



DESIGN AND ANALYSIS OF ALGORITHMS

Surabhi Narayan

Department of Computer Science & Engineering

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Transform and Conquer

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Transform and Conquer



Transform and Conquer:

- In Transformation stage, the problem's instance is modified to be, for one reason or another, more amenable to solution.
- Then, in the second or conquering stage, it is solved.

There are three major variations

- Transformation to a simpler or more convenient instance of the same problem—we call it *instance simplification*.
- Transformation to a different representation of the same instance—we call it *representation change*.
- Transformation to an instance of a different problem for which an algorithm is already available—we call it *problem reduction*.

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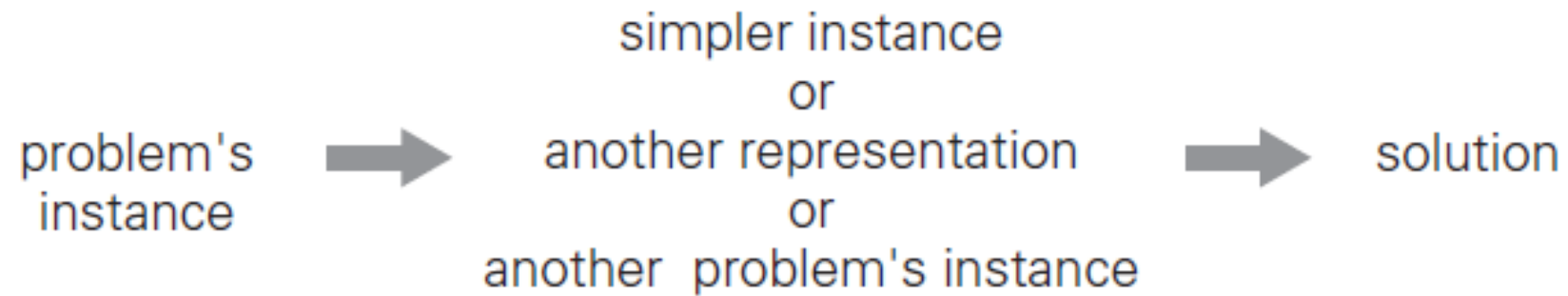


FIGURE 6.1 Transform-and-conquer strategy.

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Transform and Conquer



Checking element uniqueness in an array

The brute-force algorithm compared pairs of the array's elements until either two equal elements were found or no more pairs were left. Its worst-case efficiency was in (n^2) .

Alternatively, we can sort the array first and then check only its consecutive elements: if the array has equal elements, a pair of them must be next to each other, and vice versa.

ALGORITHM *PresortElementUniqueness*($A[0..n - 1]$)

//Solves the element uniqueness problem by sorting the array first

//Input: An array $A[0..n - 1]$ of orderable elements

//Output: Returns “true” if A has no equal elements, “false” otherwise

sort the array A

for $i \leftarrow 0$ **to** $n - 2$ **do**

if $A[i] = A[i + 1]$ **return** false

return true

$$T(n) = T_{\text{sort}}(n) + T_{\text{scan}}(n) \in \Theta(n \log n) + \Theta(n) = \Theta(n \log n).$$



THANK YOU

Surabhi Narayan

Department of Computer Science & Engineering

surabhinarayan@pes.edu