The loop with normal having spherical angles to and to can be viewed as volating a loop eying in the not plane by first volating to around y axis, and to around & axis. Then, any point or direction originally in the noy plane can be determined by multiplying the vector with the rotation matrix, which is given by

$$T = \begin{pmatrix} \cos \phi_0 & \sin \phi_0 & o \\ -\sin \phi_0 & \cos \phi_0 & o \end{pmatrix} \begin{pmatrix} \cos \phi_0 & o & -\sin \phi_0 \\ o & 1 & o \\ -\sin \phi_0 & o & \cos \phi_0 \end{pmatrix}$$

Point a(cosp, sizp, v) becomes

$$\begin{array}{c} (u) = a \begin{pmatrix} (u) & ($$

Direction (-sing, wsp, o) becomes

$$\mathcal{V}(\phi) = \begin{pmatrix} -\sin\phi \cos\phi \cos\phi + \cos\phi & \sin\phi \\ \sin\phi & \cos\phi & \sin\phi \\ \sin\phi & \sin\phi \end{pmatrix} = \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix}$$

 $\vec{F} = \int \vec{J}(\vec{n}) \times \vec{B}(\vec{n}) d^{3}n = I \int d\vec{i} \times \vec{B}(\vec{n}) d^{3}n = I a \int \vec{v} \times \vec{B}(\vec{u}(\theta)) d\theta$ 

First order term in cosp and sixp will drop out

$$\vec{F} = \beta J \vec{a} B_{\rho} \int_{0}^{\infty} \left( -u_{1} v_{1} \hat{a} + u_{1} v_{2} \hat{j} + \left( u_{1} v_{1} - u_{1} v_{2} \right) \hat{k} \right) d\phi$$

Further, sind wish terms will also deep out

$$\dot{\vec{F}} = \beta \vec{l} \vec{a} \vec{b}_0 \int_0^{\infty} \left( -\sin^2 \phi \sin \theta_0 \sin \phi_0 \hat{i} + \sin^2 \phi \sin \theta_0 \cos \phi_0 \hat{j} \right) \left( \cos 2\phi \cos \phi_0 \sin \phi_0 \cos \phi_0 + \cos 2\phi \cos \phi_0 \sin \phi_0 \cos \phi_0 \right) \hat{k} d\phi$$

Then 
$$\vec{f} = \mathcal{V}(\vec{m} \cdot \vec{B}) = Iza^2 \mathcal{V}(\hat{n} \cdot \vec{B})$$
  

$$= Jza^2 B_0 \mathcal{V}(1+\beta y) \sin \theta_0 \cos \phi_0 - (1+\beta x) \sin \theta_0 \sin \phi_0)$$

$$= \beta Iza^2 B(-\sin \theta_0 \sin \phi_0 \hat{i} + \sin \theta_0 \cos \phi_0 \hat{j})$$

Which agrees wich enact calculation

$$= I\pi a^2 B \left| \frac{\hat{i}}{\sin \theta_0 \cos \theta_0} - \sin \theta_0 \sin \theta_0 \right| = I\pi \kappa^2 B \left( -\cos \theta_0 \cdot \hat{i} + \cos \theta_0 \cdot \hat{j} + \sin \theta_0 (\cos \theta_0 + \sin \theta_0) \cdot \hat{k} \right)$$