

11.3 Using the rapidity parameterization, the first transformation is

$$x'_0 = x_0 \cosh \xi_1 - x_1 \sinh \xi_1,$$

$$x'_1 = -x_0 \sinh \xi_1 + x_1 \cosh \xi_1,$$

With $\tanh \xi_1 = v_1/c$. Then, a second transformation, with $\tanh \xi_2 = v_2/c$, the 0-component is given by

$$x''_0 = x'_0 \cosh \xi_2 - x'_1 \sinh \xi_2$$

$$= (x_0 \cosh \xi_1 - x_1 \sinh \xi_1) \cosh \xi_2 - (-x_0 \sinh \xi_1 + x_1 \cosh \xi_1) \sinh \xi_2$$

$$= x_0 (\cosh \xi_1 \cosh \xi_2 + \sinh \xi_1 \sinh \xi_2) - x_1 (\sinh \xi_1 \cosh \xi_2 + \cosh \xi_1 \sinh \xi_2)$$

$$= x_0 \cosh(\xi_1 + \xi_2) - x_1 \sinh(\xi_1 + \xi_2).$$

Then, the equivalent velocity is

$$\frac{v}{c} = \tanh(\xi_1 + \xi_2) = \frac{\tanh \xi_1 + \tanh \xi_2}{1 + \tanh \xi_1 \tanh \xi_2} = \frac{\frac{v_1}{c} + \frac{v_2}{c}}{1 + \frac{v_1 v_2}{c^2}},$$

or

$$v = \frac{v_1 + v_2}{1 + v_1 v_2 / c^2}$$