

Overview

Linear Regression

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머신러닝의 학습 방법들

- **Gradient descent based learning**
- **Probability theory based learning**
- **Information theory based learning**
- **Distance similarity based learning**

머신러닝의 학습 방법들

- Gradient descent based learning

실제 값과 학습된 모델 예측치의 오차를 최소화

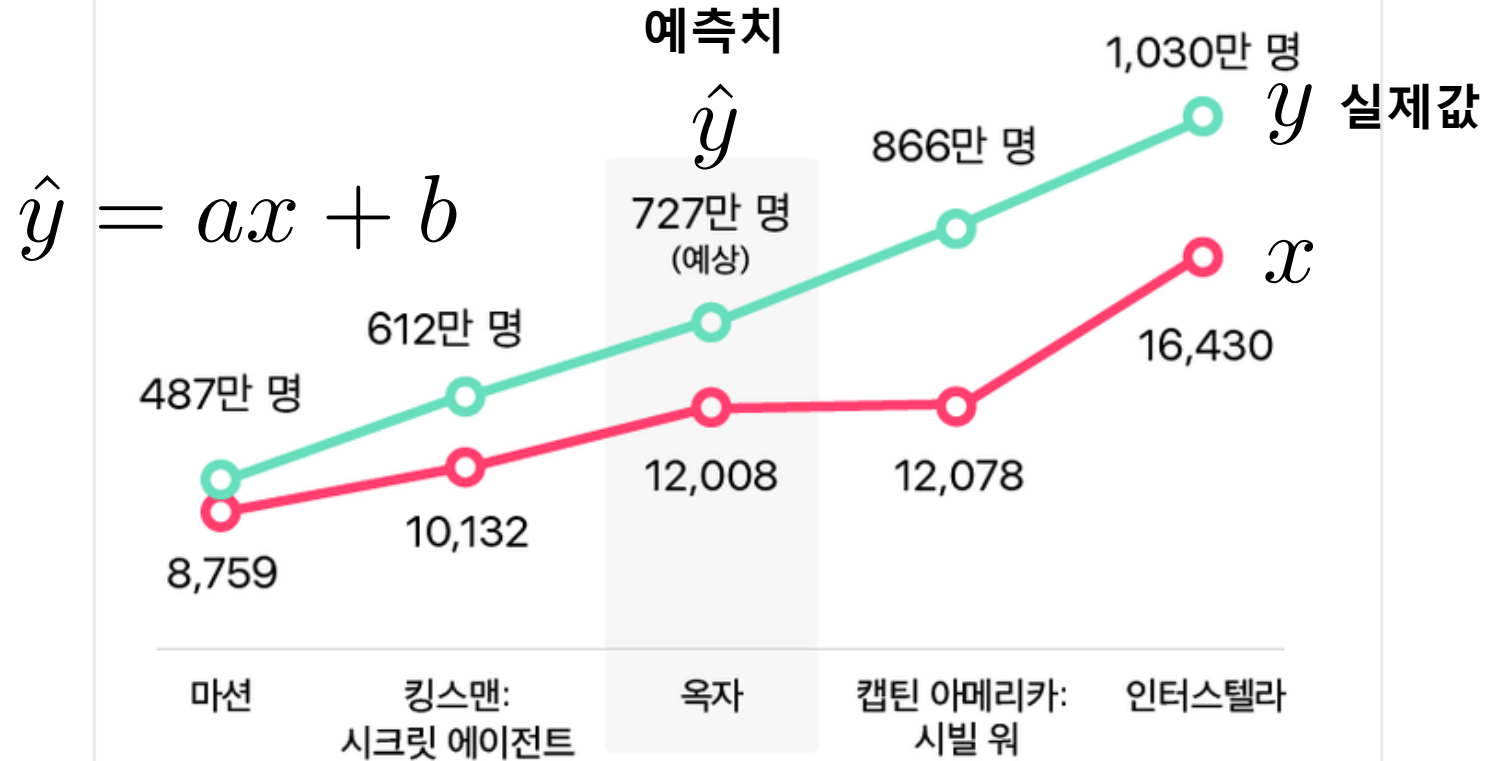
모델의 최적 parameter 찾기가 목적

gradient descent 활용

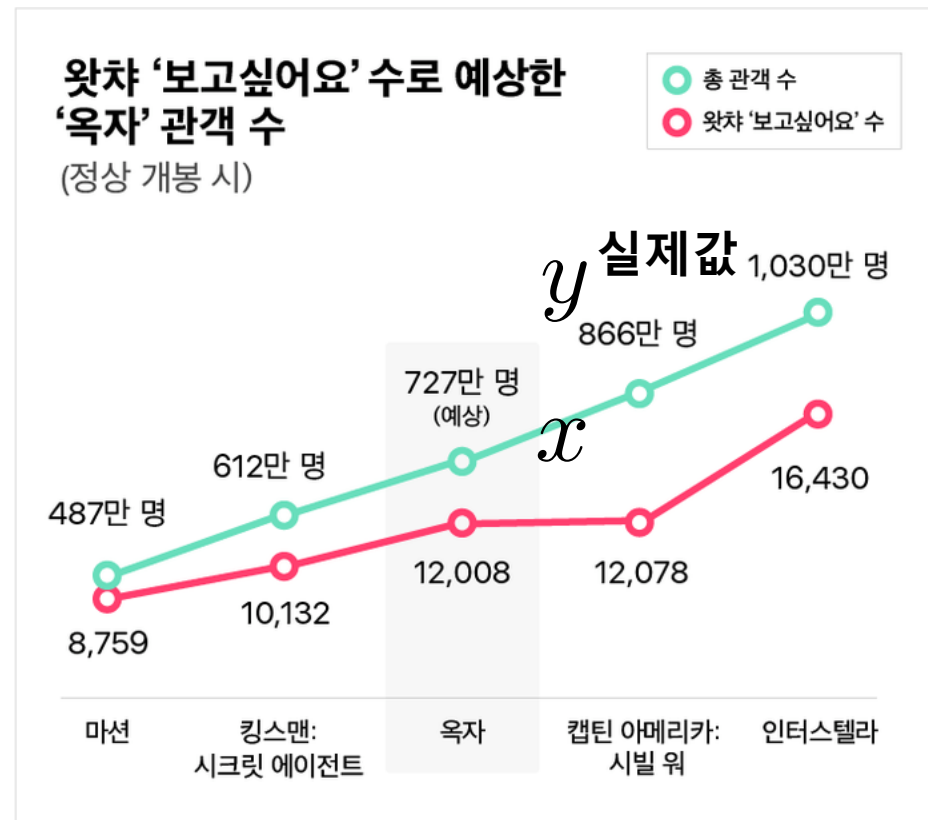
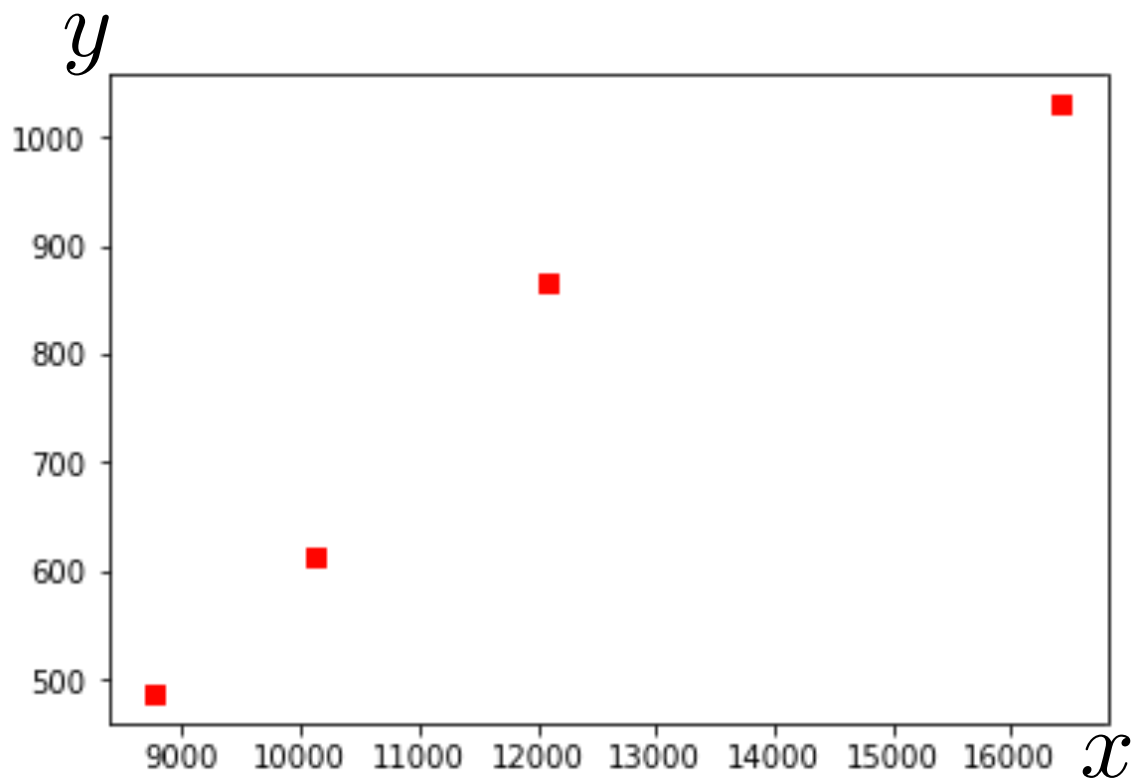
왓차 '보고싶어요' 수로 예상한 '옥자' 관객 수

(정상 개봉 시)

- 총 관객 수
- 왓차 '보고싶어요' 수

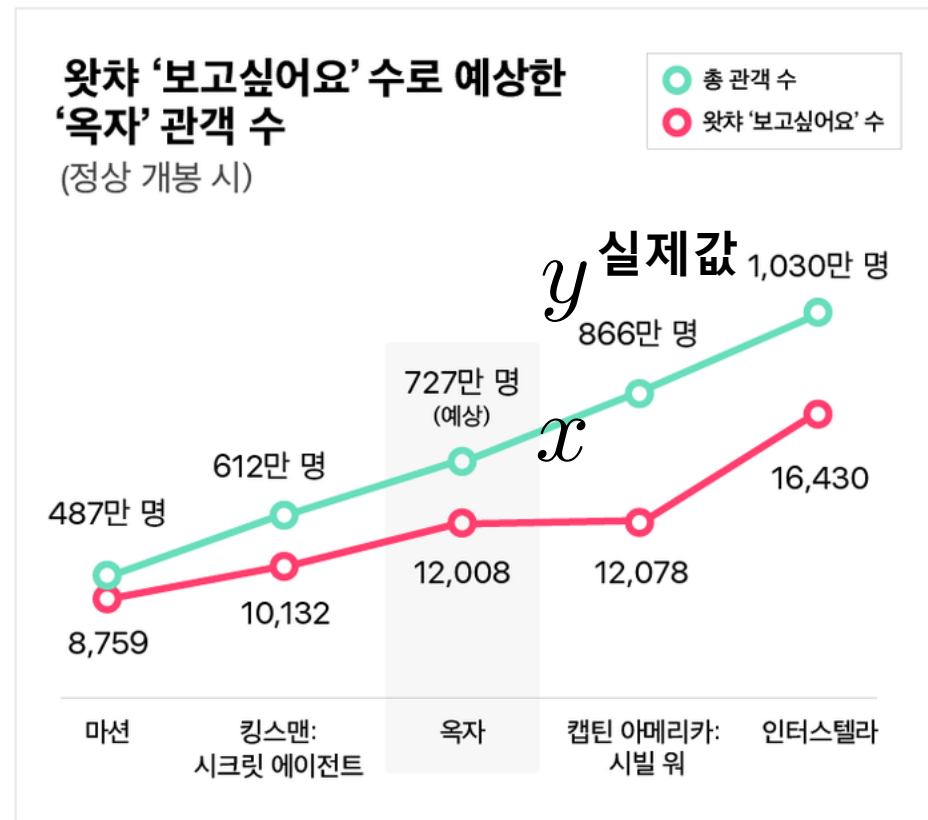
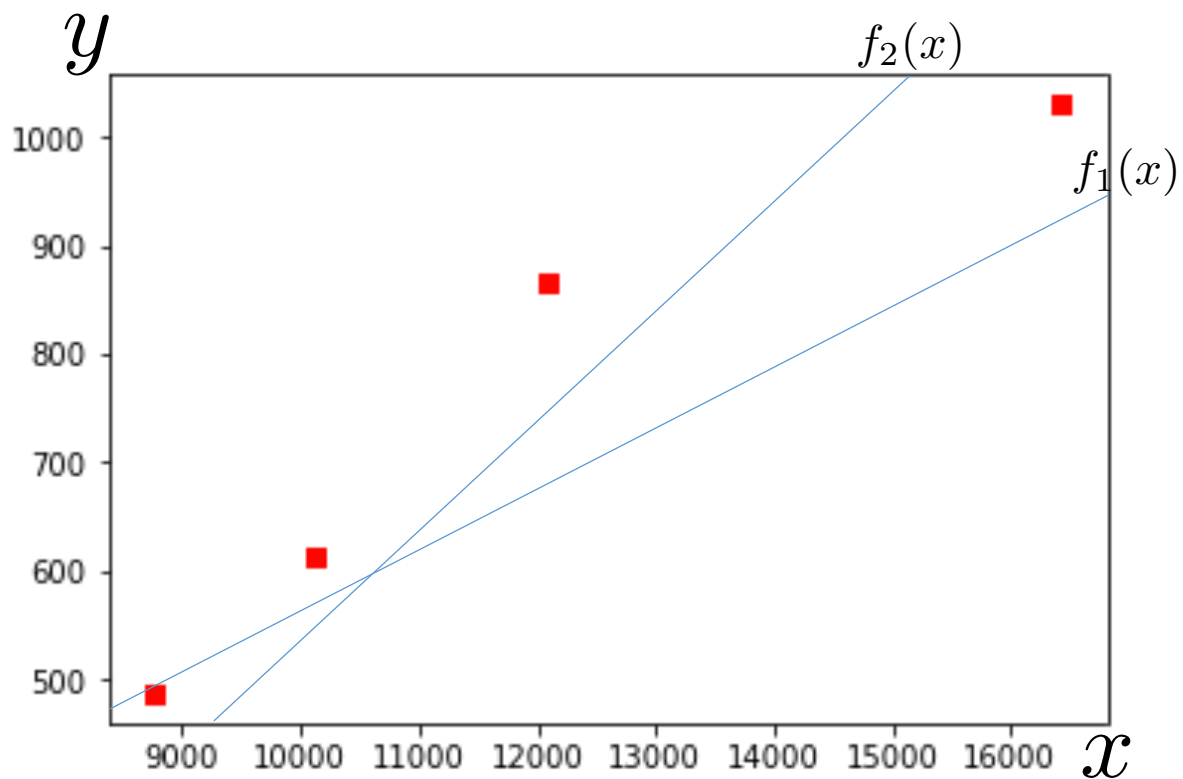


Source: <http://platum.kr/archives/83757>



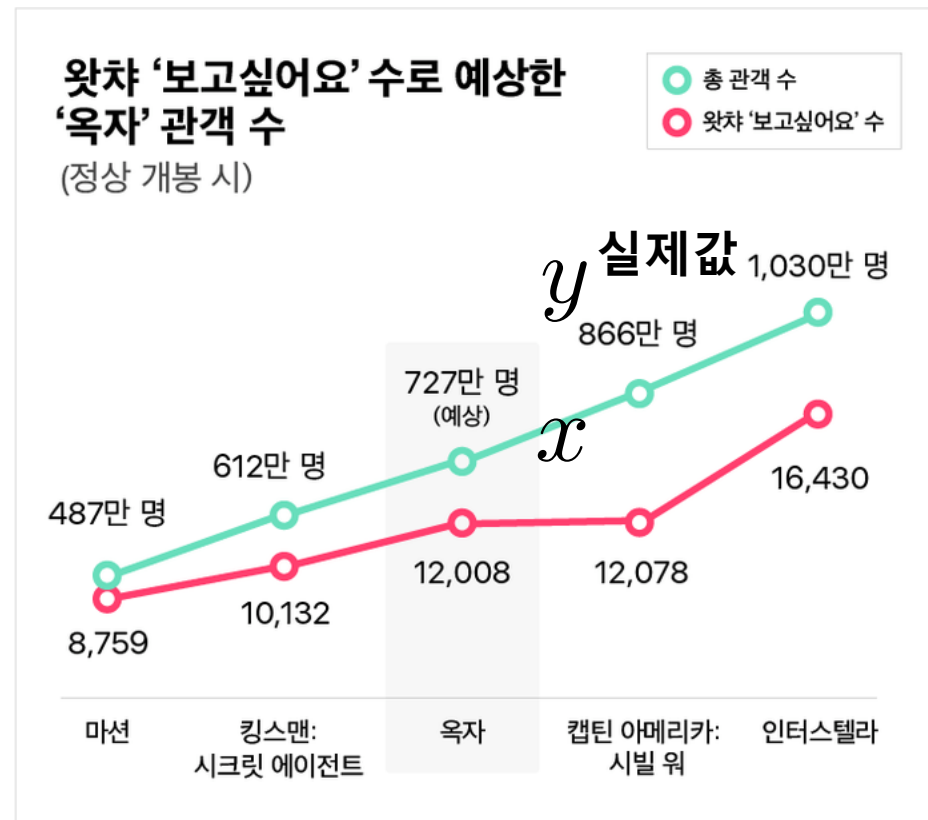
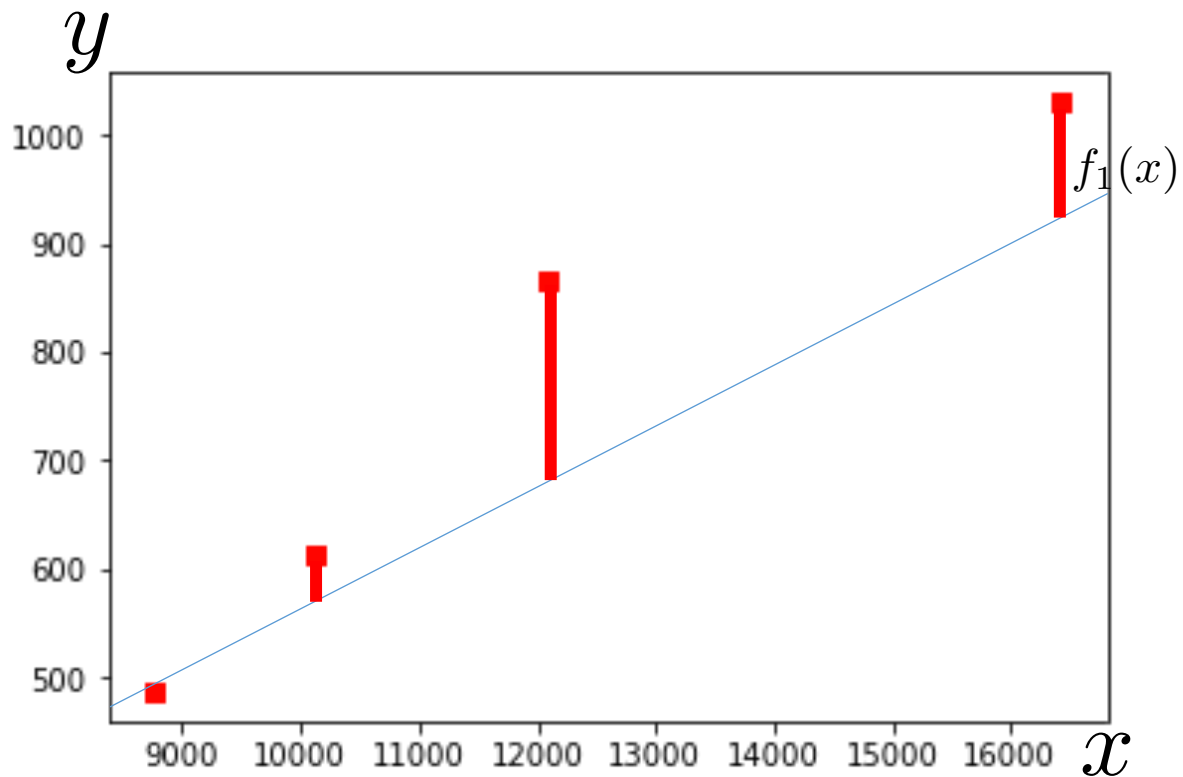
Source: <http://platum.kr/archives/83757>

$$f(x) = \hat{y} = ax + b$$



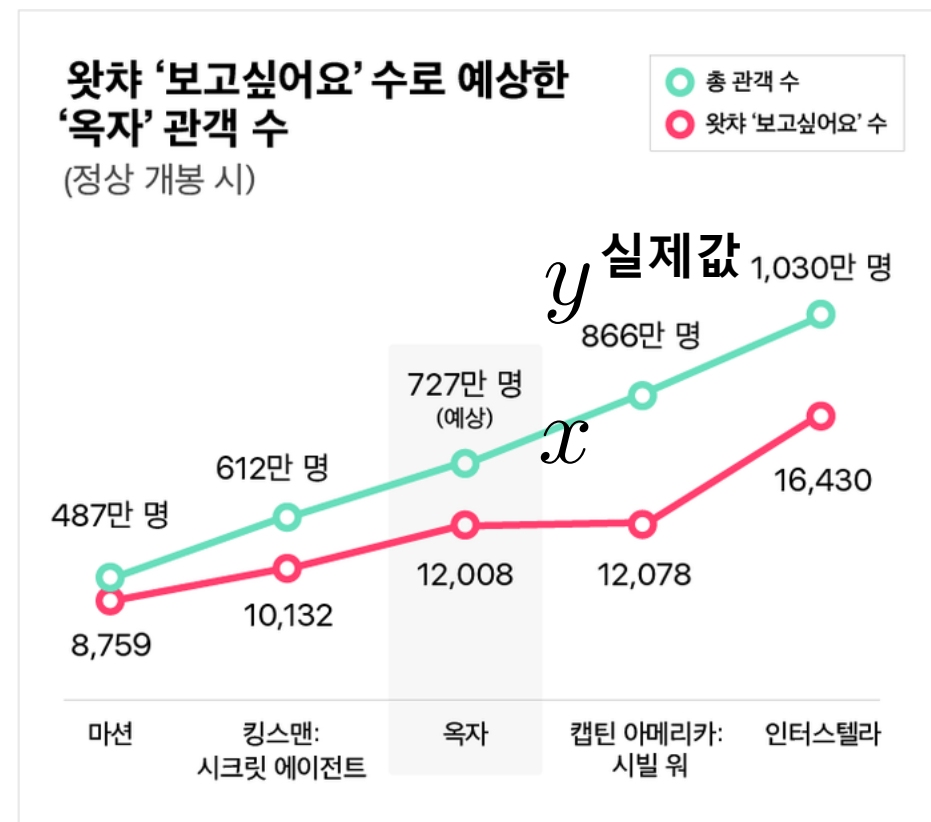
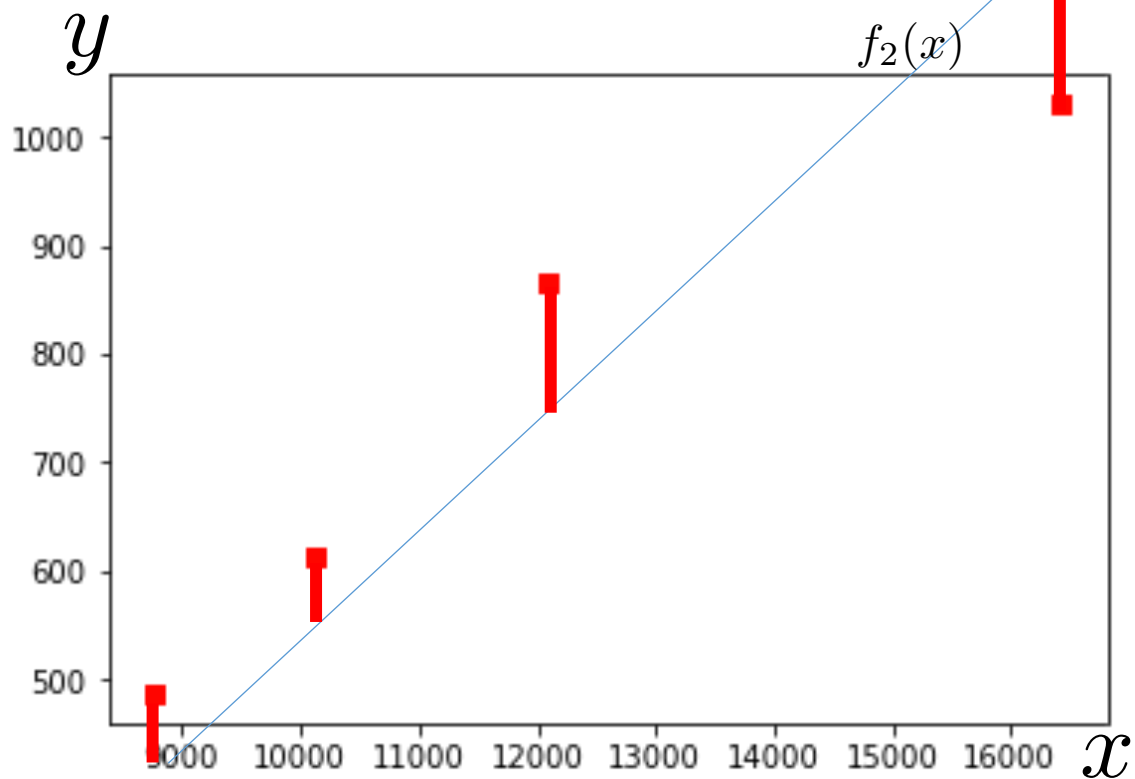
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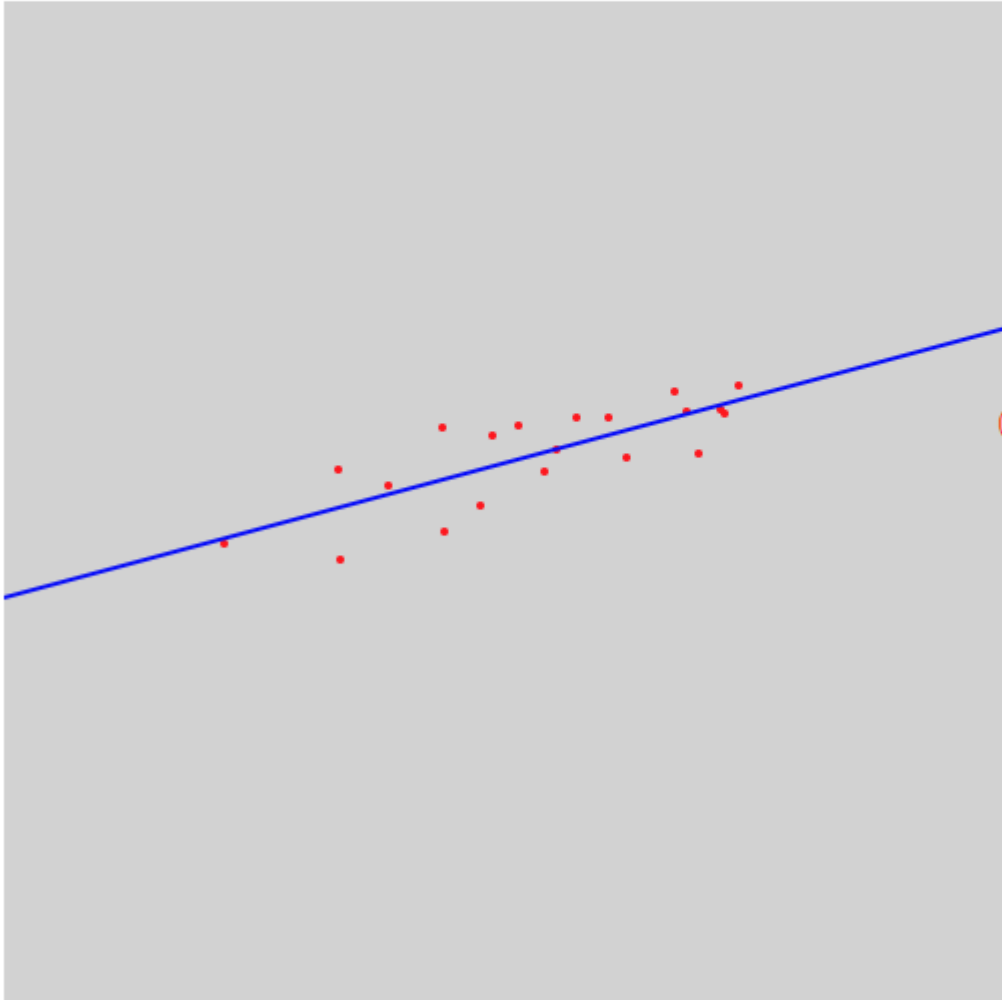


Source: <http://platum.kr/archives/83757>

- [Home](#)
- [Linear Regression - Ordinary Least Squares Method](#)

Linear Regression - Ordinary Least Squares Method

Y: $-0.26898102867433593x + 297.9945080961918$



<https://sujinleeme.github.io/javascript-machine-learning/linear-regression-ols>
<https://www.facebook.com/sujinlee.me>

**예측 함수와 실제 값의
오차를 줄여보자!**

오차의 합

$$(\hat{y}^{(1)} - y^{(1)}) + (\hat{y}^{(2)} - y^{(2)}) + (\hat{y}^{(3)} - y^{(3)}) + (\hat{y}^{(4)} - y^{(4)})$$

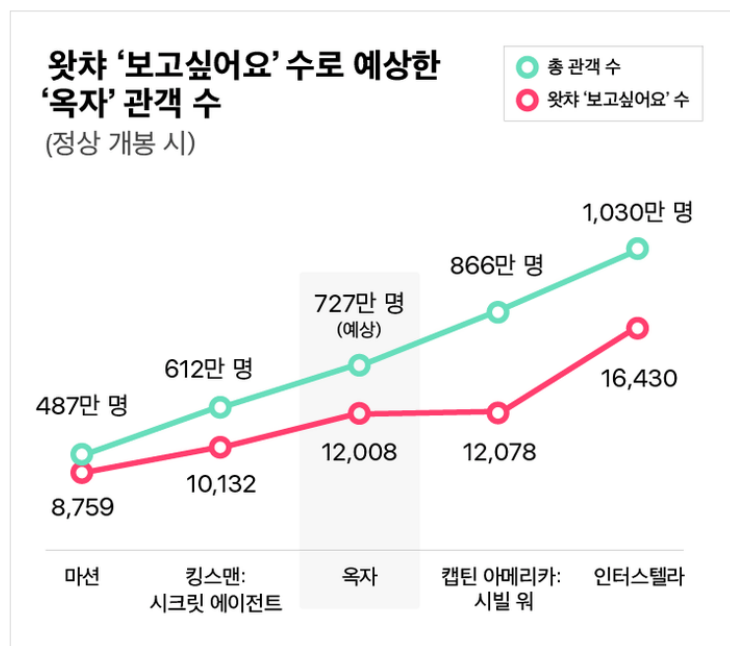
오차는 양수 또는 음수 가능 → 상쇄될 수 있음

$$(\hat{y}^{(1)} - y^{(1)})^2 + (\hat{y}^{(2)} - y^{(2)})^2 + (\hat{y}^{(3)} - y^{(3)})^2 + (\hat{y}^{(4)} - y^{(4)})^2$$

제곱의 합으로 변환

$$\sum_{i=1}^n (\hat{y}^{(i)} - y^{(i)})^2$$

$$\hat{y} = \begin{bmatrix} w_1 \times 8759 + w_0 \\ w_1 \times 10132 + w_0 \\ w_1 \times 12078 + w_0 \\ w_1 \times 16430 + w_0 \end{bmatrix} \quad y = \begin{bmatrix} 487 \\ 612 \\ 866 \\ 1030 \end{bmatrix}$$



$$(\hat{y} - y)^2 = \begin{bmatrix} (w_1 \times 8759 + w_0 - 487)^2 \\ (w_1 \times 10132 + w_0 - 612)^2 \\ (w_1 \times 12078 + w_0 - 866)^2 \\ (w_1 \times 16430 + w_0 - 1030)^2 \end{bmatrix}$$

Squared Error

**Squared Error를 최소화
할 수 있는 weight값의 발견**

$$\sum_{i=1}^n (w_1 x^{(i)} + w_0 \times 1 - y^{(i)})^2$$

최소 또는 최대의 문제 → 미분으로 해결하기

찾고자 하는 값은? w_1, w_0



Human knowledge belongs to the world.