16.10 (a) The Abraham - Lorentz equation $m(\vec{v} - T\vec{v}) = \vec{F}$ can be expressed as $\frac{d}{dt} \left(e^{-t/z} \vec{v} \right) = -\frac{1}{mt} \vec{F}(t) e^{-t/z}$

To eliminate the runaway solution, we require that $\vec{v}(tvo)$ to be finite. Integrating from t to tvo, we have $e^{-Wt}\vec{v}(u)\Big|_{+}^{+vo}=-\frac{1}{m\tau}\int_{+}^{+vo}\vec{F}(u)e^{-W\tau}du$,

or $-e^{-t/\tau}\vec{y}(t) = -\frac{1}{m\tau}\int_{t}^{tw}\vec{F}(u)e^{-u/\tau}du \Rightarrow m\vec{v}(t) = \frac{1}{\tau}\int_{t}^{+\infty}\vec{F}(u)e^{(t-u)/\tau}du$

Make the substitution U=t+TS is the ritegral, we will obtain

mith = fto e-5 F(++ TS) ds

(b) The force can be Paylor expanded as FITTES) = \frac{1}{n!} \frac{d^n Fit}{dt^n}. Using the identity,

from e-s sn ds = [(n+1) = n!, we have

mith = 2 To drift)

Keeping only the first stow sterms, $m\ddot{v}(t) = \vec{F}(t) + T \frac{d\vec{F}(t)}{dt}$. We can approximate $\vec{F}(t)$ as $m\ddot{v}(t) = \vec{F}(t) + T \frac{d\vec{F}(t)}{dt} = m\ddot{v}(t)$. This leads to the Abraham-Lorentz equation, $m(\vec{v}(t) - T \ddot{v}(t)) = \vec{F}(t)$.

(c) For t > 0, $F(t + Ts) = F_0$ for s > 0. Then $m \dot{v}(t) = F_0 \int_0^{+\infty} e^{-s} ds = F_0$, $\dot{v}(t) = F_0/m$.

For t < 0, $F(t + Ts) = F_0$, for s > -t/c. Then, $m \dot{v}(t) = F_0 \int_{-t/c}^{+\infty} e^{-s} ds = F_0 e^{-t/c}$, $\dot{v}(t) = F_0 e^{-t/c}/m$.

Now, $v(t) = \int_{-\infty}^{+\infty} \dot{v}(u) du = \begin{cases} \frac{F_0 \dot{v}}{m} e^{-t/c}, & t < 0 \\ \frac{F_0 \dot{v}}{m} e^{-t/c}, & t > 0 \end{cases}$