



$$\frac{dL}{dx} = 1$$

$$\frac{dxy}{dx} = y$$

$$\frac{d^n}{dx^n} = n \times x^{n-1}$$

$$\frac{d \sin(x)}{dx} = \cos(x)$$

$$\frac{d e^x}{dx} = e^x$$

$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$

$$\frac{d \text{sigmoid}(x)}{dx} = \text{sigmoid}(x) \times (1 - \text{sigmoid}(x))$$

$$\frac{d \tanh(x)}{dx} = (1 - \tanh^2(x))$$

$$\frac{d}{dx} [f(u)] = \frac{d}{du} [f(u)] \frac{du}{dx}$$

$$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial O_8} \cdot \frac{\partial O_8}{\partial O_7} \cdot \frac{\partial O_7}{\partial O_6} \cdot \frac{\partial O_6}{\partial O_5} \cdot \frac{\partial O_5}{\partial O_4} \cdot \left(\frac{\partial O_4}{\partial O_3} \cdot \frac{\partial O_3}{\partial O_1} \right) \cdot \frac{\partial O_1}{\partial w_1}$$

$$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial O_{17}} \cdot \frac{\partial O_{17}}{\partial O_{16}} \cdot \frac{\partial O_{16}}{\partial O_{15}} \cdot \frac{\partial O_{15}}{\partial O_{14}} \cdot \frac{\partial O_{14}}{\partial O_{12}}$$

$$1) \frac{\partial (y - O_8 - O_{17})^2}{\partial O_8} = -2 (y - O_8 - O_{17})$$

$$\frac{\partial L}{\partial O_{17}} = -2 (y - O_8 - O_{17})$$

$$2) \frac{\partial O_8}{\partial O_7} = \frac{d(\tanh O_7)}{dO_7} = 1 - \tanh^2(O_7)$$

$$\frac{\partial O_7}{\partial O_6} = w_9$$

remaining derivatives

- remaining derivatives
- 3) $\frac{\partial O_7}{\partial O_6} = 1$
 - 4) $\frac{\partial O_6}{\partial O_5} = e^{O_5} \Rightarrow O_6$
 - 5) $\frac{\partial O_5}{\partial O_4} = 1$
 - 6) $\frac{\partial O_4}{\partial O_3} = \frac{dO_3^2}{dO_3} = 2O_3$
 - 7) $\frac{\partial O_3}{\partial O_1} = 1$
 - 8) $\frac{\partial O_1}{\partial w_1} = f_1$

$$\frac{\partial O_3}{\partial O_2} = 1$$

$$\frac{\partial O_2}{\partial w_2} = f_2$$

$$\frac{\partial O_{16}}{\partial O_{15}} = \frac{\partial (\text{sig}(O_{15}))}{\partial O_{15}} = \text{sig}(O_{15})(1 - \text{sig}(O_{15}))$$

$$\frac{\partial O_{15}}{\partial O_{14}} = 1$$

$$\frac{\partial O_{14}}{\partial O_{12}} = O_{13}$$

$$\frac{\partial O_{12}}{\partial O_9} = \cos(O_9)$$

$$\frac{\partial O_9}{\partial w_2} = f_3$$

$$\frac{\partial O_{14}}{\partial O_{13}} = O_{12}$$

$$\frac{\partial O_{13}}{\partial O_{11}} = 1$$

$$\frac{\partial O_{13}}{\partial O_{10}} = 1$$

$$\frac{\partial O_{10}}{\partial w_4} = f_4$$

$$\frac{\partial O_{11}}{\partial w_5} = f_5$$