



Automata Formal Languages & Logic

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Unit 3

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Example 1:

Construct CFG for $L=\{uvwv^R, |u|=|w|=2, |v|>1, w \in \{a,b\}^*\}$

Solution :

$S \rightarrow A B$

$A \rightarrow aa \mid bb \mid ab \mid ba$

$B \rightarrow aBa \mid bBb \mid A$

Example 2:

Construct a CFG for $L = \{w \mid n_a(w) = n_b(w), w \in \{a,b\}^*\}$

Solution :

$S \rightarrow aSb \mid bSa \mid \lambda \mid SS$

Example 3:

Construct a CFG for $L = \{w \in \{a,b\}^* \mid n_a(w) = n_b(w) + 1\}$

Solution :

$S \rightarrow aSb \mid bSa \mid a \mid SS$

Example 4:

Construct a CFG for $L = \{w \mid n_a(w) = 2 \times n_b(w), w \in \{a,b\}^*\}$

Solution :

$S \rightarrow aSaSb \mid bSaSa \mid aSbSb \mid SS \mid \lambda$

Example 5:

Construct a CFG for $L = \{n_a(w) > n_b(w), w \in \{a,b\}^*\}$

Solution :

$S \rightarrow aSb \mid bSa \mid SS \mid aA \mid a$

Example 6:

Construct a CFG for $L = \{w \in \{a,b\}^* \mid n_a(w) \neq n_b(w)\}$

Solution :

$S \rightarrow A \mid B$

$A \rightarrow aAb \mid bAa \mid AA \mid aA \mid Aa \mid a$

$B \rightarrow aBb \mid bBa \mid BB \mid bB \mid Bb \mid b$

Example 7:

Construct a CFG for $L = \{a^n b^n \cup a^n b^{2n}\}$.

Solution :

$S \rightarrow S1 \mid S2$
 $S1 \rightarrow aS1b \mid \lambda$
 $S2 \rightarrow aS2bb \mid \lambda$

Example 8:

**Construct /a CFG for Language of proper nesting(parenthesis matching)
where $\Sigma = \{ (,) \}$.**

Solution :

$S \rightarrow (S) \mid SS$

$S \rightarrow \lambda$

Example 9:

**Construct /a CFG for Language of proper nesting(parenthesis matching)
where $\Sigma = \{(\{,[\ ,\},\},)\}$.**

Solution :

$S \rightarrow (S) \mid \{S\} \mid [S] \mid SS \mid \lambda$

Example 10:

Construct a CFG for Language to generate arithmetic expressions.

Solution :

$E \rightarrow E + E \mid E - E \mid E * E \mid E / E \mid (E) \mid id \mid number$

Example 11:

Construct a CFG for nested if else.

Solution :

$S \rightarrow \text{if condition then } S$

$S \rightarrow \text{if condition then } S \text{ else } S$

$S \rightarrow \{\text{statement}\}$

Example 12:

Construct a CFG to take care of variable declarations in C Language.

Solution :

$D \rightarrow \text{Type List}$

$\text{List} \rightarrow \text{List, id} \mid \text{id}$

$\text{Type} \rightarrow \text{int} \mid \text{float} \mid \text{char}$

Example 13:

Construct a CFG to generate nested while loops.

Solution :

$S \rightarrow \text{while}(\text{condition})S \mid \{\text{statement}\}$

Do while loop:

$S \rightarrow \text{while}(\text{condition})S \mid \text{do } S \text{ while } (\text{condition})\{\text{statement}\}$



THANK YOU

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