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PES UNIVERSITY, BENGALURU
(ESTABLISHED UNDER KARNATAKA ACT NO. 16 OF 2013)

UE17CS254

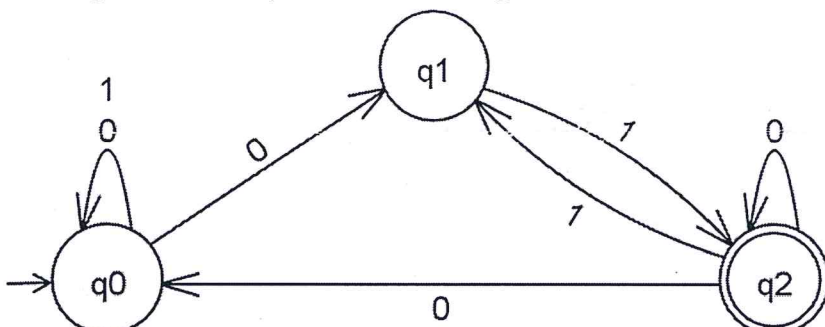
MAY 2019: END SEMESTER ASSESSMENT (ESA) B.TECH. IV SEMESTER

UE17CS254–THEORY OF COMPUTATION

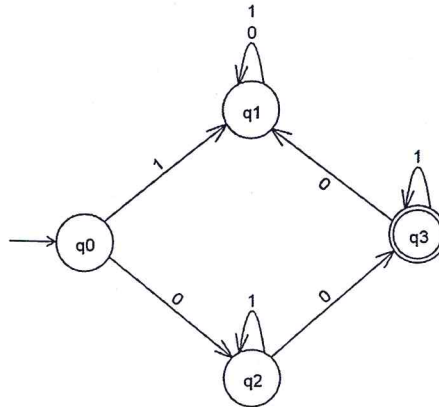
TIME: 3 HRS.

ANSWER ALL QUESTIONS

MAX MARKS:100

1.	a)	Define the following terms: i. Alphabet ii. Transition function iii. Grammar iv. Language	04																										
	b)	Construct a DFA to accept strings over {a, b} not ending with abb.	04																										
	c)	Convert the following NFA to its equivalent DFA using subset construction method: 	06																										
	d)	Minimize the following DFA using table filling algorithm: <table border="1" data-bbox="228 1397 1418 1554"><thead><tr><th>States</th><th>→A</th><th>B</th><th>*C</th><th>D</th><th>E</th><th>F</th><th>G</th><th>H</th></tr></thead><tbody><tr><td>0</td><td>B</td><td>G</td><td>A</td><td>C</td><td>H</td><td>C</td><td>H</td><td>G</td></tr><tr><td>1</td><td>F</td><td>C</td><td>C</td><td>G</td><td>F</td><td>G</td><td>F</td><td>C</td></tr></tbody></table>	States	→A	B	*C	D	E	F	G	H	0	B	G	A	C	H	C	H	G	1	F	C	C	G	F	G	F	C
States	→A	B	*C	D	E	F	G	H																					
0	B	G	A	C	H	C	H	G																					
1	F	C	C	G	F	G	F	C																					

2.	a)	Construct regular expressions for the following languages: i. $L = \{w \mid w \in \{a, b\}^* \text{ and } w \text{ has exactly one pair of consecutive } a\}$ ii. $L = \{a^n b^m : n \geq 3, m \text{ is odd}\}$ iii. Set of all strings over {a, b}* not ending with the substring 'ab'.	06
	b)	Using pumping lemma, show that the formal language of addition is not regular. For convenience, $r = p + q$ is represented as $a^p b^q c^r$.	06
	c)	Obtain regular expression for the following DFA using state elimination technique:	08



3.	a)	Can every linear grammar be converted to a form in which all productions look like $A \rightarrow ax$, where $a \in T$, $x \in V \cup \{\lambda\}$. Justify your answer.	02
	b)	Remove λ -productions, unit-productions, and useless productions from the following grammar: $S \rightarrow aA \mid aBB$ $A \rightarrow aaA \mid \lambda$ $B \rightarrow bB \mid bbC$ $C \rightarrow B$ What language does this grammar generates?	08
	c)	Convert the following grammar into Greibach Normal Form: $S \rightarrow ABb \mid a \mid b$ $A \rightarrow aaA \mid B \mid \lambda$ $B \rightarrow bAb$	06
	d)	Find an S-grammar for the following: i. $L = \{a^n b^n : n \geq 2\}$ ii. $L = \{a^n b^{n+1} : n \geq 1\}$	04
4.	a)	Construct an NPDA that accepts the following language over $\Sigma = \{a, b, c\}$: $L = \{a^n b^{n+m} c^m : n \geq 0, m \geq 1\}$	06
	b)	Discuss the steps involved in converting CFG to PDA & convert the following CFG to PDA. $S \rightarrow aSSab \mid \lambda$	10
	c)	State and prove pumping lemma for context-free languages.	04
5.	a)	Design a Turing Machine that reads a string representing a binary number and erases all leading 0's in the string. However, if the string comprises of only 0's, it keeps the least significant 0.	06
	b)	Let M be a Turing machine defined by the following transition table: $(\square = \text{blank})$	06

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	<table><tr><th>δ</th><th>\square</th><th>a</th><th>b</th><th>c</th></tr><tr><td>$\rightarrow q_0$</td><td>q_1, \square, R</td><td></td><td></td><td></td></tr><tr><td>q_1</td><td>q_2, \square, L</td><td>q_1, a, R</td><td>q_1, c, R</td><td>q_1, c, R</td></tr><tr><td>$*q_2$</td><td></td><td>q_2, c, L</td><td></td><td>q_2, b, L</td></tr></table>	δ	\square	a	b	c	$\rightarrow q_0$	q_1, \square, R				q_1	q_2, \square, L	q_1, a, R	q_1, c, R	q_1, c, R	$*q_2$		q_2, c, L		q_2, b, L	
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$*q_2$		q_2, c, L		q_2, b, L																		
	<p>i. Trace the computation for the input string $\square aabca \square$</p> <p>ii. Give the state diagram of M.</p> <p>iii. Describe the result of a computation in M.</p>																					
c)	<p>Write short notes on:</p> <p>i. Universal Turing machine</p> <p>ii. Post correspondence problem</p>		08																			
