

11.2 By following the argument of Prob. 11.1(c), the constancy of $|h(v)/f(v)|$ is straightforward.

Consider the reference frames in the problem, then we must have

$$v_3 = \frac{v_1 + v_2}{1 + v_1 v_2 h(v_1)/f(v_1)}$$

Now, if K' moves with velocity v_2 w.r.t. K , and K'' with v_1 w.r.t. K' , then

$$v_3' = \frac{v_2 + v_1}{1 + v_2 v_1 h(v_2)/f(v_2)}$$

We must have $v_3 = v_3'$, due to the group nature of the transformation, then it is obvious

$$\frac{h(v_1)}{f(v_1)} = \frac{h(v_2)}{f(v_2)}, \text{ which means, } |h(v)/f(v)| \text{ is a universal constant. By dimensional}$$

analysis, it must have the dimension of inverse speed squared.