



# Spatial acquisition, digital archiving, and interactive auralization of church acoustics

*IWAENC 2022, Bamberg, Germany, Sept. 2022*

Toon van Waterschoot

**STADIUS** Center for Dynamical Systems, Signal  
Processing, and Data Analytics  
**ESAT** – Department of Electrical Engineering  
KU Leuven, Belgium



# Context & Motivation



Ghent Altarpiece (J. & H. van Eyck, 1432)

Flemish primitives

KU LEUVEN

# Context & Motivation

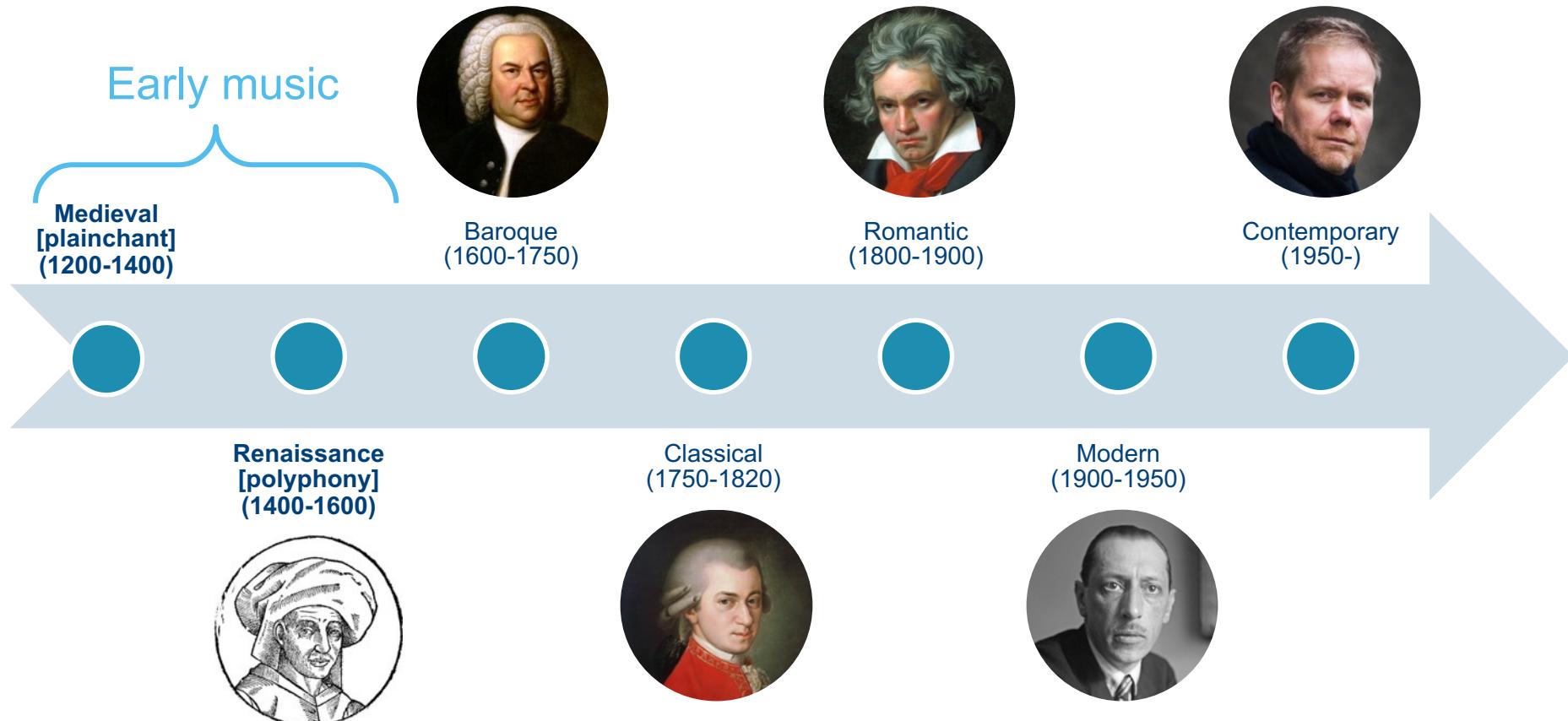


Nymphes des bois (J. des Prez, 1497, performed by Capella Pratensis)

**Franco-Flemish polyphony**

**KU LEUVEN**

# Context & Motivation



A concise timeline of Western music

# Context & Motivation

## Early Music Research

### Source



### Performer



### Environment



# Context & Motivation

- **Research questions**

Early Music Research

Source



Performer



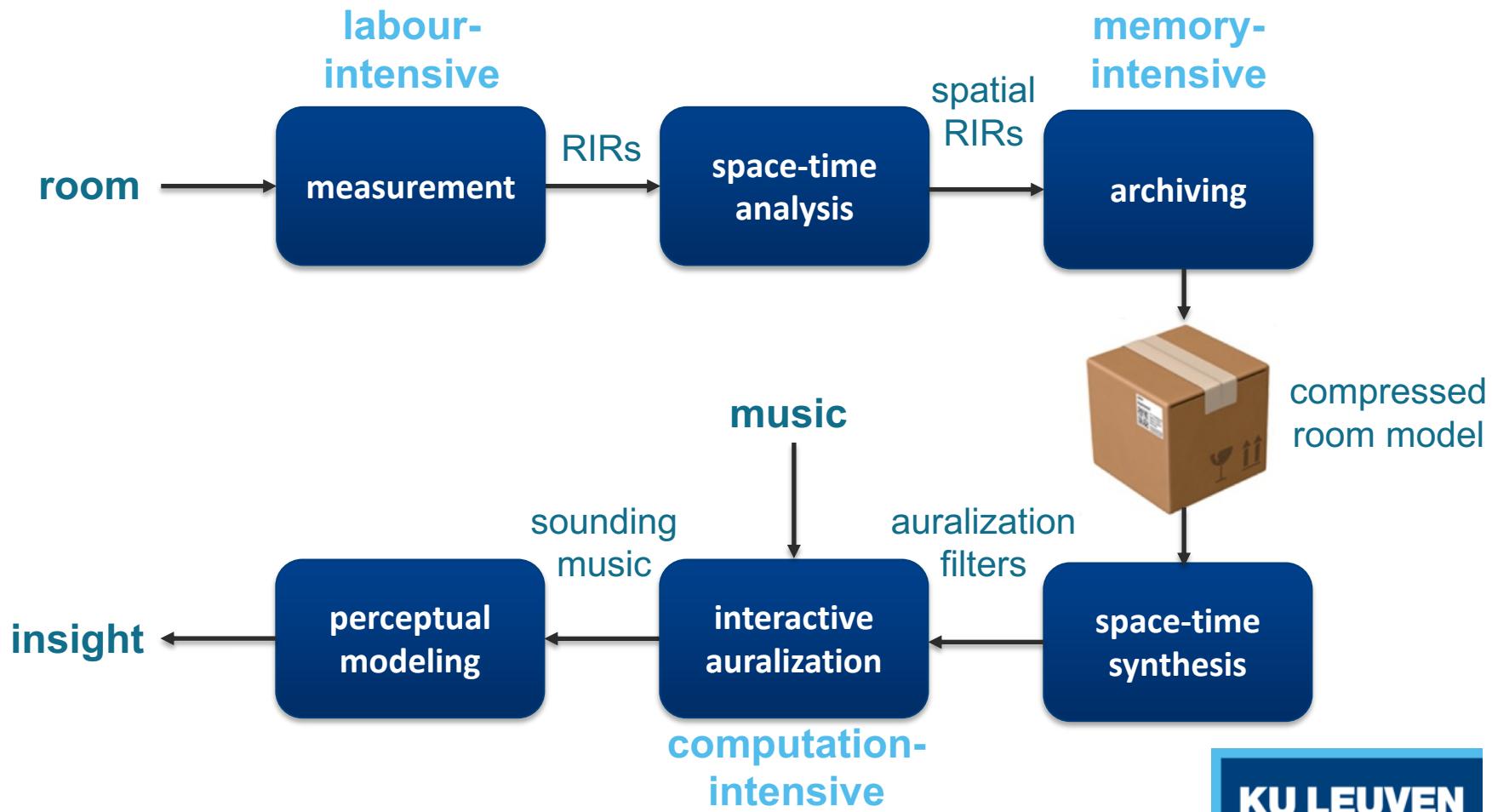
Environment



- How to **capture** the acoustics of a space to auralize/reproduce it at a different time and place?
- How to **archive** the acoustics of a historically valuable space for later reuse?
- How to achieve **interactive auralization** in a flexible and ecological manner?
- How to increase **understanding** of the relevance and quality of the acoustic characteristics of a space for musical performance?

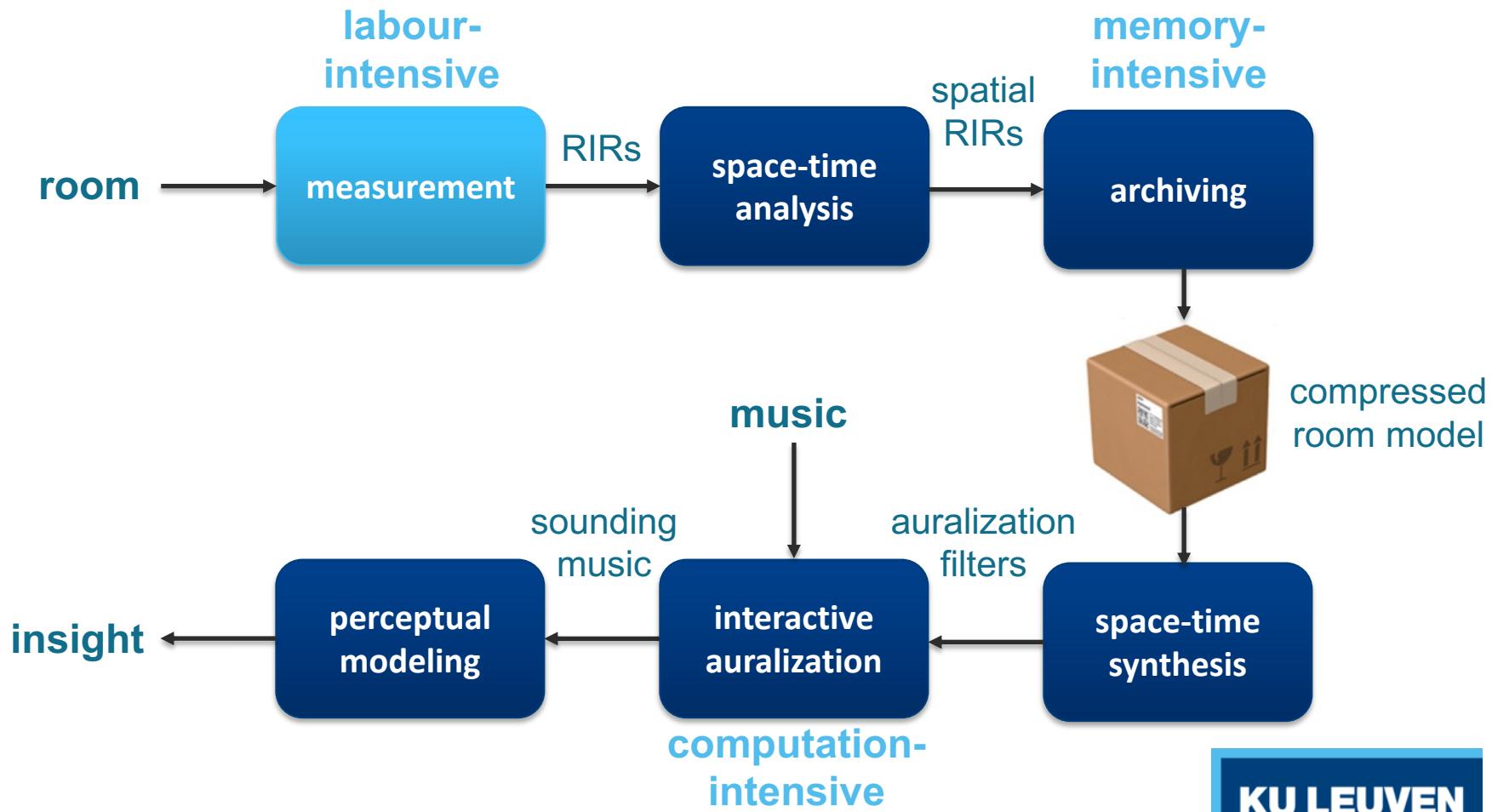
# Outline

- **System overview & challenges**



# Outline

- **System overview & challenges**



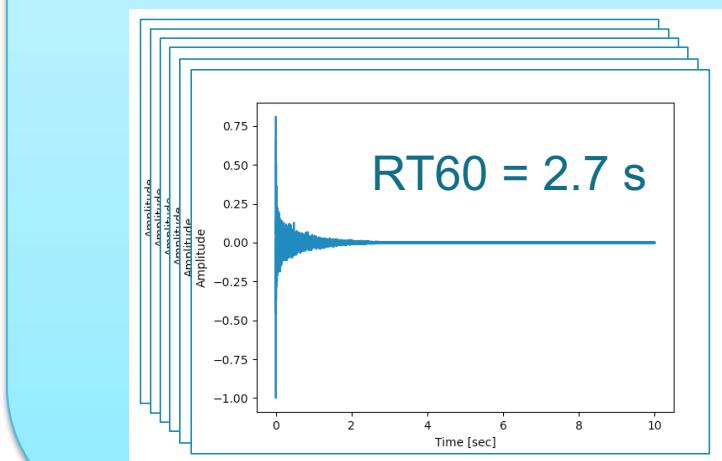
# Measurement

- **RIR measurement**  
= well-established procedure
- **Challenges:**
  - (Nightly) access to venue
  - Ownership of measurements

- Labour-intensive
- RIR = point-to-point model

→ *how to choose  
source/mic positions?*

## Case study: Nassau Chapel, Royal Library Brussels



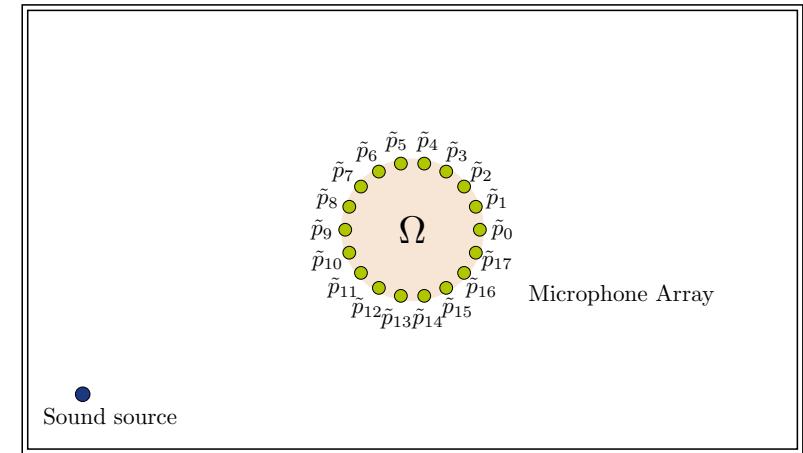
# Measurement

- **Key idea: RIR measurement at “few” positions + RIR interpolation**
  - Reduce labor-intensity
  - Expand potential use to other positions than those measured
  - Reduce memory required for archiving
  - Allow for auralization with moving sources/listeners
- **RIR interpolation problem:**

*given RIR measurements*

$$\tilde{\mathbf{P}} = [\tilde{\mathbf{p}}_0 \dots \tilde{\mathbf{p}}_{N_m-1}]$$

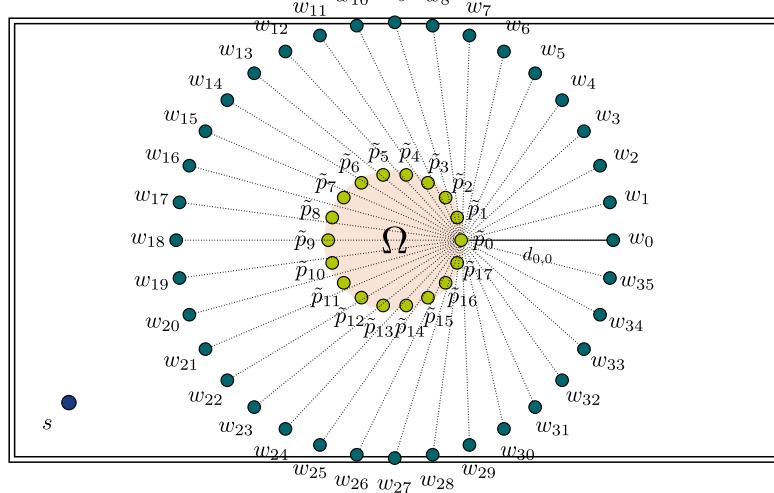
*find RIR for same source  
at any mic position  $\mathbf{r}$  in  $\Omega$*



# Measurement

- **Time-domain equivalent source method (TESM)**
  - Model RIR  $h(t, \mathbf{r})$  for mic position  $\mathbf{r}$  in  $\Omega$  as sum of propagating equivalent source signals  $w_l(t) \neq \delta(t)$

$$h(t, \mathbf{r}) = \sum_{l=0}^{N_w-1} \frac{1}{4\pi d_l(\mathbf{r})} \delta(t - d_l(\mathbf{r})/c) * w_l(t) = \mathcal{D}(\mathbf{r})[\mathbf{W}]$$



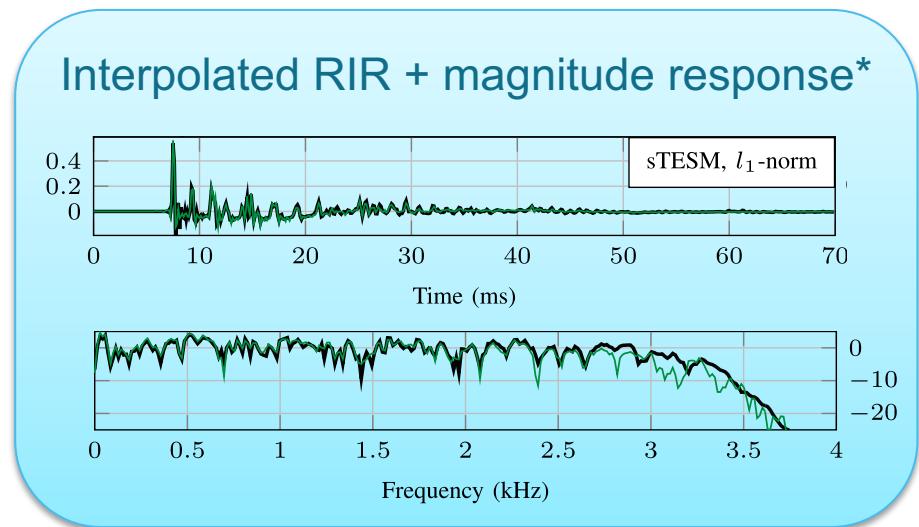
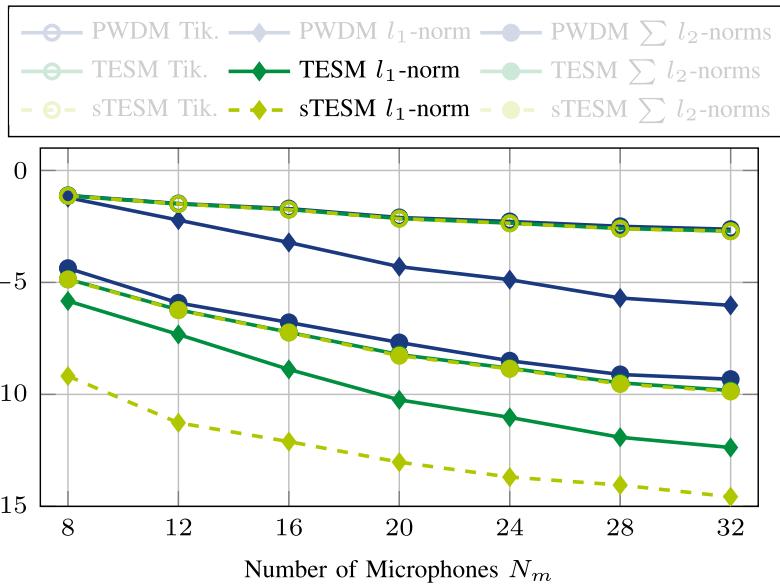
independent of  $\mathbf{r}$  !

$$\begin{aligned} \mathbf{W} &= [\mathbf{w}_0 \dots \mathbf{w}_{N_w-1}] \\ \mathcal{D}(\mathbf{r})[\cdot] &= \text{linear operator} \\ &\quad (\text{delays + attenuations}) \end{aligned}$$

# Measurement

- **Time-domain equivalent source method (TESM)**
  - Finding TESM signals  $w_l(t)$  by matching pressure signals  $\tilde{p}_m(t)$  (= measured RIR) at microphones = **underdetermined problem**
  - Regularization by **imposing spatio-temporal sparsity**

$$\min_{\mathbf{W}} \|D(\mathbf{W}) - \tilde{\mathbf{P}}\|_F^2 + \lambda \|\text{vec}(\mathbf{W})\|_1$$

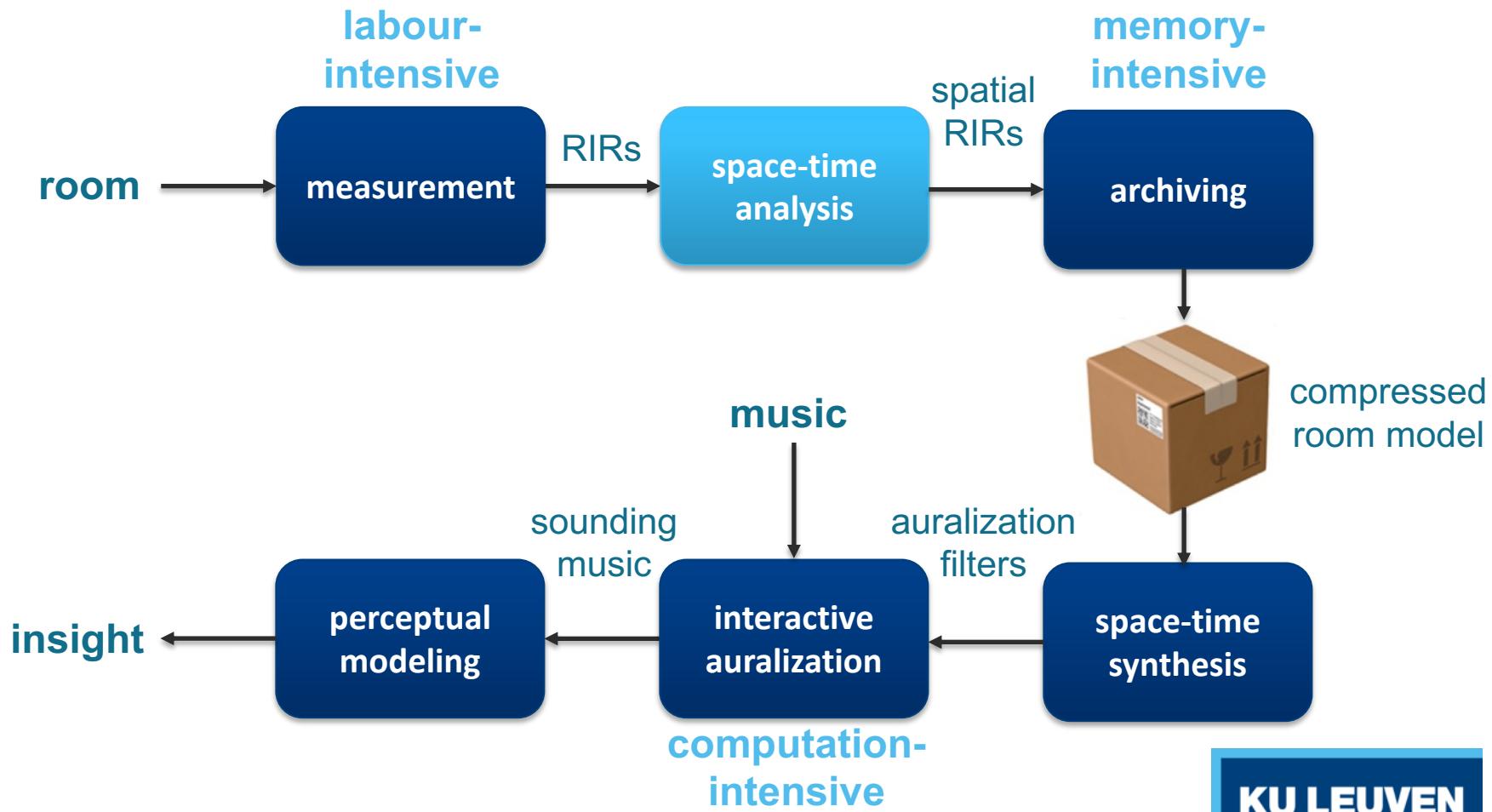


\*worst case result

\*\*average result

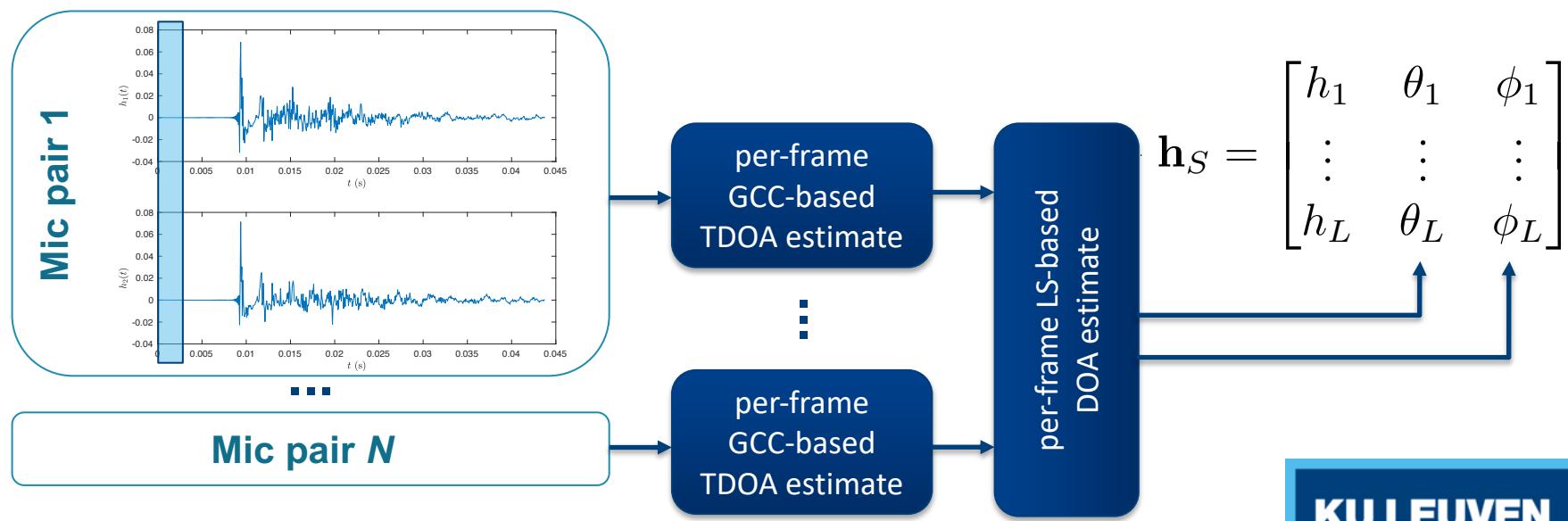
# Outline

- **System overview & challenges**



# Space-time analysis

- **Key model: Spatial room impulse response (SRIR)**
  - Include **direction of arrival information** (azimuth and elevation angles  $\theta, \phi$ ) to each RIR “peak” representing room reflection
- **Key method: Spatial decomposition method (SDM)**
  - TDOA estimation of corresponding RIR “peaks” in each mic pair
  - Least-squares DOA estimation from TDOAs of all mic pairs in array



# Space-time analysis



- **SDM challenges**

- Find phase-matched microphones
- Find RIR “peaks”
- Match “peaks” in different RIRs  $\rightarrow$  generalized cross-correlation (GCC)
- Estimate TDOAs with subsample accuracy  $\rightarrow$  TDOA interpolation

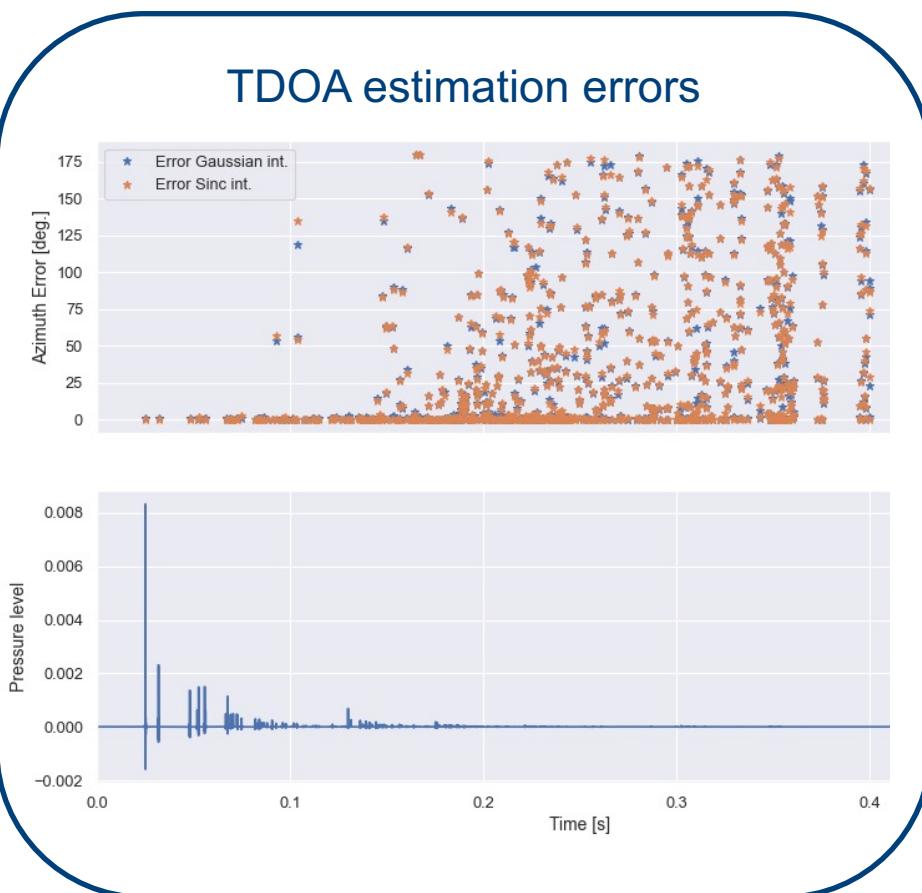
- **Subsample TDOA estimation**

- Due to bandlimited nature of measurement system, RIR “peaks” are sinc functions rather than impulse functions
- GCC  $R_{m,n}(t)$  of two time-shifted sinc functions = sinc function
- Optimal subsample TDOA estimation method is hence based on sinc interpolation rather than parabolic/Gaussian interpolation

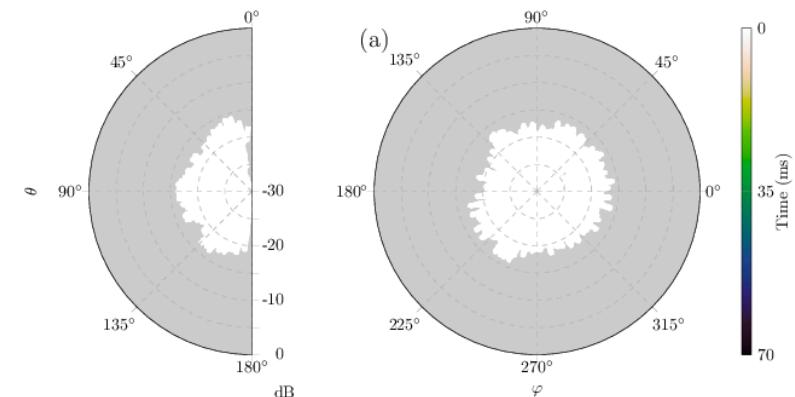
$$\tau_{\text{sinc}} = \arg \min_{\tau} \int_{-\infty}^{\infty} \left| \text{sinc}(\pi f_s(t - \tau)) - \frac{R_{m,n}(t)}{\max(R_{m,n}(t))} \right|^2 dt$$

# Space-time analysis

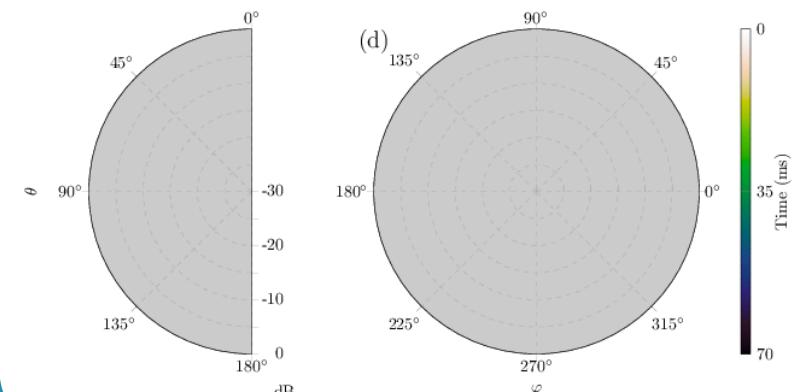
- **Resulting space-time model**



### SRIR visualization of interpolated RIRs



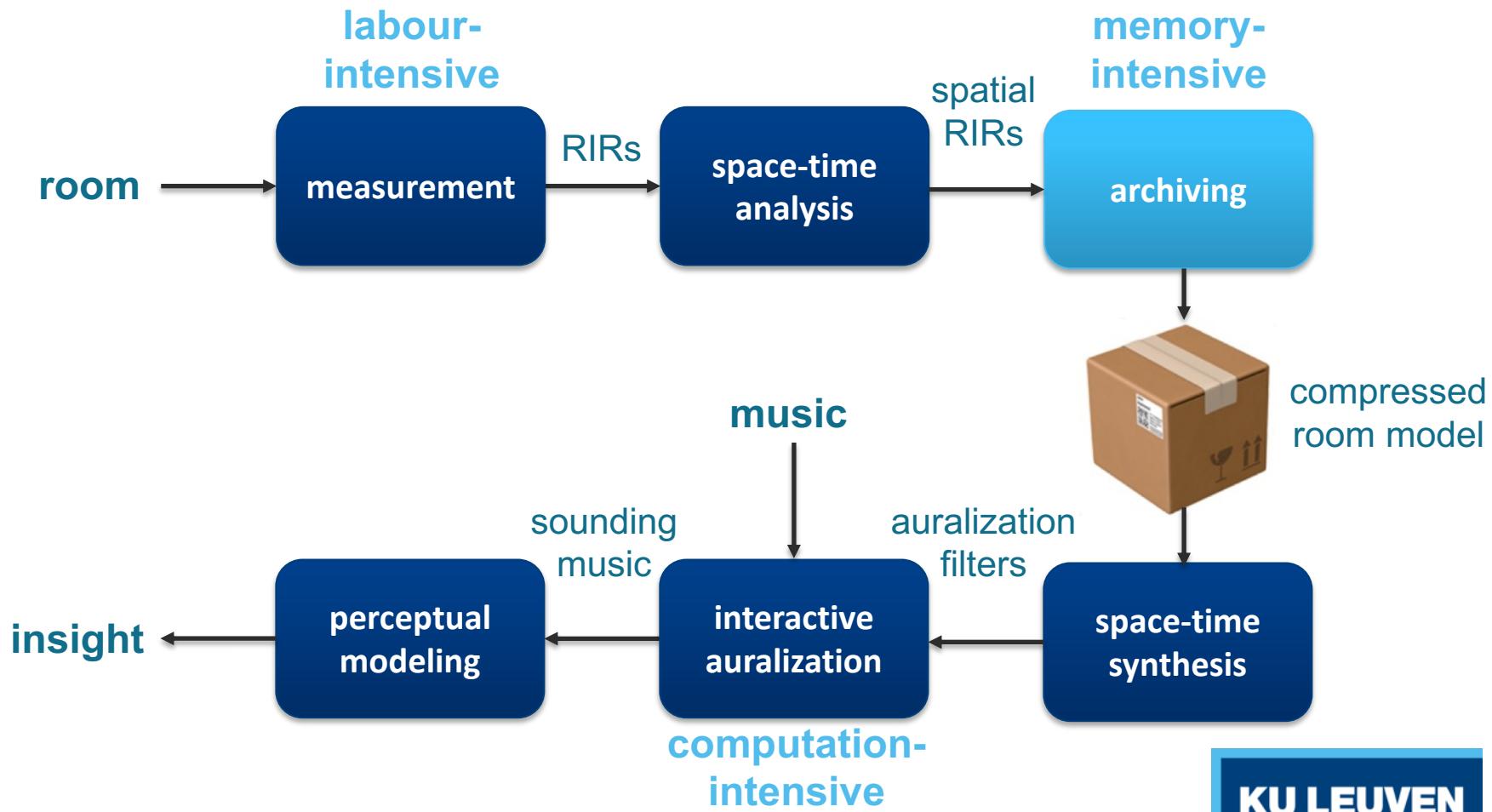
*without sparse regularization*



*with sparse regularization*

# Outline

- **System overview & challenges**



# Archiving

- **Why is archiving of church acoustics a challenge?**
  - Impulse response contains  $L \sim 10^4$  samples  $\sim 10^5$  bits
  - 1 spatial impulse response = 6 impulse responses  $\sim 10^6$  bits
  - Plenacoustic sampling theory: accurate sound field reconstruction requires spatial resolution of  $\sim 10$  cm  
 $\sim (100)^3$  source positions x  $(100)^3$  observer positions  
 $\sim 10^{12}$  spatial impulse responses  $\sim 10^{18}$  bits  **$\sim 100$  petabyte**



# Archiving

- How to “compress” a room impulse response?

- Truncation
- Hard thresholding
- Sparse approximation
- Low-rank approximation

## Physical justification

non-homogenous Helmholtz equation

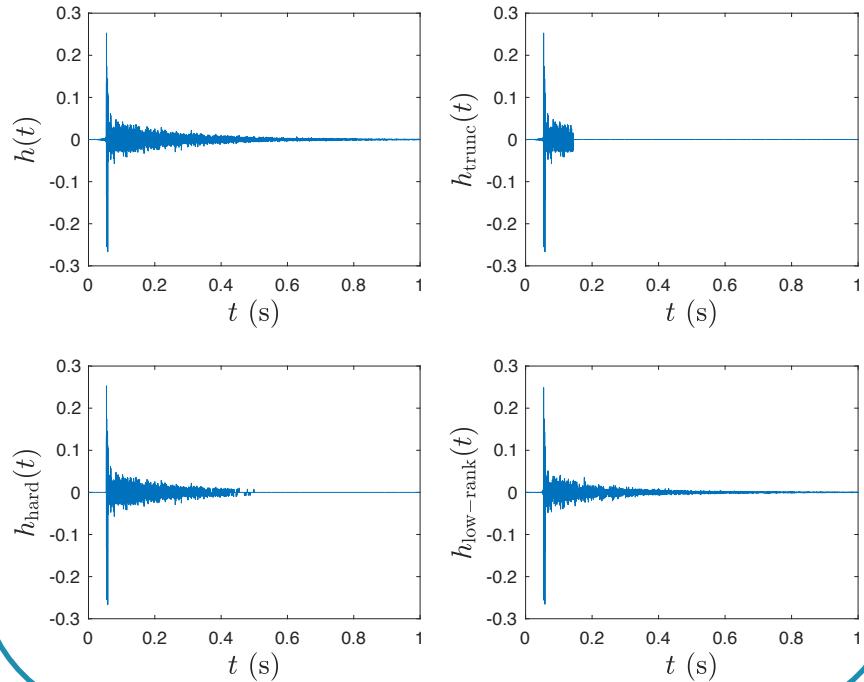
$$(\nabla^2 + k^2)H(\mathbf{r}, \mathbf{r}_s, \omega) = -j\omega\rho_0Q\delta(\mathbf{r} - \mathbf{r}_s)$$



RIR  $\approx$  sum of damped sinusoids

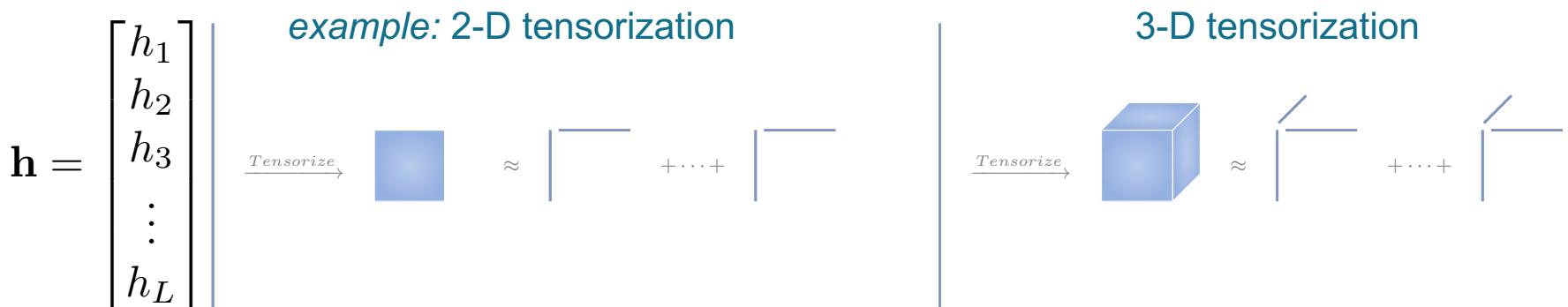
$$h(t) \approx \sum_{m=1}^M \mu_m e^{-\beta_m t} \cos(\omega_m t + \phi_m), \quad t \geq 0$$

RIR with three compression methods  
(compression rate = 85 %)



# Archiving

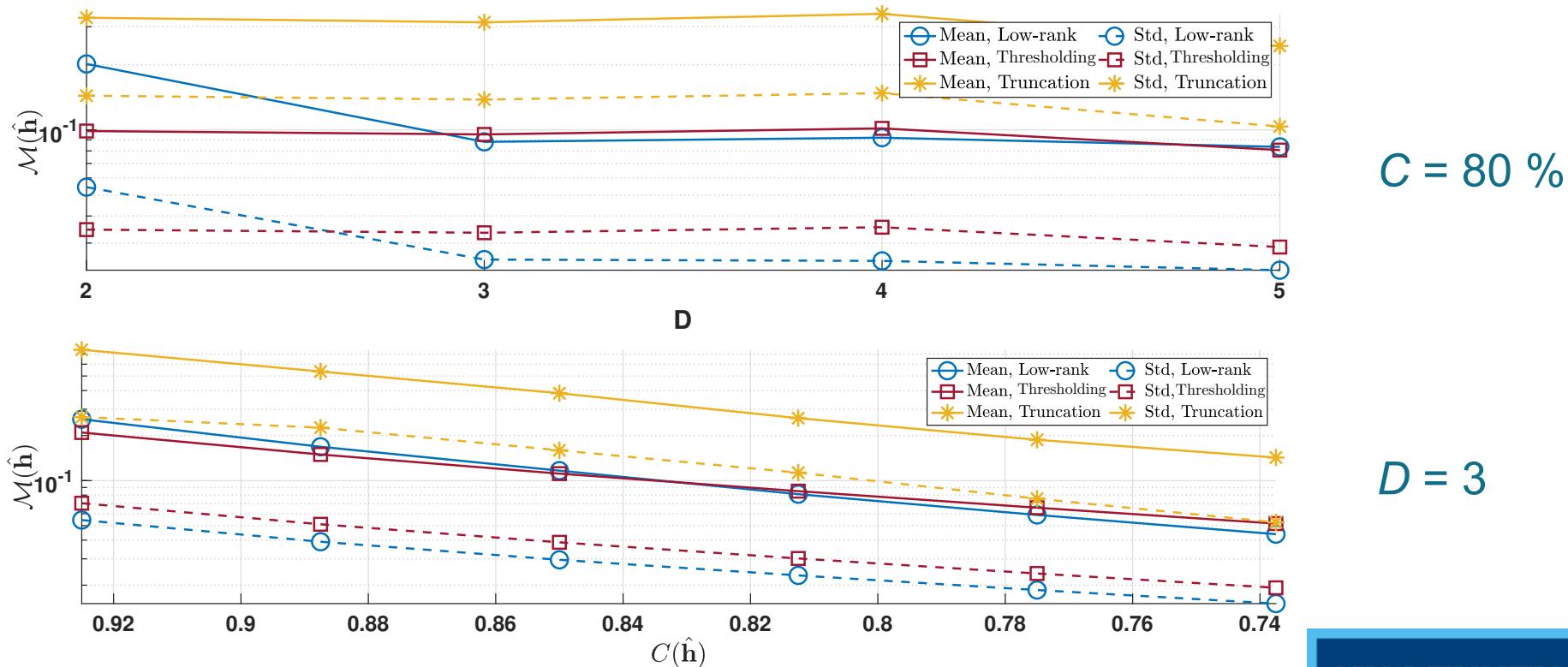
- **Key idea: Sum of  $M$  (damped) sinusoids admits matricization/tensorization of rank  $2M$** 
  - Impulse response vector  $\mathbf{h}$  (= 1-D array) of length  $L$  can be **reshaped** into  $N$ -D array of dimensions  $\sqrt[N]{L} \times \sqrt[N]{L} \times \dots \times \sqrt[N]{L}$
  - $N$ -D array can be **approximated** as sum of  $2M$  rank-1 terms (SVD or canonical polyadic decomposition)



$$\mathbf{h} = \text{vec} \left( \sum_{m=1}^{2M} \mathbf{u}_m^{(1)} \circ \mathbf{u}_m^{(2)} \circ \dots \circ \mathbf{u}_m^{(N)} \right)$$

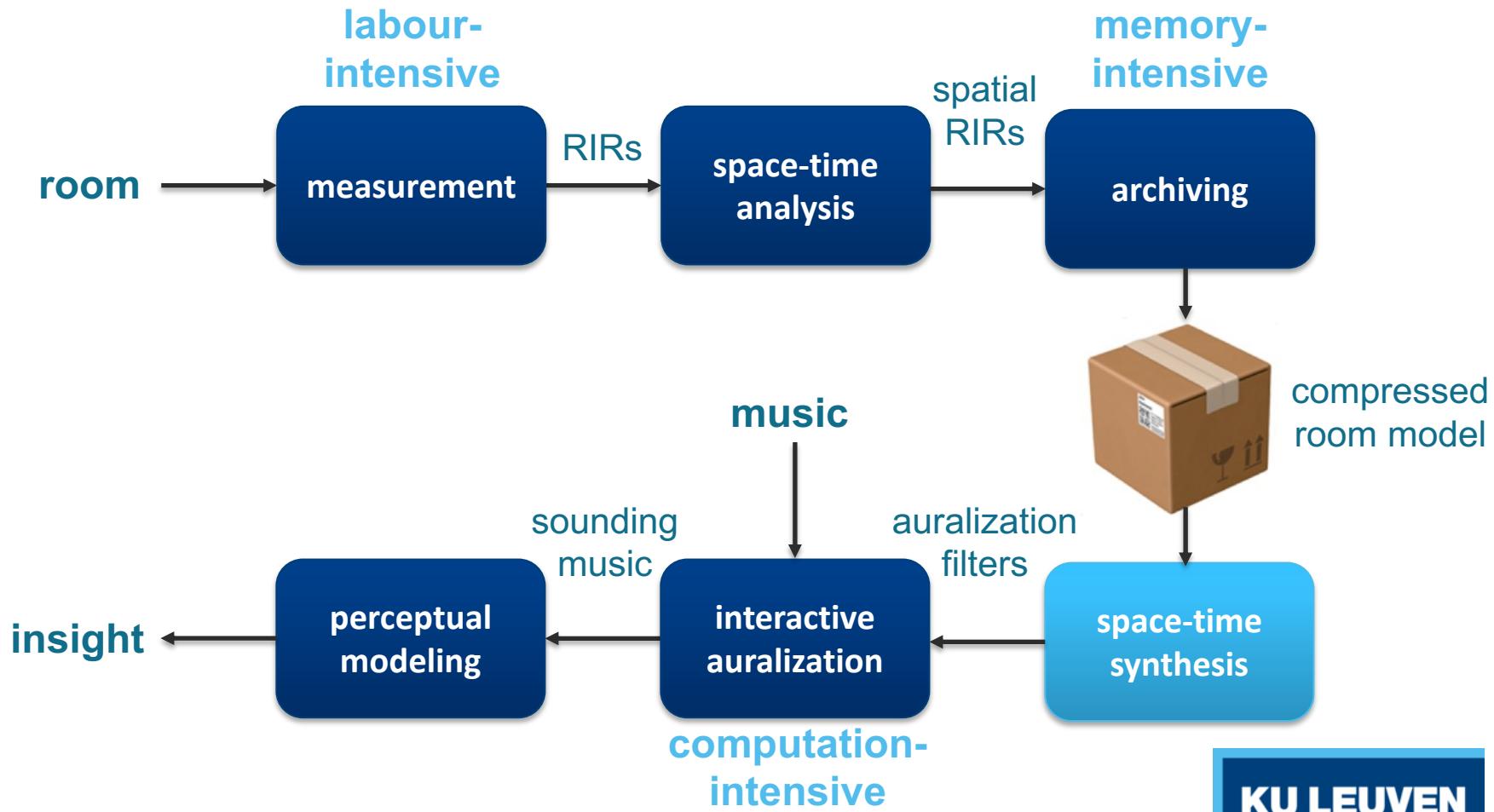
# Archiving

- **Misadjustment results after RIR compression**
  - Methods: truncation, hard thresholding, low-rank approximation
  - Misadjustment vs. tensorization dimension  $D$  & compression rate  $C$



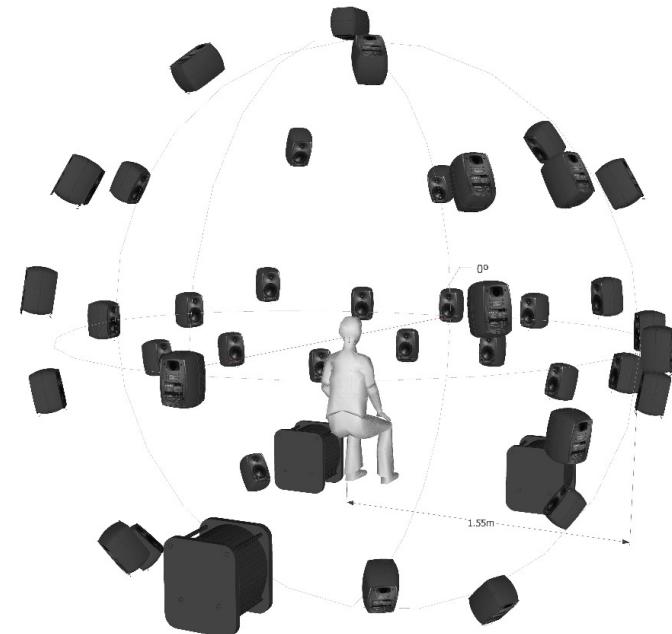
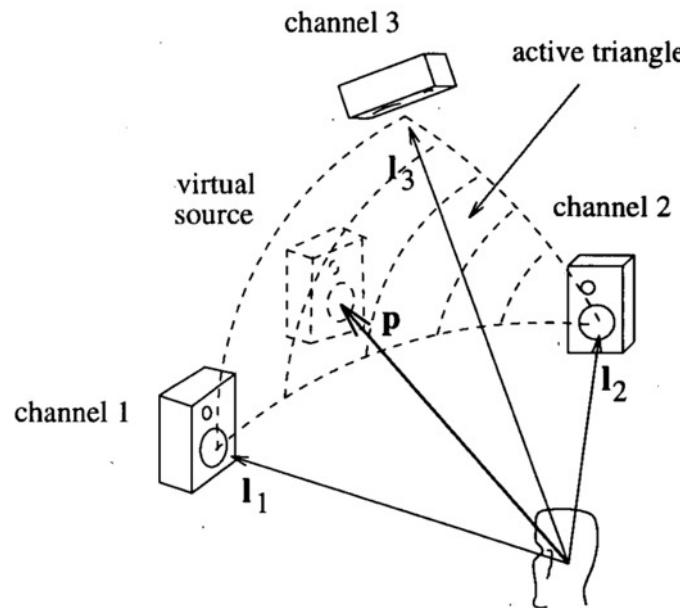
# Outline

- **System overview & challenges**



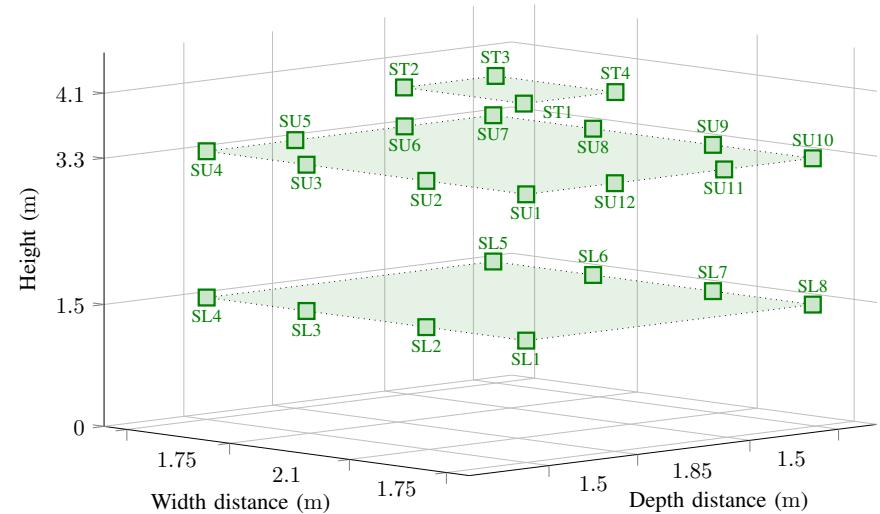
# Space-time synthesis

- Key idea: Mapping of room reflections to loudspeakers
  - Conversion of SRIR to set of per-loudspeaker impulse responses
    - Vector base amplitude panning (VBAP)
    - Nearest-loudspeaker mapping



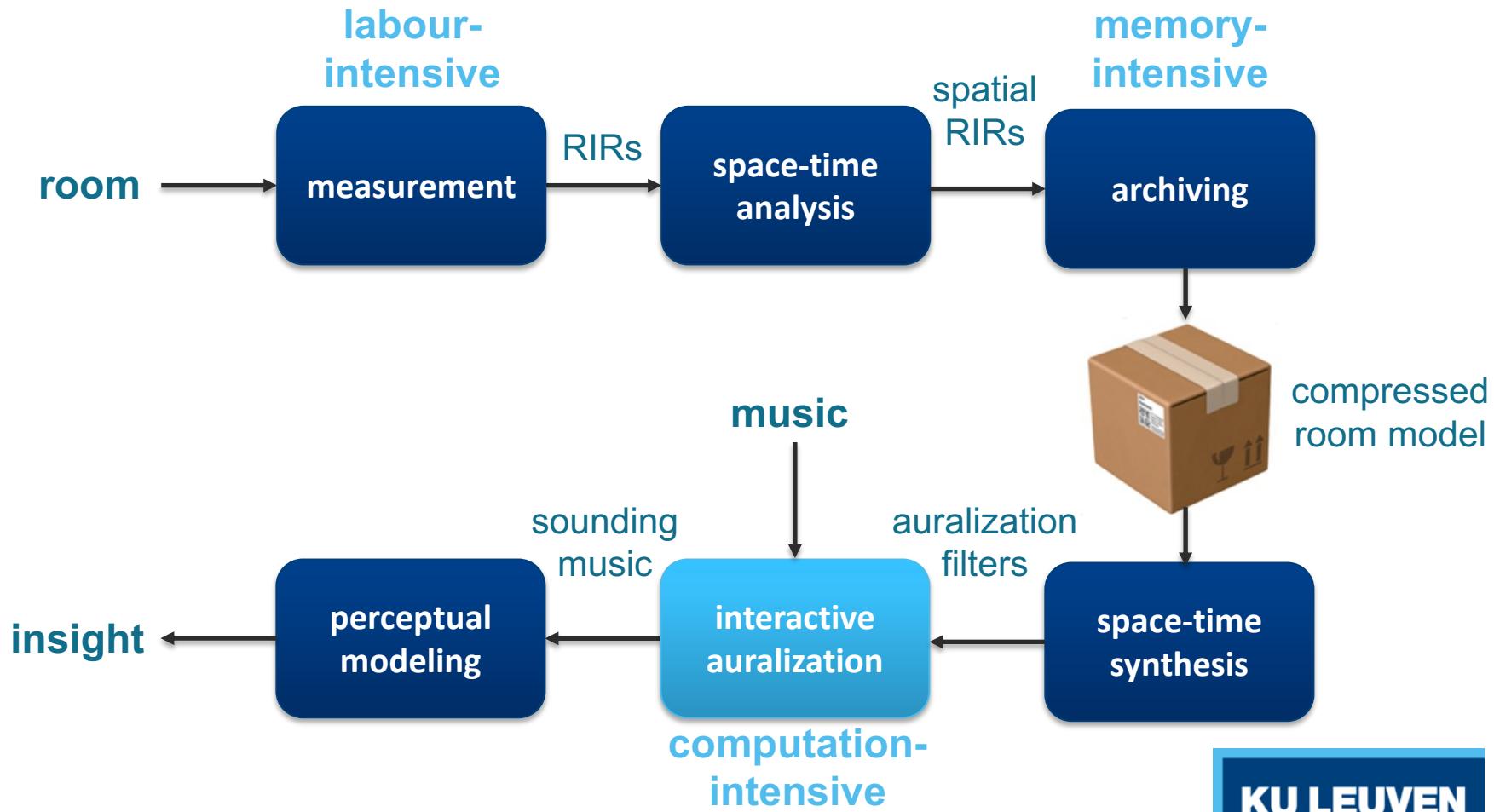
# Space-time synthesis

- **Loudspeaker set-up: Library of Voices (Leuven)**
  - 3-D array of 20–24 Martin Audio 6,5" CDD loudspeakers
  - Reproduction room: RT60 = 0.5 s (with curtains closed)



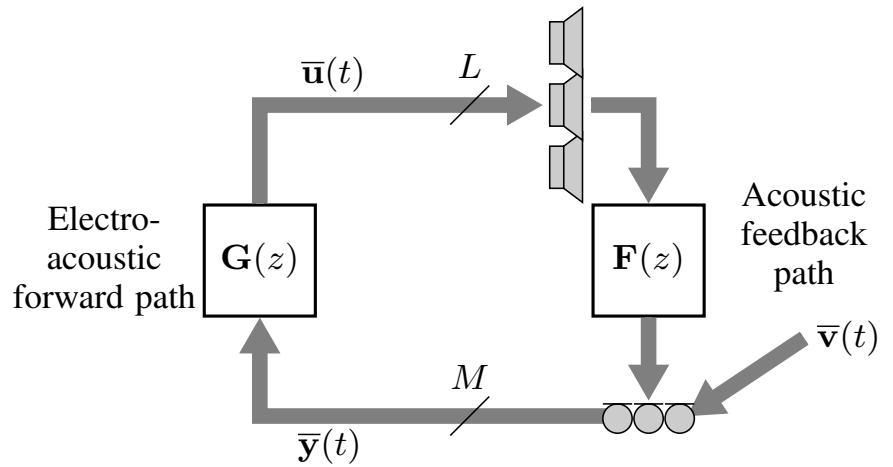
# Outline

- **System overview & challenges**



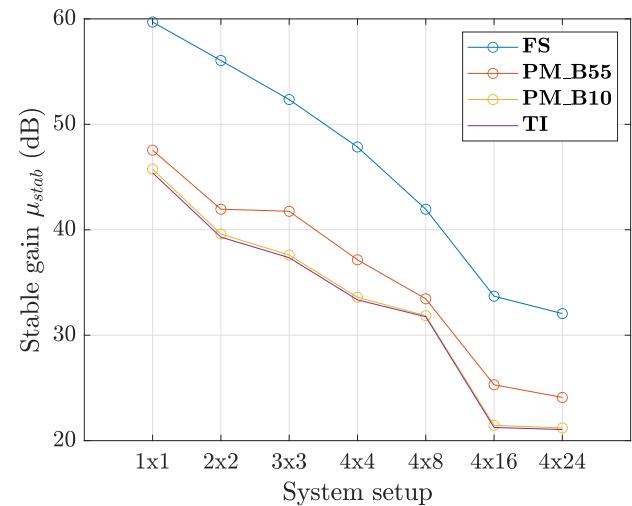
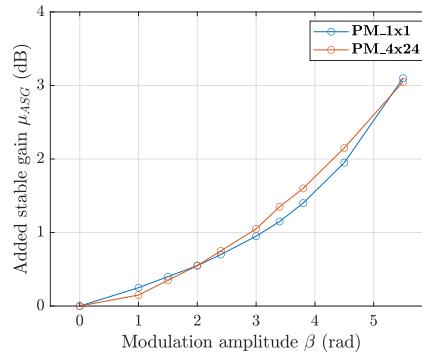
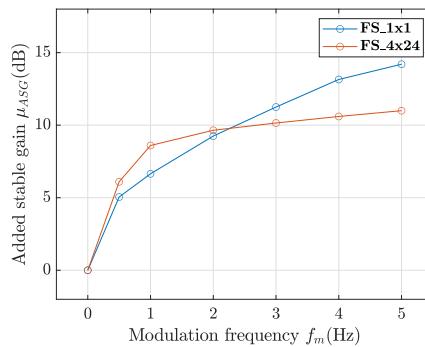
# Interactive auralization

- **Challenges:**
  - Multi-channel acoustic feedback control
  - Low-latency real-time multi-channel convolution



# Interactive auralization

- **Multi-channel acoustic feedback control**
  - Gain before instability decreases with increasing # channels
  - Feedback-related artefacts: howling, ringing, coloration
- **Acoustic feedback control methods:**
  - Phase modulation methods  $\rightarrow$  *Reverberation enhancement systems*
  - Gain reduction methods
  - Spatial filtering methods
  - Room modeling methods



**FS** = frequency shifting (5 Hz)

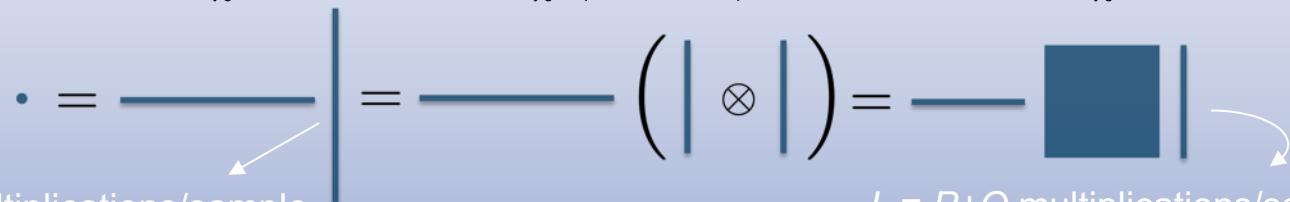
**PM** = phase modulation with  
modulation index  $\beta=1.0$  or  $5.5$

# Interactive auralization

- **Low-latency real-time multi-channel convolution**
  - Key idea: Rewrite convolution operation using compressed RIR
    - **Low latency:** no buffering required by staying in time domain
    - **Real-time:** reduced # input buffer reads and # FLOPS
      - Truncation  $\rightarrow$  shorter FIR filter
      - Hard thresholding  $\rightarrow$  FIR filter with fewer non-zero coefficients
      - Sparse approximation  $\rightarrow$  short “warped” FIR filter (mixed-Kautz model)
      - Low-rank approximation  $\rightarrow$  “low-rank convolution”

**Low-rank convolution:** illustration for rank-1 model  $\mathbf{h}_{L \times 1} = \mathbf{u}_{P \times 1} \otimes \mathbf{v}_{Q \times 1}$

$$y_k = \mathbf{x}_k^T \mathbf{h} = \mathbf{x}_k^T (\mathbf{u} \otimes \mathbf{v}) = \mathbf{v}^T \mathbf{X}_k^T \mathbf{u}$$

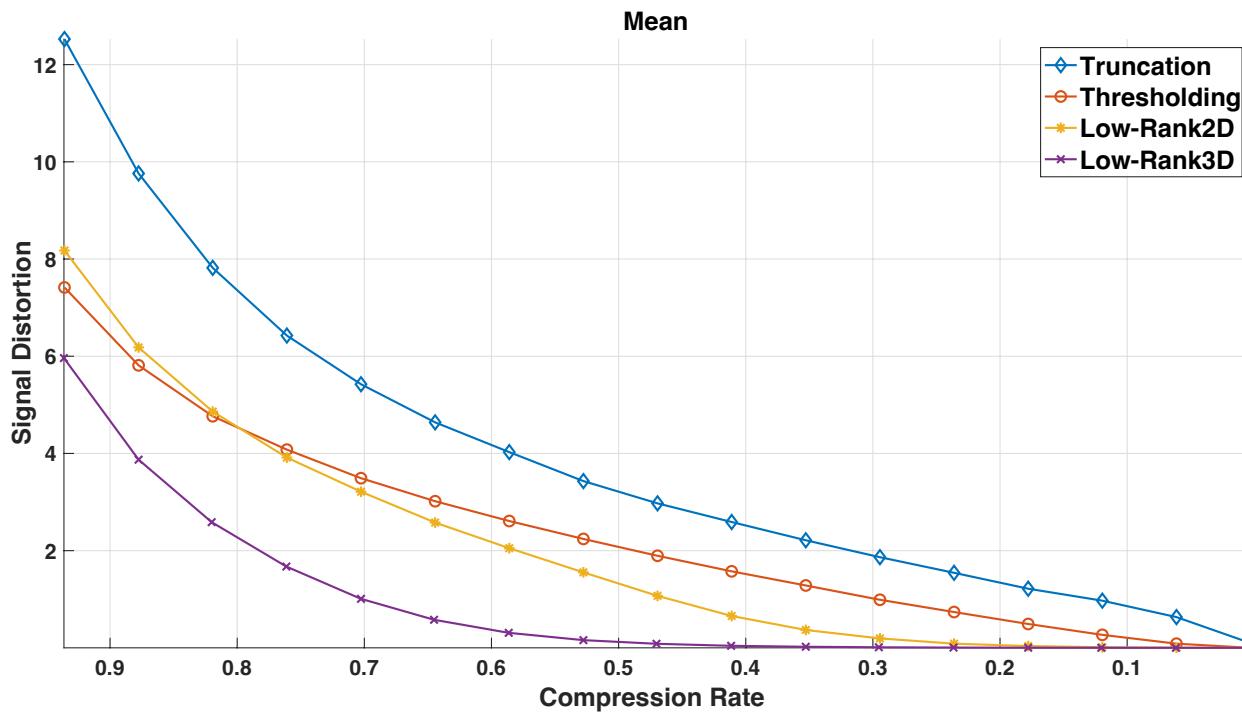


$L = PQ$  multiplications/sample

$L = P+Q$  multiplications/sample

# Interactive auralization

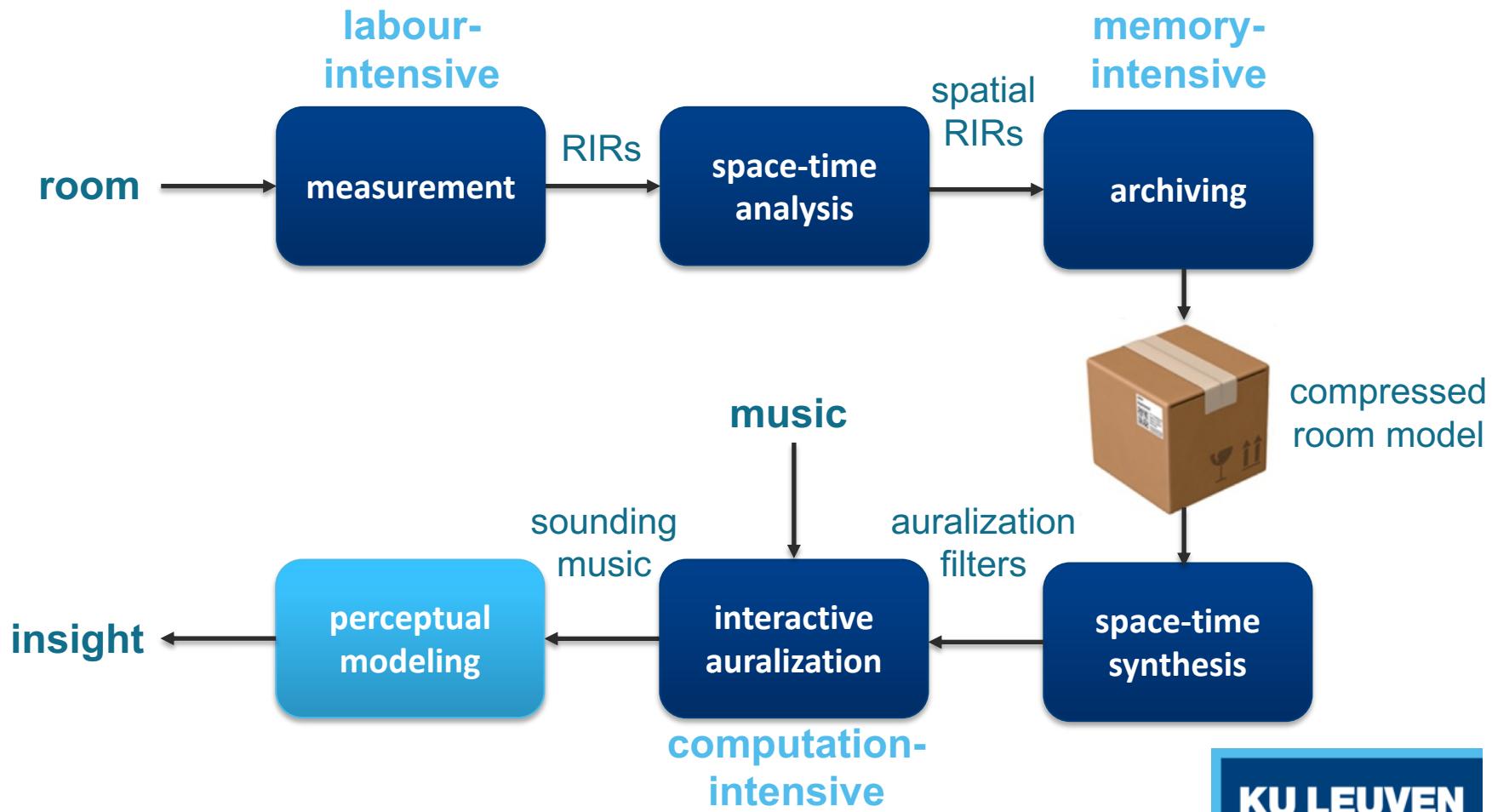
- **Signal distortion after compressed RIR convolution**
  - Methods: truncation, hard thresholding, low-rank approximation
  - Mean ERB-weighted signal distortion vs. RIR compression rate C



input = dry vocal music  
RIR = Nassau Chapel RIR,  
RT60 = 2.7 s,  $L = 117649$

# Outline

- **System overview & challenges**



# Perceptual modeling

- **Aim:** understand relation between acoustic characteristics of church and their perceived quality (broadly defined)
- **Key methodology:** Flash Profile rapid sensory analysis
  - Originally developed in frame of **food tasting** experiments
  - Validated for perceptual modeling of virtual acoustics **by listening** (e.g. auralization of concert halls, car cabins, domestic rooms)
  - Evaluated in preliminary experiments for perceptual modeling of virtual church acoustics **by listening while singing**



## Materials

- 6 virtual acoustic spaces
- 4 expert listeners: male singers from Cappella Pratensis
- 2 pieces: plainchant + polyphonic



# Perceptual modeling

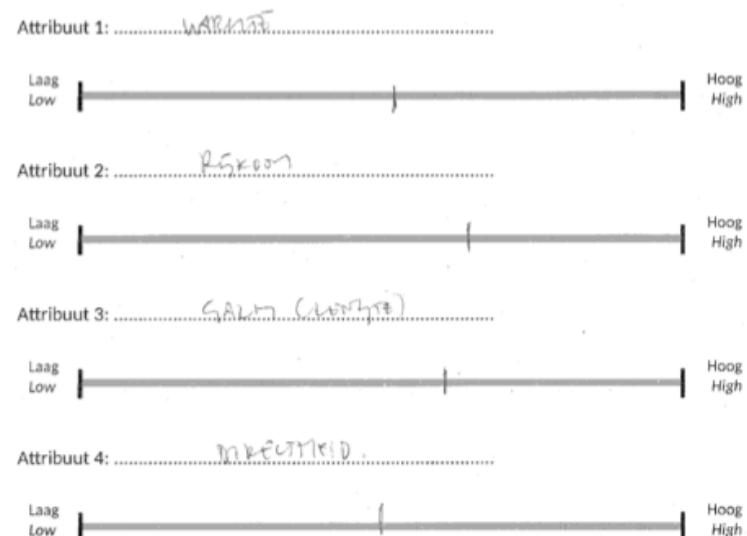
- **Flash Profile Methodology:** experiment design
  - **1) Elicitation phase:** individual semantic definition of perceptual attributes to characterize differences between virtual spaces
  - **2) Ranking phase:** continuous-scale (low-high) quantification of each perceptual attribute for each virtual space

Expert 1

1 DRYNESS  
2 SHARPNESS  
3 WARMTH  
4 LOWER FREQUENCY FRIENDLINESS  
5 FULLNESS

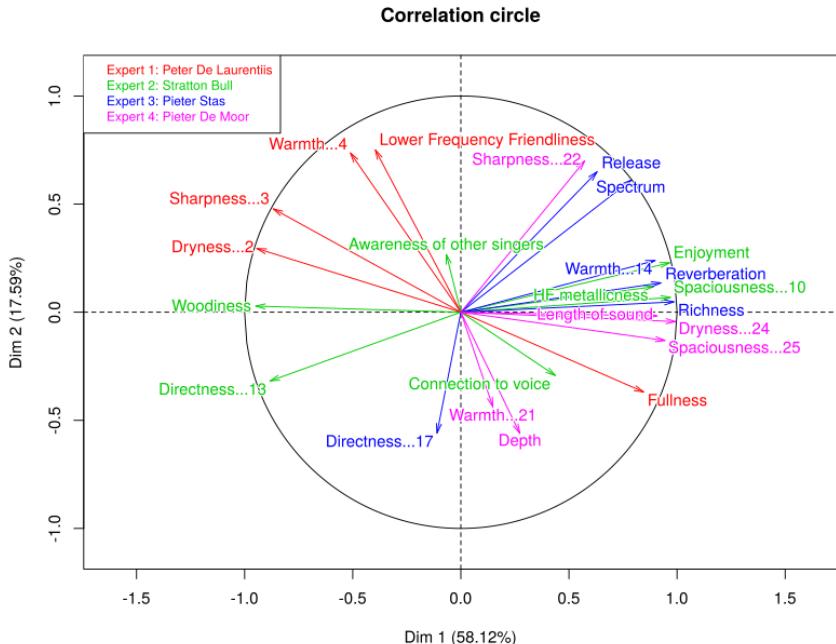
Expert 2

① enjoyment  
② awareness of othersingers  
③ woodiness  
④ spaciousness  
⑤ connection to voice  
⑥ high frequency-metallic  
⑦ directness



# Perceptual modeling

- **Flash Profile Methodology:** statistical data analysis
  - Multi-factor principal component analysis + clustering



- 75% of perceived variance among spaces is modeled by two largest principal components
- two largest principal components correlate to perceptual attributes of **spaciousness/reverberance** (Dim 1) and **spectral content** (Dim 2)
- six virtual spaces can then be mapped into this 2-D principal component subspace

# Conclusion

- **Some take-home messages...**
  - **Acoustic signal processing in digital humanities:** case studies in humanities/musicology/cultural heritage/... may carry remarkably many research challenges relevant to our community
  - **Fundamental signal processing research** (sampling & interpolation, sparse & low-rank modeling, ...) can be highly relevant to address application-specific bottlenecks relating to labour, memory, and computational resources
  - **Interdisciplinary research** is much more than putting together diverse team – it requires to learn common language and mutual scientific understanding, attract funding, develop proper research methodology, ... which is not easy but very enriching
  - Looking for challenging research topic in acoustic signal enhancement? Consider **multi-channel acoustic feedback control**

# Thank you...

- **This presentation is the result of joint work with:**  
*Niccolò Antonello, Stratton Bull, David Burn, Bart De Moor, Enzo De Sena, Bart Demuyt, Efren Fernandez-Grande, Ann Kelders, Martin Jälmby, Rudi Knoops, Hannes Rosseel, Wannes Van Ransbeeck ... and many more*
- **The work presented here has been carried out and supported by:**



DEPARTEMENT  
ECONOMIE  
WETENSCHAP &  
INNOVATIE



- **Contact**

[toon.vanwaterschoot@esat.kuleuven.be](mailto:toon.vanwaterschoot@esat.kuleuven.be)

<https://tvanwate.github.io>