"Results! Why, man, I have gotten a lot of results! I know several thousand things that won't work."

-- Thomas Edison

1. Brace matching or parentheses matching, is a syntax highlighting feature of certain text editors and IDEs that highlights matching sets of braces in languages, such as Java and C++ that uses them.

Brace matching is one of the applications of *stack* data structure. Make use of the template Stack class (that you have already created) to create a *parentheses matcher*. Accept expressions of the form:

```
(14+(20 * 31)/42)
1+2
()
2+3*(2^3) etc.
```

Accept expressions contains positive integers separated by white spaces and the operators +, -, \*, ^ and /. Presence of any other characters should be reported as *parse error*.

Create a *template* Token and Tokenizer classes to tokenize the input expressions. The Tokenizer class should have a function by the name get\_token() that returns the *next token* from the input stream. The type of tokens returned should be:

```
enum Token_Type {
                 /* End of Line.
     EOL,
                 /* Value.
     VALUE,
     LPAREN,
                /* Left parenthesis.
     RPAREN,
                /* Right parenthesis.
                 /* Addition
     PLUS,
                /* Subtraction.
     MINUS,
                /* Division.
     DIV,
                /* Multiplication.
                                         * /
     MULT,
                                         * /
     EXP,
                /* Exponentiation.
                /* Unknown token.
     UNKNOWN
};
```

The Token template class should be designed as follows:

## Data members:

Name of data type	Description	
Token_Type token_type;	For storing the type of the token (LPAREN, RPAREN, PLUS, etc.)	
Typename token_value;	The value of the token.	
	In our case, only the VALUE token possesses value. VALUE token represents integer numbers. For example, the input 10 is represented by a combination of (VALUE, 10).	
	Other tokens like left-parenthesis, plus, minus, etc. do not have a value. The token alone is required for them.	

### Constructors:

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Constructor	Description	
Token(Token_Type tt = EOL, const T& val = 0);	Default constructor.	

## Member functions:

Function name	Description
Token_Type get_type()const ;	To get the type of token.
<pre>const T&amp; get_value()const ;</pre>	To get the value of token.

The Tokenizer template class should be designed as follows:

## Data members:

Name of data type	Description
std::istream& in;	The input stream to which the Tokenizer is connected to.

#### Constructors:

Constructor	Description
Tokenizer(std::istream& is);	Default constructor.

## Member functions:

Function name	Description
Token <t> get_token();</t>	To get the next token.
<pre>void clear();</pre>	To clear the input stream connected to the tokenizer.

# Sample run of program:

```
Enter expression: (
Unbalanced left parenthesis
Enter expression: )
Unbalanced right parenthesis
Enter expression: ()
Equal number of LPAREN & RPAREN
Enter expression: 1
Equal number of LPAREN & RPAREN
Enter expression: 1+2
Equal number of LPAREN & RPAREN
Enter expression: (1+2)*
Equal number of LPAREN & RPAREN
Enter expression: (1)+(2+3)
Unbalanced right parenthesis
Enter expression: ((1)+(2+3)
Unbalanced left parenthesis
Enter expression: $
Parse Error
Enter expression: 1/2<sup>4</sup>
Equal number of LPAREN & RPAREN
```

- 2. Modify the main program to accept *real numbers* instead of *integer* numbers alone. For example, (1.2 + 2.3) /1.0 etc. Do you have to make changes to the Tokenizer or Token classes?
- 3. Write a program to evaluate *postfix* expressions (*Reverse Polish notations*). Make use of the Tokenizer and the Stack template classes that you have already made. Use *white spaces* to separate the individual elements of the expression. The expression can contain real numbers and not just integers alone.

## Sample run of the program:

```
1 2 +
3
1.2 2.3 +
3.5
1
```

```
1 + 2

Error

*

Error

$

Parse error

1 2 + 3 4 * /

0.25

1 2 * *

Error
```