

# **Weekly Lab Agenda**

- Go over reminders/goals
- Review past material
- Work in groups of 2-3 to solve a few exercises
  - Lab leaders will assign new groups this week
- Discussion leaders will walk around and answer questions
- Solutions to exercises will be reviewed as a class
- Attendance taken at the end

### Reminders

- Great job this semester everyone, you should be proud of your hard work!
- Previous Final Review Sessions will be available on canvas.
- Office hours will continue to happen as scheduled.
  - Exceptions will be announced on campuswire.
- Exam Logistics:
  - Monday May 13th 3:30pm 5:30pm in Totman Gym.
  - Make sure to check SPIRE on exam day in case there is a last minute location change!
- Please fill out the <u>SRTI course survey</u>, this really helps make the class better!
- HW8 is due tomorrow midnight
- HW7 Self Eval on gradescope is due Friday midnight

## Feedback (We would greatly appreciate it!)

Code	Time	Room	TA	UCA 1	UCA 2	Feedback Form
LU	We 9:05AM - 9:55AM	Lederle Grad Res Ctr rm A301	Max	Victor		Feedback Form
LN	We 11:15AM - 12:05PM	Lederle Grad Res Ctr rm A301	Jeng-Yu	Atharva Kale		Feedback Form
LQ	We 11:15AM - 12:05PM	Flint Laboratory room 105	Angela	Manu	Liam	Feedback Form
LR	We 11:15AM - 12:05PM	Flint Lab room 201	Yiquan	Noah	Vinayak	Feedback Form
LS	We 12:20PM - 1:10PM	Flint Lab room 201	Ashraful	Vishwesh	Wenhao	Feedback Form
LM	We 1:25PM - 2:15PM	Flint Laboratory room 105	Kyler	Atharva Nikhil		Feedback Form
LL	We 1:25PM - 2:15PM	Flint Lab room 201	Chaolong	Saadhvi	Aarav	Feedback Form

# **Today's Goals**

- Practice working with program correctness
- Practice working with asynchronous programming

## **Exercise: Program Correctness**

The following code should partition the given array in-place such that all odd numbers come before all even numbers.

First, write the invariants which satisfy the high-level algorithm.

Then, fill in the code to satisfy the invariants.

```
function partition even odd(arr) {
  if (arr.length === 0) { return; }
 let low = ???:
 let high = ???;
  // low/high form a window, the outside of which is partitioned;
  // the window shrinks iteratively until everything is partitioned
  while (???) {
   if (???) {
     // swap arr[low] and arr[high]
      333
    if (???) {
      // update low
      ???
    if (???) {
      // update high
      333
```

```
function partition even odd(arr) {
 if (arr.length === 0) { return; }
 let low = ???;
 let high = ???;
  while (???) {
   // low/high form a window, the outside of which is partitioned
   // => (everything before low is odd) and (everything above high is even)
   // \Rightarrow (forall i: (i < low) \Rightarrow (arr[i] is odd)) and (forall i: (i > high) \Rightarrow (arr[i] is even))
   if (???) {
     // swap arr[low] and arr[high]
                                                  write a loop invariant; we can take our intuitive
      ???
                                                  understanding the algorithm, write it down in plain english,
   if (???) {
                                                  then iteratively refine it until it is more mathematically formal
     // update low
      ???
   if (???) {
     // update high
      333
```

```
function partition_even_odd(arr) {
 if (arr.length === 0) { return; }
 let low = ???;
 let high = ???;
 // let P1 be (forall i: (i < low) => (arr[i] is odd)) and (forall i: (i > high) => (arr[i] is even))
 // P1
 while (???) {
  // P1
   if (???) {
    // P1
                                          fill in all invariants that are directly implied via control flow
     // swap arr[low] and arr[high]
     ???
     // P1
   // P1
   if (???) {
     // P1
     // update low
     ???
     // P1
   // P1
   if (???) {
     // P1
     // update high
     ???
     // P1
   // P1
  // P1
```

```
function partition even odd(arr) {
                                           we now have enough information to fill in initialization; there is
 if (arr.length === 0) { return; }
                                           only one option which satisfies the invariant
 let low = 0;
 let high = arr.length - 1;
 // let P1 be (forall i: (i < low) \Rightarrow (arr[i] is odd)) and (forall i: (i > high) \Rightarrow (arr[i] is even))
 // P1
 while (???) {
   // P1
   if (???) {
     // P1
                                                                     we know how to swap two elements;
     let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
     // P1
                                                                     this does not violate the invariants
   // P1
   if (arr[low] % 2 === 1) {
     // P1 and (arr[low] is odd)
     // note that (forall i: (i < low) => (arr[i] is odd)) and (arr[low] is odd)
     // => (forall i: (i < low+1) => (arr[i] is odd))
     low += 1;
                                           we have an idea of an update, but it would violate the
     // P1
                                           invariant; we can modify the invariant inside the "if body" to
   // P1
                                           match, and that informs the "if condition"
   if (arr[high] % 2 === 0) {
     // P1 and (arr[high] is even)
     // note that (forall i: (i > high) => (arr[i] is even)) and (arr[high] is even)
     // => (forall i: (i > high-1) => (arr[i] is even))
     high -= 1;
     // P1
   // P1
 // P1
```

```
function partition even odd(arr) {
 if (arr.length === 0) { return; }
 let low = 0;
 let high = arr.length - 1;
 // let P1 be (forall i: (i < low) \Rightarrow (arr[i] is odd)) and (forall i: (i > high) \Rightarrow (arr[i] is even))
 // P1
 while (???) {
  // P1
   if (???) {
   // P1
     let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
     // P1
   // P1
   if (arr[low] % 2 === 1) {
     // P1 and (arr[low] is odd)
     low += 1;
     // P1
   // P1
   if (arr[high] % 2 === 0) {
     // P1 and (arr[high] is even)
                                      in order to know what the "while condition" should be, we need to
     high -= 1;
                                      know what state we want when the "while loop" finishes; we want the
     // P1
                                      array to be fully partitioned at the end
   // P1
 // P1 and (???)
 //=> (exists i: (forall j: (j <= i) => (arr[j] is odd)) and (forall j: (i < j) => (arr[j] is even)))
```

```
function partition even odd(arr) {
  if (arr.length === 0) { return; }
 let low = 0;
  let high = arr.length - 1;
 // let P1 be (forall i: (i < low) \Rightarrow (arr[i] is odd)) and (forall i: (i > high) \Rightarrow (arr[i] is even))
 // P1
  while (low <= high) {</pre>
   // P1
    if (???) {
    // P1
     let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
     // P1
    // P1
    if (arr[low] % 2 === 1) {
     // P1 and (arr[low] is odd)
     low += 1;
      // P1
   // P1
    if (arr[high] % 2 === 0) {
     // P1 and (arr[high] is even)
      high -= 1;
      // P1
                                        once we have figured out what needs to hold after the "while loop" is
   // P1
                                        over, then the "while condition" will just be the negation of that
 // P1 and (low > high)
 // \Rightarrow (exists i: (forall j: (j <= i) \Rightarrow (arr[j] is odd)) and (forall: j (i < j) \Rightarrow (arr[j] is even)))
```

```
function partition even odd(arr) {
                                     Are we making progress in each iteration, i.e., is high-low decreasing? Let's look at the 4
 if (arr.length === 0) { return; }
                                     cases.
 let low = 0;
 let high = arr.length - 1;
 // let P1 be (forall i: (i < low) \Rightarrow (arr[i] is odd)) and (forall i: (i > high) \Rightarrow (arr[i] is even))
 // P1
                                                                                                              4 cases
 while (low <= high) {</pre>
   // P1
                                                                          Value at
                                                                                        Value at
                                                                                                      Progress (high-low)
    if (???) {
                                                                          idx low
                                                                                        idx high
    // P1
     let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
     // P1
                                                                          odd
                                                                                        odd
                                                                                                      decreases by 1
    // P1 and (???)
    if (arr[low] % 2 === 1) {
     // P1 and (arr[low] is odd)
                                                                                                      decreases by 1
                                                                          even
                                                                                        even
     low += 1;
     // P1 and (high-low decreases)
                                                                          odd
                                                                                                      decreases by 2
                                                                                        even
    // P1 and (???) and ((arr[old low] was odd) => (high-low decrease)
    if (arr[high] % 2 === 0) {
     // P1 and (arr[high] is even)
                                                                          even
                                                                                        odd
                                                                                                      What should ??? be to
     high -= 1;
     // P1 and (high-low decreases)
                                                                                                      guarantee progress?
   // P1 and (???) and ((arr[old low] was odd) => (high-low decreases))) and ((arr[old high] was even) => (high-low
decreases))
   // => P1 and (???) and (((arr[old low] was odd) or (arr[old high] was even)) => (high-low decreases)))
    // => P1 and (high-low decreases))
 // P1 and (low > high)
 //=> (exists i: (forall j: (j <= i) => (arr[j] is odd)) and (forall: j (i < j) => (arr[j] is even)))
```

```
function partition even odd(arr) {
 if (arr.length === 0) { return; }
 let low = 0;
 let high = arr.length - 1;
 // let P1 be (forall i: (i < low) \Rightarrow (arr[i] is odd)) and (forall i: (i > high) \Rightarrow (arr[i] is even))
 // P1
 while (low <= high) {</pre>
   // P1
    if (???) {
    // P1
     let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
     // P1
                                          we are still missing one more "if condition", and no clear violations of the invariants;
   // P1 and (???)
                                          however, there is a hidden assumption that we want the loop to "make progress" on
   if (arr[low] % 2 === 1) {
                                          every iteration; from the "while condition" we see that our definition of "make progress"
     // P1 and (arr[low] is odd)
                                          is either increasing "low" or decreasing "high". This implies decreasing value of
     low += 1;
                                          high-low compared to previteration and a progress towards termination.
     // P1 and (high-low decreases)
    // P1 and (???) and ((arr[old low] was odd) => (high-low decreases))
    if (arr[high] % 2 === 0) {
     // P1 and (arr[high] is even)
     high -= 1;
     // P1 and (high-low decreases)
   // P1 and (???) and ((arr[old low] was odd) => (high-low decreases))) and ((arr[old high] was even) => (high-low
decreases))
   // => P1 and (???) and (((arr[old low] was odd) or (arr[old high] was even)) => (high-low decreases)))
    // => P1 and (high-low decreases))
 // P1 and (low > high)
 //=> (exists i: (forall j: (j <= i) => (arr[j] is odd)) and (forall: j (i < j) => (arr[j] is even)))
```

```
if (arr.length === 0) { return; }
let low = 0;
let high = arr.length - 1;
// let P1 be (forall i: (i < low) => (arr[i] is odd)) and (forall i: (i > high) => (arr[i] is even))
// P1
while (low <= high) {</pre>
 // P1
 if (???) {
   // P1
    let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
   // P1
                                                             so we figure out that the condition
  // P1 and ((arr[low] is odd) or (arr[high] is even))
                                                             ((arr[low] is odd) or (arr[high] is even))
  if (arr[low] % 2 === 1) {
                                                             must hold after our incomplete "if statement"
   // P1 and (arr[low] is odd)
   low += 1;
    // P1 and (high-low decreases)
  // P1 and ((arr[old low] was odd) or (arr[high] is even)) and ((arr[old low] was odd) => (high-low decreases))
 // => P1 and ((arr[high] is even) or (high-low decreases))
  if (arr[high] % 2 === 0) {
   // P1 and (arr[high] is even)
    high -= 1;
    // P1 and (high-low decreases)
 // P1 and ((arr[old high] was even) or (high-low decreases)) and ((arr[old high] is even) => (high-low decreases))
  // => P1 and (high-low decreases)
// P1 and (low > high)
// \Rightarrow (exists i: (forall j: (j <= i) \Rightarrow (arr[j] is odd)) and (forall: j (i < j) \Rightarrow (arr[j] is even)))
```

function partition even odd(arr) {

```
if (arr.length === 0) { return; }
let low = 0;
let high = arr.length - 1;
// let P1 be (forall i: (i < low) \Rightarrow (arr[i] is odd)) and (forall i: (i > high) \Rightarrow (arr[i] is even))
// P1
while (low <= high) {</pre>
 // P1
  if (arr[low] % 2 === 0 && arr[high] % 2 === 1) {
   // P1 and (arr[low] is even) and (arr[high] is odd)
    let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
    // P1 and (arr[low] is odd) and (arr[high] is even)
    // => P1 and ((arr[low] is odd) or (arr[high] is even))
  } else {
    // P1 and ((arr[low] is odd) or (arr[high] is even))
  // P1 and ((arr[low] is odd) or (arr[high] is even))
  if (arr[low] % 2 === 1) {
    // P1 and (arr[low] is odd)
   low += 1;
    // P1 and (high-low decreases)
  // P1 and ((arr[high] is even) or (high-low decreases))
  if (arr[high] % 2 === 0) {
    // P1 and (arr[high] is even)
    high -= 1;
    // P1 and (high-low decreases)
  // P1 and (high-low decreases)
// P1 and (low > high)
//=> (exists i: (forall j: (j <= i) => (arr[j] is odd)) and (forall: j (i < j) => (arr[j] is even)))
```

function partition even odd(arr) {

we can finally finish the last bit of code; all invariants hold at every step, so the code is guaranteed to be correct

```
function partition even odd(arr) {
 if (arr.length === 0) { return; }
 let low = 0;
 let high = arr.length - 1;
 // let P1 be (forall i: (i < low) => (arr[i] is odd)) and (forall i: (i > high) => (arr[i] is even))
 // P1
 while (low <= high) {</pre>
   // P1
   if (arr[low] % 2 === 0 && arr[high] % 2 === 1) {
     // P1 and (arr[low] is even) and (arr[high] is odd)
     let t = arr[low]; arr[low] = arr[high]; arr[high] = t;
     // P1 and (arr[low] is odd) and (arr[high] is even)
   // P1 and ((arr[low] is odd) or (arr[high] is even))
   if (arr[low] % 2 === 1) {
     // P1 and (arr[low] is odd)
     low += 1;
     // P1 and (high-low decreases)
   // P1 and ((arr[high] is even) or (high-low decreases))
   if (arr[high] % 2 === 0) {
     // P1 and (arr[high] is even)
     high -= 1;
     // P1 and (high-low decreases)
   // P1 and (high-low decreases)
 // P1 and (low > high)
 // \Rightarrow (exists i: (forall j: (j <= i) \Rightarrow (arr[j] is odd)) and (forall: j (i < j) \Rightarrow (arr[j] is even)))
```

Write a function asyncPosMap(arr: T[], f: T => Promise(number)): Promise<T[]>. This function takes a generic array, arr and an asynchronous function f, and returns a new Promise. That promise should be fulfilled with a new array containing the elements of arr that for which f resolved to a positive number. The promise should reject if at any point f rejects. Ensure that calls to f occur asynchronously, by using Promise.all.

Fall 2022 Midterm 2 Makeup - 20pts

**UMassAmherst** 

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```
function asyncPosMap(arr: T[], f: T => Promise<number>): Promise<T[]> {
```

// The first thing we have to do is get the result of applying f to every element in arr.

```
UMassAmherst
```

```
function asyncPosMap(arr: T[], f: T => Promise<number>): Promise<T[]> {
    return Promise.all( );

// To do this we'll use Promise.all. Why do we need to do this?
```

**UMassAmherst** 

```
function asyncPosMap(arr: T[], f: T => Promise<number>): Promise<T[]> {
    return Promise.all(arr.map(f))

// Let's think about what arr.map(f) will return. It returns an array of promises that will
    // resolve to a number, i.e., Promise<number>[].
    // It would be a lot more convenient if we had a Promise that resolved to a number[]
    // when all the asynchronous functions return.
    // This is what Promise.all will do.
    // It will transform our Promise<number>[] into a Promise<number[]>.
}
```

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// If any call to f rejects, Promise.all will return a promise that rejects. This will bubble // though our .then. Thus, if f rejects, so does our returned promise.