



STATISTICAL THINKING IN PYTHON I

Probability density functions

Continuous variables

- Quantities that can take any value, not just discrete values

Michelson's speed of light experiment



measured speed of light (1000 km/s)

299.85	299.74	299.90	300.07	299.93
299.85	299.95	299.98	299.98	299.88
300.00	299.98	299.93	299.65	299.76
299.81	300.00	300.00	299.96	299.96
299.96	299.94	299.96	299.94	299.88
299.80	299.85	299.88	299.90	299.84
299.83	299.79	299.81	299.88	299.88
299.83	299.80	299.79	299.76	299.80
299.88	299.88	299.88	299.86	299.72
299.72	299.62	299.86	299.97	299.95
299.88	299.91	299.85	299.87	299.84
299.84	299.85	299.84	299.84	299.84
299.89	299.81	299.81	299.82	299.80
299.77	299.76	299.74	299.75	299.76
299.91	299.92	299.89	299.86	299.88
299.72	299.84	299.85	299.85	299.78
299.89	299.84	299.78	299.81	299.76
299.81	299.79	299.81	299.82	299.85
299.87	299.87	299.81	299.74	299.81
299.94	299.95	299.80	299.81	299.87

Image: public domain, Smithsonian

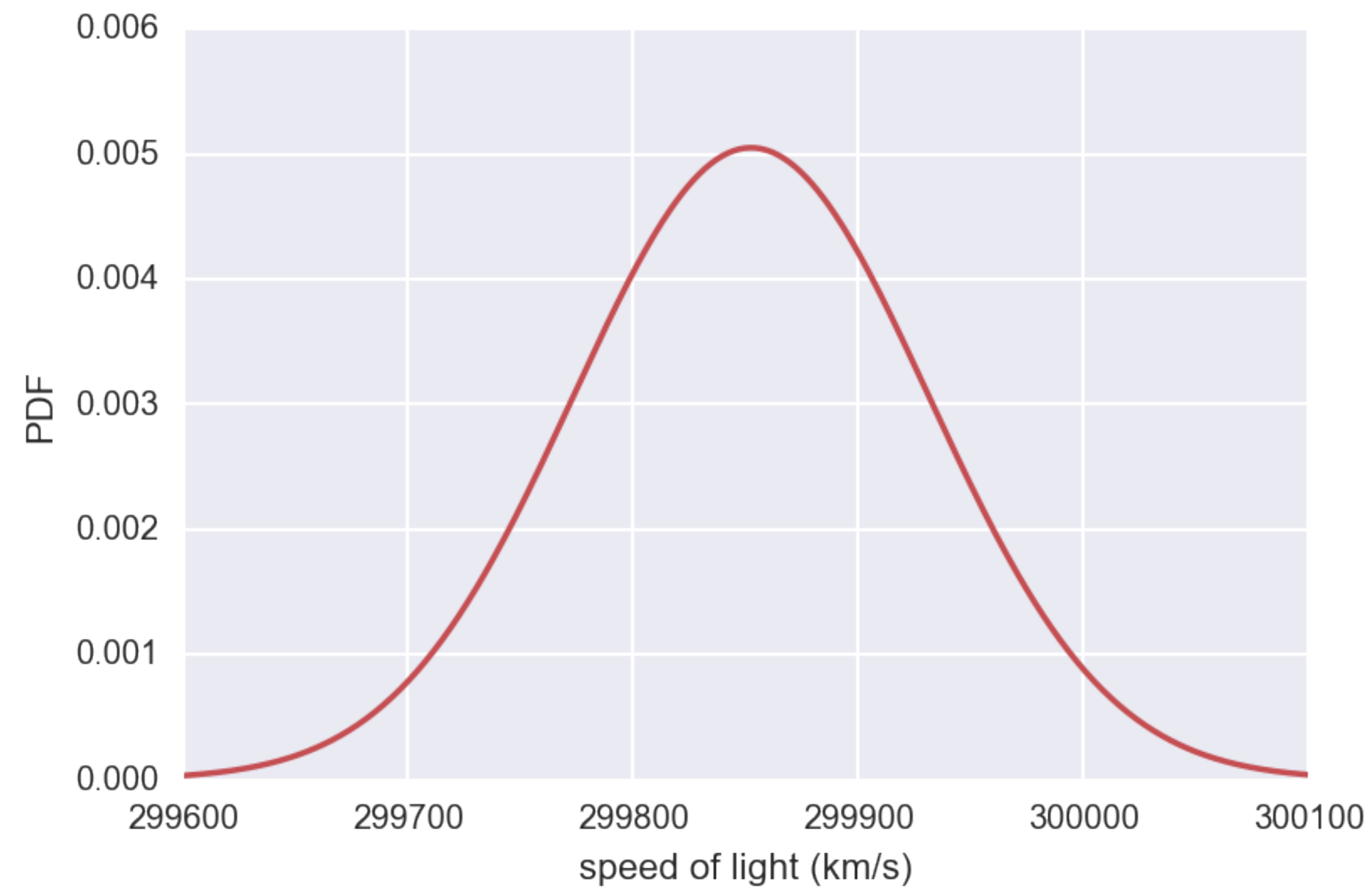
Data: Michelson, 1880

Probability density function (PDF)

- Continuous analog to the PMF
- Mathematical description of the relative likelihood of observing a value of a continuous variable

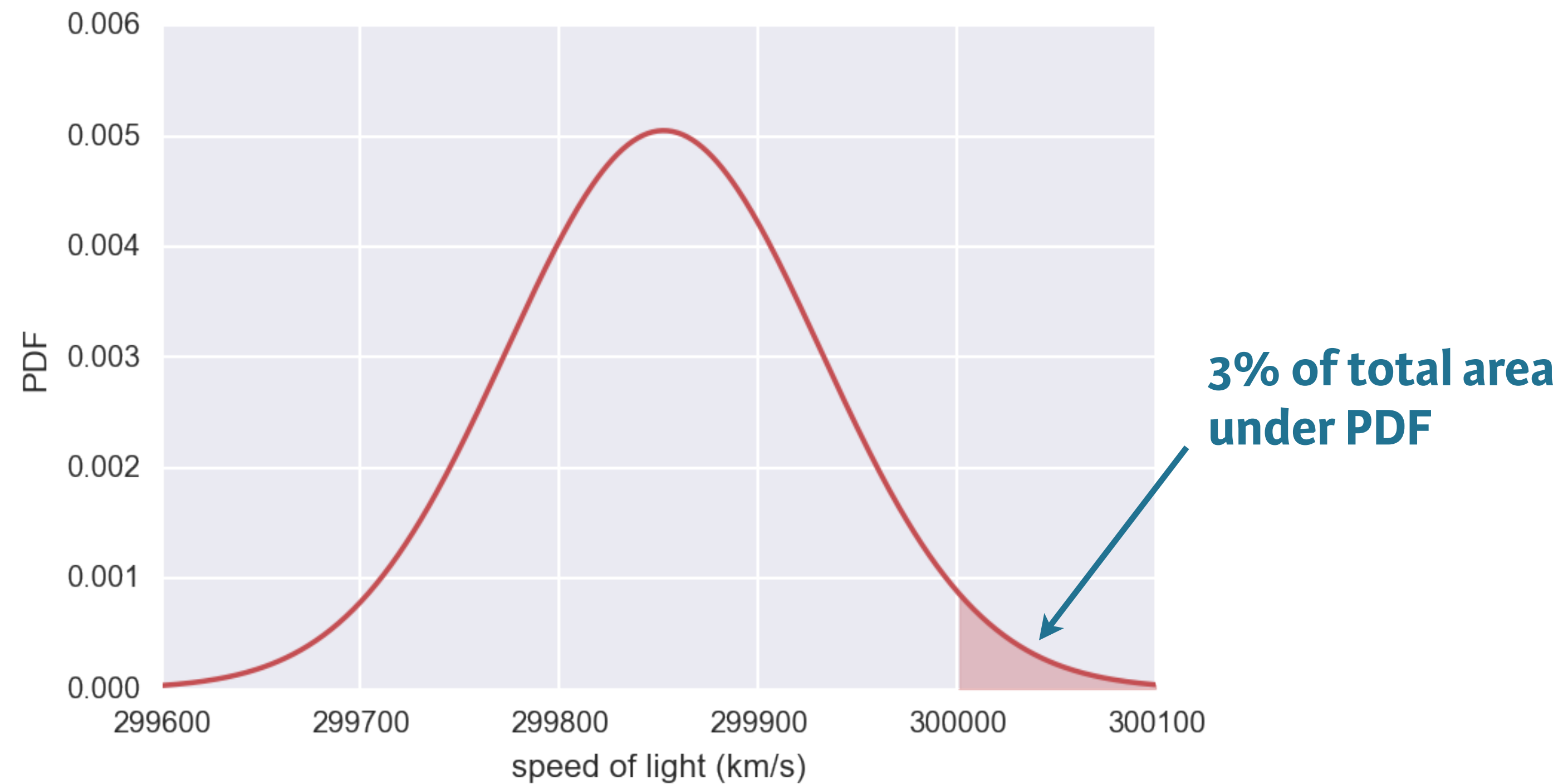


Normal PDF

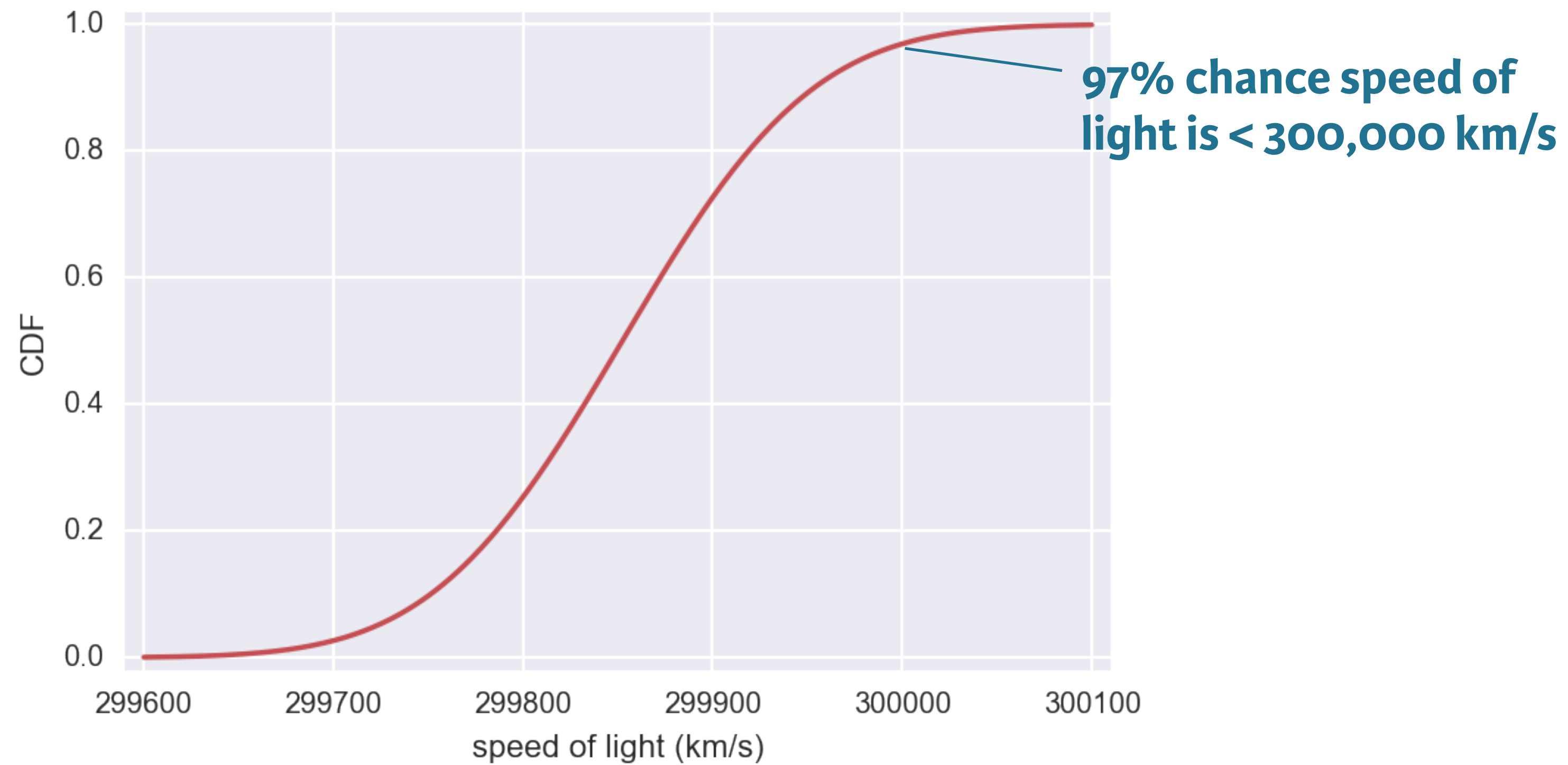




Normal PDF



Normal CDF





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Let's practice!



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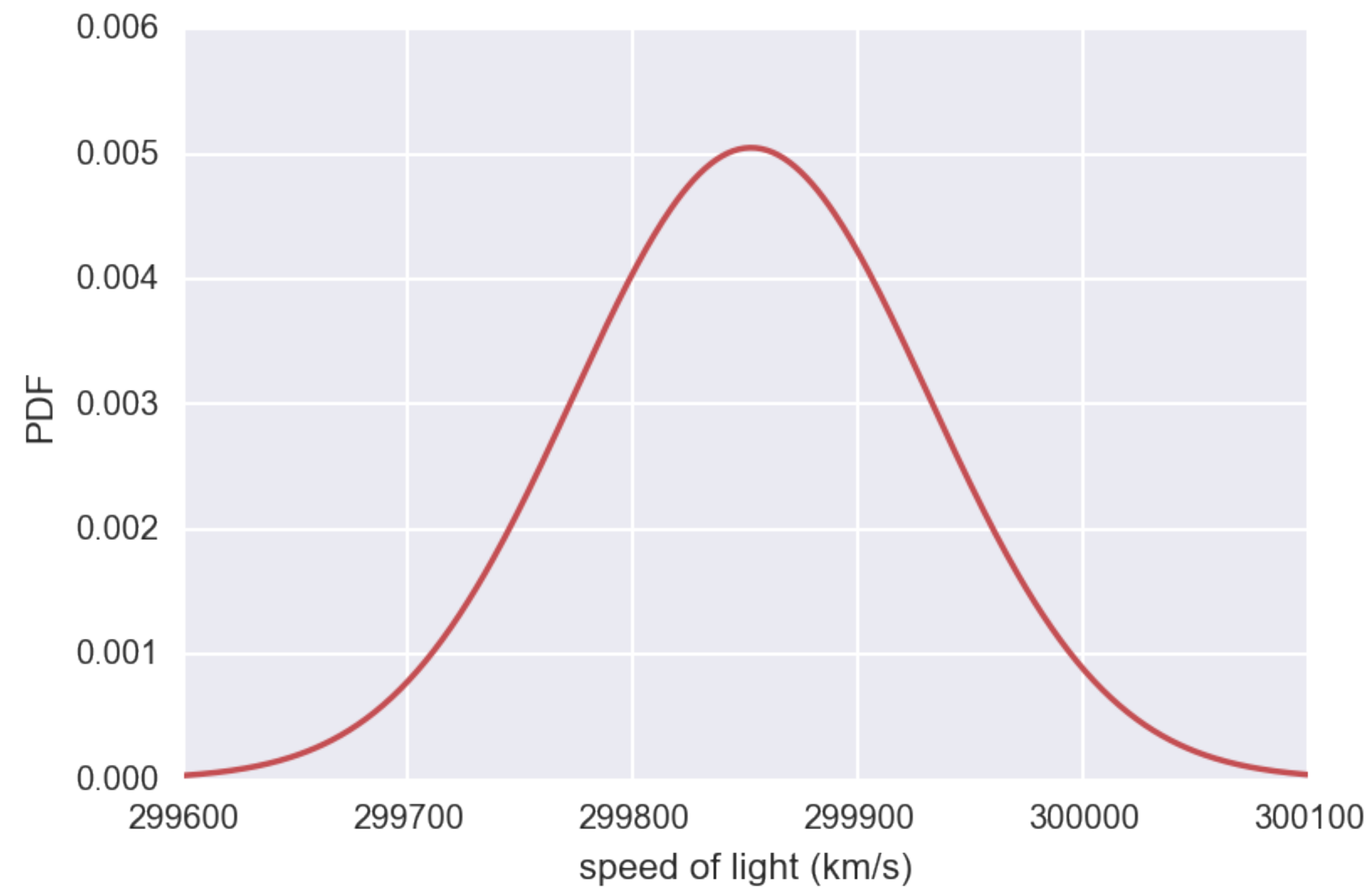
Introduction to the Normal distribution

Normal distribution

- Describes a continuous variable whose PDF has a single symmetric peak.

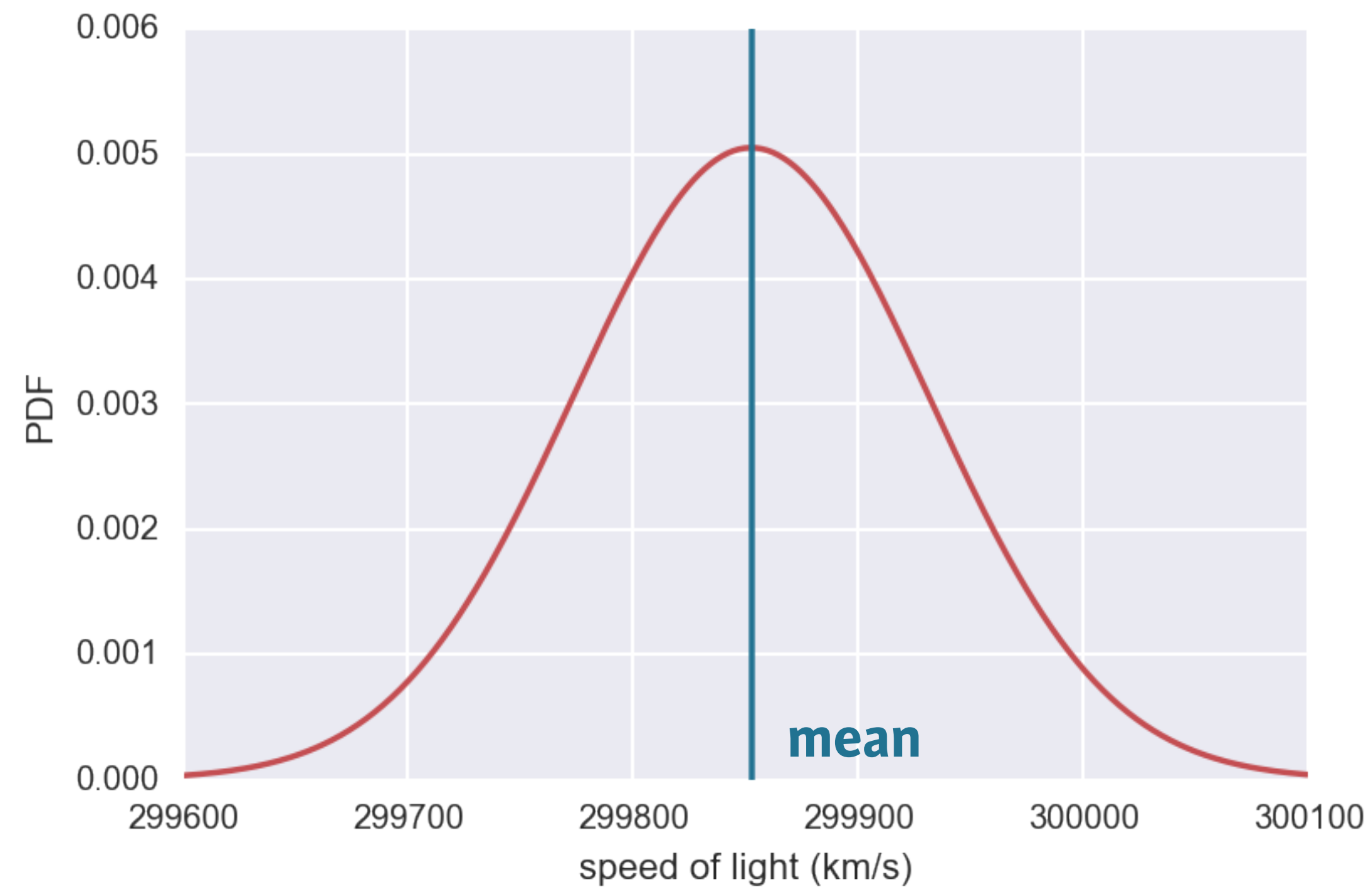


Normal distribution



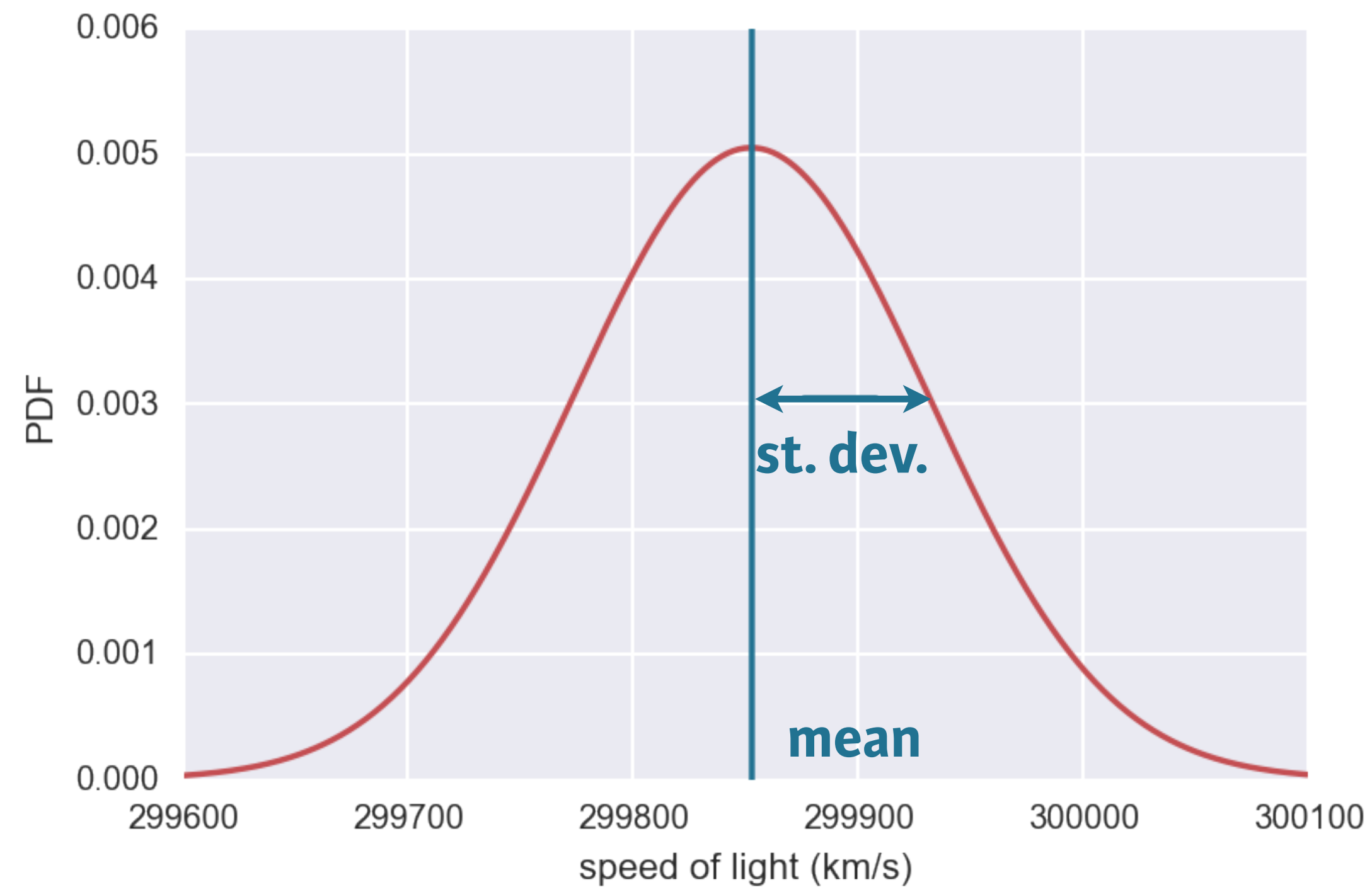


Normal distribution





Normal distribution





Parameter

mean of a
Normal distribution

st. dev. of a
Normal distribution

Calculated from data

mean computed
from data

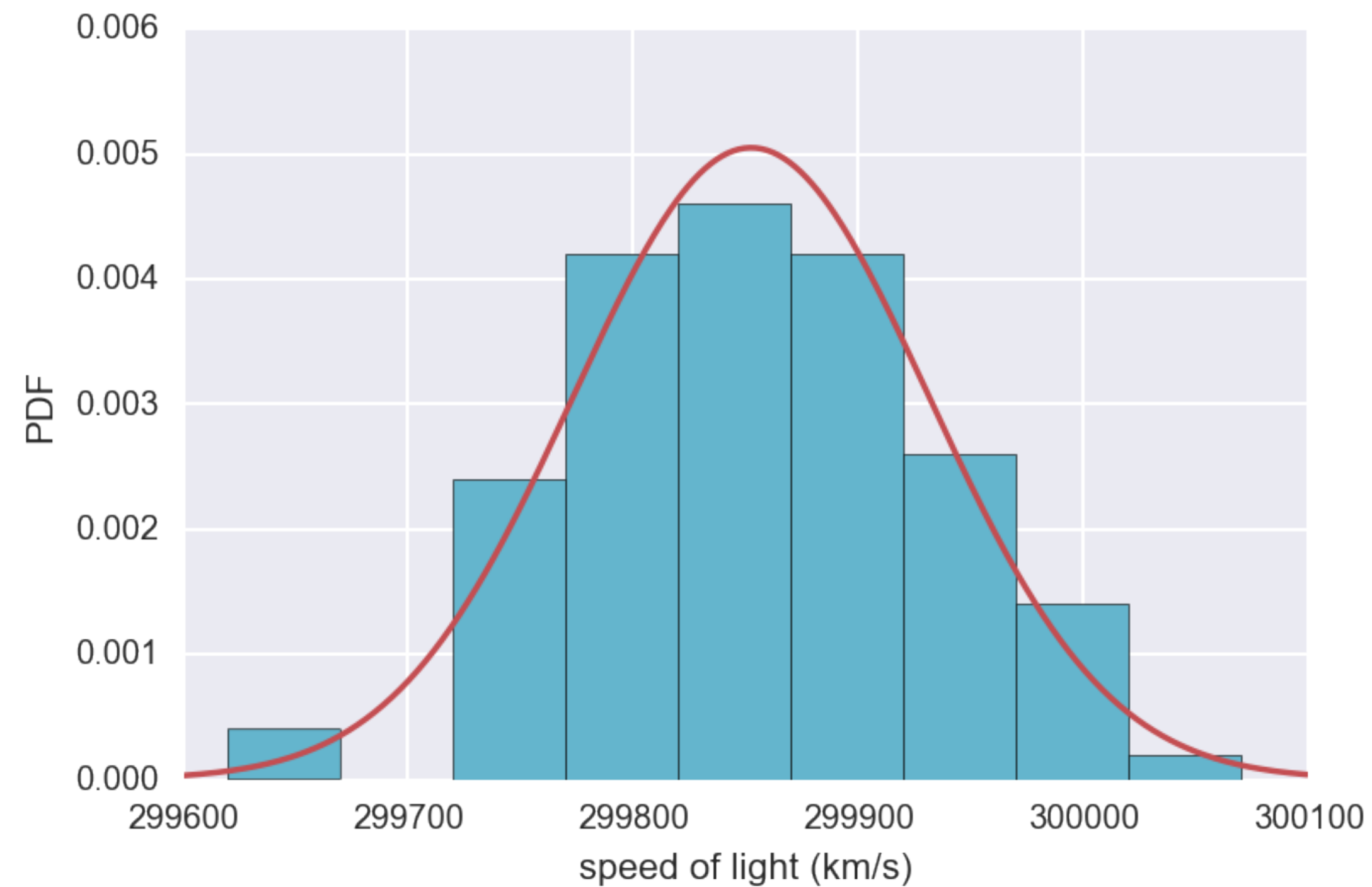
standard deviation
computed from data

≠

≠



Comparing data to a Normal PDF





Checking Normality of Michelson data

```
In [1]: import numpy as np

In [2]: mean = np.mean(michelson_speed_of_light)

In [3]: std = np.std(michelson_speed_of_light)

In [4]: samples = np.random.normal(mean, std, size=10000)

In [5]: x, y = ecdf(michelson_speed_of_light)

In [6]: x_theor, y_theor = ecdf(samples)
```




Checking Normality of Michelson data

```
In [1]: import matplotlib.pyplot as plt
```

```
In [2]: import seaborn as sns
```

```
In [3]: sns.set()
```

```
In [4]: _ = plt.plot(x_theor, y_theor)
```

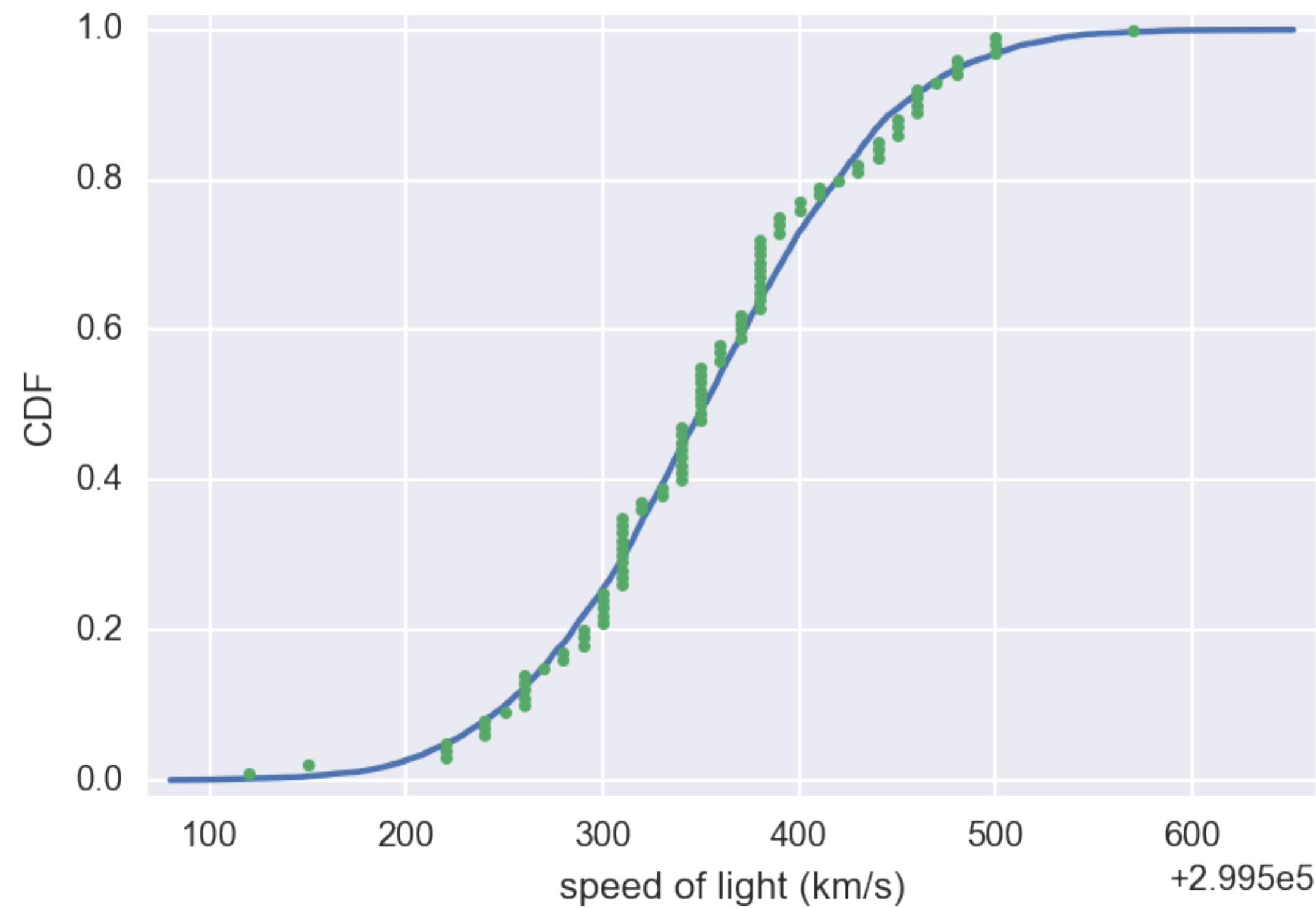
```
In [5]: _ = plt.plot(x, y, marker='.', linestyle='none')
```

```
In [6]: _ = plt.xlabel('speed of light (km/s)')
```

```
In [7]: _ = plt.ylabel('CDF')
```

```
In [8]: plt.show()
```

Checking Normality of Michelson data





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Let's practice!

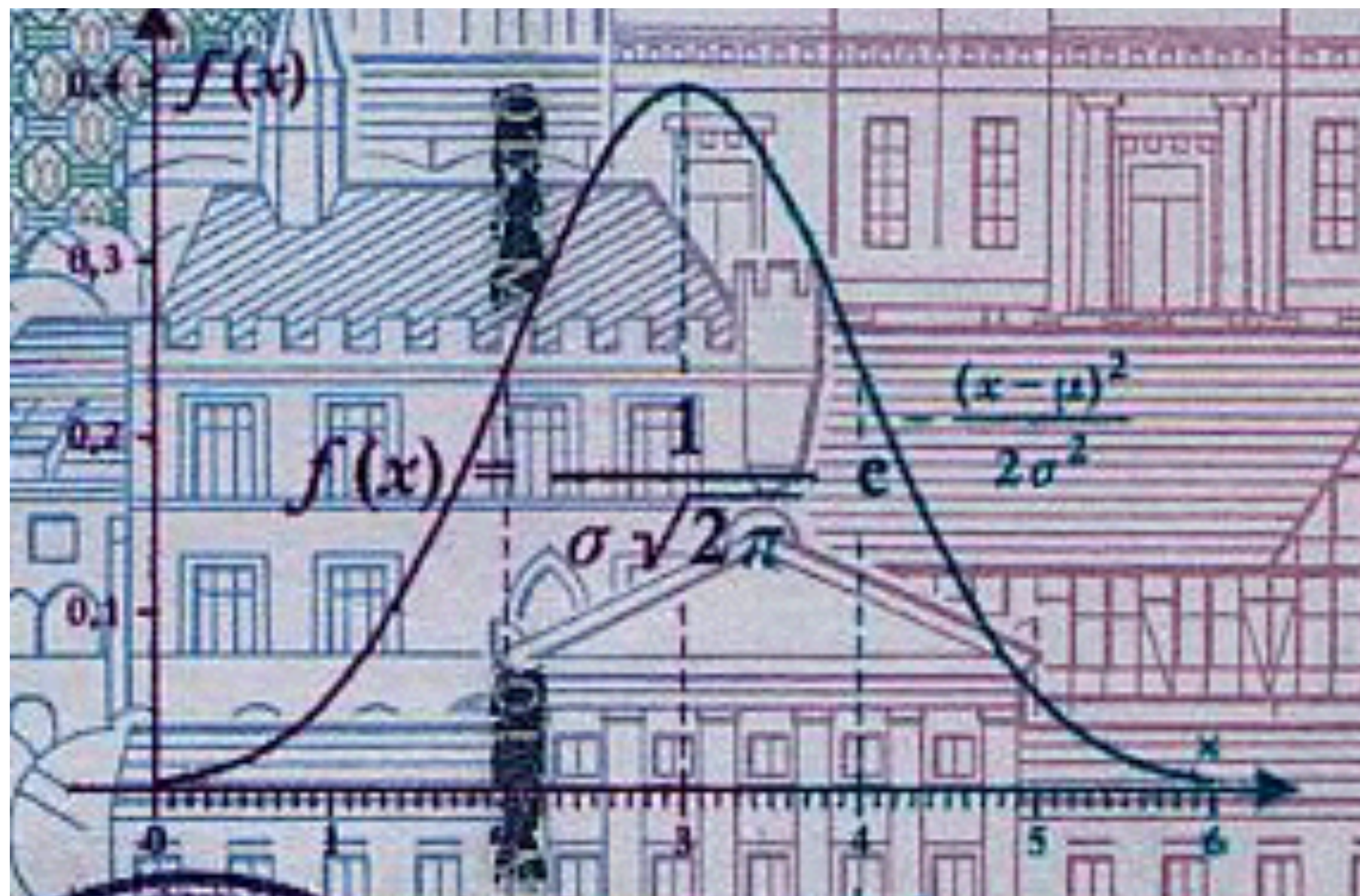


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The Normal distribution: Properties and warnings

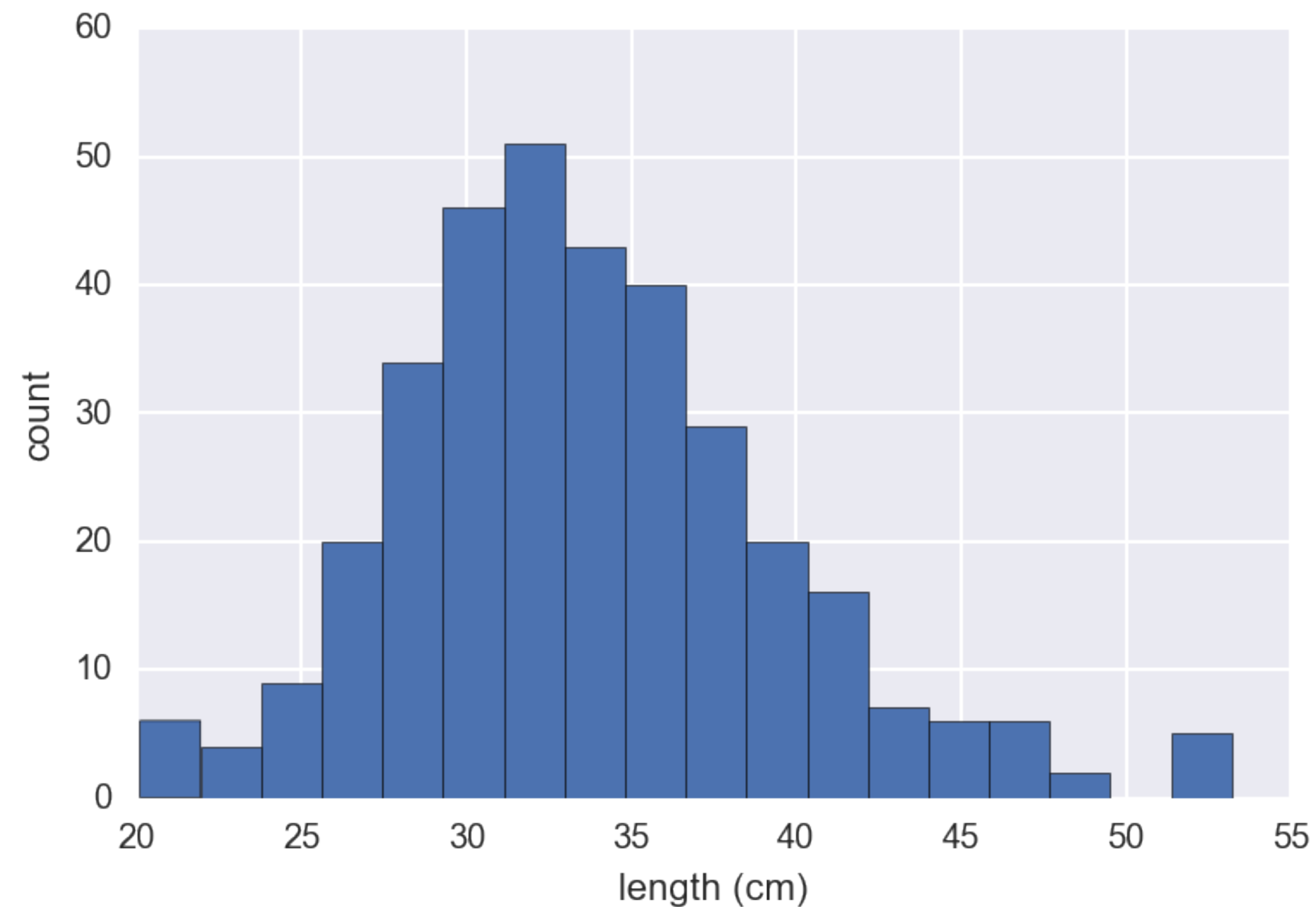


The Gaussian distribution



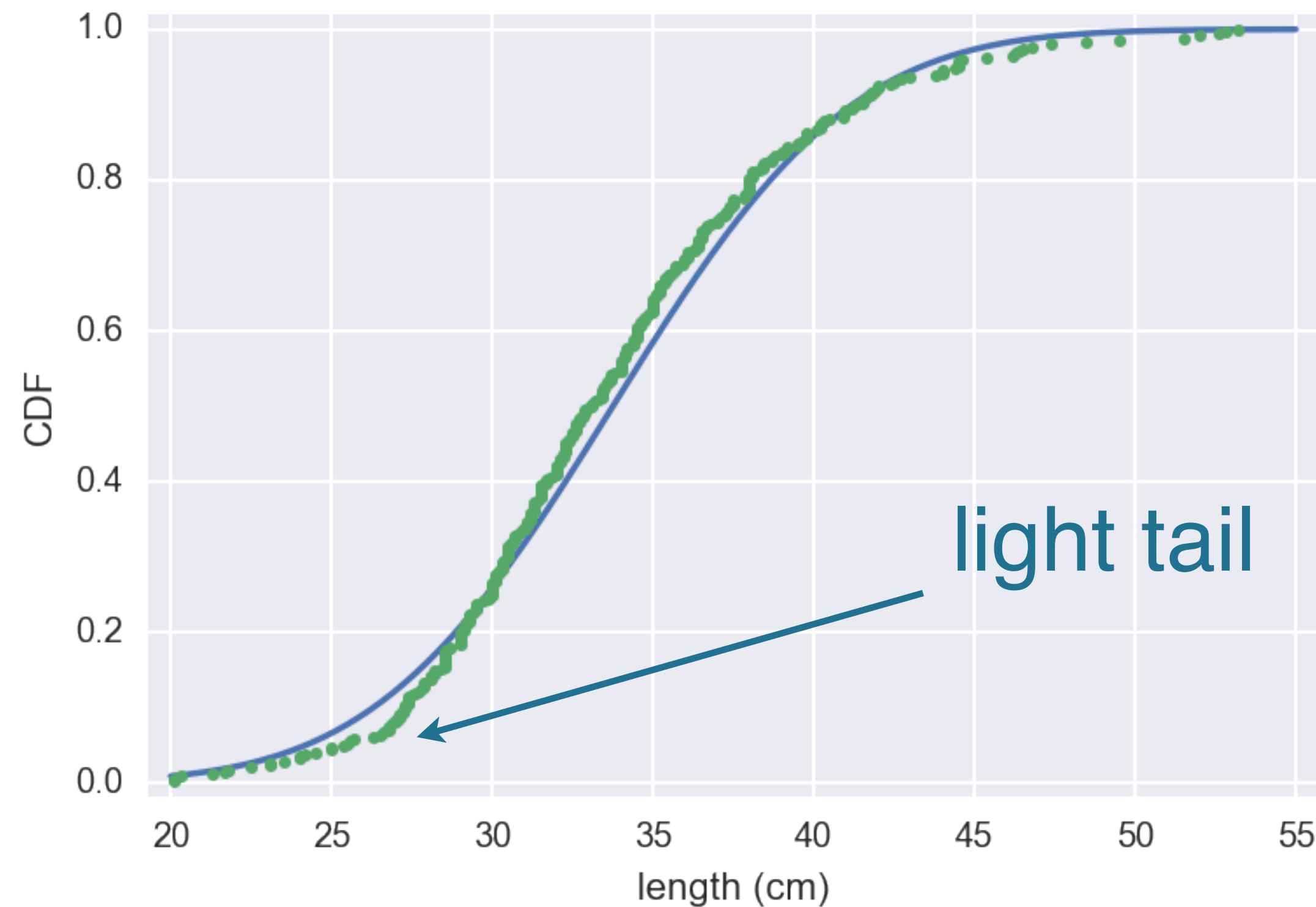


Length of MA large mouth bass



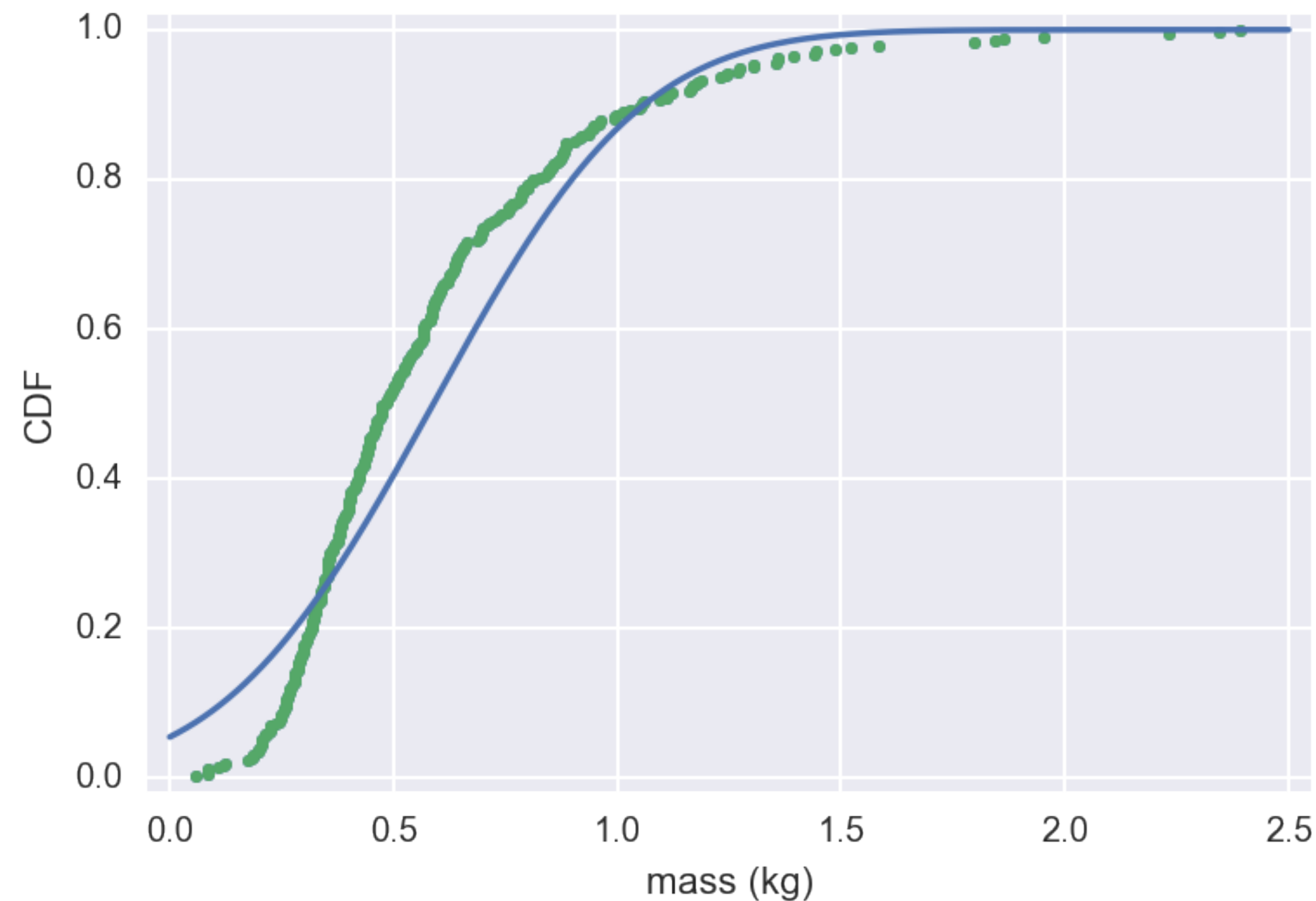


Length of MA large mouth bass



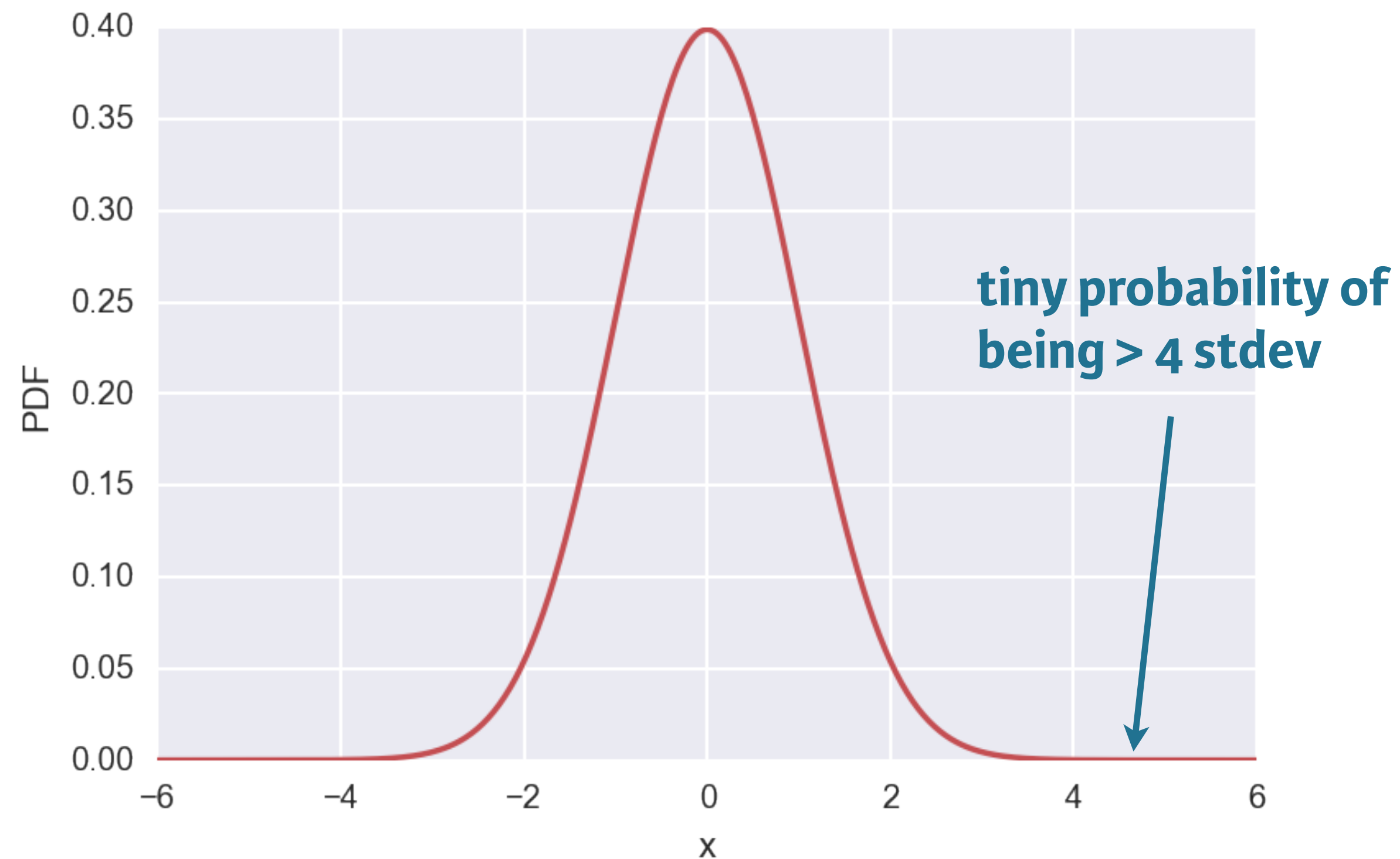


Mass of MA large mouth bass





Light tails of the Normal distribution





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Let's practice!



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The Exponential distribution

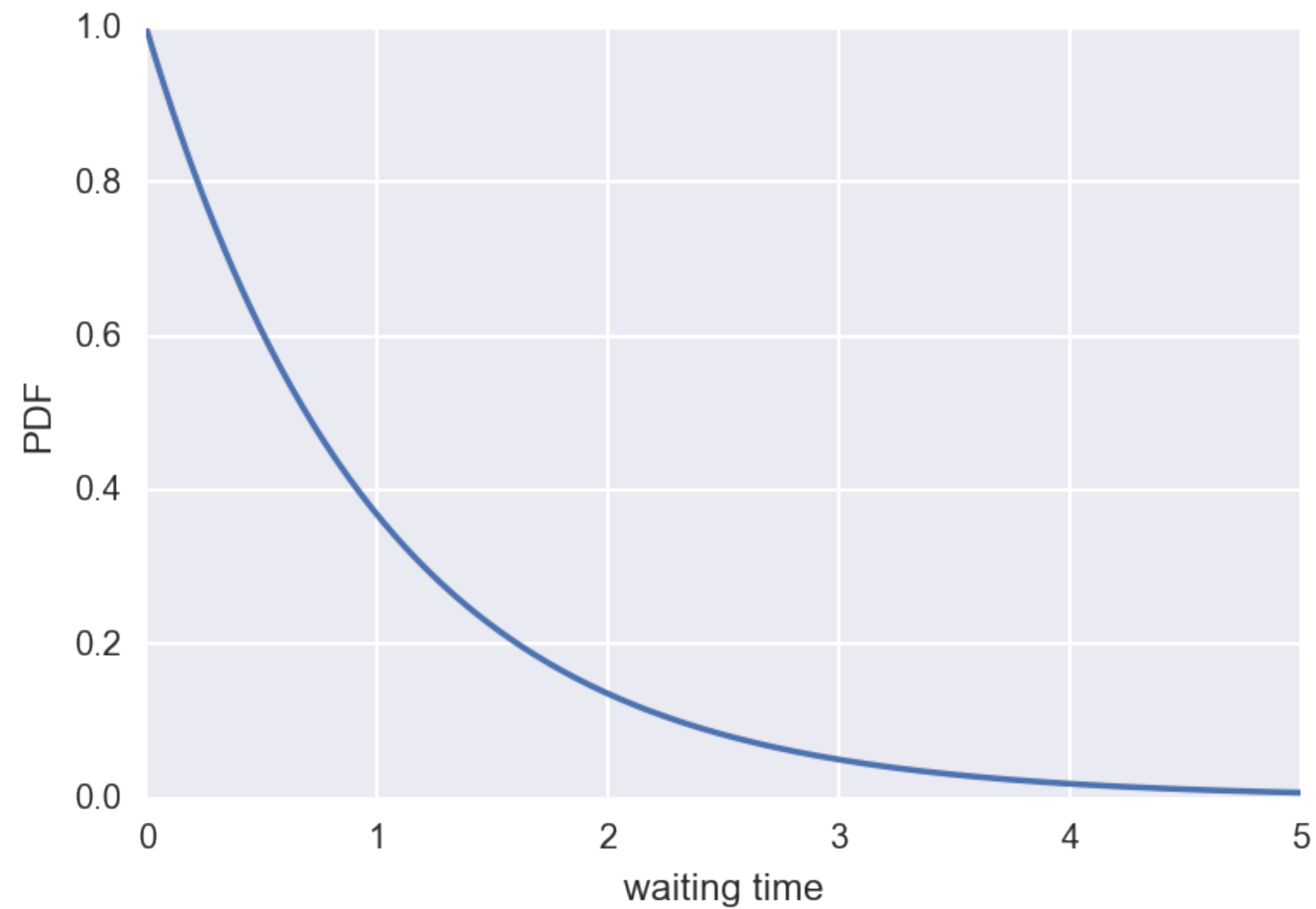
The Exponential distribution

- The waiting time between arrivals of a Poisson process is Exponentially distributed





The Exponential PDF





Possible Poisson process

- Nuclear incidents:
 - Timing of one is independent of all others



Exponential inter-incident times

```
In [1]: mean = np.mean(inter_times)

In [2]: samples = np.random.exponential(mean, size=10000)

In [3]: x, y = ecdf(inter_times)

In [4]: x_theor, y_theor = ecdf(samples)

In [5]: _ = plt.plot(x_theor, y_theor)

In [6]: _ = plt.plot(x, y, marker='.', linestyle='none')

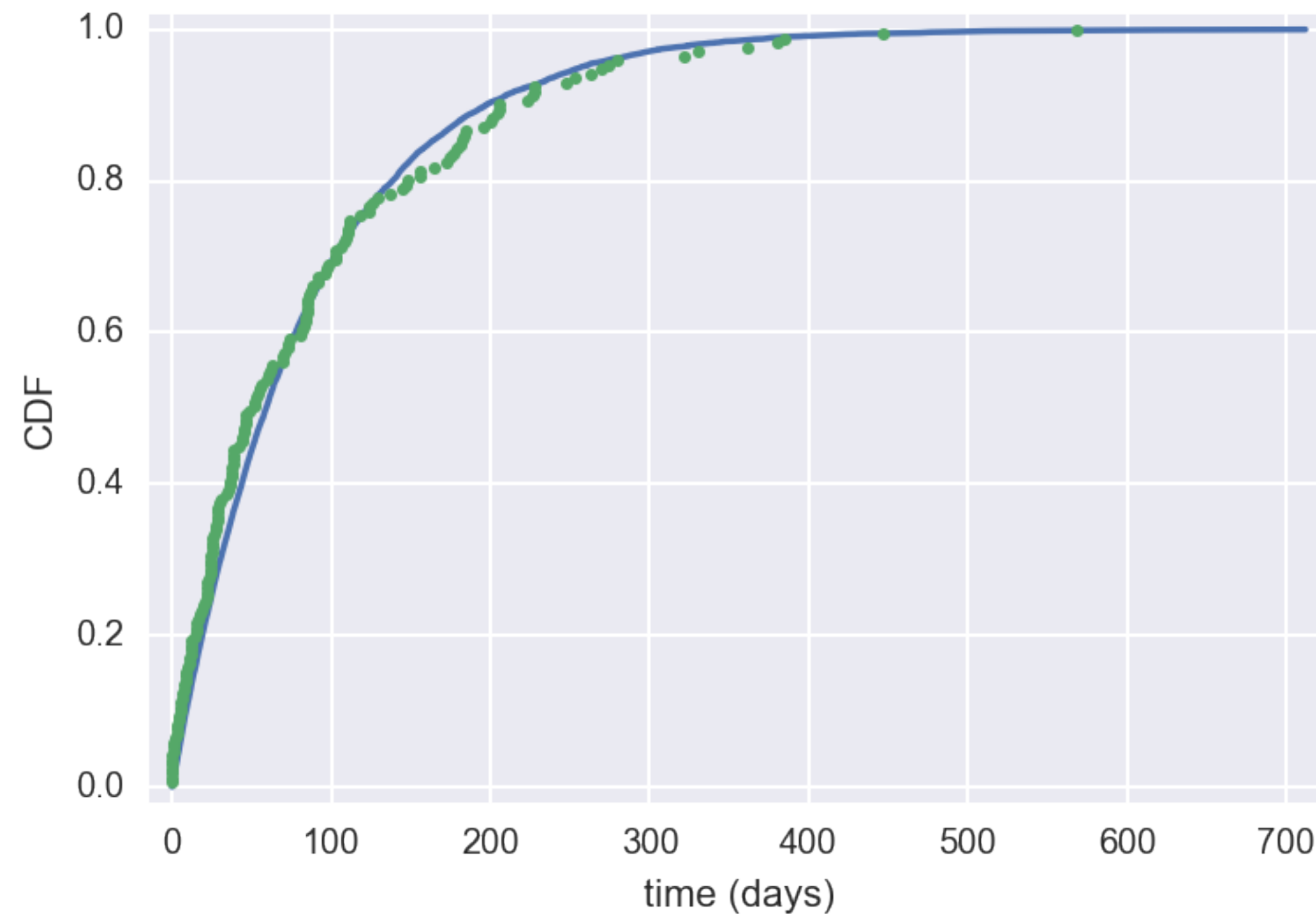
In [7]: _ = plt.xlabel('time (days)')

In [8]: _ = plt.ylabel('CDF')

In [9]: plt.show()
```




Exponential inter-incident times





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Let's practice!



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Final thoughts

You now can...

- Construct (beautiful) instructive plots
- Compute informative summary statistics
- Use hacker statistics
- Think probabilistically

In the sequel, you will...

- Estimate parameter values
- Perform linear regressions
- Compute confidence intervals
- Perform hypothesis tests



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See you in the sequel!