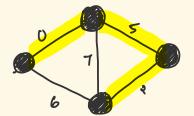
Minimum spanning trees

Sunday, October 29, 2023 6:40 A

- subset of edges which connects all vertices together (without cycles) while minimizing the total costs.



Prim's MST Algorithm

- Greedy algo that works well on dense graphs.
- Performs better than other algos on dense graphs.
- However, in case of a disconnected graph the edgo has to be own on every single component.

Must be sum on each component

-2 implementations O(Exlog(E)t +O(Exlog(V)) faster

```
14 struct compare{
       bool operator()(pair<int, int> a, pair<int, int> b)
   { return a.second > b.second; }
16 };
17
18 int Prims(int src){
19
       priority_queue<pair<int, int>, vector<pair<int,</pre>
   int>>, compare> pq;
20
       pq.push({src, 0});
21
       fill(visited, visited+n, false);
22
       int mst_cost = 0;
24
       while(!pq.empty()){
           auto p = pq.top();
27
           pq.pop();
           int node = p.first;
29
           int cost = p.second;
30
31
           if(visited[node]) continue;
           mst_cost += cost;
33
           visited[node] = true;
34
           // Iterate through all the adjacent nodes of
   the node
           // push the adjacent nodes in the pq only if
   they are not visited yet
           for(auto next : adj_list[node]){
37
38
               int adj_node = next.first;
39
               if(!visited[adj_node]) pq.push(next);
40
41
       return mst_cost;
```

The reason we check visited twice is that we are adding every single edge to the pq.

--- A node might hu alredy been visited with a emaller cost.

- We avoid including the other edge with larger cost.

```
PQ (7,1) not visited (7,2) not visited (7,2) (5,2) not visited (5,1) visited (5,1) visited (7,0) visited (7,0) visited (7,0) visited
```

- We store all the edges to unvisited nodes in the priority queue.
- Poionity queue will always return the min edge.

Kruskal's MST algorithm

- Sort all edges.
- Take edge with min cost.
- Repeat while discording cycle.

```
13 int collapsive_find(int a){
        // finds parent of subset this node belongs to
        while(parent[a] != a){
            parent[a] = parent[parent[a]]; // collapsive find operation
16
            a = parent[a];
       return a;
27 void weighted_union(int a, int b){
       int d = collapsive_find(a);
int e = collapsive_find(b);
       parent[d] = parent[e]; // merge two subsets
33 int KruskalsMST(){
       int cost, minCst = 0;
for(int i = 0; i < v; i++){</pre>
            a = edges[i].second.first;
b = edges[i].second.second;
            cost = edges[i].first;
                 minCst += cost;
                 weighted_union(a, b);
        return minCst;
```