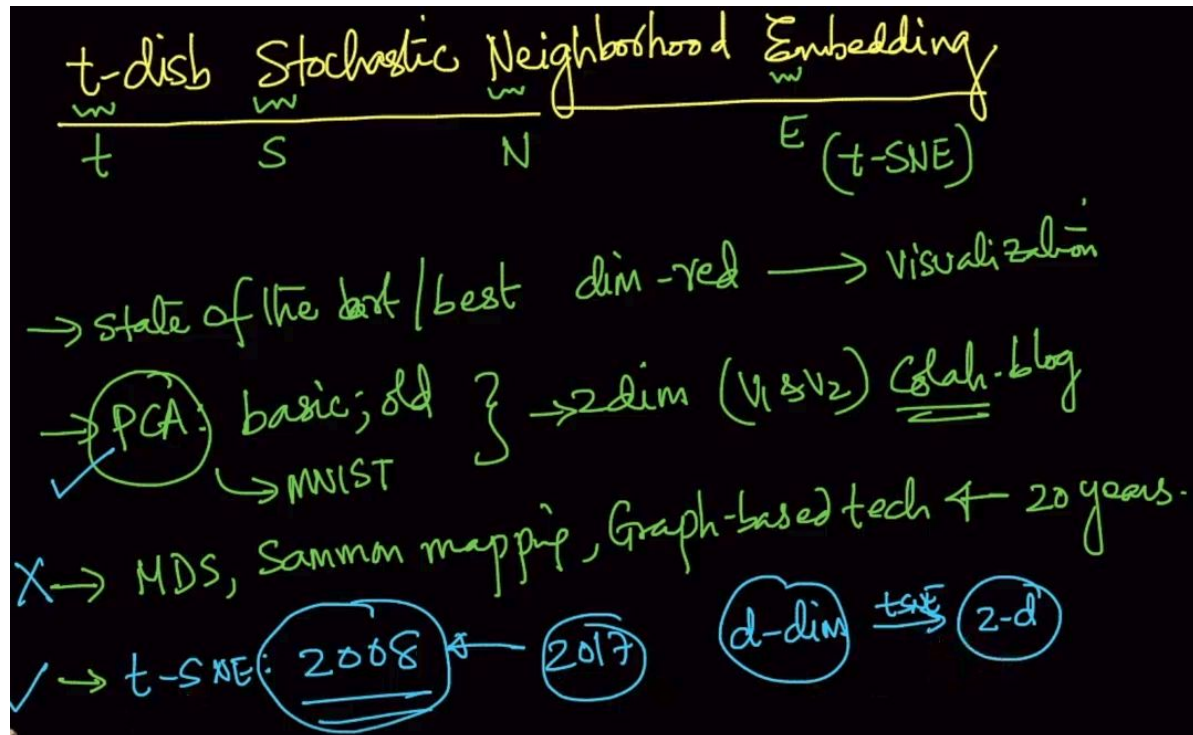
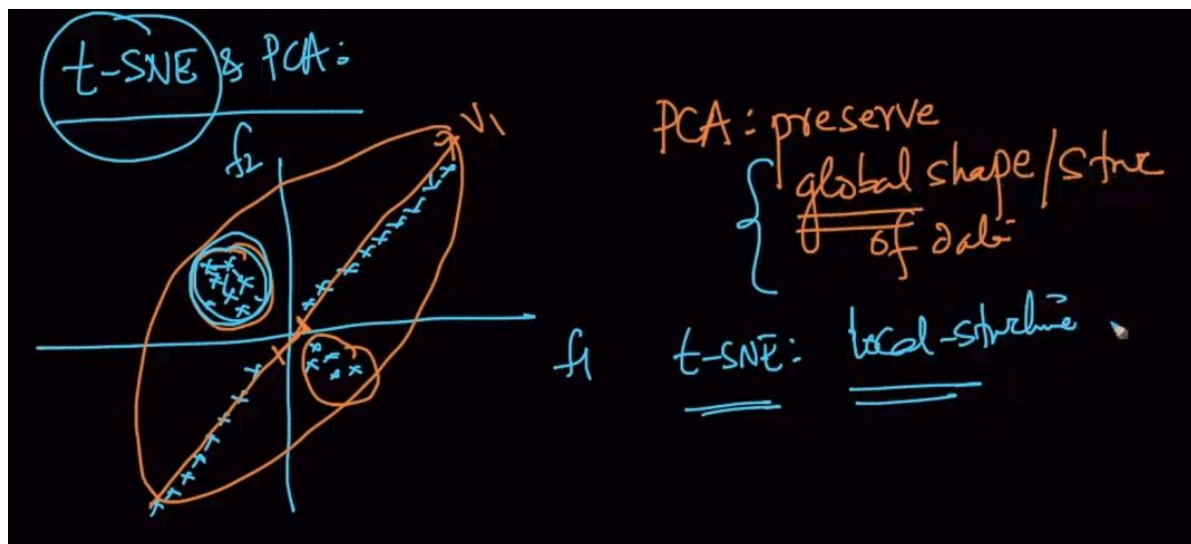


## t-SNE (T-distributed Stochastic Neighborhood Embedding)



t-SNE is state of the art / best dimensionality reduction technique for visualization.

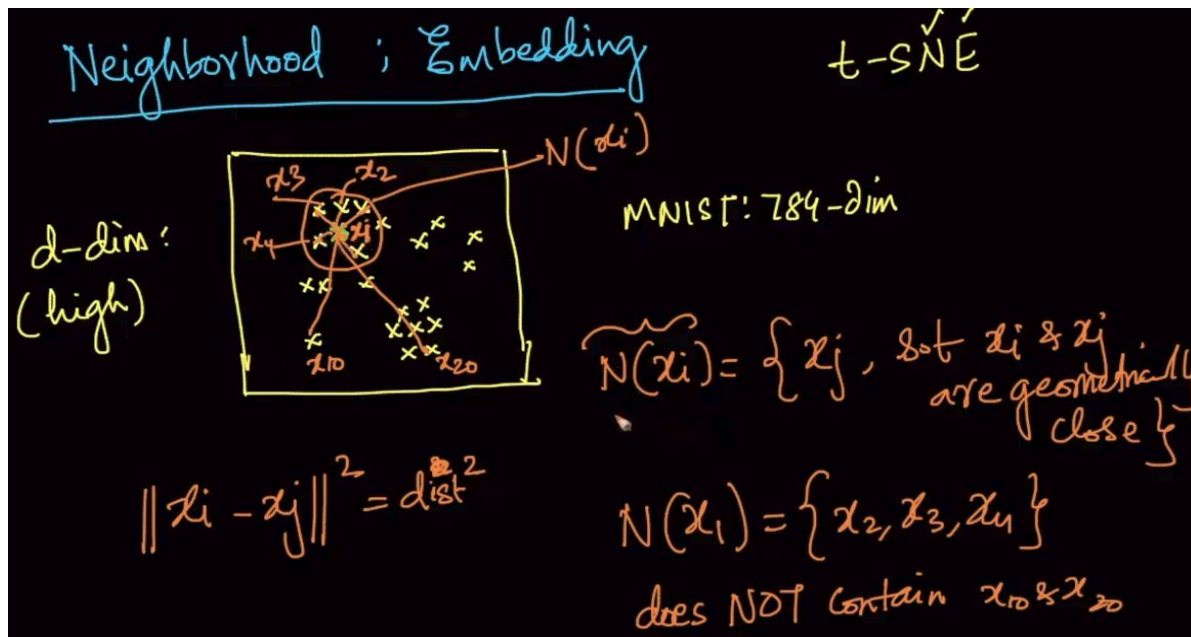
### DIFFERENCE BETWEEN PCA AND t-SNE



PCA : Preserves global shape/structure of data

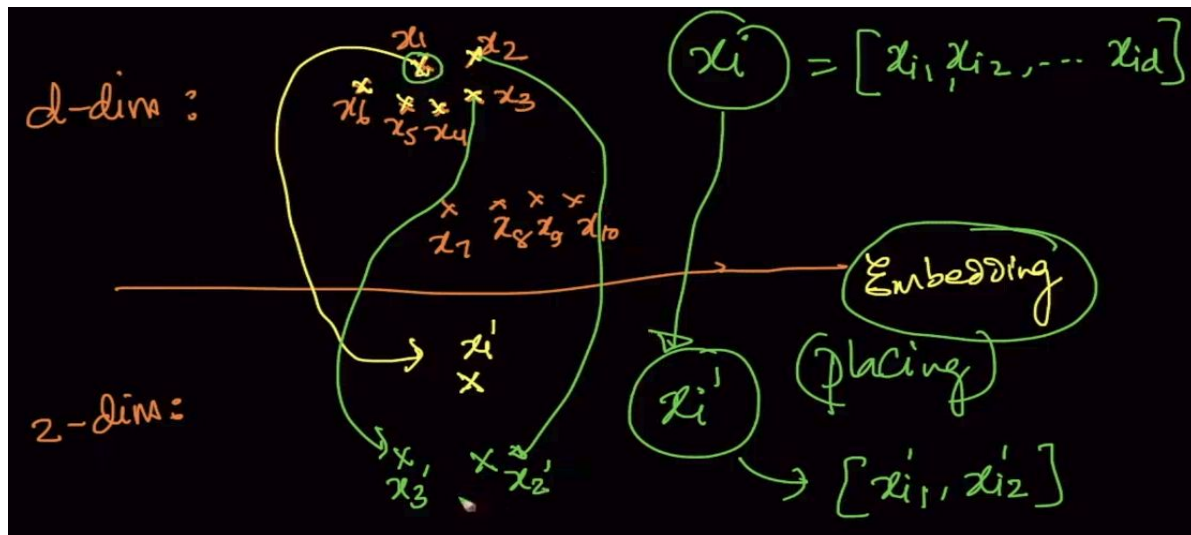
t-SNE : Local Structure

## NEIGHBORHOOD



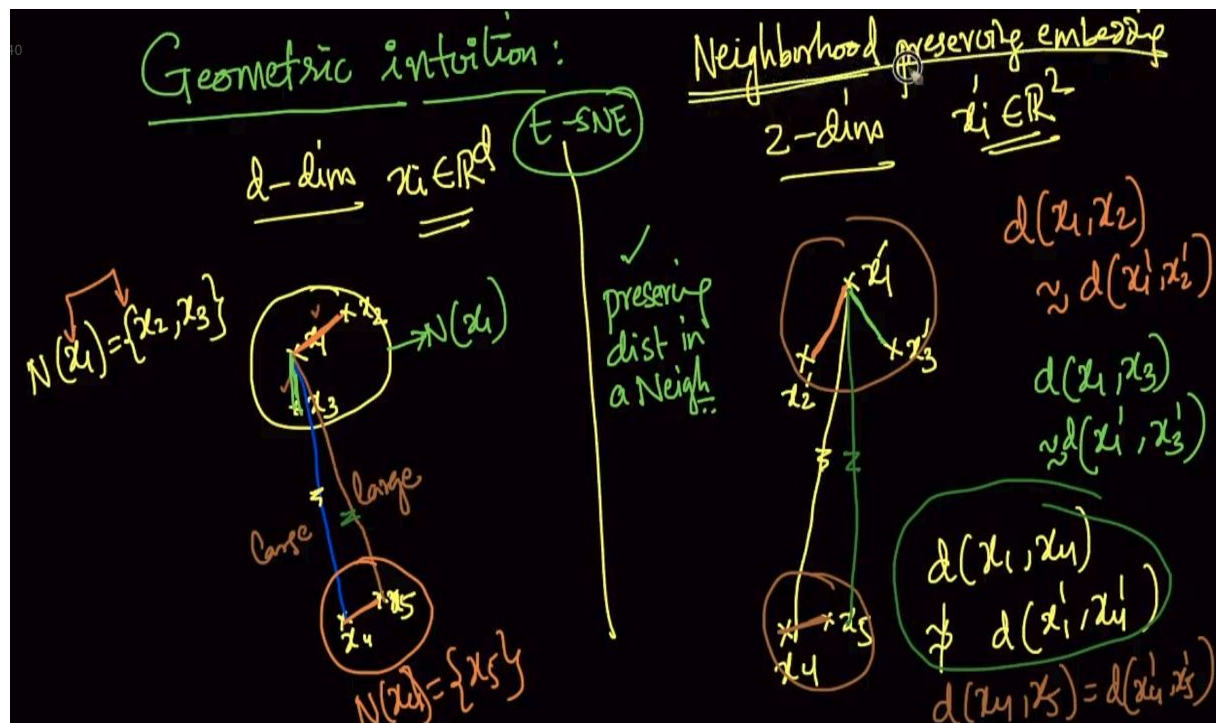
Neighborhood (N) is all the points that are closer to the data point/ Distance between datapoints is small. Here,  $x_i$  a data point and it's  $N = \{x_2, x_3, x_4\}$

## EMBEDDING



Embedding means taking a datapoint in a high dimensional space and placing it in a low dimensional space/ finding corresponding point in low dimensional space.

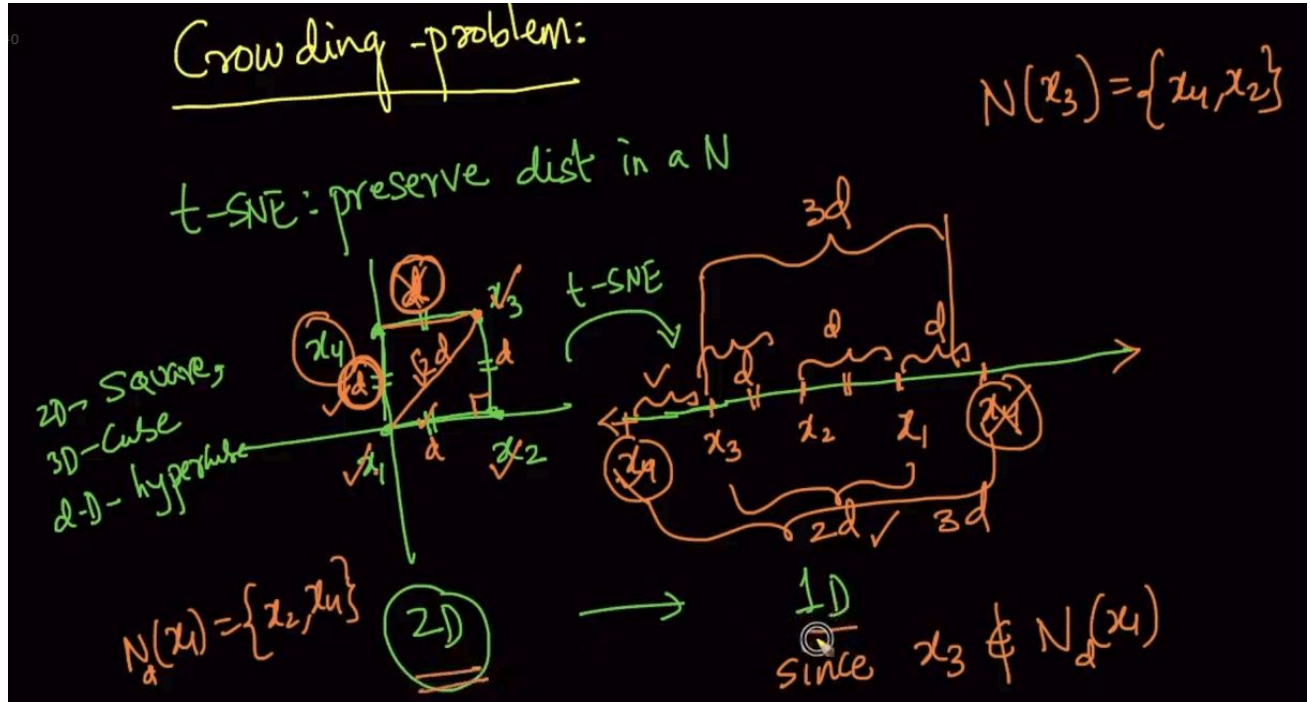
## GEOMETRIC INTUITION of t-SNE



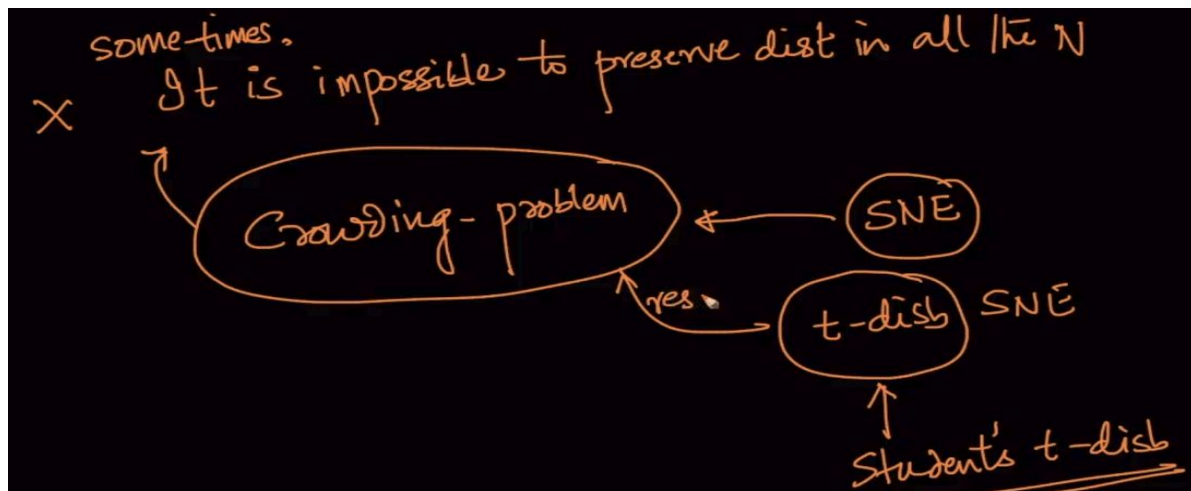
Suppose we have a  $d$ -dim data as shown and we are embedding it in 2-d. The neighborhood  $N(x_1) = \{x_2, x_3\}$  so when we are looking to embed them we try to preserve their neighborhood as seen above but for the data points which are farther like  $x_4, x_5$  it doesn't guarantee to preserve its distance.

**Mathematical Intuition:** Fairly advanced math so it is postponed.

## CROWDING PROBLEM



We are trying to embed 2-d to 1-d . So we are placing points to preserve their distances at distance  $d$  from  $x_1$  as seen  $N(x_1) = \{x_2, x_4\}$  but when doing it the  $d$  of  $x_4$  becomes greater from  $x_3$  and the distance isn't preserved . Same if we try to preserve from  $x_3$  . It won't be preserved from  $x_1$ .



Impossible to preserve distance in all the distances .It is called crowding problem which is solved by t-disb



## How to apply t-SNE and interpret its output

**(\*) Never run t-SNE just once**

popular: it's incredibly  
other dimensionality-  
that very flexibility makes it  
; the algorithm makes all  
tions. Don't let the hidden  
nique, though. The good  
in simple cases, it's possible

- 1) run steps/iter  
till shapes  
stabilize
- 2) perplexity  $2 \leq p < n$
- 3) re-run t-SNE  
p, step  
→ stable or not

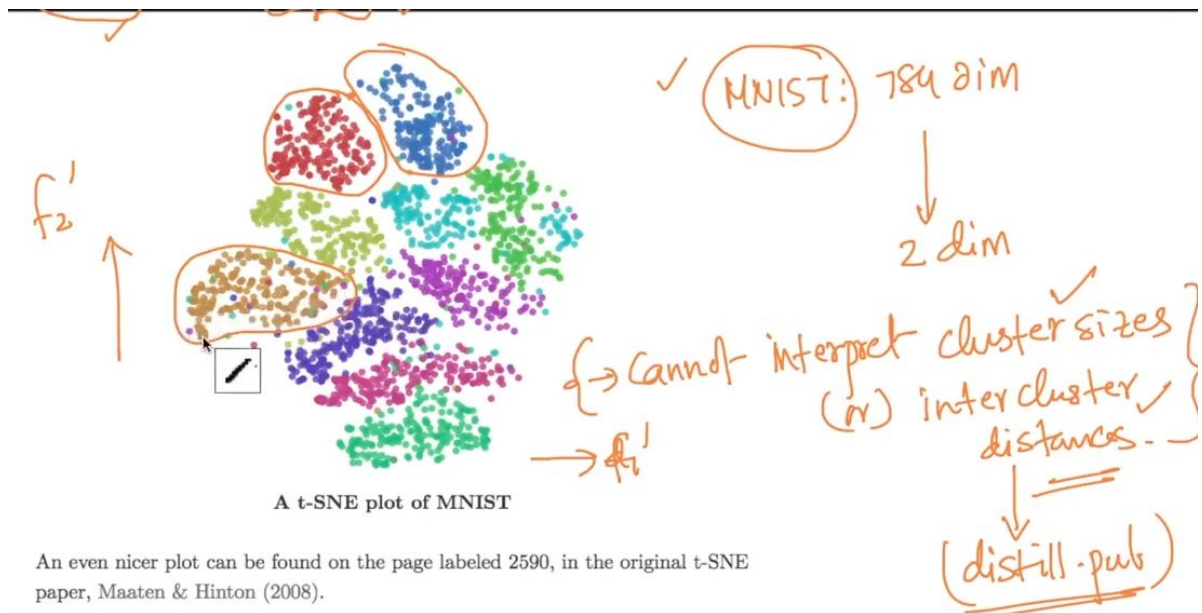
Perplexity : It is nothing but the no. of near data points taken as mentioned

Example: If perplexity is 5 then 5 nearest data points are taken when running t-SNE

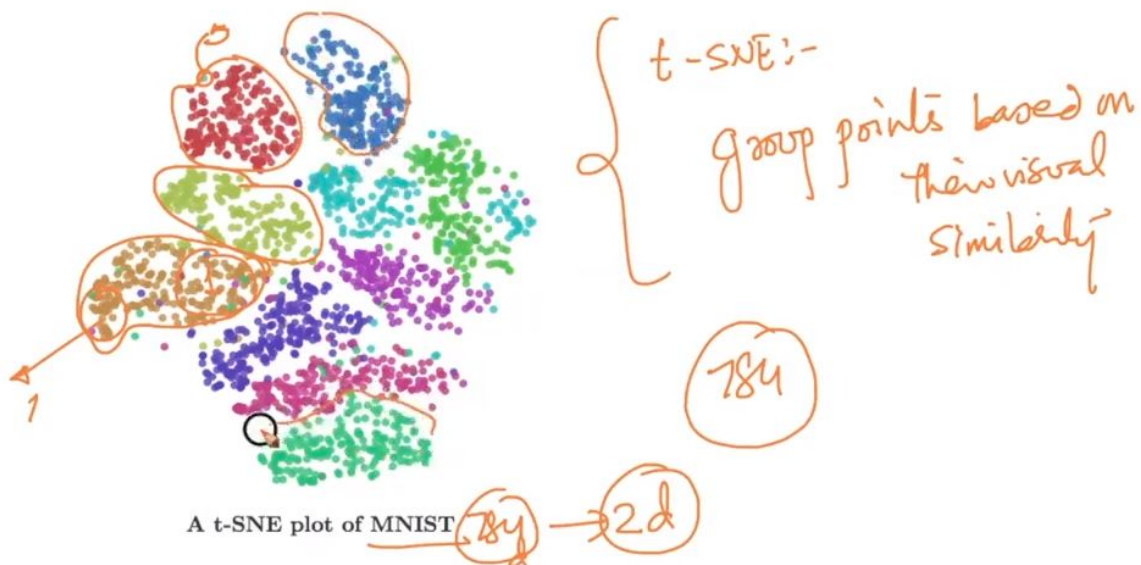
[t-SNE visualize video](#)

[t-SNE visualize blog](#)

## t-SNE on MNIST



It is separating clusters well but we cannot interpret cluster sizes or intercluster distances



After running t-SNE on MNIST we can see that slanted 1's (1) are grouped together and straight 1's are clustered together as well. So it group points based their visual similarity