

## Bernsteins' s Algorithm on Employees Table

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We will be using Bernsteins' algorithm to build/check the schema for Employees. We will start with only a list of attributes that belong to the table and a list of functional dependencies in the table.

### Step 1:

List of attributes:

- UserId
- BranchID
- EmployeeMonthlySalary
- EmployeeSINNumber
- EmployeePermissions

**F = {**

**UserID** -> {BranchID, EmployeeMonthlySalary, EmployeeSINNumber  
EmployeePermissions},

**EmployeeSINNumber** -> UserID,

**}**

### Step 2a:

**F = {**

**UserID** -> BranchID,

**UserID** -> EmployeeMonthlySalary,

**UserID** -> EmployeeSINNumber

**UserID** -> EmployeePermissions,

**EmployeeSINNumber** -> UserID,

**}**

Now we perform closure on the determinant of each functional dependency to remove redundant FD's

1. We determine that **UserID** -> BranchID is not a redundant FD. If we modify **F** by removing **UserID** -> BranchID (**MF**) and then subsequently calculate the closure of UserID using **MF**, BranchID is not in that closure.
2. We determine that **UserID** -> EmployeeMonthlySalary is not a redundant FD. If we modify **F** by removing **UserID** -> EmployeeMonthlySalary (**MF**) and then subsequently calculate the

closure of UserID using **MF**, EmployeeMonthlySalary is not in that closure.

3. We determine **UserID**  $\rightarrow$  EmployeeSINNumber is not a redundant FD. If we modify **F** by removing **UserID**  $\rightarrow$  EmployeeSINNumber (**MF**) and then subsequently calculate the closure of UserID using **MF**, EmployeeSINNumber is not in that closure.
4. We determine **UserID**  $\rightarrow$  EmployeePermissions is not a redundant FD. If we modify **F** by removing **UserID**  $\rightarrow$  EmployeePermissions (**MF**) and then subsequently calculate the closure of UserID using **MF**, EmployeePermissions is not in that closure.

### Step 2b:

In step 2b we will check if each FD itself is redundant.

Here is our current F:

```
F = {  
  
    UserID  $\rightarrow$  BranchID,  
    UserID  $\rightarrow$  EmployeeMonthlySalary,  
    UserID  $\rightarrow$  EmployeeSINNumber  
    UserID  $\rightarrow$  EmployeePermissions,  
    EmployeeSINNumber  $\rightarrow$  UserID,  
}
```

Checking each FD involves the following steps:

1. Eliminate an attribute A on the LHS of one of the FDs
2. Look at the remainder Q of attributes on the LHS for that FD
3. Find Q<sup>+</sup> in the original set of FDs
4. If Q<sup>+</sup> contains the RHS of the FD in question then the attribute A is redundant

However, this process is unnecessary because each determinant in our current F is only 1 attribute. Therefore, no FD's are redundant and step 2b is completed implicitly

### Step 3:

Now we must determine the keys. An attribute is a key if its closure is every attribute initially listed in Step 1.

```
UserID + = {UserID, BranchID, EmployeeMonthlySalary, EmployeeSINNumber  
            EmployeePermissions}
```

```
EmployeeSINNumber + = {UserID, BranchID,  
EmployeeMonthlySalary, EmployeeSINNumber  
EmployeePermissions}
```

Therefore, UserID and EmployeeSINNumber are the keys. We don't need to check if the subsets of {UserID} and {EmployeeSINNumber} are keys.

#### Step 4:

We combine the FD's with the same left hand side:

```
F = {  
  
    UserID -> BranchID,  
    UserID -> EmployeeMonthlySalary,  
    UserID -> EmployeeSINNumber  
    UserID -> EmployeePermissions,  
    EmployeeSINNumber -> UserID,  
}
```

Below is the final F after combining:

```
F = {  
  
    UserID -> {BranchID, EmployeeMonthlySalary, EmployeeSINNumber  
EmployeePermissions},  
  
    EmployeeSINNumber -> UserID,  
}
```