

11.13 (a) Assume the wire is along the z -direction, then

$$\vec{E}' = \frac{\lambda_0}{r'} \hat{r}, \quad \vec{B}' = 0.$$

Where r' is the distance from the wire. Then, apply the Lorentz transform for $\vec{\beta} = \vec{v}/c$ along z -direction.

We have $\vec{E} = \gamma \vec{E}' = \frac{\gamma \lambda_0}{r} \hat{r}$, $\vec{B} = \gamma \vec{\beta} \times \vec{E}' = \frac{\gamma \beta \lambda_0}{r} \hat{\phi}$. Here, $r' = r$ as it is the transverse distance.

(b) In the lab frame, the wire is moving in the z -direction with velocity \vec{v} . Then, unit length in the frame moving with the wire becomes $\sqrt{1-\beta^2}$ in the lab frame. Therefore, the charge density in the lab frame becomes $\lambda_0 / \sqrt{1-\beta^2} = \gamma \lambda_0$, and the current density is $\gamma \lambda_0 \vec{v}$. In the rest frame, the charge density

is λ_0 and the current density is 0.

(c) The electric and magnetic field can be easily determined due to cylindrical symmetry.

$$\vec{E} = \frac{\gamma \lambda_0}{r} \hat{r}, \quad \vec{B} = \frac{\gamma \beta \lambda_0}{r} \hat{\phi},$$

identical to those part (a).