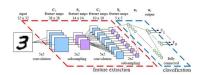
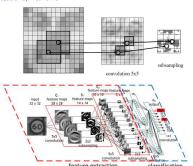
# Convolutional Networks



- DNNs suitable for image recognition, since they exhibit invariance to translation, scaling, rotations, and warping.
   Convolution: Detection of local features, e.g. a<sub>j</sub> is computed from a 5x5 pixel patch of the image.
   To achieve invariance, the units in the convolution layer share the same activation function and weights.
   Subsampling: Combination of local features into higher-order features, e.g. a<sub>k</sub> is compute from a 2x2 pixel patch of the convoluted image.
   There are several feature maps in each layer, to compensate the reduction in resolution by increasing in the number of features being detected.
   The final layer is a regular NN for classification.

# Convolutional Networks



# Convolutional Networks

- DNNs allow increased depth because
  - they are sparse, which allows the gradient to propagate further, and
     they have relatively few weights to fit due to feature locality and weight sharing.
- ▶ The backpropagation algorithm needs to be adapted, by modifying the derivatives with respect to the weights in each convolution layer m. ▶ Since  $E_n$  depends on  $w_i^{(m)}$  only via  $a_j^{(m)}$ , and  $a_j^{(m)} \equiv \sum_{i \in I_i^{(m)}} w_i^{(m)} z_i^{(m)} = 1$ . where  $L_i^{(m)}$  is the set of indexes of the input units, then

$$\frac{\partial E_n}{\partial w_i^{(m)}} = \sum_j \frac{\partial E_n}{\partial a_j^{(m)}} \frac{\partial a_j^{(m)}}{\partial w_i^{(m)}} = \sum_j \delta_j^{(m)} z_i^{(m-1)}$$

▶ Note that  $w_i^{(m)}$  does not depend on j by weight sharing, whereas  $i \in L_j^{(m)}$  by feature locality.

# Rectifier Activation Function





- $rectifier(x) = max\{0,x\}$ , i.e. hidden units are off or operating in a linear
- ► The most popular choice nowadays.
- Sparsity promoting: Uniform initialization of the weights implies that around 50 % of the hidden units are off.
   Piece-wise linear mapping: The input selects which hidden units are active, and the output is a liner function of the input in the selected hidden units.

# Rectifier Activation Function



- It simplifies the backpropagation algorithm as h'(s) = 1 for the selected units. So, there is no gradient vanishing on the parts of selected units. Compare with the sigmoid of hyperbolic tangent, for which
   the gradient is smaller than one, or
   even zero due to saturation.
- \* even zero due to saturation. Note that h'(0) does not exist since  $h'_{*}(0) \neq h'_{*}(0)$ . We can get around this problem by simply returning one of two one-sided derivatives. Or using a generalization of the rectifier function. Regularization is typically added to prevent numerical problems due to the activation being unbounded, e.g. when forward propagating.

# Layer-Wise Pre-Training

- The pre-training aims to find a good starting point for the subsequent run of the backpropagation algorithm.
   Supervised version:
- - Train each layer of the DNN as if it was the hidden layer in a depth-two NN. As input, use the output of the last of the previously trained layers. As output, use the original classification or regression function.
    Run the backpropagation algorithm to fine-tune the weights.
- Unsupervised version: Similar to the supervised one but the hidden layers (except the last one) are trained to learn an encoding of the output of the previous layer, instead of the original classification or regression function.