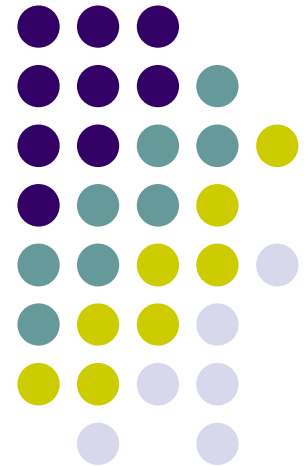


Practical Parallel Computing (実践的並列コンピューティング)

2025 Class No.6
[OpenMP Part] (4)
Bottleneck, Race Condition etc.

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Overview of This Course

- Introduction Part
 - 2 classes
- OpenMP (OMP) Part
 - 4 classes ← We are here (4/4)
 - Report (required)
- OpenACC (ACC) Part
 - 2 classes
 - Report (required)
- CUDA Part
 - 3 classes
 - Report (elective)
- MPI Part
 - 3 classes
 - Report (elective)



Today's Topic

- Bottleneck, mutual exclusion, reduction in OpenMP

samples:

- base/lumm, omp/lumm (Optional)
- base/pi, omp/pi-bad, omp/pi-slow-omp, omp/pi-fast, omp/pi

“lumm” sample: LU Matrix Multiply

ppcomp-ex/base/lumm/

A: a (n×n) matrix
B: a (n×n) matrix
C: a (n×n) matrix

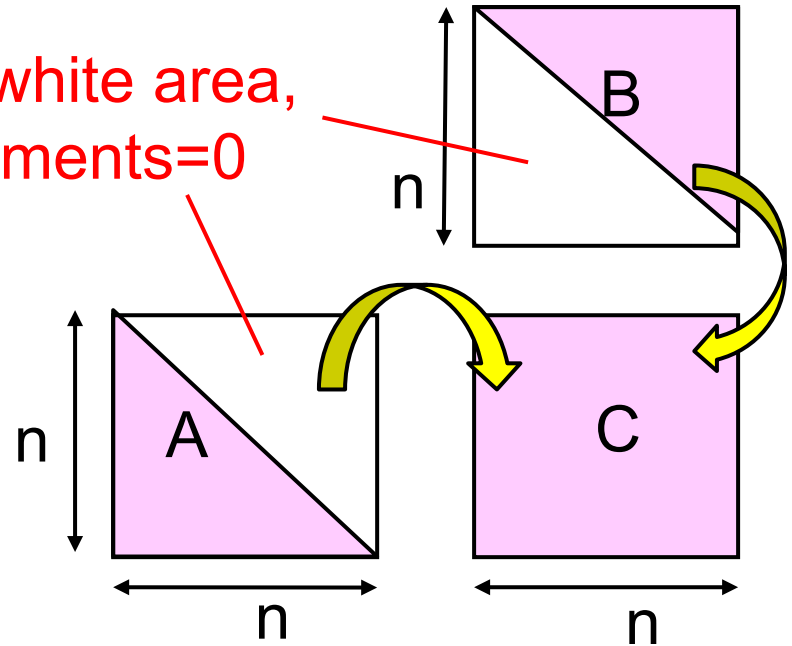
Square matrices

$C \leftarrow A \ B$

- Execution: `./lumm [n]`

`lumm` is similar to `mm` sample, but

- A is a Lower triangular matrix
- B is an Upper triangular matrix



Difference between “mm” and “lumm”

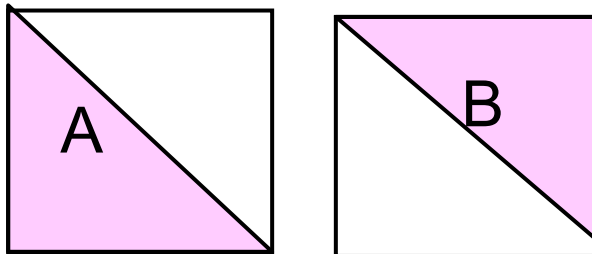


- (usual) Matrix multiply

```
for (j = 0; j < n; j++) {  
  for (l = 0; l < k; l++) {  
    for (i = 0; i < m; i++) {  
       $C_{i,j} += A_{i,l} * B_{l,j};$   
    } } }
```

⇒ $2n^3$ computation

If we know $A_{i,l} = 0$ or $B_{l,j} = 0$, we can skip computation





Computation in “lumm”

- **LU** Matrix multiply

```
for (j = 0; j < n; j++) {  
  for (l = 0; l <= j; l++) {  
    for (i = l; i < n; i++) {  
      Ci,j += Ai,l * Bl,j;  
    } } }  
}
```

⇒ $(2/3)n^3$ computation

Comparing time between
“mm 2000 2000 2000” and “lumm 2000”

	1thread
mm	1.77 (sec)
lumm	0.539 (sec)
mm / lumm	3.28

→ Shorter time in lumm 😊
(around 1/3)



“lumm-omp”: OpenMP version

[ppcomp-ex/omp/lumm/](https://github.com/ppcomp-ex/omp/lumm/)

```
#pragma omp parallel private(l,l)
#pragma omp for
for (j = 0; j < n; j++) {
    for (l = 0; l <= j; l++) {
        for (i = l; i < m; i++) {
            Ci,j += Ai,l * Bi,j;
        } } }
```

memo:
github's version is already
fast. please edit

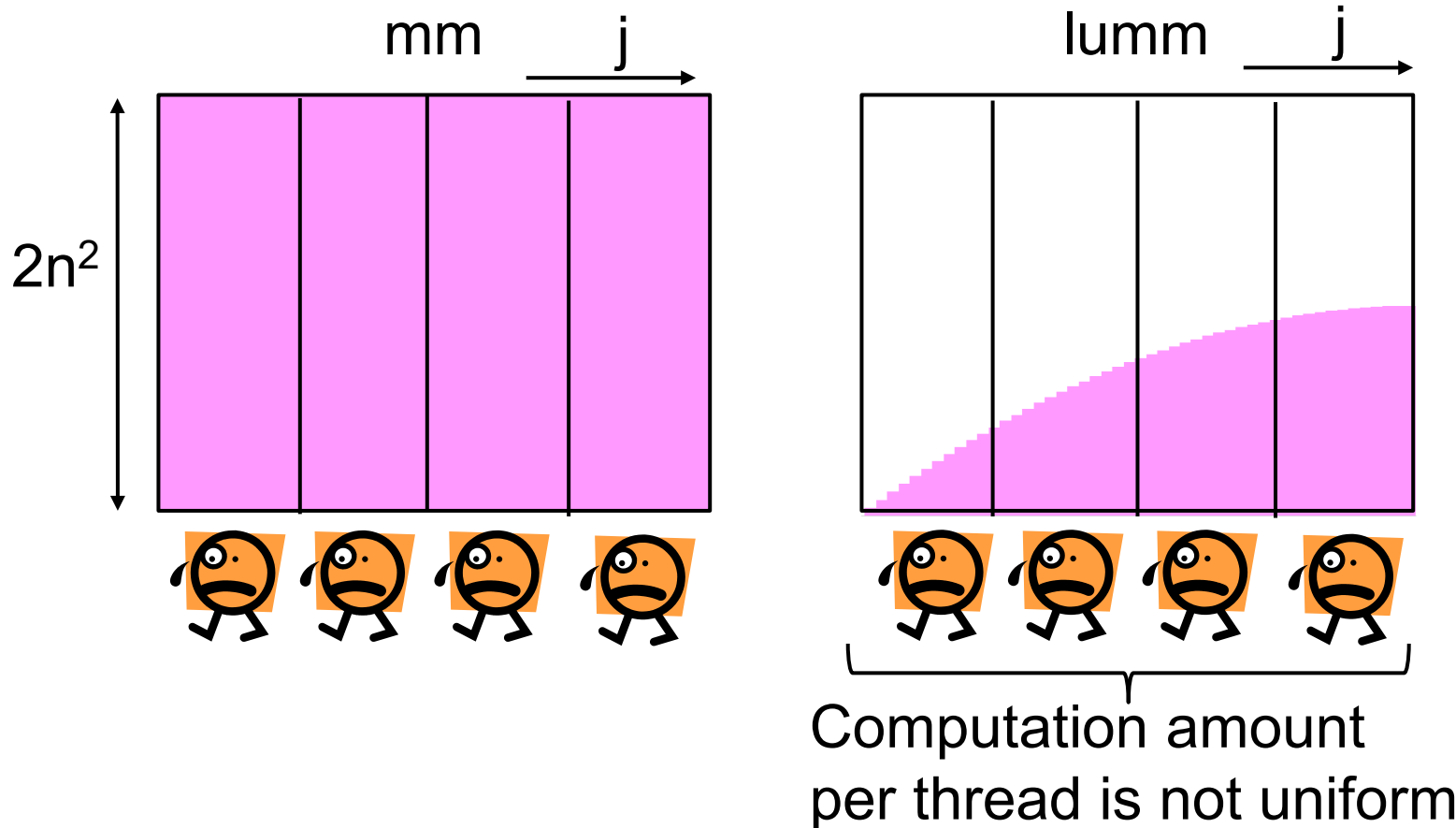
	1thread	4threads	8threads
mm-omp	1.77 (sec)	0.470	0.237
lumm-omp	0.539 (sec)	0.210	0.105
mm-omp / lumm-omp	3.28	2.24	2.26

lumm-omp is faster, but the ratio gets worse. Why?



Effects of Load Imbalance

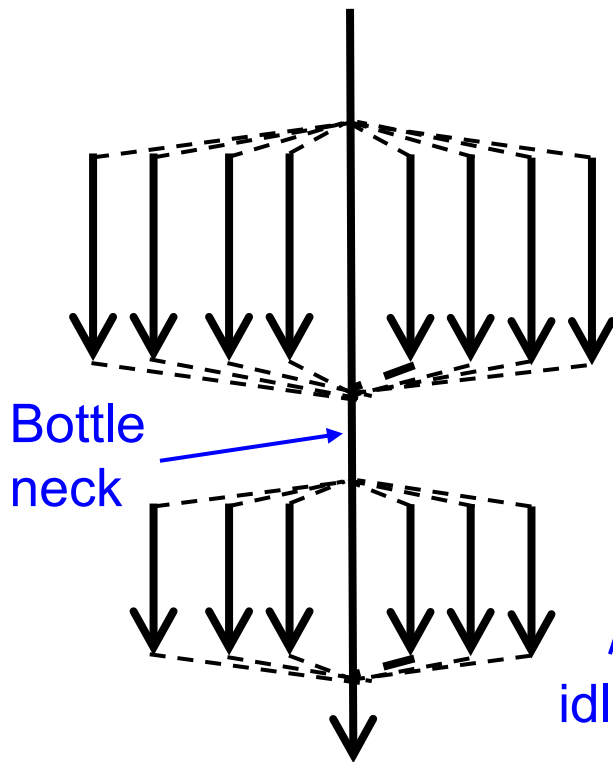
- In lumm, computation amount for each j is not uniform



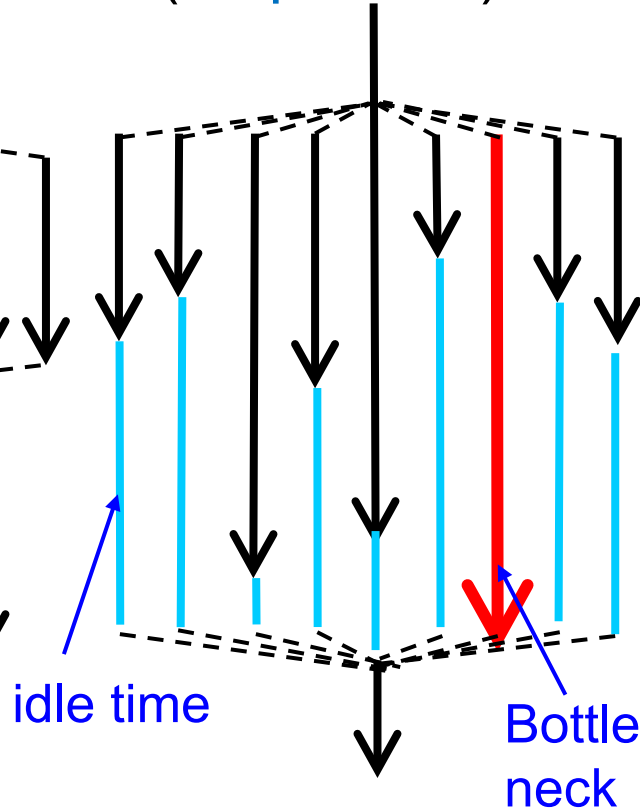


Various Bottlenecks

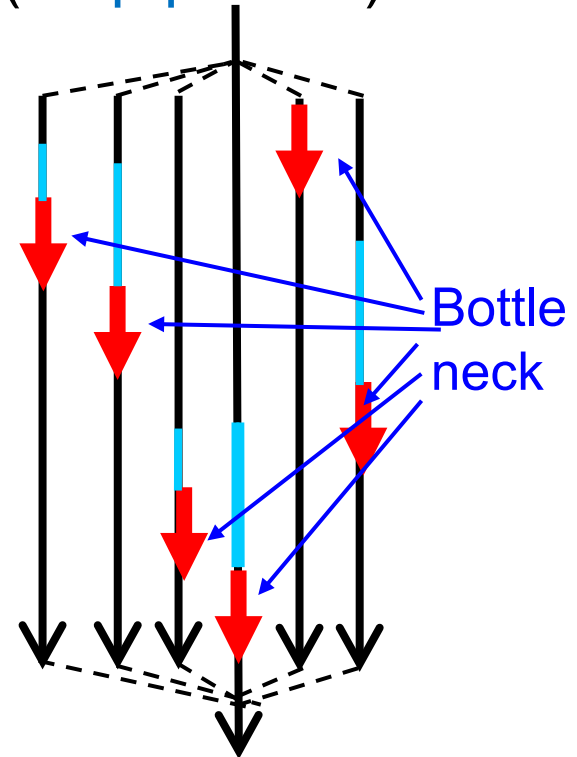
Bottleneck by sequential part



Bottleneck by load imbalance
(`omp/lumm`)



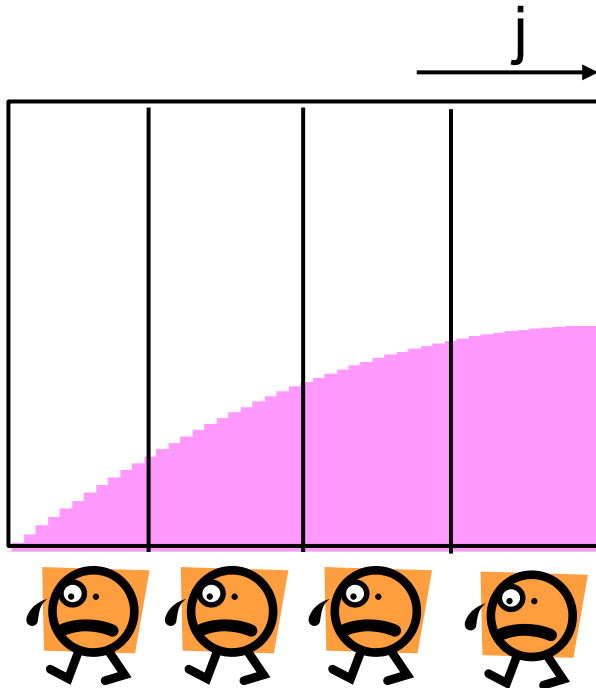
Bottleneck by critical sections
(`omp/pi-slow`)



Moreover, There are architectural bottlenecks



Improvement of lumm-omp



- Imbalance is caused by the default rule of “omp for”
 - “block distribution”
- Rule of “omp for” can be changed by **schedule** option

#pragma omp for **schedule (...)**

Changing “schedule” of omp for

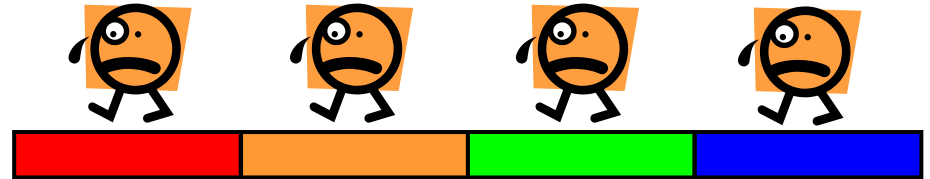


- OpenMP provides several scheduling methods (mapping between iteration and threads)

#pragma omp for `schedule(...)`

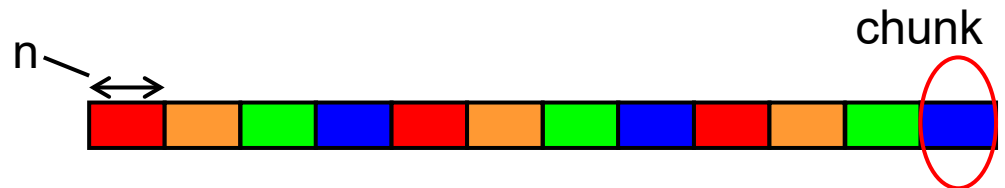
`schedule(static)`

Uniform block distribution (default)



`schedule(static, n)`

Cyclic distribution
n is “chunk” size



`schedule(dynamic, n)`

An Idle thread take a new chunk



`schedule(guided, n)`

Similar to dynamic, but
“chunk size” gets gradually smaller



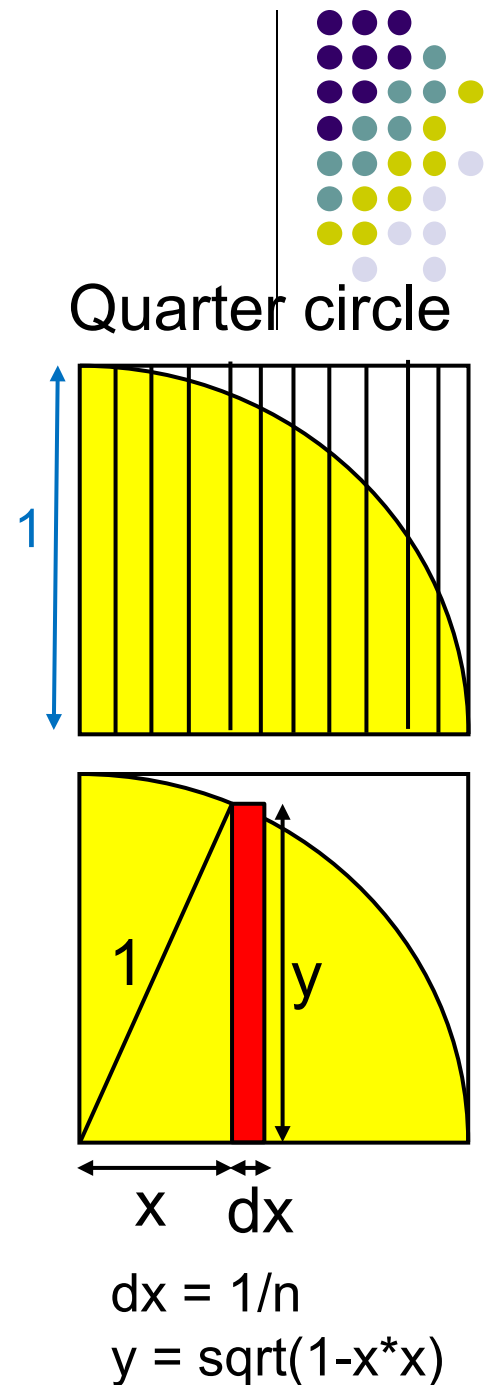
[Q] In lumm-omp, `#pragma omp for schedule(static,1)` works better than `#pragma omp for`. Why?

“pi” sample

Compute an approximation of $\pi = 3.14159\dots$
(circumference/diameter)

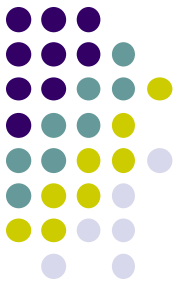
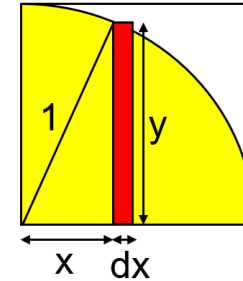
- [ppcomp-ex/base/pi/](#)
- Method
 - $SUM \leftarrow$ Approximation of the yellow area
 - $\pi \leftarrow 4 \times SUM$
- Execution: `./pi [n]`
 - n: Number of division
 - Cf) `./pi 100000000`
- Compute complexity: $O(n)$

*Note: This program is only for a simple sample.
 π is usually computed by different algorithms.*



Algorithm of “pi”

```
double pi(int n) {  
    int i;  
    double sum = 0.0;  
    double dx = 1.0 / (double)n;  
  
    for (i = 0; i < n; i++) {  
        double x = (double)i * dx;  
        double y = sqrt(1.0 - x*x);  
        sum += dx*y;  
    }  
  
    return 4.0*sum; }
```





Simple Parallelization of “pi” ??

```
double pi(int n) {  
    int i;  
    double sum = 0.0;  
    double dx = 1.0 / (double)n;
```

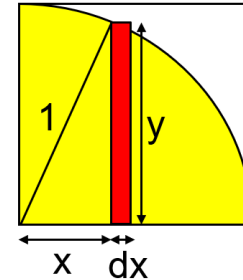
```
#pragma omp parallel
```

```
#pragma omp for
```

→ ok???

```
    for (i = 0; i < n; i++) {  
        double x = (double)i * dx;  
        double y = sqrt(1.0 - x*x);  
        sum += dx*y;  
    }
```

```
    return 4.0*sum; }
```



- This version has a bug!



Several Versions of pi Sample

- `base/pi` : sequential version

Followings use OpenMP

- `omp/pi-bad` :
 - “`#pragma omp parallel for`” is simply used
→ This has **a bug** that produces incorrect results
- `omp/pi-slow` : results are correct, but slow
- `omp/pi-fast` : results are correct and faster
- `omp/pi` : similar to `pi-fast-omp` but uses “reduce” option

do “make” and execute by “`./pi 1000000000`”

Caution: since `pi-slow` is very slow, please try
`./pi 1000000` (smaller N)



Execution Sample

base/pi

approximation of π

```
./pi 100000000  
Result=3.141592673589216: Pi took 0.378869 sec --> 0.264 Gsamples/sec  
Result=3.141592673589216: Pi took 0.378757 sec --> 0.264 Gsamples/sec  
Result=3.141592673589216: Pi took 0.378708 sec --> 0.264 Gsamples/sec  
Result=3.141592673589216: Pi took 0.378767 sec --> 0.264 Gsamples/sec  
Result=3.141592673589216: Pi took 0.379036 sec --> 0.264 Gsamples/sec
```

omp/pi-bad

```
export OMP_NUM_THREADS=8  
./pi 100000000  
Result=0.561908397695098: Pi took 0.736543 sec --> 0.136 Gsamples/sec  
Result=0.549626144994676: Pi took 0.762682 sec --> 0.131 Gsamples/sec  
Result=0.561650379038136: Pi took 0.731312 sec --> 0.137 Gsamples/sec  
Result=0.526911533756178: Pi took 0.612839 sec --> 0.163 Gsamples/sec  
Result=0.414727757933077: Pi took 0.489859 sec --> 0.204 Gsamples/sec
```

Results are far from π !
Also they change largely

slower than base/pi



Can We Parallelize the loop in pi?

- Let us consider computations with different i

C1 ($i=i_1$)

```
x = (double)i * dx;  
y = sqrt(1.0 - x*x);  
sum += dx*y;
```

these parts
are **independent**

dependent

C2 ($i=i_2$)

```
x = (double)i * dx;  
y = sqrt(1.0 - x*x);  
sum += dx*y;
```

$R(C1) = \{\text{sum}, dx\}$, $W(C1) = \{\text{sum}\}$

$R(C2) = \{\text{sum}, dx\}$, $W(C2) = \{\text{sum}\}$

⌘ Here, private variables x , y and loop counter i are safely omitted

- $W(C1) \cap W(C2) \neq \emptyset \rightarrow$ C1 and C2 are **Dependent!**

\rightarrow Do we have to abandon parallel execution?



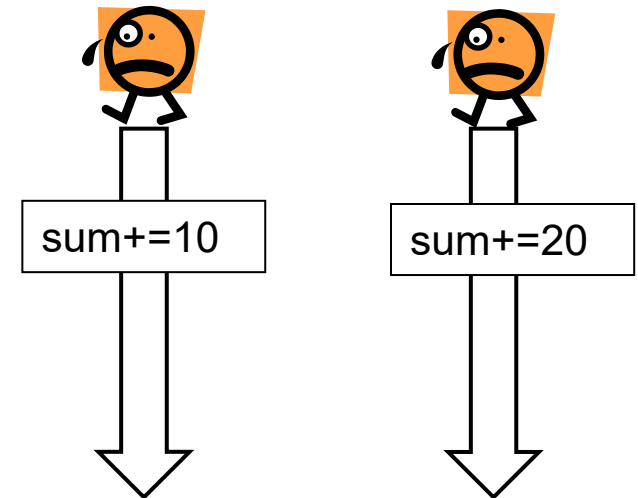


Race Condition Problem (1)

- To discuss the problem in omp/pi-bad, we consider a simpler program

`export OMP_NUM_THREADS=2`

```
int sum = 0;  
#pragma omp parallel // 2 threads  
{  
    if (omp_get_thread_num() == 0)  
        sum += 10; // C0 (by thread 0)  
    else  
        sum += 20; // C1 (by thread 1)  
}
```



After this program, we expect “sum == 30”. It it ok??

Race Condition Problem (2)

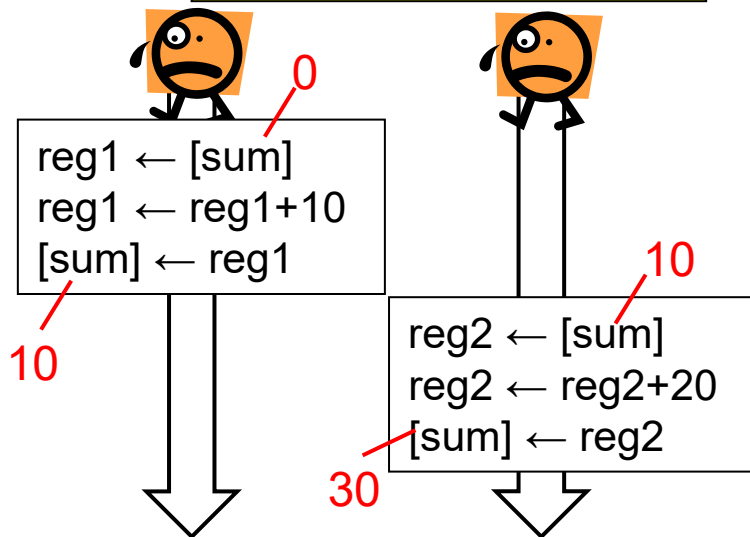


- [Q] Does execution order of C0 and C1 affect the results?
 - Note: “**sum += 10**” is compiled into machine codes like

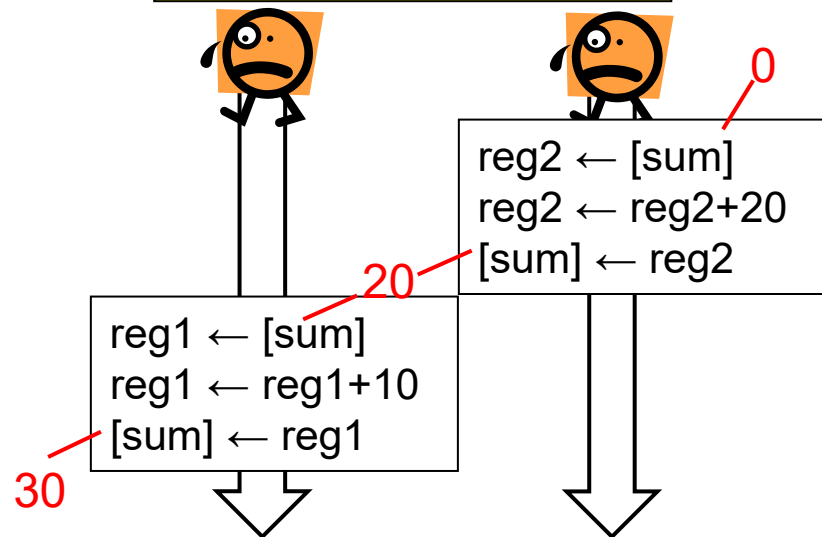
```
reg1 ← [sum]
reg1 ← reg1+10
[sum] ← reg1
```

※ reg1, reg2... are CPU registers, which are thread private

Case A: C0 then C1



Case B: C1 then C0

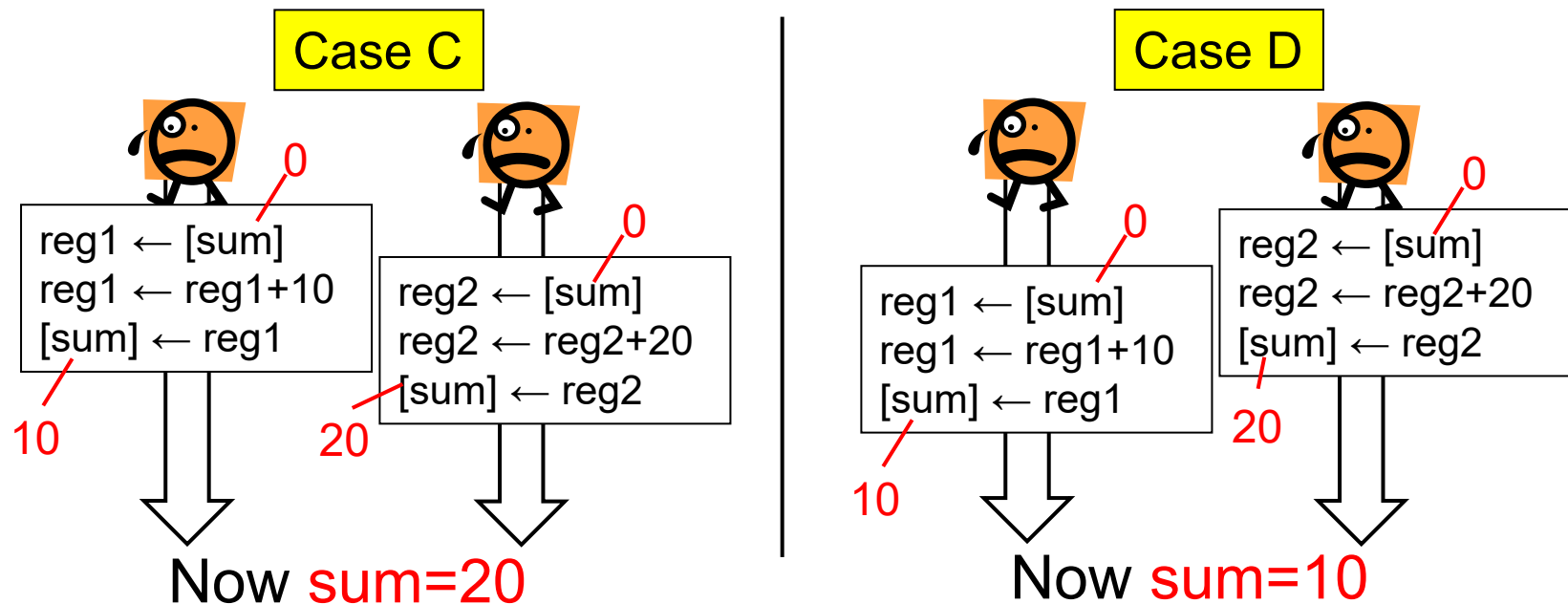


The results are same: sum=30. Ok to parallelize???



Race Condition Problem (3)

- **No!!!** The results can be **different** if C0 & C1 are executed (almost) simultaneously

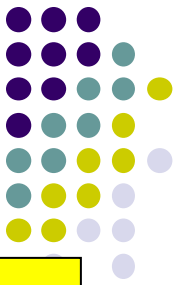


The expected result is 30, but we may get bad results

Such a bad situation is called “**Race Condition**”

→ This problem occurs in “**pi-bad-omp**”

Mutual Exclusion to Avoid Race Condition



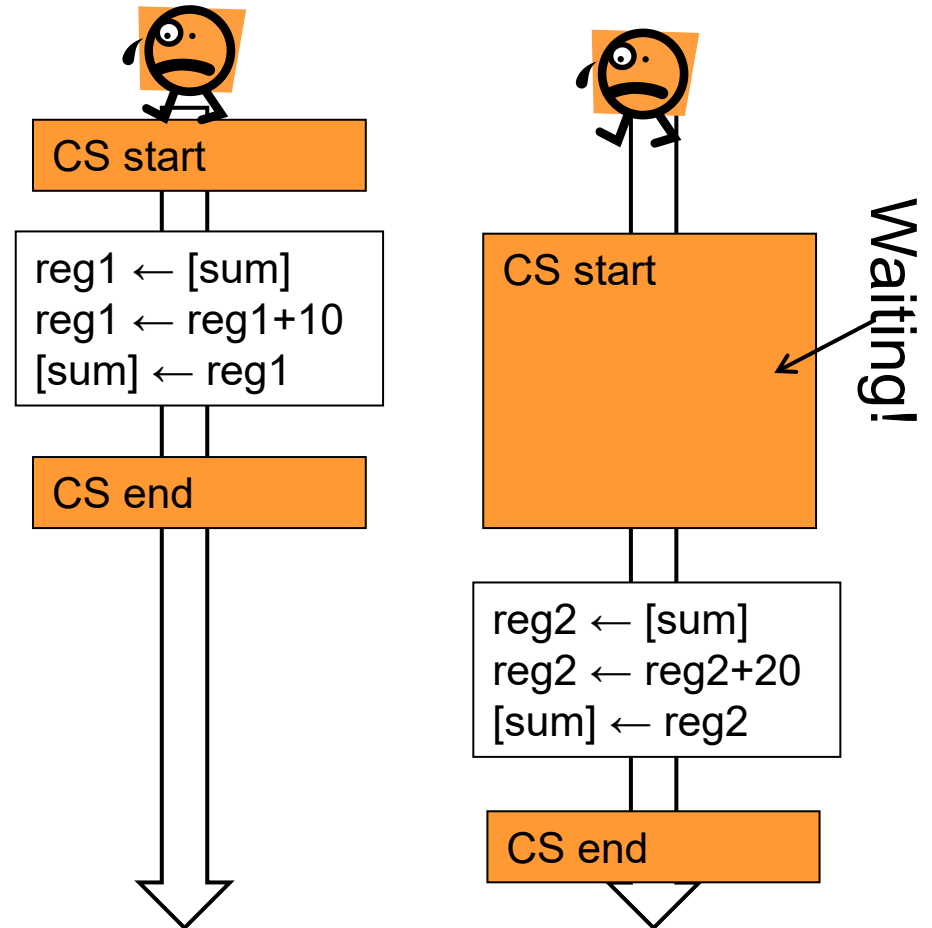
Mutual exclusion (mutex):

Mechanism to control threads so that only a single thread can enter a “specific region”

- The region is called **critical section**

⇒ With mutual exclusion, race condition is avoided

Case C with Mutual Exclusion



sum=30



Mutual Exclusion in OpenMP

#pragma omp critical makes
the following block/sentence
be **critical section**

```
double sum = 0;
#pragma omp parallel
{
    [ do something ]
    #pragma omp critical
    sum += myans;
}
```

Caution

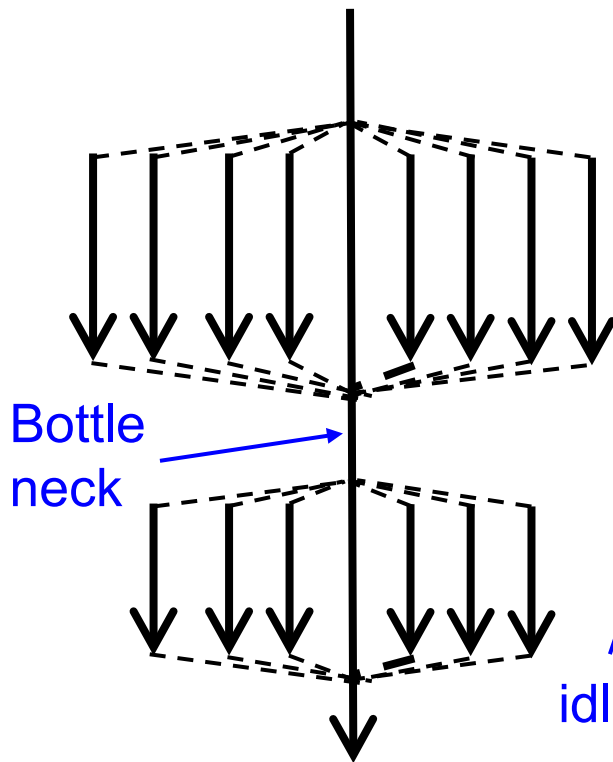
“omp/pi-slow” is very slow!

./pi 100000000 (10^8) takes too long,
so please use smaller N

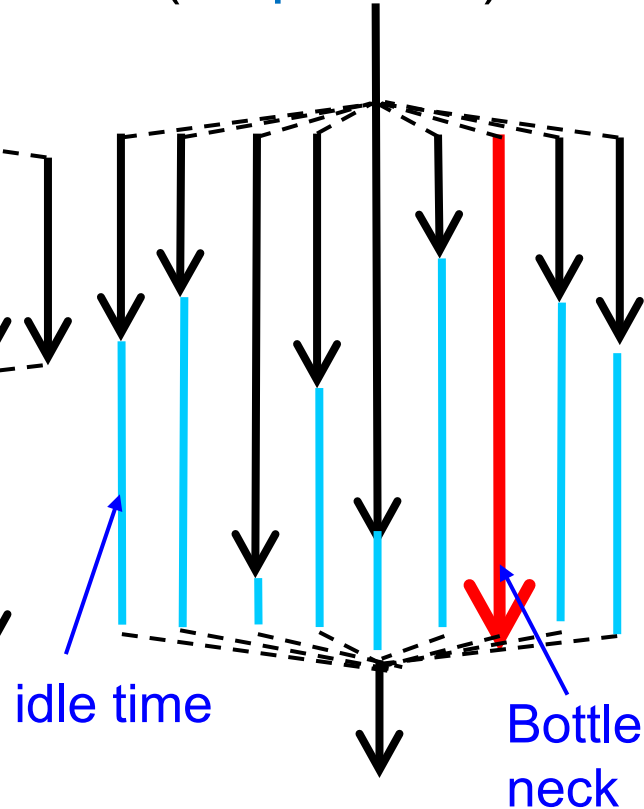
cf) ./pi 1000000
(10^6)

We are Seeing Bottlenecks

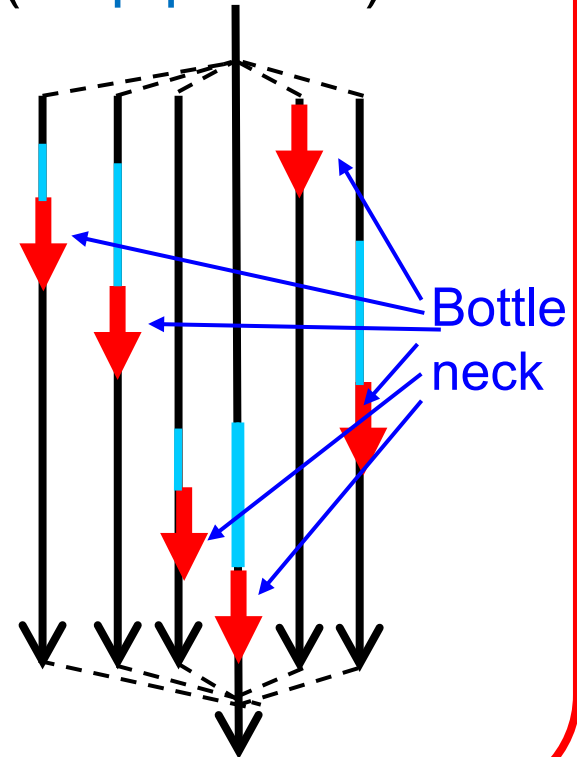
Bottleneck by sequential part



Bottleneck by load imbalance
(`omp/lumm`)



Bottleneck by critical sections
(`omp/pi-slow`)



Amdahl's Law: Modeling Bottlenecks

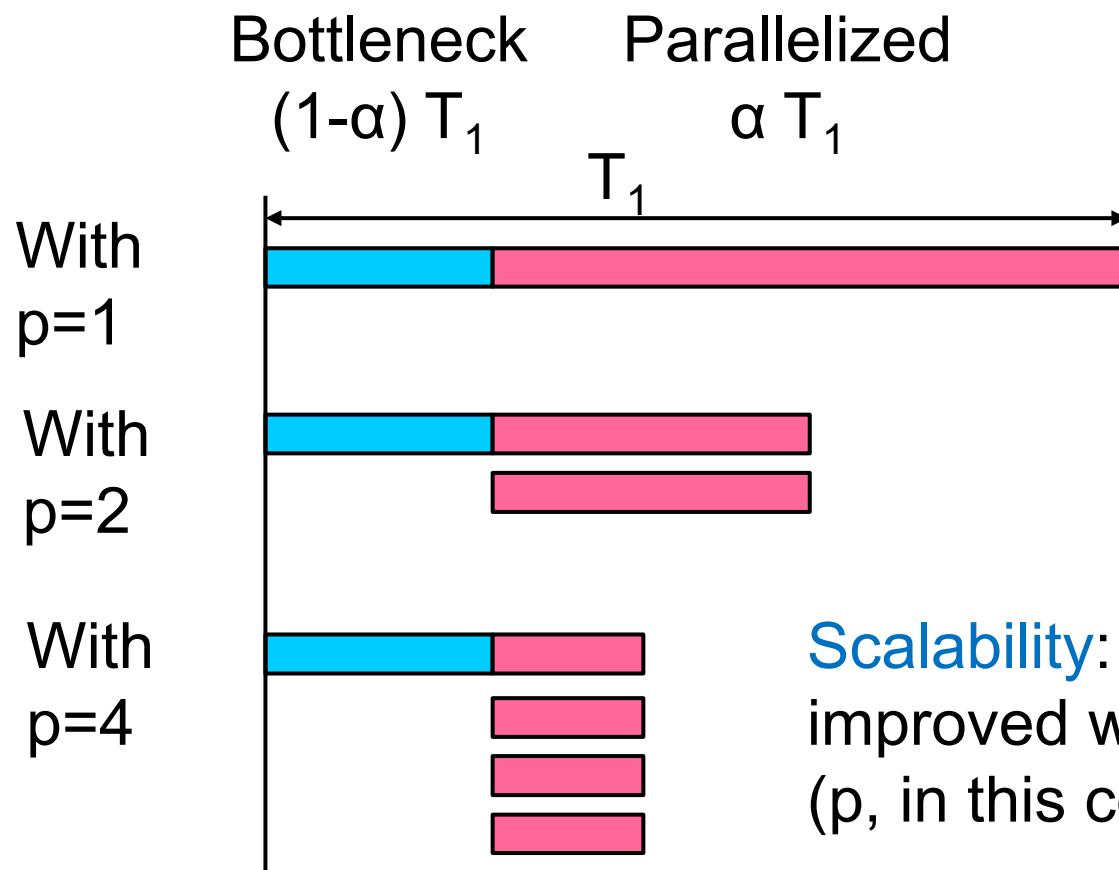


- We consider an algorithm. Then we let
 - T_1 : execution time with 1 processor core
 - α : ratio of computation that can be parallelized
 - $1-\alpha$: ratio that CANNOT be parallelized (bottleneck)
- ⇒ Estimated execution time with p processor cores is $T_p = ((1 - \alpha) + \alpha / p) T_1$

Due to bottleneck, there is limitation in speed-up no matter how many cores are used

$$T_{\infty} = (1-\alpha) T_1$$

An Illustration of Amdahl's Law



Scalability: How performance is improved with larger resources (p , in this context)

Amdahl's law tells us

- if $\alpha=0.9$, we only achieve up to 10x speed up with ∞ cores
- if $\alpha=0.99$, we only achieve up to 100x speed up with ∞ cores



The Fact is Harder Than Theory


- According to Amdahl's law, T_p is monotonically decreasing
→ Is large p always harmless ??

Performance comparison of pi-omp and pi-slow-omp

```
export OMP_NUM_THREADS= [p]
```

```
./pi 1000000000 # 10^9
```

p	omp/pi-fast omp/pi	omop/pi-slow
1	2.44 (sec)	5.59 (sec)
4	0.61	~60
8	0.305	~150
16	0.153	250~400



Slower! 😞

Reducing bottleneck is even more important
(than Amdahl's law tells)

Reducing Bottlenecks

- Approaches for reducing bottlenecks depend on algorithms!
 - We need to consider, consider
 - Some algorithms are essentially difficult to be parallelized
- Some directions
 - Improving load balance
 - Reducing access to shared variables
 - Reducing length of dependency chains
 - called “critical path”
 - Reducing parallelization costs
 - entering/exiting “omp parallel”, “omp critical”... is not free



lumm sample

pi sample



Cases of “pi” Sample

- “[omp/pi-slow](#)” is slow, since each thread enters a critical section too frequently
- To improve this, another [omp/pi-fast](#) version introduces private variables

Step 1: Each thread accumulates values into **private** “local_sum”

Step 2: Then each thread does “sum += local_sum” in a critical section
once per thread

→ [omp/pi-fast](#) is fast 😊

→ [But program is more complex ☹️](#)

Please see [omp/pi-fast/pi.c](#)



omp/pi-fast Algorithm

```
double sum = 0.0; // share var

#pragma omp parallel
{
    double local_sum = 0.0; // private var
    #pragma omp for
    for (i = 0; i < n; i++) {
        double x = (double)i * dx;
        double y = sqrt(1.0 - x*x);
        local_sum += dx*y;
    }

    #pragma omp critical // critical section
    sum += local_sum;
}
```

- This uses critical section, but much less often than pi-slow!

Reduction Computations in “omp for”



- “*Summation in a for-loop*” is one of typical computations
→ called **reduction computations**
- In OpenMP, they can be integrated to “**omp for**”

```
double sum = 0.0;

#pragma omp parallel
#pragma omp for reduction (+:sum)
    for (i = 0; i < n; i++) {
        double x = (double)i * dx;
        double y = sqrt(1.0 - x*x);
        sum += dx*y;
    }
```

Operator is one of
+, -, *, &&, ||,
max, min, etc

Name of reduction
variable

→ omp/pi is fast, like omp/pi-fast 😊

→ Also, programming is easier 😊



Why is “omp for reduction” Fast?

Why is omp/pi with reduction also fast?

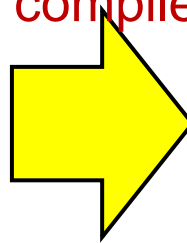
“omp for reduction(...)” is internally compiled to a similar code to pi-fast-omp

```
double sum = 0.0;

#pragma omp parallel

#pragma omp for reduction (+:sum)
for (i = 0; i < n; i++) {
    double x = (double)i * dx;
    double y = sqrt(1.0 - x*x);
    sum += dx*y;
}
```

automatically
compiled



```
double sum = 0.0;

#pragma omp parallel
{
    double local_sum = 0.0;
    #pragma omp for
    for (i = 0; i < n; i++) {
        double x = (double)i * dx;
        double y = sqrt(1.0 - x*x);
        local_sum += dx*y;
    }
    #pragma omp critical
    sum += local_sum;
}
```

Assignments in OpenMP Part (Abstract)



Choose one of [O1]—[O4], and submit a report

Due date: May 1 (Thu)

[O1] Parallelize “diffusion” sample program by OpenMP.

[O2] Parallelize “bsort” sample program by OpenMP.

[O3] Parallelize “qsort” sample program by OpenMP.

[O4] (Freestyle) Parallelize *any* program by OpenMP.

For more detail, please see [ppcomp25-3](#) slides



Next Part: OpenACC (ACC) Part

- Class #7
 - Introduction to GPU programming and OpenACC
 - Parallelization of loops
 - Assignment in OpenACC part
- Class #8
 - Discussion on diffusion sample wit OpenACC
 - Data transfer cost