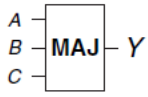
PES University,
Department of Computer Science and Engineering
UE19CS201: Digital Design and Computer Organization
Boolean Fucntions

1. What is the largest unsigned 32-bit binary number?
2. What is the largest 16-bit binary number that can be represented With,
   a) unsigned numbers? b) two's complement numbers? c) sign/magnitude numbers?
3. What is the smallest (most negative) 16-bit binary number that can be represented with,
   a) unsigned numbers? b) two's complement numbers? c) sign/magnitude numbers?
4. A majority gate produces a TRUE output if and only if more than half of its inputs are TRUE. Complete a truth table for the three-input majority gate shown in figure



5. A three-input AND-OR (AO) gate shown in Figure below produces a TRUE output if both A and B are TRUE, or if C is TRUE. Complete a truth table for the gate.

6. There are 16 different truth tables for Boolean functions of two variables. List each truth table. Give each one a short descriptive name (such as OR, NAND, and so on).
7. How many different truth tables exist for Boolean functions of N variables?
8. Sketch a schematic for the two-input XOR function using only NAND gates. How few can you use?
9. A gate or set of gates is universal if it can be used to construct any Boolean function. For example, the set {AND, OR, NOT} is universal.
   (a) Is an AND gate by itself universal? Why or why not? (b) Is the set {OR, NOT} universal? Why or why not?
   (c) Is a NAND gate by itself universal? Why or why not?
10. Write a Boolean equation in sum-of-products canonical form for each of the truth tables

(a)

A	B	Y
0	0	1
0	1	0
1	0	1
1	1	1

(b)

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

(c)

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

(d)

A	B	C	D	Y
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	0

(e)

A	B	C	D	Y
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

11. Write a Boolean equation in sum-of-products canonical form for each of the truth tables.

(a)

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

(b)

A	B	C	Y
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

(c)

A	B	C	Y
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

(d)

A	B	C	D	Y
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

(e)

A	B	C	D	Y
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

12. Write a Boolean equation in product-of-sums canonical form for the truth tables in question 10.
13. Ben Bitdiddle will enjoy his picnic on sunny days that have no ants. He will also enjoy his picnic any day he sees a hummingbird, as well as on days where there are ants and ladybugs. Write a Boolean equation for his enjoyment (E) in terms of sun (S), ants (A), hummingbirds (H), and ladybugs (L).

Note: The problems are taken from the text Book: Digital Design and Computer Architecture,David Money Harris,Sarah L. Harris Second Edition,