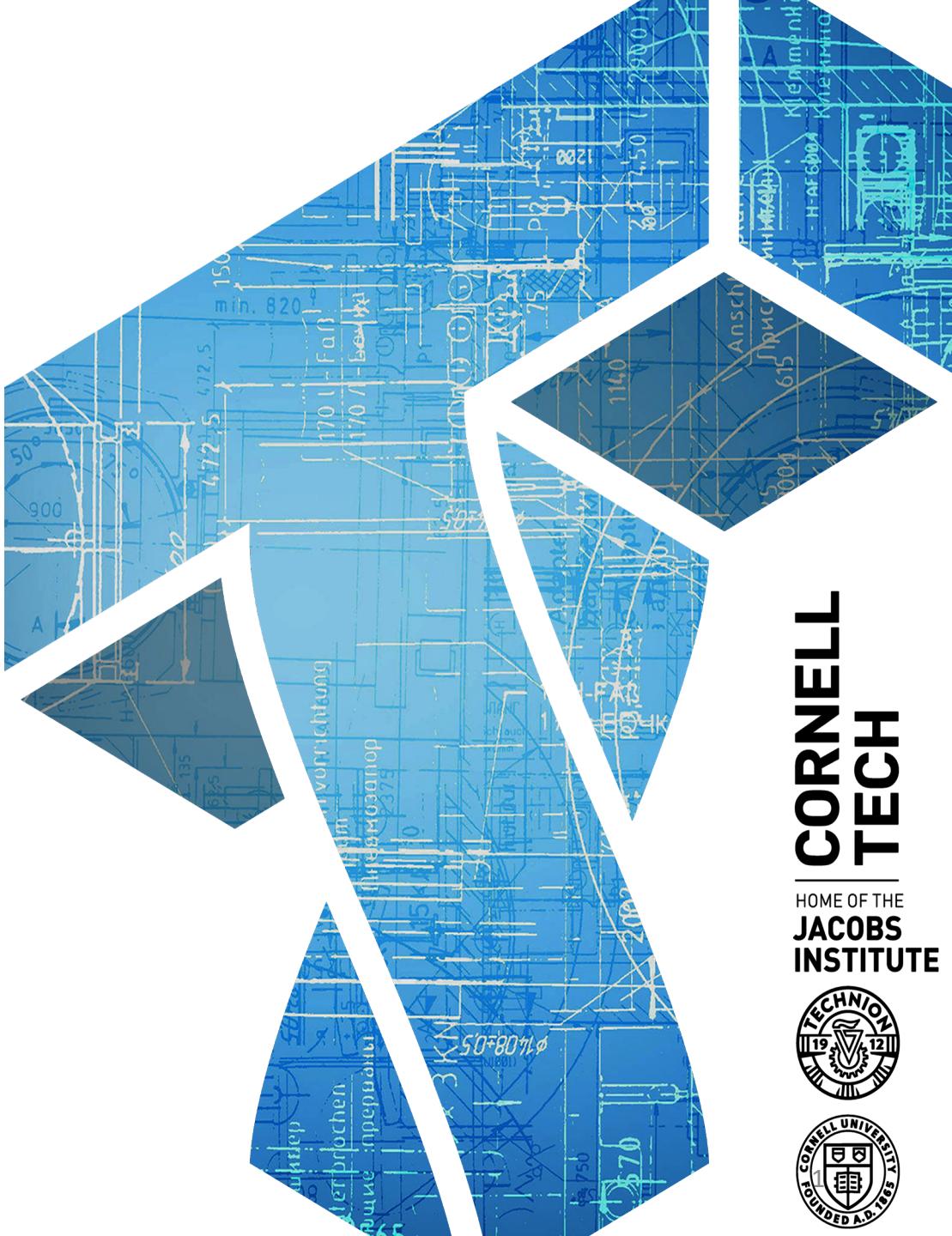


CS 5435: Cryptography part 3

Instructor: Tom Ristenpart

<https://github.com/tomrist/cs5435-fall2019>



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Today's lecture

- Wrapping up CBC padding oracle attacks
- Message authentication
- Authenticated encryption

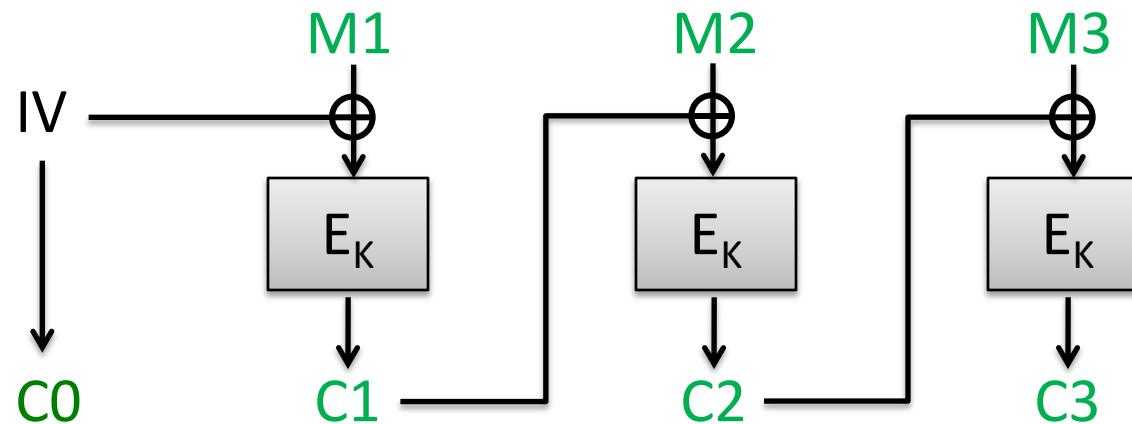
CBC mode

Ciphertext block chaining (CBC)

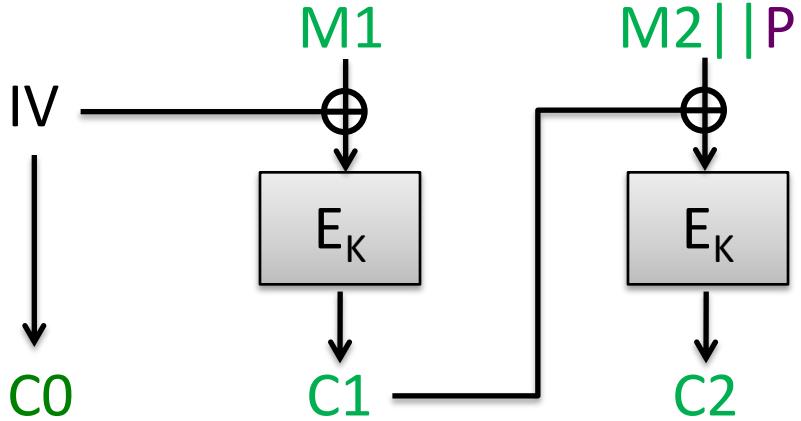
Pad message M to M_1, M_2, M_3, \dots where each block M_i is n bits

Choose random n-bit string IV

Then:



Padding oracle attack



Assume that
M₁ || M₂ has length
2n-8 bits

P is one byte of padding
that must equal 0x00



Adversary
obtains
ciphertext
C₀, C₁, C₂

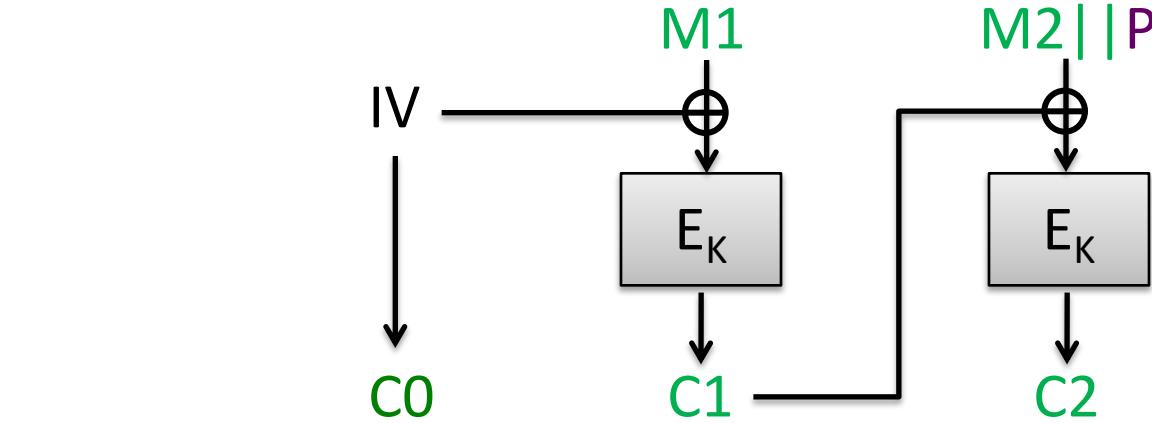
C₀, C₁, C₂
ok

C₀, C₁ ⊕ 1, C₂
error



Dec(K, C')
M₁' || M₂' || P' = CBC-Dec(K, C')
If P' ≠ 0x00 then
 Return error
Else
 Return ok

Padding oracle attack



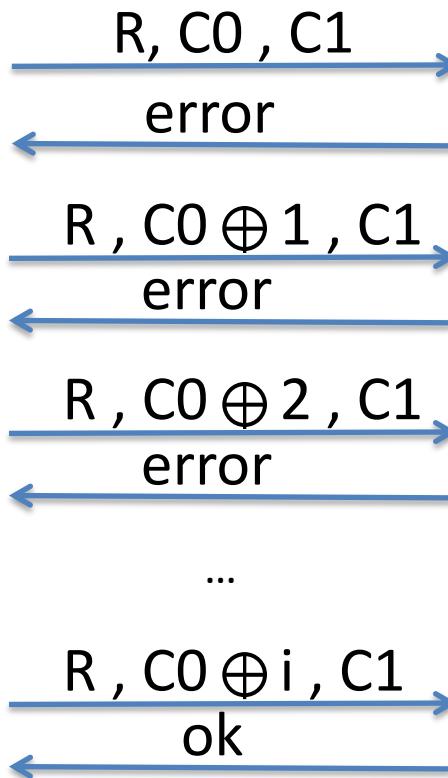
Low byte of M1
equals i



Adversary
obtains
ciphertext

$C = C_0, C_1, C_2$

Let R be arbitrary
n bits



Assume that
 $M_1 || M_2$ has length
2n-8 bits

P is one byte of padding
that must equal 0x00



Dec(K, C')

$M_1' || M_2' || P' = \text{CBC-Dec}(K, C')$

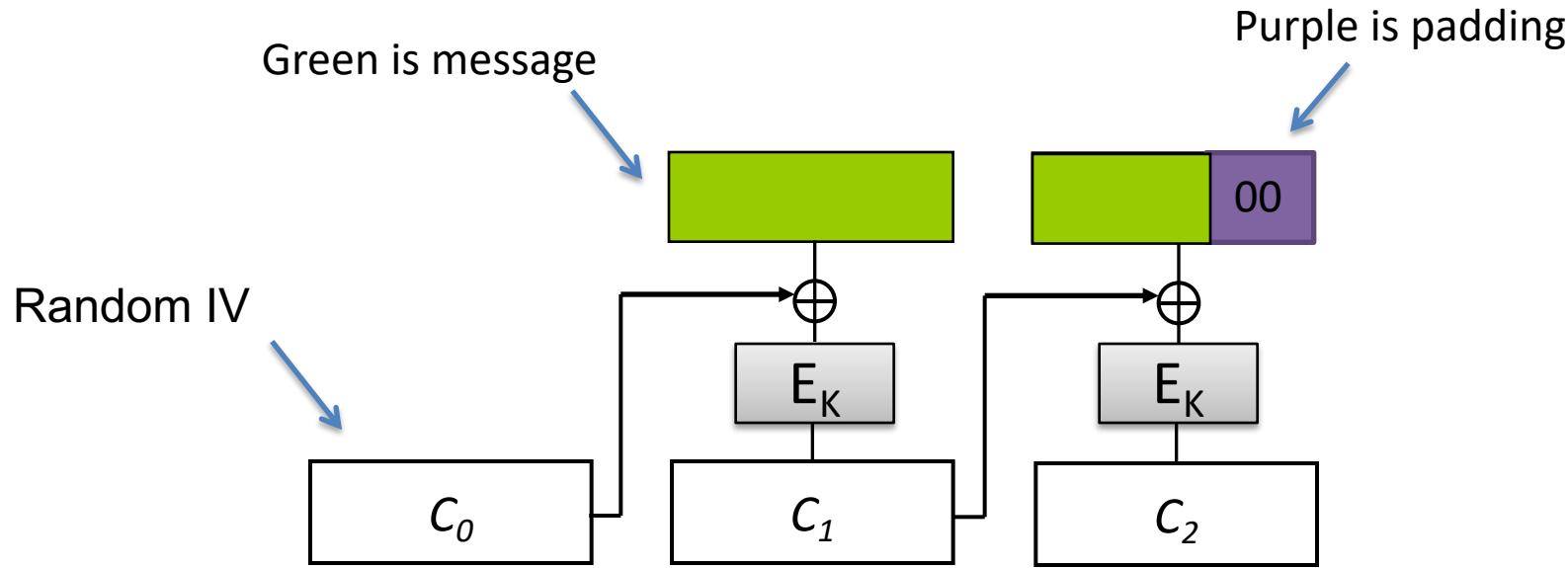
If $P' \neq 0x00$ then

Return error

Else

Return ok

Padding for CBC Mode in TLS



Possible paddings in TLS:

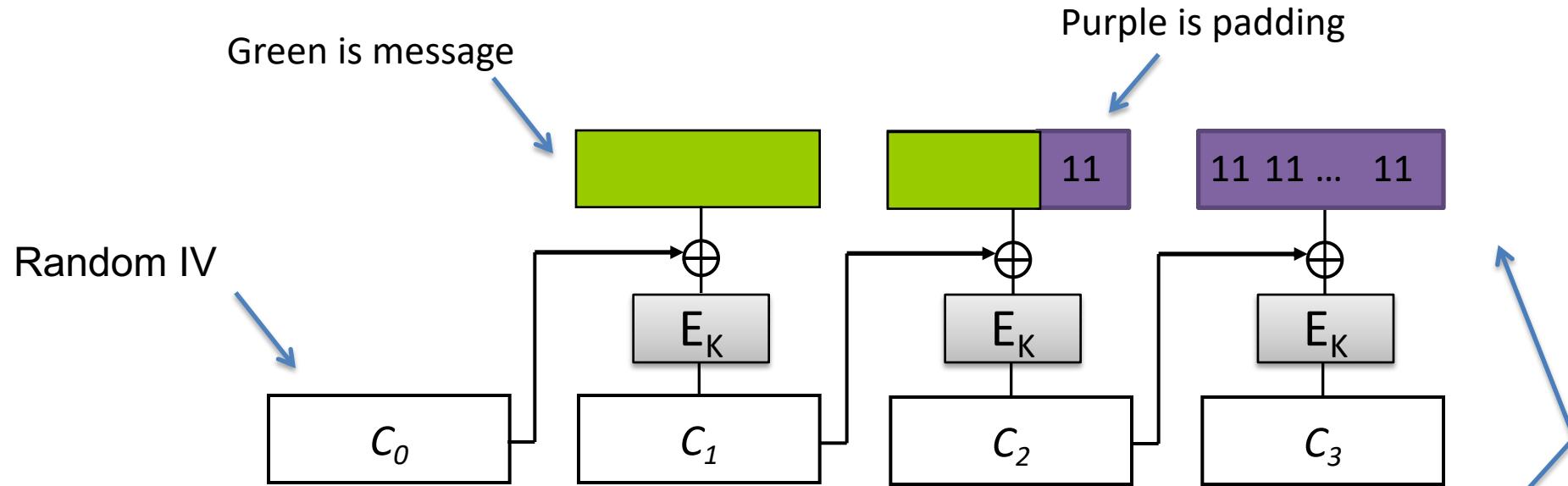
00

01 01

02 02 02

etc.

Padding for CBC Mode in TLS



Possible paddings in TLS:

00

01 01

02 02 02

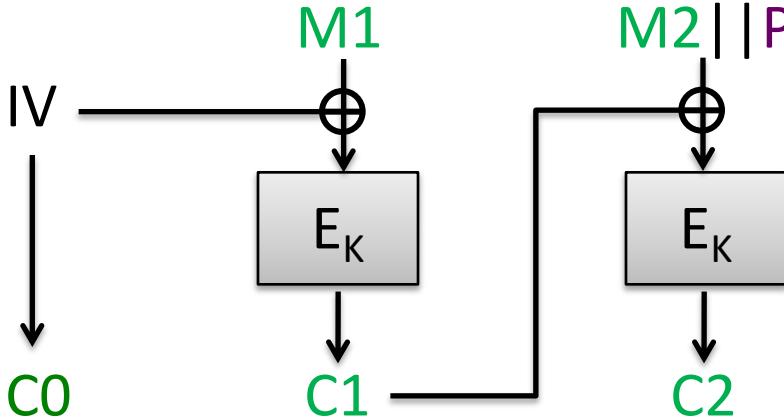
etc.

“Lengths longer than necessary might be desirable to frustrate attacks on a protocol that are based on analysis of the lengths of exchanged messages.”

RFC 5246

Called “traffic analysis attacks”

Vaudenay's padding oracle attack

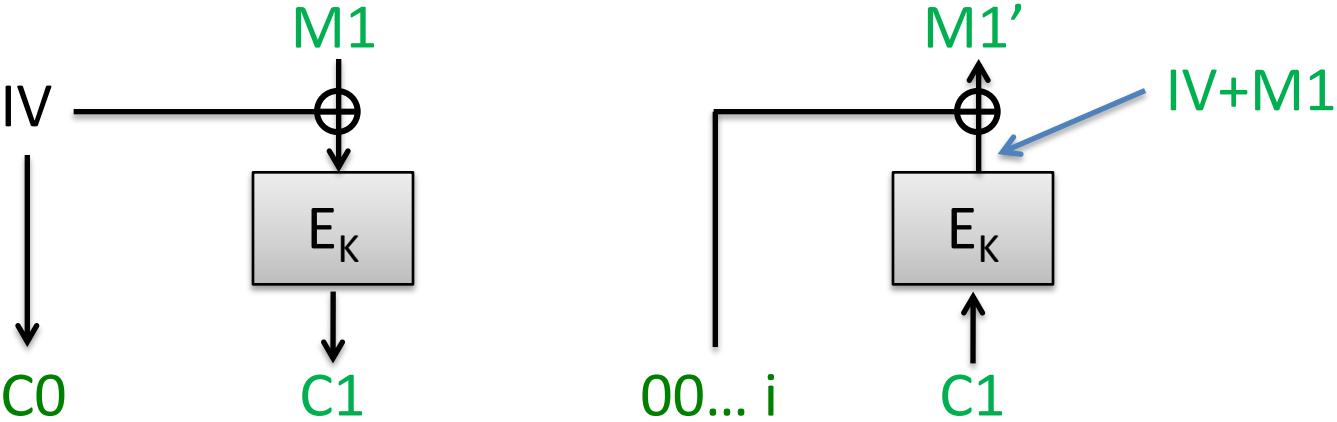


Goal:
Decrypt entire plaintext



```
Dec(K, C')
M1' = CBC-Dec(K,C')
(X,plen) <- lastbyte(M1')
For i = 0 to padlen do
    (X,plen') <- lastbyte(X)
    If plen' != plen
        Return Error
Return Ok
```

Vaudenay's padding oracle attack



We know that:

$$00 = i + IV[n] + M1[n]$$

Or do we? Could be:

$$01 = i + IV[n] + M1[n]$$

$$01 = IV[n-1] + M1[n-1]$$

Easy to exclude other cases

00...00, C1

error

00...01 , C1

error

00...02 , C1

error

...

00... i, C1

ok

Dec(K, C')

$$M1' = \text{CBC-Dec}(K, C')$$

$$(X, plen) \leftarrow \text{lastbyte}(M1')$$

For $i = 0$ to padlen do

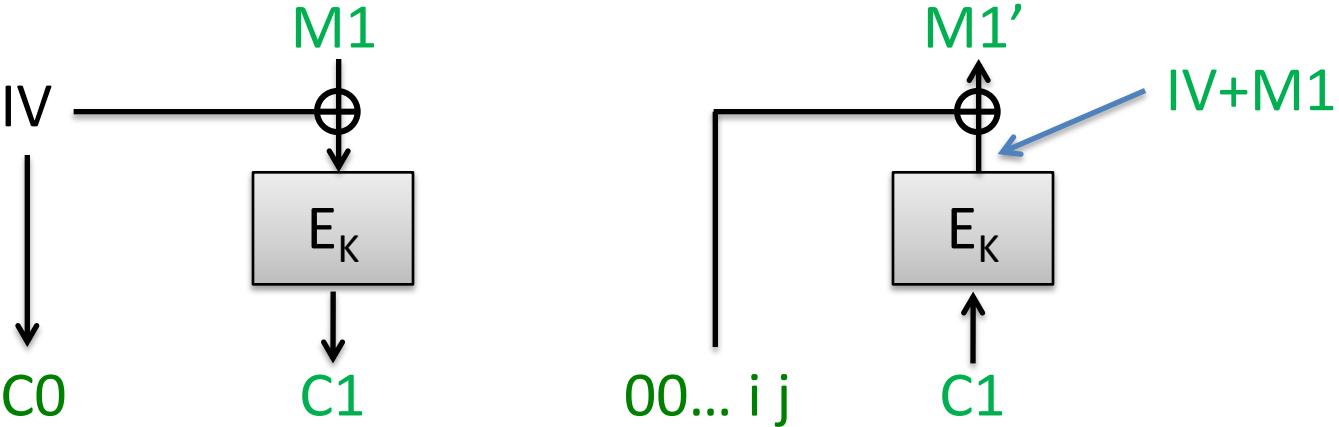
$$(X, plen') \leftarrow \text{lastbyte}(X)$$

If $plen' \neq plen$

Return Error

Return Ok

Vaudenay's padding oracle attack



We know $M_1[n]$. Let's get second to last byte.

Solve j to make $M_1'[n] = 01$
 $01 = j + IV[n] + M_1[n]$

Know that:

$$01 = i + IV[n-1] + M_1[n-1]$$

Repeat for all n bytes

00...00 j , C₁ →

error

00...01 j , C₁ →

error

00...02 j , C₁ →

error

00...i j , C₁ →

ok

Dec(K, C')

$M_1' = \text{CBC-Dec}(K, C')$

$(X, plen) \leftarrow \text{lastbyte}(M_1')$

For $i = 0$ to padlen do
 $(X, plen') \leftarrow \text{lastbyte}(X)$
If $plen' \neq plen$
Return Error

Return Ok

Chosen ciphertext attacks against CBC

Attack	Description	Year
Vaudenay	10's of chosen ciphertexts, recovers message bits from a ciphertext. Called "padding oracle attack"	2001
Canvel et al.	Shows how to use Vaudenay's ideas against TLS	2003
Degabriele, Paterson	Breaks IPsec encryption-only mode	2006
Albrecht et al.	Plaintext recovery against SSH	2009
Duong, Rizzo	Breaking ASP.net encryption	2011
Jager, Somorovsky	XML encryption standard	2011
Duong, Rizzo	"Beast" attacks against TLS	2011

In-class exercise

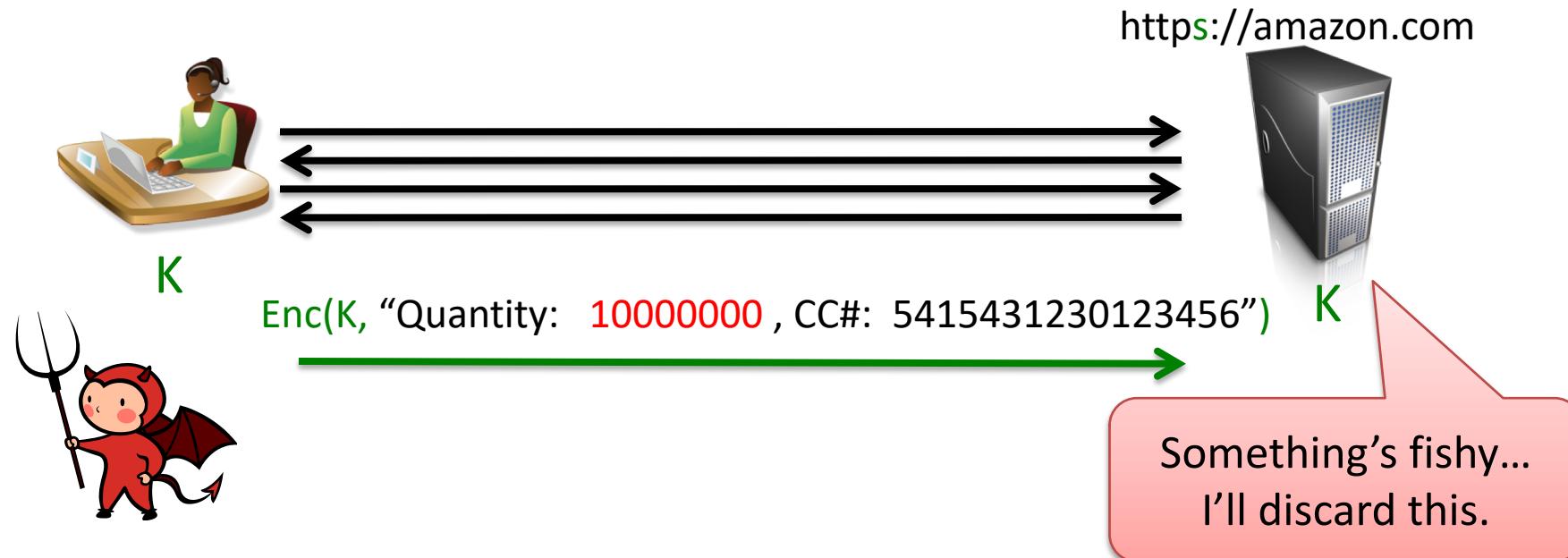
- Take five minutes and discuss with your neighbor...
 - Are padding oracles possible against CTR mode?
 - Are padding oracles possible against ECB mode?
 - How would you prevent padding oracle attacks?
Cryptographic countermeasure or “system-level”?

We need new primitives

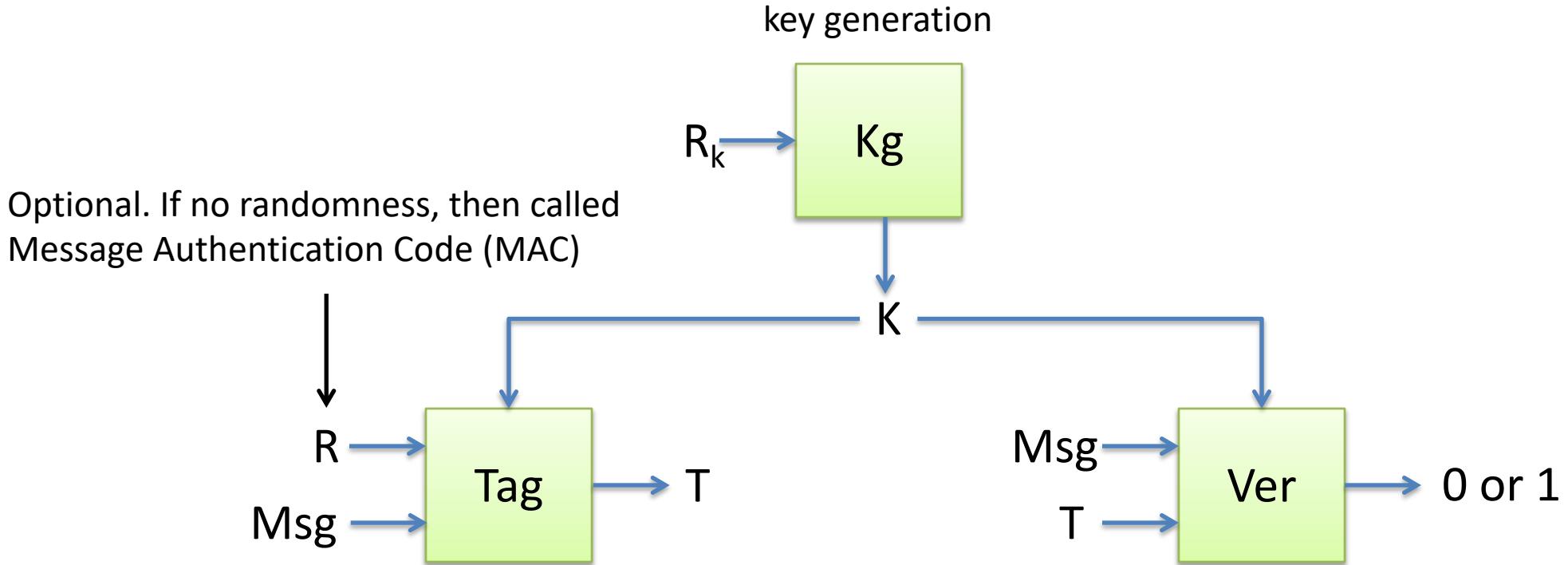
Message authentication makes malicious modifications detectable

Goal is *authenticated encryption* (AE): Hide message and detect modifications

Can build by combining encryption with message authentication scheme

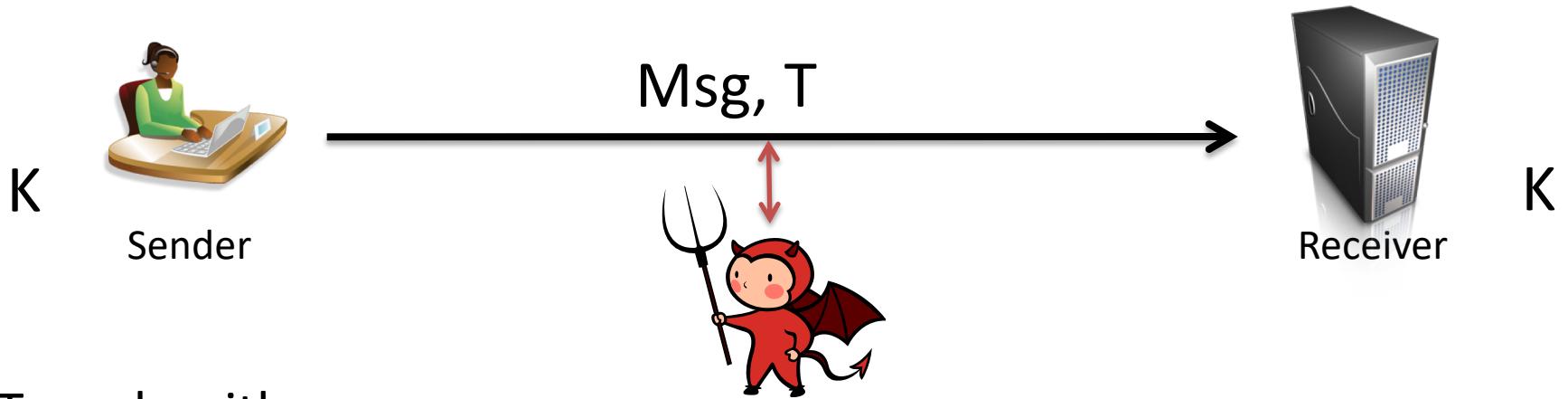


Message authentication



Correctness: $\text{Ver}(K , \text{Tag}(K,\text{Msg},R)) = 1$ with probability 1 over randomness R used

Message authentication



Two algorithms:

- (1) $\text{Tag}(K, \text{Msg})$ outputs a tag T
- (2) $\text{Verify}(K, \text{Msg}, T)$ outputs 0/1 (invalid / valid)

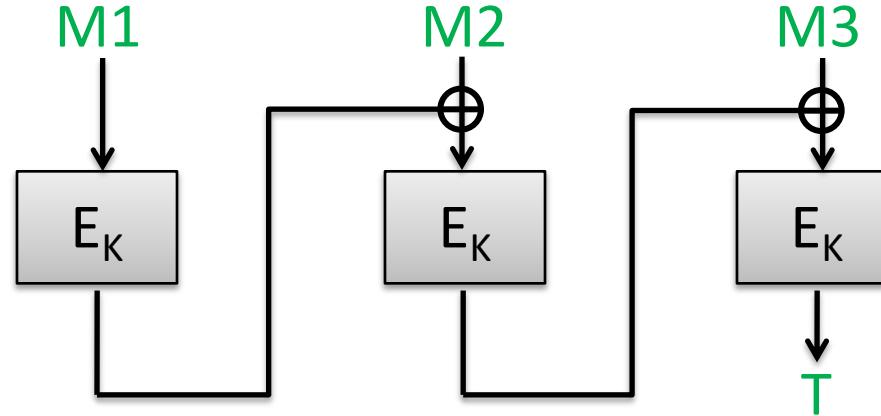
Security: No computationally efficient attacker can forge tags for a new message even when attacker gets

$$(\text{Msg}_1, T_1), (\text{Msg}_2, T_2), \dots, (\text{Msg}_q, T_q)$$

for messages of his choosing and reasonably large q .

CBC-MAC

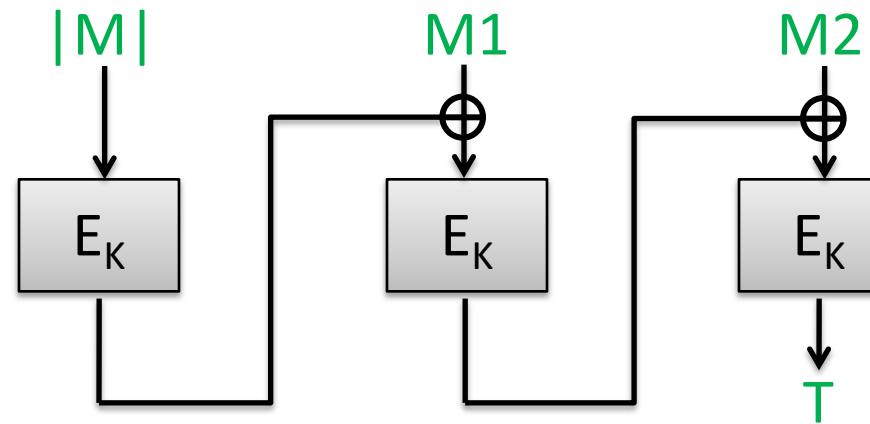
Split Msg into blocks M_1, M_2, M_3



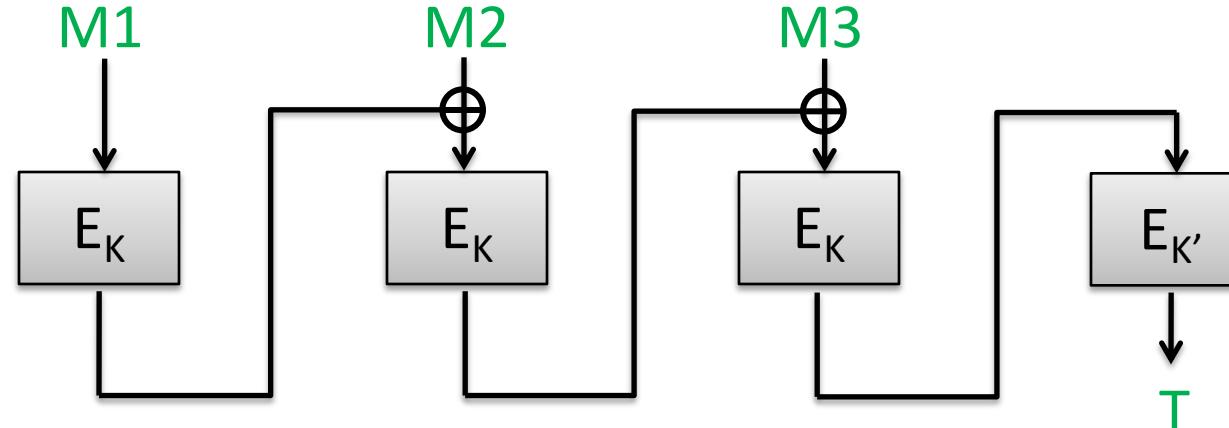
Turns out this is secure MAC
if K used only on same-length messages

Variable-message-length CBC-MAC

- Prepend message length

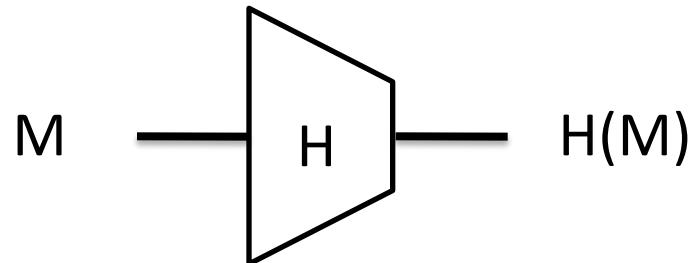


- Encrypted CBC-MAC



Hash functions and message authentication

Hash function H maps arbitrary bit string to fixed length string of size m



~~MD5: $m = 128$ bits~~
~~SHA-1: $m = 160$ bits~~
SHA-256: $m = 256$ bits

Some security goals:

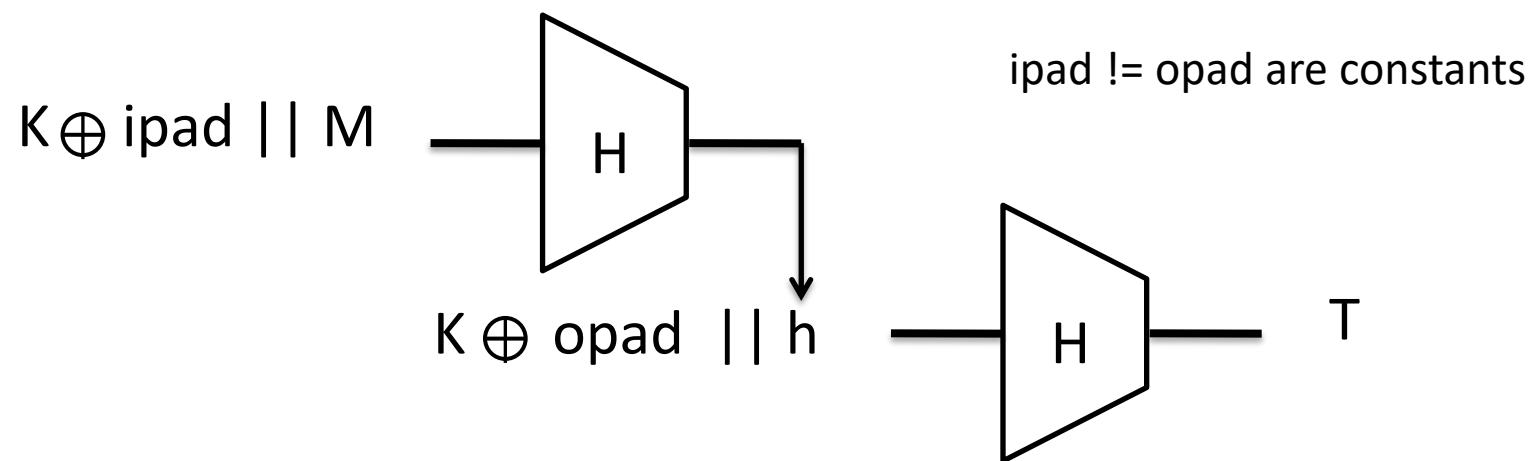
- collision resistance: can't find $M \neq M'$ such that $H(M) = H(M')$
- “behaves like” random function: $H(M)$ is uniformly distributed bit string for all M
- Sometimes called the random oracle model (ROM)

Message authentication with HMAC

Use a hash function H to build MAC.

K_g outputs uniform bit string K

$\text{Tag}(K, M) = \text{HMAC}(K, M)$ defined by:

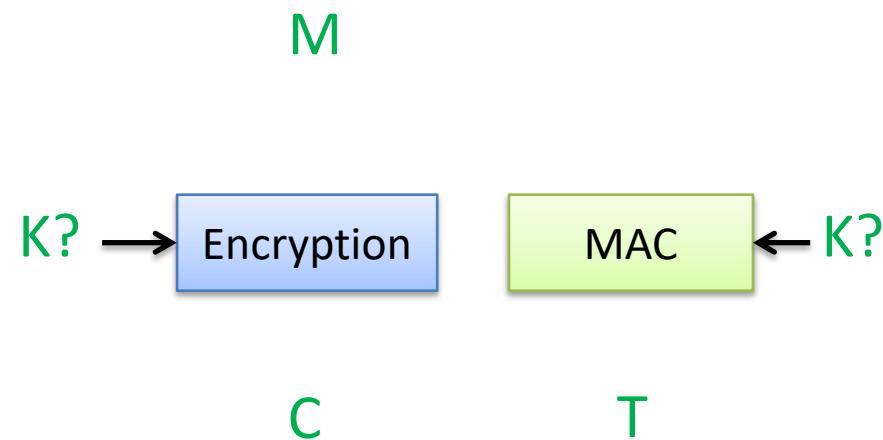


To verify a M, T pair, check if $\text{HMAC}(K, M) = T$

Unforgeability holds if H behaves like a random function

Build *authenticated encryption*...?

- Recall that our goal is authenticated encryption
- Want to combine some encryption scheme with a MAC
 - how do we do this? Any ideas?

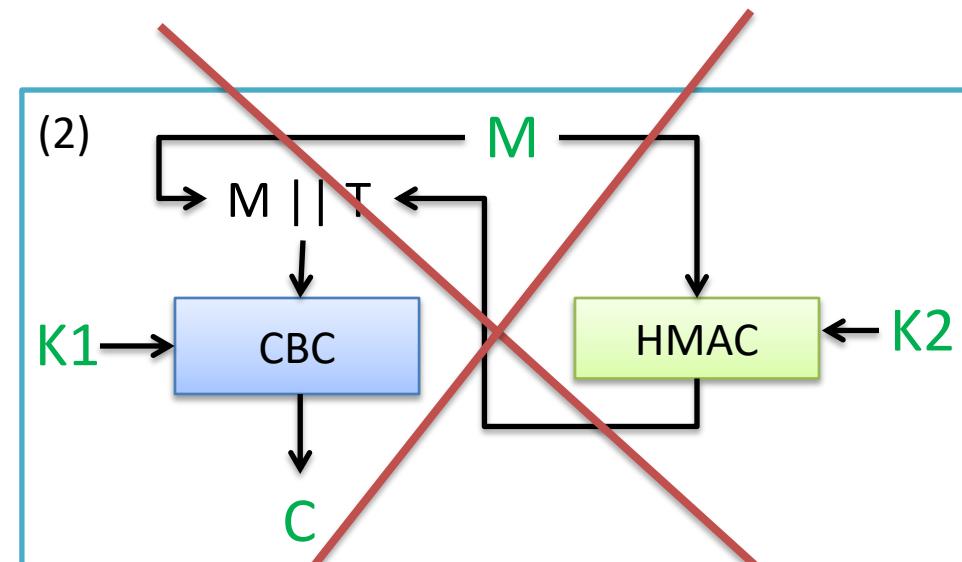
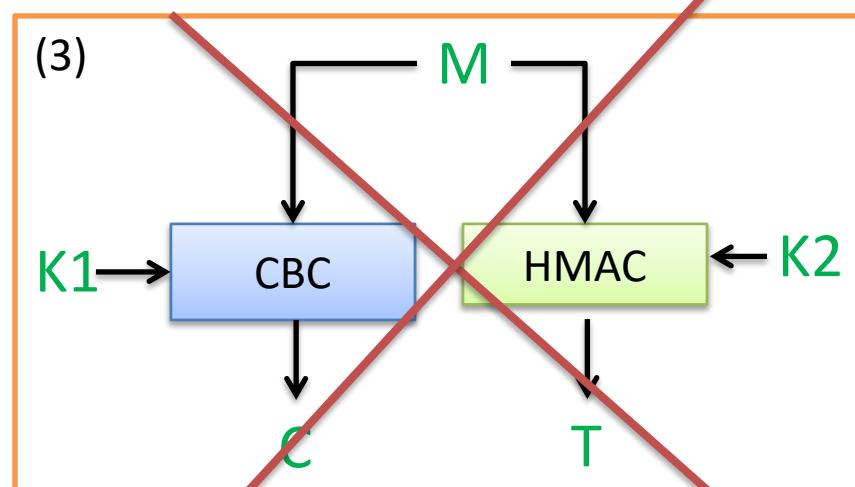
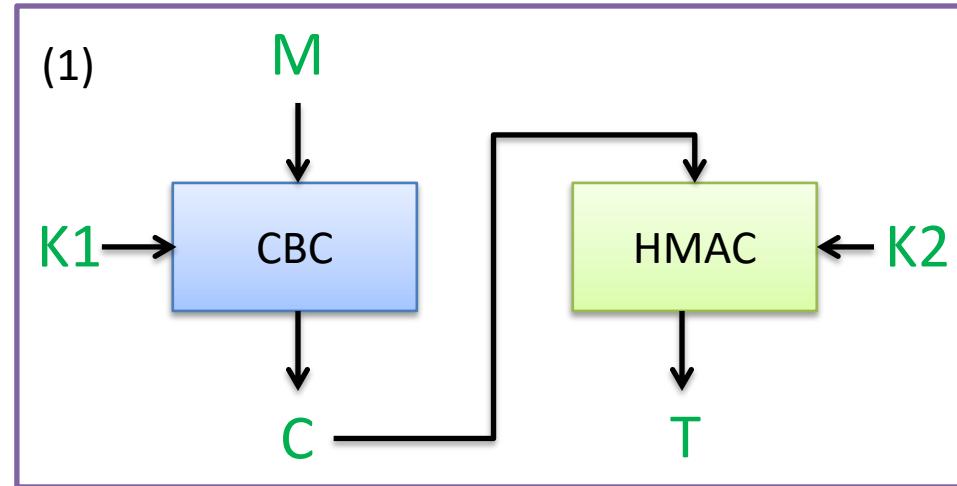


Build a new scheme from CBC and HMAC

Kg outputs CBC key K1 and HMAC key K2

Several ways to combine:

- (1) encrypt-then-mac
- (2) mac-then-encrypt
- (3) encrypt-and-mac

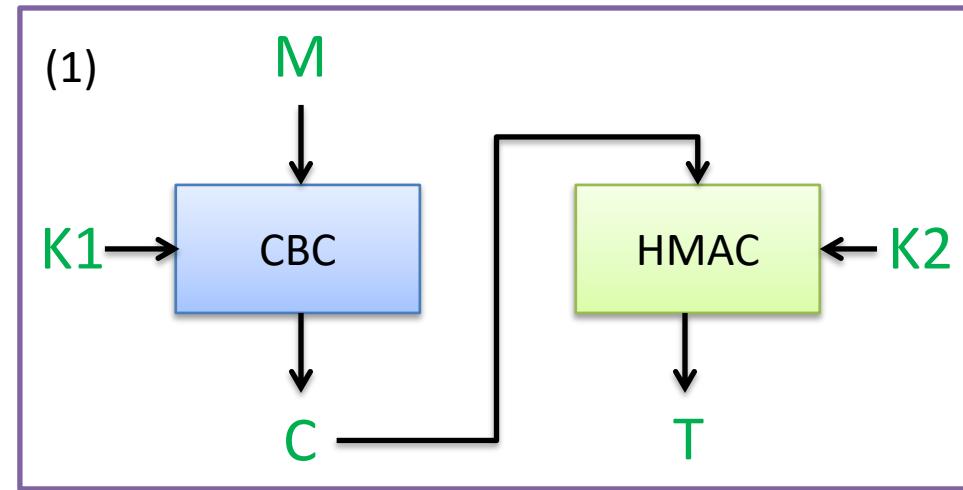


Build a new scheme from CBC and HMAC

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Several ways to combine:

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- (3) encrypt-and-mac



Thm. If encryption scheme provides confidentiality against passive attackers and MAC provides unforgeability, then Encrypt-then-MAC provides secure authenticated encryption

Dedicated authenticated encryption schemes

Attack	Inventor(s)	Notes
OCB (Offset Codebook)	Rogaway	One-pass mode and fastest
AES-GCM (Galois Counter Mode)	McGrew, Viega	CTR mode plus Carter-Wegman MAC
ChaCha20/Poly1305	Bernstein	“essentially” CTR mode plus special Carter-Wegman MAC
CCM	Housley, Ferguson, Whiting	CTR mode plus CBC-MAC
EAX	Wagner, Bellare, Rogaway	CTR mode plus OMAC

Other considerations in AE:

robustness & IV misuse, deterministic AE, associated data, ...

Next time: asymmetric cryptography

So far we've seen how to encrypt using shared key

We'll introduce asymmetric cryptography next lecture