

8.3 1a) The magnetic field is constant in the line, and  $E = \sqrt{\frac{\mu}{\epsilon}} H_0$ , then

$$P = \frac{1}{2} \int E H da = \frac{ab}{2} \sqrt{\frac{\mu}{\epsilon}} |H_0|^2.$$

The energy attenuation is

$$-\frac{dP}{dz} = \frac{1}{2\sigma\delta} \oint |\vec{n} \times \vec{H}_t|^2 dl = \frac{1}{2\sigma\delta} \cdot 2H_0^2 b = \frac{H_0^2 b}{\sigma\delta},$$

$$\text{and } \gamma = -\frac{1}{2P} \frac{dP}{dz} = \frac{1}{2\sigma\delta} \sqrt{\frac{\epsilon}{\mu}}$$

The voltage is  $V = E \cdot a = \sqrt{\frac{\mu}{\epsilon}} H_0 a$ , and the current is  $I = H_0 b \cdot 2$ .

$$Z_0 = \frac{V}{I} = \sqrt{\frac{\mu}{\epsilon}} \frac{a}{b}$$

$$\text{The resistance is } R = \frac{2}{I^2} \left| \frac{dP}{dz} \right| = \frac{2}{\sigma\delta b}$$

The energy in the wire is  $W_{\text{wire}} = \frac{1}{2} \mu H_0^2 ab$ , in the strip, it is given by

$$W_{\text{strip}} = 2 \cdot \frac{\mu_c}{2} \cdot b \cdot \int_0^{+\infty} H_0^2 e^{-2z/\delta} dz = \frac{\mu_c \delta}{2} H_0^2 b. \text{ Then,}$$

$$L = \frac{2}{I^2} (W_{\text{wire}} + W_{\text{strip}}) = \frac{\mu a + \mu_c \delta}{b}$$