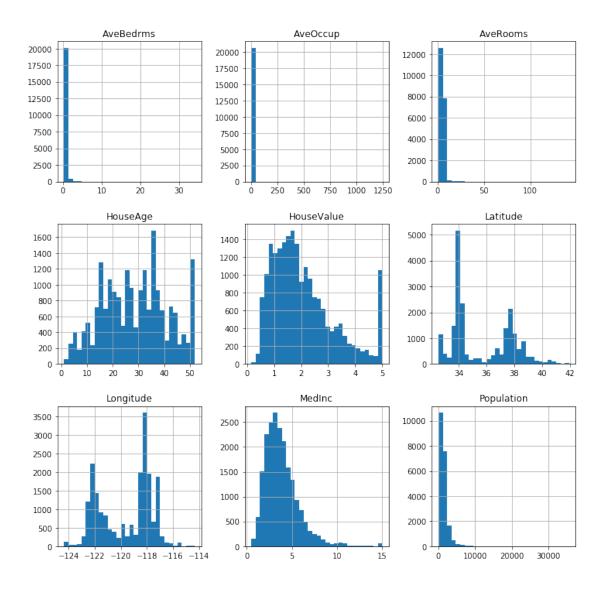
## Task 1

## February 7, 2018

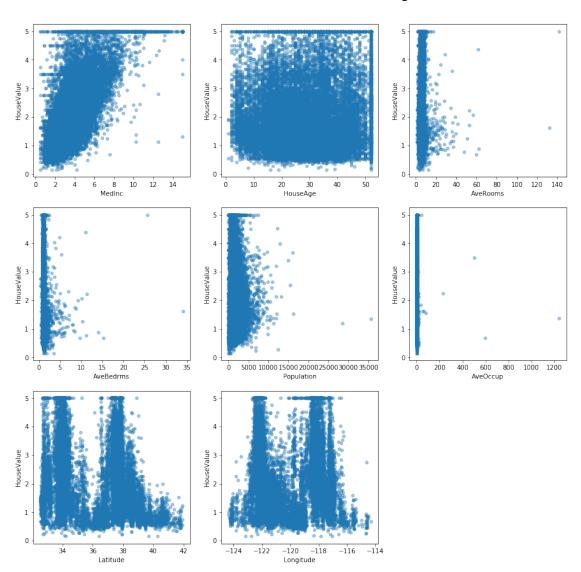
```
In [1]: import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        %matplotlib inline
In [2]: from sklearn.datasets import fetch_california_housing
        from sklearn.linear_model import LinearRegression, Lasso, Ridge, ElasticNet
        from sklearn.model_selection import train_test_split, cross_val_score, GridSearchCV
        from sklearn.preprocessing import StandardScaler
In [3]: calhouse = fetch_california_housing(data_home='task1_data')
In [4]: calhouse_df = pd.DataFrame(calhouse.data, columns=calhouse.feature_names)
0.0.1 Task 1.1: Visualize the univariate distribution of each feature, and the distribution of the
      target
In [5]: #Visualize distribution of each feature, including target feature
        calhouse_target_df = calhouse_df
        calhouse_target_df = calhouse_target_df.assign(HouseValue = calhouse.target)
        fig2 = plt.figure(figsize = (12,12))
        _ = calhouse_target_df.hist(bins = 30, ax = plt.gca())
/home/tungngo/anaconda2/envs/py36/lib/python3.6/site-packages/IPython/core/interactiveshell.py:2
  exec(code_obj, self.user_global_ns, self.user_ns)
```



#### Observations:

- Outliers in AveRooms, AveBedrms, Population, AveOccup.
  - Most values of these variables are small, except for very small number of data points having big values
- Target value variable HouseValue goes up toward the end. Same observation for HouseAge.
  - HouseValue has 965 values = 5.00001
  - HouseAge 1273 values = 52

### 0.0.2 Task 1.2: Visualize the dependency of the target on each feature



# 0.0.3 Task 1.3: Evaluate Linear Regression (OLS), Ridge, Lasso and ElasticNet using cross-validation with the default parameters

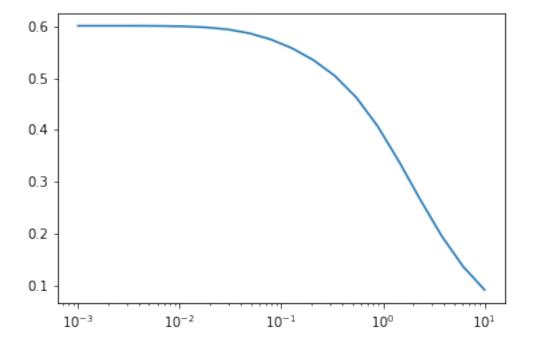
```
In [9]: print("linear regression score: {}".format(lr_score))
       print("ridge regression score: {}".format(ridge_score))
        print("lasso regression score: {}".format(lasso_score))
        print("elastic net score: {}".format(enet_score))
linear regression score: 0.6009222504208382
ridge regression score: 0.6009322158862299
lasso regression score: 0.27846544566928083
elastic net score: 0.41865896236326555
In [10]: #Use Standard scaler to scale data
         scaler = StandardScaler()
         scaler.fit(X_train)
         X_train_scaled = scaler.transform(X_train)
In [11]: #Use scaled data for regression
         slr_score = np.mean(cross_val_score(LinearRegression(), X_train_scaled, y_train))
         sridge_score = np.mean(cross_val_score(Ridge(random_state=20),X_train_scaled,y_train))
         slasso_score = np.mean(cross_val_score(Lasso(random_state=20),X_train_scaled,y_train))
         senet_score = np.mean(cross_val_score(ElasticNet(random_state=20),X_train_scaled,y_train_scaled)
In [12]: print("linear regression score (scaled): {}".format(slr_score))
         print("ridge regression score (scaled): {}".format(sridge_score))
         print("lasso regression score (scaled): {}".format(slasso_score))
         print("elastic net score (scaled): {}".format(senet_score))
linear regression score (scaled): 0.6009222504208398
ridge regression score (scaled): 0.6009303872146475
lasso regression score (scaled): -0.0005254527749588936
elastic net score (scaled): 0.19901416988152856
In [13]: print("linear regression scaled vs non-scaled: {}".format(slr_score-lr_score))
         print("ridge regression scaled vs non-scaled: {}".format(sridge_score-ridge_score))
         print("lasso regression scaled vs non-scaled: {}".format(slasso_score-lasso_score))
         print("elastic net scaled vs non-scaled: {}".format(senet_score-enet_score))
linear regression scaled vs non-scaled: 1.5543122344752192e-15
ridge regression scaled vs non-scaled: -1.828671582382313e-06
lasso regression scaled vs non-scaled: -0.27899089844423974
elastic net scaled vs non-scaled: -0.219644792481737
```

Scaling the data does not help improve performance of linear regression or ridge regression. It even worsens the performance of lasso regression and elastic net.

### 0.0.4 Task 1.4: Tune the parameters of the models using GridSearchCV

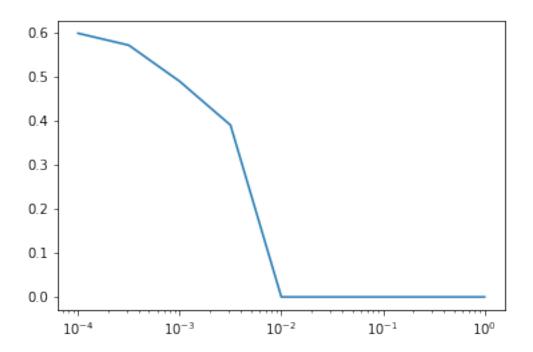
```
In [14]: param_grid_ridge = {'alpha': np.logspace(-3, 1, 20)}
        grid_ridge = GridSearchCV(Ridge(random_state=20, normalize=True), param_grid_ridge)
        grid_ridge.fit(X_train, y_train)
Out[14]: GridSearchCV(cv=None, error_score='raise',
                estimator=Ridge(alpha=1.0, copy_X=True, fit_intercept=True, max_iter=None,
           normalize=True, random_state=20, solver='auto', tol=0.001),
               fit_params=None, iid=True, n_jobs=1,
               param_grid={'alpha': array([ 1.00000e-03, 1.62378e-03,
                                                                           2.63665e-03,
                                                                                          4.281
                                                              2.97635e-02,
                 6.95193e-03, 1.12884e-02, 1.83298e-02,
                  4.83293e-02, 7.84760e-02, 1.27427e-01, 2.06914e-01,
                  3.35982e-01, 5.45559e-01, 8.85867e-01, 1.43845e+00,
                  2.33572e+00, 3.79269e+00,
                                               6.15848e+00,
                                                              1.00000e+01])},
               pre_dispatch='2*n_jobs', refit=True, return_train_score=True,
               scoring=None, verbose=0)
In [15]: print(grid_ridge.best_params_)
        print(grid_ridge.best_score_)
{'alpha': 0.001623776739188721}
0.600990210481
In [16]: param_grid_lasso = {'alpha': np.logspace(-4, 0, 9)}
        grid_lasso = GridSearchCV(Lasso(random_state=20, normalize=True), param_grid_lasso)
        grid_lasso.fit(X_train, y_train)
Out[16]: GridSearchCV(cv=None, error_score='raise',
                estimator=Lasso(alpha=1.0, copy_X=True, fit_intercept=True, max_iter=1000,
           normalize=True, positive=False, precompute=False, random_state=20,
           selection='cyclic', tol=0.0001, warm_start=False),
               fit_params=None, iid=True, n_jobs=1,
               param_grid={'alpha': array([ 1.00000e-04, 3.16228e-04,
                                                                           1.00000e-03,
                                                                                          3.162
                  1.00000e-02, 3.16228e-02, 1.00000e-01,
                                                              3.16228e-01,
                  1.00000e+00])},
               pre_dispatch='2*n_jobs', refit=True, return_train_score=True,
               scoring=None, verbose=0)
In [17]: print(grid_lasso.best_params_)
        print(grid_lasso.best_score_)
{'alpha': 0.0001}
0.598328713871
In [18]: param_grid_elastic = {'alpha': np.logspace(-4, -1, 7),
                       'l1_ratio': [0.01, .1, .5, .9, .98, 1]}
        grid_elastic = GridSearchCV(ElasticNet(random_state=20, normalize=True), param_grid_ela
        grid_elastic.fit(X_train, y_train)
```

In [20]: #Visualize the dependence of the validation score on the parameters for Ridge, Lasso an ridge\_line, = plt.semilogx(param\_grid\_ridge['alpha'],grid\_ridge.cv\_results\_['mean\_test\_



0.598328713871

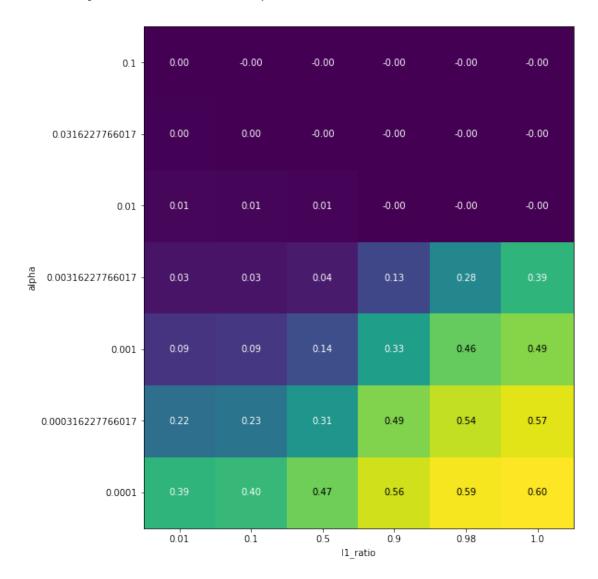
In [21]: lasso\_line, = plt.semilogx(param\_grid\_lasso['alpha'],grid\_lasso.cv\_results\_['mean\_test\_



```
In [22]: elastic_net_para = pd.pivot_table(pd.DataFrame(grid_elastic.cv_results_),
             values='mean_test_score', index='param_alpha', columns='param_l1_ratio')
In [23]: def heatmap(values, xlabel, ylabel, xticklabels, yticklabels, cmap=None,
                     vmin=None, vmax=None, ax=None, fmt="%0.2f"):
             if ax is None:
                 ax = plt.gca()
             # plot the mean cross-validation scores
             img = ax.pcolor(values, cmap=cmap, vmin=vmin, vmax=vmax)
             img.update_scalarmappable()
             ax.set_xlabel(xlabel)
             ax.set_ylabel(ylabel)
             ax.set_xticks(np.arange(len(xticklabels)) + .5)
             ax.set_yticks(np.arange(len(yticklabels)) + .5)
             ax.set_xticklabels(xticklabels)
             ax.set_yticklabels(yticklabels)
             ax.set_aspect(1)
             for p, color, value in zip(img.get_paths(), img.get_facecolors(),
                                         img.get_array()):
                 x, y = p.vertices[:-2, :].mean(0)
                 if np.mean(color[:3]) > 0.5:
                     c = {}^{1}k^{1}
                 else:
                     c = w^{\dagger}
```

```
ax.text(x, y, fmt % value, color=c, ha="center", va="center")
return img
```

Out[24]: <matplotlib.collections.PolyCollection at 0x7f1b741e7b00>

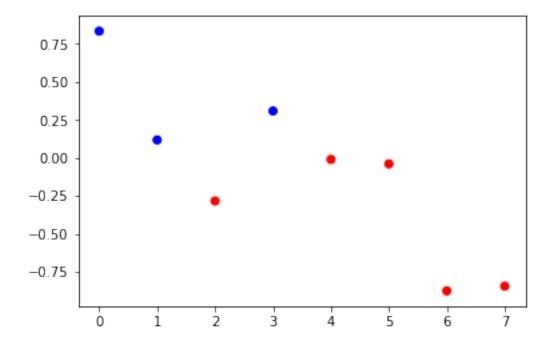


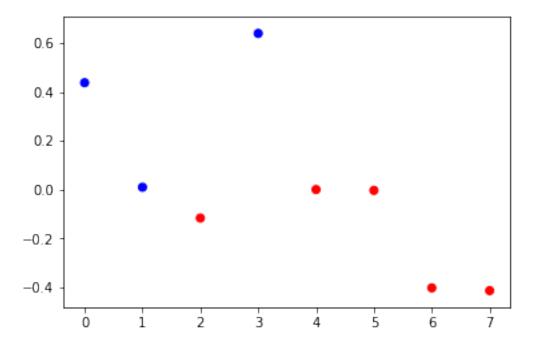
Tuning the parameter helps Lasso regression and Elastic Net approach the accuracy of linear regression and ridge regression, but tuning does not help improve the accuracy of the best model. The best score still stays at 60.1% - belongs to linear regression and ridge regression.

### 0.0.5 Task 1.5

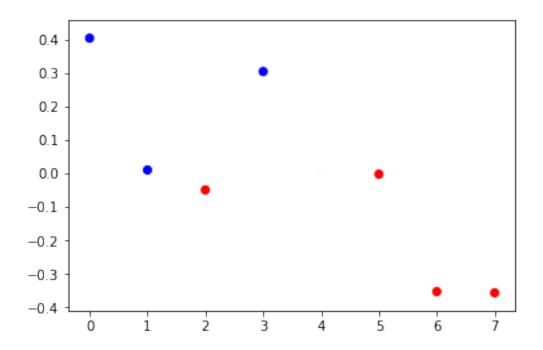
In [25]: #Visualize the coefficients of the resulting models

Out[26]: <matplotlib.collections.PathCollection at 0x7f1b740d05c0>

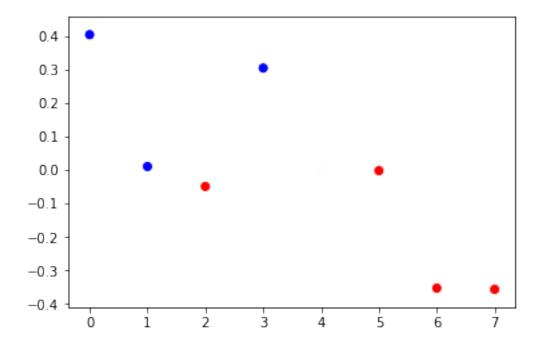




Out[29]: <matplotlib.collections.PathCollection at 0x7f1b74088160>



Out[30]: <matplotlib.collections.PathCollection at 0x7f1b6f7dc198>



All models agree on which features have positive or negative coefficients. However, the resulting models differ in term of scale of features. While linear regression seems to take negative and positive-coefficient features to the extreme, ridge regression scales down these coefficients - which is expected from the effect of regularization. We can say the same about lasso regression and elastic net when compared with linear regression (for example, features 0,6,7 are lower in absolute values in the 3 models - around 0.4 - compared to linear regression around 0.8). The resulting models of lasso regression and elastic net are very similar as the l1 ratio of elastic net is 1. Final observation is that feature 3 of ridge regression have higher importance - positive coefficient of around 0.6 - compared to other 3 models - coefficient of around 0.3

## Task 2

## February 7, 2018

```
In [1]: import pandas as pd
       import numpy as np
        import matplotlib.pyplot as plt
       import seaborn as sns
        sns.set()
       %matplotlib inline
In [2]: from sklearn.linear_model import LogisticRegression
       from sklearn.svm import LinearSVC
       from sklearn.neighbors import NearestCentroid
       from sklearn.model_selection import train_test_split, cross_val_score, GridSearchCV, KFc
       from sklearn.preprocessing import StandardScaler
In [3]: from sklearn.datasets import fetch_covtype
In [4]: data = fetch_covtype(data_home='task2_data')
In [5]: data
Out[5]: {'DESCR': 'Forest covertype dataset.\n\nA classic dataset for classification benchmarks,
         'data': array([[ 2.59600000e+03,
                                            5.10000000e+01,
                                                              3.00000000e+00, ...,
                  0.0000000e+00,
                                    0.0000000e+00,
                                                      0.0000000e+00],
                [ 2.59000000e+03,
                                    5.60000000e+01,
                                                      2.00000000e+00, ...,
                  0.0000000e+00, 0.0000000e+00,
                                                      0.0000000e+00],
                [ 2.80400000e+03,
                                    1.39000000e+02,
                                                      9.0000000e+00, ...,
                  0.0000000e+00,
                                    0.0000000e+00,
                                                      0.00000000e+00],
                [ 2.38600000e+03,
                                    1.59000000e+02,
                                                      1.70000000e+01, ...,
                  0.0000000e+00,
                                    0.00000000e+00,
                                                      0.0000000e+00],
                [ 2.38400000e+03,
                                    1.70000000e+02,
                                                      1.50000000e+01, ...,
                  0.0000000e+00, 0.0000000e+00,
                                                      0.0000000e+00],
                [ 2.38300000e+03,
                                   1.65000000e+02,
                                                      1.3000000e+01, ...,
                  0.00000000e+00,
                                                      0.0000000e+00]]),
                                    0.00000000e+00,
         'target': array([5, 5, 2, ..., 3, 3, 3], dtype=int32)}
In [6]: cov = pd.DataFrame(data['data'])
        cov['Cover_Type'] = data['target']
```

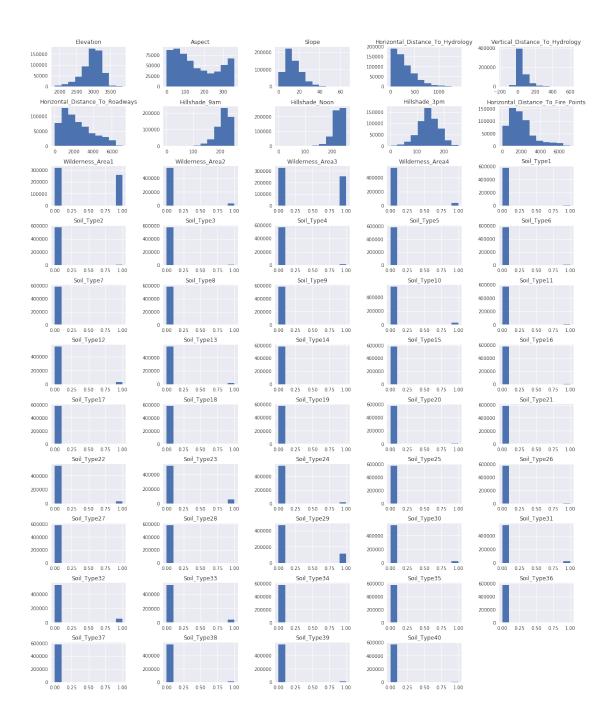
```
In [7]: # Get column names
        feature_file = open('feature_names','r')
        features = []
        for line in feature_file:
            features.append(line.split()[0])
In [8]: wildareas = [features[10] + str(i) for i in range(1,5)]
        soiltypes = [features[11] + str(i) for i in range(1,41)]
        features = features[:10] + wildareas + soiltypes + [features[12]]
In [9]: cov.columns = features
In [10]: cov.head()
Out[10]:
            Elevation Aspect Slope Horizontal_Distance_To_Hydrology \
               2596.0
                          51.0
                                  3.0
                                                                    258.0
                                  2.0
         1
               2590.0
                          56.0
                                                                    212.0
         2
               2804.0
                         139.0
                                  9.0
                                                                    268.0
         3
               2785.0
                         155.0
                                 18.0
                                                                    242.0
         4
               2595.0
                          45.0
                                  2.0
                                                                    153.0
            Vertical_Distance_To_Hydrology Horizontal_Distance_To_Roadways \
         0
                                        0.0
                                                                         510.0
                                        -6.0
         1
                                                                         390.0
         2
                                       65.0
                                                                        3180.0
         3
                                      118.0
                                                                        3090.0
         4
                                        -1.0
                                                                         391.0
            Hillshade_9am Hillshade_Noon Hillshade_3pm \
         0
                     221.0
                                     232.0
                                                     148.0
         1
                     220.0
                                     235.0
                                                     151.0
                     234.0
         2
                                     238.0
                                                     135.0
         3
                     238.0
                                     238.0
                                                     122.0
                     220.0
         4
                                     234.0
                                                     150.0
            Horizontal_Distance_To_Fire_Points
                                                               Soil_Type32 Soil_Type33 \
         0
                                          6279.0
                                                     . . .
                                                                       0.0
                                                                                     0.0
                                          6225.0
                                                                       0.0
                                                                                     0.0
         1
                                                     . . .
         2
                                          6121.0
                                                                       0.0
                                                                                     0.0
                                                     . . .
         3
                                          6211.0
                                                                       0.0
                                                                                     0.0
                                                     . . .
         4
                                          6172.0
                                                                       0.0
                                                                                     0.0
                                                     . . .
            Soil_Type34 Soil_Type35 Soil_Type36
                                                     Soil_Type37
                                                                  Soil_Type38 \
         0
                     0.0
                                  0.0
                                                0.0
                                                              0.0
                                                                           0.0
                     0.0
                                  0.0
                                                0.0
                                                              0.0
                                                                           0.0
         1
                     0.0
                                  0.0
                                                0.0
                                                              0.0
                                                                           0.0
         2
         3
                     0.0
                                  0.0
                                                0.0
                                                              0.0
                                                                           0.0
         4
                     0.0
                                  0.0
                                                0.0
                                                              0.0
                                                                           0.0
```

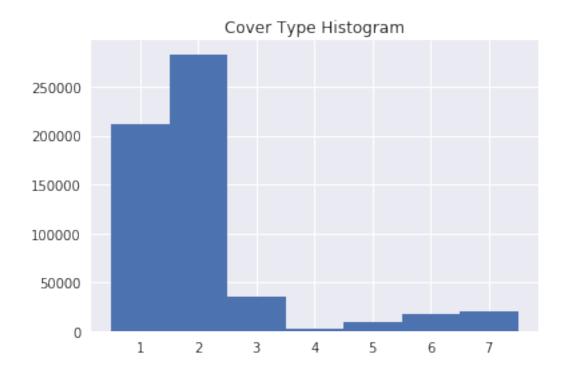
```
Soil_Type39 Soil_Type40 Cover_Type
0
           0.0
                        0.0
                                       5
                                       5
1
           0.0
                         0.0
2
           0.0
                         0.0
                                       2
                                       2
           0.0
                         0.0
3
           0.0
                         0.0
                                       5
4
```

[5 rows x 55 columns]

```
In [11]: cov.shape
Out[11]: (581012, 55)
```

# 0.0.1 Task 2.1: Visualize the univariate distribution of each feature, and the distribution of the target





# 0.0.2 Task 2.2: Split data into training and test set. Evaluate Logistic Regression, linear support vector machines and nearest centroids using cross-validation

0.705947542451 0.194639694306

Logistic regression and Linear SVM have close scores - Logistic regression is slightly better, while Nearest Centroid has very bad score compared to other 2 algorithms. When applying StandardScaler, all 3 algorithms improve in score: logistic regression from 70.8% to 71.5%, linear SVM from 70.6% to 71.3%. Nearest Centroid improves the greatest from 19.5% to 54.9%, althought final score is still far behind other 2 algorithms.

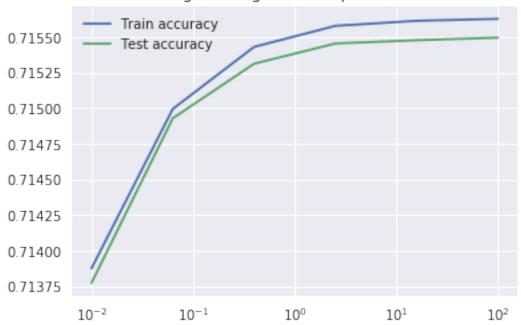
### 0.0.3 Task 2.3: Tune the parameters using GridSearchCV

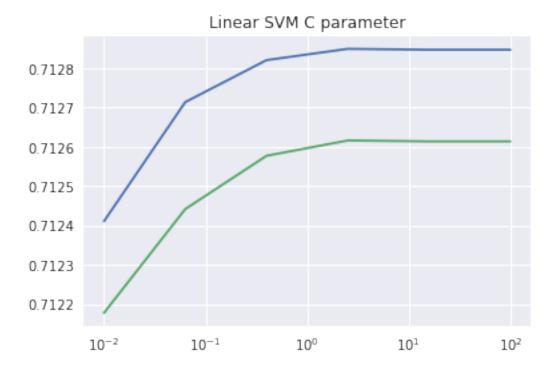
```
In [22]: #Tune logistic regression
         param_grid_logit = {'C':np.logspace(-2,2,6)}
         grid_logit = GridSearchCV(LogisticRegression(tol=0.0001,random_state=20), param_grid_logit
         grid_logit.fit(X_train_scaled, y_train)
         print(grid_logit.best_params_)
         print(grid_logit.best_score_)
{'C': 100.0}
0.715496409713
In [23]: #Tune Linear SVM
         param_grid_svm = {'C':np.logspace(-2,2,6)}
         grid_svm = GridSearchCV(LinearSVC(tol=0.0001, dual=False, random_state=20), param_grid_
         grid_svm.fit(X_train_scaled, y_train)
         print(grid_svm.best_params_)
         print(grid_svm.best_score_)
{'C': 2.5118864315095824}
0.712616377401
In [24]: #Tune Nearest Centroid
         param_grid_NC = {'shrink_threshold':np.linspace(0,20,11)}
```

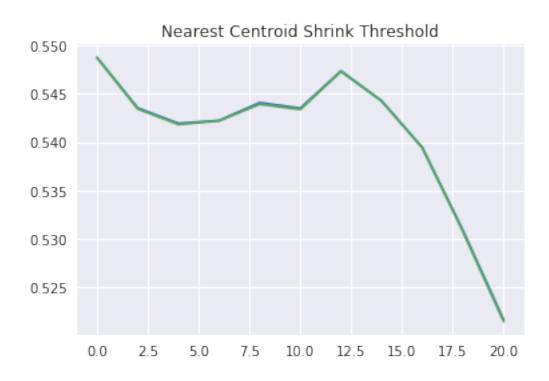
### In [25]: #Visualize GridSearch results

```
plt.semilogx(param_grid_logit['C'],grid_logit.cv_results_['mean_train_score'],label='Tr
plt.semilogx(param_grid_logit['C'],grid_logit.cv_results_['mean_test_score'],label='Tes
_ = plt.title('Logistic Regression C parameter')
_ = plt.legend()
```

# Logistic Regression C parameter







After GridSearch, the scores for all 3 algorithms do not improve by too much.

# 0.0.4 Task 2.4: Change the cross-validation strategy from 'stratified k-fold' to 'kfold' with shuffling

```
In [28]: #Change cross-validation strategy to KFold with shuffling and run GridSearch
         kfoldshuffle = KFold(shuffle=True, random_state=1)
In [29]: #Tune logistic regression with KFold with shuffling
         grid_logit_kfold = GridSearchCV(LogisticRegression(tol=0.0001,random_state=20), param_g
         grid_logit_kfold.fit(X_train_scaled, y_train)
         print(grid_logit_kfold.best_params_)
         print(grid_logit_kfold.best_score_)
{'C': 100.0}
0.715503294252
In [30]: #Tune Linear SVM with KFold with shuffling
         grid_svm_kfold = GridSearchCV(LinearSVC(tol=0.0001, dual= False, random_state=20), para
         grid_svm_kfold.fit(X_train_scaled, y_train)
         print(grid_svm_kfold.best_params_)
         print(grid_svm_kfold.best_score_)
{'C': 2.5118864315095824}
0.712731119724
In [31]: #Tune Nearest Centroid with KFold with shuffling
         grid_NC_kfold = GridSearchCV(NearestCentroid(), param_grid_NC,cv=kfoldshuffle)
         grid_NC_kfold.fit(X_train_scaled, y_train)
         print(grid_NC_kfold.best_params_)
         print(grid_NC_kfold.best_score_)
{'shrink_threshold': 0.0}
0.548782698694
In [32]: #Change random seed of the shuffling
        kfoldshuffle2 = KFold(shuffle=True, random_state=2)
In [33]: #Tune logistic regression with KFold with shuffling
         grid_logit_kfold2 = GridSearchCV(LogisticRegression(tol=0.0001,random_state=20), param_
         grid_logit_kfold2.fit(X_train_scaled, y_train)
         print(grid_logit_kfold2.best_params_)
         print(grid_logit_kfold2.best_score_)
```

```
{'C': 15.848931924611142}
0.715455102476
In [34]: #Tune Linear SVM with KFold with shuffling
         grid_svm_kfold2 = GridSearchCV(LinearSVC(tol=0.0001,dual=False, random_state=20), param
         grid_svm_kfold2.fit(X_train_scaled, y_train)
         print(grid_svm_kfold2.best_params_)
         print(grid_svm_kfold2.best_score_)
{'C': 15.848931924611142}
0.71274718365
In [35]: #Tune Nearest Centroid with KFold with shuffling
         grid_NC_kfold2 = GridSearchCV(NearestCentroid(), param_grid_NC,cv=kfoldshuffle2)
         grid_NC_kfold2.fit(X_train_scaled, y_train)
         print(grid_NC_kfold2.best_params_)
         print(grid_NC_kfold2.best_score_)
{'shrink_threshold': 0.0}
0.548617469748
In [52]: #Change random state of split and run GridSearch
         X_train3, X_test3, y_train3, y_test3 = train_test_split(data['data'],data['target'],ran
         X_train3_scaled = scaler.fit_transform(X_train3)
In [56]: #Tune logistic regression with different random split
         grid_logit_split2 = GridSearchCV(LogisticRegression(tol=0.0001,random_state=3), param_g
         grid_logit_split2.fit(X_train3_scaled, y_train3)
         print(grid_logit_split2.best_params_)
         print(grid_logit_split2.best_score_)
{'C': 100.0}
0.714791891848
In [62]: #Tune Linear SVM with with different random split
         grid_svm_split2 = GridSearchCV(LinearSVC(tol=0.0001,dual=False,random_state=3), param_g
         grid_svm_split2.fit(X_train3_scaled, y_train3)
         print(grid_svm_split2.best_params_)
         print(grid_svm_split2.best_score_)
{'C': 2.5118864315095824}
0.712142942554
```

The parameters after GridSearch do not change after changing from StratifiedKFold to KFold with shuffling. However the parameters do change when we change the random state of the shuffling, from (100,2.5) for Logistic Regression and Linear SVM to (15.8,15.8). When changing the random state of the split into training and test data, the parameters also do not change compared to original set of parameters. In the 3 cases, parameters of Nearest Centroid do not change.

# 0.0.5 Task 2.5: Visualize the coefficients for LogisticRegression and Linear Support Vector Machines

```
In [42]: #Logistic regression model
         logitmodel = LogisticRegression(tol=0.0001,C=grid_logit.best_params_['C'],random_state=
         logitmodel.fit(X_train_scaled,y_train)
         #Linear SVM model
         linearSVMmodel = LinearSVC(tol=0.0001, dual=False, C=grid_svm.best_params_['C'], random
         linearSVMmodel.fit(X_train_scaled, y_train)
Out[42]: LinearSVC(C=2.5118864315095824, class_weight=None, dual=False,
              fit_intercept=True, intercept_scaling=1, loss='squared_hinge',
              max_iter=1000, multi_class='ovr', penalty='12', random_state=20,
              tol=0.0001, verbose=0)
In [43]: fig = plt.figure(figsize=(15,15))
         for i in range(1,8):
             ax = fig.add_subplot(4,2,i)
             ax.scatter(range(X_train.shape[1]), logitmodel.coef_[i-1], label='Logistic Regressic
             ax.scatter(range(X_train.shape[1]), linearSVMmodel.coef_[i-1],label='Linear SVM')
             ax.set(title='Cover Type '+str(i))
             plt.legend()
```

