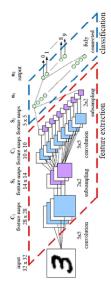
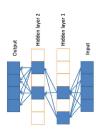
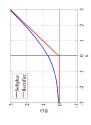
Convolutional Networks



- DNNs suitable for image recognition, since they exhibit invariance to translation, scaling, rotations, and warping.
 Convolution: Detection of local features, e.g. aj is computed from a 5x5
 - ▶ To achieve invariance, the units in the convolution layer share the same activation function and weights. pixel patch of the image.
- Subsampling: Combination of local features into higher-order features, e.g. a_k is compute from a 2x2 pixel patch of the convoluted image.
 There are several feature maps in each layer, to compensate the reduction in resolution by increasing in the number of features being detected.
 The final layer is a regular NN for classification.

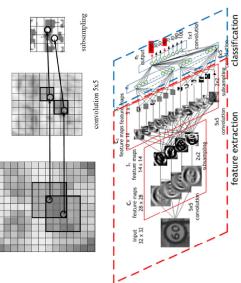
Rectifier Activation Function





adients in a network of rectifier units. The in this subset. Right: Rectifier and softplus propagation active neurons a Figure 2: Left: Sparse proping the selects a subset of active activation functions. The se

- rectifier(x) = $\max\{0, x\}$, i.e. hidden units are off or operating in a linear
 - The most popular choice nowadays. regime.
- Sparsity promoting: Uniform initialization of the weights implies that around 50 % of the hidden units are off.
- Piece-wise linear mapping: The input selects which hidden units are active, and the output is a liner function of the input in the selected hidden units.



Convolutional Networks

feature extraction

Convolutional Networks

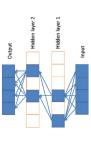
- DNNs allow increased depth because
- they are sparse, which allows the gradient to propagate further, and
 they have relatively few weights to fit due to feature locality and weight
- $\,$ The backpropagation algorithm needs to be adapted, by modifying the derivatives with respect to the weights in each convolution layer m.
- Since E_n depends on $w_i^{(m)}$ only via $a_j^{(m)}$, and $a_j^{(m)} = \sum_{i \in L_j^{(m)}} w_i^{(m)} z_i^{(m-1)}$

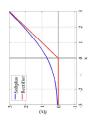
where $L_j^{(m)}$ is the set of indexes of the input units, then

$$\frac{\partial E_n}{\partial \mathbf{w}_i^{(m)}} = \sum_j \frac{\partial E_n}{\partial a_j^{(m)}} \frac{\partial a_j^{(m)}}{\partial \mathbf{w}_i^{(m)}} = \sum_j \delta_j^{(m)} z_i^{(m-1)}$$

Note that $w_i^{(m)}$ does not depend on j by weight sharing, whereas $i \in L_j^{(m)}$ by feature locality.

Rectifier Activation Function





and gradients in a network of rectifier units. The is linear in this subset. Right: Rectifier and softplus on of the first. Figure 2: Left: Sparse propagation input selects a subset of active neurons activation functions. The second one activation functions.

- It simplifies the backpropagation algorithm as $h'(a_j) = 1$ for the selected units. So, there is no gradient vanishing on the paths of selected units. Compare with the sigmoid or hyperbolic tangent, for which the sigmoid or hyperbolic tangent, for which the very zero due to saturation.
- this problem by simply returning one of two one-sided derivatives. Or using a generalization of the rectifier function. Regularization is the rectifier function. ▶ Note that h'(0) does not exist since $h'_+(0) \neq h'_-(0)$.
- Regularization is typically added to prevent numerical problems due to the activation being unbounded, e.g. when forward propagating.

Layer-Wise Pre-Training

- $\,$ The pre-training aims to find a good starting point for the subsequent run of the backpropagation algorithm.
- Supervised version:
- Train each layer of the DNN as if it was the hidden layer in a depth-two NN. As input, use the output of the last of the previously trained layers. As output, use the original classification or regression function.
 Run the backpropagation algorithm to fine-tune the weights.
- Unsupervised version: Similar to the supervised one but the hidden layers (except the last one) are trained to learn an encoding of the output of the previous layer, instead of the original classification or regression function.