



PROGRAMMING AND OPTIMIZATION FOR INTEL® ARCHITECTURE

One-Day Workshop

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WELCOME

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COMPUTING APPLICATIONS

Just some examples

Natural sciences
Drug development
Space weather
New particle discovery

Finance
Risk analysis
Fraud prevention
Real-time hedging

Internet
Natural speech interaction
Video streaming and archiving
Facial recognition

Aerospace
Rocket engine simulation
Radiation protection studies
Aircraft aerodynamics

Computing

Medicine
Medical imaging
Radiation treatment simulation
Human error detection

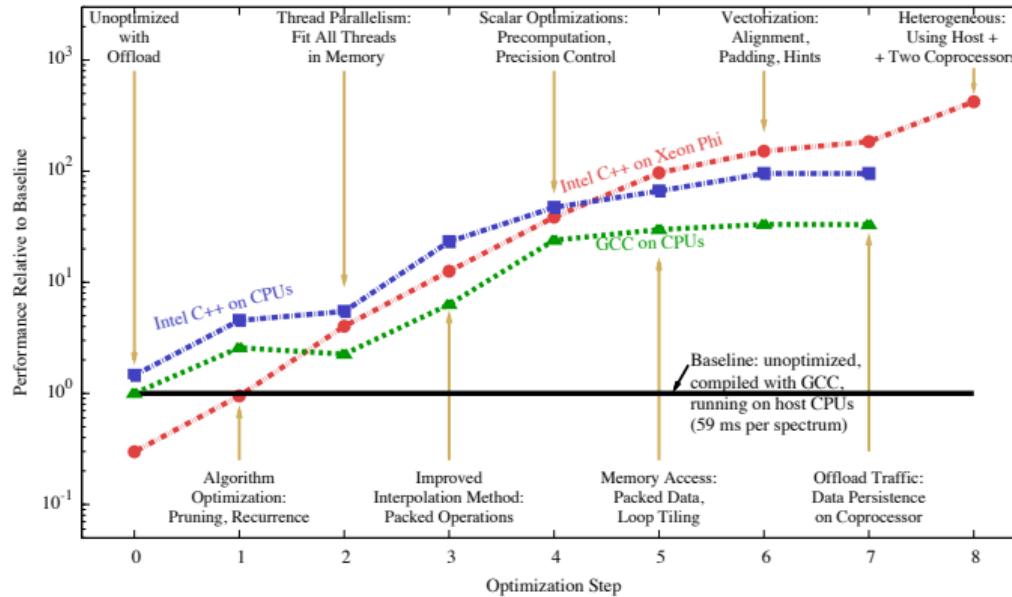
Manufacturing
Simulation of material processing
Development of new materials
Robotic operations

Environment
Weather prediction
Earthquake simulation
Pollutant propagation

Energy
Oil reservoir simulation
Climate change science
Nuclear fusion research

PROGRAMMING MODEL CONTINUITY

Common story for many applications:



(see <http://xeonphi.com/papers/heatcode>)

OPTIMIZATION AREAS

9

Scalar Tuning

what goes on in the pipeline?

Vectorization

is SIMD parallelism used well?

Threading

do cores cooperate efficiently?

Memory

is cache usage maximized or
RAM access streamlined?

Communication

can coordination in a distributed or
heterogeneous system be improved?

§2. PROGRAMMING, OPTIMIZATION BY EXAMPLE

DIRECT N-BODY SIMULATION

N-BODY SIMULATION ON CPU AND COPROCESSOR



N-body simulation on...

Two
Intel® Xeon®
CPUs



One
Intel® Xeon Phi™
coprocessor



Two
Intel® Xeon Phi™
coprocessors



Paper: <http://xeonphi.com/papers/nbody-basic>

Demo: [click here](#)

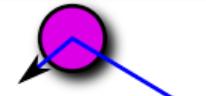
Gravitational N-body dynamics:

Newton's law of universal gravitation:

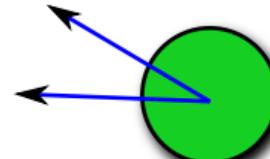
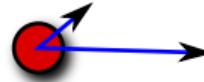
$$M_i \vec{R}_i''(t) = G \sum_j \frac{M_i M_j}{\left| \vec{R}_i - \vec{R}_j \right|^3} \left(\vec{R}_j - \vec{R}_i \right)$$

where:

$$\left| \vec{R}_i - \vec{R}_j \right| = \sqrt{(R_{i,x} - R_{j,x})^2 + (R_{i,y} - R_{j,y})^2 + (R_{i,z} - R_{j,z})^2}$$



particles are attracted to each other
with the gravitational force



1. Astrophysics:

- planetary systems
- galaxies
- cosmological structures

2. Electrostatic systems:

- molecules
- crystals

This work: “toy model” with all-to-all $O(n^2)$ algorithm. Practical N-body simulations may use tree algorithms with $O(n \log n)$ complexity.



Source: [APOD](#), credit: Debra Meloy Elmegreen (Vassar College) et al., & the Hubble Heritage Team (AURA/ STScI/ NASA)

ALL-TO-ALL APPROACH ($O(n^2)$ COMPLEXITY SCALING)

Each particle is stored as a structure:

```
1 struct ParticleType {  
2     float x, y, z;  
3     float vx, vy, vz;  
4 };
```

main() allocates an array of ParticleType:

```
1 ParticleType* particle = new ParticleType[nParticles];
```

Particle propagation step is timed:

```
1 const double tStart = omp_get_wtime(); // Start timing  
2 MoveParticles(nParticles, particle, dt);  
3 const double tEnd = omp_get_wtime(); // End timing
```

PARTICLE UPDATE ENGINE

```
1 void MoveParticles(int nParticles, ParticleType* particle, float dt) {
2     for (int i = 0; i < nParticles; i++) { // Particles that experience force
3         float Fx = 0, Fy = 0, Fz = 0; // Gravity force on particle i
4         for (int j = 0; j < nParticles; j++) { // Particles that exert force
5             // Newton's law of universal gravity
6             const float dx = particle[j].x - particle[i].x;
7             const float dy = particle[j].y - particle[i].y;
8             const float dz = particle[j].z - particle[i].z;
9             const float drSquared = dx*dx + dy*dy + dz*dz + 1e-20;
10            const float drPower32 = pow(drSquared, 3.0/2.0);
11            // Calculate the net force
12            Fx += dx/drPower32;  Fy += dy/drPower32;  Fz += dz/drPower32;
13        }
14        // Accelerate particles in response to the gravitational force
15        particle[i].vx+=dt*Fx; particle[i].vy+=dt*Fy;  particle[i].vz+=dt*Fz;
16    }
```

INTEL ARCHITECTURE

COMPUTING PLATFORMS

Intel Xeon
Processor



Current: Broadwell
Upcoming: Skylake

Intel Xeon Phi
Coprocessor, 1st generation



Knights Corner (KNC)

Intel Xeon Phi
Processor, 2nd generation*



* socket and coprocessor versions

Knights Landing (KNL)

Multi-Core Architecture

Intel Many Integrated Core (MIC) Architecture

BIRD'S EYE VIEW

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- C/C++/Fortran
- Linux/Windows
- ≤ 3 TiB DDR4
- ≤ 44 cores (2-way)
- ≈ 3 GHz
- 2 HT/core
- 256-bit AVX



- C/C++/Fortran
- Special Linux
- ≤ 16 GiB GDDR5
- 57-61 cores
- ≈ 1.2 GHz
- 4 HW THR/core
- 512-bit IMCI



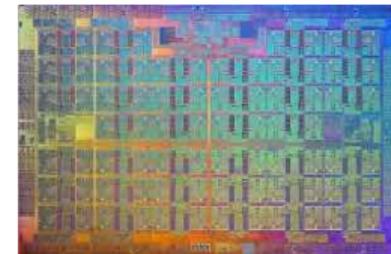
- C/C++/Fortran
- Linux
- MCDRAM+DDR4
- 64-72 cores
- 1.3-1.5 GHz
- 4 HT/core
- 512-bit AVX-512

CORES AND VECTORS

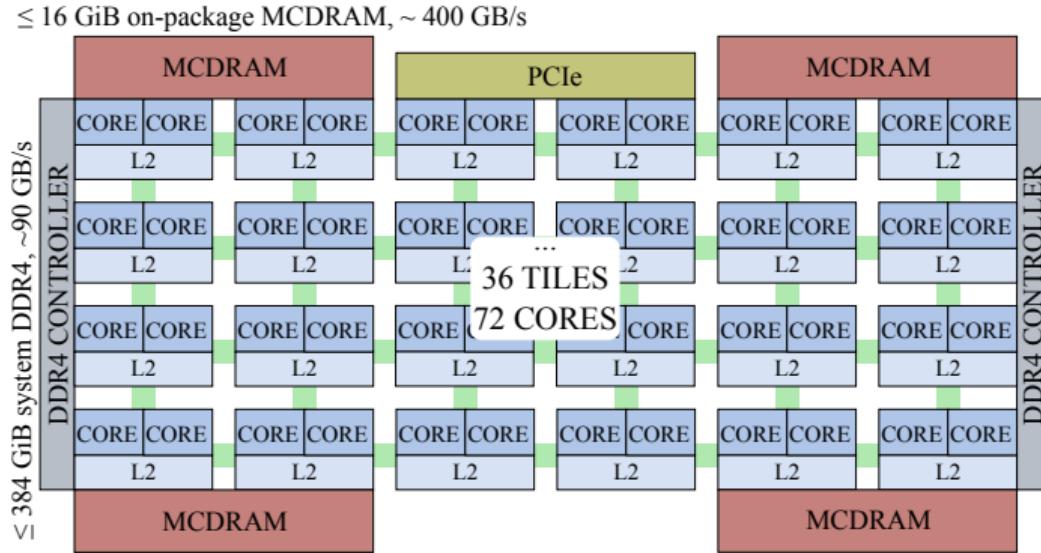
INTEL XEON PHI PROCESSORS (2ND GEN)

Specialized platform for demanding computing applications.

- ▷ Socket version or coprocessor
- ▷ 64-72 cores × 4 HT at 1.3-1.5 GHz
- ▷ 3+ TFLOP/s in DP (FMA)
- ▷ 6+ TFLOP/s in SP (FMA)
- ▷ ≤ 384 GiB DDR4 (> 90 GB/s)
- ▷ 16 GiB HBM (MCDRAM, > 400 GB/s)
- ▷ Binary-compatible with Xeon
- ▷ Common OS
(RHEL/CentOS/SUSE/Windows)

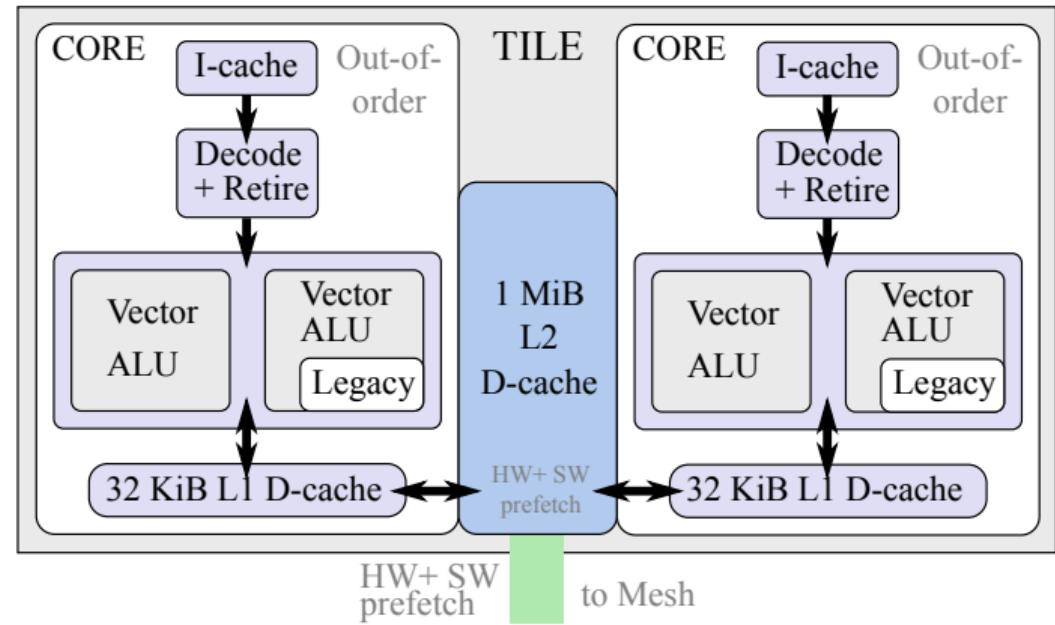


- ▶ Mesh interconnect relaxes data locality requirement [somewhat]
 - ▶ All-to-all, quadrant or sub-numa domain communication in mesh



KNL CORES

- ▶ Even more power in vector units
- ▶ Binary compatible with Xeon, but in legacy mode



INCORPORATING THREAD PARALLELISM

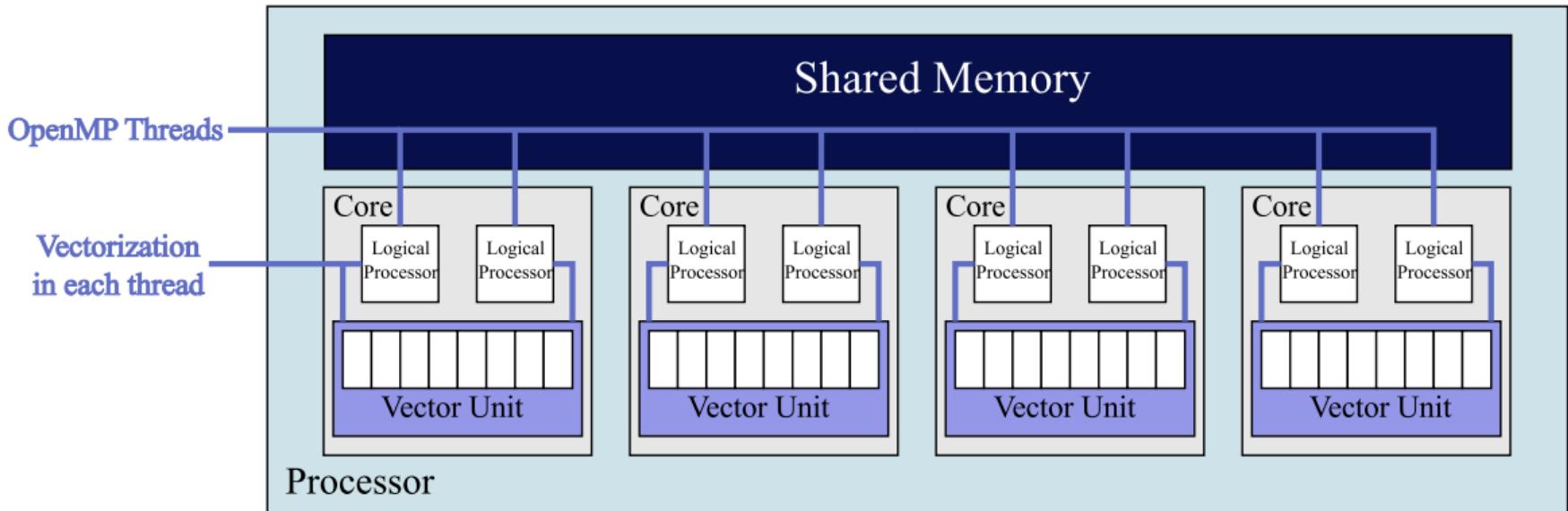
Before:

```
1  for (int i = 0; i < nParticles; i++) { // Particles that experience force
2      float Fx = 0, Fy = 0, Fz = 0; // Gravity force on particle i
3      for (int j = 0; j < nParticles; j++) { // Particles that exert force
4          // Newton's law of universal gravity
5          ...
6      }
```

After:

```
1 #pragma omp parallel for
2     for (int i = 0; i < nParticles; i++) { // Particles that experience force
3         float Fx = 0, Fy = 0, Fz = 0; // Gravity force on particle i
4         for (int j = 0; j < nParticles; j++) { // Particles that exert force
5             // Newton's law of universal gravity
6             ...
7         }
```

CO-EXISTENCE WITH VECTORS



Utilize cores: run multiple threads/processes (MIMD)

Utilize vectors: each thread (process) issues vector instructions (SIMD)

SIMULTANEOUS THREADING AND VECTORIZATION

This approach often works:

```
1 #pragma omp parallel for
2 for (int i = 0; i < n; i++) // Thread parallelism in outer loop
3 #pragma simd
4     for (int j = 0; j < m; j++) // Vectorization in inner loop
5         DoSomeWork(A[i][j]);
```

That works as well:

```
1 #pragma omp parallel for simd
2 for (int i = 0; i < n; i++) // If the problem is all data-parallel
3     DoSomeWork(A[i]);
```

SHORT VECTOR SUPPORT

Vector instructions – one of the implementations of SIMD (Single Instruction Multiple Data) parallelism.

Scalar Instructions

$$\begin{array}{r} 4 \\ + 1 \\ \hline 5 \end{array}$$
$$\begin{array}{r} 0 \\ + 3 \\ \hline 3 \end{array}$$
$$\begin{array}{r} -2 \\ + 8 \\ \hline 6 \end{array}$$
$$\begin{array}{r} 9 \\ + -7 \\ \hline 2 \end{array}$$

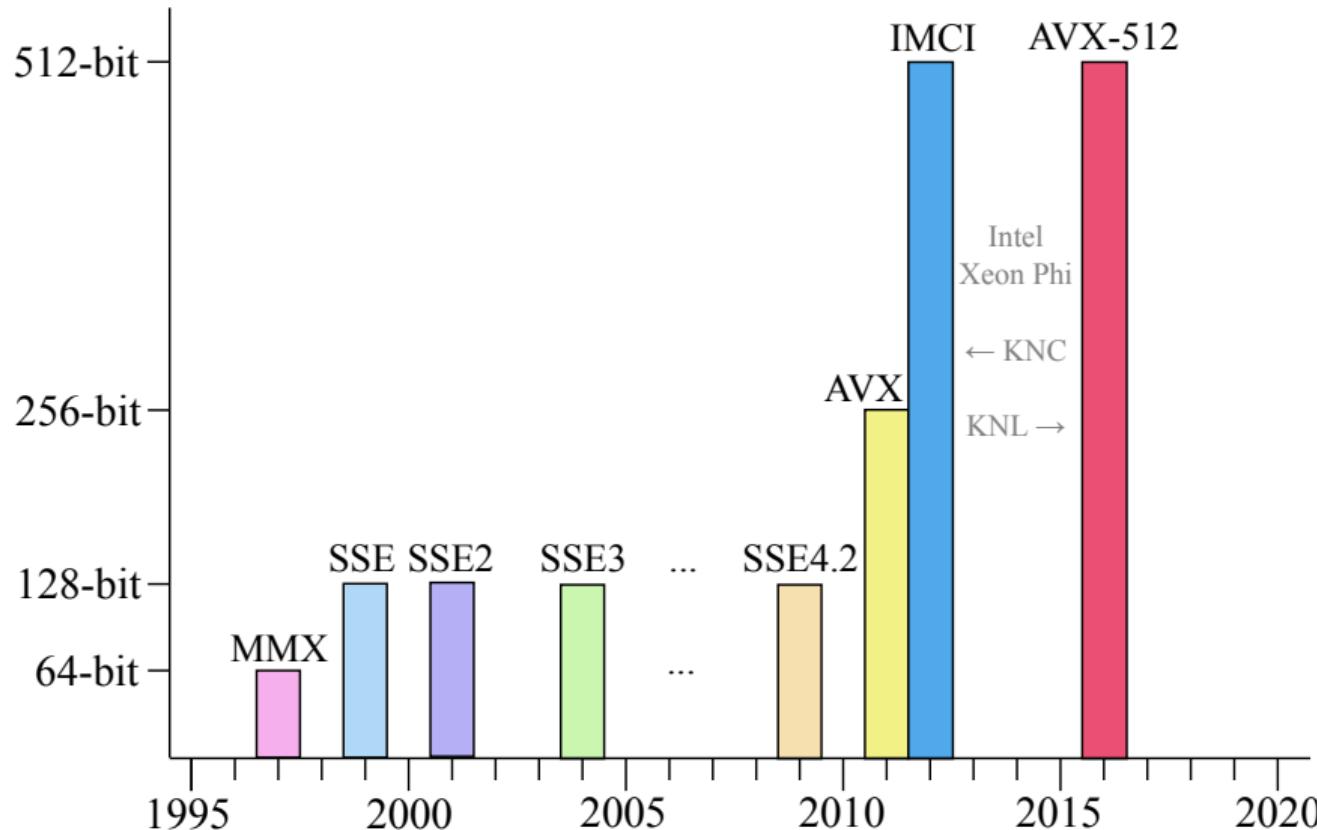
Vector Instructions

$$\begin{array}{c} 4 \\ 0 \\ -2 \\ 9 \end{array} + \begin{array}{c} 1 \\ 3 \\ 8 \\ -7 \end{array} = \begin{array}{c} 5 \\ 3 \\ 6 \\ 2 \end{array}$$

Vector Length



INSTRUCTION SETS IN INTEL ARCHITECTURE



VECTORIZING WITH UNIT-STRIDE MEMORY ACCESS

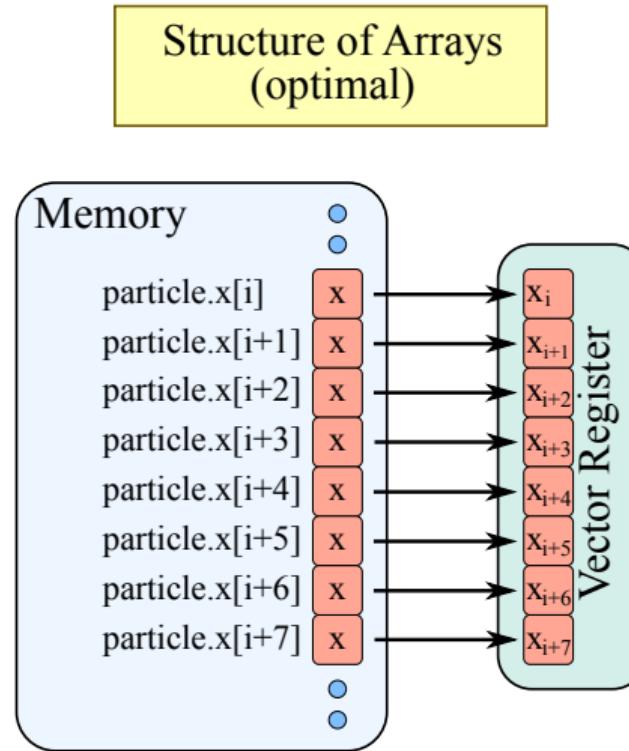
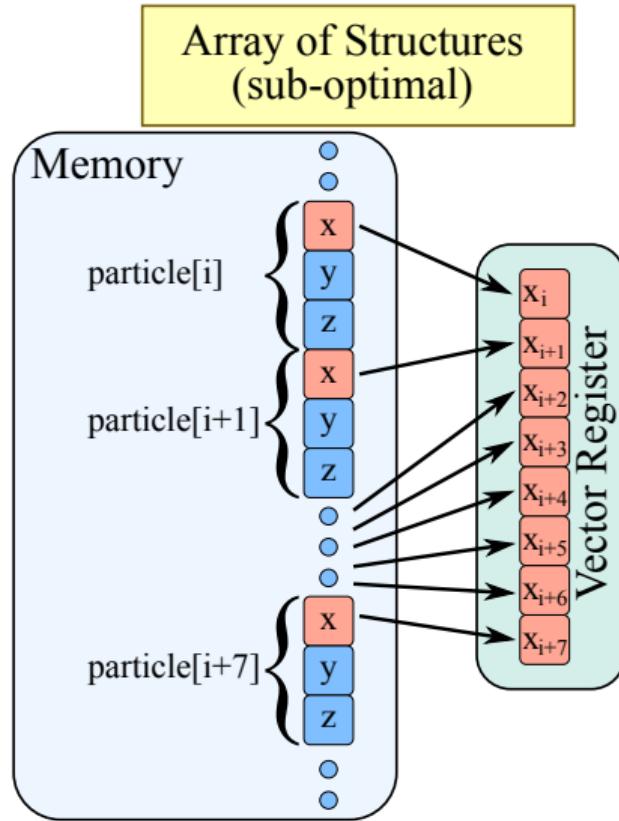
Before:

```
1 struct ParticleType {  
2     float x, y, z, vx, vy, vz;  
3 }; // ...  
4     const float dx = particle[j].x - particle[i].x;  
5     const float dy = particle[j].y - particle[i].y;  
6     const float dz = particle[j].z - particle[i].z;
```

After:

```
1 struct ParticleSet {  
2     float *x, *y, *z, *vx, *vy, *vz;  
3 }; // ...  
4     const float dx = particle.x[j] - particle.x[i];  
5     const float dy = particle.y[j] - particle.y[i];  
6     const float dz = particle.z[j] - particle.z[i];
```

WHY AOS TO SOA CONVERSION HELPS: UNIT STRIDE



IMPROVING SCALAR EXPRESSIONS

Before:

```
1 const float drSquared = dx*dx + dy*dy + dz*dz + 1e-20;
2 const float drPower32 = pow(drSquared, 3.0/2.0);
3 // Calculate the net force
4 Fx += dx/drPower32; Fy += dy/drPower32; Fz += dz/drPower32;
```

After:

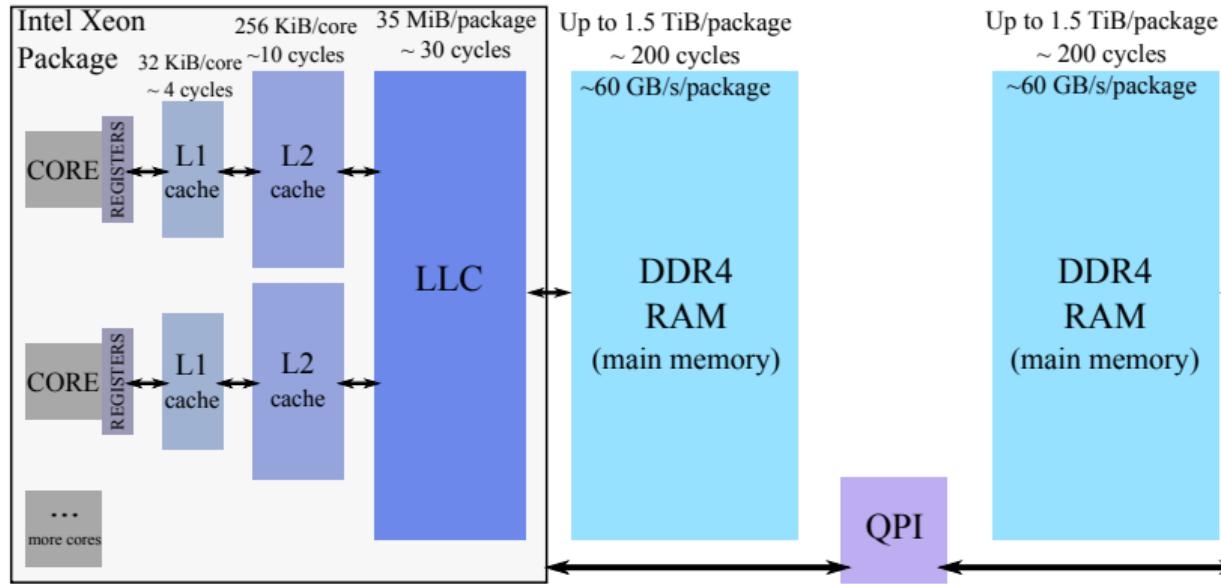
```
1 const float drRecip     = 1.0f/sqrdf(dx*dx + dy*dy + dz*dz + 1e-20);
2 const float drPowerN32 = drRecip*drRecip*drRecip;
3 // Calculate the net force
4 Fx += dx*drPowerN32; Fy += dy*drPowerN32; Fz += dz*drPowerN32;
```

- ▶ Strength reduction (division → multiplication by reciprocal)
- ▶ Precision control (suffix `-f` on single-precision constants and functions)
- ▶ Reliance on hardware-supported reciprocal square root

MEMORY ORGANIZATION

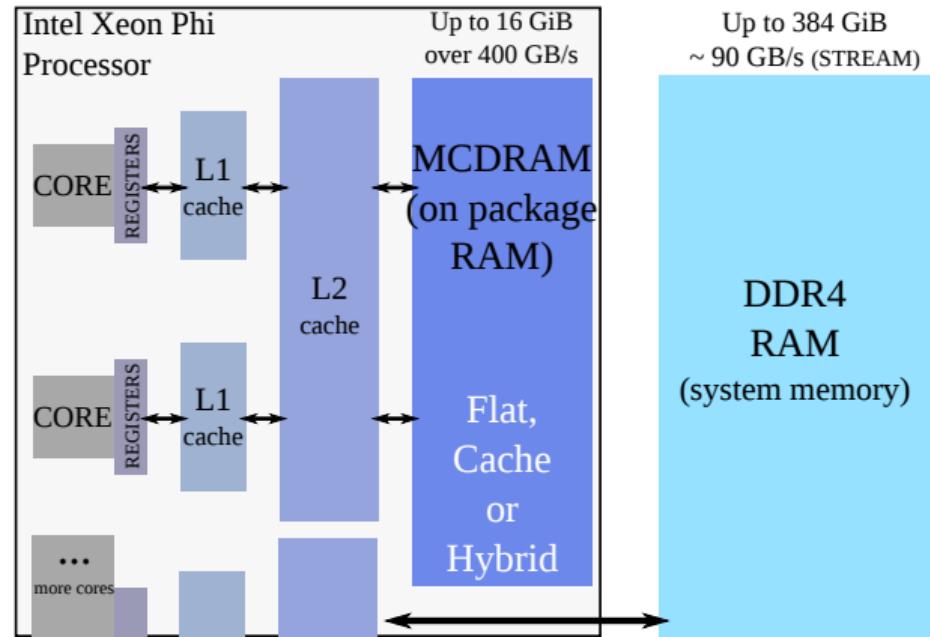
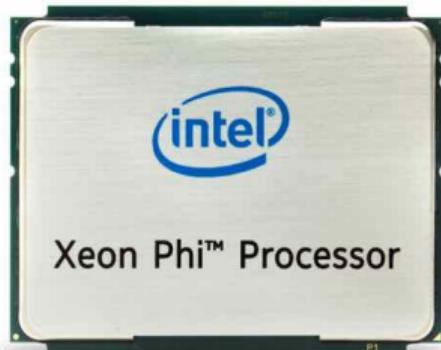
INTEL XEON CPU: MEMORY ORGANIZATION

- ▷ Hierarchical cache structure
- ▷ Two-way processors have NUMA architecture



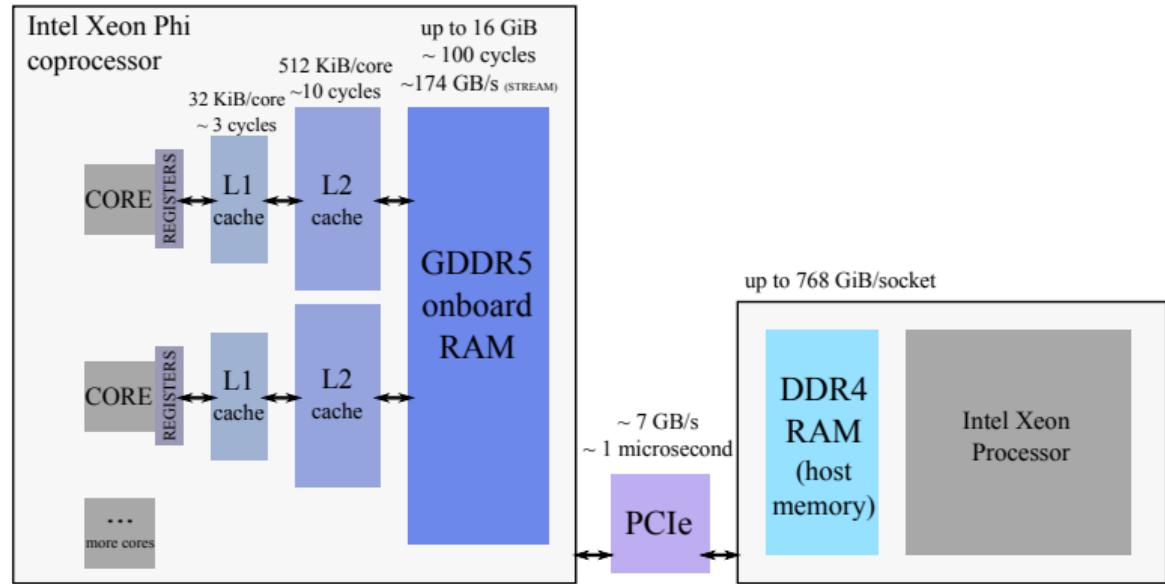
KNL MEMORY ORGANIZATION (BOOTABLE)

- ▶ Direct access to on-platform RAM and on-package HBM
- ▶ Use HBM as cache, in flat mode, or as hybrid



KNC MEMORY ORGANIZATION

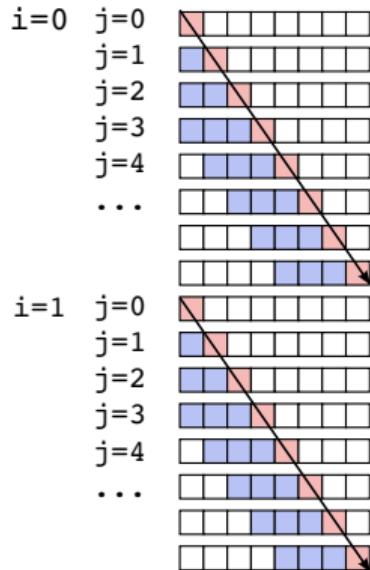
- ▶ Direct access to ≤ 16 GiB of cached GDDR5 memory on board
- ▶ No access to system DDR4, connected to host via PCIe



LOOP TILING

Original:

```
for (i=0; i<m; i++)
    for (j=0; j<n; j++)
        ...=...*b[j];
```



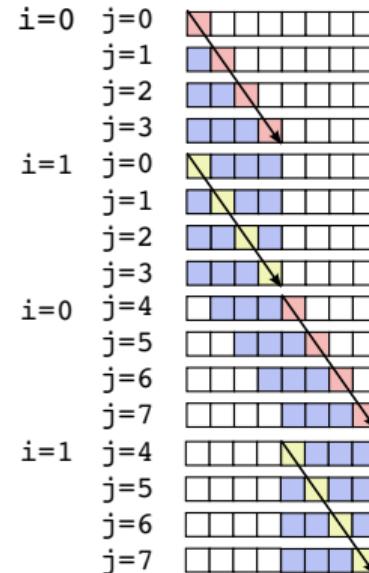
█ - cached, LRU eviction policy
█ - cache miss (read from memory, slow)
█ - cache hit (read from cache, fast)

Cache size: 4
 TILE=4
 (must be tuned to cache size)

Cache hit rate without tiling: 0%
 Cache hit rate with tiling: 50%

Tiled:

```
for (jj=0; jj<n; jj+=TILE)
    for (i=0; i<m; i++)
        for (j=jj; j<jj+TILE; j++)
            ...=...*b[j];
```



IMPROVING CACHE TRAFFIC

Before:

```

1  for (int i = 0; i < nParticles; i++) { // Particles that experience force
2      float Fx = 0, Fy = 0, Fz = 0; // Gravity force on particle i
3      for (int j = 0; j < nParticles; j++) { // Particles that exert force
4          //
5          Fx += dx*drPowerN32;   Fy += dy*drPowerN32;   Fz += dz*drPowerN32;

```

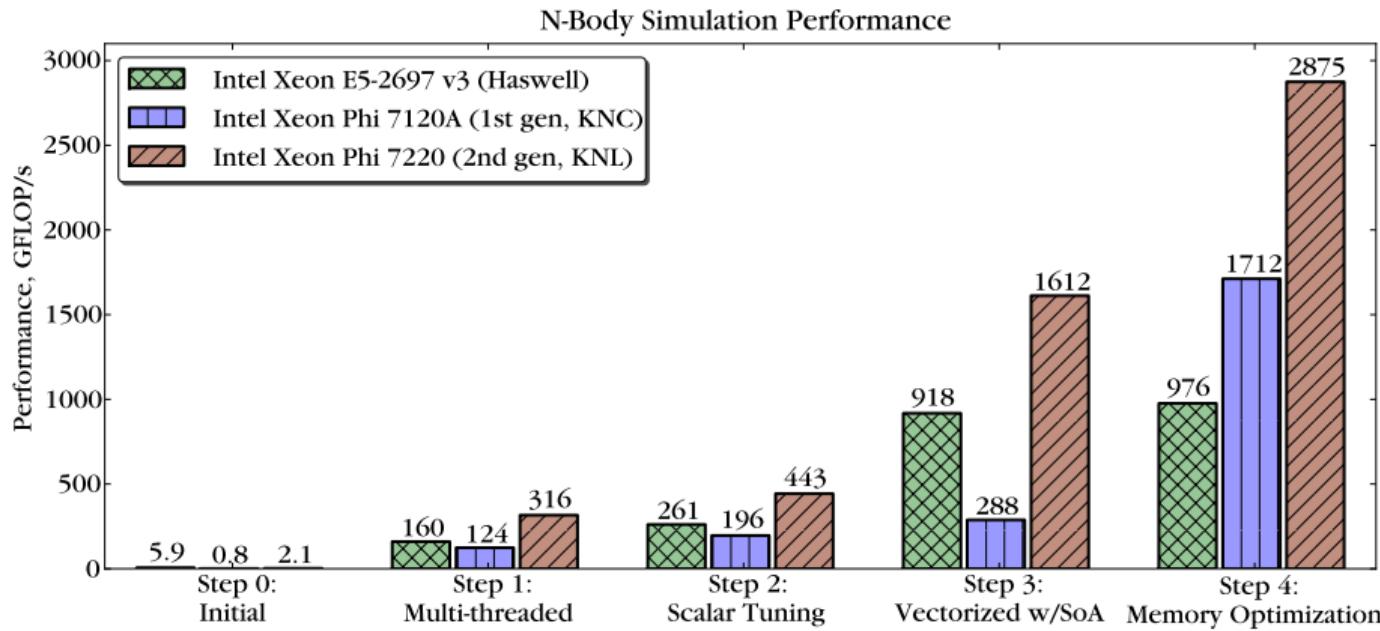
After: (tileSize = 16)

```

1  for (int ii = 0; ii < nParticles; ii += tileSize) { // Particle blocks
2      float Fx[tileSize], Fy[tileSize], Fz[tileSize]; // Force on particle block
3      Fx[:] = Fy[:] = Fz[:] = 0;
4      #pragma unroll(tileSize)
5      for (int j = 0; j < nParticles; j++) { // Particles that exert force
6          for (int i = ii; i < ii + tileSize; i++) { // Traverse the block
7              //
8          Fx[i-ii] += dx*drPowerN32; Fy[i-ii] += dy*drPowerN32; Fz[i-ii] += dz*drPowerN32;

```

IMPACT OF CODE OPTIMIZATION

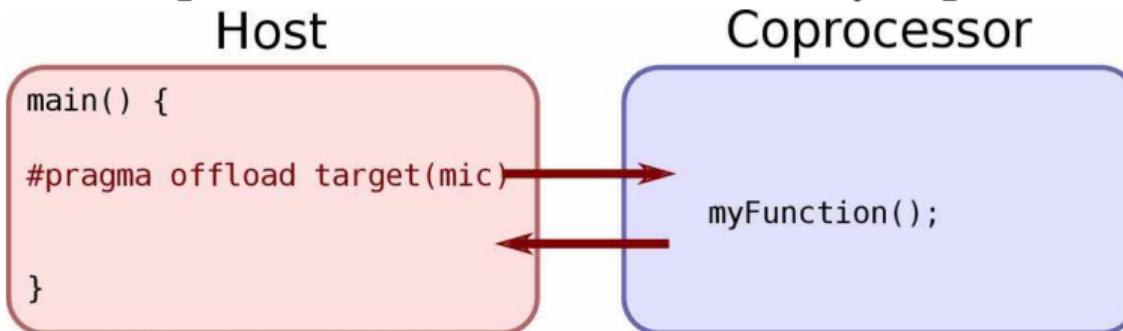


Contributed as Chapter 23 in “[Intel Xeon Phi Processor High Performance Programming, Knights Landing Edition](#)” (2016)

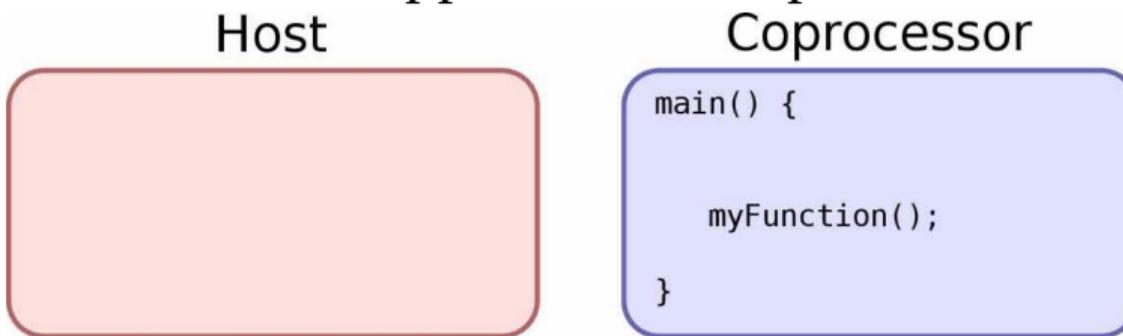
COPROCESSORS AND CLUSTERS

OFFLOAD AND NATIVE MODELS

- Offload model (explicit/virtual-shared memory/OpenMP 4.0):



- Native model (standalone application/MPI process):



INTEL COMPILERS + INTEL XEON PROCESSOR

“Hello World” application:

```
1 #include <cstdio>
2 #include <unistd.h>
3 int main(){
4     printf("Hello world! I have %ld logical processors.\n",
5         sysconf(_SC_NPROCESSORS_ONLN));
6 }
```

Compile and run on host CPU:

```
vega@lyra% icpc hello.cc -xhost
vega@lyra% ./a.out
Hello world! I have 48 logical processors.
vega@lyra%
```

NATIVE EXECUTION ON AN INTEL XEON PHI COPROCESSOR (KNC)

Compile and run the same code on the coprocessor in the native mode:

```
vega@lyra% icpc hello.cc -mmic # Cross-compile
vega@lyra% scp a.out mic0:~/ # Put executable on coprocessor
a.out 100% 10KB 10.4KB/s 00:00
vega@lyra% ssh mic0 # Log in to coprocessor
vega@mic0% pwd
/home/lyra
vega@mic0% ls
a.out
vega@mic0% ./a.out # Launch application
Hello world! I have 244 logical processors.
vega@mic0%
```

- ▶ Use `-mmic` to produce executable for MIC architecture
- ▶ Must transfer executable to coprocessor (or NFS-share) and run from shell
- ▶ Native MPI applications work the same way (need Intel MPI library)

NATIVE APPLICATIONS WITH AUTOTOOLS

- ▷ Use the Intel compiler with flag `-mmic`
- ▷ Knights Landing: `-xMIC-AVX512`
- ▷ Eliminate assembly and unnecessary dependencies
- ▷ Use `--host=x86_64` to avoid “program does not run” errors

Example, the GNU Multiple Precision Arithmetic Library (GMP):

```
vega@lyra% wget https://ftp.gnu.org/gnu/gmp/gmp-5.1.3.tar.bz2
vega@lyra% tar -xf gmp-5.1.3.tar.bz2
vega@lyra% cd gmp-5.1.3
vega@lyra% ./configure CC=icc CFLAGS="-mmic" --host=x86_64 --disable-assembly
...
vega@lyra% make
...
```

EXPLICIT OFFLOAD: PRAGMA-BASED APPROACH

“Hello World” in the explicit offload model:

```
1 #include <cstdio>
2 int main() {
3     printf("Hello World from host!\n");
4 #pragma offload target(mic)
5     {
6         printf("Hello World from coprocessor!\n"); fflush(stdout);
7     }
8     printf("Bye\n");
9 }
```

Application runs on the host, but some parts of code and data are moved (“offloaded”) to the coprocessor.

Detailed syntax in the [Intel C++ Compiler Reference](#).

COMPILING AND RUNNING AN OFFLOAD APPLICATION

```
vega@lyra% icpc hello_offload.cc -o hello_offload
vega@lyra% ./hello_offload
Hello World from host!
Bye
Hello World from coprocessor!
```

- ▶ No additional arguments (for Intel compiler)
- ▶ Launch on host as a regular application
- ▶ Code inside of #pragma offload is offloaded automatically
- ▶ Console output on coprocessor buffered, mirrored to the host
- ▶ If no coprocessor available, default behavior is error; may be overridden to fall back to host

OFFLOADING MULTIPLE FUNCTIONS

```
1 #pragma offload_attribute(push, target(mic))
2 void MyFunctionOne() {
3     // ... implement function as usual
4 }
5
6 void MyFunctionTwo() {
7     // ... implement function as usual
8 }
9 #pragma offload_attribute(pop)
```

- ▶ To mark a long block of code with the offload attribute, use `#pragma offload_attribute(push/pop)`

DATA MARSHALLING FOR DYNAMICALLY ALLOCATED DATA

```
1 double *p1=(double*)malloc(sizeof(double)*N);
2 double *p2=(double*)malloc(sizeof(double)*N);
3
4 #pragma offload target(mic) in(p1 : length(N)) out(p2 : length(N))
5 {
6     // ... perform operations on p1[] and p2[]
7 }
```

- ▶ `#pragma offload` recognizes clauses `in`, `out`, `inout` and `nocopy`
- ▶ Data size (`length`), alignment, redirection, and other properties may be specified
- ▶ Marshalling is required for pointer-based data

OPTIONAL OFFLOAD, FALL-BACK TO HOST

```
1 #pragma offload target(mic) optional
2 {
3     printf("Hello World! I have %d logical processors.\n",
4         sysconf(_SC_NPROCESSORS_ONLN )); fflush(stdout);
5 }
```

```
vega@lyra% icpc Offload-Fallback.cc -o Offload-Fallback
vega@lyra% ./Offload-Fallback
Hello World! I have 244 logical processors.
vega@lyra% sudo systemctl stop mpss # Disabling coprocessors
vega@lyra% ./Offload-Fallback
Hello World! I have 48 logical processors.
```

OPENMP 4.0 TARGET OFFLOAD

- ▶ Another API for offload: `#pragma omp target`
- ▶ Part of the OpenMP 4.0 standard
- ▶ Designed as portable solution (coprocessors, GPGPUs)
- ▶ On Xeon Phi, uses the same back-end as `#pragma offload`

```
1 #pragma omp target
2 {
3 #pragma omp parallel for
4     for(int i=0; i<size; i++)
5         data[i] = 0;
6 }
```

Application runs on the host, but some parts of code and data are moved (“offloaded”) to the coprocessor. Scope-local scalars and stack arrays offloaded automatically.

CLAUSES OF PRAGMA OMP TARGET

1

```
#pragma omp target [clause[, clause[, ...]]]
```

- ▶ device(int) – offload to a specific device (coprocessor)
- ▶ map([type:] variables) – create data environment. type is to, from, tofrom or alloc
- ▶ if(expr) – optional offload

Link to [reference manual](#).

SHARED VIRTUAL MEMORY MODEL

```
1 _Cilk_shared int arr[N]; // This is a virtual-shared array
2
3 _Cilk_shared void Compute() { // This function may be offloaded
4     // ... function uses array arr[]
5 }
6
7 int main() {
8     // arr[] can be initialized on the host
9     _Cilk_offload Compute(); // and used on coprocessor
10    // and the values are returned to the host
11 }
```

- ▶ Alternative to Explicit Offload
- ▶ Data synced from host to coprocessor before the start of offload
- ▶ Data synced from coprocessor to host at the end of offload

SHARED VIRTUAL MEMORY MODEL

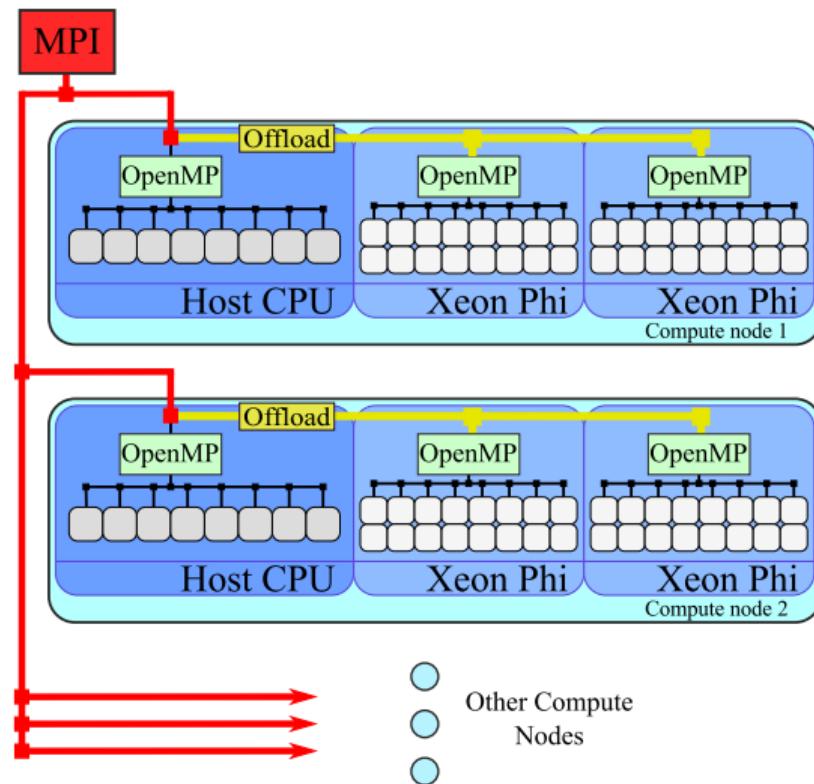
```
1 int* _Cilk_shared data; // Pointer to a virtual-shared array
2
3 int main() {
4     // Working with pointer-based data is illustrated below:
5     data = (_Cilk_shared int*)_Offload_shared_malloc(N*sizeof(float));
6     _Offload_shared_free(data);
7 }
```

- ▶ Addresses of virtual-shared pointers identical on host and coprocessors
- ▶ Synchronized before and after offload, with page granularity

HETEROGENEOUS DISTRIBUTED COMPUTING WITH XEON PHI

Option 1: MPI+OpenMP with Offload.

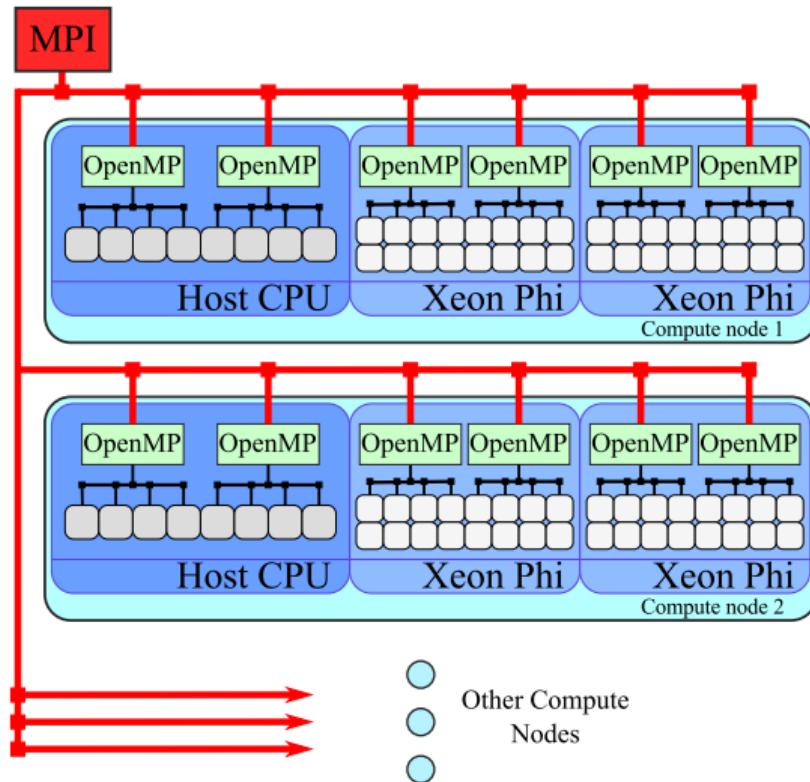
- ▷ MPI processes are multi-threaded with OpenMP.
- ▷ MPI runs only on CPUs.
- ▷ MPI processes offload to coprocessor(s).
- ▷ OpenMP in offload regions.



HETEROGENEOUS DISTRIBUTED COMPUTING WITH XEON PHI

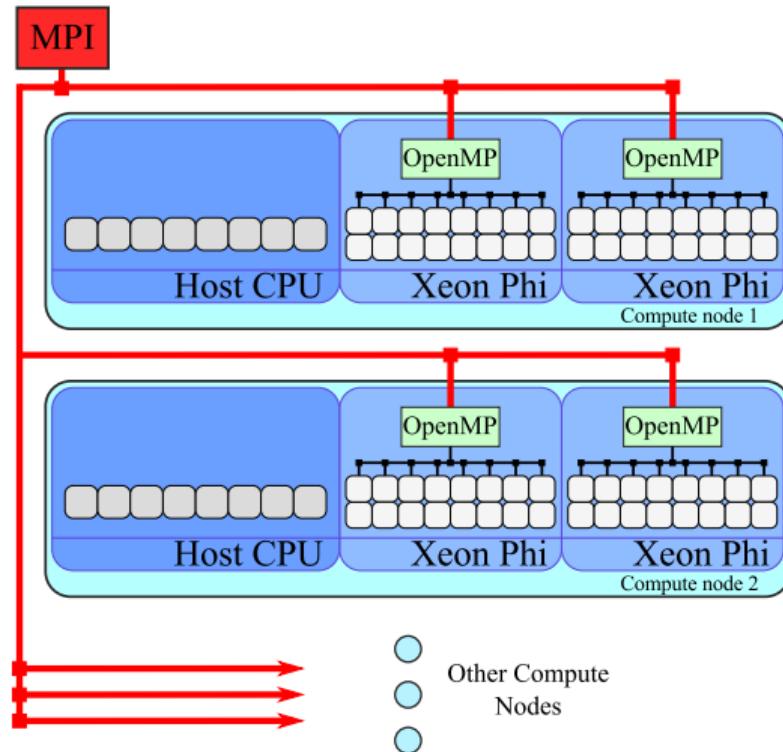
Option 2: Symmetric hybrid MPI+OpenMP.

- ▷ MPI processes on hosts
- ▷ Native MPI processes on the coprocessor.
- ▷ Multi-threading with OpenMP.



SCALING ACROSS A CLUSTER WITH COPROCESSORS WITH MPI

- ▷ MPI processes only on CPUs
- ▷ Divide data between coprocessors
- ▷ Concurrent offload from multiple host threads
- ▷ Synchronize data between nodes with MPI



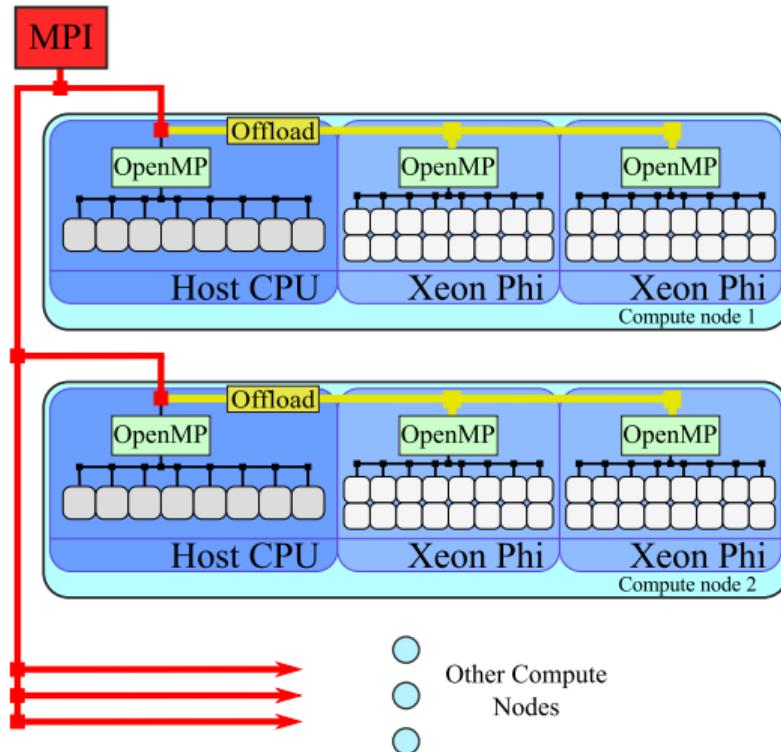
CORE OF MPI-ONLY IMPLEMENTATION

Simple: all particles on each compute node; exchange updated particle coordinates.

```
1 void MoveParticles(int nParticles, ParticleSet& particle, float dt,
2                     int mpiRank, int mpiWorldSize) {
3     const int myParticles = nParticles/mpiWorldSize;
4     const int startParticle = (mpiRank      )*myParticles;
5     const int endParticle = (mpiRank + 1)*myParticles;
6     // Outer loop over only the subset of particles processed by present process
7 #pragma omp parallel for schedule(guided)
8     for (int ii = startParticle; ii < endParticle; ii += tileSize) {
9         for (int j = 0; j < nParticles; j++) // ...But inner loop over all particles
10            //...
11    }
12    // ... Propagate results of time step across the cluster
13    MPI_Allgather(MPI_IN_PLACE, 0, MPI_DATATYPE_NULL, particle.x,
14                  myParticles, MPI_FLOAT, MPI_COMM_WORLD);
15    // ...
```

SCALING ACROSS A CLUSTER WITH COPROCESSORS

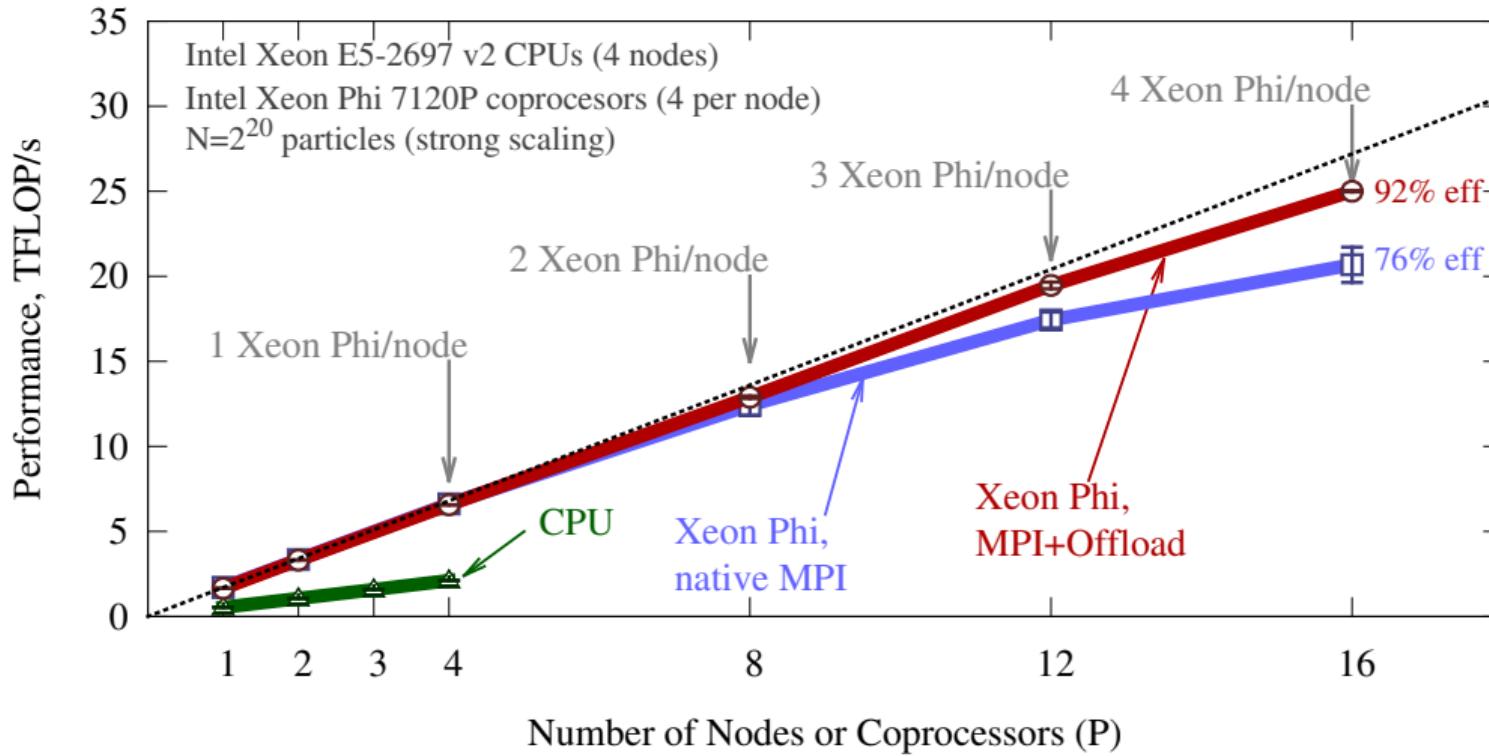
- ▷ MPI processes only on CPUs
- ▷ Divide data between coprocessors
- ▷ Concurrent offload from multiple host threads
- ▷ Synchronize data between nodes with MPI



MPI WITH OFFLOAD IMPLEMENTATION

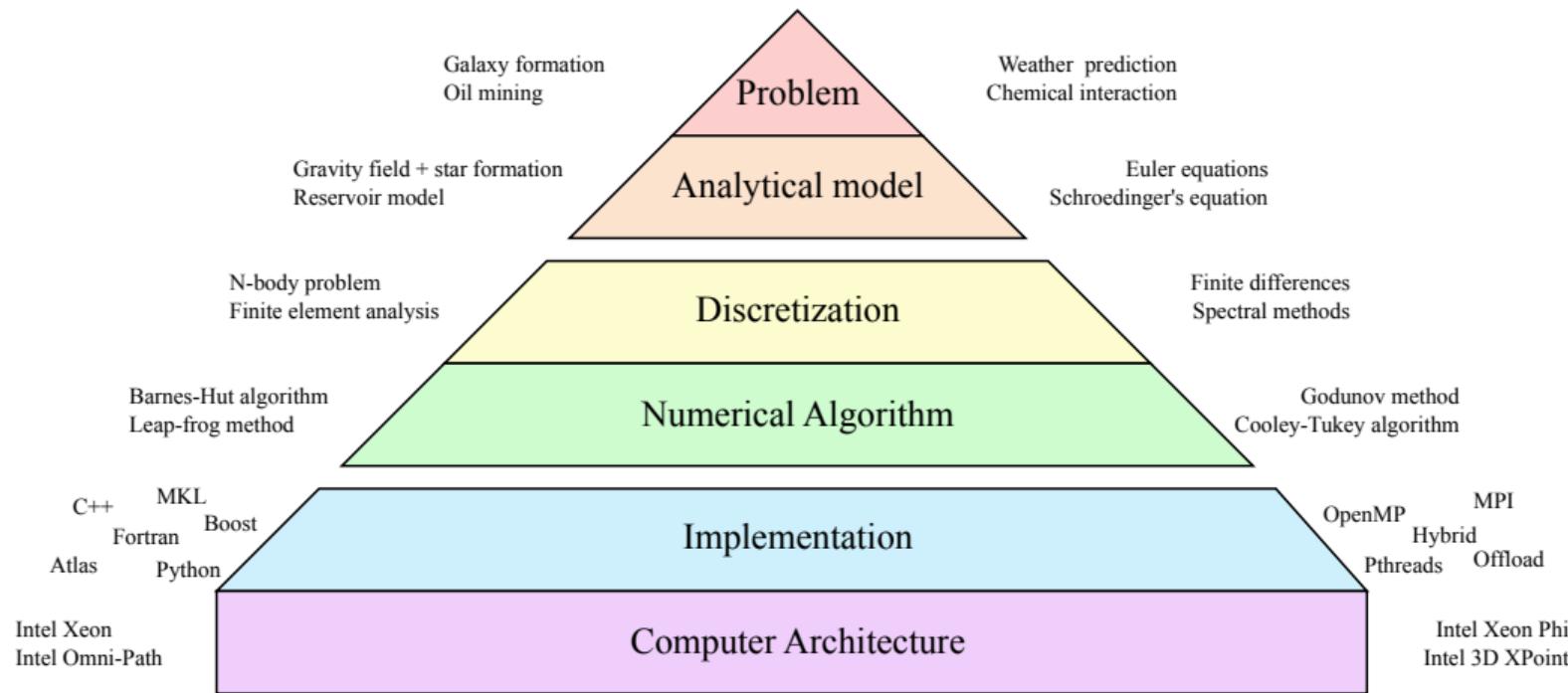
```
1 const int nDevices = _Offload_number_of_devices();
2 const int particlesPerDevice=(nDevices==0 ? myParticles : myParticles/nDevices);
3 #pragma omp parallel num_threads(nDevices) if(nDevices>0)
4 {
5     const int iDevice = omp_get_thread_num();
6     const int startParticle = rankStartParticle + (iDevice )*particlesPerDevice;
7 #pragma offload target(mic:iDevice) if(nDevices>0)           \
8     in (x : length(nParticles)                      alloc_if(alloc==1) free_if(0)) \
9     out(x  [startParticle:particlesPerDevice] : alloc_if(0) free_if(alloc==-1)) \
10    in (vx: length(nParticles*alloc*alloc)          alloc_if(alloc==1) free_if(0)) \
11 //...
12 { // Loop over particles that experience force
13 #pragma omp parallel for schedule(guided)
14     for (int ii = startParticle; ii < endParticle; ii += tileSize) {
15         // ...
```

RESULTS WITH MPI+OFFLOAD



§3. OPTIMIZATION POINTERS

COMPUTING IN SCIENCE AND ENGINEERING



SCOPE OF THIS COURSE

Areas of code optimization for Intel architecture:

1. **Scalar optimization** (compiler-friendly practices)
2. **Vectorization** (must use 16- or 8-wide vectors)
3. **Multi-threading** (must scale to 100+ threads)
4. **Memory access** (streaming access or tiling)
5. **Communication** (offload, MPI traffic control)

SCALAR TUNING

OPTIMIZATION LEVEL

Default optimization level -O2

- ▷ optimization for speed
- ▷ automatic vectorization
- ▷ inlining
- ▷ constant propagation
- ▷ dead-code elimination
- ▷ loop unrolling

Optimization level -O3

- ▷ aggressive optimization
- ▷ loop fusion
- ▷ block-unroll-and-jam
- ▷ if-statement collapse
- ▷ *may or may not be better than -O2*

SETTING OPTIMIZATION LEVEL

For the entire file:

```
vega@lyra% icpc -o mycode -O3 source.cc
```

For a specific function:

```
1 #pragma intel optimization_level 3
2 void my_function() {
3     //...
4 }
```

STRENGTH REDUCTION

Common Subexpression Elimination.

```

1 for (int i = 0; i < n; i++) {
2     A[i] /= B;
3 }
```

```

1 const float Br = 1.0f/B;
2 for (int i = 0; i < n; i++)
3     A[i] *= Br;
```

Replace division with multiplication.

```

1 for (int i = 0; i < n; i++) {
2     P[i] = (Q[i]/R[i])/S[i];
3 }
```

```

1 for (int i = 0; i < n; i++) {
2     P[i] = Q[i]/(R[i]*S[i]);
3 }
```

Use functions with Hardware support.

```

1 double r = pow(r2, -0.5);
2 double v = exp(x);
3 double y = y0*exp(log(x/x0)*
4                 log(y1/y0)/log(x1/x0));
```

```

1 double r = 1.0/sqrt(r2);
2 double v = exp2(x*1.44269504089);
3 double y = y0*exp2(log2(x/x0)*
4                 log2(y1/y0)/log2(x1/x0));
```

CONSISTENCY OF PRECISION: CONSTANTS

```

1 // Bad: 2 is "int"
2 long b=a*2;
3
4 // Bad: overflow
5 long n=100000*100000;
6
7 // Bad: excessive
8 float p=6.283185307179586;
9
10 // Bad: 2 is "int"
11 float q=2*p;
12
13 // Bad: 1e9 is "double"
14 float r=1e9*p;
15
16 // Bad: 1 is "int"
17 double t=s+1;

```

```

1 // Good: 2L is "long"
2 long b=a*2L;
3
4 // Good: correct
5 long n=100000L*100000L;
6
7 // Good: accurate
8 float p=6.283185f;
9
10 // Good: 2.0f is "float"
11 float q=2.0f*p;
12
13 // Good: 1e9f is "float"
14 float r=1e9f*p;
15
16 // Good: 1.0 is "double"
17 double t=s+1.0;

```

CONSISTENCY OF PRECISION: FUNCTIONS

```
1 // Bad: 3.14 is a double  
2 float x = 3.14;  
  
3  
4 // Bad: sin() is a  
5 // double precision function  
6 float s = sin(x);  
  
7  
8 // Bad: round() takes double  
9 // and returns double  
10 long v = round(x);  
  
11  
12 // Bad: abs() is not from IML  
13 // it takes int and returns int  
14 int v = abs(x);
```

```
1 // Good: 3.14f is a float  
2 float x = 3.14f;  
  
3  
4 // Good: sin() is a  
5 // single precision function  
6 float s = sinf(x);  
  
7  
8 // Good: lroundf() takes float  
9 // and returns long  
10 long v = lroundf(x);  
  
11  
12 // Good: fabsf() is from IML  
13 // It takes and returns a float  
14 float v = fabsf(x);
```

MOVE BRANCHES OUTSIDE OF LOOPS

74

```
1 // Elegant, but bad for performance
2 for (i = 0; i < n; i++) {
3     if (i == 0) {
4         // Absorbing boundary
5         B[i] = 0.0;
6     } else if (i == n - 1) {
7         // Injection at boundary
8         B[i] = B[i] + 1.0;
9     } else {
10        // Diffusion between boundaries
11        B[i] = 0.25*(A[i-1] +
12                           2.0*A[i] + A[i+1]);
13    }
14 }
```

```
1 // Moving branches out of loops
2
3
4 // Absorbing boundary
5 B[i] = 0.0;
6
7 for (i = 1; i < n - 1; i++) {
8     // Diffusion between boundaries
9     B[i] = 0.25*(A[i-1] + 2.0*A[i] +
10                   A[i+1]);
11 }
12
13 // Injection at boundary
14 B[n-1] = B[n-1] + 1.0;
```

REDUNDANT CODE IS OK

```
1 // Elegant, but bad for performance
2 for (ii = 0; ii < n; ii+=16) {
3     for (i = ii; i < ii+16; i++)
4         // Branch causes unnecessary
5         // masking of vector iterations
6     if (i < n) {
7         A[k*n + i] = ...
8     }
9 }
```

```
1 // Redundant code, but faster
2 const int nTrunc = n - 16;
3 for (ii = 0; ii < nTrunc; ii+=16) {
4     for (i = ii; i < ii+16; i++)
5         A[k*n + i] = ...
6
7 for (i = nTrunc; i < n; i++)
8     A[k*n + i] = ...
9 }
```

VECTORIZATION

AUTOMATIC VECTORIZATION OF LOOPS

```

1 #include <cstdio>
2
3 int main(){
4     const int n=8;
5     int i;
6     int A[n] __attribute__((aligned(64)));
7     int B[n] __attribute__((aligned(64)));
8
9     // Initialization
10    for (i=0; i<n; i++)
11        A[i]=B[i]=i;
12
13    // This loop will be auto-vectorized
14    for (i=0; i<n; i++)
15        A[i]+=B[i];
16
17    // Output
18    for (i=0; i<n; i++)
19        printf("%2d %2d %2d\n", i, A[i], B[i]);
20}

```

```

vega@lyra% icpc autovec.cc -qopt-report
vega@lyra% cat autovec.optrpt
...
LOOP BEGIN at autovec.cc(14,3)
remark #15399: vectorization support:
unroll factor set to 2 [autovec.cc(14,3)]
remark #15300: LOOP WAS VECTORIZED
[autovec.cc(14,3)]
LOOP END
...
vega@lyra% ./a.out
0 0 0
1 2 1
2 4 2
3 6 3
4 8 4
5 10 5
6 12 6
7 14 7

```

VECTORIZE MORE LOOPS: #pragma simd

Statement `#pragma simd` is used to “enforce vectorization of loops”, which includes:

- ▶ Loops with SIMD-enabled functions (see below)
- ▶ Second innermost loops
- ▶ Failed vectorization due to compiler decision
- ▶ Loops where guidance is required (vector length, reduction, etc.)

See compiler reference on `#pragma simd` for more information.

EXTENSIONS FOR ARRAY NOTATION

Array notation is a method for specifying

- ▷ slices of arrays (begin, length)

```
1 A[0:16] += B[32:16]; // B[32]...B[47] added to A[0]...A[15]
```

- ▷ a stride (begin, length, stride)

```
1 A[0:16:2] += B[32:16:4]; // B[32],B[36]...B[92] added A[0],A[2]...A[30]
```

- ▷ Multi-dimensional arrays

```
1 A[:, :] += B[:, :]; // Add B to A; arrays are of the same shape
```

Better than strided loops (e.g., [this paper](#)).

SIMD-ENABLED FUNCTIONS

(formerly “elemental functions”)

What if the implementation of a function is in a separate source code file
(e.g., a library function)?

```
1 float my_simple_add(float x1, float x2){  
2     return x1 + x2;  
3 }
```

```
1 // ...in a separate source file:  
2 for (int i = 0; i < N, ++i) {  
3     output[i] = my_simple_add(inputa[i], inputb[i]);  
4 }
```

Compiler will refuse to automatically vectorize this loop.

SIMD-ENABLED FUNCTIONS

The solution is to design and declare the function as *SIMD-enabled*:

```
1 __attribute__((vector)) float my_simple_add(float x1, float x2) {  
2     return x1 + x2;  
3 }
```

When using SIMD-enabled functions, use `#pragma simd`.

```
1 // ...in a separate source file:  
2 #pragma simd  
3 for (int i = 0; i < N, ++i) {  
4     output[i] = my_simple_add(inputa[i], inputb[i]);  
5 }
```

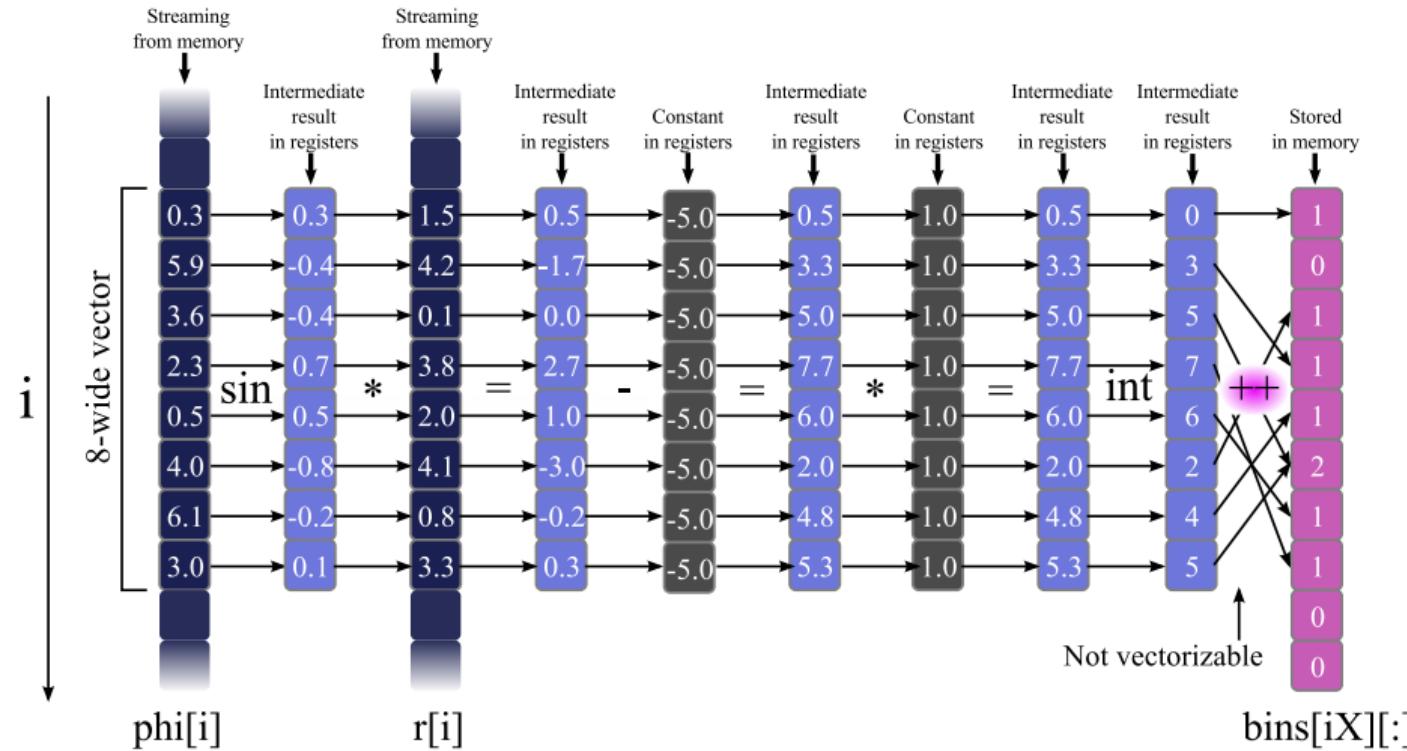
In this case, automatic vectorization succeeds.

AUTO-VECTORIZED LOOPS MAY BE COMPLEX (EXAMPLE 1)

```
1  for (int i = ii; i < ii + tileSize; i++) { // Target for auto-vectorization
2
3      // Newton's law of universal gravity
4      const float dx = particle.x[j] - particle.x[i]; // x[j] is a const
5      const float dy = particle.y[j] - particle.y[i]; // x[i] makes SIMD vector
6      const float dz = particle.z[j] - particle.z[i];
7      const float rr = 1.0f/sqrta(dx*dx + dy*dy + dz*dz + softening);
8      const float drPowerN32 = rr*rr*rr;
9
10     // Calculate the net force
11     Fx[i-ii] += dx * drPowerN32;
12     Fy[i-ii] += dy * drPowerN32;
13     Fz[i-ii] += dz * drPowerN32;
14 }
```

See also [this presentation](#)

AUTO-VECTORIZED LOOPS MAY BE COMPLEX (EXAMPLE 2)



See [this paper](#) for more details

ASSUMED VECTOR DEPENDENCE

- True vector dependence makes vectorization impossible:

```

1 float *a, *b;
2 for (int i = 1; i < n; i++)
3     a[i] += b[i]*a[i-1]; // dependence on the previous element

```

- Assumed vector dependence*: when compiler cannot determine whether vector dependence exists, auto-vectorization fails:

```

1 void mycopy(int n,
2             float* a, float* b) {
3     for (int i = 0; i < n; i++)
4         a[i] = b[i];
5 }

```

```

vega@lyra% icpc -c vdep.cc -qopt-report \
> -qopt-report-phase:vec
vega@lyra% cat vdep.optrpt
...
remark #15304: loop was not
vectorized: non-vectorizable loop
instance from multiversing
...

```

IGNORING ASSUMED VECTOR DEPENDENCE

To ignore assumed vector dependence

```
#pragma ivdep
```

```
1 void mycopy(int n,
2             float* a, float* b) {
3 #pragma ivdep
4     for (int i = 0; i < n; i++)
5         a[i] = b[i];
6 }
```

```
vega@lyra% icpc -c vdep.cc -qopt-report \
> -qopt-report-phase:vec
vega@lyra% cat vdep.optrpt
...
LOOP BEGIN at vdep.cc(4,1)
<Multiversioned v2>
remark #15300: LOOP WAS VECTORIZED
LOOP END
```

MULTIVERSIONING

```
user@host% icpc -c code.cc -qopt-report -qopt-report-phase:vec
user@host% cat code.optrpt
...
LOOP BEGIN at code.cc(4,1)
<Multiversioned v1>
    remark #25228: LOOP WAS VECTORIZED
LOOP END
...
LOOP BEGIN at code.cc(4,1)
<Multiversioned v2>
    remark #15304: loop was not vectorized: non-vectorizable loop instance ....
LOOP END
```

Aliasing (true vector dependence) checked at *runtime* to choose the implementation.

POINTER DISAMBIGUATION TO PREVENT MULTIVERSIONING

Prevent multiversioning by using `#pragma ivdep`

```
1 #pragma ivdep
2   for (int i = 0; i < n; i++)
3     // ...
```

```
user@host% icpc -c code.cc -qopt-report -qopt-report-phase:vec
user@host% cat vdep.optrpt
```

```
...
LOOP BEGIN at code.cc(4,1)
  remark #25228: LOOP WAS VECTORIZED
LOOP END
...
```

When keyword `restrict` is used instead, may not disambiguate different offsets of same pointer (e.g, `A[i*n+j] += A[b*n+j]`).

UNIT-STRIDE ACCESS

Unit-stride access is optimal:

```
1 for (int i = 0; i < n; i++)
2     A[i] += B[i];
```

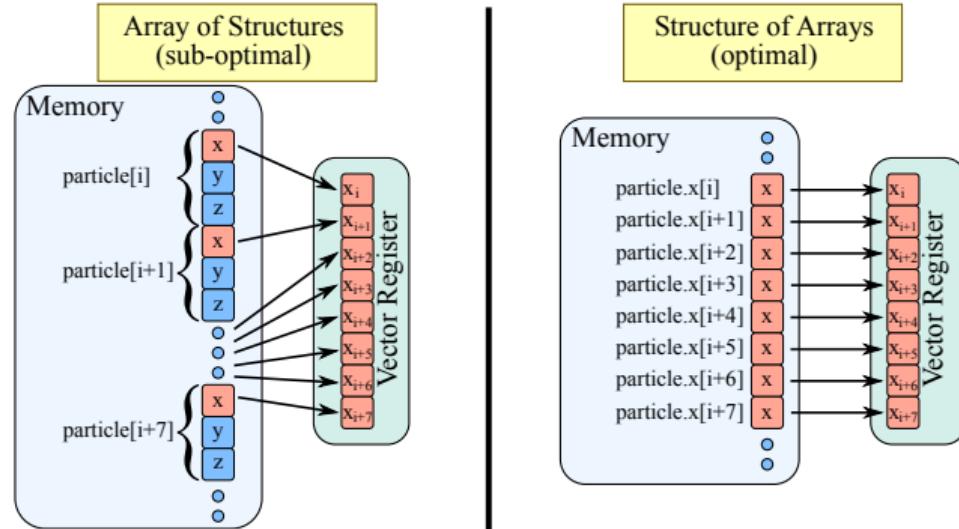
Non-unit stride is slower:

```
1 for (int i = 0; i < n; i++)
2     A[i*stride] += B[i];
```

Stochastic access may be vectorized (but not efficient):

```
1 for (int i = 0; i < n; i++)
2     A[offset[i]] += B[i];
```

It may be a question of changing the order of loop nesting, but sometimes you need to modify data structures:



DATA ALIGNMENT REQUIREMENTS

Array `char* p` is n-byte aligned if $((\text{size_t})p \% n == 0)$.

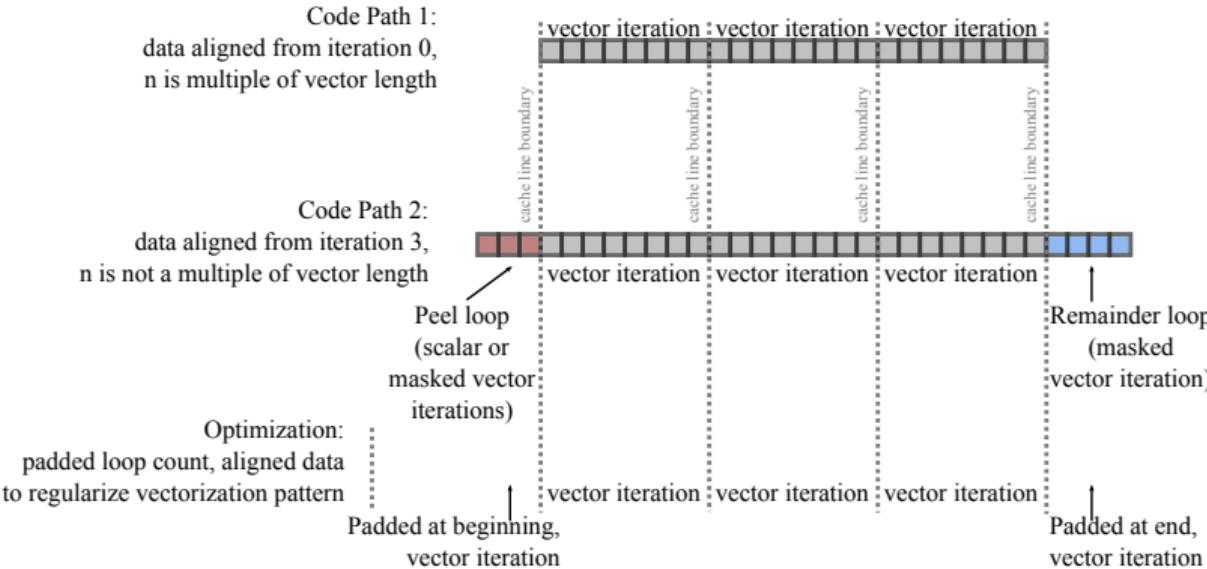
Processor	Operation	Alignment
Xeon (Westmere and earlier)	SSE load, store	16-byte
Xeon (Sandy Bridge and later)	AVX load, store	32-byte (relaxed)
Xeon Phi (1st gen)	IMCI load, store	64-byte (strict)
Xeon Phi (1st gen)	DMA transfer in offload	4096-byte (preferred)
Xeon Phi (2nd gen)	AVX-512 load, store	64-byte (relaxed)

Why align: speed up vector load/stores, avoid false sharing (see Session 7), accelerate RDMA.

WHAT HAPPENS WITHOUT ALIGNMENT

Compiler may implement peel and remainder loops:

```
for (i = 0; i < n; i++) A[i] = ...
```



CREATING ALIGNED DATA CONTAINERS

- ▶ Data alignment on the stack

```
1 float A[n] __attribute__((aligned(64))); // 64-byte alignment applied
```

- ▶ Data alignment on the heap

```
1 float *A = (float*) _mm_malloc(sizeof(float)*n, 64);
```

- ▶ A[0] is aligned on a 64-byte boundary.
- ▶ Very high alignment value may lead to wasted virtual memory.
- ▶ Fortran: directive or compiler argument -align array64byte

PADDING MULTI-DIMENSIONAL CONTAINERS FOR ALIGNMENT

To use aligned instructions, you may need to pad inner dimension of multi-dimensional arrays to a multiple of 16 (in SP) or 8 (DP) elements.

Incorrect:

```
1 // A - matrix of size (n x n)
2 // n is not a multiple of 16
3 float* A =
4 _mm_malloc(sizeof(float)*n*n, 64);
5
6 for (int i = 0; i < n; i++)
7     // A[i*n + 0] may be unaligned
8     for (int j = 0; j < n; j++)
9         A[i*n + j] = ...
```

Correct:

```
1 // ... Padding inner dimension
2 int lda=n + (16-n%16); // lda%16==0
3 float* A =
4 _mm_malloc(sizeof(float)*n*lda, 64);
5
6 for (int i = 0; i < n; i++)
7     // A[i*lda + 0] aligned for any i
8     for (int j = 0; j < n; j++)
9         A[i*lda + j] = ...
```

VECTORIZATION PRAGMAS, KEYWORDS AND COMPILER ARGUMENTS

- ▷ `#pragma simd`
- ▷ `#pragma vector always`
- ▷ `#pragma vector aligned | unaligned`
- ▷ `__assume_aligned` keyword
- ▷ `#pragma vector nontemporal | temporal`
- ▷ `#pragma novector`
- ▷ `#pragma ivdep`
- ▷ `restrict` qualifier and `-restrict` command-line argument
- ▷ `#pragma loop count`
- ▷ `-qopt-report -qopt-report-phase:vec`
- ▷ `-O[n]`
- ▷ `-x[code]`

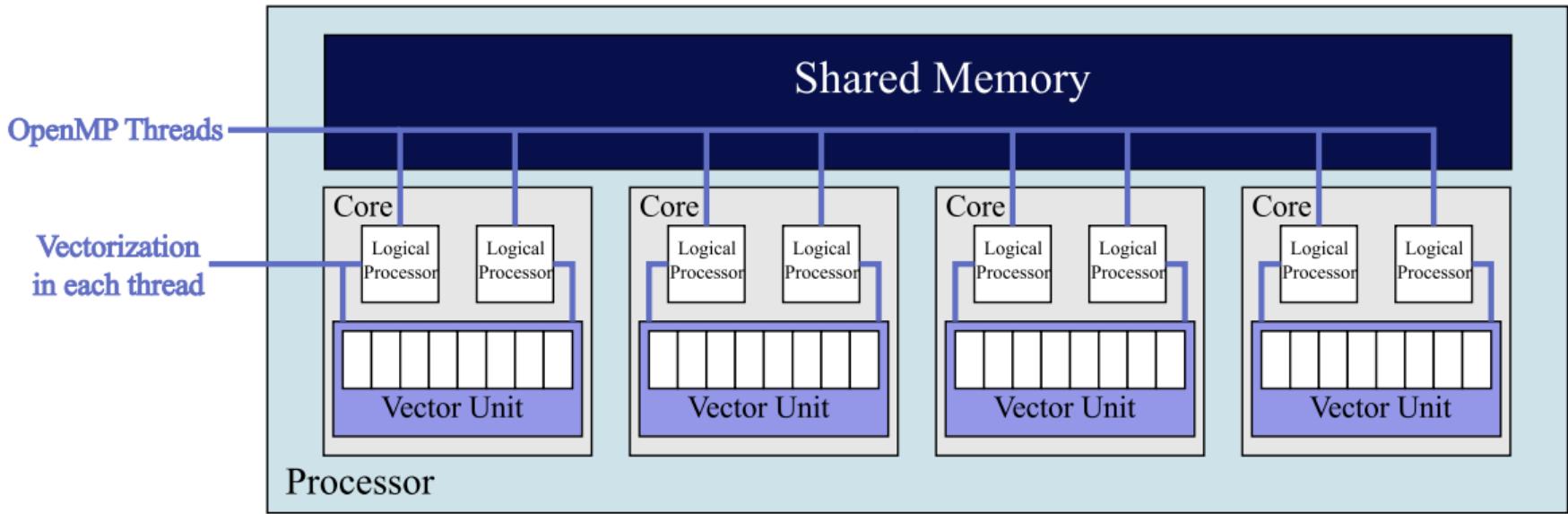
MULTI-THREADING

"HELLO WORLD" OPENMP PROGRAM

```
1 #include <omp.h>
2 #include <stdio.h>
3
4 int main(){
5     // This code is executed by only 1 thread
6     const int nt=omp_get_max_threads();
7     printf("OpenMP with %d threads\n", nt);
8
9 #pragma omp parallel
10 {
11     // This code is executed in parallel
12     // by multiple threads
13     printf("Hello World from thread %d\n",
14                         omp_get_thread_num());
15 }
16 }
```

- ▷ OpenMP = “Open Multi-Processing” = computing-oriented framework for shared-memory programming
- ▷ Threads – streams of instructions that share memory address space
- ▷ Distribute threads across CPU cores for parallel speedup

CO-EXISTENCE WITH VECTORS

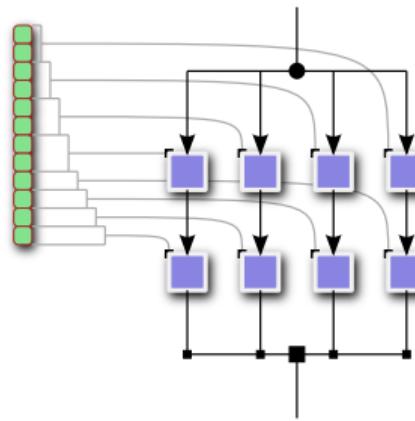
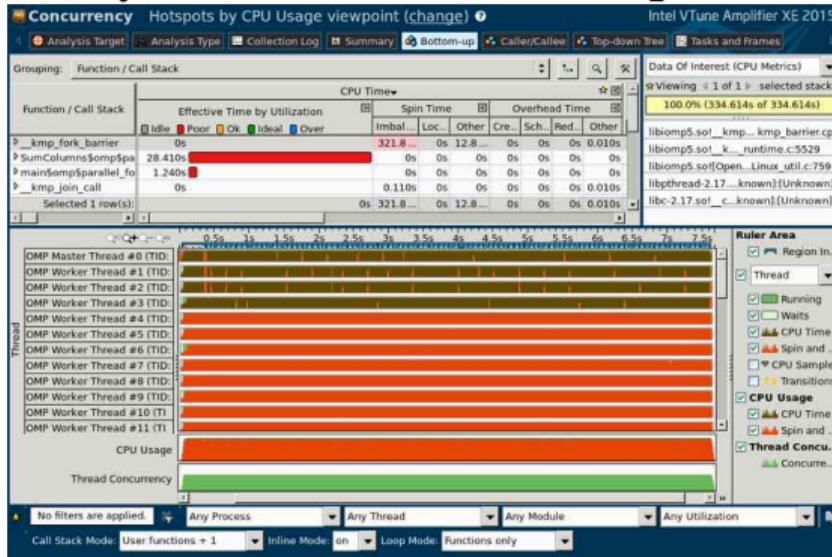


Utilize cores: run multiple threads/processes (MIMD)

Utilize vectors: each thread (process) issues vector instructions (SIMD)

INSUFFICIENT PARALLELISM

Analysis in Intel VTune Amplifier XE



- ▷ Occurs when there are not enough iterations or parallel work-items exposed to the parallel loop in OpenMP.

EXAMPLE: DEALING WITH INSUFFICIENT PARALLELISM

$$S_i = \sum_{j=0}^n M_{ij}, \quad i = 0 \dots m. \quad (1)$$

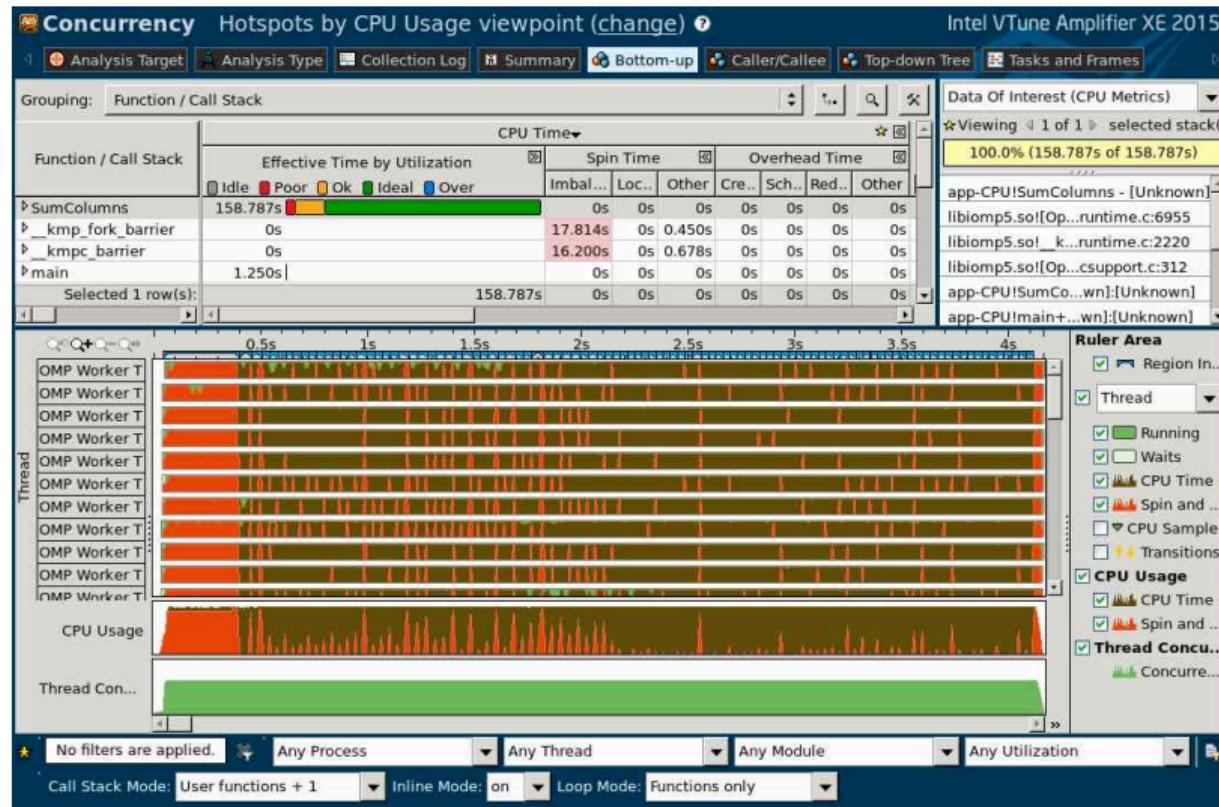
- ▷ $m=4$ is small, smaller than the number of threads in the system
- ▷ $n \approx 10^8$ is large enough so that matrix does not fit into cache

```
1 void sum_unoptimized(const int m, const int n, long* M, long* s){  
2 #pragma omp parallel for  
3     for (int i=0; i<m; i++) { // m=4  
4         long total=0;  
5 #pragma vector aligned  
6         for (int j=0; j<n; j++) // n=100000000  
7             total+=M[i*n+j];  
8         s[i]=total; } }
```

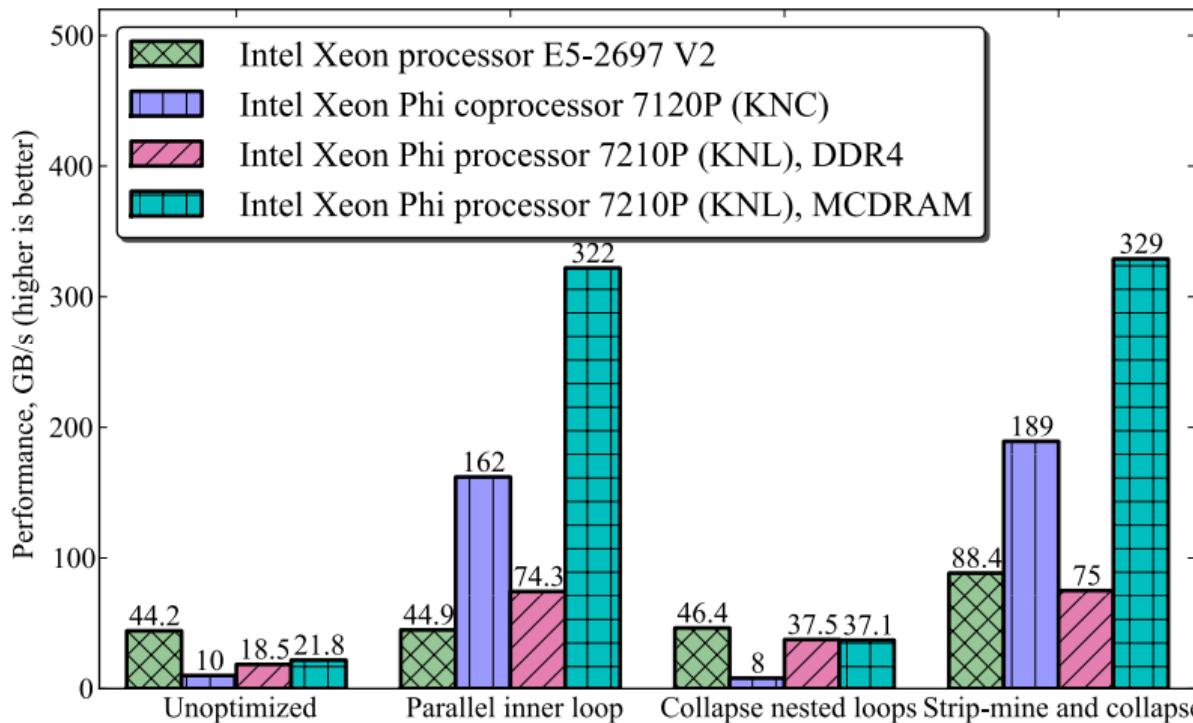
EXPOSING PARALLELISM: STRIP-MINING AND LOOP COLLAPSE

```
1 void sum_stripmine(const int m, const int n, long* M, long* s){  
2     const int STRIP=1024;  
3     assert(n%STRIP==0);  
4     s[0:m]=0;  
5 #pragma omp parallel  
6 {  
7     long total[m];    total[0:m]=0;  
8 #pragma omp for collapse(2) schedule(guided)  
9     for (int i=0; i<m; i++)  
10        for (int jj=0; jj<n; jj+=STRIP)  
11 #pragma vector aligned  
12        for (int j=jj; j<jj+STRIP; j++)  
13            total[i]+=M[i*n+j];  
14        for (int i=0; i<m; i++)           // Reduction  
15 #pragma omp atomic  
16        s[i]+=total[i];  
17    } }
```

EXPOSING PARALLELISM: STRIP-MINING AND LOOP COLLAPSE



DEALING WITH INSUFFICIENT PARALLELISM



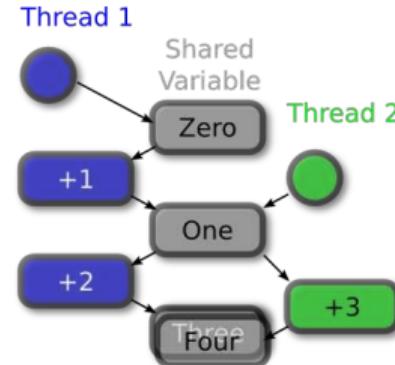
RACE CONDITIONS AND UNPREDICTABLE PROGRAM BEHAVIOR

```

1 #include <omp.h>
2 #include <cstdio>
3 int main() {
4     const int n = 1000;
5     int total = 0;
6     #pragma omp parallel for
7     for (int i = 0; i < n; i++) {
8         total = total + i; // Race condition
9     }
10    printf("total=%d (must be %d)\n",
11                      ((n-1)*n)/2);
12 }
```

```

vega@lyra% icpc -o app omp-race.cc -qopenmp
vega@lyra% ./app
total=208112 (must be 499500)
```



Race Condition!

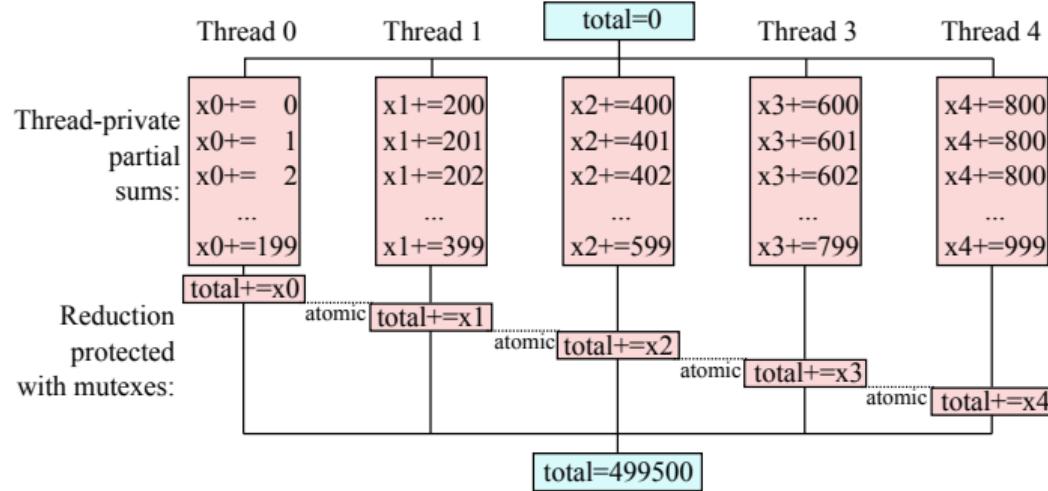
- ▷ Occurs when 2 or more threads access the same memory address, and at least one of these accesses is for writing

AVOIDING RACES WITH THREAD-PRIVATE STORAGE

Correct and efficient code:

```

1 int total = 0;
2 #pragma omp parallel
3 {
4     int total_thr = 0;
5 #pragma omp for
6     for (int i=0; i<n; i++)
7         total_thr += i;
8
9 #pragma omp atomic
10    total += total_thr;
11
12 }
```



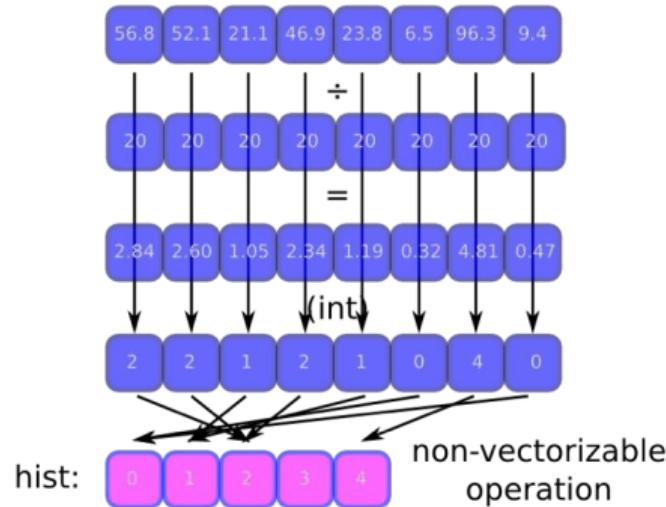
EXAMPLE: BINNING PROBLEM

Computing a histogram ($m \ll n$):

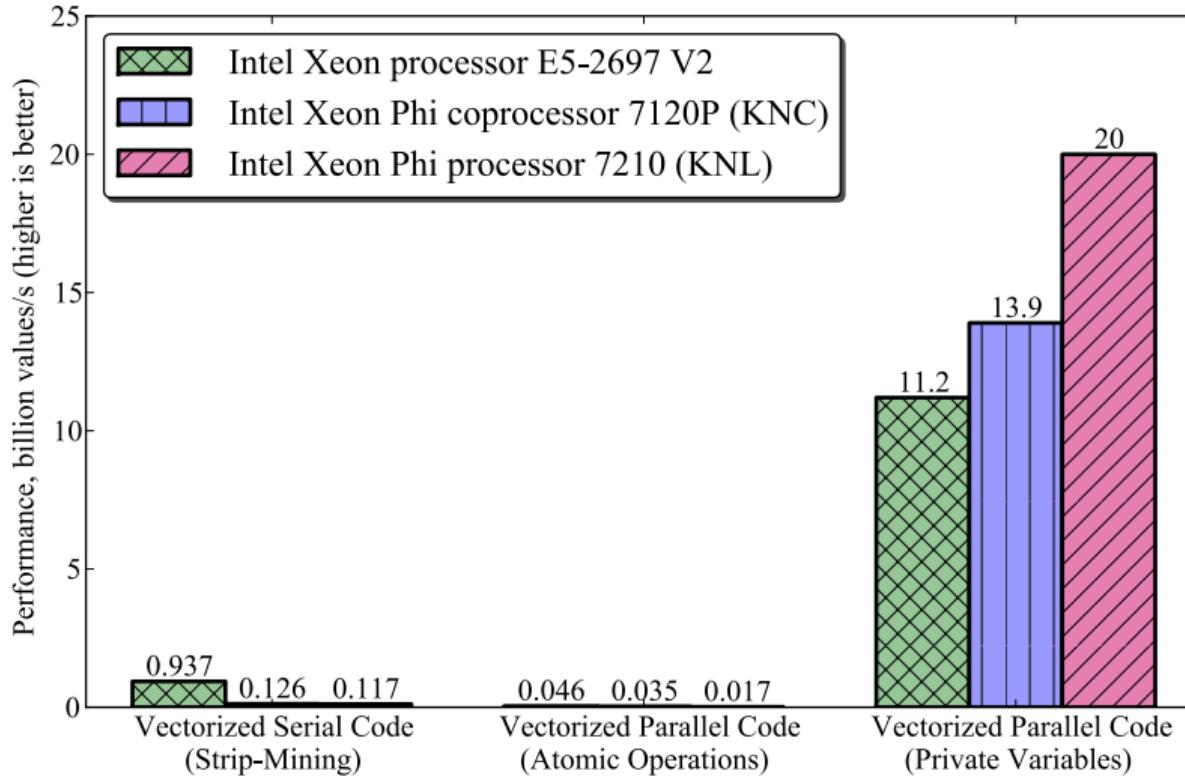
```

1 void Histogram(
2   // Ages, values from 0.0f to 100.0f:
3   const float* age,
4   // Size of array age, n=100000000:
5   const int n,
6   // Output: counts in groups:
7   int* const hist,
8   // Size of array hist, m=5:
9   const int m,
10  const float group_width) {
11    for (int i = 0; i < n; i++) {
12      const int j = int(age[i]/group_width);
13      hist[j]++;
14    }
15 }
```

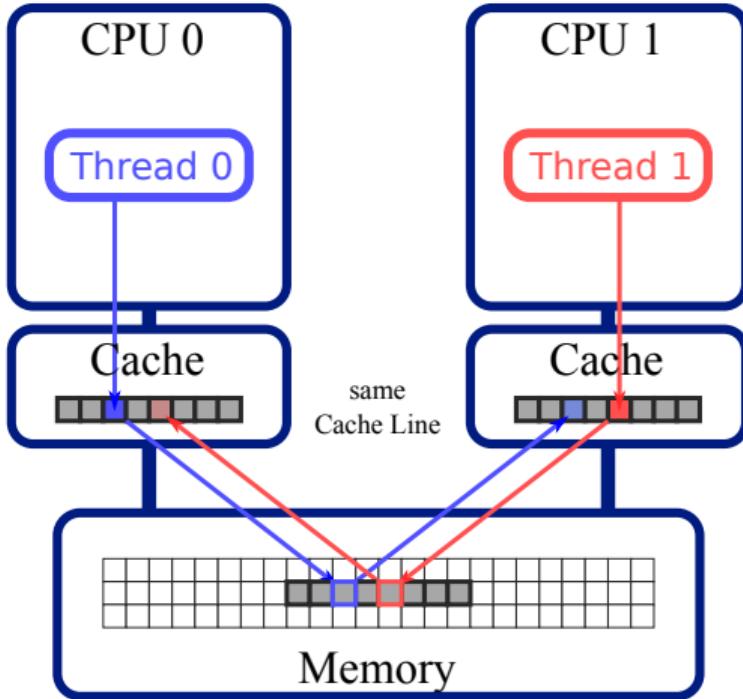
- ▷ Vector dependence in $hist[j]++$
- ▷ Strip-mine or use conflict detection



USING REDUCTION INSTEAD OF SYNCHRONIZATION

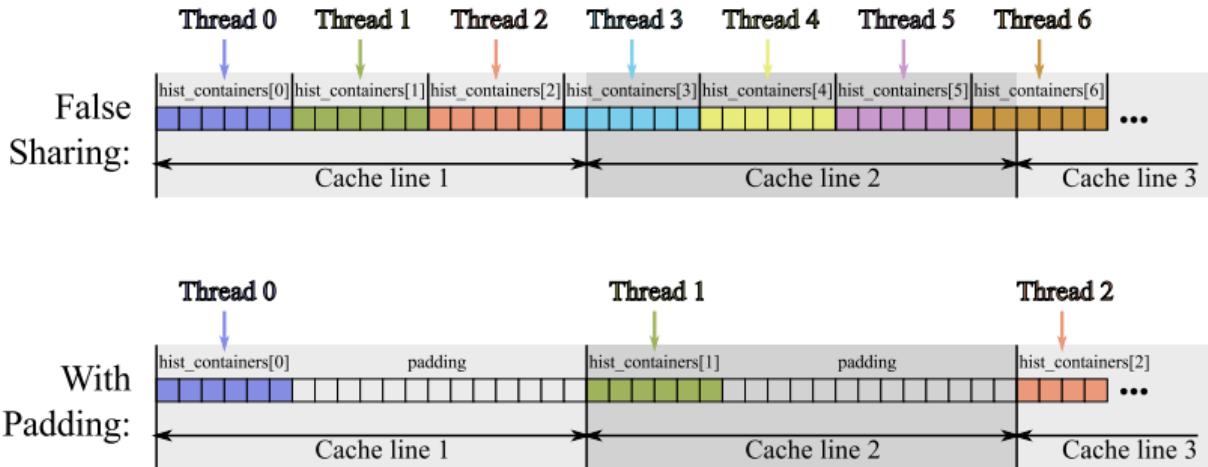


FALSE SHARING. DATA PADDING AND PRIVATE VARIABLES



- ▶ Occurs when 2 or more threads access the same cache line, and at least one of the accesses is for writing
- ▶ Caused by *coherent caches*
- ▶ Cache line is 64-byte wide (in modern Intel architectures)

PADDING TO AVOID FALSE SHARING

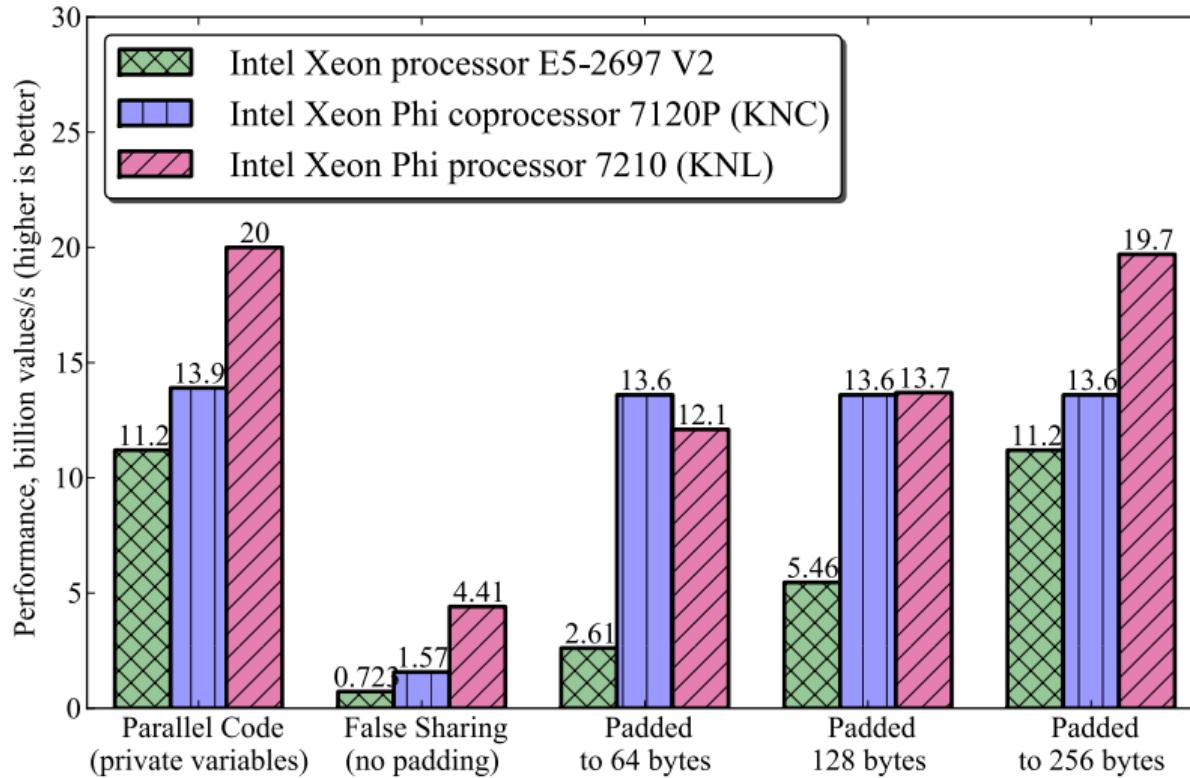


```

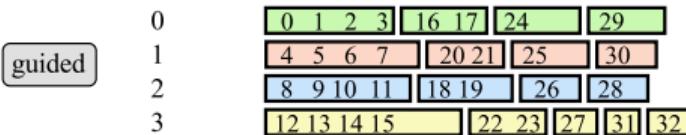
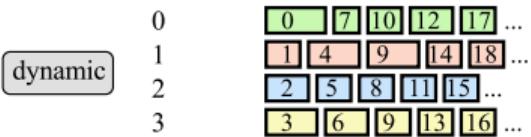
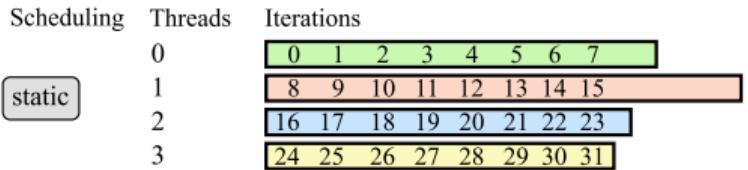
1 // Padding to avoid sharing a cache line between threads
2 const int paddingBytes = 64;
3 const int paddingElements = paddingBytes / sizeof(int);
4 const int mPadded = m + (paddingElements-m%paddingElements);
5 int histContainers[nThreads][mPadded]; // New container

```

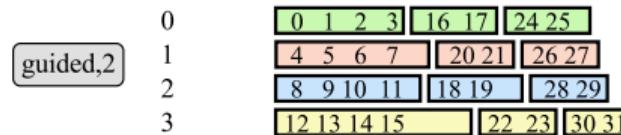
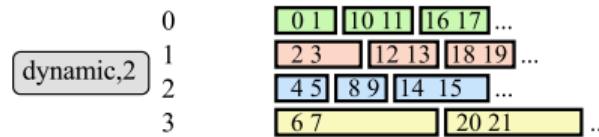
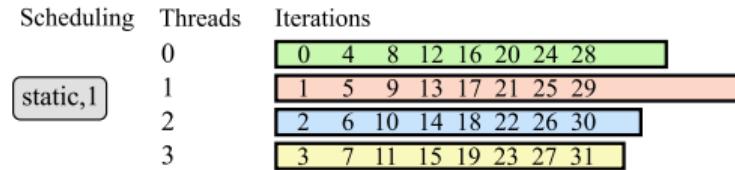
PADDING TO AVOID FALSE SHARING



LOOP SCHEDULING MODES IN OPENMP



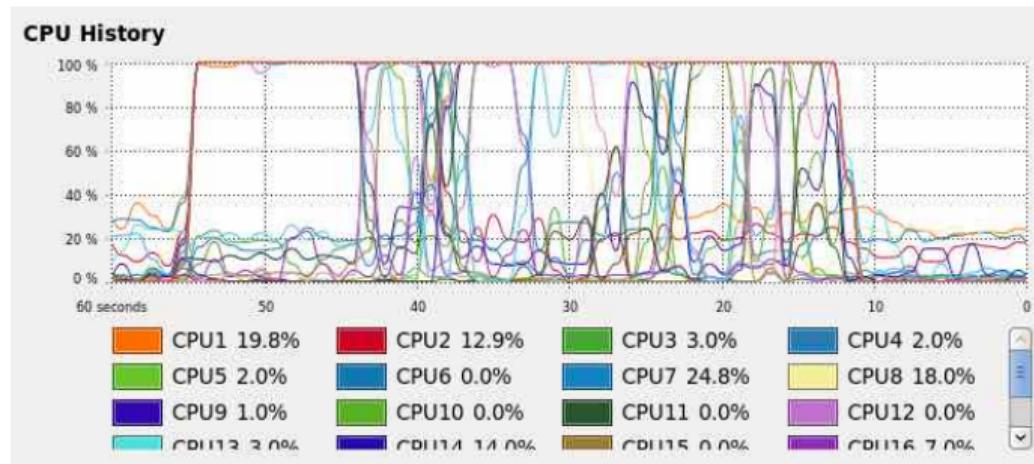
Time



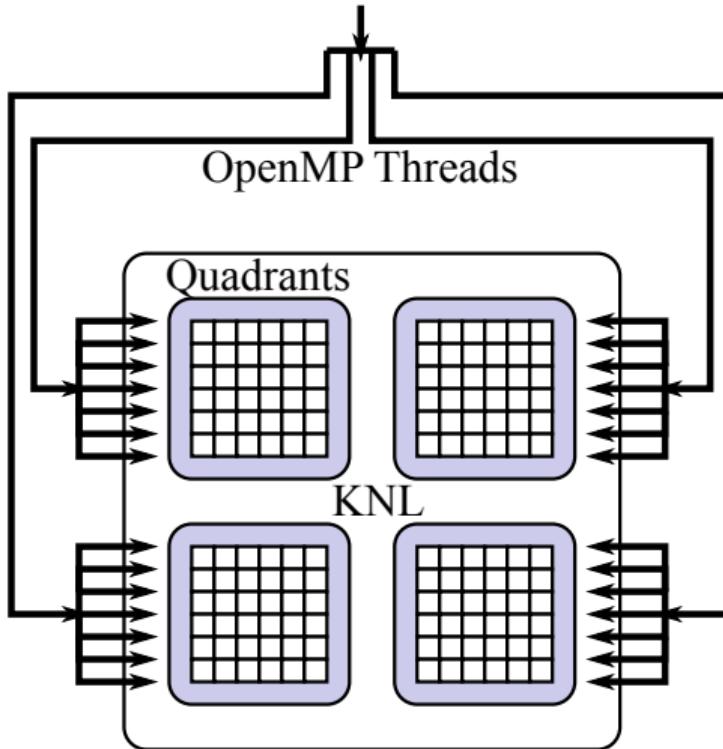
Time

WHAT IS THREAD AFFINITY

- ▶ OpenMP threads may migrate between cores
- ▶ Forbid migration — improve locality — increase performance
- ▶ Affinity patterns “scatter” and “compact” may improve cache sharing, relieve thread contention



NESTED PARALLELISM WITH OPENMP



```
1 #pragma omp parallel
2 {
3     #pragma omp parallel
4     {
5         // ...
6     }
7 }
```

- ▷ Tune granularity of parallelism
- ▷ Improve resource sharing in NUMA systems

CACHE AND MEMORY ACCESS

HOW CHEAP ARE FLOPS?

Theoretical estimates, Intel Xeon E5-2697 V3 processor

Performance = 28 cores \times 2.7 GHz \times (256/64) vec.lanes \times 2 FMA \times 2 FPU \approx 1.2 TFLOP/s

Required Data Rate = 1.2 TFLOP/s \times 8 bytes \approx 10 TB/s

Memory Bandwidth = $\eta \times 2 \times 59.7 \approx 0.1$ TB/s

Ratio = 10/0.1 \approx 100 (FLOPs)/(Memory Access)

If the Arithmetic Intensity is...

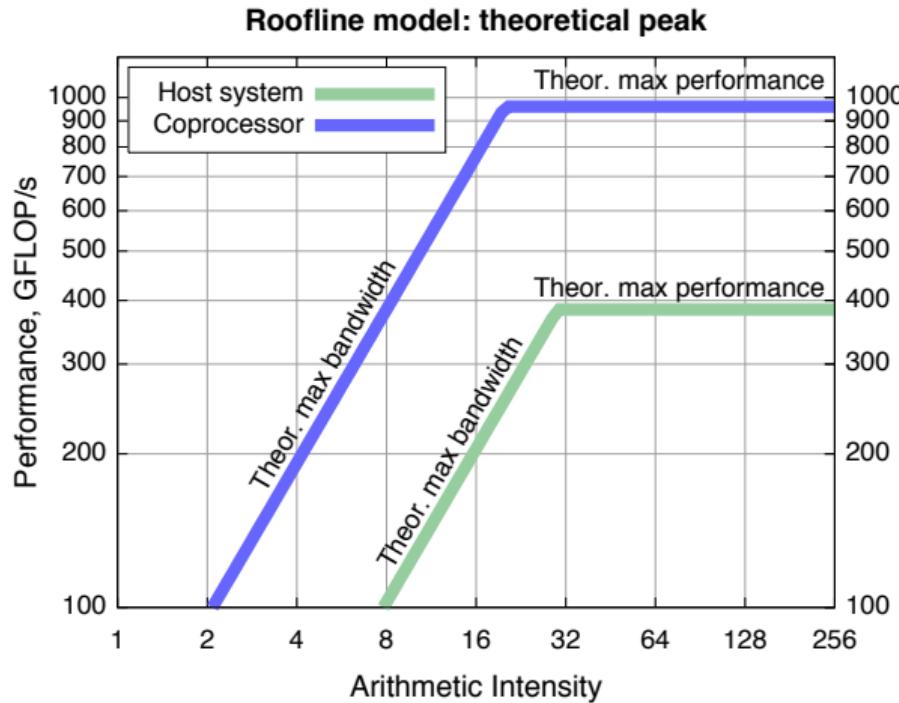
- ▶ > 100 (FLOPs)/(Memory Access) — Compute Bound Application
- ▶ < 100 (FLOPs)/(Memory Access) — Bandwidth Bound Application

ON COMPUTATIONAL COMPLEXITY OF ALGORITHMS

Type	Properties	Examples
$O(N)$	Each data element is used a fixed number of times. Memory-bound unless the number of times is large.	Array scaling, image brightness adjustment, vector dot-product.
$O(N^\alpha)$	Each element is used $N^{\alpha-1}$ times. A lot of data reuse for $\alpha > 1$. Good implementation can be compute-bound, poor one – memory-bound.	Matrix-matrix multiplication: $O(N^{3/2})$ (N = amount of data in matrix), direct N-body calculation: $O(N^2)$
$O(N \log N)$	Each element is used $\log N$ times. For small problems – memory-bound, for very large problems transitions to compute-bound	Fast Fourier transform, merge sort
$O(\log N)$	Always memory-bound.	Binary search

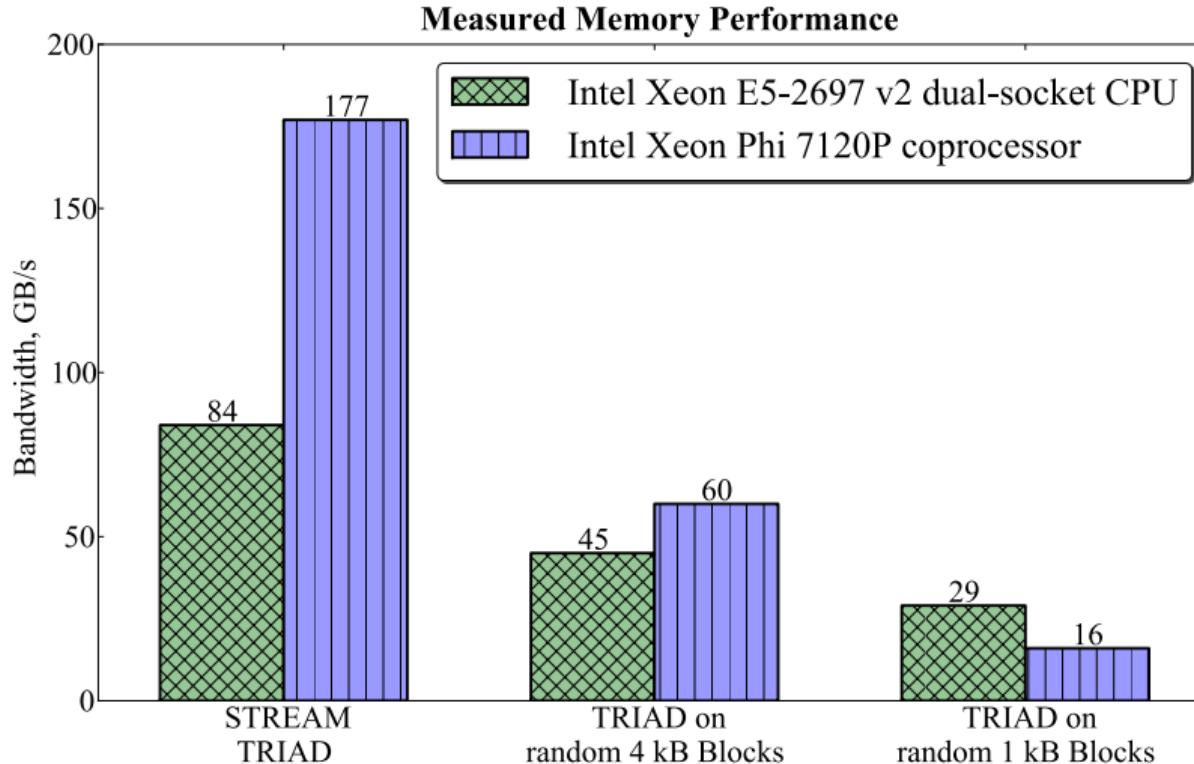
N = data size

ARITHMETIC INTENSITY AND ROOFLINE MODEL



More on roofline model: [Williams et al.](#)

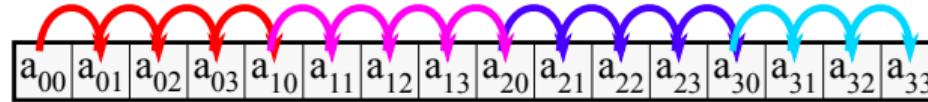
STREAMING VERSUS RANDOM ACCESS



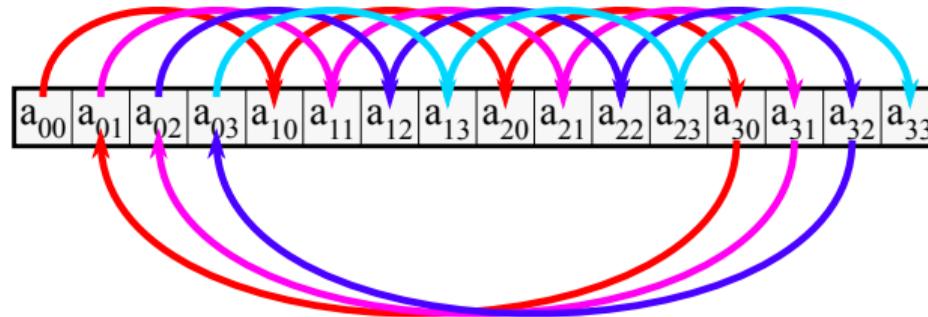
PRINCIPLE

Choose loop order to maintain unit-stride memory access

a ₀₀	a ₀₁	a ₀₂	a ₀₃
a ₁₀	a ₁₁	a ₁₂	a ₁₃
a ₂₀	a ₂₁	a ₂₂	a ₂₃
a ₃₀	a ₃₁	a ₃₂	a ₃₃



a ₀₀	a ₀₁	a ₀₂	a ₀₃
a ₁₀	a ₁₁	a ₁₂	a ₁₃
a ₂₀	a ₂₁	a ₂₂	a ₂₃
a ₃₀	a ₃₁	a ₃₂	a ₃₃



Compiler may or may not be able to automate loop permutation.

EXAMPLE: OVER-SIMPLIFIED MATRIX-MATRIX MULTIPLICATION

$$C = AB \Leftrightarrow C_{ij} = \sum_{k=0}^{n-1} A_{ik}B_{kj}$$

Before:

```

1 #pragma omp parallel for
2 for (int i = 0; i < n; i++)
3     for (int j = 0; j < n; j++)
4 #pragma vector aligned
5     for (int k = 0; k < n; k++)
6         C[i*n+j] += A[i*n+k]*B[k*n+j];

```

After:

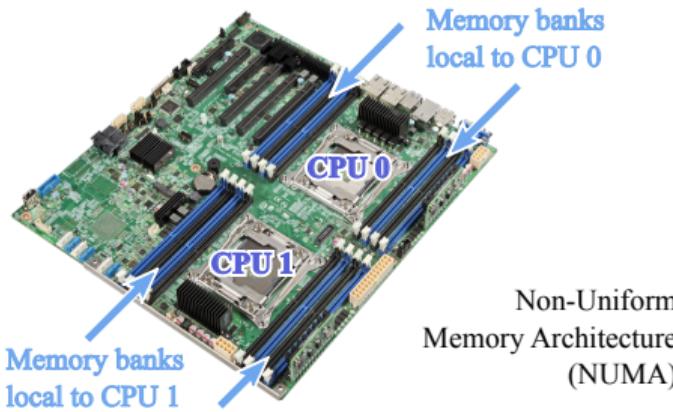
```

1 #pragma omp parallel for
2 for (int i = 0; i < n; i++)
3     for (int k = 0; k < n; k++)
4 #pragma vector aligned
5     for (int j = 0; j < n; j++)
6         C[i*n+j] += A[i*n+k]*B[k*n+j];

```

NUMA ARCHITECTURES

NUMA = Non-Uniform Memory Access. Cores have fast access to local memory, slow access to remote memory.



Examples:

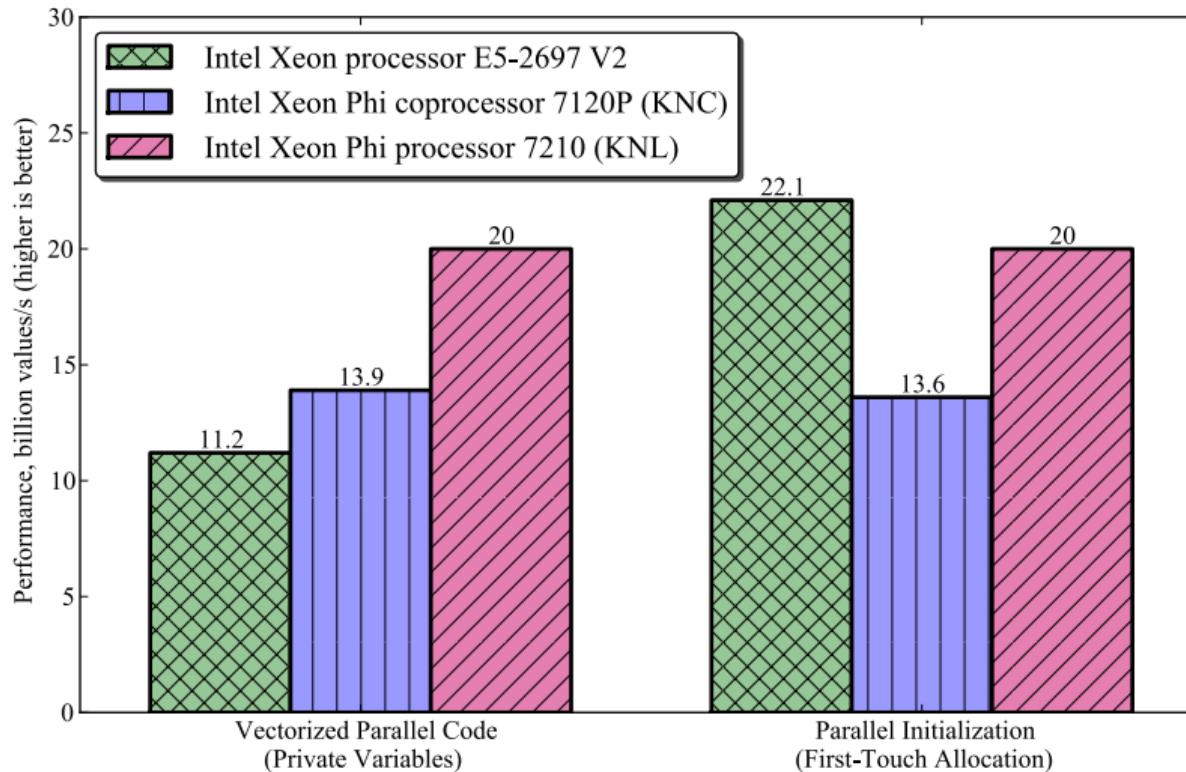
- ▷ Multi-socket Intel Xeon processors
- ▷ Second generation Intel Xeon Phi

ALLOCATION ON FIRST TOUCH

- ▷ Memory allocation occurs not during `_mm_malloc()`, but upon the first write to the buffer (“first touch”)
- ▷ Default NUMA allocation policy is “on first touch”
- ▷ For better performance in NUMA systems, initialize data with the same parallel pattern as during data usage

```
1 float* A = (float*)_mm_malloc(n*m*sizeof(float), 64);  
2  
3 // Initializing from parallel region for better performance  
4 #pragma omp parallel for  
5 for (int i = 0; i < n; i++)  
6     for (int j = 0; j < m; j++)  
7         A[i*m + j] = 0.0f;
```

FIRST-TOUCH ALLOCATION POLICY



- ▶ The order of nested loops must be chosen for best locality of data access
- ▶ At -O2 and above, the compiler automatically interchanges loops in some cases
- ▶ In other cases, loop interchange must be investigated manually

LOOP FUSION TECHNIQUE

Re-use data in cache by fusing loops in a data processing pipeline

```
1 MyDataType* data = new MyDataType(n);  
2  
3 for (int i = 0; i < n; i++)  
4     Initialize(data[i]);  
5  
6 for (int i = 0; i < n; i++)  
7     Stage1(data[i]);  
8  
9 for (int i = 0; i < n; i++)  
10    Stage2(data[i]);
```

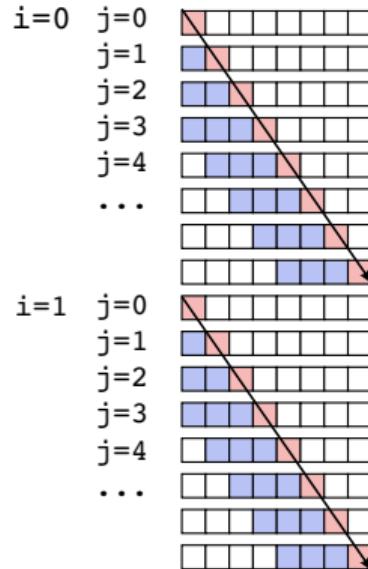
```
1 MyDataType* data = new MyDataType(n);  
2  
3 for (int i = 0; i < n; i++) {  
4  
5     Initialize(data[i]);  
6  
7     Stage1(data[i]);  
8  
9     Stage2(data[i]);  
10 }
```

Potential positive side-effect: less data to carry between stages, reduced memory footprint, improved performance (see, e.g., [this paper](#)).

LOOP TILING

Original:

```
for (i=0; i<m; i++)
    for (j=0; j<n; j++)
        ...=...*b[j];
```



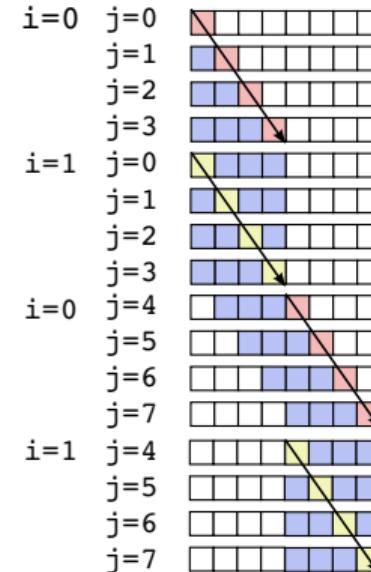
█ - cached, LRU eviction policy
█ - cache miss (read from memory, slow)
█ - cache hit (read from cache, fast)

Cache size: 4
 TILE=4
 (must be tuned to cache size)

Cache hit rate without tiling: 0%
 Cache hit rate with tiling: 50%

Tiled:

```
for (jj=0; jj<n; jj+=TILE)
    for (i=0; i<m; i++)
        for (j=jj; j<jj+TILE; j++)
            ...=...*b[j];
```



LOOP TILING (CACHE BLOCKING) -- PROCEDURE

```
1  for (int i = 0; i < m; i++) // Original code:  
2      for (int j = 0; j < n; j++)  
3          compute(a[i], b[j]); // Memory access is unit-stride in j
```

```
1  // Step 1: strip-mine inner loop  
2  for (int i = 0; i < m; i++)  
3      for (int jj = 0; jj < n; jj += TILE)  
4          for (int j = jj; j < jj + TILE; j++)  
5              compute(a[i], b[j]); // Same order of operation as original
```

```
1  // Step 2: permute  
2  for (int jj = 0; jj < n; jj += TILE)  
3      for (int i = 0; i < m; i++)  
4          for (int j = jj; j < jj + TILE; j++)  
5              compute(a[i], b[j]); // Re-use to j=jj sooner
```

EXAMPLE: MATRIX-VECTOR MULTIPLICATION

$$c_i = \sum_{j=0}^n A_{ij} b_j, \quad i = 0, 1, \dots, (m-1). \quad (2)$$

```
1 void Multiply(const double* const A, const double* const b,
2                 double* const c, const long n, const long m){
3     assert(n%64 == 0);
4     #pragma omp parallel for
5     for (long i = 0; i < m; i++)
6     #pragma vector aligned
7         for (long j = 0; j < n; j++) // Each value of A[i*n+j] is used only once
8             c[i] += A[i*n+j] * b[j]; // Each value of b[j] is used a total of m times
9 }
```

Non-optimal performance due to inefficient cache use

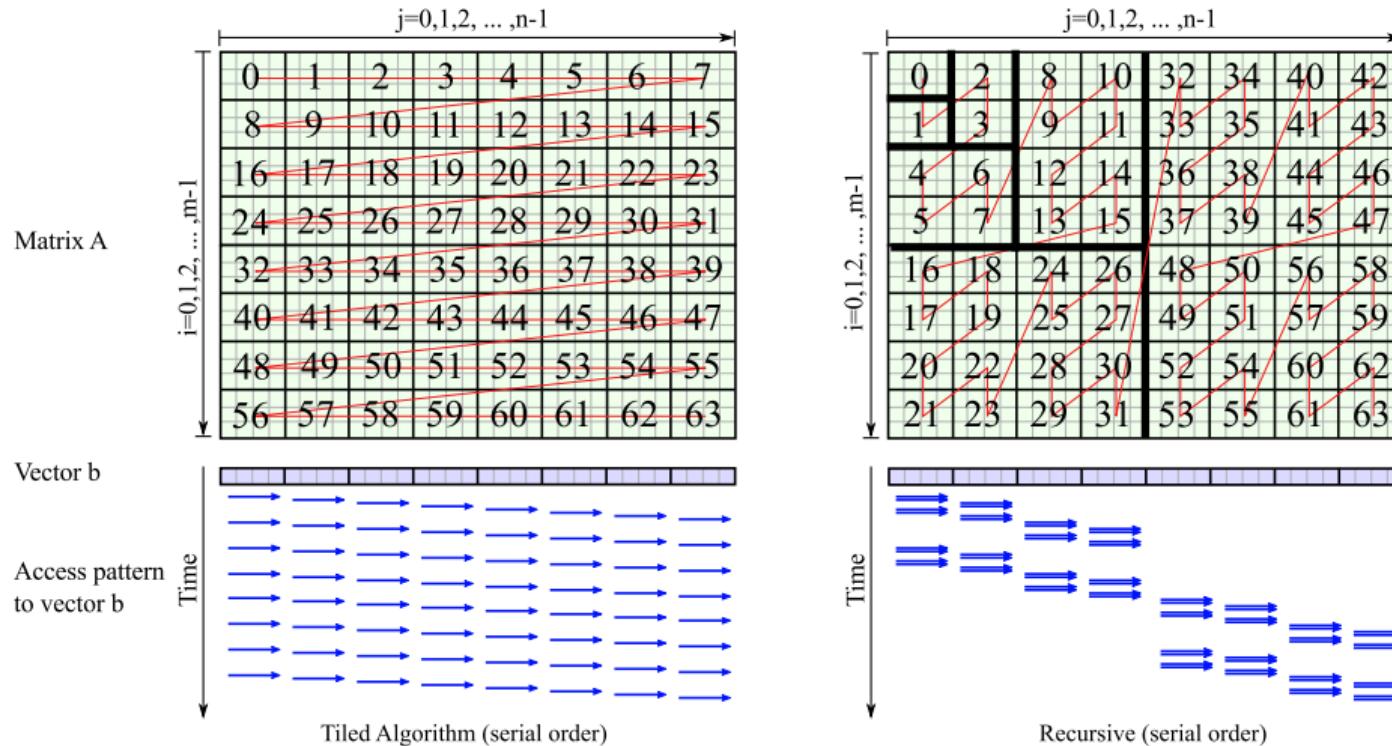
APPLYING TILING

```
1 const long jTile = 4096L; assert(n%jTile == 0);
2 #pragma omp parallel
3 {
4     double temp_c[m] __attribute__((aligned(64)));
5     temp_c[:] = 0;
6 #pragma omp for
7     for (long jj = 0; jj < n; jj+=jTile) // Loop Tiling in j
8         for (long i = 0; i < m; i++)
9 #pragma vector aligned
10        for (long j = jj; j < jj+jTile; j++)
11            temp_c[i] += A[i*n+j] * b[j];
12
13    for (long i = 0; i < m; i++) { // Reduction
14 #pragma omp atomic
15        c[i] += temp_c[i];
16    } } }
```

CACHE BLOCKING + STRIP-MINE AND COLLAPSE

```
1 const long iTile = 64L;    assert(m%iTile == 0);
2 const long jTile = 4096L; assert(n%jTile == 0);
3 #pragma omp parallel
4 {
5     double temp_c[m] __attribute__((aligned(64))); temp_c[:] =0;
6 #pragma omp for collapse(2)
7     for (long ii = 0; ii < m; ii += iTile)
8         for (long jj = 0; jj < n; jj += jTile)
9             for (long i = ii; i < ii+iTile; i++)
10 #pragma vector aligned
11     for (long j =jj; j < jj+jTile; j++)
12         temp_c[i] += A[i*n+j] * b[j];
13
14     for(long i = 0; i < m; i++) {
15 #pragma omp atomic
16         c[i] += temp_c[i];
17     } } }
```

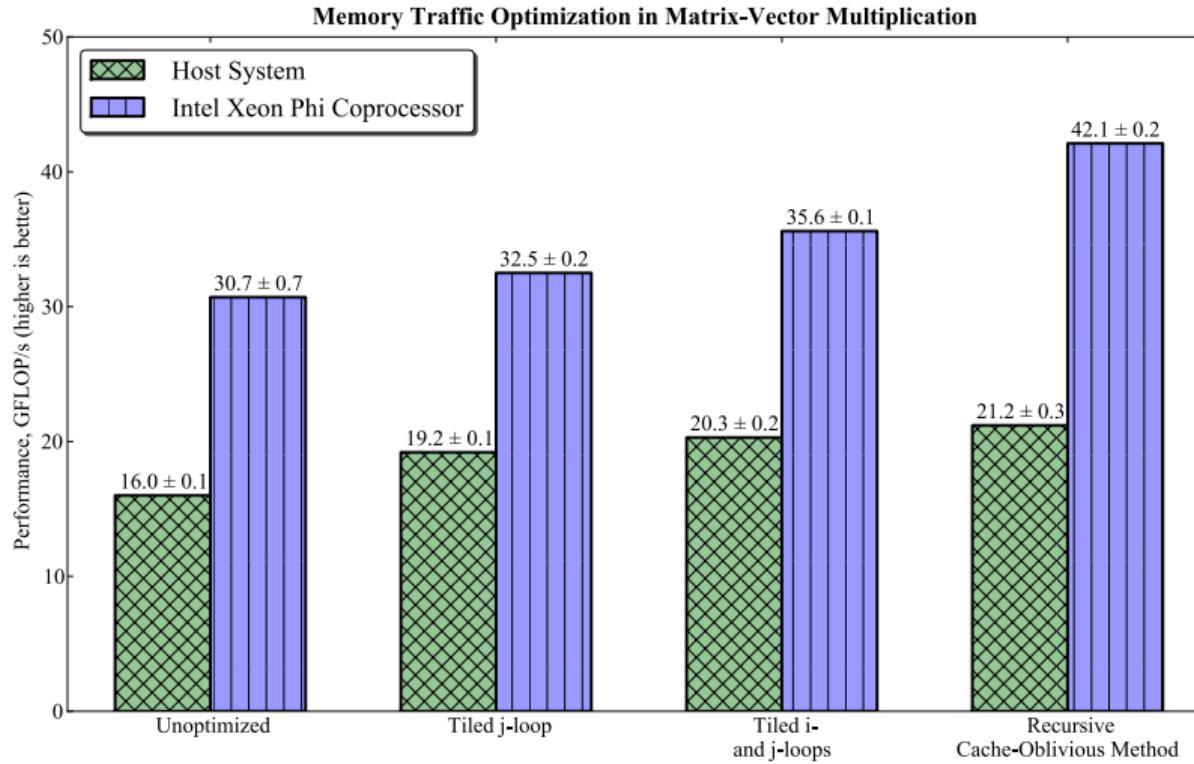
PRINCIPLE



EXAMPLE: MATRIX-VECTOR MULTIPLICATION

```
1 void RecursMultiply(const double* const A, const double* const b,
2                     double* const c, const long n, const long m, const long lda){
3     const long jThreshold = 8192L; assert(n%jThreshold == 0);
4     const long iThreshold = 64L;    assert(m%iThreshold == 0);
5     if ((m<=iThreshold) && (n<=jThreshold)) { // Recursion threshold
6         // .... Base Case: Compute the result inside the tile ... //
7     } else { // Recursive divide-and-conquer
8         if (m*jThreshold > n*iThreshold) { // Split i-wise
9             double c1[m/2] __attribute__((aligned(64)));
10            #pragma omp task
11                { RecursMultiply(&A[0*lda + 0], &b[0], c1, n, m/2, lda); }
12            double c2[m/2] __attribute__((aligned(64)));
13            RecursMultiply(&A[(m/2)*lda + 0], &b[m/2], c2, n, m/2, lda);
14            #pragma omp taskwait
15                c[0:m/2] += c1[0:m/2]; c[m/2:m/2] += c2[0:m/2]; // Reduction
16            } else { // .... Split j-wise .... // }
17        }
```

PERFORMANCE OF MATRIX VECTOR MULTIPLICATION



COMMUNICATION CONTROL

STRUCTURE OF MPI APPLICATIONS: HELLO WORLD

```
1 #include "mpi.h"
2 #include <stdio.h>
3 int main (int argc, char *argv[]) {
4     MPI_Init (&argc, &argv); // Initialize MPI environment
5     int rank, size, namelen;
6     char name[MPI_MAX_PROCESSOR_NAME];
7     MPI_Comm_rank (MPI_COMM_WORLD, &rank); // ID of current process
8     MPI_Get_processor_name (name, &namelen); // Hostname of node
9     MPI_Comm_size (MPI_COMM_WORLD, &size); // Number of processes
10    printf ("Hello World from rank %d running on %s!\n", rank, name);
11    if (rank == 0) printf("MPI World size = %d processes\n", size);
12    MPI_Finalize (); // Terminate MPI environment
13 }
```

HETEROGENEOUS MPI APPLICATIONS: MACHINE FILE

```
vega@lyra% cat hosts.txt
localhost:2
mic0:2
mic1:2
vega@lyra% export I_MPI_MIC_POSTFIX=.MIC
vega@lyra% mpirun -machinefile hosts.txt ~/Hello
Hello World from rank 0 running on localhost!
Hello World from rank 1 running on localhost!
Hello World from rank 2 running on mic1!
Hello World from rank 3 running on mic1!
Hello World from rank 4 running on mic0!
Hello World from rank 5 running on mic0!
MPI World size = 6 ranks
```

- ▷ Specify Xeon executable for host processes
- ▷ MIC executable obtained by appending I_MPI_MIC_POSTFIX

COMPILING AND RUNNING MPI APPLICATIONS

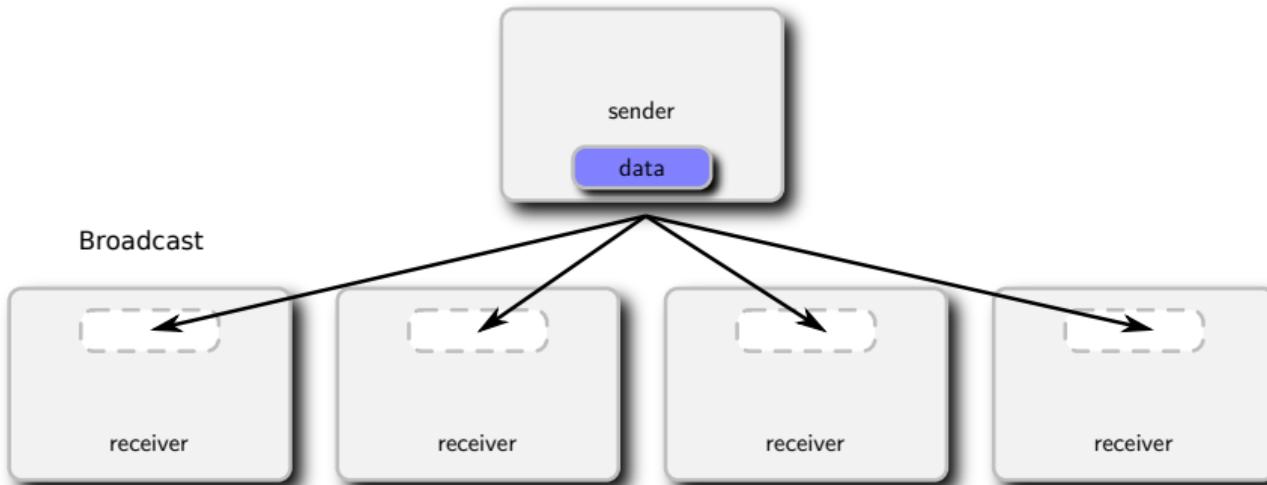
1. Compile and link with the MPI wrapper of the compiler:
 - `mpiicc` for C,
 - `mpiicpc` for C++,
 - `mpiifort` for Fortran 77 and Fortran 95.
2. Set up MPI environment variables *and* `I_MPI_MIC=1`
3. NFS-share or copy the MPI library and the application executable to the coprocessors
4. Launch with the tool `mpirun`
 - Colon-separated list of executables and hosts (argument `-host hostname`),
 - Alternatively, use the machine file to list hosts
 - Coprocessors have hostnames defined in `/etc/hosts`

POINT TO POINT COMMUNICATION

```
1 if (rank == sender) {  
2  
3     char outgoingMsg[messageLength];  
4     strcpy(outgoingMsg, "Hi There!");  
5     MPI_Send(&outgoingMsg, messageLength, MPI_CHAR, receiver, tag, MPI_COMM_WORLD);  
6  
7 } else if (rank == receiver) {  
8  
9     char incomingMsg[messageLength];  
10    MPI_Recv (&incomingMsg, messageLength, MPI_CHAR, sender,  
11                tag, MPI_COMM_WORLD, &stat);  
12    printf ("Received message with tag %d: '%s'\n", tag, incomingMsg);  
13  
14 }  
15  
16 }
```

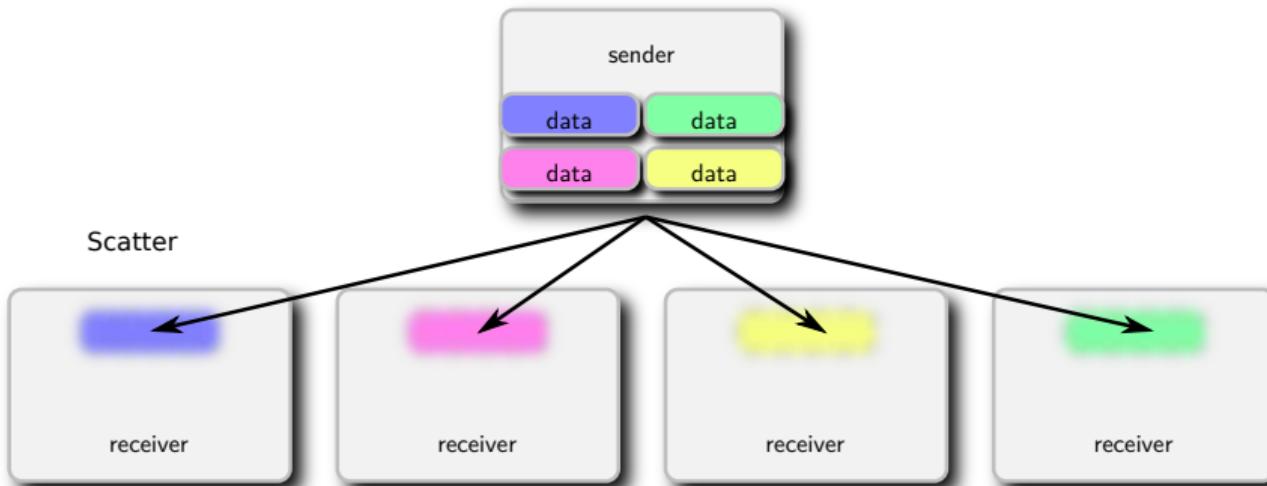
COLLECTIVE COMMUNICATION: BROADCAST

```
1 int MPI_Bcast( void *buffer, int count, MPI_Datatype datatype,
2                 int root, MPI_Comm comm );
```



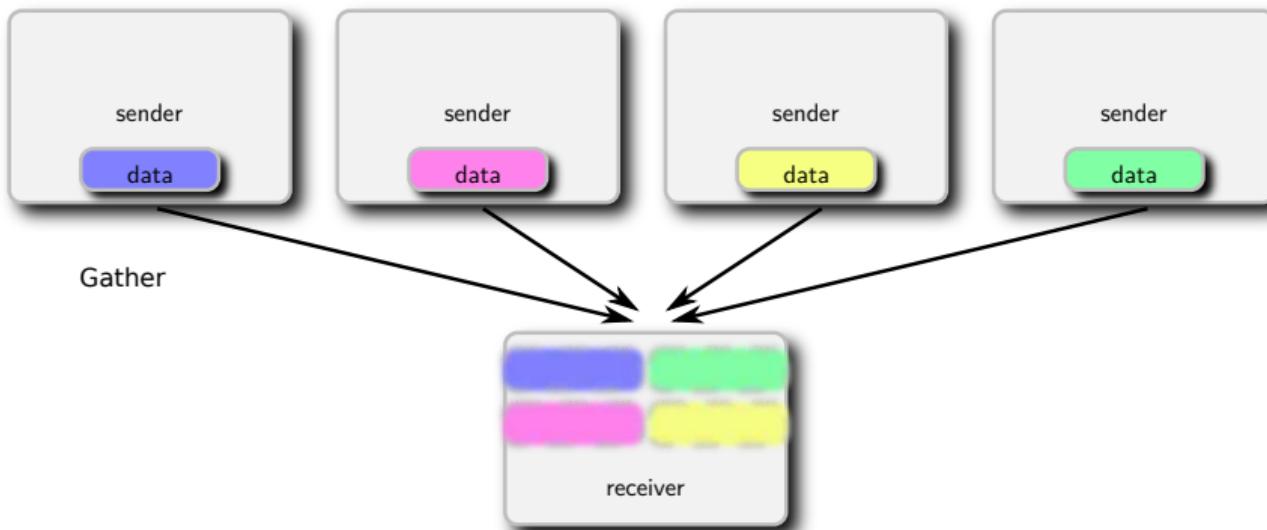
COLLECTIVE COMMUNICATION: SCATTER

```
1 int MPI_Scatter(void *sendbuf, int sendcnt, MPI_Datatype sendtype, void *recvbuf,  
2 int recvcnt, MPI_Datatype recvtype, int root, MPI_Comm comm);
```



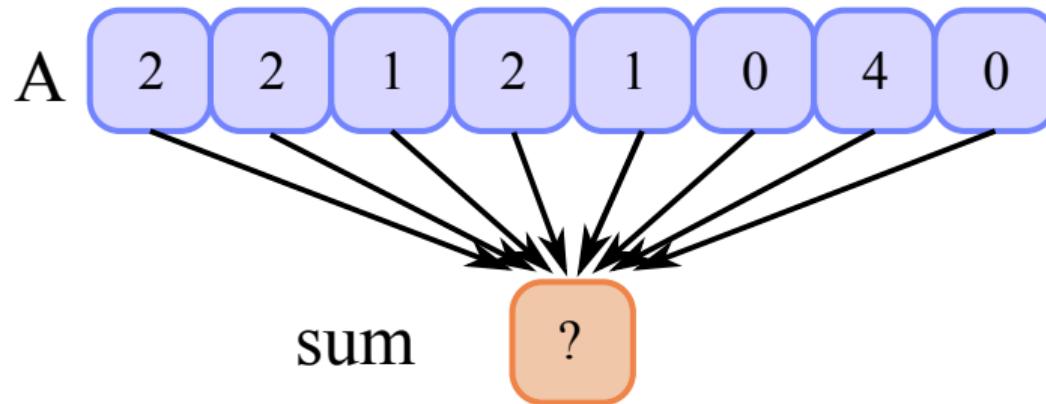
COLLECTIVE COMMUNICATION: GATHER

```
1 int MPI_Gather(void *sendbuf, int sendcnt, MPI_Datatype sendtype,  
2                 void *recvbuf, int recvcnt, MPI_Datatype recvtype, int root, MPI_Comm comm);
```



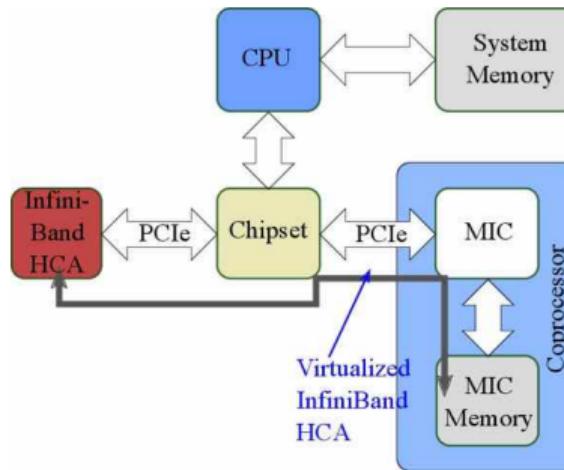
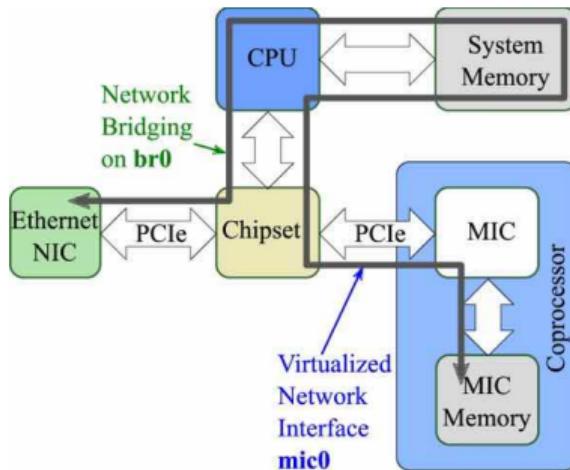
COLLECTIVE COMMUNICATION: REDUCTION

```
1 int MPI_Reduce(void *sendbuf, void *recvbuf, int count, MPI_Datatype datatype,
2 MPI_Op op, int root, MPI_Comm comm);
```



Available reducers: max/min, minloc/maxloc, sum, product, AND, OR, XOR (logical or bitwise).

PEER-TO-PEER COMMUNICATION BETWEEN COPROCESSORS

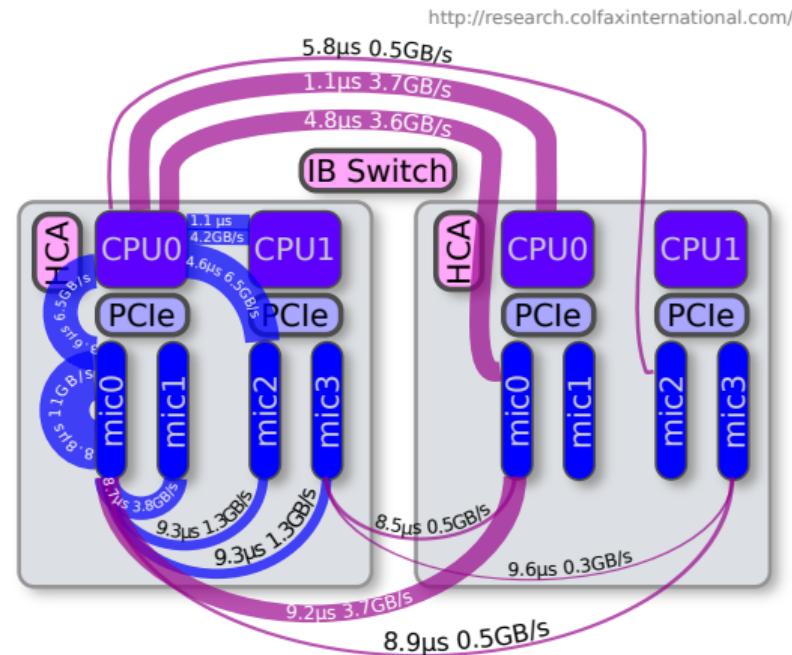


- ▶ Left: Gigabit Ethernet bridging on host allows to place coprocessors on the same subnet as hosts
- ▶ Right: Coprocessor Communication Link (CCL) – virtualization of an InfiniBand device on each coprocessor

MPI FABRIC SELECTION

- ▷ MPI communication between CPU and coprocessors as efficient as offload
- ▷ Peer-to-peer communication not uniform, but better than with Gigabit Ethernet
- ▷ Control: environment variable `I_MPI_FABRICS`

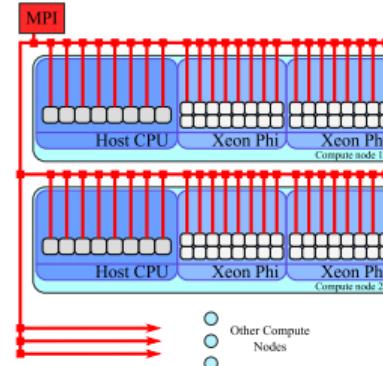
Our publication with details:
<http://xeonphi.com/papers/p2p>



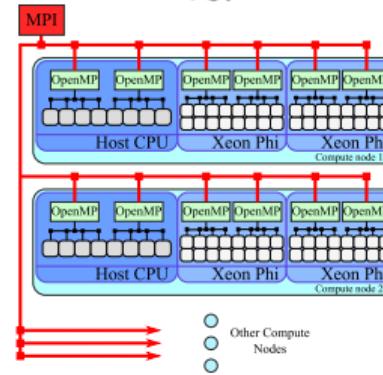
HYBRID MPI+OPENMP

Using OpenMP inside of MPI processes:

- ▷ Reduces the memory footprint
- ▷ Decreases the number of MPI ranks, which reduces communication
- ▷ May incur thread synchronization overhead
- ▷ Optimal number of threads in MPI processes must be established empirically



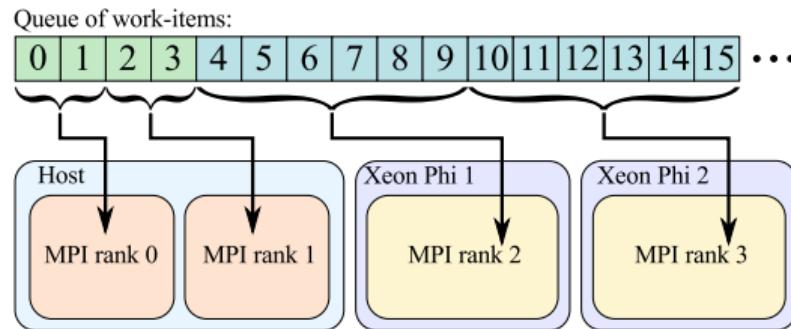
VS.



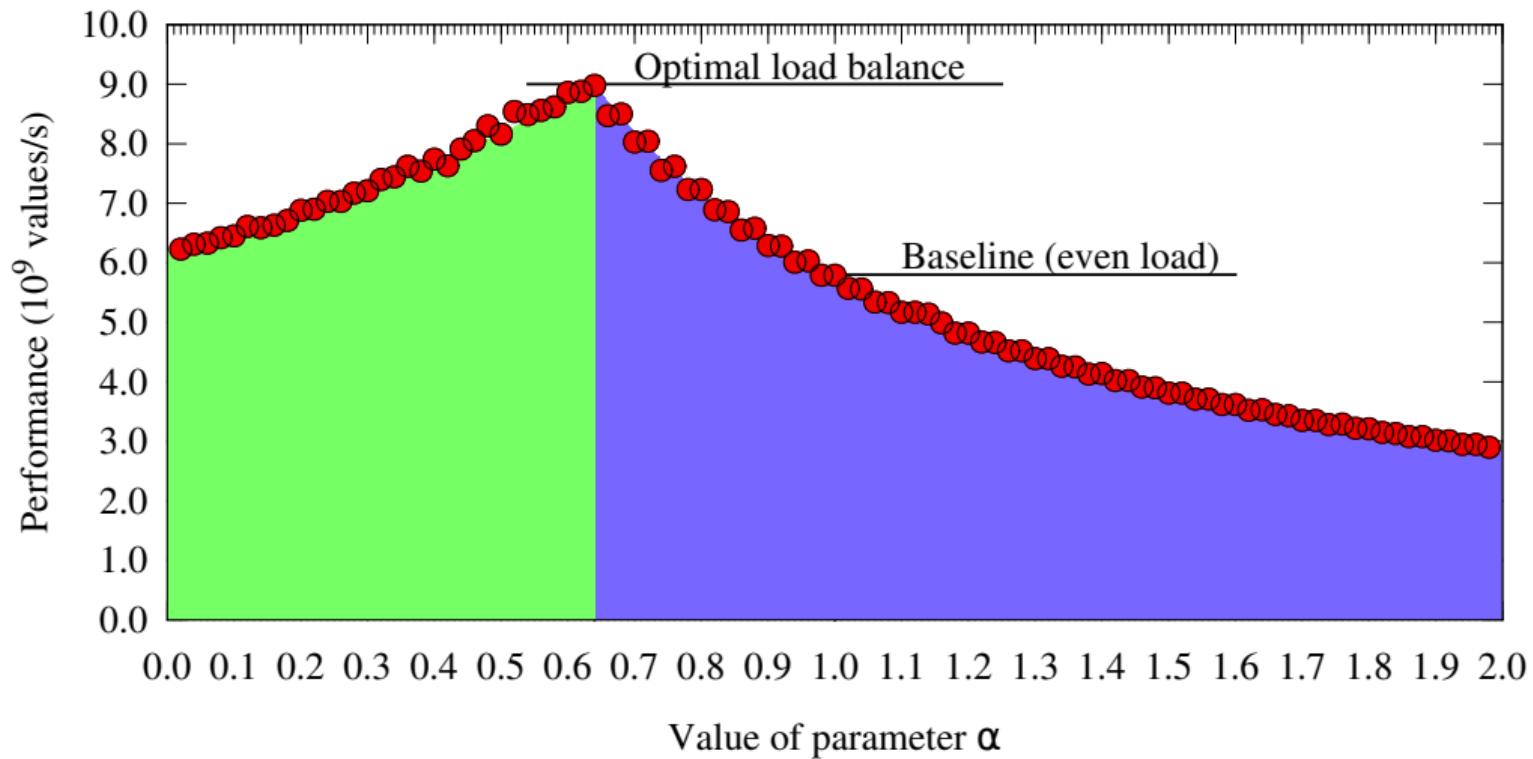
STATIC LOAD BALANCING

```

1 if (rankTypes[myRank] == 0) { // I am a MIC-based rank
2     double optionsPerProc = double(lastOptForCPUs)/double(cpuRanks.size());
3     myFirstOpt = int(optionsPerProc*(myGroupRank));
4     myLastOpt = int(optionsPerProc*(myGroupRank+1.0));
5 } else { // I am a CPU-based rank
6     double optionsPerProc = double(nOpts-lastOptForCPUs)/double(micRanks.size());
7     myFirstOpt=lastOptForCPUs+int(optionsPerProc*(myGroupRank));
8     myLastOpt=lastOptForCPUs+int(optionsPerProc*(myGroupRank+1.0)); }
```



STATIC LOAD BALANCING: PARAMETER TUNING

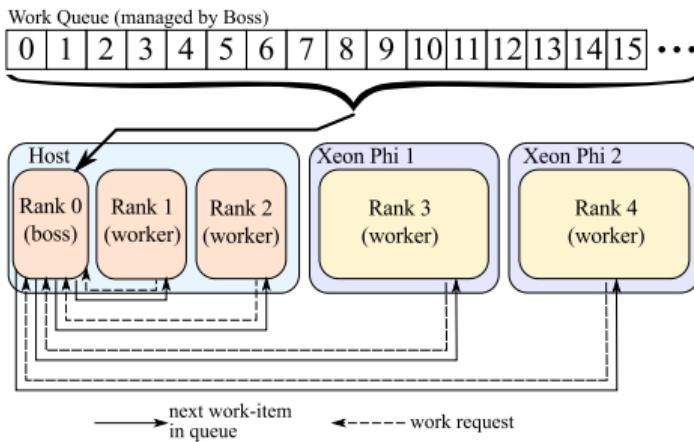


DYNAMIC LOAD BALANCING

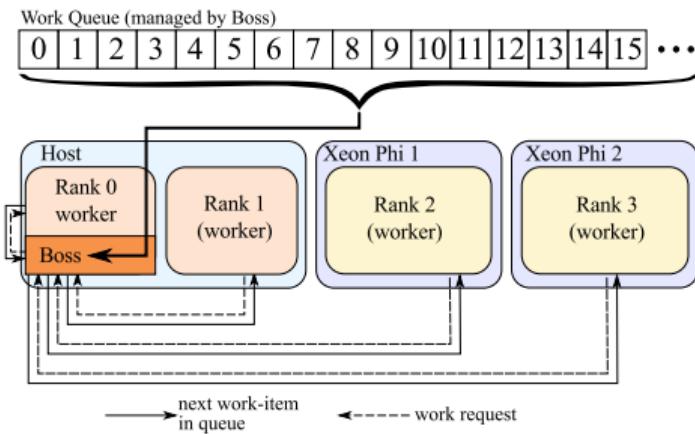
```

1   if (myRank == 0) // Boss's branch
2       DistributeWork(nOptions, option, mpiWorldSize);
3   else // Workers' branch
4       ReceiveWork(option, payoff, myRank);

```



or

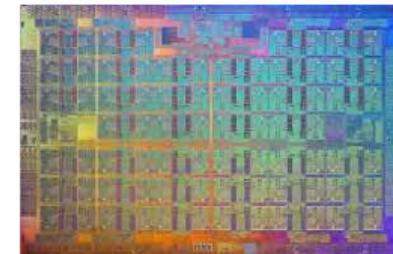


§4. PREPARING FOR INTEL XEON PHI PROCESSORS

INTEL XEON PHI PROCESSORS (2ND GEN)

Specialized platform for demanding computing applications.

- ▷ Socket version or coprocessor
- ▷ 64-72 cores × 4 HT at 1.3-1.5 GHz
- ▷ 3+ TFLOP/s in DP (FMA)
- ▷ 6+ TFLOP/s in SP (FMA)
- ▷ ≤ 384 GiB DDR4 (> 90 GB/s)
- ▷ 16 GiB HBM (MCDRAM, > 400 GB/s)
- ▷ Binary-compatible with Xeon
- ▷ Common OS
(RHEL/CentOS/SUSE/Windows)



BOOTABLE INTEL XEON PHI PROCESSORS

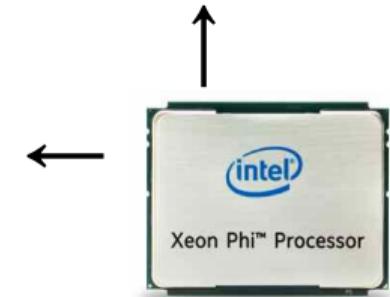
- ▷ Bootable Host Processor
- ▷ RHEL/CentOS/SUSE/Win
- ▷ 64 cores × 4 HT, 1.3 GHz
- ▷ ≤ 384 GiB DDR4, > 90 GB/s
- ▷ 16 GiB HBM, > 400 GB/s
- ▷ PCIe bus for networking

dap.xeonphi.com

Servers:



Workstations:



GET READY FOR INTEL® XEON PHI PROCESSORS (CODENAMED: KNIGHTS LANDING)

GET READY FOR KNL*

3

papers

AVX-512 | CLUSTERING MODES | MCDRAM

* Colfax series of webinars, training and white papers

colfaxresearch.com/knl-ready

HOW SERIES "KNIGHTS LANDING":

PROGRAMMING AND OPTIMIZATION FOR
INTEL XEON PHI X200 FAMILY

Free 2-hour video course

colfaxresearch.com/how-knl

COMPILING WITH AVX-512

AVX-512 FEATURES

- ▷ AVX-512F (Fundamentals)
 - Extension of most AVX2 instructions to 512-bit vector registers.
- ▷ AVX-512CD (Conflict Detection)
 - Efficient conflict detection (application: binning).
- ▷ AVX-512ER (Exponential and Reciprocal)
 - Transcendental function (exp, rcp and rsqrt) support.
- ▷ AVX-512PF (Prefetch)
 - Prefetch for scatter and gather.

Learn more: colfaxresearch.com/avx-512

INTEL COMPILER SUPPORT FOR AVX-512

Intel C, C++ and Fortran compilers ≥ 15.0 support AVX-512

```
user@kn1% icc -v
icc version 16.0.1 (gcc version 4.8.5 compatibility)
user@kn1% icc -help
// ... truncated output ... //
-x<code>
...
MIC-AVX512
CORE-AVX512
COMMON-AVX512
```

- ▷ **-xMIC-AVX512** : for KNL (supports F, CD, ER, PF)
- ▷ **-xCORE-AVX512** : for future Xeon (supports F, CD, DQ, BW, VL)
- ▷ **-xCOMMON-AVX512** : common to KNL and Xeon (supports F, CD)

GCC SUPPORT FOR AVX-512

GCC \geq 4.9.1 supports AVX-512 instruction set.

```
1 for(int i = 0; i < n; i++)
2     B[i] = A[i] + B[i];
```

Basic automatic vectorization support: add -m flags and -O3:

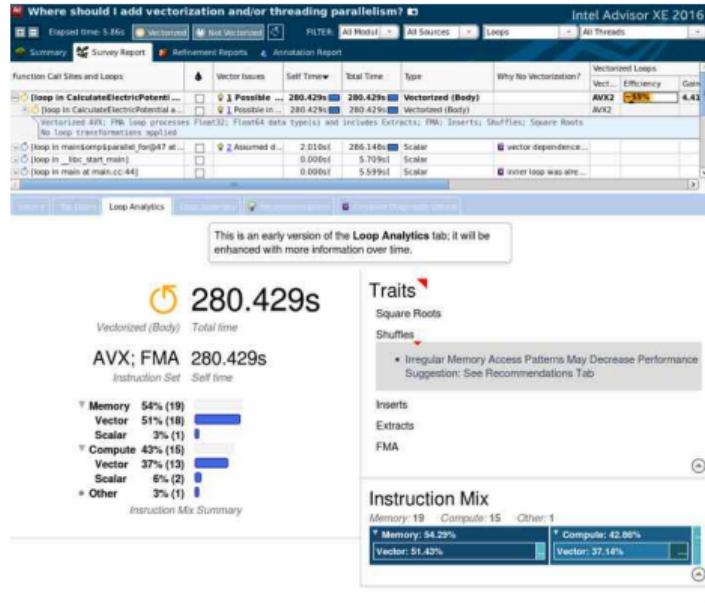
```
user@kn1% g++ -v
gcc version 4.9.2 (GCC)
user@kn1% g++ foo.cc -mavx512f -mavx512er -mavx512cd -mavx512pf -O3
```

Get assembly:

```
user@kn1% g++ -s foo.cc -mavx512f -O3
user@kn1% cat foo.s
...
vmovapd -16432(%rbp,%rax), %zmm0
vaddpd -8240(%rbp,%rax), %zmm0, %zmm0
vmovapd %zmm0, -8240(%rbp,%rax)
```

PERFORMANCE CONSIDERATIONS

Even if your code is vectorized, tuning may unlock more performance.



[download paper](#) to learn more

► Providing enough parallelism.

- More consecutive vector operations required to overcome vectorization latency.

► Loop pipelining and unrolling.

- Double the pipeline stages to populate.

► Better vectorization patterns.

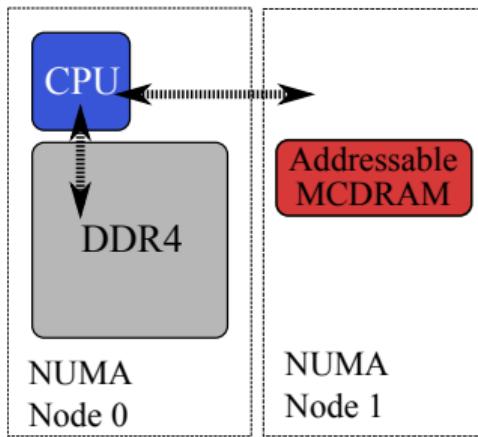
- Avoid long latency operations with unit-stride and unmasked operations.

USING HIGH-BANDWIDTH MEMORY

MODES OF HBM OPERATION

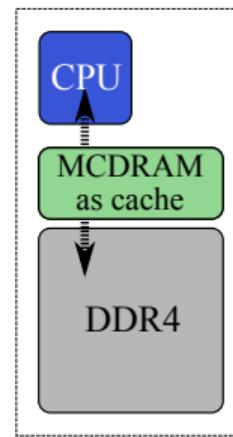
Flat Mode

- ▷ MCDRAM treated as a NUMA node
- ▷ Users control what goes to MCDRAM



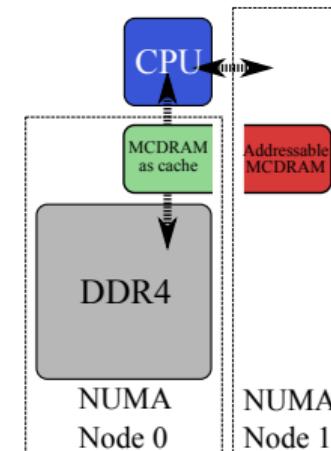
Cache Mode

- ▷ MCDRAM treated as a Last Level Cache (LLC)
- ▷ MCDRAM is used automatically

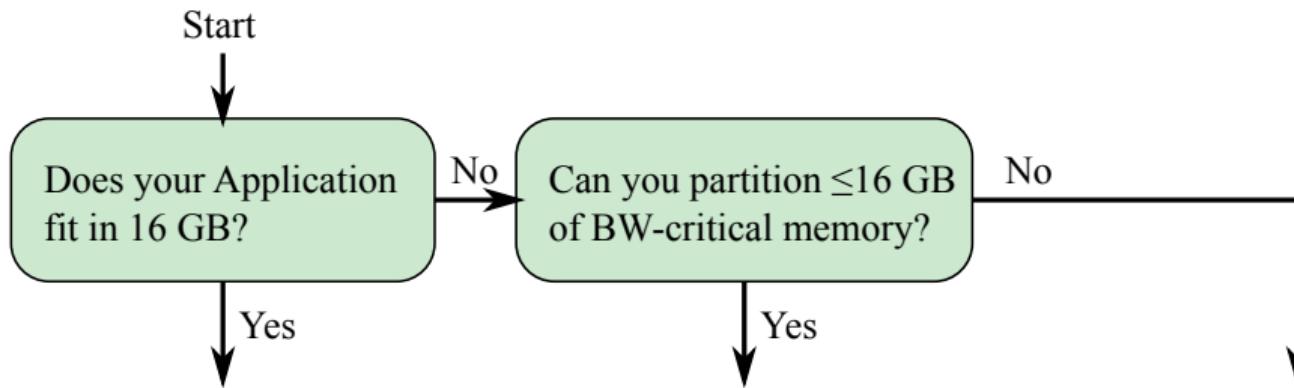


Hybrid Mode

- ▷ Combination of Flat and Cache
- ▷ Ratio can be chosen in the BIOS



FLOW CHART FOR BANDWIDTH-BOUND APPLICATIONS



numactl	Memkind	Cache mode
<ul style="list-style-type: none"> ▷ Run the whole program in HBM ▷ No code modification 	<ul style="list-style-type: none"> ▷ Selectively allocate data to HBM ▷ Add memkind calls 	<ul style="list-style-type: none"> ▷ Allow the chip to figure out how to use HBM ▷ No code modification

RUNNING APPLICATIONS IN HBM WITH NUMACTL

- ▶ Finding information about the NUMA nodes in the system.

```
user@kn1% # In Flat mode of MCDRAM
user@kn1% numactl -H
available: 2 nodes (0-1)
node 0 cpus: 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 ... 254 255
node 0 size: 98207 MB
node 0 free: 94798 MB
node 1 cpus:
node 1 size: 16384 MB
node 1 free: 15991 MB
```

- ▶ Binding the application to HBM (Flat/Hybrid)

```
user@kn1% gcc myapp.c -o runme -mavx512f -O2
user@kn1% numactl --membind 1 ./runme
// ... Application running in HBM ... //
```

ALLOCATION IN HBM WITH MEMKIND LIBRARY

Manual allocation to HBM possible with hbwmalloc and Memkind Library.

```
1 #include <hbwmalloc.h>
2
3 // Basic allocation in HBM
4 double* A = (double*) hbw_malloc(sizeof(double)*n);
5
6 // Allocation with alignment
7 double* B;
8 int ret = hbw_posix_memalign((void**) &B, 64, sizeof(double)*n);
9
10 hbw_free(A); hbw_free(b); // Special deallocator
```

In Fortran:

```
1 REAL, ALLOCATABLE :: A(:)
2 !DEC$ ATTRIBUTES FASTMEM :: A
3 ALLOCATE (A(1:N))
```

COMPILATION WITH MEMKIND LIBRARY AND HBWMALLOC

To compile C/C++ applications:

```
user@kn1% icpc -lmemkind foo.cc -o runme  
user@kn1% g++ -lmemkind foo.cc -o runme
```

To compile Fortran applications:

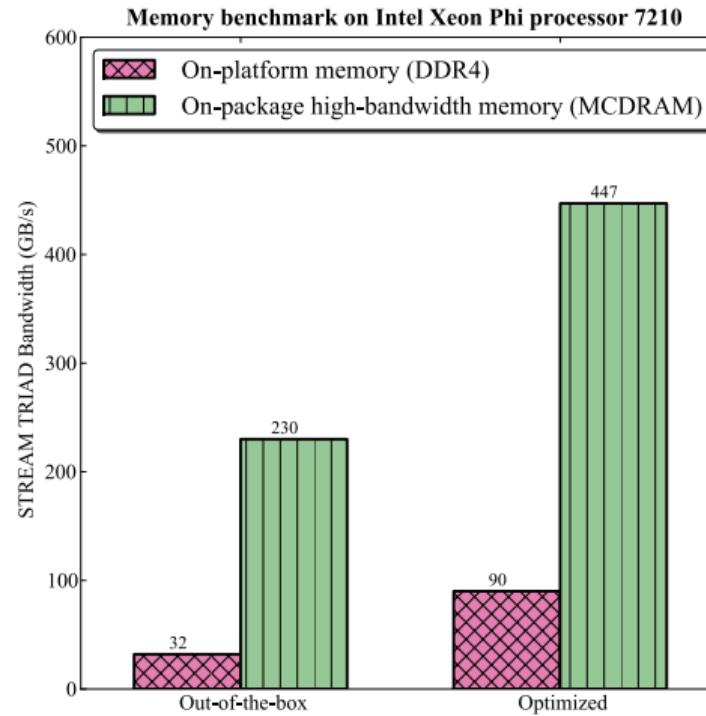
```
user@kn1% ifort -lmemkind foo.f90 -o runme  
user@kn1% gfortran -lmemkind foo.f90 -o runme
```

Open source distribution of Memkind library can be found at:
memkind.github.io/memkind

Learn more:
colfaxresearch.com/knl-mcdram

STREAM BENCHMARK

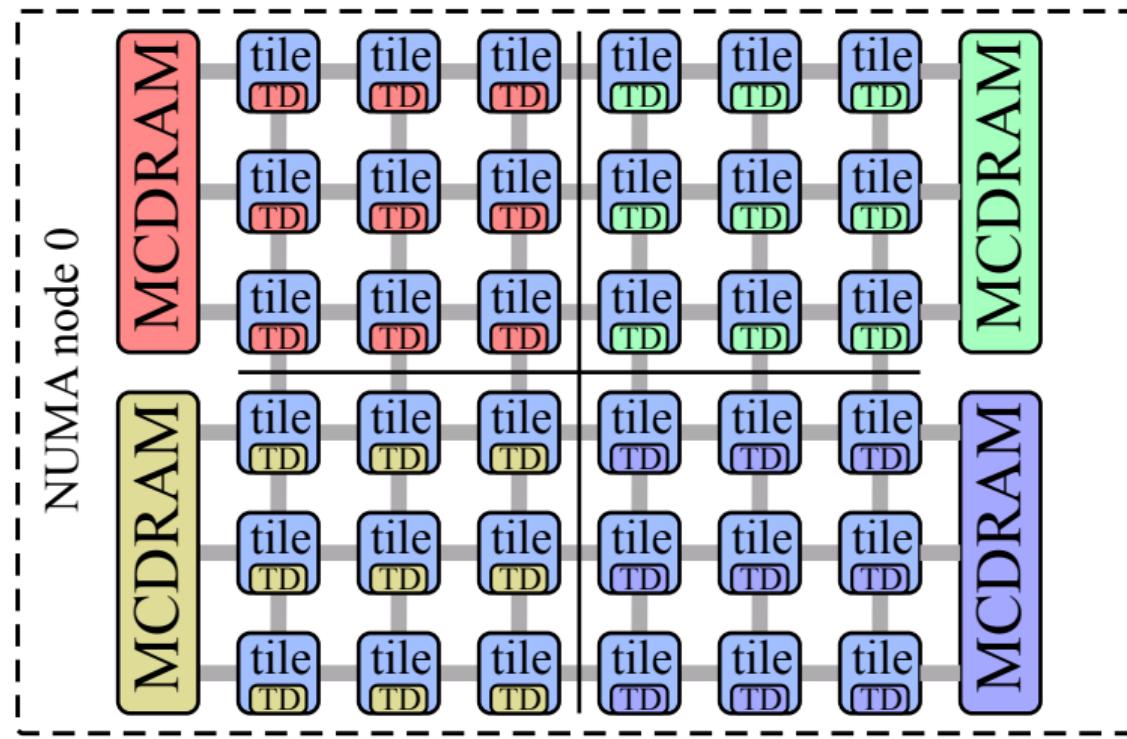
- ▷ Industry-standard tool for memory bandwidth measurement
- ▷ 4 tests: COPY, ADD, SCALE and TRIAD
- ▷ Download from Dr. John McCalpin's site:
www.cs.virginia.edu/stream/



LEVERAGING CLUSTERING MODES

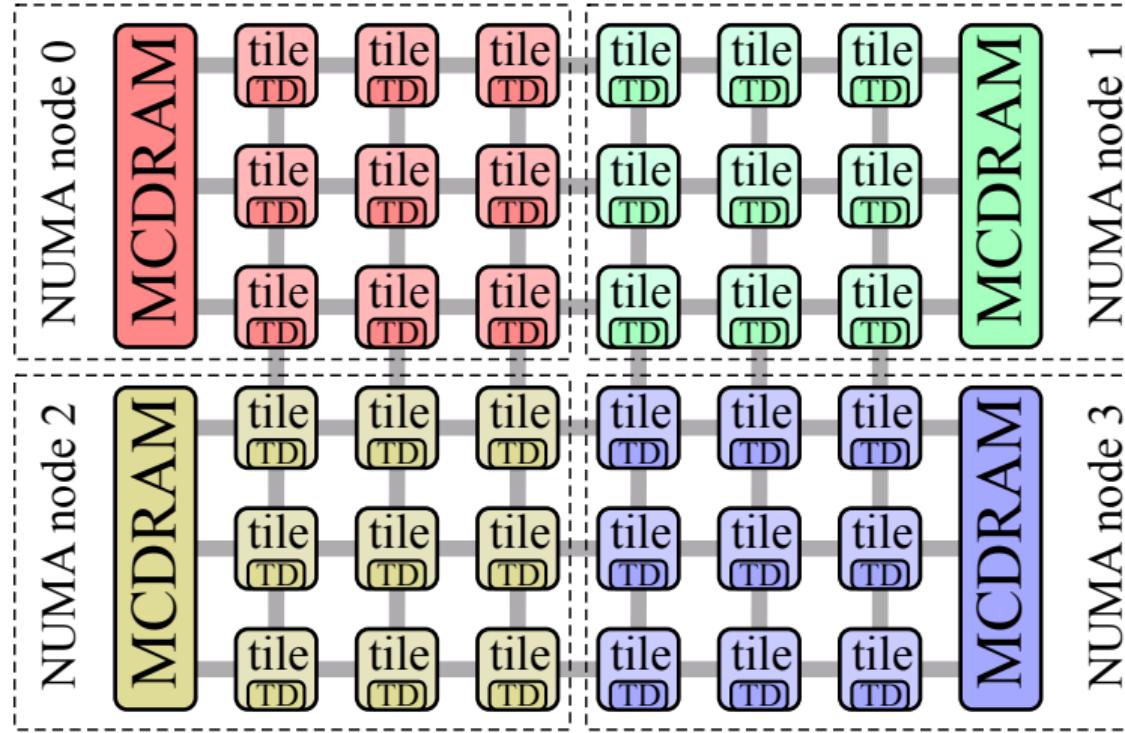
CLUSTERING MODES: QUADRANT/HEMISPHERE

Tag Directory (TD) and memory reside in the same quadrant.



CLUSTERING MODES: SNC-4/SNC-2

Cores appear as 4 (or 2) NUMA nodes.

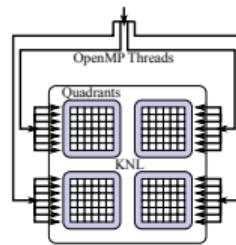


HOW TO USE CLUSTERING MODES

Nested OpenMP

```

1 #pragma omp parallel
2 {
3     // ...
4     #pragma omp parallel
5     {
6         // ...
7     }
8 }
```



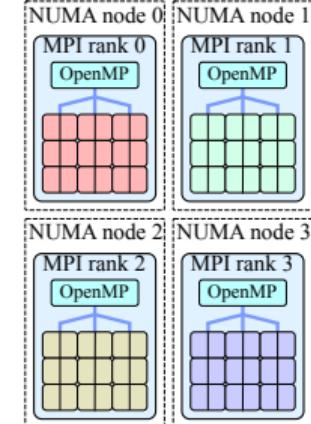
```

user@knl% OMP_NUM_THREADS=4,72
user@knl% OMP_NESTED=1
```

MPI+OpenMP

```

1 stat = MPI_Init();
2 // ...
3 #pragma omp parallel
4 {
5     // ...
6 }
7 // ...
8 MPI_Finalize();
```



```

user@knl% mpirun -host knl \
> -np 4 ./myparallel_app
```

Learn more: colfaxresearch.com/knl-numa

COPROCESSOR AND KNL-F

FUTURE FORM-FACTORS

KNLF: KNL with Fabric

- ▷ Fabric integrated on CPU
 - Intel® Omni-Path Architecture
- ▷ Socket mount processor



*KNC image



KNL Coprocessor

- ▷ PCIe add-in card
 - Requires host
- ▷ Multiple KNLs in a system