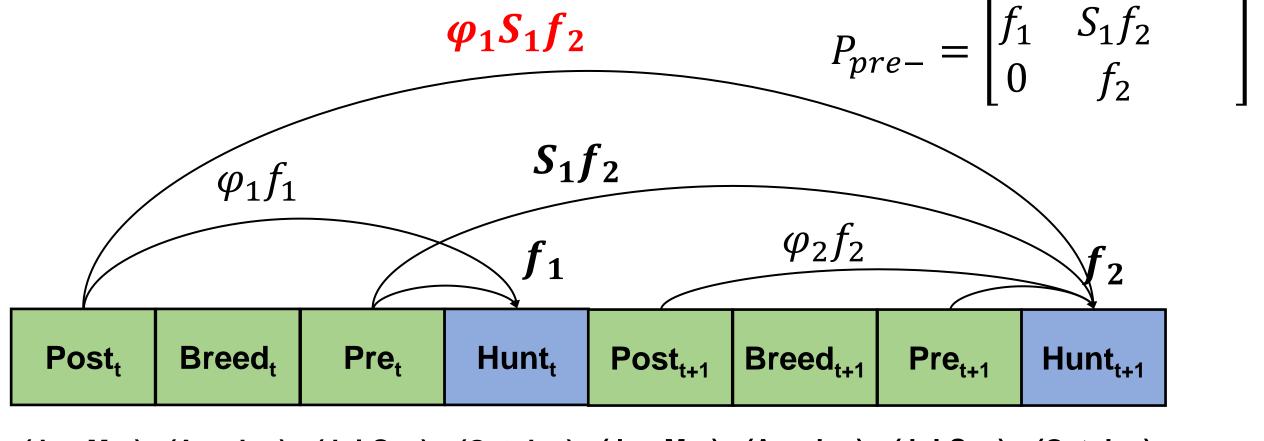
$$P_{post-} = \begin{bmatrix} \varphi_1 f_1 & \varphi_1 S_1 f_2 \\ 0 & \varphi_2 f_2 \end{bmatrix}$$



$$P_{post-} = \begin{bmatrix} \boldsymbol{\varphi_1 f_1} & \varphi_1 S_1 f_2 \\ 0 & \varphi_2 f_2 \end{bmatrix}$$



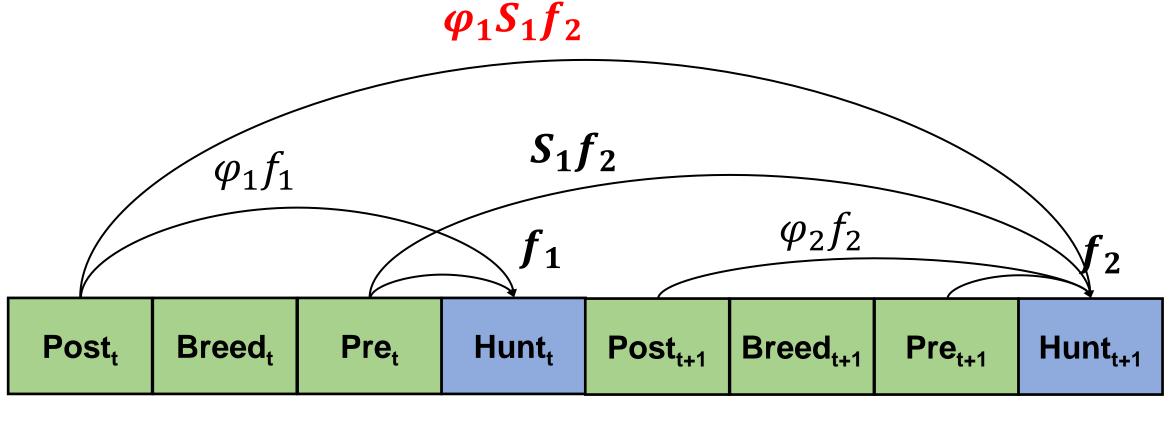
$$P_{post-} = \begin{bmatrix} \varphi_1 f_1 & \varphi_1 S_1 f_2 \\ 0 & \varphi_2 f_2 \end{bmatrix}$$



(Jan-Mar) (Apr-Jun) (Jul-Sep) (Oct-Jan) (Jan-Mar) (Apr-Jun) (Jul-Sep) (Oct-Jan)

$$P_{post-} = \begin{bmatrix} \varphi_1 f_1 & \varphi_1 S_1 f_2 \\ 0 & \varphi_2 f_2 \end{bmatrix}$$

#### Survival



(Jan-Mar) (Apr-Jun) (Jul-Sep) (Oct-Jan) (Jan-Mar) (Apr-Jun) (Jul-Sep) (Oct-Jan)

$$S_1 = \varphi_2 \times \omega_1 (1 - \kappa_1)$$

## **Lincoln estimates**

# 50 is 10% of <u>500</u>

$$f_2 = \frac{100}{1000} = 0.1$$

$$50 = 500 * 0.1$$

$$500 = 1000 * S_1$$

If we shoot 50 birds banded in the first year in year two, and we know we're shooting 10% of the ducks, then how many were available to be shot?

<u>500</u>

If there are 1m birds, and we shoot 10% of them...

How many will we shoot?

If there are 1m birds, and we shoot 10% of them...

How many will we shoot?

100k

What if...

We estimate total harvest was 100k

And we estimate we harvested 10% of the birds?

How many birds are there?

What if...

We estimate total harvest was 100k

And we estimate we harvested 10% of the birds?

How many birds are there?

1m

### **Lincoln estimates**

$$N_t = \frac{H_t}{h_t}$$

$$f_t = h_t \times \rho_t$$