

statistics

FOR

DATA SCIENCE

UNIT-1

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# Sampling Methods

## RANDOM SAMPLING

### 1) Simple random sampling

- assign numbers to members of population and select randomly
- good for small population

#### ADVANTAGES

easier, low error, no prior information required

#### DISADVANTAGES

can be biased, not proportionate, hard to scale

### 2) Stratified random sampling

- population proportion reflected in sample
- divide population into strata/ groups (gender, hair colour, age etc)

#### ADVANTAGES

enhanced representation, more scalable and efficient

#### DISADVANTAGES

classification error, time consuming, expensive

example: a student council surveys 50 students by getting random samples of 25 juniors and 25 seniors

### 3) Systematic Sampling

- Find the  $k^{\text{th}}$  value

### **ADVANTAGES**

easy to select, evenly spread sample, cost effective

### **DISADVANTAGES**

biased, no equal chance, ignored elements

**example:** a principal takes an alphabetised list of students and picks every fourth student from a random starting point

## **4) Cluster Sampling**

- Population divided into non-overlapping areas (clusters)
- Each cluster microcosm of population

### **ADVANTAGES**

convenient for geographically dispersed populations, simplified administration

### **DISADVANTAGES**

less efficient statistically, higher sampling error, more problems

**example:** airline company randomly selects 5 flights and surveys everyone on them

## NON-RANDOM SAMPLING

### 1) Convenience / Accidental

- subjects for sampling easily available
- when population not clearly defined

#### ADVANTAGES

easy to select, saves time and money

#### DISADVANTAGES

biased, sampling errors, cannot generalise

### 2) Judgmental Sampling

- researcher chooses / is related to sample based on their judgement

#### ADVANTAGES

minimum time

#### DISADVANTAGES

selection bias, sample size

### 3) Quota Sampling

- non-probability equivalent of stratified
- till quota is met

#### ADVANTAGES

minimum time

#### DISADVANTAGES

bias

#### 4) Snowball Sampling

- for rare characteristic / difficulty
- from initial subject, referrals

#### ADVANTAGES

lowers cost

#### DISADVANTAGES

bias

#### selection BIAS

- leave out hard to reach people
- Replace with accessible people
- Outdated sample frame

#### nonresponse BIAS

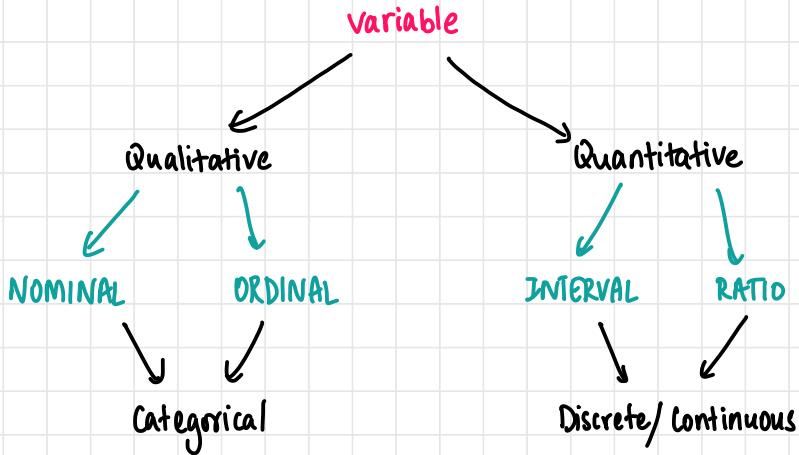
- people who do not respond to survey

#### ERRORS

Sampling errors  
(random)  
sample not representative

Non-sampling errors  
(systematic)  
during collection  
↳ missing data  
↳ technique

## TYPES OF DATA



### NOIR

- in increasing order of accuracy, powerfulness of measurement, precision and application

#### 1. Nominal

- name and countable (frequency)
- data is alphabetical or numeric only
- only counting & grouping
- no other arithmetic operations
- bar graphs are appropriate
- keeping track of objects / people / names etc

#### 2. Ordinal

- comparison between types allowed
- order matters, difference between values not
- eg: level of spiciness, satisfaction, pain scales etc

### 3. Interval

- differences also meaningful
- no absolute zero
- eg: standardised scores, temperature

### 4. Ratio

- all mathematical operations, clear absolute 0
- eg: height, weight, real scores

Note: salary / money is typically discrete

## TYPES OF STUDIES

Observational  
(surveys)

- do not control / interfere with sample/pop
- no treatment is given

Experiments  
(control + exp/treatment)

- sample/pop split into 2 groups
- treatment given to experimental group, control group given a placebo

## Web Scraping

- Process of getting data from specific websites
- Not to be confused with web crawling (automatically scans through www - search engines)
- Using APIs, scrape data from certain websites
- Using **BeautifulSoup** to pull contents from HTML or XML pages (make sure you have permission!!!)

### Process

1. Request-response
2. Parse & extract
3. Transform the data

## Data Cleaning

- Missing data / discrepancies should be checked
- NaN values
- Inaccurate, incomplete, irrelevant, inconsistent
- Outlier - identify using **Box plot / data summary / bar chart (categorical)**
- Cleaning data is very important
- Format standardisation (eg: date, address)

### Missing Data

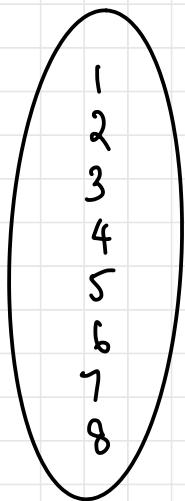
- impute - use other values (mean/mode)
- drop - delete

## Types of Statistics

- descriptive: organise, summarise data, tables, graphs, central ten.
- inferential: draw conclusions, hypothesis testing

### DESCRIPTIVE STATISTICS

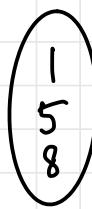
Parameter  
population



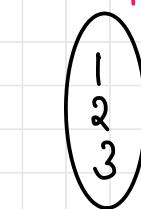
$N=10$

$\mu = 4.5$   
(mean)

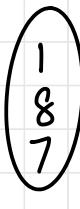
Statistic  
sample



$n=3$



$n=3$



$n=3$

Should be rep. of pop

$$\bar{x} = 4.67$$

(mean)

$$\bar{x} = 2$$

(mean)

$$\bar{x} = 5.33$$

(mean)

statistic

parameter

Difference b/w  $\mu$  and  $\bar{x}$ : sampling error

## Central Tendency

- 3 measures
- mean, median, mode, trimmed / truncated mean

cut off end  
outliers

## Trimmed mean

- 10% trimmed  $\rightarrow$  10% up & 10% down (80% used)

$\times \times \times \times \times \times \times$

Q:  $5, 4, 7, 6, 8, 10, 11, 0, 7, 18$  find mean, median, mode, trimmed mean (10%; 20%)

$$n = 10$$

$$\text{mean} = 7.6$$

$$\text{median} = ?$$

$0, 4, 5, 6, 7, 7, 8, 10, 11, 18$

$$\text{median} = 7$$

$$\text{mode} = 7$$

$$10\% \text{ trimmed mean} \Rightarrow (n)(0.10) = 10 \times 0.1 = 1 \text{ cut off each} \\ = 7.25$$

$$20\% \text{ trimmed mean} \Rightarrow \text{cut off 2 each} \\ = 7.167$$

D: 30, 75, 79, 80, 80, 105, 126, 138, 149, 179, 179, 191, 223, 232, 232, 236, 240, 242, 245, 247, 254, 274, 384, 470

n=24

$$\text{mean} = \frac{4690}{24} = 195.42$$

$$\text{median} = \frac{191+223}{2} = 207$$

mode = 80, 79, 232 (meaningless)

5% trimmed:  $(24)(0.05) = 1.2 \approx 1$   
drop 1

$$= 190.45$$

10% trimmed:  $(24)(0.10) = 2.4 \approx 2$   
drop 2  
= 186.55

20% trimmed:  $(24)(0.20) = 4.8 \approx 5$   
drop 5  
 $= \frac{2717}{14} = 194.07$

Q:  ~~$39, 92, 75, 61, 45, 87, 59, 51, 87, 12, 8, 93, 74, 16, 32, 39, 39, 45, 47, 50, 51, 59, 61, 74, 75, 87, 87, 87, 92, 93$~~

Find 5%, 10%, 20% trimmed mean

~~$8, 12, 12, 16, 32, 39, 39, 45, 47, 50, 51, 59, 61, 74, 75, 87, 87, 87, 92, 93$~~

$$n=20$$

$$\text{total} = 300 + 766 = 1066$$

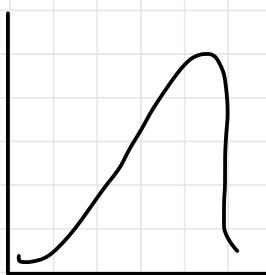
$$\text{mean} = 53.3$$

$$\begin{aligned} 5\% \text{ trimmed: } & 20 \times 0.05 = 1 \text{ drop} \\ & = 53.61 \end{aligned}$$

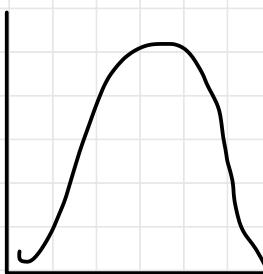
$$\begin{aligned} 10\% \text{ trimmed: } & 2 \text{ drop} \\ & = 53.8125 \end{aligned}$$

$$\begin{aligned} 20\% \text{ trimmed: } & 4 \text{ drop} \\ & = 54.92 \end{aligned}$$

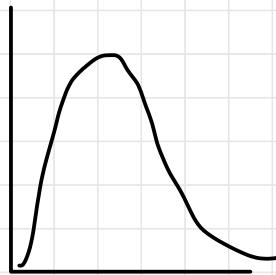
Symmetrical vs Skewed



negatively skewed



symmetric



positively skewed

## Measures of Dispersion / Spread

- How data is spread
- range, variance, std. deviation

### Range

- max value - min value
- misleading with outliers
- can indicate useful info for data without outliers

### Variance

#### Population

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^n (x_i - \mu)^2$$

#### Sample

$$s^2 = \frac{1}{(n-1)} \sum_{i=1}^n (x_i - \bar{x})^2$$

$\uparrow$   
(n-1) used  
Bessel's correction\*

### Standard deviation

#### Population

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^n (x_i - \mu)^2}$$

#### Sample

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

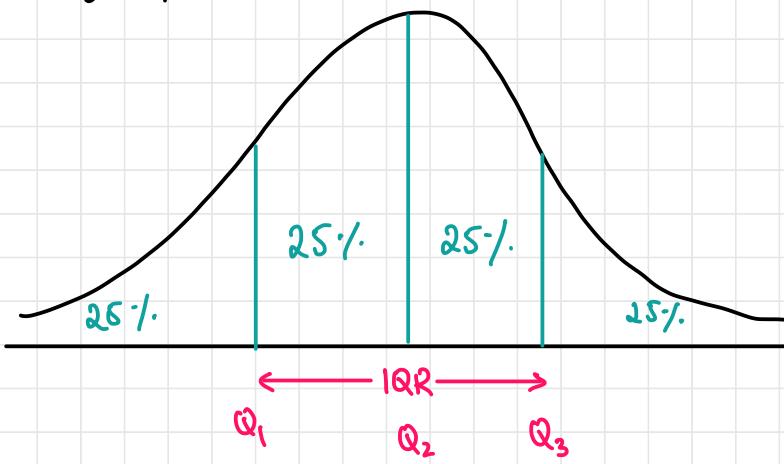
\* look up

## Quartiles

1. First quartile: 25<sup>th</sup> percentile =  $0.25(n+1)^{\text{th}}$  term  $Q_1$
2. Second quartile: 50<sup>th</sup> percentile =  $0.5(n+1)^{\text{th}}$  term  $Q_2$  (median)
3. Third quartile: 75<sup>th</sup> percentile =  $0.75(n+1)^{\text{th}}$  term  $Q_3$

## Interquartile range

$$= Q_3 - Q_1 \quad \text{IQR}$$



Q: Find quartiles and IQR

5, 7, 12, 14, 15, 22, 25, 30, 36, 42, 53, 65

$$\begin{aligned} \text{1}^{\text{st}} \text{ quartile} &= 0.25(12+1) = 3.25 = (3^{\text{rd}} + 4^{\text{th}})/2 \\ &= 13 \end{aligned}$$

$$\begin{aligned} \text{2}^{\text{nd}} \text{ quartile} &= 0.5(12+1) = 6.5 \\ &= (Q2 + Q5)/2 \\ &= 23.5 \end{aligned}$$

$$\begin{aligned} \text{3}^{\text{rd}} \text{ quartile} &= 0.75(12+1) = 9.75^{\text{th}} \\ &= (36 + 42)/2 \\ &= 39 \end{aligned}$$

$$\text{IQR} = 39 - 13 = 26$$

## PERCENTILE

- divides data into 100 equal parts
- to find  $p^{\text{th}}$  percentile,  $\left(\frac{p}{100}\right)(n+1)$  where  $n$  is the sample size.

Q: Find  $65^{\text{th}}$  percentile

30, 75, 79, 80, 80, 105, 126, 138, 149, 179,  
 179, 191, 223, 232, 232, 236, 240, 242, 245,  
 247, 254, 274, 384, 470

$$(0.65)(25) = 16.25$$

$$(16^{\text{th}} + 17^{\text{th}})/2$$

$$= (236 + 240)/2 = 238$$

## Tertile

- divide data into thirds

## Decile

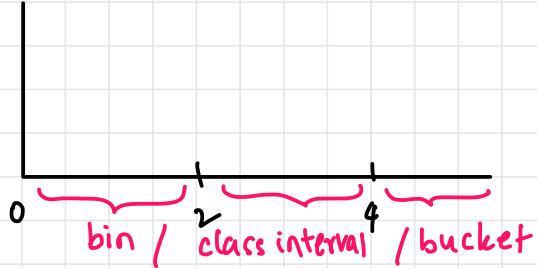
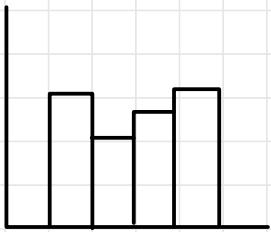
- divides data into tenths

# SUMMARY STATISTICS FOR CATEGORICAL DATA

- frequencies & relative frequencies *% of data in that category*
- sample proportion:  $\frac{\text{frequency}}{\text{sample size}}$

statquest

## 1 Histogram



- frequency distribution table
- does not include right end point

## FREEDMAN - DIACONIS RULE

$$\text{Bin size} = \frac{2 \cdot \text{IQR}(x)}{\sqrt[3]{n}}$$

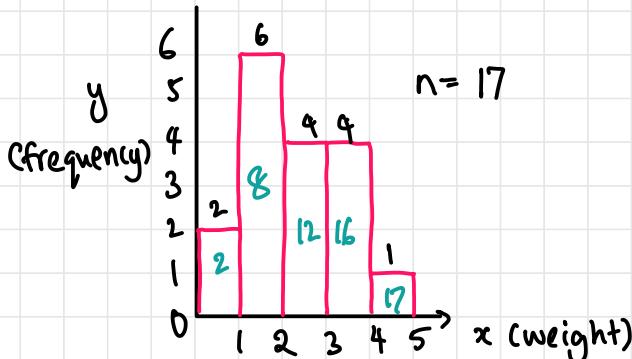
for unequal class width, height is density

$$\text{Density} = \frac{\text{relative frequency}}{\text{class width}}$$

or frequency

total density ] meaningless

### Mean, median, mode in histogram



$$\text{mode} = [1-2] = \frac{1+2}{2} = 1.5$$

median

$$\text{pos} = (0.5)(n+1) = 9 \\ 9 \text{ lies in } [2-3]$$

$$\text{median} = \frac{\text{lower} + (\text{pos}-\text{cf}) \times \text{C.W}}{\text{freq}}$$

$$= 2 + \frac{(9-8) \times 1}{4} = 2.25$$

## Quartiles

$$Q_1 = \text{pos} = (0.25)(n+1) = 4.5 \quad \text{lies in } [1-2]$$

$$Q_1 = \text{low} + \frac{(\text{pos} - \text{cf})}{\text{freq}} \times \text{cw}$$

$$= 1 + \frac{(4.5-2)}{6} \times 1 = 1.42$$

$$Q_3 = \text{pos} = (0.75)(18) = 13.5 \quad [3-4]$$

$$Q_3 = 3 + \frac{(13.5-12)}{4} \times 1 = 3.375$$

$$\text{IQR} = 1.96$$

$$\text{mean} = \frac{2 \times \left( \frac{0+1}{2} \right) + 6 \times \left( \frac{1+2}{2} \right) + 4 \left( \frac{2+3}{2} \right) + 4 \left( \frac{3+4}{2} \right) + \left( \frac{4+5}{2} \right) \times 1}{17}$$
$$= 2.265$$

$$\text{density} = \frac{\text{rel. freq}}{\text{class wid}}$$

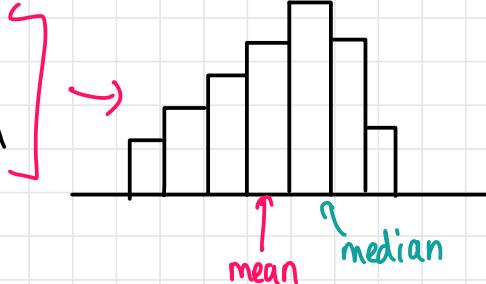
# Histogram Distributions

## 1) Symmetric

- normal, gaussian
- mean = median = mode

## 2) Left-skewed

- mean < median
- negatively skewed



## 3) Right-skewed

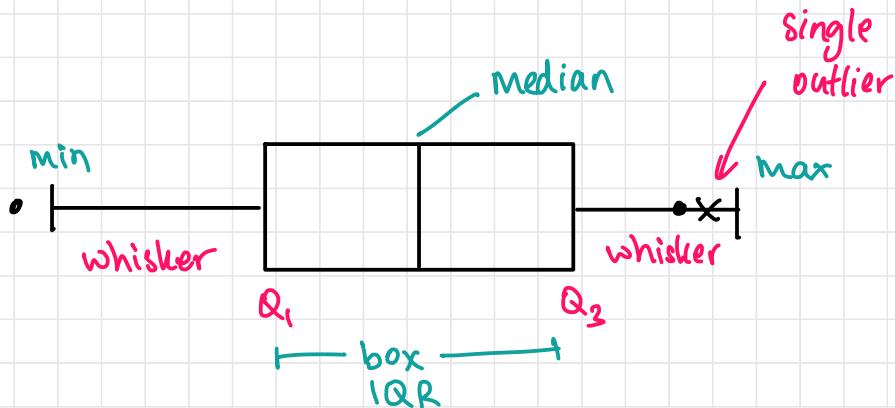
- mean > median
- distribution of wealth

Unimodal vs Polymodal  
single mode      multiple modes

- helps find outlier

## 2. Box Plot

- box-and-whisker plot



## Outliers

lower Whisker

$$= Q_1 - (1.5)(IQR)$$

upper Whisker

$$= Q_3 + (1.5)(IQR)$$



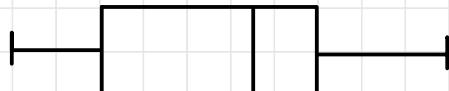
outliers  
outside  
this  
range

### 1) Symmetric

- normal, Gaussian
- mean = median = mode

### 2) Left-skewed

- mean < median
- negative



### 3) Right-skewed

- mean > median
- distribution of wealth
- positive



## Unimodal vs Polymodal

single mode

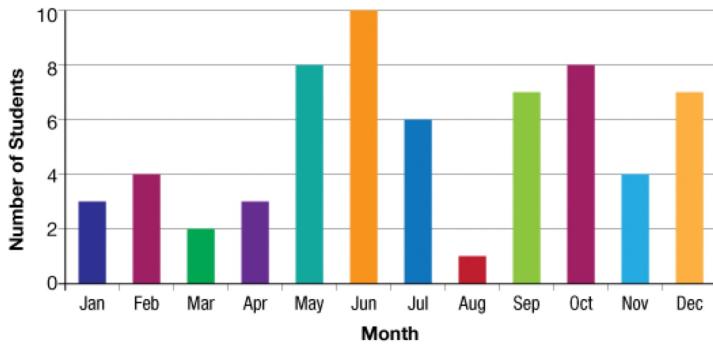
multiple modes

- helps find outlier

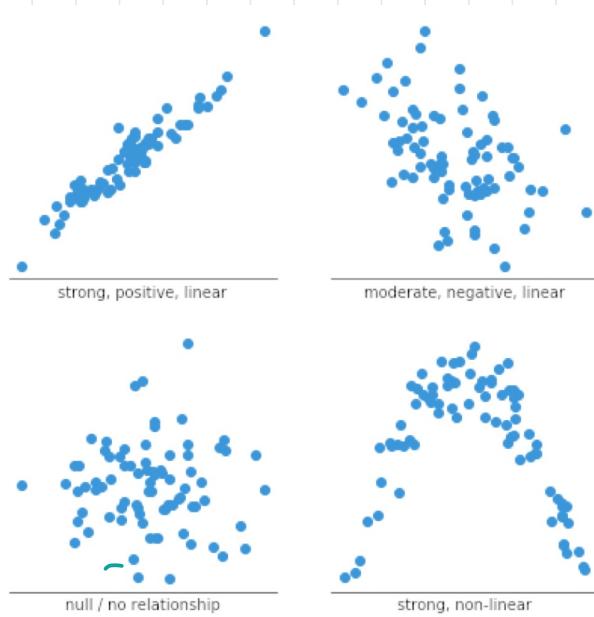
## Scatter Plots, Bar Charts, Heatmaps

### Bar Chart

Birthday of Students by Month



### Scatter Plot



# Heatmap

