# LETTERS

# Inapparent infections and cholera dynamics

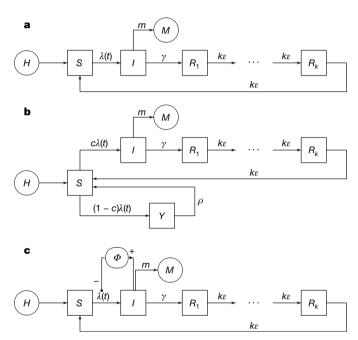
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In many infectious diseases, an unknown fraction of infections produce symptoms mild enough to go unrecorded, a fact that can seriously compromise the interpretation of epidemiological records. This is true for cholera, a pandemic bacterial disease. where estimates of the ratio of asymptomatic to symptomatic infections have ranged from 3 to 100 (refs 1-5). In the absence of direct evidence, understanding of fundamental aspects of cholera transmission, immunology and control has been based on assumptions about this ratio and about the immunological consequences of inapparent infections. Here we show that a model incorporating high asymptomatic ratio and rapidly waning immunity, with infection both from human and environmental sources, explains 50 yr of mortality data from 26 districts of Bengal, the pathogen's endemic home. We find that the asymptomatic ratio in cholera is far higher than had been previously supposed and that the immunity derived from mild infections wanes much more rapidly than earlier analyses have indicated. We find, too, that the environmental reservoir<sup>5,6</sup> (free-living pathogen) is directly responsible for relatively few infections but that it may be critical to the disease's endemicity. Our results demonstrate that inapparent infections can hold the key to interpreting the patterns of disease outbreaks. New statistical methods<sup>7</sup>, which allow rigorous maximum likelihood inference based on dynamical models incorporating multiple sources and outcomes of infection, seasonality, process noise, hidden variables and measurement error, make it possible to test more precise hypotheses and obtain unexpected results. Our experience suggests that the confrontation of time-series data with mechanistic models is likely to revise our understanding of the ecology of many infectious diseases.

Cholera is a diarrhoeal disease caused by enteric infection with the bacterium *Vibrio cholerae*. Six of the seven cholera pandemics that have swept the globe since 1817 originated in the low-lying, densely populated regions north of the Bay of Bengal, where the disease is endemic. Although much attention has been focused on cholera<sup>1.8</sup>, unsolved puzzles remain about its mode of transmission and the role of host immunity in its dynamics. This is largely because, in regions where cholera is endemic, most cholera cases are mild or asymptomatic but the true extent of asymptomatic infection has been difficult to assess. Estimates of the ratio of asymptomatic to symptomatic cases vary greatly, and the importance of inapparent infections in the dynamics of cholera outbreaks is unknown. To determine what role is played by inapparent infections, we used an approach that allows indirect inference about unobserved variables.

A remarkably rich data set on the pattern of cholera epidemics exists in the form of mortality records kept by the sanitary commissioners of the former British East Indian province of Bengal<sup>9</sup>. The data consist of monthly cholera death counts in each of 26 districts over the period 1891–1940 (Supplementary Fig. 1). To analyse these data, we formulated a series of models incorporating known or hypothesized mechanisms of transmission and immunity. A

parsimonious model for cholera dynamics is of susceptible—infectious—recovered—susceptible (SIRS) form (Fig. 1a). A novel feature of this model is that it incorporates both transmission tied to human prevalence (using a traditional mass-action term) and transmission from an environmental reservoir (where the pathogen is commonly living in aquatic environments)<sup>5,6,10–12</sup>. This model is a



**Figure 1** | **The mechanistic models used. a**, SIRS model; **b**, two-path model; **c**, environmental-phage model. Births, related to the total population size *H*, are assumed to feed the pool of susceptibles, S. Individuals are susceptible to infection when born. Exposure to the pathogen occurs at time-dependent rate  $\lambda(t)$ . c is the probability that an exposure leads to a contagious infection (class *I*). Note that when c = 1 and  $\rho = \infty$ , the two-path model (**b**) reduces to the SIRS model (a); when c < 1, some exposures result in short-term immunity (class Y). Infected individuals die at an excess rate m and recover at a rate  $\gamma$ ; the time an individual spends within the *I* class is exponentially distributed. We assume that an individual remains immune to reinfection for a duration gamma-distributed with mean  $1/\varepsilon$  and variance  $1/k\varepsilon^2$ . Once immunity has waned, an individual re-enters the susceptible pool (S). The measured variable is monthly deaths, M. The mean duration of short-term immunity is  $1/\rho$ . Individuals in each class are subject to constant background mortality at rate 0.02 yr<sup>-1</sup>. The force of infection,  $\lambda(t)$ , includes terms for environmental and human sources of infection and is assumed to vary seasonally. Because the seasonality of cholera dynamics in Bengal is complex, we used a semi-mechanistic approach: transmission was modelled by a flexible periodic function of time. In the environmental-phage model (c), as infected hosts shed pathogen, phage  $\Phi$  builds up in the environment and reduces transmissibility. The equations specifying these models are given in the Supplementary Equations.

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partially observed, nonlinear, stochastic dynamical system in continuous time and as such is not amenable to analysis by standard statistical techniques. Inference for such systems has recently been facilitated by a new likelihood maximization procedure<sup>7</sup> which allows for measurement error, non-stationarity, irregular sampling intervals and the mechanistic inclusion of covariates (see Methods). We fitted the SIRS model to each district's data, assessed its explanatory power using log likelihood and the Akaike information criterion (AIC $_c$ ) and compared it with a semi-mechanistic time-series model for cholera<sup>13</sup> and two non-mechanistic time-series models.

The SIRS model explained the data dramatically better than the previous best fit<sup>13</sup> ( $\triangle$ AIC<sub>c</sub> > 58; Supplementary Table 1). Parameter estimates reveal some surprises. A prediction of the model, robustly consistent across districts, is that immunity must wane on a timescale of weeks to months (Fig. 2 and Supplementary Table 3). This is in stark contrast to the widely held belief that infection-derived immunity to cholera wanes on a timescale of 3–10 yr (refs 13–17). The model also robustly predicts low case fatality (0.004  $\pm$  0.002, mean  $\pm$  s.d. across 26 districts). Because fatality among hospitalized cases was historically in excess of 50% 18, this implies a very large asymptomatic ratio. The implication is that most exposures result not in severe cholera, but in mild or asymptomatic infection, the immunological memory of which is short-lived. This prediction of a high asymptomatic ratio is consistent with the only intensive field studies of inapparent infections of which we are aware<sup>3,4</sup>. However, because in this model all infected individuals are equally infectious, the prediction is that the vast majority of infectives are 'silent shedders'—infectious but without symptoms. The evidence for such a conclusion is mixed but weak at best<sup>2</sup>. Moreover, because in this model all infections are alike, it is unclear whether the improved dynamical description afforded by the SIRS model over the previous best fit is due to the higher proportion of asymptomatic infections or to the shorter duration of immunity.

To tease apart the immunological consequences of exposure to the pathogen from the degree of infectiousness induced, and to allow for heterogeneity in infectiousness, we formulated a second mechanistic model in which exposed individuals can follow an alternate pathway, deriving immunity to infection while shedding a negligible quantity of vibrio and suffering a negligible disease-induced mortality (Fig. 1b). In essence, this model allows for the possibility that exposure to the pathogen effectively vaccinates against reinfection. We leave it to the data to determine how frequently such natural vaccination occurs and how long the resulting immunity lasts.

Under the two-path model, the timescale of short-term immunity  $(9.9 \pm 4.7 \, \text{weeks}, \, \text{mean} \pm \text{s.d.} \, \text{across} \, 26 \, \text{districts})$  agrees with that of the SIRS model. The estimated case fatality under this model is  $0.34 \pm 0.21$ —consistent with conditions during this period<sup>1</sup>—and survivors of severe infections receive longer-lasting immunity

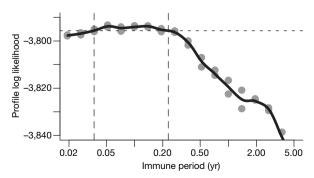


Figure 2 | Profile likelihood of the duration of immunity,  $1/\varepsilon$ , in the SIRS model for the data from Dacca district. Dacca (now spelled Dhaka) is the only district for which comparable analyses have been performed <sup>13,27</sup>. To compute the profile likelihood,  $\varepsilon$  is fixed and the likelihood is maximized over the remaining parameters. The vertical dashed lines embrace the approximate 95% confidence interval (2–12 weeks).

 $(1.5\pm0.7\,\mathrm{yr})$ , consistent with experimental evidence  $^{14,15,19}$ . Although in some districts the evidence strongly favours the two-path model, the data taken as a whole are equivocal on the subject of which model is better (see Supplementary Table 2). The implication is that it is the short-term immunity and high asymptomatic ratio predicted by both models, and not a large fraction of silent shedders, that accounts for the dramatically improved description afforded by our models.

A second robust prediction of both models is that, in typical epidemics, relatively few cases are due to the environmental reservoir. More precisely, though our models cannot speak to the exact route of transmission (that is, food-borne, water-borne, fomites, etc.), our results clearly indicate the relative importance of the positive feedback associated with the human-associated source of infection over the human-independent environmental source of infection. Nevertheless, the seasonally averaged basic reproductive number,  $R_0$ , for human-associated transmission is estimated to be quite low (SIRS model,  $1.5 \pm 0.2$ ; two-path model,  $1.5 \pm 0.2$ ). This contrasts sharply with the much higher values of  $R_0$  recently proposed<sup>20</sup> and suggests, paradoxically, that for V. cholerae, in this the region where cholera is most persistent and outbreaks most frequent, humans are potentially a marginal habitat: the persistence of the disease may be largely due to the environmental reservoir which provides a small extrinsic force of infection. The strength of this environmental force of infection varies geographically in a pattern (Supplementary Fig. 2) that mirrors the earlier suggestion that the coastal regions of Bangladesh are the native habitat of classical cholera<sup>21</sup>. Both the SIRS and two-path models make the simplifying assumption that the force of infection due to the environmental reservoir has negligible seasonal fluctuation. To relax this assumption<sup>22</sup>, we fit a third model which extends the SIRS model but allows for seasonality in the environmental reservoir. This model explains the data significantly better in many districts, but our conclusions about low  $R_0$ , rapid loss of immunity and high prevalence of inapparent infection remain unchanged (see Supplementary Information).

A central challenge in cholera epidemiology is to explain how the outbreaks can be so explosive at the outset and yet self-limiting to the point that sizable epidemics can recur twice annually. Our explanation contrasts sharply with those proposed earlier<sup>13,17</sup>. Simulations of the various models (Fig. 3) make plain the contrasts between the explanations. In the previous view, infection-derived immunity tends to wane over the scale of years, the explosiveness of outbreaks is controlled by spatial effects, and it is the seasonal drop in transmissibility (presumably related to environmental drivers) that stops the epidemics. Because in the previous view the ratio of deaths to infections is comparatively modest, the susceptible population is depleted only slightly by each epidemic and is continually replenished by births and the waning of immunity. In the new view, epidemics are again triggered by rising seasonal transmissibility and the presence of a reservoir, but the high asymptomatic ratio means that many more individuals are exposed. The vast majority of these receive short-term protection from infection so that depletion of the susceptible pool brings the epidemic to a halt. As immunity wanes, on the timescale of weeks to months, the susceptible pool is replenished, setting the stage for the next outbreak. In the new view, severe cases play little role in shaping the dynamics.

It has been proposed that the seasonality of cholera in this region may be due to the interaction of free-living vibrio with lytic bacteriophage in surface waters<sup>23–25</sup>. According to this hypothesis, as an epidemic progresses, the density of phage in the environment increases and survivorship of vibrio consequently declines, which in turn leads to attenuation of transmissibility. To determine whether such an effect might explain the data, we formulated a fourth model, which extends the SIRS model by allowing for phage to build up in the environment (as infected individuals shed pathogen into surface waters) and ultimately interrupt transmission (Fig. 1c and Supplementary Equations). Using the same methods, we estimated

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the strength and timescale of this effect; the results are presented in the Supplementary Information. In brief, the main conclusions described above are robust to the inclusion of the environmental phage effect: the estimated duration of immunity remains short  $(9.3 \pm 8.3 \text{ weeks})$ , fatality low  $(0.004 \pm 0.002)$ , compare the corresponding value for the SIRS model) and  $R_0$  small  $(1.6 \pm 0.3)$ . Overall, the historical mortality data are not strong evidence in favour of the environmental-phage hypothesis. Furthermore, a critical implication of the environmental-phage hypothesis is that the phage cycles must lag behind cholera cycles, but not too far: the initial drop in cholera cases is predicted to be roughly coincident with high levels of ambient phage. In the one instance where concurrent data on cholera cases and ambient phage densities are available, however, the phage appear to lag approximately 180 degrees behind cholera cases<sup>24</sup>. Thus cholera cases begin to fall while phage concentrations remain small, and cholera cases begin to climb again while phage densities remain high. This is further, independent, evidence against the notion that phage-vibrio interaction in the environment is responsible for cholera seasonality.

The models presented here make several testable predictions. In particular, our results suggest that population surveys using sensitive

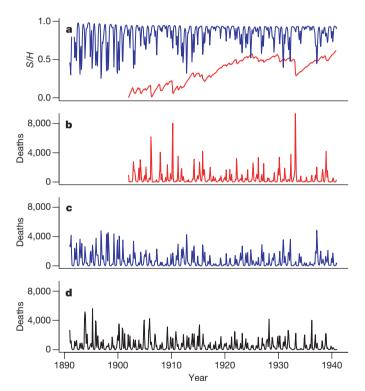


Figure 3 | Typical model simulations versus data for the district of Dacca. a, Simulated susceptible fraction (S/H) from our SIRS model with seasonal reservoir (blue) and from the time-series SIRS (TSIRS) model of Koelle et  $\it al.^{13,17}$  (red). The estimated susceptible fraction of the population is much lower under the TSIRS model, and grows with time. By contrast, under the models introduced here, rapid waning of immunity allows the susceptible fraction to return seasonally to high levels. The predicted high prevalence of inapparent infection implies that the susceptible pool is rapidly depleted during an outbreak. b, Simulated monthly deaths from the TSIRS model. Despite the low susceptible fraction and that model's non-mass-action transmission assumption, the relatively low prevalence of inapparent infection leads to overly explosive outbreaks and overly deep crashes. c, Simulated monthly deaths from the SIRS model with seasonal reservoir. d, Cholera death data from Dacca district. Parameter estimates for the seasonal-reservoir SIRS model are reported in the Supplementary Information; parameters for the TSIRS model are from K. Koelle (personal communication). The semi-parametric regression used to fit the TSIRS model is initialized using the first 11 yr of data: no simulated data are therefore generated over that interval.

techniques to detect the presence of *V. cholerae*, cholera-specific bacteriophage and/or coproantibodies in stools of healthy and mildly symptomatic individuals should reveal a much higher prevalence of inapparent infection than is currently understood to be the case. Such inapparent infections are predicted to be associated with reduced susceptibility to infection. Studies that centre on cholera patients, on the other hand, because they focus on the tail of the distribution of disease severity, can be expected to yield severely biased results when extrapolated to the population level. Further implications of our results for public health are discussed in the Supplementary Information.

In all models of epidemiological dynamics, critical quantities include the fraction of individuals susceptible to infection, immune from infection and asymptomatically infected. Yet it is almost never the case that available data include direct measurements of these quantities. Moreover, it is frequently true that many asymptomatic—or merely unrecorded—infections exist for each case that is recorded. Our results demonstrate that conclusions about the biological mechanisms underlying a pattern of disease outbreaks can depend sensitively on the prevalence of inapparent infections. New modelling approaches that allow indirect inference in the face of hidden variables and incomplete information are therefore likely to revise our understanding of the ecology of many infectious diseases.

#### **METHODS SUMMARY**

All models were formulated as stochastic differential equations, which were integrated using the Euler–Maruyama algorithm. Details of the equations and simulation methods are given in the Methods. The iterated filtering algorithm<sup>7</sup> was used to fit the models to the data. This algorithm is described in detail in the Supplementary Methods and is implemented as part of an open-source package, pomp, within the R statistical computing environment<sup>26</sup>. All codes will be made available by the authors on request.

**Full Methods** and any associated references are available in the online version of the paper at www.nature.com/nature.

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**Supplementary Information** is linked to the online version of the paper at www.nature.com/nature.

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**Author Contributions** A.A.K. formulated and implemented the models, implemented the fitting algorithm, performed the analyses, and drafted and revised the text. E.L.I. provided input on the models and statistical analyses, and drafted much of the Supplementary Information. M.P. provided input on the models and commented on the text. M.J.B. extracted and assembled the data and provided input on the models and on the historical and clinical aspects of cholera.

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#### **METHODS**

**Inference for dynamical systems.** A stochastic dynamical system is generated by a suitable function  $f(x, s, t, \theta, W)$ . Here, W is a stochastic quantity that is drawn independently each time the function is evaluated and  $\theta$  is a vector of parameters. Thus, for a sequence of times  $t_0 \le t_1 \le \cdots \le t_N$ , the recursion

$$X(t_n) = f(X(t_{n-1}), t_{n-1}, t_n, \theta, W),$$

together with the initial value  $X(t_0)$ , specifies a Markov process. The unspecified nature of  $f(\cdot)$  reflects the idea that the evolution of the system could correspond to an essentially arbitrary stochastic simulation algorithm. In the context of this paper, X(t) is a vector of counts in each disease class and  $f(\cdot)$  corresponds to a (numerical) solution of any of the stochastic differential equation systems in the Supplementary Equations. The data consist of observations  $y_1, \dots, y_n$  at times  $t_1, \dots, t_n$ . We suppose that, conditional on  $\{X(t_k) = x_k\}_{k=1}^n, y_n$  is drawn from a density  $g(y_n|x_{t_0}, t_{t_0}, \theta)$ .

In the Supplementary Methods, we present a pseudocode description of an iterated filtering methodology (maximization by iterated filtering, MIF) which has recently been shown to enable likelihood-based inference for this framework<sup>7</sup>. This procedure allows inference for rather general partially observed, stochastic, multivariate, continuous-time dynamical systems. The MIF algorithm also accommodates measurement error, non-stationarity, irregular observation times and the mechanistic inclusion of covariates. It has been implemented in the R statistical language<sup>26</sup> as part of the package pomp. Note that the algorithmic parameters play a role in the computational efficiency of the method but do not affect the scientific conclusions once likelihood maximization has been confirmed by diagnostic plots<sup>7</sup>. The package and all other codes will be made available by the first author on request.

Fitting the Bengal data. Our statistical inference technique is based on simulation of the stochastic dynamical system. To simulate the stochastic dynamical systems, we used the Euler-Maruyama numerical scheme<sup>28</sup> with a timestep of 0.05 months. We fit the parameters of each model to the data from each district using the algorithm given in the Supplementary Methods. We used J = 10,000particles, a fixed lag L = 60 and M = 80 iterations with a cooling factor, a = 0.95. Using the same algorithm, we then constructed profile likelihoods against the parameters  $\varepsilon$  and c. This analysis revealed the existence of weak non-identifiabilities among the parameters c,  $\gamma$ , m,  $\varepsilon$  and  $\rho$ . Despite this, certain combinations of parameters, such as  $R_0 = c \langle \beta_{\text{seas}}(t) \rangle / (\gamma + \delta + m)$  and the case fatality  $m / (\gamma + \delta)$ + m), are well-identified. Moreover, although estimates of the durations of short-term immunity vary considerably among districts, it is the case that, for all districts, the duration of immunity is predicted to be far shorter than that derived from severe infections induced experimentally 13-17. Construction of the profile likelihoods also facilitated the location of the global maximum likelihood estimates, which, after further refinement using the algorithm above with 30,000 particles, are reported in the Supplementary Tables.

Review of likelihood-based inference. We give a review of likelihood-based inference in the context of this paper. This review focuses on practical considerations; we refer the reader to Casella & Berger<sup>29</sup> or Rice<sup>30</sup> for a complete introduction, and to Barndorff-Nielsen & Cox<sup>31</sup> for a more advanced treatment. For a discussion of the role of likelihood, profile likelihood ratio tests applied to stochastic models for biological systems, we direct the reader to Hilborn & Mangel<sup>32</sup>. Reasons to use likelihood as a basis for inference include statistical efficiency (that is, making the strongest conclusions available from limited data), objectivity (that is, providing a single criterion applicable to a wide range of models and data) and the availability of useful techniques for comparing rival hypotheses.

For time-series data, written as  $x_{1:T} = x_1, \dots, x_T$ , a stochastic model consists of a density function  $f(x_{1:T}|\theta)$  depending on a vector  $\theta$  of unknown parameters. The likelihood function arises from considering the density as a function of  $\theta$ , treating the data as fixed. Thus the log likelihood is defined to be

$$\log \mathcal{L}(\theta) = \log f(x_{1:T}|\theta),$$

where log is the natural logarithm. Rival hypotheses, labelled  $H_0$  and  $H_1$ , concerning the appropriate structure for a stochastic model can be formalized in terms of whether  $\theta$  takes a value in  $\Theta_0$  or  $\Theta_1$  respectively, where  $\Theta_0$  and  $\Theta_1$  are subsets of the set  $\Theta$  of all possible parameter vectors. We refer to  $H_0$  and  $H_1$  as hypotheses or models interchangeably.

**Comparison of nested models.** Suppose that  $H_0$  and  $H_1$  are nested, meaning that  $\Theta_0$  is a subset of  $\Theta_1$ . In practical terms, this is taken to mean that  $\Theta_0$  is described by  $d_0$  freely varying parameters, whereas  $\Theta_1$  is described by these  $d_0$  parameters together with a number  $d_1-d_0$  of additional parameters. Thus  $\Theta_0$  can be written in terms of a vector of length  $d_0$  and  $\Theta_1$  in terms of a vector of length  $d_1$ . The

maximum likelihood parameter estimate for model  $H_0$  is denoted by  $\hat{\theta}_0$ , and corresponds to the parameter value giving rise to the largest value of  $\log \mathcal{L}(\theta)$  among all values of  $\theta$  in  $\Theta_0$ . A corresponding definition applies to  $\hat{\theta}_1$ . Because  $\Theta_1$  includes  $\Theta_0$ , it follows that  $\log \mathcal{L}(\hat{\theta}_1) \geq \log \mathcal{L}(\hat{\theta}_0)$ . Under standard regularity conditions, twice the improvement in the log likelihood that occurs when moving from the simpler model  $H_0$  to the more complex model  $H_1$  can be compared with a  $\chi^2$  random variable on  $d_1-d_0$  degrees of freedom. Thus, Supplementary Table 1 presents a P-value of the form

$$P = \operatorname{Prob}\left[\chi_{d_1 - d_0}^2 > 2\left\{\log \mathcal{L}\left(\hat{\theta}_1\right) - \log \mathcal{L}\left(\hat{\theta}_0\right)\right\}\right]. \tag{1}$$

The *P*-value given by equation (1) is an approximation. More precise *P*-values can in principle be obtained by simulation, but this  $\chi^2$  approximation is a widely used technique that has been found to be reliable for many practical purposes<sup>33</sup>. It is both conceptually and operationally simpler to calculate initially the standard  $\chi^2$  approximation in equation (1); if this gives rise to an unequivocal answer, there is little reason to present a simulation study as additional evidence.

Modifications to equation (1) are required when the models under consideration are nested in a non-standard way<sup>34</sup>. This arises in the context of the analysis presented in Supplementary Table 1, owing to the non-standard nesting of the two-path model within the SIRS model. Specifically, the two-path model reduces to the SIRS model when c=1 at which point  $\rho$  is unidentified. Anisimova et al.<sup>35</sup> investigated similar situations and demonstrated that the chi-squared approximation to the likelihood ratio test is conservative in such cases. In the caption of Supplementary Table 1, we report the P-value associated with such a test on three degrees of freedom:  $\rho$ , c and the initial condition  $Y_0$ .

Non-nested models may still be compared by their likelihood, for example by the use of Akaike's information criterion<sup>36,37</sup>, but formal testing of hypotheses becomes more awkward. Thus, in Supplementary Table 1, we contrast the best-fitting SIRS model with the nested SIRS model constrained to match the duration of immunity found by Koelle & Pascual<sup>13</sup>. Another consideration motivating this comparison is that the nested SIRS model has a similar likelihood to the model of Koelle & Pascual<sup>13</sup>, while having fewer parameters to estimate. Additionally, this approach avoids the issue that the comparison with previously published models might be unfair because the procedure used to fit the models in this paper may be more effective than that used by previous research.

**Profile likelihood.** The profile likelihood is a description of the weight of evidence about the value of a single component of the vector of unknown parameters. Setting  $\theta = (\theta_1, \dots, \theta_d)$ , the log likelihood can be written as  $\log \mathcal{L}(\theta_1, \dots, \theta_d)$  and the profile log likelihood of  $\theta_1$  is

$$\log \mathcal{L}_{profile}(\theta_1) = \max_{\theta_2, \dots, \theta_d} \log \mathcal{L}(\theta_1, \dots, \theta_d).$$

From equation (1), a 95% confidence region for  $\theta_1$  is given by the range of values of  $\theta_1$  for which

$$2\left(\log \mathcal{L}\left(\hat{\theta}\right) - \log \mathcal{L}_{\text{profile}}(\theta_1)\right) < c,$$

where *c* is defined by Prob  $\left[\chi_1^2 < c\right] = 0.95$ . This is how the confidence interval in Fig. 2 was constructed.

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# SUPPLEMENTARY INFORMATION

# Inapparent infections and cholera dynamics Supplementary Information

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#### **Supplementary Equations**

SIRS and two-path model equations. We let S(t) denote the real-valued approximation to the (integer-valued) number of individuals in class S at time t. I(t),  $R_1(t)$ , ...,  $R_k(t)$ , Y(t) are defined similarly. The diagram in Fig. 1B is interpreted as a system of coupled stochastic differential equations,

$$\frac{dS}{dt} = k\epsilon R_k + \rho Y + \frac{dH}{dt}(t) + \delta H(t) - (\lambda(t) + \delta) S$$

$$\frac{dI}{dt} = c\lambda(t) S - (m + \gamma + \delta) I$$

$$\frac{dY}{dt} = (1 - c)\lambda(t) S - (\rho + \delta) Y$$

$$\frac{dR_1}{dt} = \gamma I - (k\epsilon + \delta) R_1$$

$$\vdots$$

$$\frac{dR_k}{dt} = k\epsilon R_{k-1} - (k\epsilon + \delta) R_k$$
(1)

In the case c = 1, these equations collapse to the SIRS model. Environmental stochasticity enters through noise added to the time-varying force of infection,  $\lambda(t)$ . This is modeled by

$$\lambda(t) = \omega + \left[\bar{\beta} e^{\beta_{trend} t} \beta_{seas}(t) + \sigma \xi(t)\right] \frac{I(t)}{H(t)}.$$

Here  $\xi(t) = dW/dt(t)$ , Gaussian white noise<sup>1</sup>. Although the Brownian motion W(t) is not differentiable,  $\xi(t)$  is interpreted via the convention that  $\xi(t) dt = dW(t)$ . Multiplying Eq. 1 through by dt then gives an infinitesimal equation. The Gaussian infinitesimal dW(t) is basic to the construction and solution of stochastic differential equations<sup>2,3</sup>. The term  $\bar{\beta} e^{\beta_{trend} t} \beta_{seas}(t) + \sigma \xi(t)$  corresponds to human-to-human transmission. Seasonality of transmission is modeled by

$$\log \beta_{seas}(t) = \sum_{k=0}^{5} b_k s_k(t),$$

where  $\{s_k(t)\}$  is a periodic cubic B-spline basis<sup>4</sup> defined so that  $s_k(t)$  has a maximum at t = (2k+1)/12 and normalized so that  $\sum_{k=0}^{5} s_k(t) = 1$ . Here, time is measured in units of years;  $\beta_{trend}$  captures a long-term change in transmission rates;  $\sigma$  is an environmental stochasticity parameter, resulting in infinitesimal variance proportional to  $S^2$ ; and  $\omega$  corresponds to a non-human reservoir of disease. The scaling constant  $\bar{\beta} = 1$  yr<sup>-1</sup>.

All other transitions in Eq. 1 except those from S to I and Y, are modeled deterministically, ignoring demographic stochasticity. The parameter c is the probability that an exposure leads to a contagious infection;  $\gamma$  is the rate at which individuals recover;  $1/\varepsilon$  is the mean duration of immunity;  $1/\sqrt{k}$  is the coefficient of variation of the immune period;  $1/\rho$  is the mean duration of short-term immunity;  $1/\delta$  is the life expectancy excluding cholera mortality. Analysis of a subset of districts showed that the shape parameter k=3 gave the best results. We fixed k at this value for all subsequent analyses.

The population size H(t), and hence also dH/dt, are treated as known via interpolation from decadal census data. The equation for dS/dt in Eq. 1 is based on cholera mortality being a

negligible proportion of total mortality. The number of fatal cholera cases for the n-th month, n = 1, ..., 600, is modeled as  $M_n = \int_{(n-1)/12}^{n/12} mI(t) dt$ . The relationship of  $M_n$  to the observed mortality  $y_n$  is modeled by a conditional Gaussian distribution,  $y_n \sim \text{normal}(M_n, \tau^2 M_n^2)$ . This allows for variability in the accuracy of reporting, with variance is proportional to  $M_n^2$ . It allows for over-reporting, e.g., due to misdiagnosis, as well as under-reporting.

There is some subtlety in the correct interpretation of  $\beta$  and  $\omega$ . In the context of the models, these quantities are just two components of the force of infection:  $\beta$  scales that component proportional to the size of the infective pool;  $\omega$  quantifies the component independent of the infective pool. From the perspective of the disease dynamics, the distinguishing property of "human-to-human" transmission is not whether it occurs through water, food, fomites, or still another route, but whether its rate is influenced by previous levels of infection in the population, *i.e.*, through a dynamical feedback. Transmission from a reservoir is from this perspective unambiguously distinguished from "human-to-human" transmission by its being effectively decoupled from the previous dynamics of the disease. This distinction is of fundamental importance for the dynamics <sup>5,6</sup>.

Seasonality in the environmental reservoir. The models above assume that the environmental reservoir is constant in time. We can relax this assumption by letting  $\omega = \omega(t)$ , as we have done with the transmission rate,  $\beta_{seas}(t)$ . This has the effect of introducing more parameters and making the model more flexible. Because it allows for the seasonality to be explained—in whole or in part—by the environmental reservoir, it also has the potential to change the results derived using the simpler models. To model  $\omega(t)$ , we use the same six-knot periodic B-spline basis as before:

$$\log \frac{\omega(t)}{\bar{\omega}} = \sum_{k=0}^{5} \omega_k \, s_k(t),$$

The scaling constant  $\bar{\omega}=1~{\rm yr}^{-1}$ . (Of course, the parameters  $\omega_k$  are estimated entirely independently of  $b_k$ .) Maximum likelihood estimates of all parameters for this seasonal-reservoir model are presented in Table S-5. In some districts, as judged by AIC<sub>c</sub>, there is sufficient information in the data to support the additional parameters. In all districts, however, the seasonal signal in  $\beta$  remains strong. Critically, the predictions of high prevalence of inapparent infection, rapidly-waning immunity, and low  $R_0$  are robust to the inclusion of seasonality in the reservoir: estimated case fatality  $0.004 \pm 0.002$ ; estimated duration of immunity,  $9.6 \pm 8.2$  wk; estimated  $R_0$ ,  $1.5 \pm 0.2$ . Moreover, as do the simpler models, this model predicts a small force of infection from the reservoir relative to the total:  $1.3 \pm 0.5\%$  (mean  $\pm$  SE) of all cases derive from this source of infection under the seasonal-reservoir model vs.  $1.0 \pm 0.4\%$  for the SIRS model and  $0.19 \pm 0.06\%$  for the two-path model.

Environmental-phage model equations. In a theoretical investigation, Jensen  $et\ al.^7$  examined the hypothesis that build-up of ambient phage can interrupt transmission. We formulated a model to evaluate this hypothesis against the historical cholera mortality data. The environmental-phage model is built to extend the SIRS model. The equations are those of Eq. 1 with c=1 with

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one additional state variable:

$$\frac{dS}{dt} = k\epsilon R_k + \frac{dH}{dt}(t) + \delta H(t) - (\lambda_{\phi}(t) + \delta) S$$

$$\frac{dI}{dt} = \lambda_{\phi}(t) S - (m + \gamma + \delta) I$$

$$\frac{dR_1}{dt} = \gamma I - (k\epsilon + \delta) R_1$$

$$\vdots$$

$$\frac{dR_k}{dt} = k\epsilon R_{k-1} - (k\epsilon + \delta) R_k$$

$$\frac{d\Phi}{dt} = I - \mu \Phi$$

Here,  $\Phi$  represents the effect of lytic vibriophage in the environment. Ambient phage are assumed to have first-order kinetics, with a source term proportional to the number of infections and an exponential decay term. The effect of buildup of ambient phage is to reduce the force of infection,  $\lambda_{\phi}$ :

$$\lambda_{\phi}(t) = \frac{\lambda(t)}{1 + a \, \Phi(t)}$$

There are two additional parameters and one initial condition to be estimated from the data: the phage decay constant is  $\mu$ , the parameter a measures the strength of the environmental phage effect.

# Supplementary Methods

#### Algorithm: maximum likelihood via iterated filtering

#### Model input:

```
process model f(\cdot), measurement model g(\cdot|\cdot), data y_1, \ldots, y_N, times t_0, \ldots, t_N
```

#### Algorithmic parameters:

```
number of particles J, fixed lag L, number of iterations M; cooling factor 0 < a < 1, b > 0; initial state vector X_I^{(1)}, initial parameter vector \theta^{(1)}; variance-covariance matrices \Sigma_I, \Sigma_{\theta}.
```

#### **Procedure:**

```
1. for m=1 to M
        draw X_I(t_0, j) \sim \text{normal}(X_I^{(m)}, a^{m-1}\Sigma_I), \quad j = 1, \dots, J
        set X_F(t_0, j) = X_I(t_0, j)
 3.
        draw \theta(t_0, j) \sim \text{normal}(\theta^{(m)}, ba^{m-1}\Sigma_{\theta})
 4.
 5.
        set \bar{\theta}(t_0) = \theta^{(m)}
 6.
        for n = 1 to N
 7.
           set X_P(t_n, j) = f(X_F(t_{n-1}, j), t_{n-1}, t_n, \theta(t_{n-1}, j), W)
           set w(n, j) = q(y_n | X_P(t_n, j), t_n, \theta(t_{n-1}, j))
 8.
 9.
            draw k_1, \ldots, k_J such that \text{Prob}[k_i = i] = w(n, i) / \sum_l w(n, l)
10.
           set X_F(t_n, j) = X_P(t_n, k_i)
            set X_I(t_n, j) = X_I(t_{n-1}, k_j)
11.
           draw \theta(t_n, j) \sim \text{normal}(\theta(t_{n-1}, k_j), a^{m-1}(t_n - t_{n-1})\Sigma_{\theta})
12.
            set \bar{\theta}_i(t_n) to be the sample mean of \{\theta_i(t_{n-1},k_i), j=1,\ldots,J\}
13.
            set V_i(t_n) to be the sample variance of \{\theta_i(t_n, j), j = 1, \dots, J\}
14.
15.
        end for
        \theta_i^{(m+1)} = \theta_i^{(m)} + V_i(t_1) \sum_{n=1}^N V_i^{-1}(t_n) (\bar{\theta}_i(t_n) - \bar{\theta}_i(t_{n-1}))
16.
        set X_I^{(m+1)} to be the sample mean of \{X_I(t_L, j), j = 1, \dots, J\}
17.
```

#### Return:

18. end for

```
maximum likelihood estimate for parameters, \hat{\theta} = \theta^{(M+1)};
maximum likelihood estimate for initial values, \hat{X}(t_0) = X_I^{(M+1)};
maximized log likelihood estimate, \log \mathcal{L}(\hat{\theta}) = \sum_n \log(\sum_j w(n,j)/J)
```

#### Note:

Here, normal  $(\mu, \Sigma)$  denotes a multivariate normal random variable with mean vector  $\mu$  and covariance matrix  $\Sigma$ .  $X(t_n)$  takes values in  $\mathbb{R}^{d_x}$ ,  $y_n$  takes values in  $\mathbb{R}^{d_y}$ ,  $\theta$  takes values in  $\mathbb{R}^{d_\theta}$  and has components  $\{\theta_i, i = 1, \ldots, d_\theta\}$ . The computationally challenging steps (6–15) correspond to a standard implementation of particle filtering<sup>8</sup>; many refinements are possible within the context of this algorithm. The update equation (16) is the main innovation of Ionides et al.<sup>9</sup>.

#### Supplementary Discussion

Biological basis for short-term immunity. Our results imply that, in the vast bulk of cases, exposure to the pathogen induces a rapidly-waning protection from reinfection; they also give some clues as to the likely nature of this protection. Such protection may derive entirely from the host immune system. It is known that protection is due to the secretory IgA antibody response localized to the mucosae of the gut <sup>10–20</sup>. Both laboratory and field studies suggest that, following recovery, mucosal IgA levels wane on a timescale commensurate with our predictions <sup>18,21,22</sup>. On the other hand, it may also be that the high asymptomatic ratio and short-term protection effects derive in part from a high prevalence of coinfection with lytic bacteriophage (a mechanism distinct from the putative environmental effect of phage discussed in the preceding paragraph). Many observations have been made of such coinfection and of its protective effects <sup>23–25</sup>, but it remains unclear how commonly phage coinfection is responsible for reducing disease severity in the field. In short, while plausible biological mechanisms for the effects revealed here exist, further work is needed to fully elucidate the immunological and ecological consequences of asymptomatic cholera infections.

**Public health implications.** Many decades of effort have gone into cholera vaccine research. Though reasonably effective vaccines have been developed, the protection they afford typically wanes within a short time <sup>26</sup>. Our results not only confirm the suspicion that this may be the best that can be hoped for, but suggest that "natural vaccination" is the key to understanding why cholera outbreaks were historically not more deadly than they were. They suggest too that even the incomplete and rapidly-waning immunity provided by an inexpensive vaccine could be effective at controlling outbreaks if applied immediately prior to an outbreak's (predicted) initiation.

Further public health implications of our findings center on what determines whether an exposure results in contagious infection and/or acquired immunity. Dose-size almost certainly plays a key role <sup>27–31</sup>; transmission route may as well <sup>28,29</sup>. Thus while a relatively small dose of live bacteria induces a severe case of cholera when the innoculum is buffered, as by food, a large dose is needed when delivery is via contaminated water <sup>27,29,32</sup>. Moreover, the fact that recently-shed vibrio <sup>33</sup> are hyperinfectious implies that within-household transmission is more likely to result in severe infection. These facts, together with the relatively small estimated magnitude of the environmental reservoir effect, suggests the need for experimental quantification of routes of transmission other than the water-borne.

Comparison with earlier models. The continuous-time mechanistic models presented here represent a distinct improvement in explanatory power over the discrete-time models that have been applied before to cholera<sup>34,35</sup> and other infectious diseases<sup>36,37</sup>. This is in part due to the greater flexibility of the continuous-time models (see Fig. S-3), which can readily include terms for environmental force of infection, seasonality in one or more transmission rates, etc. Such models can be fitted because our inference method is simulation based. The models used here, moreover, take account of measurement error in addition to process noise. Previous approaches<sup>34,35</sup> assumed that all variability in the data was due to process noise. Finally, time discretization itself can introduce instability into model dynamics<sup>38</sup>. The appearance of non-mass-action transmission terms in TSIR-type models may be attributable, at least in part, to the need to tame this instability. This departure between the discrete-time model and the continuous-time process it is meant to represent may introduce bias into the estimates obtained using discrete-time models.

## Supplementary Figures

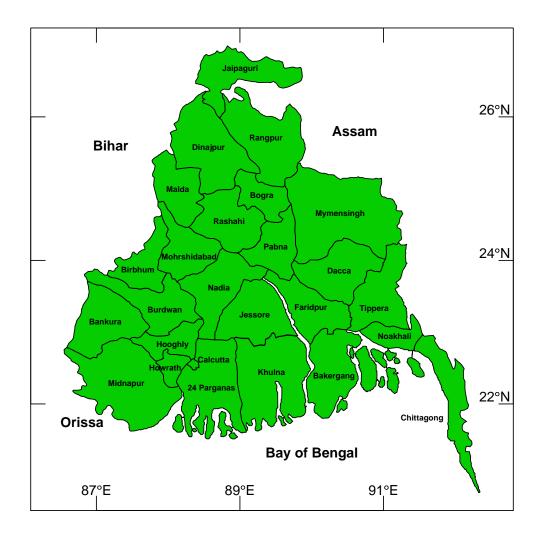


Figure S-1: The 26 districts for which we fit models to cholera mortality data. Data from the northern highlands district of Darjeeling were also available, but we were not successful in fitting the models to these data. This failure is likely due to the fact that, in Darjeeling district, cholera incidence is generally quite low and, in fact, the disease is entirely absent for months at a time. Our models are designed for endemic cholera dynamics and thus fail to accommodate the extremely epidemic dynamics of Darjeeling.

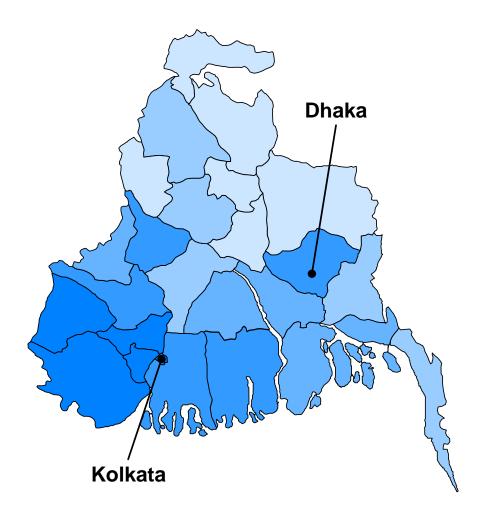


Figure S-2: Estimates of the environmental reservoir parameter,  $\omega$ , for each of the 26 districts, under the SIRS model. Darker color corresponds to higher values of the parameter. The geographical pattern mirrors the suggestion that the southern regions of Bangladesh are the native habitat of classical cholera<sup>39</sup>. The pattern is similar under the two-path model. Numerical values of estimates of this and the other model parameters are provided in the Supplementary Tables.

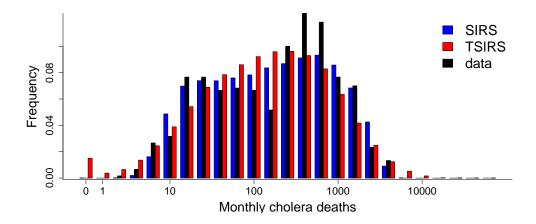


Figure S-3: Comparison of discrete- and continuous-time model predictions. Distributions of actual monthly deaths from the Dacca district (1891–1940, black) and simulated monthly cholera deaths from the continuous-time SIRS model with seasonal reservoir (blue) and the discrete-time TSIRS model of Koelle & Pascual<sup>34</sup> (red). The TSIRS model overpredicts both large epidemics and fadeouts. With fewer parameters, the continuous-time SIRS model is nevertheless considerably more flexible: the distribution it predicts is more compact and it captures some of the bimodality apparent in the data. Model parameters used correspond to the Dacca district; for each model, 200 simulated time series were used.

## Supplementary Tables

Table S-1: Model comparison for the data from Dacca, (nowadays spelled Dhaka) the only district for which comparable analyses have been performed <sup>34,40</sup>. We compared models using log likelihood and second-order Akaike information criterion (AIC<sub>c</sub>). AIC<sub>c</sub> is defined as  $-2 \log \mathcal{L} +$ (2k+2(k+1)/(n-k-1)), where  $\mathcal{L}$  is the likelihood, k is the number of fitted parameters and n is the number of observations. Two non-mechanistic models are used to establish a baseline for comparison. The first (seasonal mean) simply uses the monthly mean and variance in mortality. The second is a seasonal autoregressive moving-average (SARMA) model. While these models give some indication as to how predictable the data series are, they are not easy to interpret since they lack all description of mechanism. The semi-parametric method of Koelle & Pascual 34 does not lend itself to easy determination of the effective number of parameters; we report a lower bound on the AIC<sub>c</sub> for this model. When the SIRS model is constrained to a 4 yr mean immunity, comparable to the estimate of Koelle & Pascual<sup>34</sup>, the log likelihood (-3843.3) is also comparable. The increase in log likelihood obtained from removing the constraint  $1/\varepsilon = 4$  yr is highly statistically signficant (p < 0.001, likelihood ratio test, df = 1); likewise the two-path model affords a significantly better fit (p < 0.001, likelihood ratio test, df = 3, see Supplementary Methods) than the SIRS model.Parameter estimates for all districts are in Tables S-3 through S-6.

model	log likelihood	$AIC_c$
SIRS with seasonal reservoir	-3763.8	7573.4
two-path	-3784.7	7610.8
environmental-phage	-3787.9	7617.2
SIRS	-3793.4	7621.9
$SARMA((2,2)\times(1,1))$	-3804.5	7625.2
Koelle & Pascual <sup>34</sup>	-3840.1	> 7680.1
seasonal mean	-3989.1	8028.2

Table S-2: **Model comparison for all districts.** The quantities shown are  $\Delta AIC_c$ , i.e., the difference in  $AIC_c$  between a given model and the best model (smallest  $AIC_c$ ) for that district (denoted by \*).

	SIRS	two-path	seasonal-reservoir	environmental-phage
Bakergang	7.4	*	15.4	16.5
Bankura	*	2.0	11.5	8.8
Birbhum	1.2	16.4	*	8.4
Bogra	17.0	*	24.7	40.9
Burdwan	50.6	63.3	*	56.1
Calcutta	6.2	*	8.9	13.9
Chittagong	19.7	13.1	23.7	*
Dacca	48.4	37.4	*	43.8
Dinajpur	5.7	11.4	17.7	*
Faridpur	49.8	52.6	*	55.5
Hooghly	40.6	53.7	*	47.5
Howrath	9.8	3.0	*	17.2
Jaipaguri	7.1	7.3	*	7.0
Jessore	18.2	25.4	*	24.9
Khulna	9.6	11.4	*	5.8
Malda	14.5	14.9	30.5	*
Midnapur	*	1.7	4.6	9.4
Mohrshidabad	*	14.1	2.1	6.5
Mymensingh	22.7	8.8	37.7	*
Nadia	4.1	10.4	*	10.1
Noakhali	4.1	*	5.0	11.0
Pabna	2.5	*	12.4	10.5
Rangpur	3.3	*	7.8	6.7
Rashahi	16.2	32.5	*	24.1
Tippera	29.9	34.0	41.3	*
24 Parganas	39.2	51.0	*	46.4

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Table S-3: Maximum likelihood estimates for the SIRS model. The units of  $\gamma$ , m,  $\varepsilon$ ,  $\omega$ , and  $\beta_{trend}$  are yr<sup>-1</sup>; the other quantities are dimensionless.

	1 0	ATC	$r^2$						1
Dalsannann	$\log \mathcal{L}$	$AIC_c$		$R_0$	$\frac{\gamma}{11.2}$	0.028		$\varepsilon$	$\frac{\log \omega}{\varepsilon}$
Bakergang	-3663.2	7361.4	0.855	1.35		0.028	36.		-5.0
Bankura	-3039.0	6113.0	0.568	1.45	7.3	0.019	3.		-3.5
Birbhum	-3082.4	6199.9	0.492	1.52	9.0	0.066	13.		-4.9
Bogra	-2849.2	5733.4	0.545	1.97	14.1	0.044	2.		-10.2
Burdwan	-3412.4	6859.9	0.584	1.48	5.0	0.043	6.		-4.0
Calcutta	-3041.7	6118.5	0.759	1.22	16.0	0.028	51.		-3.5
Chittagong	-3255.0	6545.1	0.709	1.53	4.9	0.043	4.		-5.9
Dacca	-3793.4	7621.9	0.849	1.28	17.3	0.057	9.		-4.8
Dinajpur	-2946.2	5927.4	0.501	1.64	12.3	0.021	3.		-5.6
Faridpur	-3661.8	7358.7	0.785	1.31	19.3	0.066	6.		-5.0
Hooghly	-3248.6	6532.2	0.575	1.09	7.1	0.019	10.		-2.3
Howrath	-3372.1	6779.2	0.769	1.33	7.7	0.041	6.		-3.7
Jaipaguri	-2391.1	4817.3	0.592	1.41	22.9	0.104	3.		-9.4
Jessore	-3500.9	7036.9	0.750	1.57	15.8	0.036	12.		-5.2
Khulna	-3508.8	7052.7	0.722	1.40	8.0	0.024	32.		-4.3
Malda	-2903.4	5841.8	0.589	1.73	25.5	0.090	3.		-10.9
Midnapur	-3881.5	7798.1	0.670	1.32	5.4	0.014	21.		-2.3
Mohrshidabad	-3400.7	6836.5	0.624	1.69	11.3	0.036	5.		-4.8
Mymensingh	-3989.7	8014.4	0.803	1.36	17.3	0.069	9.		-8.3
Nadia	-3403.3	6841.6	0.732	1.63	12.2	0.032	27.		-5.4
Noakhali	-3477.0	6989.0	0.695	1.80	6.0	0.032	2.		-5.0
Pabna	-3288.3	6611.6	0.694	1.48	23.0	0.102	3.		-9.5
Rangpur	-3269.0	6573.1	0.633	1.52	14.7	0.070	1.		-7.4
Rashahi	-3301.9	6638.8	0.694	1.48	16.6	0.056	5.		-5.8
Tippera	-3647.8	7330.6	0.763	1.50	11.4	0.017	23.		-5.4
24 Parganas	-3777.8	7590.7	0.844	1.35	6.3	0.034	15.	4	-3.8
	$\beta_{trend} \times 10$	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$	σ	$\tau$
Bakergang	$\beta_{trend} \times 10^{-5}$	$\frac{b_0}{1}$ $\frac{b_0}{0.1}$	$b_1 = 7.1$	$\frac{b_2}{-8.6}$	b <sub>3</sub> 1.9	$b_4$ 2.1	$b_5$ 5.3	$\frac{\sigma}{2.6}$	$\tau$ 0.33
Bakergang Bankura	$\beta_{trend} \times 10$ $-5$ $-3$	$ \begin{array}{c cccc}  & b_0 \\  & 0.1 \\  & 3.0 \end{array} $	$b_1$ 7.1 3.1	$b_2$ $-8.6$ $0.7$	b <sub>3</sub> 1.9 4.9	$b_4$ 2.1 -2.6	$b_5$ $5.3$ $2.6$	$\frac{\sigma}{2.6}$ $3.7$	$ \begin{array}{c} \tau \\ 0.33 \\ 0.48 \end{array} $
Bakergang Bankura Birbhum	$\beta_{trend} \times 10^{-5}$ 35.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$b_1$ 7.1 3.1 3.8	$b_2$ -8.6 0.7 0.6	b <sub>3</sub> 1.9 4.9 4.4	$b_4$ 2.1 -2.6 0.4	$b_5$ $5.3$ $2.6$ $4.4$	$\frac{\sigma}{2.6}$ $3.7$ $4.0$	$ au 0.33 \\ 0.48 \\ 0.53$
Bakergang Bankura Birbhum Bogra	$\beta_{trend} \times 10^{-5}$ 556.	$ \begin{array}{c cccc}  & b_0 \\  & 0.1 \\  & 3.0 \\  & 1.7 \\  & 6 & 2.3 \end{array} $	$b_1$ 7.1 3.1 3.8 4.7	$b_2$ -8.6 0.7 0.6 1.9	$b_3$ 1.9 4.9 4.4 3.4	$ \begin{array}{r} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \end{array} $	$b_5$ $5.3$ $2.6$ $4.4$ $3.3$	$ \begin{array}{c} \sigma \\ 2.6 \\ 3.7 \\ 4.0 \\ 4.9 \end{array} $	$ au 0.33 \\ 0.48 \\ 0.53 \\ 0.66 \\$
Bakergang Bankura Birbhum Bogra Burdwan	$\beta_{trend} \times 10^{-5}$ .  -5.  -5.  -6.  -8.	$ \begin{array}{c cccc} \hline 3 & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \end{array} $	$b_1$ 7.1 3.1 3.8 4.7	$ \begin{array}{r} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \end{array} $	b <sub>3</sub> 1.9 4.9 4.4 3.4 1.6	$ \begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \end{array} $	$b_5$ $5.3$ $2.6$ $4.4$ $3.3$ $3.0$	$ \begin{array}{c} \sigma \\ 2.6 \\ 3.7 \\ 4.0 \\ 4.9 \\ 3.5 \end{array} $	au 0.33 0.48 0.53 0.66 0.38
Bakergang Bankura Birbhum Bogra Burdwan Calcutta	$\beta_{trend} \times 10^{-5}$ .  -5.  -3.  -5.  -6.  -8.  -4.	$\begin{array}{cccc}  & & b_0 \\ 1 & & 0.1 \\ 2 & & 3.0 \\ 1 & & 1.7 \\ 6 & & 2.3 \\ 8 & & 1.7 \\ 7 & & 3.0 \end{array}$	$b_1$ 7.1 3.1 3.8 4.7 4.7 3.8	$ \begin{array}{r} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \end{array} $	$ \begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \end{array} $	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \end{array}$	$b_5$ $5.3$ $2.6$ $4.4$ $3.3$ $3.0$ $3.1$	$ \begin{array}{c} \sigma \\ 2.6 \\ 3.7 \\ 4.0 \\ 4.9 \\ 3.5 \\ 2.1 \end{array} $	au 0.33 0.48 0.53 0.66 0.38 0.23
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong	$\beta_{trend} \times 10^{-5}$ .  -535684.	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \end{array} $	$ \begin{array}{r} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \end{array} $	$ \begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \end{array} $	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \end{array}$	$b_5$ $5.3$ $2.6$ $4.4$ $3.3$ $3.0$ $3.1$ $4.6$	σ 2.6 3.7 4.0 4.9 3.5 2.1 3.0	$\begin{array}{c} \tau \\ 0.33 \\ 0.48 \\ 0.53 \\ 0.66 \\ 0.38 \\ 0.23 \\ 0.42 \end{array}$
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca	$\beta_{trend} \times 10$ -5356810.	$\begin{array}{c cccc} & & & & & & \\ \hline & & & & & \\ 1 & & & & \\ 2 & & & & \\ 3.0 & & & \\ 1 & & & & \\ 1.7 & & & \\ 6 & & & & \\ 2.3 & & & \\ 8 & & & & \\ 1.7 & & & \\ 7 & & & & \\ 3.0 & & & \\ 7 & & & & \\ 0 & & & & \\ 1.2 & & & \\ \end{array}$	$ \begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \end{array} $	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \end{array}$	$ \begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \end{array} $	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \end{array}$	$b_5$ $5.3$ $2.6$ $4.4$ $3.3$ $3.0$ $3.1$ $4.6$ $4.3$	σ 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2	$\begin{array}{c} \tau \\ 0.33 \\ 0.48 \\ 0.53 \\ 0.66 \\ 0.38 \\ 0.23 \\ 0.42 \\ 0.25 \end{array}$
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur	$\beta_{trend} \times 10$ -5356841055.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \end{array}$	$\begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \end{array}$	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \end{array}$	σ 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2	$\begin{array}{c} \tau \\ 0.33 \\ 0.48 \\ 0.53 \\ 0.66 \\ 0.38 \\ 0.23 \\ 0.42 \\ 0.25 \\ 0.63 \end{array}$
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur	$\beta_{trend} \times 10$ -5356810555.	$\begin{array}{c cccc} & b_0 & & & \\ \hline 1 & 0.1 & 2 & 3.0 \\ 1 & 1.7 & & \\ 6 & 2.3 & & \\ 8 & 1.7 & & \\ 7 & 3.0 & & \\ 7 & -0.8 & & \\ 0 & 1.2 & & \\ 1 & 1.9 & & \\ 0 & 1.4 & & \\ \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \end{array}$	b <sub>3</sub> 1.9 4.9 4.4 3.4 1.6 2.2 1.0 3.9 1.8 4.3	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \end{array}$	σ 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4	$\begin{array}{c} \tau \\ 0.33 \\ 0.48 \\ 0.53 \\ 0.66 \\ 0.38 \\ 0.23 \\ 0.42 \\ 0.25 \\ 0.63 \\ 0.39 \\ \end{array}$
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly	$\beta_{trend} \times 10$ -53568105559.	$\begin{array}{c cccc} & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \end{array}$	$\begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \end{array}$	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \end{array}$	σ 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 3.0	τ 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath	$\beta_{trend} \times 10$ -53568410556.	$\begin{array}{c cccc} & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \end{array}$	$\begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \end{array}$	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \end{array}$	σ 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 3.0 2.3	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri	$\begin{array}{c} \beta_{trend} \times 10 \\ -5. \\ -3. \\ -5. \\ -6. \\ -8. \\ -4. \\ -10. \\ -5. \\ -5. \\ -3. \\ -9. \\ -4. \\ -1. \end{array}$	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \end{array}$	$\begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ \end{array}$	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ \end{array}$	σ 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 3.0 2.3 4.0	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore	$\beta_{trend} \times 10$ -53568410539411.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ 5 & 1.5 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \end{array}$	$\begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ \end{array}$	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ \end{array}$	$\begin{array}{c} \sigma \\ 2.6 \\ 3.7 \\ 4.0 \\ 4.9 \\ 3.5 \\ 2.1 \\ 3.0 \\ 3.2 \\ 4.3 \\ 3.4 \\ 3.0 \\ 2.3 \\ 4.0 \\ 4.1 \end{array}$	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna	$\beta_{trend} \times 10$ -5356841053941137.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ 5 & 1.5 \\ 0 & -1.1 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \end{array}$	$\begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ \end{array}$	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.6 \\ \end{array}$	7 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 3.4 4.0 4.1 2.6	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda	$\beta_{trend} \times 10$ -53568410539411372.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ 5 & 1.5 \\ 0 & -1.1 \\ 3 & 2.8 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ \end{array}$	$\begin{array}{c} b_3 \\ 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ \end{array}$	$\begin{array}{c} b_4 \\ 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.6 \\ 4.1 \\ \end{array}$	7 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 4.0 4.1 2.6 5.2	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur	$\beta_{trend} \times 10$ -5356841053941137210.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ 5 & 1.5 \\ 0 & -1.1 \\ 3 & 2.8 \\ 0 & 2.0 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.6 \\ 4.1 \\ 3.4 \\ \end{array}$	7 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 4.0 4.1 2.6 5.2 2.9	0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad	$\beta_{trend} \times 10$ -5356841053941372104.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ 5 & 1.5 \\ 0 & -1.1 \\ 3 & 2.8 \\ 0 & 2.0 \\ 9 & 1.9 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ \end{array}$	$\begin{array}{c} b_5 \\ 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.6 \\ 4.1 \\ 3.4 \\ 3.5 \\ \end{array}$	7 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 4.0 4.1 2.6 5.2 2.9 4.4	0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh	$\beta_{trend} \times 10$ -5356841055394113721042.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ 5 & 1.5 \\ 0 & -1.1 \\ 3 & 2.8 \\ 0 & 2.0 \\ 9 & 1.9 \\ 6 & 1.7 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \\ 4.9 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \\ 0.9 \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ 3.0 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ 3.7 \\ \end{array}$	$\begin{array}{c} b_5 \\ \hline 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.1 \\ 3.4 \\ 3.5 \\ 3.9 \\ \end{array}$	7 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 4.0 2.6 5.2 2.9 4.4 3.0	0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41 0.28
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia	$\beta_{trend} \times 10$ -5356841053941137210427.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \\ 4.9 \\ 5.9 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \\ 0.9 \\ -2.5 \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ 3.0 \\ 2.0 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ 3.7 \\ 4.2 \\ \end{array}$	$\begin{array}{c} b_5 \\ \hline 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.1 \\ 3.4 \\ 3.5 \\ 3.9 \\ 3.7 \\ \end{array}$	7 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 4.1 2.6 5.2 2.9 4.4 3.0 4.1	0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41 0.28 0.47
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali	$\beta_{trend} \times 10$ -535684105539411372104276.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \\ 4.9 \\ 5.9 \\ 7.0 \\ \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \\ 0.9 \\ -2.5 \\ -6.7 \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ 3.0 \\ 2.0 \\ 3.3 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ 3.7 \\ 4.2 \\ 1.6 \\ \end{array}$	$\begin{array}{c} b_5 \\ \hline 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.1 \\ 3.4 \\ 3.5 \\ 3.9 \\ 3.7 \\ 5.0 \\ \end{array}$	7 2.6 3.7 4.0 4.9 3.5 2.1 3.0 3.2 4.3 3.4 4.0 4.1 2.6 5.2 2.9 4.4 3.0 4.1 3.9	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41 0.28 0.47 0.39
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna	$\beta_{trend} \times 10$ -5356841055394113721042761.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \\ 4.9 \\ 5.9 \\ 7.0 \\ 5.7 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \\ 0.9 \\ -2.5 \\ -6.7 \\ 0.6 \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ 3.0 \\ 2.0 \\ 3.3 \\ 4.1 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ 3.7 \\ 4.2 \\ 1.6 \\ 4.0 \\ \end{array}$	$\begin{array}{c} b_5 \\ \hline 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.1 \\ 3.4 \\ 3.5 \\ 3.9 \\ 3.7 \\ 5.0 \\ 3.8 \\ \end{array}$	σ       2.6       3.7       4.0       4.9       3.5       2.1       3.0       3.2       4.3       3.4       3.0       4.1       3.0       4.1       3.0       4.1       3.9       4.0	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41 0.28 0.47 0.39 0.51
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna Rangpur	$\beta_{trend} \times 10$ -53568410553941137210427616.	$\begin{array}{c cccc} \hline & b_0 \\ \hline 1 & 0.1 \\ 2 & 3.0 \\ 1 & 1.7 \\ 6 & 2.3 \\ 8 & 1.7 \\ 7 & 3.0 \\ 7 & -0.8 \\ 0 & 1.2 \\ 1 & 1.9 \\ 0 & 1.4 \\ 0 & 0.5 \\ 1 & 2.3 \\ 8 & 3.1 \\ 5 & 1.5 \\ 0 & -1.1 \\ 3 & 2.8 \\ 0 & 2.0 \\ 9 & 1.9 \\ 6 & 1.7 \\ 3 & 1.2 \\ 8 & -1.4 \\ 9 & 2.1 \\ 6 & 1.2 \\ \hline \end{array}$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \\ 4.9 \\ 5.9 \\ 7.0 \\ 5.7 \\ 5.3 \\ \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \\ 0.9 \\ -2.5 \\ -6.7 \\ 0.6 \\ 0.8 \\ \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ 3.0 \\ 2.0 \\ 3.3 \\ 4.1 \\ 3.4 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ 3.7 \\ 4.2 \\ 1.6 \\ 4.0 \\ 3.5 \\ \end{array}$	$\begin{array}{c} b_5 \\ \hline 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.1 \\ 3.4 \\ 3.5 \\ 3.9 \\ 3.7 \\ 5.0 \\ 3.8 \\ 3.6 \\ \end{array}$	$\begin{array}{c} \sigma \\ \hline \sigma \\ \hline 2.6 \\ 3.7 \\ 4.0 \\ 4.9 \\ 3.5 \\ 2.1 \\ 3.0 \\ 3.2 \\ 4.3 \\ 3.4 \\ 3.0 \\ 2.3 \\ 4.0 \\ 4.1 \\ 3.9 \\ 4.0 \\ 4.1 \\ 3.9 \\ 4.1 \\ 3.9 \\ 4.1 \\ \end{array}$	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41 0.28 0.47 0.39 0.51 0.62
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna Rangpur Rashahi	$\beta_{trend} \times 10$ -535684105539411372104276165.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \\ 4.9 \\ 5.9 \\ 7.0 \\ 5.7 \\ 5.3 \\ 5.3 \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \\ 0.9 \\ -2.5 \\ -6.7 \\ 0.6 \\ 0.8 \\ 0.7 \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ 3.0 \\ 2.0 \\ 3.3 \\ 4.1 \\ 3.4 \\ 3.2 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ 3.7 \\ 4.2 \\ 1.6 \\ 4.0 \\ 3.5 \\ 3.5 \\ \end{array}$	$\begin{array}{c} b_5 \\ \hline 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.5 \\ 3.9 \\ 3.7 \\ 5.0 \\ 3.8 \\ 3.6 \\ 4.1 \\ \end{array}$	$\begin{array}{c} \sigma \\ \hline \sigma \\ \hline 2.6 \\ 3.7 \\ 4.0 \\ 4.9 \\ 3.5 \\ 2.1 \\ 3.0 \\ 3.2 \\ 4.3 \\ 3.4 \\ 3.0 \\ 4.1 \\ 3.0 \\ 4.1 \\ 3.9 \\ 4.0 \\ 4.1 \\ 4.1 \\ 4.1 \\ \end{array}$	7 0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41 0.28 0.47 0.39 0.51 0.62 0.48
Bakergang Bankura Birbhum Bogra Burdwan Calcutta Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna Rangpur	$\beta_{trend} \times 10$ -53568410553941137210427616.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} b_1 \\ 7.1 \\ 3.1 \\ 3.8 \\ 4.7 \\ 4.7 \\ 3.8 \\ 4.8 \\ 6.2 \\ 4.2 \\ 6.5 \\ 5.8 \\ 3.4 \\ 4.3 \\ 5.6 \\ 6.7 \\ 4.8 \\ 2.8 \\ 4.6 \\ 4.9 \\ 5.9 \\ 7.0 \\ 5.7 \\ 5.3 \\ \end{array}$	$\begin{array}{c} b_2 \\ -8.6 \\ 0.7 \\ 0.6 \\ 1.9 \\ -6.0 \\ 2.1 \\ -0.5 \\ -3.4 \\ 2.3 \\ -3.6 \\ -6.6 \\ -0.7 \\ 3.2 \\ -1.2 \\ -6.5 \\ 3.0 \\ -2.9 \\ 0.2 \\ 0.9 \\ -2.5 \\ -6.7 \\ 0.6 \\ 0.8 \\ \end{array}$	$\begin{array}{c} b_3 \\ \hline 1.9 \\ 4.9 \\ 4.4 \\ 3.4 \\ 1.6 \\ 2.2 \\ 1.0 \\ 3.9 \\ 1.8 \\ 4.3 \\ 1.1 \\ 1.9 \\ 3.3 \\ 3.4 \\ 1.4 \\ 3.6 \\ 2.0 \\ 3.8 \\ 3.0 \\ 2.0 \\ 3.3 \\ 4.1 \\ 3.4 \\ \end{array}$	$\begin{array}{c} b_4 \\ \hline 2.1 \\ -2.6 \\ 0.4 \\ 3.9 \\ 1.6 \\ 3.3 \\ 0.7 \\ 3.2 \\ 3.6 \\ 3.0 \\ 2.2 \\ 2.5 \\ 3.6 \\ 3.4 \\ 2.8 \\ 4.3 \\ 1.4 \\ 3.0 \\ 3.7 \\ 4.2 \\ 1.6 \\ 4.0 \\ 3.5 \\ \end{array}$	$\begin{array}{c} b_5 \\ \hline 5.3 \\ 2.6 \\ 4.4 \\ 3.3 \\ 3.0 \\ 3.1 \\ 4.6 \\ 4.3 \\ 3.6 \\ 4.5 \\ 3.3 \\ 3.1 \\ 3.3 \\ 4.6 \\ 4.1 \\ 3.4 \\ 3.5 \\ 3.9 \\ 3.7 \\ 5.0 \\ 3.8 \\ 3.6 \\ \end{array}$	$\begin{array}{c} \sigma \\ \hline \sigma \\ \hline 2.6 \\ 3.7 \\ 4.0 \\ 4.9 \\ 3.5 \\ 2.1 \\ 3.0 \\ 3.2 \\ 4.3 \\ 3.4 \\ 3.0 \\ 2.3 \\ 4.0 \\ 4.1 \\ 3.9 \\ 4.0 \\ 4.1 \\ 3.9 \\ 4.1 \\ 3.9 \\ 4.1 \\ \end{array}$	0.33 0.48 0.53 0.66 0.38 0.23 0.42 0.25 0.63 0.39 0.35 0.20 0.69 0.39 0.36 0.62 0.28 0.41 0.28 0.47 0.39 0.51

 $$\operatorname{S}\text{-}12$$  www.nature.com/nature

Table S-4: Maximum likelihood estimates for the two-path model. The units of  $\gamma$ , m,  $\varepsilon$ ,  $\omega$ , and  $\beta_{trend}$  are yr<sup>-1</sup>; the other quantities are dimensionless

	$\log \mathcal{L}$	$AIC_c$	$r^2$	$R_0$	$\gamma$		$\overline{m}$	ρ	ε	$\log \omega$	c
Bakergang	-3656.3	7354.0	0.857	1.38	7.1	2.74		8.5	0.5	-4.5	
Bankura	-3036.8	6115.0	0.556	1.41	11.0	2.49	94	4.5	0.3	-4.6	0.0107
Birbhum	-3086.8	6215.0	0.492	1.61	1.3	6.41	17	5.3	0.5	-4.4	
Bogra	-2837.5	5716.4	0.522	2.30	21.6	0.24		2.6	0.4	-10.9	
Burdwan	-3415.6	6872.7	0.580	1.44	1.8	4.13	35	4.3	1.0	-3.5	0.0079
Calcutta	-3035.4	6112.3	0.762	1.27	11.3	4.66	32	5.6	0.7	-4.3	0.0104
Chittagong	-3248.5	6538.5	0.713	1.43	8.4	3.62	27	4.7	0.6	-5.5	0.0113
Dacca	-3784.7	7610.8	0.852	1.29	8.0	9.23	38	7.1	0.7	-4.5	0.0051
Dinajpur	-2945.8	5933.1	0.508	1.87	4.3	1.30	04	3.0	0.7	-4.6	0.0057
Faridpur	-3660.0	7361.5	0.783	1.34	10.7	8.66	31	7.1	0.7	-5.0	0.0056
Hooghly	-3251.9	6545.3	0.573	1.11	3.2	4.40		5.1	0.8	-2.3	
Howrath	-3365.5	6772.4	0.771	1.32	11.2	5.26	32	5.7	0.6	-4.4	0.0114
Jaipaguri	-2388.1	4817.6	0.585	1.47	23.9	0.15	55	17.0	3.3	-9.8	0.4598
Jessore	-3501.3	7044.1	0.750	1.63	9.6	4.19	97	9.2	1.7	-4.6	0.0053
Khulna	-3506.5	7054.5	0.720	1.44	4.2	3.94	41	7.2	0.7	-4.2	0.0053
Malda	-2900.3	5842.1	0.592	1.63	29.3	0.13	34	22.9	2.8	-10.6	0.4809
Midnapur	-3879.2	7799.8	0.674	1.31	10.9	3.73	37	5.9	0.5	-3.7	0.0099
Mohrshidabad	-3404.6	6850.6	0.623	1.82	6.0	3.64	49	3.3	0.4	-4.3	0.0079
Mymensingh	-3979.5	8000.5	0.804	1.44	13.6	3.83	31	2.5	0.4	-7.9	0.0279
Nadia	-3403.3	6848.0	0.733	1.66	6.7	5.16	64	9.2	0.9	-5.3	0.0054
Noakhali	-3471.7	6984.9	0.691	1.71	9.5	3.10	03	4.4	0.5	-5.3	0.0108
Pabna	-3283.8	6609.0	0.695	1.47	12.3	13.75	56	4.4	0.8	-7.5	0.0059
Rangpur	-3264.2	6569.8	0.631	1.55	17.3	0.13	34	14.0	1.4	-7.8	0.3894
Rashahi	-3306.8	6655.1	0.691	1.52	9.0	4.28	85	5.8	0.8	-5.1	0.0079
Tippera	-3646.6	7334.7	0.763	1.53	7.5	3.26	37	5.2	3.2	-5.2	0.0056
24 Parganas	-3780.6	7602.6	0.844	1.38	2.8	3.88	89	4.7	0.8	-3.7	0.0079
	$\beta_{tre}$	$_{end} \times 10^3$	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$			$\sigma$	$\overline{\tau}$
Bakergang	g	-4.8	4.0	13.2	-10.7	2.8	6.8				.31
Bankura		-4.5	7.9	7.7	6.9	8.4	6.1				.47
Birbhum		-5.2	6.1	9.1	4.5	9.6	4.5				.53
Bogra		-7.4	4.5	6.5	4.3	5.4	5.7				.65
Burdwan		-9.7	6.3	9.7	0.1	8.1	5.6				.39
Calcutta		-5.7	7.6	8.3	6.7	6.9	7.9				.23
Chittagon	ıg	-6.8	6.0	8.9	6.2	7.5	6.2				.44
Dacca		-6.8	6.5	11.4	2.1	9.0	8.6				.23
Dinajpur		-10.5	4.2	10.7	4.2	4.4	8.9				.63
Faridpur		-3.6	6.7	11.4	2.3	9.5	8.3				.38
Hooghly		-9.4	6.7	10.7	1.2	6.7	7.9				.35
Howrath		-2.5	7.6	8.0	6.7	7.4	7.6				.20
Jaipaguri		-1.5	4.0	5.1	4.3	4.0	4.5				.68
Jessore		-4.5	6.3	11.3	2.6	8.5	8.5				.38
Khulna		-8.0	4.5	11.6	-0.5	6.9	8.0				.36
Malda		-2.1	3.7	5.5	4.0	4.3	5.1				.63
Midnapur		-5.0	7.8	7.3	7.2	7.5	7.3				.29
Mohrshid		-5.9	6.3	9.9	3.8	8.8	7.7				.42
Mymensir	ngh	-5.8	5.4	8.5	4.6	6.6	7.4				.28
Nadia		-7.6	6.3	11.3	2.0	7.3	9.3				.46
Noakhali		-3.5	5.9	9.3	5.5	8.2	6.9			3.3 0	.38
Pabna		-2.2	7.6	10.6	6.4	9.2	9.2				.50
Rangpur		-5.1	2.9	5.9	2.6	4.4	4.7				.61
Rashahi		-8.6	5.3	10.8	3.7	8.1	8.0				.48
Tippera		-5.2	6.7	10.3	1.2	8.4	8.0	9.5		.3 0	.40
04 D			F 77	0.0	0.5	7.0	0.0	0.5	2000		1.0

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9.3

-0.5 7.0 6.2

 $9.5 \quad 329.5 \quad 0.16$ 

-5.7 5.7

24 Parganas

Table S-5: Maximum likelihood estimates for the seasonal-reservoir model. The units of  $\gamma$ , m,  $\varepsilon$ , and  $\beta_{trend}$  are yr<sup>-1</sup>; the other quantities are dimensionless.

	$\log \mathcal{L}$	$AIC_c$	$r^2$	$R_0$	$\gamma$	$\overline{m}$	ε	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$
Bakergang	-3661.8	7369.4	0.855	1.35	11.2	0.029	36.7	0.1	7.1	-8.7	1.9	2.2	5.2
Bankura	-3039.3	6124.5	0.570	1.40	7.4	0.019	3.9	3.0	3.0	0.6	4.9	-2.6	2.7
Birbhum	-3076.4	6198.6	0.499	1.50	9.0	0.068	13.2	1.6	3.7	0.6	4.3	0.5	4.4
Bogra	-2847.7	5741.1	0.540	1.90	14.1	0.042	2.1	2.2	4.7	1.6	3.5	3.9	3.3
Burdwan	-3381.8	6809.3	0.610	1.50	5.3	0.046	6.6	1.7	4.8	-6.0	1.5	1.8	3.3
Calcutta	-3037.7	6121.2	0.761	1.20	16.1	0.030	51.9	3.0	3.8	2.1	2.2	3.3	3.0
Chittagong	-3251.6	6549.0	0.713	1.52	5.3	0.046	3.7	-0.5	4.9	-0.5	0.8	1.0	4.5
Dacca	-3763.8	7573.4	0.858	1.22	18.0	0.064	10.6	1.2	6.2	-3.5	3.7	3.4	4.2
Dinajpur	-2946.8	5939.4	0.499	1.62	12.3	0.021	3.2	1.8	4.2	2.3	1.8	3.8	3.5
Faridpur	-3631.6	7309.0	0.800	1.26	20.6	0.071	6.6	1.4	6.5	-3.6	4.3	3.2	4.5
Hooghly	-3222.9	6491.6	0.604	1.05	7.6	0.022	10.0	0.4	5.8	-6.7	1.0	2.4	3.3
Howrath	-3361.8	6769.4	0.773	1.30	7.9	0.043	6.6	2.3	3.4	-0.7	2.0	2.5	3.1
Jaipaguri	-2382.3	4810.3	0.599	1.39	21.9	0.109	3.2	3.1	4.3	3.2	3.1	3.5	3.1
Jessore	-3486.5	7018.7	0.760	1.54	16.1	0.037	12.8	1.5	5.6	-1.3	3.3	3.5	4.5
Khulna	-3498.7	7043.1	0.726	1.38	8.1	0.024	33.0	-1.1	6.7	-6.8	1.4	2.9	4.5
Malda	-2906.0	5857.8	0.587	1.68	25.5	0.090	3.2	2.8	4.7	3.0	3.5	4.3	4.0
Midnapur	-3878.5	7802.7	0.675	1.31	5.4	0.014	22.1	2.0	2.7	-2.9	1.9	1.5	3.4
Mohrshidabad	-3396.4	6838.5	0.627	1.68	11.5	0.037	5.7	1.9	4.5	0.3	3.6	3.1	3.5
Mymensingh	-3991.8	8029.4	0.805	1.34	17.3	0.068	9.0	1.7	4.8	0.8	3.0	3.7	3.9
Nadia	-3395.9	6837.6	0.739	1.60	12.3	0.033	27.3	1.2	5.9	-2.6	2.0	4.2	3.6
Noakhali	-3472.1	6989.9	0.698	1.81	6.0	0.032	2.5	-1.4	6.9	-6.7	3.3	1.6	5.0
Pabna	-3287.9	6621.5	0.690	1.45	23.0	0.103	3.8	2.2	5.6	0.6	4.0	4.0	3.7
Rangpur	-3265.9	6577.6	0.633	1.63	14.6	0.065	1.5	1.4	5.2	1.1	3.4	3.7	3.5
Rashahi	-3288.4	6622.6	0.701	1.42	17.1	0.059	5.4	1.5	5.3	0.6	3.1	3.5	4.1
Tippera	-3648.1	7341.9	0.765	1.53	11.4	0.016	24.0	1.6	4.9	-2.6	3.3	2.8	4.4
24 Parganas	-3752.9	7551.5	0.853	1.29	6.8	0.037	15.5	0.8	4.5	-6.8	1.8	1.5	4.6

	$\beta_{trend} \times 10^3$	$\sigma$	au	$\omega_0$	$\omega_1$	$\omega_2$	$\omega_3$	$\omega_4$	$\omega_5$
Bakergang	-4.6	2.5	0.32	-4.5	-4.9	-4.8	-4.7	-5.5	-4.4
Bankura	-5.2	3.8	0.47	-3.7	-3.2	-3.9	-3.8	-3.3	-4.0
Birbhum	-6.1	4.1	0.53	-4.4	-4.3	-4.9	-5.7	-5.8	-4.7
Bogra	-7.1	4.9	0.68	-9.7	-9.8	-10.2	-12.9	-10.2	-10.8
Burdwan	-10.2	3.6	0.35	-3.9	-3.7	-3.5	-2.5	-4.9	-5.4
Calcutta	-4.9	2.2	0.22	-3.6	-3.3	-3.1	-3.8	-4.0	-3.1
Chittagong	-11.8	3.0	0.41	-5.2	-5.0	-5.3	-5.8	-6.6	-6.1
Dacca	-4.8	3.1	0.22	-3.4	-4.0	-4.1	-4.1	-6.6	-4.7
Dinajpur	-7.2	4.4	0.69	-5.2	-6.1	-5.3	-5.9	-6.4	-5.4
Faridpur	-2.7	3.4	0.35	-4.0	-4.5	-3.7	-4.4	-7.1	-4.0
Hooghly	-9.3	3.1	0.35	-1.9	-1.8	-1.8	-1.7	-3.8	-2.6
Howrath	-4.0	2.3	0.19	-3.6	-2.6	-2.6	-3.6	-3.9	-4.4
Jaipaguri	-2.5	4.2	0.74	-8.8	-9.3	-10.1	-10.7	-11.2	-7.8
Jessore	-4.4	4.2	0.38	-4.7	-4.9	-4.0	-4.5	-6.6	-5.2
Khulna	-7.9	2.6	0.35	-3.7	-4.0	-2.9	-3.6	-5.5	-4.1
Malda	-0.8	4.9	0.65	-11.0	-10.9	-11.0	-11.0	-11.0	-11.0
Midnapur	-11.3	2.9	0.27	-1.8	-3.2	-2.2	-2.3	-3.1	-2.3
Mohrshidabad	-5.7	4.4	0.40	-4.5	-5.0	-5.0	-4.0	-5.8	-5.0
Mymensingh	-2.3	3.0	0.27	-8.3	-8.3	-8.3	-8.4	-8.3	-8.3
Nadia	-8.6	4.2	0.47	-5.1	-5.0	-4.9	-4.7	-6.8	-5.8
Noakhali	-9.7	3.9	0.39	-4.3	-4.1	-4.7	-4.9	-5.9	-4.4
Pabna	-2.6	3.9	0.52	-8.9	-9.2	-9.5	-9.8	-9.4	-9.9
Rangpur	-7.7	4.6	0.69	-6.7	-7.5	-7.0	-8.0	-8.5	-7.9
Rashahi	-6.5	4.1	0.48	-5.3	-5.4	-5.0	-5.1	-7.0	-6.6
Tippera	-5.1	3.2	0.40	-5.2	-5.4	-5.0	-5.1	-5.8	-5.1
24 Parganas	-5.1	2.5	0.15	-2.9	-3.4	-3.2	-2.6	-5.0	-4.7

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Table S-6: Maximum likelihood estimates for the environmental-phage model. The units of  $\gamma$ , m,  $\varepsilon$ ,  $\omega$ ,  $\beta_{trend}$ , a, and  $\mu$  are yr<sup>-1</sup>; the other quantities are dimensionless.

	$\log \mathcal{L}$	$AIC_c$	$r^2$	$R_0$	$\log a$	- 11	$\gamma$	$\overline{m}$	$\varepsilon$
Bakergang	-3664.5	7370.4	0.855	1.41	-17.3	$\frac{\mu}{0.32}$	11.2	0.028	39.8
Bankura	-3040.2	6121.8	0.555	1.40	-17.0	0.32	7.3		4.0
Birbhum	-3082.8	6207.0	0.495	1.53	-15.5	0.35	9.1	0.013	13.9
Bogra	-3052.5 $-2857.9$	5757.3	0.435 $0.536$	2.05	-13.3 $-13.1$	3.66	14.1	0.042	1.9
Burdwan	-2637.9 $-3412.0$	6865.5	0.584	1.43	-15.1 $-15.5$	2.21	5.1	0.042 $0.045$	6.4
Calcutta	-3412.0 $-3042.3$	6126.2	0.760	1.43	-16.7	0.36	16.2	0.045	52.4
	-3042.3 $-3241.9$						4.9		4.1
Chittagong		6525.3	0.714	2.02 1.28	-9.5	8.81		0.046	$\frac{4.1}{10.5}$
Dacca	-3787.9	7617.2	0.851		-17.5	1.11	17.3		
Dinajpur	-2940.1	5921.7	0.494	2.00	-8.8	23.94	11.7		3.7
Faridpur	-3661.5	7364.4	0.786	1.31	-16.9	0.50	19.0	0.066	5.9
Hooghly	-3248.8	6539.1	0.575	1.11	-16.5	0.10	7.1	0.021	9.1
Howrath	-3372.6	6786.6	0.769	1.36	-18.5	0.18	7.7	0.039	6.6
Jaipaguri	-2387.9	4817.3	0.588	1.66	-12.3	0.14	21.9	0.112	3.8
Jessore	-3501.1	7043.6	0.748	1.57	-17.1	1.30	15.6	0.035	12.7
Khulna	-3503.7	7048.9	0.723	1.39	-17.5	4.07	8.0	0.023	33.5
Malda	-2892.9	5827.3	0.578	1.86	-8.5	8.32	25.5		3.7
Midnapur	-3883.0	7807.5	0.671	1.34	-16.9	0.75	5.4		21.5
Mohrshidabad	-3400.7	6842.9	0.626	1.71	-16.4	0.68	11.3	0.037	5.4
Mymensingh	-3975.1	7991.7	0.812	1.64	-10.4	7.17	16.6	0.102	13.2
Nadia	-3403.1	6847.7	0.734	1.70	-14.6	1.79	12.2		27.0
Noakhali	-3477.2	6995.9	0.694	1.84	-17.2	0.47	5.9	0.031	2.6
Pabna	-3289.0	6619.5	0.690	1.48	-18.1	0.06	23.0	0.096	3.8
Rangpur	-3267.5	6576.5	0.629	1.79	-13.5	0.35	14.2		1.5
Rashahi	-3302.6	6646.7	0.694	1.47	-16.1	0.45	16.6	0.059	5.3
Tippera	-3629.6	7300.7	0.771	2.02	-11.1	6.95	11.0		26.8
24 Parganas	-3778.2	7597.9	0.844	1.38	-17.4	0.47	6.3	0.032	18.6
	$\log \omega  \beta_t$	$_{trend} \times 10^3$	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$	$b_5$ $c$	au
Bakergang	-4.9	-3.5	0.1	7.2	-9.0	2.2	2.1	5.3 2.6	0.32
Bankura	-3.5	-5.9	3.0	3.1	0.6	4.9 -	-2.6	2.6 3.9	0.48
Birbhum	-5.0	-4.8	1.8	3.7	0.7	4.3	0.4	4.4 4.1	0.53
Bogra	-11.0	-8.0		4.9	1.7	3.5	4.0	3.4 5.4	
Burdwan				4.0	6.0	1.3	1.5	21 2	0.90
	-3.9	-9.5	1.6	4.8	-0.0			O.1 O.4	E 0.38
Calcutta	$-3.9 \\ -3.4$	$-9.5 \\ -7.0$		4.8 3.8	$-6.0 \\ 2.2$	2.2	3.3	3.1 3.4 3.1 2.3	
	-3.4	-7.0	3.1	3.8	2.2		3.3	3.1 2.3	0.22
Calcutta Chittagong Dacca	$-3.4 \\ -5.7$	$-7.0 \\ -9.2$	3.1 -0.6		$2.2 \\ -0.6$	1.4	3.3 0.9	3.1 2.3 4.8 4.1	0.22 0.40
Chittagong Dacca	-3.4 $-5.7$ $-4.6$	-7.0 $-9.2$ $-7.3$	3.1 $-0.6$ $1.3$	3.8 5.4 6.1	$   \begin{array}{r}     2.2 \\     -0.6 \\     -3.3   \end{array} $	$\frac{1.4}{3.7}$	3.3 0.9 3.3	3.1 2.3 4.8 4.1 4.3 3.3	0.22 0.40 0.23
Chittagong Dacca Dinajpur	-3.4 $-5.7$ $-4.6$ $-5.7$	-7.0 $-9.2$ $-7.3$ $-6.9$	3.1 $-0.6$ $1.3$ $2.0$	3.8 5.4 6.1 4.4	2.2 $-0.6$ $-3.3$ $2.5$	1.4 3.7 1.7	3.3 0.9 3.3 3.8	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4	3 0.22 0.40 3 0.23 4 0.68
Chittagong Dacca Dinajpur Faridpur	-3.4 $-5.7$ $-4.6$ $-5.7$ $-4.9$	$     \begin{array}{r}       -7.0 \\       -9.2 \\       -7.3 \\       -6.9 \\       -3.4   \end{array} $	3.1 $-0.6$ $1.3$ $2.0$ $1.4$	3.8 5.4 6.1 4.4 6.4	2.2 $-0.6$ $-3.3$ $2.5$ $-3.6$	1.4 3.7 1.7 4.3	3.3 0.9 3.3 3.8 3.0	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4	3 0.22 0.40 3 0.23 4 0.68 4 0.38
Chittagong Dacca Dinajpur Faridpur Hooghly	-3.4 $-5.7$ $-4.6$ $-5.7$ $-4.9$ $-2.2$	-7.0 $-9.2$ $-7.3$ $-6.9$ $-3.4$ $-7.7$	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$	3.8 5.4 6.1 4.4 6.4 5.9	2.2 $-0.6$ $-3.3$ $2.5$ $-3.6$ $-6.8$	1.4 3.7 1.7 4.3 0.8	3.3 0.9 3.3 3.8 3.0 2.2	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath	-3.4 $-5.7$ $-4.6$ $-5.7$ $-4.9$ $-2.2$ $-3.6$	$     \begin{array}{r}       -7.0 \\       -9.2 \\       -7.3 \\       -6.9 \\       -3.4 \\       -7.7 \\       -4.0 \\    \end{array} $	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$	3.8 5.4 6.1 4.4 6.4 5.9 3.4	2.2 $-0.6$ $-3.3$ $2.5$ $-3.6$ $-6.8$ $-0.4$	1.4 3.7 1.7 4.3 0.8 1.9	3.3 0.9 3.3 3.8 3.0 2.2 2.4	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri	$ \begin{array}{r} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \end{array} $	$ \begin{array}{r} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \end{array} $	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$	3.8 5.4 6.1 4.4 6.4 5.9 3.4 4.5	$\begin{array}{c} 2.2 \\ -0.6 \\ -3.3 \\ 2.5 \\ -3.6 \\ -6.8 \\ -0.4 \\ 3.4 \end{array}$	1.4 3.7 1.7 4.3 0.8 1.9 3.3	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore	$ \begin{array}{r} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \end{array} $	$ \begin{array}{r} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \end{array} $	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$ $1.5$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6	$\begin{array}{c} 2.2 \\ -0.6 \\ -3.3 \\ 2.5 \\ -3.6 \\ -6.8 \\ -0.4 \\ 3.4 \\ -1.2 \end{array}$	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0 4.5 4.1	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 0.39
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna	$ \begin{array}{r} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \end{array} $	$ \begin{array}{r} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \end{array} $	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$ $1.5$ $-1.1$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8	$\begin{array}{c} 2.2 \\ -0.6 \\ -3.3 \\ 2.5 \\ -3.6 \\ -6.8 \\ -0.4 \\ 3.4 \\ -1.2 \\ -6.9 \end{array}$	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0 4.5 4.1 4.5 2.5	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 0 0.39 5 0.35
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda	$ \begin{array}{r} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \end{array} $	$ \begin{array}{r} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \end{array} $	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$ $1.5$ $-1.1$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8	$\begin{array}{c} 2.2 \\ -0.6 \\ -3.3 \\ 2.5 \\ -3.6 \\ -6.8 \\ -0.4 \\ 3.4 \\ -1.2 \\ -6.9 \\ 3.1 \end{array}$	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0 4.5 4.1 4.5 2.5 4.3 5.6	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 1 0.39 5 0.35 6 0.65
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur	$ \begin{array}{r} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \end{array} $	$ \begin{array}{r} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \\ -11.1 \end{array} $	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$ $1.5$ $-1.1$ $2.8$ $2.2$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6	2.2 -0.6 -3.3 2.5 -3.6 -6.8 -0.4 3.4 -1.2 -6.9 3.1 -2.8	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 4.5 4.1 4.5 2.3 4.3 5.6 3.4 3.1	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 5 0.35 6 0.35 6 0.65 0.28
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \end{array}$	$\begin{array}{c} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \\ -11.1 \\ -5.4 \end{array}$	3.1 -0.6 1.3 2.0 1.4 0.6 2.3 3.3 1.5 -1.1 2.8 2.2	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5	2.2 -0.6 -3.3 2.5 -3.6 -6.8 -0.4 3.4 -1.2 -6.9 3.1 -2.8 0.3	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.1 3.5 4.5	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 5 0.35 6 0.35 6 0.65 0.28 6 0.40
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \end{array}$	$\begin{array}{c} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \\ -11.1 \\ -5.4 \\ -4.4 \end{array}$	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$ $1.5$ $-1.1$ $2.8$ $2.2$ $2.0$ $2.0$	3.8 5.4 6.1 4.4 6.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0	2.2 -0.6 -3.3 2.5 -3.6 -6.8 -0.4 3.4 -1.2 -6.9 3.1 -2.8 0.3 1.1	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 3.1	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.1 3.5 4.5 4.1 3.7	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 5 0.35 6 0.65 0 0.28 6 0.40 7 0.25
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \\ -5.5 \end{array}$	$\begin{array}{c} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \\ -11.1 \\ -5.4 \\ -4.4 \\ -8.4 \end{array}$	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$ $1.5$ $-1.1$ $2.8$ $2.2$ $2.0$ $1.2$	3.8 5.4 6.1 4.4 6.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0 6.0	$\begin{array}{c} 2.2 \\ -0.6 \\ -3.3 \\ 2.5 \\ -3.6 \\ -6.8 \\ -0.4 \\ 3.4 \\ -1.2 \\ -6.9 \\ 3.1 \\ -2.8 \\ 0.3 \\ 1.1 \\ -2.6 \end{array}$	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 2.3	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8 4.1	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.1 3.5 4.5 4.1 3.7	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 5 0.39 5 0.65 6 0.28 6 0.40 7 0.25 4 0.47
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \\ -5.5 \\ -5.0 \end{array}$	-7.0 -9.2 -7.3 -6.9 -3.4 -7.7 -4.0 -2.3 -4.3 -8.5 -1.7 -11.1 -5.4 -4.4 -8.4	$\begin{array}{c} 3.1 \\ -0.6 \\ 1.3 \\ 2.0 \\ 1.4 \\ 0.6 \\ 2.3 \\ 3.3 \\ 1.5 \\ -1.1 \\ 2.8 \\ 2.2 \\ 2.0 \\ 2.0 \\ 1.2 \\ -1.3 \end{array}$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0 6.0 7.0	$\begin{array}{c} 2.2 \\ -0.6 \\ -3.3 \\ 2.5 \\ -3.6 \\ -6.8 \\ -0.4 \\ 3.4 \\ -1.2 \\ -6.9 \\ 3.1 \\ -2.8 \\ 0.3 \\ 1.1 \\ -2.6 \\ -6.8 \end{array}$	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 3.1 2.3 3.3	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8 4.1	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.1 3.5 4.5 4.1 3.7 4.1 3.7 5.1 3.9	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 5 0.39 5 0.65 6 0.28 6 0.40 7 0.25 4 0.47 9 0.39
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \\ -5.5 \\ -5.0 \\ -9.5 \end{array}$	-7.0 -9.2 -7.3 -6.9 -3.4 -7.7 -4.0 -2.3 -4.3 -8.5 -1.7 -11.1 -5.4 -4.4 -8.4 -8.3 -2.9	3.1 -0.6 1.3 2.0 1.4 0.6 2.3 3.3 1.5 -1.1 2.8 2.2 2.0 2.0 1.2 -1.3 2.1	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0 6.0 7.0 5.7	2.2 -0.6 -3.3 2.5 -3.6 -6.8 -0.4 3.4 -1.2 -6.9 3.1 -2.8 0.3 1.1 -2.6 -6.8 0.5	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 3.1 2.3 3.3 4.1	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8 4.1 1.6 4.0	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.1 3.5 4.5 4.1 3.7 3.7 4.4 5.1 3.8	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 0 0.39 5 0.35 6 0.65 0 0.40 7 0.25 4 0.47 9 0.39 0 0.52
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna Rangpur	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \\ -5.5 \\ -5.0 \\ -9.5 \\ -7.4 \end{array}$	-7.0 -9.2 -7.3 -6.9 -3.4 -7.7 -4.0 -2.3 -4.3 -8.5 -1.7 -11.1 -5.4 -4.4 -8.4 -8.3 -2.9 -7.5	$\begin{array}{c} 3.1 \\ -0.6 \\ 1.3 \\ 2.0 \\ 1.4 \\ 0.6 \\ 2.3 \\ 3.3 \\ 1.5 \\ -1.1 \\ 2.8 \\ 2.2 \\ 2.0 \\ 2.0 \\ 1.2 \\ -1.3 \\ 2.1 \\ 1.5 \end{array}$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0 6.0 7.0 5.7 5.3	2.2 -0.6 -3.3 2.5 -3.6 -6.8 -0.4 3.4 -1.2 -6.9 3.1 -2.8 0.3 1.1 -2.6 -6.8 0.5 1.1	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 3.1 2.3 3.3 4.1 3.4	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8 4.1 1.6 4.0 3.8	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.7 3.7 4.4 5.1 3.9 3.8 4.0 3.6 4.9	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 0 0.39 5 0.35 6 0.65 0 0.28 6 0.40 7 0.25 4 0.39 0 0.35 0 0.28 0 0.39 0 0.25 0 0.40 0 0.39 0 0.39 0 0.25 0 0.40 0 0.39 0 0.35 0 0.40 0 0.39 0 0.35 0 0.40 0 0.39 0 0.39 0 0.35 0 0.40 0 0.39 0 0.39 0 0.39 0 0.39 0 0.39 0 0.35 0 0.40 0 0.39 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna Rangpur Rashahi	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \\ -5.5 \\ -5.0 \\ -9.5 \\ -7.4 \\ -5.8 \end{array}$	$\begin{array}{c} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \\ -11.1 \\ -5.4 \\ -4.4 \\ -8.4 \\ -8.3 \\ -2.9 \\ -7.5 \\ -6.2 \end{array}$	$\begin{array}{c} 3.1 \\ -0.6 \\ 1.3 \\ 2.0 \\ 1.4 \\ 0.6 \\ 2.3 \\ 3.3 \\ 1.5 \\ -1.1 \\ 2.8 \\ 2.2 \\ 2.0 \\ 2.0 \\ 1.2 \\ -1.3 \\ 2.1 \\ 1.5 \\ 1.6 \end{array}$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0 6.0 7.0 5.7 5.3 5.2	2.2 -0.6 -3.3 2.5 -3.6 -6.8 -0.4 3.4 -1.2 -6.9 3.1 -2.8 0.3 1.1 -2.6 -6.8 0.5 1.1 0.6	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 3.1 2.3 3.3 4.1 3.4 3.2	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8 4.1 1.6 4.0 3.8 3.5	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.1 3.7 4.4 5.1 3.9 3.8 4.0 3.6 4.9 4.1 4.1	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 0 0.39 6 0.35 6 0.65 0 0.28 6 0.40 7 0.25 4 0.47 0 0.39 0 0.47 0 0.39 0 0.47 0 0.47 0 0.49 0 0.48
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna Rangpur Rashahi Tippera	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \\ -5.5 \\ -5.0 \\ -9.5 \\ -7.4 \\ -5.8 \\ -5.3 \end{array}$	$\begin{array}{c} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \\ -11.1 \\ -5.4 \\ -4.4 \\ -8.3 \\ -2.9 \\ -7.5 \\ -6.2 \\ -1.5 \end{array}$	$\begin{array}{c} 3.1 \\ -0.6 \\ 1.3 \\ 2.0 \\ 1.4 \\ 0.6 \\ 2.3 \\ 3.3 \\ 1.5 \\ -1.1 \\ 2.8 \\ 2.2 \\ 2.0 \\ 2.0 \\ 1.2 \\ -1.3 \\ 2.1 \\ 1.5 \\ 1.6 \\ 2.0 \end{array}$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0 6.0 7.0 5.7 5.3 5.2 5.3	$\begin{array}{c} 2.2 \\ -0.6 \\ -3.3 \\ 2.5 \\ -3.6 \\ -6.8 \\ -0.4 \\ 3.4 \\ -1.2 \\ -6.9 \\ 3.1 \\ -2.8 \\ 0.3 \\ 1.1 \\ -2.6 \\ -6.8 \\ 0.5 \\ 1.1 \\ 0.6 \\ -2.4 \end{array}$	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 3.1 2.3 3.3 4.1 3.4 3.2 3.5	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8 4.1 1.6 4.0 3.8 3.5 3.0	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.7 3.7 4.4 5.1 3.8 3.6 4.9 4.1 4.1 4.5 4.5	3 0.22 0.40 3 0.23 4 0.68 4 0.38 2 0.35 4 0.20 0 0.74 0 0.39 6 0.35 6 0.65 0 0.28 6 0.40 7 0.25 1 0.47 0 0.39 0 0.35 1 0.47 0 0.39 0 0.48 0 0.37
Chittagong Dacca Dinajpur Faridpur Hooghly Howrath Jaipaguri Jessore Khulna Malda Midnapur Mohrshidabad Mymensingh Nadia Noakhali Pabna Rangpur Rashahi	$\begin{array}{c} -3.4 \\ -5.7 \\ -4.6 \\ -5.7 \\ -4.9 \\ -2.2 \\ -3.6 \\ -9.8 \\ -5.2 \\ -4.2 \\ -10.9 \\ -2.2 \\ -4.8 \\ -8.3 \\ -5.5 \\ -5.0 \\ -9.5 \\ -7.4 \\ -5.8 \end{array}$	$\begin{array}{c} -7.0 \\ -9.2 \\ -7.3 \\ -6.9 \\ -3.4 \\ -7.7 \\ -4.0 \\ -2.3 \\ -4.3 \\ -8.5 \\ -1.7 \\ -11.1 \\ -5.4 \\ -4.4 \\ -8.4 \\ -8.3 \\ -2.9 \\ -7.5 \\ -6.2 \end{array}$	3.1 $-0.6$ $1.3$ $2.0$ $1.4$ $0.6$ $2.3$ $3.3$ $1.5$ $-1.1$ $2.8$ $2.2$ $2.0$ $1.2$ $-1.3$ $2.1$ $1.5$ $1.6$ $2.0$	3.8 5.4 6.1 4.4 5.9 3.4 4.5 5.6 6.8 4.8 2.6 4.5 5.0 6.0 7.0 5.7 5.3 5.2	2.2 -0.6 -3.3 2.5 -3.6 -6.8 -0.4 3.4 -1.2 -6.9 3.1 -2.8 0.3 1.1 -2.6 -6.8 0.5 1.1 0.6	1.4 3.7 1.7 4.3 0.8 1.9 3.3 3.3 1.4 3.7 1.9 3.7 3.1 2.3 3.3 4.1 3.4 3.2	3.3 0.9 3.3 3.8 3.0 2.2 2.4 3.6 3.4 2.8 4.3 1.4 3.1 3.8 4.1 1.6 4.0 3.8 3.5	3.1 2.3 4.8 4.1 4.3 3.3 3.8 5.4 4.4 3.4 3.3 3.2 3.1 2.4 3.4 5.0 4.5 4.1 4.5 2.5 4.3 5.6 3.4 3.1 3.7 4.4 5.1 3.9 3.8 4.0 3.6 4.9 4.1 4.1	3 0.22 0.40 0.23 0.68 0.38 0.35 0.20 0.74 0.39 0.35 0.65 0.28 0.40 0.25 1.047 0.39 0.25 1.047 0.39 0.48 0.38

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