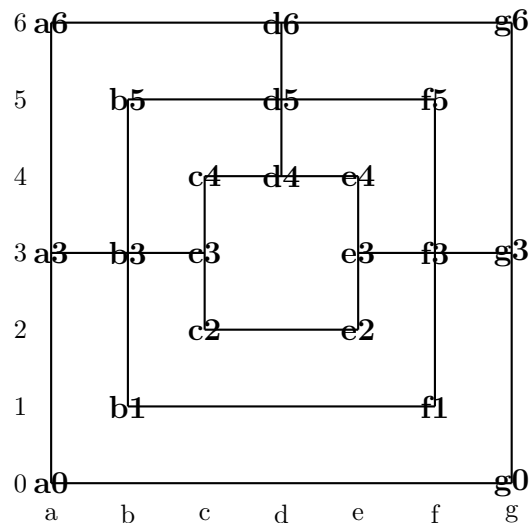
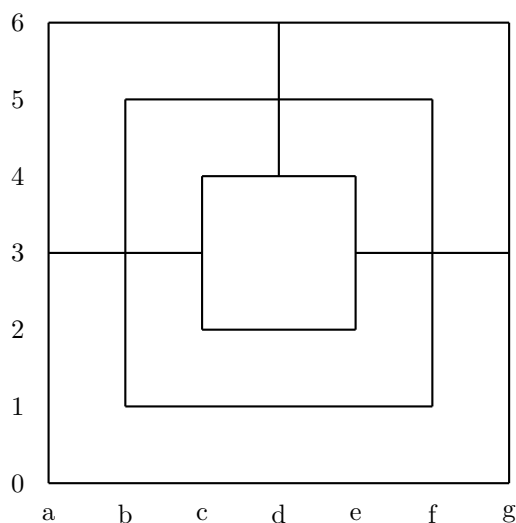


Morris Game Variant

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
a0	g0	b1	f1	c2	e2	a3	b3	c3	e3	f3	g3	c4	d4	e4	b5	d5	f5	a6	d6	g6



Nine Men's Morris

Nine Men's Morris is a board game between two players: White and Black. There are many online implementations available online. See, e.g., [first link](#), or [second link](#).

The **Morris Game Variant** is a variant of Nine Men's Morris game. Each player has 8 pieces, and the game board is as shown above. Pieces can be placed on intersections of lines. (There are a total of 21 locations for pieces.) The goal is to remove opponent's pieces by getting three pieces on a single line (a mill). The winner is the first player to reduce the opponent to only 2 pieces, or block the opponent from any further moves. The game has three distinct phases: opening, midgame, and endgame.

Opening: Players take turns placing 8 pieces - one at a time - on any vacant board intersection spot.

Midgame: Players take turns moving one piece along a board line to any adjacent vacant spot.

Endgame: A player down to only three pieces may move a piece to any open spot, not just an adjacent one (hopping).

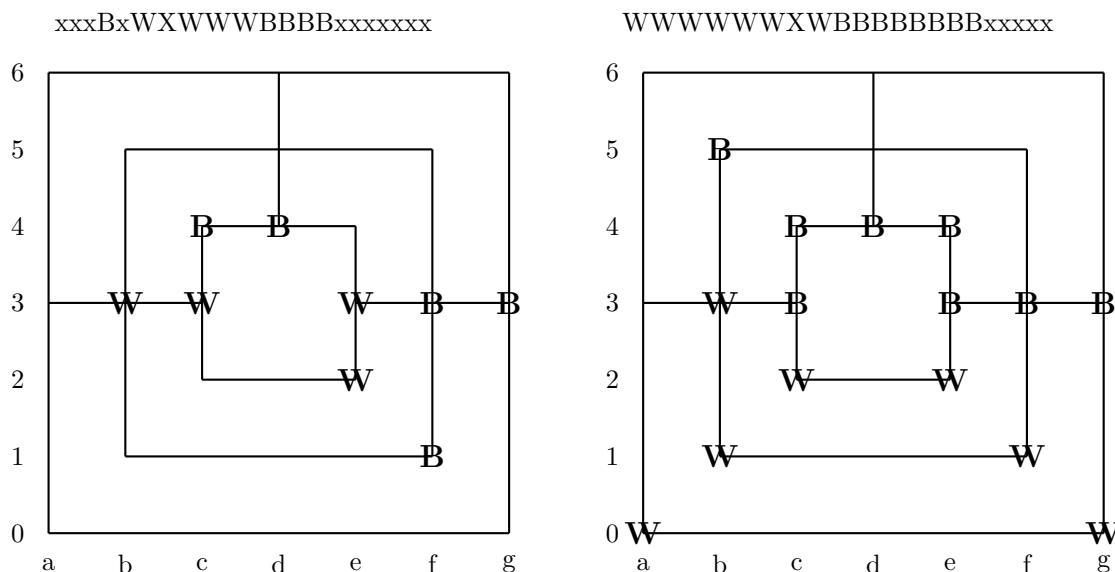
Mills: At any stage if a player gets three of their pieces on the same straight board line (a mill), then one of the opponent's isolated pieces is removed from the board. An isolated piece is a piece that is not part of a mill. (If there is no isolated piece then no piece is being removed.)

A computer program that plays Variant

The basic components of a computer program that plays Variant are a procedure that generates moves, a function for assigning static estimation value for a given position, and a MiniMax or AlphaBeta procedure.

Representing board positions

One way of representing a board position is by an array of length 21, containing the pieces as the letters W, B, x . (The letter x stands for a “non-piece”.) The array specifies the pieces starting from bottom-left and continuing left-right bottom up. Here are two examples:



Move generator

A move generator gets as input a board position and returns as output a list of board positions that can be reached from the input position. In the next section we describe a pseudo-code that can be used as a move generator for White. A move generator for Black can be obtained by the following procedure:

Input: a board position b .

Output: a list L of all positions reachable by a black move.

1. compute the board **tempb** by swapping the colors in b . Replace each W by a B , and each B by a W .
2. Generate L containing all positions reachable from **tempb** by a white move.
3. Swap colors in all board positions in L , replacing W with B and B with W .

A move generator for White

A pseudo-code is given for the following move generators: **GenerateAdd**, generates moves created by adding a white piece (to be used in the opening). **GenerateMove**, generates moves created by moving a white piece to an adjacent location (to be used in the midgame). **GenerateHopping**, generates moves created by white pieces hopping (to be used in the endgame). These routines get as an input a board and generate as output a list L containing the generated positions. They require a method of generating moves created by removing a black piece from the board. We name it **GenerateRemove**.

GenerateMovesOpening

Input: a board position

Output: a list L of board positions

Return the list produced by **GenerateAdd** applied to the board.

GenerateMovesMidgameEndgame

Input: a board position

Output: a list L of board positions

if the board has 3 white pieces Return the list produced by **GenerateHopping** applied to the board. Otherwise return the list produced by **GenerateMove** applied to the board.

GenerateAdd

Input: a board position

Output: a list L of board positions

L = empty list

for each location in board:

```
    if board[location] == empty {  
        b = copy of board; b[location] = W  
        if closeMill(location, b) generateRemove(b, L)  
        else add b to L  
    }
```

return L

GenerateHopping

Input: a board position

Output: a list L of board positions

L = empty list

for each location α in board

```
if board[ $\alpha$ ] == W {  
    for each location  $\beta$  in board  
    if board[ $\beta$ ] == empty {  
        b = copy of board; b[ $\alpha$ ] = empty; b[ $\beta$ ] = W  
        if closeMill( $\beta$ , b) generateRemove(b, L)  
        else add b to L  
    }
```

```
}  
return L
```

GenerateMove

Input: a board position

Output: a list L of board positions

```
L = empty list
for each location in board
  if board[location]==W {
    n = list of neighbors of location
    for each j in n
      if board[j] == empty {
        b = copy of board; b[location] = empty; b[j]=W
        if closeMill(j, b) GenerateRemove(b, L)
        else add b to L
      }
    }
  }
return L
```

GenerateRemove

Input: a board position and a list L

Output: positions are added to L by removing black pieces

```
for each location in board:
  if board[location]==B {
    if not closeMill(location, board) {
      b = copy of board; b[location] = empty
      add b to L
    } }
If no positions were added (all black pieces are in mills) add b to L.
```

neighbors and closeMill

The proposed coding of the methods neighbors and closeMill is by “brute force”. The idea is as follows.

neighbors

Input: a location j in the array representing the board

Output: a list of locations in the array corresponding to j’s neighbors

```
switch(j) {
  case j==0 (a0) : return [1,6]. (These are g0,a3.)
  case j==1 (g0) : return [0,11]. (These are a0,g3.)
  etc.
}
```

closeMill

Input: a location j in the array representing the board and the board b

Output: true if the move to j closes a mill

$C = b[j]$; C must be either W or B. Cannot be x.

```
switch(j) {  
    case j==0 (a0) : return true if  
        (b[6]==C and b[18]==C)  
        else return false  
    case j==6 (a3) : return true if  
        (b[0]==C and b[18]==C)  
        or (b[7]==C and b[8]==C)  
        else return false  
    etc.  
}
```

Static estimation

The following static estimation functions are proposed. Given a board position b compute:

numWhitePieces = the number of white pieces in b .

numBlackPieces = the number of black pieces in b .

L = the MidgameEndgame positions generated from b by a black move.

numBlackMoves = the number of board positions in L .

A static estimation for MidgameEndgame:

```
if (numBlackPieces  $\leq$  2) return(10000)  
else if (numWhitePieces  $\leq$  2) return(-10000)  
else if (numBlackMoves==0) return(10000)  
else return ( 1000(numWhitePieces - numBlackPieces) - numBlackMoves)
```

A static estimation for Opening:

```
return (numWhitePieces - numBlackPieces)
```