

On the Origin of Shrimpluminescence

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[illegible]

I. INTRODUCTION

Snapping shrimp, like our cute friend in Fig. 1 (left), have long been known to produce cavitating bubbles by *snapping* their claws [1; 2; 3]. They have a strong appendage (the *dactyl*) in thier claw [Fig. 1 (center)] that is used to create a very high-velocity jet of water. The low pressure region in the jet’s wake forms a bubble [Fig. 1 (t=0 ms)] that, among other things, produces an exceptionally loud noise when it collapses. The sound (i.e. the pressure wave) produced by even a *single* shrimp’s snap is detectable over a mile away [4]. The noise produced by groups of shrimp is so intense that the U.S. Navy used them as “sonar-camouflage” in the Pacific ocean during World War II [1].

The shrimp were not patriots helping the war-effort, however; they snapped for food. The shock-wave produced by the cavitating bubble is used to stun and even kill prey [1]. If the shrimp’s prey had very sensitive eyes (and also were not dead) they might notice a flash of light is also produced through an effect referred to as “shrimpoluminescence” in the case of the pistol shrimp [2], but more generally known as *sonoluminescence*.

Sonoluminescence (SL) is more precisely defined as the process by which a “driven gas bubble collapses so strongly that the energy focusing at collapse leads to light emission” [5]. Sonoluminescence comes in two forms: (i) single-bubble sonoluminescence and (ii) multi-bubble sonoluminescence. The distinction is self-explanatory: multi-bubble sonoluminescence (MBSL) consists of “the simultaneous creation and destruction of many separate, individual cavitation bubbles” [5; 6], whereas in single-bubble sonoluminescence (SBSL), rather obviously, only a single bubble is present [7]. The discovery of MBSL predates SBSL by ~ 60 years but due to the more-or-less random and fleeting nature of the bubbles, SL in general wasn’t well studied until the early 1990’s when it was discovered that single bubbles could

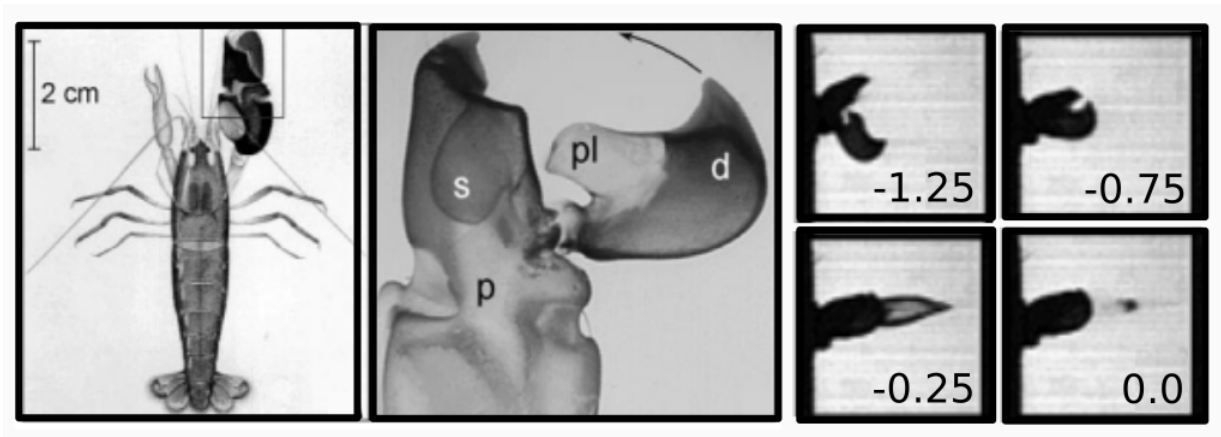


FIG. 1 (left) Snapping shrimp (*Alpheus heterochaelis*). (center) Blown-up view of the shrimp's claw. The *plunger* (pl) on the *dactyl* (d) rapidly enters the *socket* (s), ejecting a high-velocity jet of water. The water ejection and subsequent bubble formation and, finally, bubble collapse (at $t=0$) are shown on the right. The units are ms. Adapted from ref. [1]

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be created and periodically driven to produce light very high precisions [5; 6; 7; 8]. We will discuss MBSL briefly later, but for now it suffices to say that nearly all theoretical and experimental progress has been made using SBSL, with some authors even calling it “the hydrogen atom of sonoluminescence” [6; 9].

The discovery of SBSL created a rush of effort to explain the phenomena with arguments ranging from the simplest models ¹ to more exotic explanations based of quantum field theory [10; 11; 12].

But besides the obvious case of shrimpluminescence, why is SL interesting? Well, at a glance, it is not obvious why SL occurs. The acoustic wave in the liquid displaces molecules on the order of nanometers, costing an elastic energy of $\sim 1 \times 10^{-12}$ eV/molecule while emitting visible light (through e.g. electronic transitions) costs an energy ~ 1 eV/molecule [6; 9]... there is a 12-orders-of-magnitude concentration of energy. That is huge! Estimates of the temperature at the center bubble are ...

After 3 decades of studying SBSL, the physical mechanism of light production in SL is still not understood. This can be seen by glancing at the literature and noticing that there are many recent papers with different arguments for *where* ² the light comes from [13; 14; 15; 16]. Numerous aspects of the process are conveniently accessible to the experimentalist, while at the same time the theory of the bubble’s interior is quite mature. Many theories require experimental inputs as parameters, while in other cases experimental results are indirectly *inferred* by fitting to a theory. Put simply, the history of studying SBSL is a rather beautiful example of the scientific process of explaining nature. According to Brenner “SBSL has become a rather sophisticated testing ground for the ability of mathematical models and numerical simulations to explain detailed experimental data from a complicated physical process” [5].

The goal of this paper is to catch the reader up on recent efforts to explain SBSL. While the author of this paper is particularly excited about shrimpluminescence, it is important to stress that this work will focus on SBSL in general. It is apparently simpler to create and characterize SBSL in the laboratory without involving shrimp (for example, convincing the shrimp to snap requires tickling them [1; 2; 9]), so practically all work to study SL has not involved shrimp ³. Also notably absent will be any detailed discussion of MBSL since this will take us too far afield. Instead, we will summarize the history of SBSL research up to now starting at the discovery of MBSL leading to the subsequent discovery of SBSL and a rush of effort to explain it. We will explore both the experimental and theoretical discoveries along the way. Finally, we will review the current state of agreement between what is known experimentally and theoretically about SBSL.

II. HISTORICAL OVERVIEW

SL was discovered by accident in 1933 (in the form of MBSL) by Marínescu and Trillat [17] and was subsequently characterized by Frenzel and Schultes [18] ⁴ Marínescu et al. were trying to accelerate photo development by *insonating* developing fluid. They discovered that a photosensitive plate immersed in the insonated fluid became “foggy” which they attributed to exposure to light. Shortly after, Frenzel et al. repeated the experiment and confirmed that the insonated fluid emits light in the form of a faintly glowing cloud of bubbles.

This result was not particularly surprising to the community since it had been known for a while that cavitating bubbles could do tremendous damage to e.g. ships propellers. The discovery’s impact is concisely summarized by Brenner: “if the cloud [of cavitating bubbles] collapses violently enough to break molecular bonds in a solid, why should it *not* emit photons” [5]. In fact, cavitating bubbles had been of interest to engineers working on fluid mechanics for a while. The discovery of cavitation is credited to Euler (as early as 1754) who hypothesized that if the velocity in a fluid was large enough, negative pressures could become so large as to “break the fluid” [7; 19] and was confirmed to exist (and named “cavitation”) in 1895 by engineers studying the failure of a British Navy ship’s propeller [19]. Shortly after, Lord Rayleigh wrote down and solved the differential equation for a vapor filled cavity collapsing in water (the so-called Rayleigh equation), giving the first rigorous theoretical treatment of cavitation [20]. Rayleigh found that, for a bubble at a lower pressure than the surrounding fluid (and both pressures held constant), the bubble wall diverges during collapse. Still, very little information was accessible about the light emission until the 1990’s when stable, single bubbles could be created and driven to emit light [6; 7; 8]. With this discovery, serious interest took root.

¹ There are far too many to try list and we will not be interested in the vast majority of early models which are now irrelevant. References to these can be found in Gaitan [8] and Brenner et al. [5].

² We emphasize “where” since it’s not even certain if the light is *surface* or *volumetric* emission, i.e. it is literally not known *where* the light comes from [].

³ With notable exceptions [3]

⁴ Neither the paper due to Marínescu et al. nor the one due to Frenzel et al. can be found by the author; in any case he can’t read French or German so having the papers wouldn’t be much use. As such, the story of how the effect was discovered is taken from more recent sources whose authors hopefully could read French and German [5; 6; 8]

Details of a typical SBSL experiment will be given later, but for now it suffices to note that SBSL, unlike previous studies on MBSL, allowed very precise control and measurement of the SL process. With unprecedented experimental control, many discrepancies in previous assumptions about SL were discovered. Experiments measuring the duration of the light pulse found that it was orders of magnitude smaller than the time in which the bubble was compressed to its smallest radius [21; 22]. This discovery implied that SL was nearly decoupled from the bubble’s dynamics, contradicting models based on Rayleigh’s equation. New models were proposed based on *converging shock waves* at the bubble’s center with estimates of the temperature at the center of bubbles $\sim 10^8$ K [23; 24]. At the same time, experimentalists fit the bubble’s light emission spectra as a *black body emitter* and concluded that the temperature in the bubble was at least 25,000 K [25].

These very high estimates for the temperature in the bubbles lead to a spark of interest more broadly: if the temperature in the bubble were really that large, then it should be possible for nuclear *fusion* to occur []. **talk about the stupid ass movie and that asshole that faked science data.** Now talk about sonochemistry etc.

III. WHAT DO WE KNOW?

A. The Bubble Wall

As it turns out, the dynamics of the bubble in SBSL (regardless of the light emission) are quite well described both qualitatively and *quantitatively* by the classical theory of bubble dynamics. This isn’t particularly surprising since the light emission and bubble collapse occur at different timescales []. The starting point for any theory of the bubble dynamics is Rayleigh’s original expounded upon by many others []: the so called “the Rayleigh-Plesset” (RP) equation ⁵:

$$B = Dlololol \tag{1}$$

B. Experimental Results

what conditions are necessary for light emission (i.e. what is the phase space [9]):

- Ar content
- driving frequency
- P_{max}
- ...

⁵ The RP equation is derived from the Navier-Stokes equation in the appendix

IV. WHAT DON'T WE KNOW

A. The Bubble Wall (Again)

B. Experimental Anomalies

V. LET THERE BE LIGHT!

A. Thermal Arguments

B. Electric Arguments

C. The Casimir Effect

D. The Casimir Argument

VI. SUMMARY

VII. ACKNOWLEDGMENTS

Appendix A: The Rayleigh-Plesset Equation

The Rayleigh-Plesset (RP) equation can be deduced from the compressible Navier-Stokes equations []. To that end, we first remind the reader of the Navier-Stokes equations.

The *total* change (in time) of mass in an arbitrary element of a fluid (whose coordinates and boundary may depend on time) is given by $\frac{d}{dt} \int_{\Omega_t} \rho dV$ where Ω_t is the domain of the fluid element under consideration and $\rho(\mathbf{x}, t)$ is the local, time-dependent density of the fluid. Using the transport theorem of fluid dynamics [26], Gauss's theorem, and (with only some loss of generality) taking Ω_t to be a *fluid parcel* (so that the boundary of the fluid parcel, $\partial\Omega_t$, moves with the fluid's velocity, $\mathbf{u}(\mathbf{x}, t)$), this becomes

$$\frac{d}{dt} \int_{\Omega_t} \rho dV = \int_{\Omega_t} \frac{\partial \rho}{\partial t} dV + \int_{\partial\Omega_t} \rho \mathbf{u} \cdot \mathbf{n} dA = \int_{\Omega_t} \frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) dV. \quad (\text{A1})$$

Now to have *mass-continuity*, which we will require on physical grounds, we set eq. A1 to 0. Basically, we are saying no additional material is being added or removed from the fluid. Since the fluid parcel's boundary Ω_t is arbitrary, we find that $\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) \equiv 0$ which is true for every point in the fluid volume.

Newton's second law for fluids (*momentum-continuity*) is defined similarly. We write the momentum-density as $\rho \mathbf{u}$ with momentum given by $\int_{\Omega_t} \rho \mathbf{u} dV$. To simplify what follows, we focus on only the i^{th} component of velocity at a time. Then Newton's second law can be written as

$$\frac{d}{dt} \int_{\Omega_t} \rho u_i dV = \int_{\Omega_t} \frac{\partial(\rho u_i)}{\partial t} dV + \int_{\partial\Omega_t} \rho u_i (\mathbf{u} \cdot \mathbf{n}) dA = F_i. \quad (\text{A2})$$

Now using Gauss's theorem, the product rule, and mass-continuity we find $\frac{d}{dt} \int_{\Omega_t} \rho u_i dV = \int_{\Omega_t} \rho \frac{du_i}{dt} dV = F_i$. In vector notation this reads

$$\int_{\Omega_t} \rho \frac{d\mathbf{u}}{dt} = \mathbf{F} \quad (\text{A3})$$

Now let us separate the forces into *body-* and *surface-forces*: $\mathbf{F} = \int_{\Omega_t} \mathbf{f}_B dV + \int_{\partial\Omega_t} \mathbf{f}_S dA$. If we only consider an ideal fluid, the surface part can be written as $\int_{\partial\Omega_t} \mathbf{f}_S dA = - \int_{\partial\Omega_t} p \mathbf{n} dA = - \int_{\Omega_t} \nabla p dV$ with p the pressure and the minus sign being due to the sign convention: *out* of the surface $\partial\Omega_t$ is positive. If instead the fluid is real, we can't neglect viscous forces. We suppose that viscous surface term can be represented by a tensor, $\boldsymbol{\tau}$, such that $\mathbf{f}_S = -p\mathbf{n} + \boldsymbol{\tau} \cdot \mathbf{n}$ with diagonal elements of $\boldsymbol{\tau}$ the *normal* viscous stresses and the other components being *shear* stresses. Note here that $\boldsymbol{\tau} \cdot \mathbf{n}$ denotes matrix multiplication. It is conventional to combine the pressure and viscous stresses into a single entity called the *stress-tensor*. We denote it by $\boldsymbol{\sigma} = -p\mathbf{I} + \boldsymbol{\tau}$.

The components of the viscous stress tensor $\boldsymbol{\tau}$ can be deduced from Newton's law of viscosity and combined with

symmetry of the tensor itself [26]. We quote the results here ⁶:

$$\tau_{ii} = 2\eta \frac{\partial u_i}{\partial x_i} \quad (\text{A4})$$

$$\tau_{ij} = \mu \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right). \quad (\text{A5})$$

The body-force density, \mathbf{f}_B , is due to forces acting in the bulk of the liquid e.g. gravity, electrostatic forces, etc. and is typically from sources external to the liquid. Then the total force on a fluid element is $\mathbf{F} = \int_{\Omega_t} \mathbf{f}_B + \nabla \cdot \boldsymbol{\sigma} dV$. We can succinctly summarize the momentum-continuity equation as

$$\int_{\Omega_t} \rho \frac{d\mathbf{u}}{dt} - \mathbf{f}_B - \nabla \cdot \boldsymbol{\sigma} dV = 0 \quad (\text{A6})$$

which is equivalent to $\frac{d\mathbf{u}}{dt} = \frac{1}{\rho} [\mathbf{f}_B + \nabla \cdot \boldsymbol{\sigma}]$.

We would rather have an equation explicitly involving the velocity field \mathbf{u} . To that end, let us work out the stress term.

⁶ We are assuming an *isotropic* fluid so that the the viscosities η, μ are the same in all directions. This is true for water.

Appendix B: random notes

argon flash: a method of 'imaging explosions' similar to why argon is more useful for SBSL. argon has no internal DOF whereas air (i.e. N₂, O₂, water vapor) does and energy from explosions is absorbed dissociating bonds. argon, instead, becomes 'hotter' and emits more light, making photographing explosions easier. see wikipedia article "argon flash"

some dickheads 3d printed a shrimp claw and it also shrimpluminesces [3]

apparently a shitty movie called 'Chain Reaction' with Keanu Reeves was centered around the premise of MBSL as a means of clean energy production. it was based on the speculation that temperatures inside the bubbles could reach up to millions of Kelvin and lead to fusion. this was debunked by Prosperetti (see the pop sci article [27]). He points out that the temp is speculative and is based on assumptions of a perfect sphere collapsing. he notes that its probably not spherical when light is produced and even points out that groups have tried to produce fusion power by intentionally collapsing gas filled micro balloons with lasers... and failed. Tatartchecko also shows that this is horsehit [16]. in this article, Prosperetti also explains how a 'jet' of water whooshing across the bubble could be going faster than 4000 mph, fast enough to cause non-newtonian fracturing of the water leading to light production through (apparently) the same mechanism of light emission when ice or mint-o-green mints are snapped in half... huh. this is good introduction fodder. need to find the primary lit.

for fusions, also see wikipedia article on 'bubble fusion' and 'Rusi P Taleyarkhan'. Ruse was some asshole prof at purdue that claimed fusion occurred inside cavitating bubbles, but it was later found out that the faked data and interfered with peer reviews leading to him being fucking fired.

heuristic explanation of bubble trapping given by Brenner in [27].: the bonds between molecules in a fluid are very strong, so instead of 'tearing', the fluid stretches. however, if there is a bubble present, the local dilation of the fluid can change the bubbles diameter by ~ 1000 times to avoid breaking bonds at the interface between bubble and fluid. But when the compression waves comes by, the 'gas' in the bubble, which has boiled due to low pressure, offers very little resistance to compression. the wave compresses the bubble rapidly, which spikes the temp in the gas to incandescent temperatures. this heuristic explanation is on-track with Crum [6] below.

Appendix C: 1st discovery

MBSL was discovered first. its (obviously) hard to create and control single bubbles so this wasnt feasible until the 1990s, attributed to Gaitan (see below). allegedly, it was Marinesco et al [17] that discovered MBSL in 1933 (according to [8] below and to [16]) but I cant find this paper (or understand it since its in french). Other sources (e.g.. wikipedia, [6; 16]) credit Frenzel et al [18] as the discoverers. I cant German or find this paper either, but in anycase, Tatartchenko summarized thier discovery: Frenzel and coworkers were trying to speed up photo development by 'insonating' i.e. subjected developer-fluid to sound. they found that when they immersed photo-plates or whatever in the fluid, it became 'foggy' and overexposed, as if subjected to diffuse light. A bunch of other papers followed up on this. get the deets from [8] below.

Update: Brenner [5] consisely summarizes the history: Marinesco notes the photographic plates fogs in an ultrasonic bath [17] and Frenzel et al [18] deliberately studied the light emission. According to brenner, no one was surprised by this since it was already known that cavitating bubbles fuck shit up.

SBSL was discovered by Gaitan [7; 8] etc. who trapped a single air bubble in a water filled flask using piezoacoutics stuck to the outside. (note: the trapping force is called *Bjerknes force*, refs in [9]).

Appendix D: notes from [6]

pop sci type of magazine article. Gives heuristic expanation: When an intense sound field is produced within a liquid, microscopic cavities of gas or vapor can be generated when the liquid fails under tensile stress. The subsequent acoustic compression cycle forces these cavities to collapse violently, which results in a remarkable concentration of mechanical energy, estimated to be as high as 12orders of magnitude (refs are given too). Also notes that MBSL is very hard to study since the bubbles occur randomly and transiently. Describes SBSL as the *hydrogen atom of sonoluminescence*.also discusses that attempts to measure the (time) interval over which light is produced have found it be less than ~ 50 ps which is 1/1000 times smaller than theory predicts. They also found the light to be more 'stable' than the acoustic generator, i.e. more regular with more controlled intervals. an old but probably still relevant

result. mentions a neat claim that the conditions of the gas at the center of the bubble are probably more like a metal than a gas. hell, this article basically summarizes all of the anomalies present in 1994. a very good resource.

Appendix E: notes from ref [9]

SBSL was discovered by Giatan et. al. in 1990s at U. Mississippi [6; 7; 8] (note, [7] has ~1000 citations..). The SBSL experiments were done by sticking peizoacoustic transducers to the outside of a water filled glass. the 'Bjerknes' force traps the bubble and the acoustic wave drives its expansion/collapse. What Gaitan saw was that even the single bubble emits light. Wow! This was baffling since 'acoustic energy' (i dont understand this) is on the order of $\sim 10^{-12}$ eV/molecule while visible light is ~ 1 eV. NVM: I do get this. Typical acoustic waves, e.g. in air, only displace molecules on the order of nanometers, which aquires an elastic energy gain between molecules of $\sim 10^{-12}$ eV/molecule: certainly not enough to excite an electronic transition.

This paper refs the review by Prosperetti: [28]. This paper gives EOM for the bubbles radius, the so called *Plesset-Rayleigh* equation which I have seen everywhere related to bubbles. Talks about solving it, some other crap related to bubble dynamics. this requires a detailed re-read.

Later in the paper, also revisits snapping shrimp.

Appendix F: notes from ref [29]

has shit tons of relevant math. take a look. a pretty paper overall

Appendix G: notes from [8]

disseration by Giatan who is credited with discovering SBSL. says apparently SL was discovered in 1933. need to go read this crap. Apparently this was by Marinesco et. al. in 1933. Zimakov tried to explain it in 1934 and concluded that the light was due to electric discharge between vapor cavities and the glass container. Frenzel and Schultes in 1935 instead claimed it was from friction between cavitating bubbles and the water. Chamber in 1936 studied SL in other nonwater liquids. Chamber also postulated the light was from 'tribolumiscence' which occurs when the crystalline structure of the liquid-bubble lattice collapses? Apparently something similar occurs in real crystals. ... shit, a bunch more models are given. give this dis. a lot of attention.

also says cavitation was predicted by 'Euler' in 1754: *if the velocity of a fluid is high enough, negative pressures can form and the liquid can 'break'*. the 'breaking' was called cavitation in 1895 by R.E. Froude, whoever the fuck this is, when studying bubbles near propellers. Rayleigh, unsurprisingly, was the first to give a rigorous theoretical treatment of cavitation in 1917.

Appendix H: notes from [5]

defines SBSL as "Single-bubble sonoluminescence occurs when an acoustically trapped and periodically driven gas bubble collapses so strongly that the energy focusing at collapse leads to light emission".

Appendix I: QED

the ref [12] has lots of good refs. they have follow up papers extending Schwingers papers (which are refd therein) and referencing a bunch of other relevant literature. I should look for refs citing Schwingers paper to try to figure out the modern state of the art of this thin.

Appendix J: Modelling

in the ref [30], they use MD to modelling the equation of state for a collapsing bubble. they calculate the temperature and study the conditions for emitting light.

Appendix K: Refs. to different arguments

ref [31] gives examples of other origin theories (molecular excited states, black-body radiation, bremsstrahlung, ion-electron recombination, confined electrons)

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