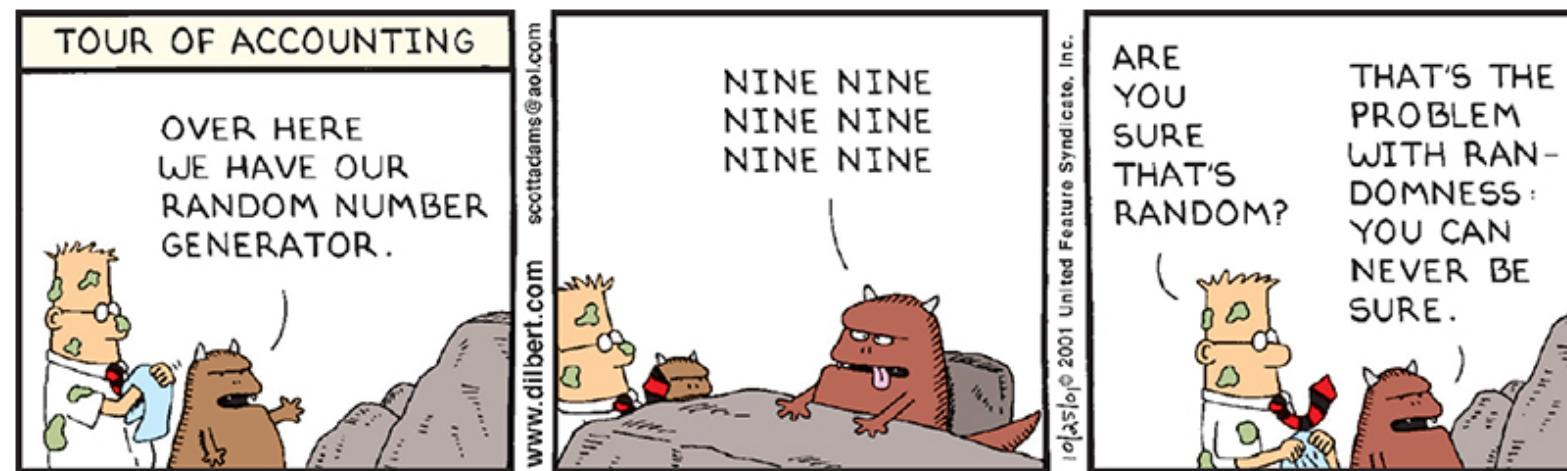


*0xFFFFFFFF EVERY TIME IS 0XDEADBEEF —*

# How a months-old AMD microcode bug destroyed my weekend [UPDATED]

AMD shipped Ryzen 3000 with a serious microcode bug in its random number generator.

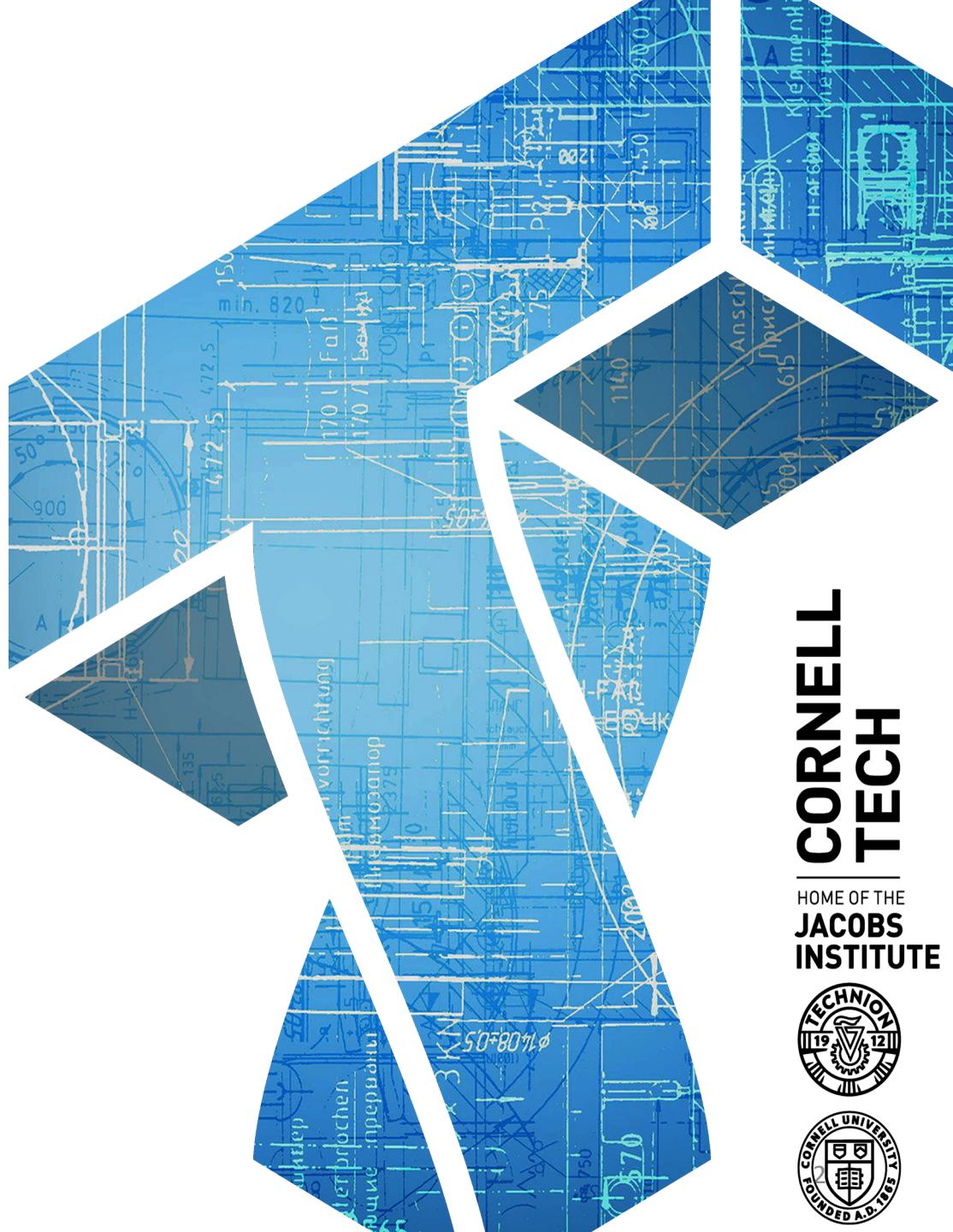
JIM SALTER - 10/29/2019, 7:00 AM



# CS 5435: Asymmetric cryptography (part 2)

Instructor: Tom Ristenpart

<https://github.com/tomrist/cs5435-fall2019>



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# Where we're at

- Last time: key exchange, key transport, public-key encryption, forward secrecy, Diffie-Hellman, man-in-the-middle attacks
- Today's lecture
  - Digital signatures
  - Public-key infrastructure (PKI)

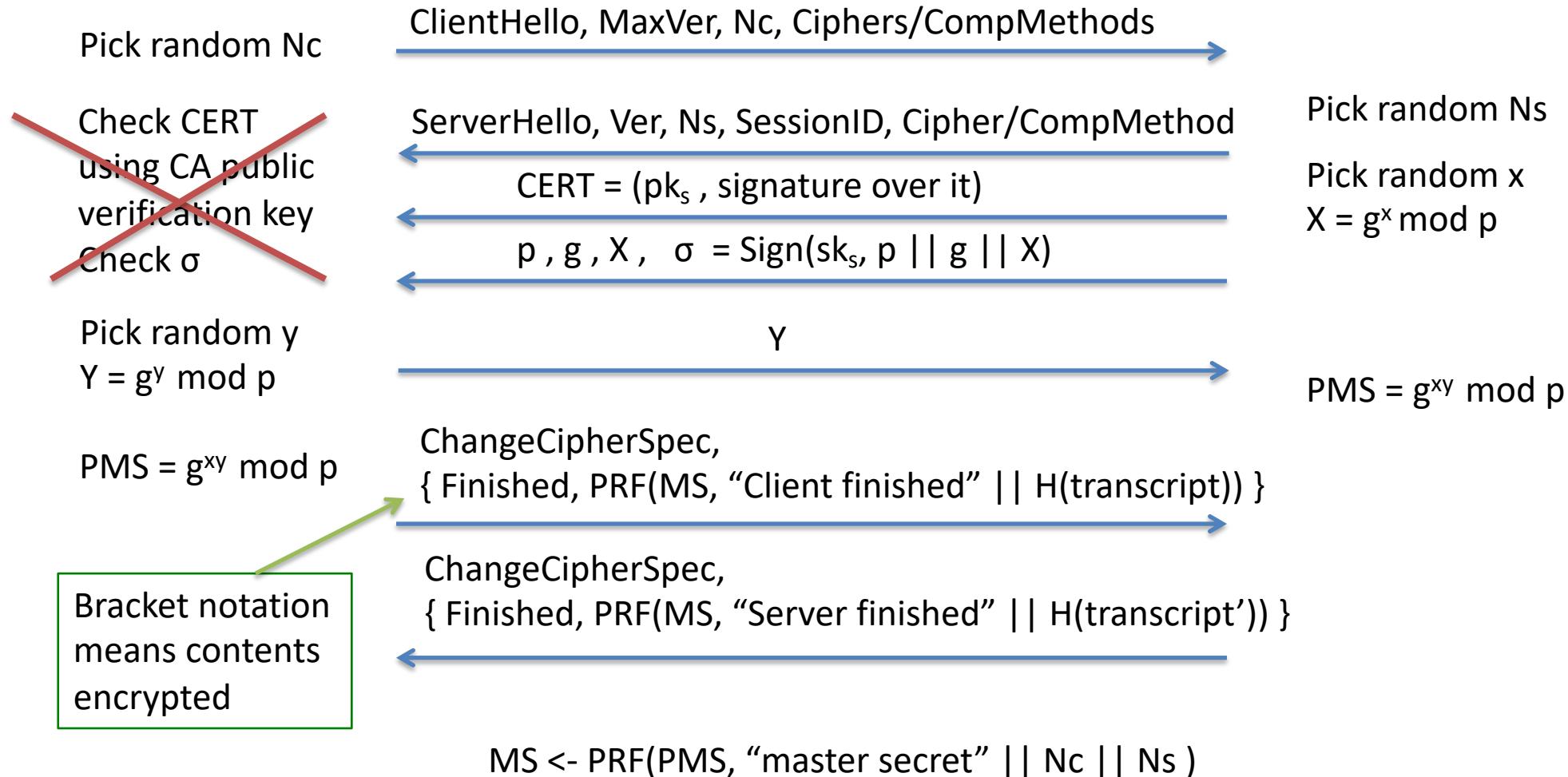


Client



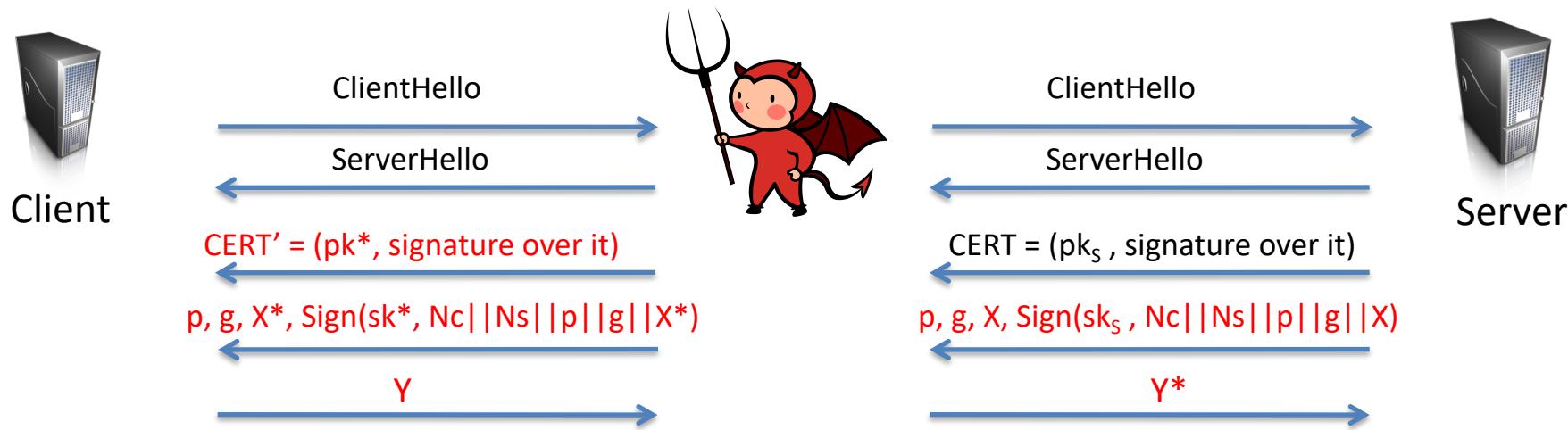
Server

# TLS handshake for Diffie-Hellman Key Exchange



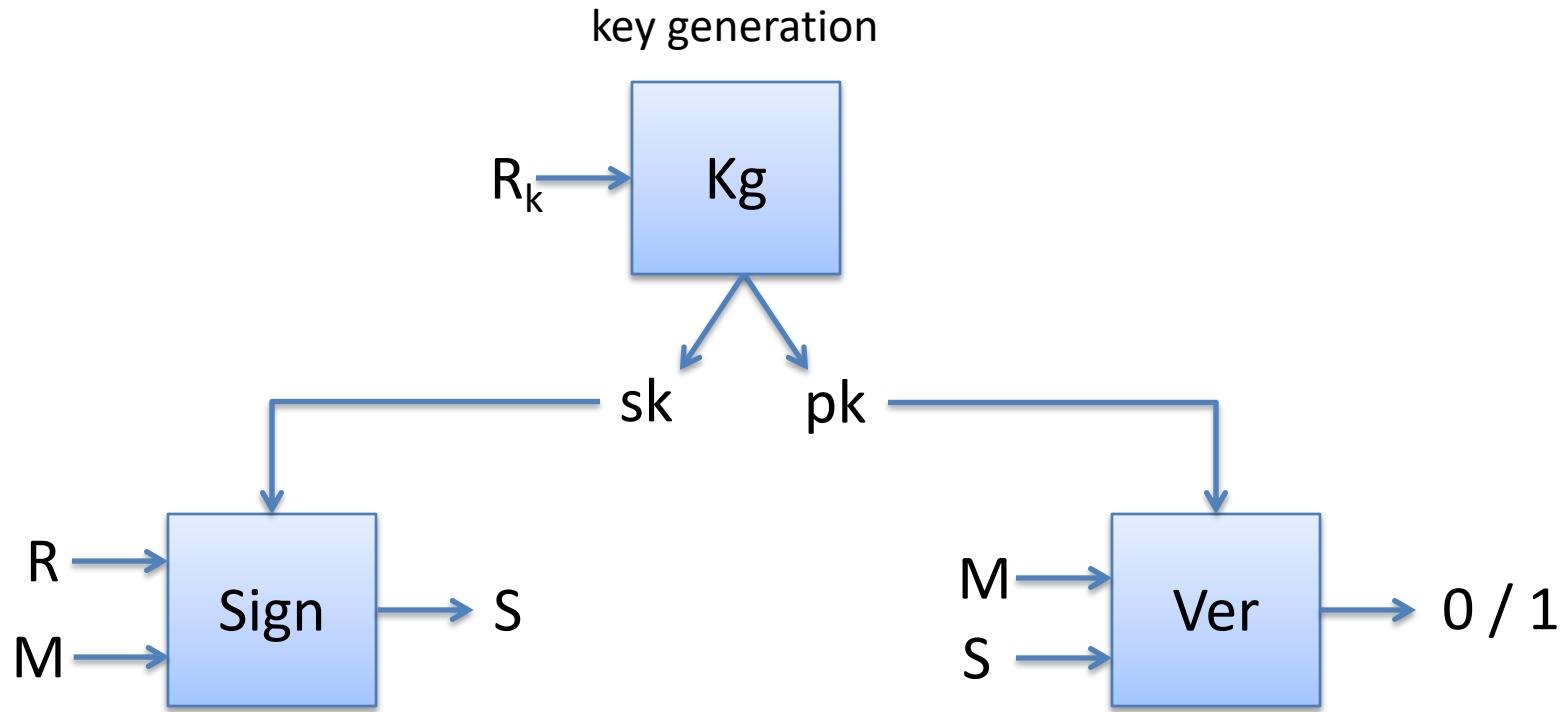
# Man-in-the-middle attacks

Suppose authentication vulnerability:  
CERT can be forged, Client doesn't check CERT, etc.



Attacker can choose  $X^*, Y^*$ , so it knows discrete logs  
Completes handshake on both sides  
Client thinks its talking to Server  
All communications decrypted by adversary, re-encrypted and forwarded to server

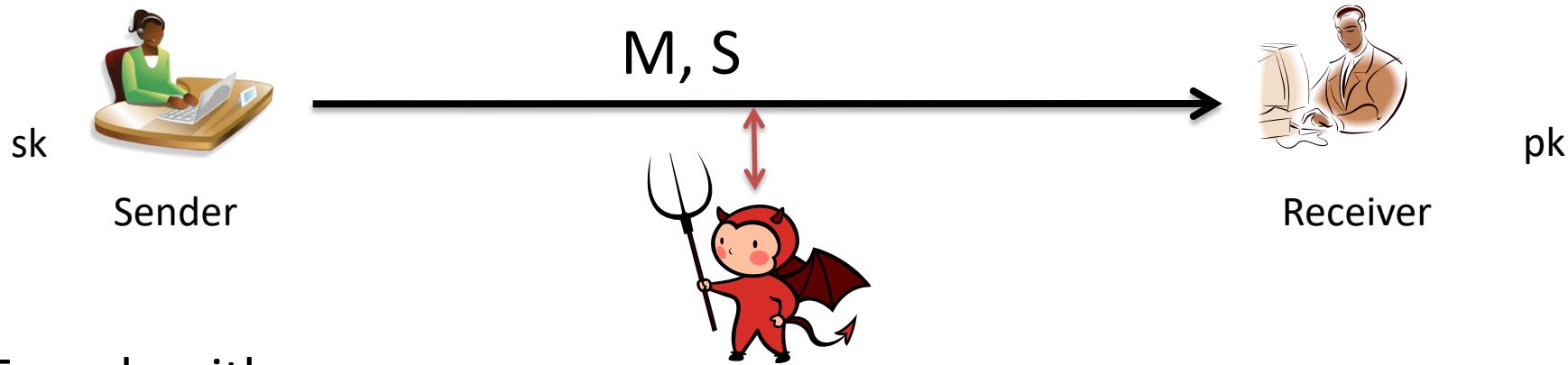
# Digital signatures



Anyone with public key can verify a signature

Only holder of secret key should be able to generate a signature

# Digital signatures



Two algorithms:

- (1) Key generation outputs  $(pk, sk)$
- (2) Sign  $(sk, M)$  outputs a signature  $S$  (may be randomized)
- (3) Ver $(pk, M, S)$  outputs 0/1 (invalid / valid)

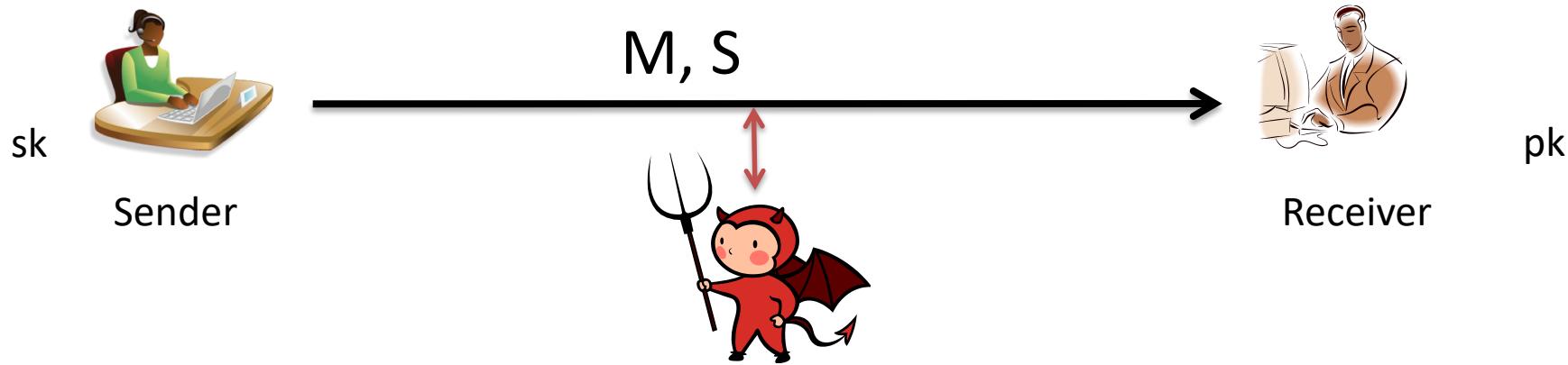
*Correctness:*  $\text{Ver}(pk, M, \text{Sign}(sk, M)) = 1$  always

*Security:* No computationally efficient attacker can forge valid signature for a new message even when attacker gets

$$(M_1, S_1), (M_2, S_2), \dots, (M_q, S_q)$$

for messages of his choosing and reasonably large  $q$ .

# Digital signatures



**“Raw” RSA as a signature scheme:**

Key generation gives  $(N,e)$ ,  $(N,d)$  s.t.  $(M^e)^d \bmod N = M$

$\text{Sign}((N,d), M) = M^d \bmod N$

$\text{Verify}((N,e), M, S)$  checks if  $S^e \bmod N = M$

Secure?

No!

$$M = 1$$

Then  $S = 1$  valid

$$\text{Get } S_1 = M^d \bmod N$$

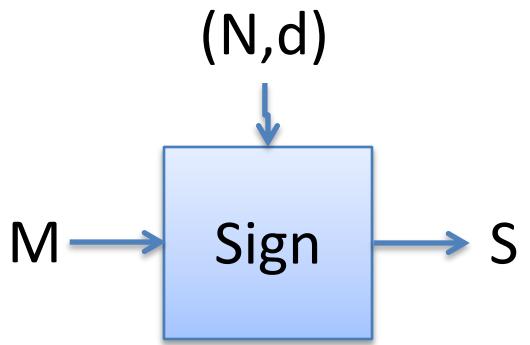
Then  $S = (M^d)^2 \bmod N$  is valid signature for  $M^2$

# PKCS #1 v1.5 RSA signing

Kg outputs  $(N,e), (N,d)$  where  $|N|_8 = n$

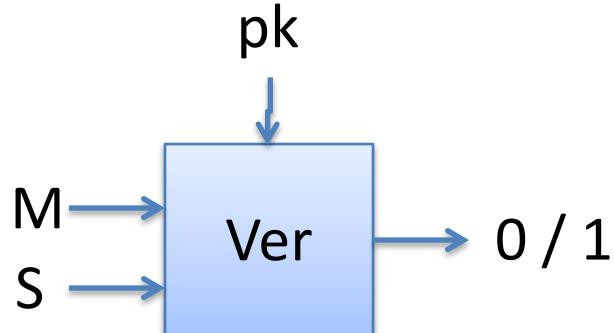
Want to sign using hash with output length  $m$  bytes

Let  $p = n - m - 3$



Sign( $(N,d)$ ,  $M$ )

$Y = 00 \parallel 01 \parallel FF^p \parallel 00 \parallel H(M)$   
Return  $Y^d \bmod N$



Verify( $(N,e)$ ,  $M$ ,  $S$ )

$Y = S^e \bmod N$  ;  $aa \parallel bb \parallel cc \parallel dd \parallel h = Y$   
If  $(aa \neq 00)$  or  $(bb \neq 01)$  or  $(cc \neq FF^p)$   
or  $(dd \neq 00)$

Return error

Return  $H(M) = h$

# PKCS#1 v1.5 digital signature security

Padding oracle attacks:

- PKCS#1 v1.5 decryption oracle can be used to forge
- PKCS#1 v1.5 signing oracle can be used to forge

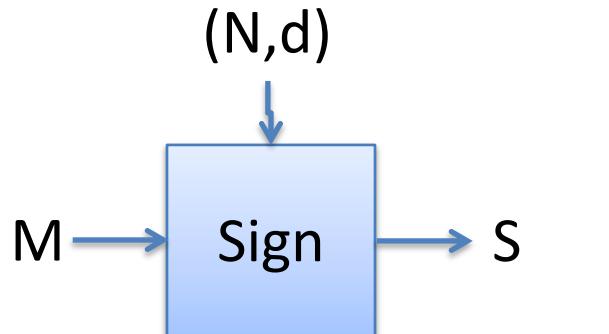
If one uses same RSA key pair for signing and encryption, then decryption and signing oracles offer similar forging / decryption opportunities

- Never use same keys for signing and encryption

# Full Domain Hash RSA

$Kg$  outputs  $pk = (N, e)$ ,  $sk = (N, d)$  where  $|N|_8 = n$

$H$  is hash with  $m$ -byte output       $k = \text{ceil}((n - 1)/m)$

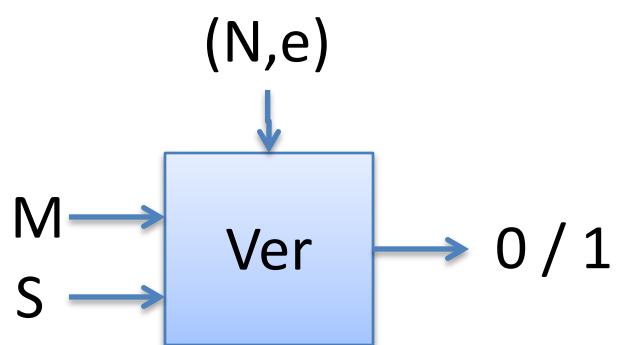


Sign( $(N, d)$ ,  $M$ )

$$X = 00 || H(1||M) || \dots || H(k||M)$$

$$S = X^d \bmod N$$

Return  $S$



Ver( $(N, e)$ ,  $M, S$ )

$$X = S^e \bmod N$$

$$X' = 00 || H(1||M) || \dots || H(k||M)$$

If  $X = X'$  then

Return 1

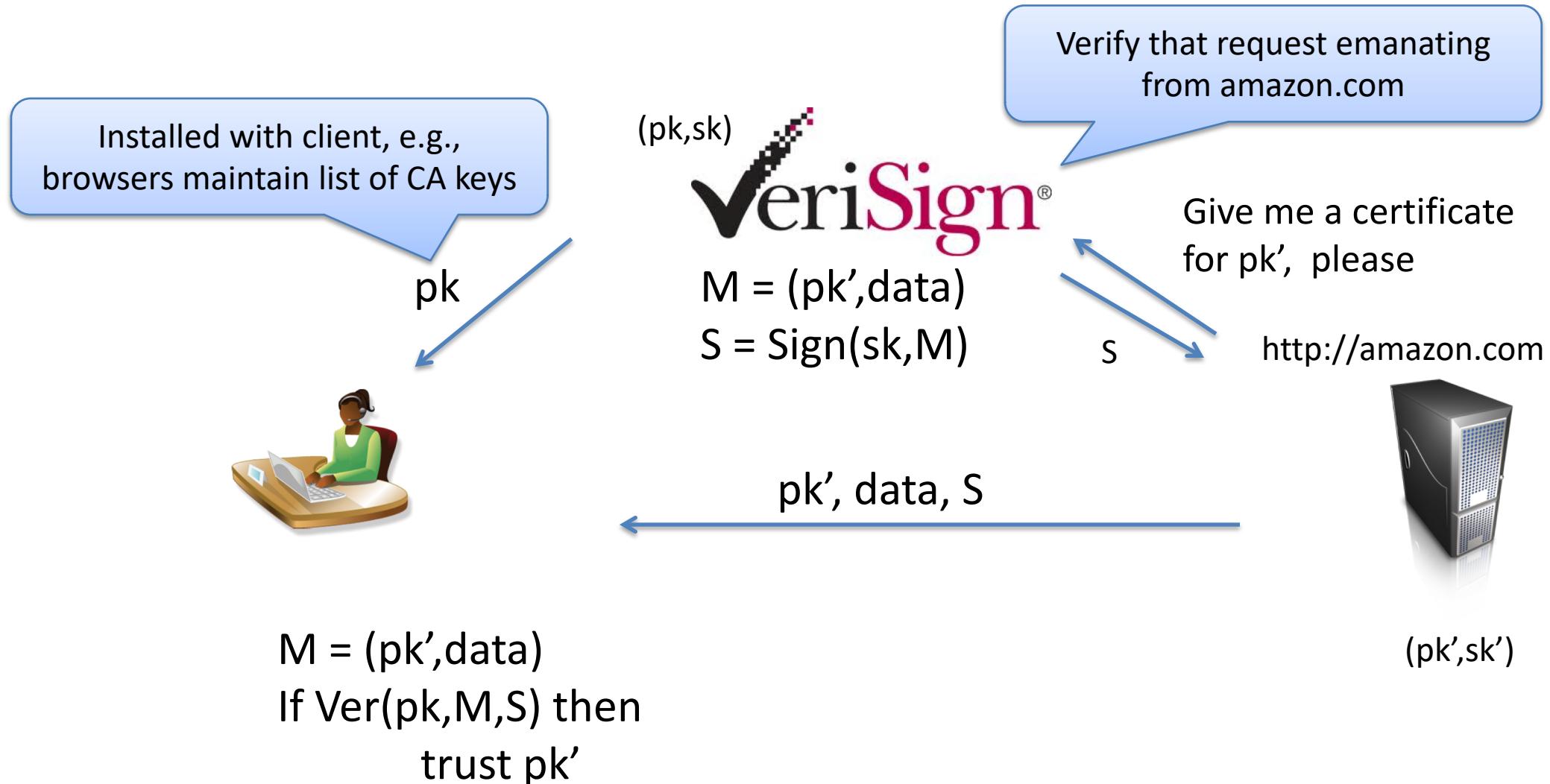
Return 0

Probabilistic Signature Scheme (PSS) variant of FDH that is widely deployed  
see PKCS#1 v2

# Digital signatures from discrete log

- Schnorr signatures
- Digital Signature Algorithm (designed by DSA)
  - Variant of Schnorr signatures designed by NSA
- ECDSA
  - Elliptic curve variant of DSA
- Reference slides describing included at end of lecture

# Certificate Authorities & Public-Key Infrastructure



Certificate Viewer: "5654961308303360-fe2.pantheonsite.io"

General Details

This certificate has been verified for the following uses:

SSL Server Certificate

**Issued To**

Common Name (CN) 5654961308303360-fe2.pantheonsite.io  
Organization (O) <Not Part Of Certificate>  
Organizational Unit (OU) <Not Part Of Certificate>  
Serial Number 03:50:CF:80:74:39:79:89:70:4F:D0:94:00:D4:42:50:91:EA

**Issued By**

Common Name (CN) Let's Encrypt Authority X3  
Organization (O) Let's Encrypt  
Organizational Unit (OU) <Not Part Of Certificate>

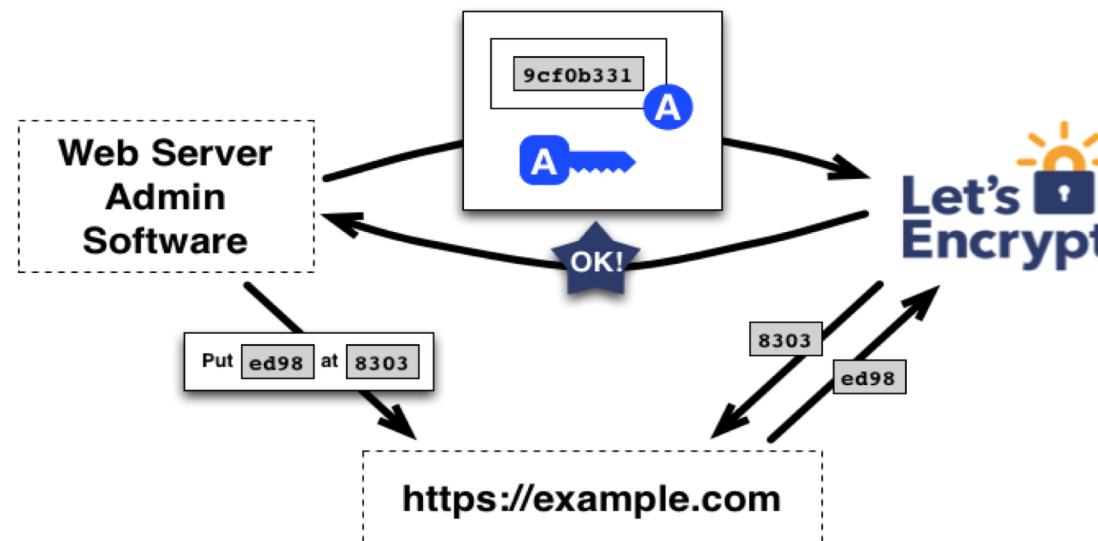
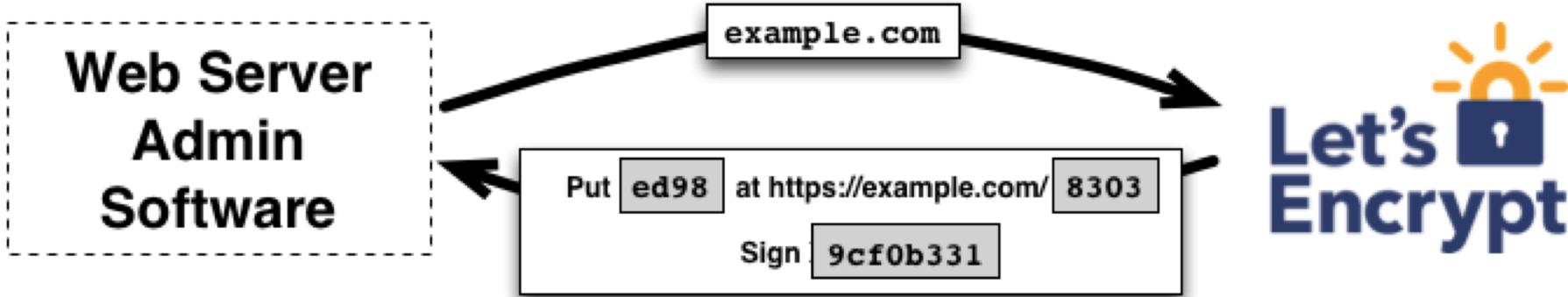
**Period of Validity**

Begins On October 26, 2019  
Expires On January 24, 2020

**Fingerprints**

SHA-256 Fingerprint 56:46:FE:46:64:42:77:F6:8E:78:0B:9E:C8:D3:5F:C4:  
9C:9C:27:8F:A5:78:0F:C7:E1:15:10:58:4D:5B:42:26  
SHA1 Fingerprint 23:85:1B:04:D2:76:88:18:EC:0D:1D:D3:A1:E7:C0:09:5F:99:0F:65

# Free CAs



# In-class exercise

Discuss with neighbor for 5 minutes:

What vulnerabilities would undermine server authentication in TLS?

Think about:

- Certificate authority protocols
- TLS handshake

Client implementation vulnerabilities

Theft of server secret signing key

Compromise of web server

CA compromise

CA identity check failure

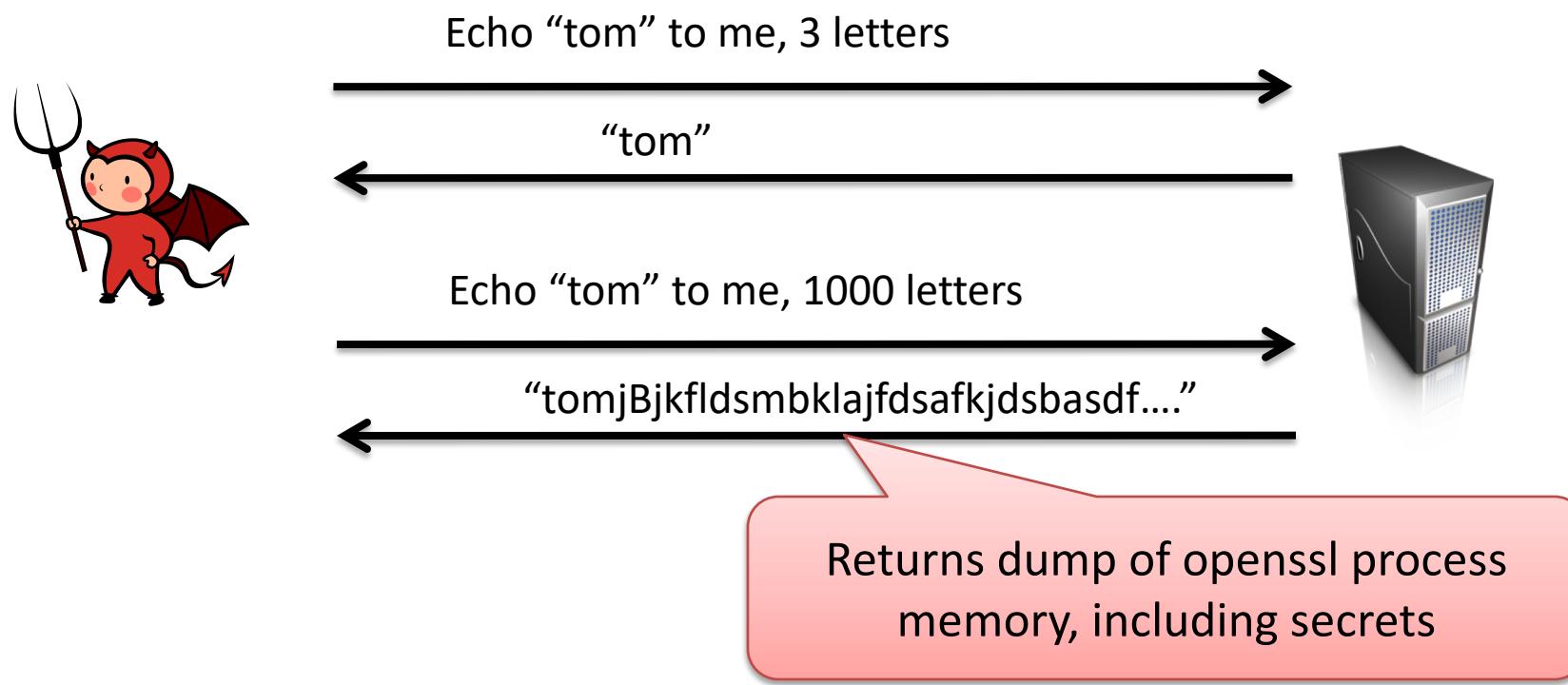
# Client side vulnerability: Apple iOS <7.0.16 signature verification code

```
        if ((err = ReadyHash(&SSLHashSHA1, &hashCtx)) != 0)
            goto fail;
        if ((err = SSLHashSHA1.update(&hashCtx, &clientRandom)) != 0)
            goto fail;
        if ((err = SSLHashSHA1.update(&hashCtx, &serverRandom)) != 0)
            goto fail;
        if ((err = SSLHashSHA1.update(&hashCtx, &signedParams)) != 0)
            goto fail;
        if ((err = SSLHashSHA1.update(&hashCtx, &signedParams)) != 0)
            goto fail;
        if ((err = SSLHashSHA1.final(&hashCtx, &hashOut)) != 0)
            goto fail;

        err = sslRawVerify(ctx,
                            ctx->peerPubKey,
                            dataToSign,
                            dataToSignLen,                      /* plaintext */
                            signature,                         /* plaintext length */
                            signatureLen);
        if(err) {
            sslErrorLog("SSLDecodeSignedServerKeyExchange: sslRawVerify "
                        "returned %d\n", (int)err);
            goto fail;
        }

fail:
    SSLFreeBuffer(&signedHashes);
    SSLFreeBuffer(&hashCtx);
    return err;
```

# Web server vulnerability: Heartbleed



Software vulnerability in OpenSSL's implementation of heartbeat protocol  
Buffer overread vulnerability  
Allowed exfiltrating server signing keys  
In code base 2012-2014

# PKI ecosystem

- Durumeric et al. Analysis of the HTTPS Certificate Ecosystem, 2013
  - <http://conferences.sigcomm.org/imc/2013/papers/imc257-durumericAemb.pdf>
- “1,800 entities that are able to issue certificates vouching for the identity of any website”



search...

Search



**Know for sure with whom you have an agreement**  
How do you check the identity of someone who's doing business online?

EV SSL + | Contact + | FAQ +

Go to ...

DigiNotar®, Internet Trust Provider

An independent Internet Trust Certificate Issuer

Announcements

> Publication report Fox-IT

Today, Microsoft issued a [Security Advisory](#) warning that fraudulent digital certificates were issued by the Comodo Certificate Authority. This could allow malicious spoofing of high profile websites, including Google, Yahoo! and Windows Live.

<https://nakedsecurity.sophos.com/2011/03/24/fraudulent-certificates-issued-by-comodo-is-it-time-to-rethink-who-we-trust/>

<https://technet.microsoft.com/library/security/2524375>

# Revocation

- Certificates must often be revoked
  - Short expirations
  - CRLs (Certificate revocation lists)
  - OCSP (online certificate status protocol)
    - Client queries CA to check on validity of cert
      - privacy concerns, performance / scalability issues
    - Stapling: server periodically gets fresh, time-stamped OCSP signature from CA. Sends to clients

# How well does revocation work?

- Liu et al. An End-to-End Measurement of Certificate Revocation in the Web's PKI, 2014
  - <http://www.ccs.neu.edu/home/cbw/static/pdf/liu-imc15.pdf>
- 8% of in-use certificates revoked
- Many browsers don't bother checking for revocation (accepting revoked certificates)

# Certificate/public-key pinning

- Can we prevent MitM due to PKI being undermined?
- Client knows what cert/pk to expect, rejects otherwise
  - Pre-install some keys
  - HPKP (HTTP Public Key Pinning)
    - HTTP header that allows servers to set a hash of public key they will use

Public-Key-Pins:

```
pin-sha256="d6qzRu9zOECb90Uez27xWltNsj0e1Md7GkYYkVoZWmM=";  
pin-sha256="LPJNul+wow4m6DsqxbninhsWHlwfp0JecwQzYpOLmCQ=";  
max-age=259200
```

<https://developers.google.com/web/updates/2015/09/HPKP-reporting-with-chrome-46?hl=en>

# Certificate transparency

- Can we detect rogue certificates?
- Force CAs to log the certificates they sign in a public tamper-evident register
  - Experimental IETF standard
- Google has been pushing this
  - Chrome requires it for “extra validation” certs
  - DigiCert has implemented

# Summary

- Digital signature schemes power PKI and verifying identities:
  - unforgeability under chosen message attack
  - RSA based schemes PKCS#1 1.5, FDH, PSS
  - Discrete-log based schemes include Schnorr, DSA, ECDSA
- Web PKI relies on various trust assumptions
  - Can be undermined in *many* ways
  - Need combination of cryptography plus other mechanisms



# Groups for Schnorr and DSA Signatures

Let  $p$  be a large prime number

Let  $q$  be a prime such that  $q$  divides  $p-1$

Example:  $p = 2q + 1$  (so-called safe prime  $p$ )

Fix the group  $G = \mathbb{Z}_p^* = \{1, 2, 3, \dots, p-1\}$

Let  $g$  be generator of sub-group of order  $q$ :

$\{g^0, g^1, g^2, \dots, g^{q-1}\}$  subset of  $G$

How to pick  $g$ ?

$g = h^{(p-1)/q} \bmod p$  for some  $h$  and check  $g \neq 1 \bmod p$

If so, try repeat with another  $h$ . Usually start with  $h = 2$

# (Variant of) Schnorr signatures

$p, q, g$  specified

$sk = x$  chosen randomly from  $\mathbb{Z}_q$        $pk = X = g^x$

Sign( $x, M$ )

$r \leftarrow \mathbb{Z}_q$

$R = g^r$  ;  $c = H(M || R)$  ;  $z = r + cx \pmod{q}$

Return  $(R, z)$

Ver( $X, M, (R, z)$ )

$c = H(M || R)$

If  $g^z = RX^c$  then Return 1

Return 0

Correctness?

$$g^z = g^{r+cx} = g^r g^{xc} = RX^c$$

# Security intuition



Assume an adversary that can output forgery  $(M, (R, z))$   
Then to be valid:

$$g^z = RX^c \text{ implies } z = r + cx$$

for  $c = H(M \parallel R)$ .

Assume  $c$  is random ( $H$  is random oracle)

Imagine we can run adversary twice but force forgery to  
be on same  $R$ , different  $c$ .

In second execution, getting  $(M', (R, z'))$

Then success second time around gives:

$$g^{z'} = RX^{c'} \text{ implies } z' = r + c'x$$

But now can compute  $z - z' / (c - c') = x$  the secret key

# Fragility of signatures

Repeat randomness failure:

Sign two messages  $M \neq M'$  and reuse randomness

$$\text{Sign}(x, M) \rightarrow (R, z)(R, r + cx \bmod q)$$

$$\text{Sign}(x, M') \rightarrow (R, z')(R, r + c'x \bmod q)$$

$$\text{Then: } x = (z - z') / (H(M || R) - H(M' || R))$$

If  $r$  is predictable/leaked, can recover secret from  $(R, z)$

Can improve security by “hedging”:

$$\text{choose } r = H(x || M || \text{randomness})$$

# Actual Schnorr signatures

$p, q, g$  specified

$sk = x$  chosen randomly from  $\mathbb{Z}_q$        $pk = X = g^x$

Sign( $x, M$ )

$r \leftarrow \mathbb{Z}_q$

$R = g^r ; c = H(M || R) ; z = r + cx \pmod{q}$

Return  $(c, z)$

Ver( $X, M, (c, z)$ )

$R' = g^s X^{-c}$

$c' = H(M || R')$

If  $c' = c$  then Return 1

Return 0

Correctness?     $R' = g^s X^{-c} = g^{r + cx} g^{x/(H(M||R))} = g^r$

# DSA (digital signature algorithm)

p,q,g specified

sk = x chosen randomly from  $Z_q$

pk = X =  $g^x$

Sign(x, M )

$r \leftarrow Z_q ; R = (g^r \text{ mod } p) \text{ mod } q$

$z = r^{-1} ( H(M) + x R ) \text{ mod } q$

Return (R,z)

Ver(X, M, (R,z))

$w = z^{-1} \text{ mod } q$

$u_1 = H(m) * w \text{ mod } q$

$u_2 = R * w \text{ mod } q$

If  $R = (g^{u_1} X^{u_2} \text{ mod } p) \text{ mod } q$

then Return 1

Else Return 0

Correctness?

$$g^{u_1} X^{u_2} = g^{H(M)w} g^{xRw} = g^{(H(M)+xR)w}$$

$$= g^{(H(M)+xR)(H(M)+xR)^{-1}r} = g^r$$

# Fragility of DSA

Repeat randomness failure:

Sign two messages  $M \neq M'$  and reuse random

$$\begin{aligned}\text{Sign}(x, M) \rightarrow (R, z) &= (R, r^{-1} ( H(M) + x R ) \bmod q) \\ \text{Sign}(x, M') \rightarrow (R, z') &= (R, r^{-1} ( H(M') + x R ) \bmod q)\end{aligned}$$

Then: Solve for  $r^{-1}$ , solve for  $x$

If  $r$  is predictable/leaked, can recover secret from  $(R, z)$

Again, can improve security by “hedging”:

$$\text{choose } r = H( x \parallel M \parallel \text{randomness} )$$

# Hackers Describe PS3 Security As Epic Fail, Gain Unrestricted Access

BY MIKE BENDEL

DECEMBER 29, 2010 @ 11:19 AM



<http://psx-scene.com/forums/content/sony-s-ps3-security-epic-fail-videos-within-581/>