



DATA STRUCTURES AND ITS APPLICATIONS

Balanced Trees

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DATA STRUCTURES AND ITS APPLICATIONS

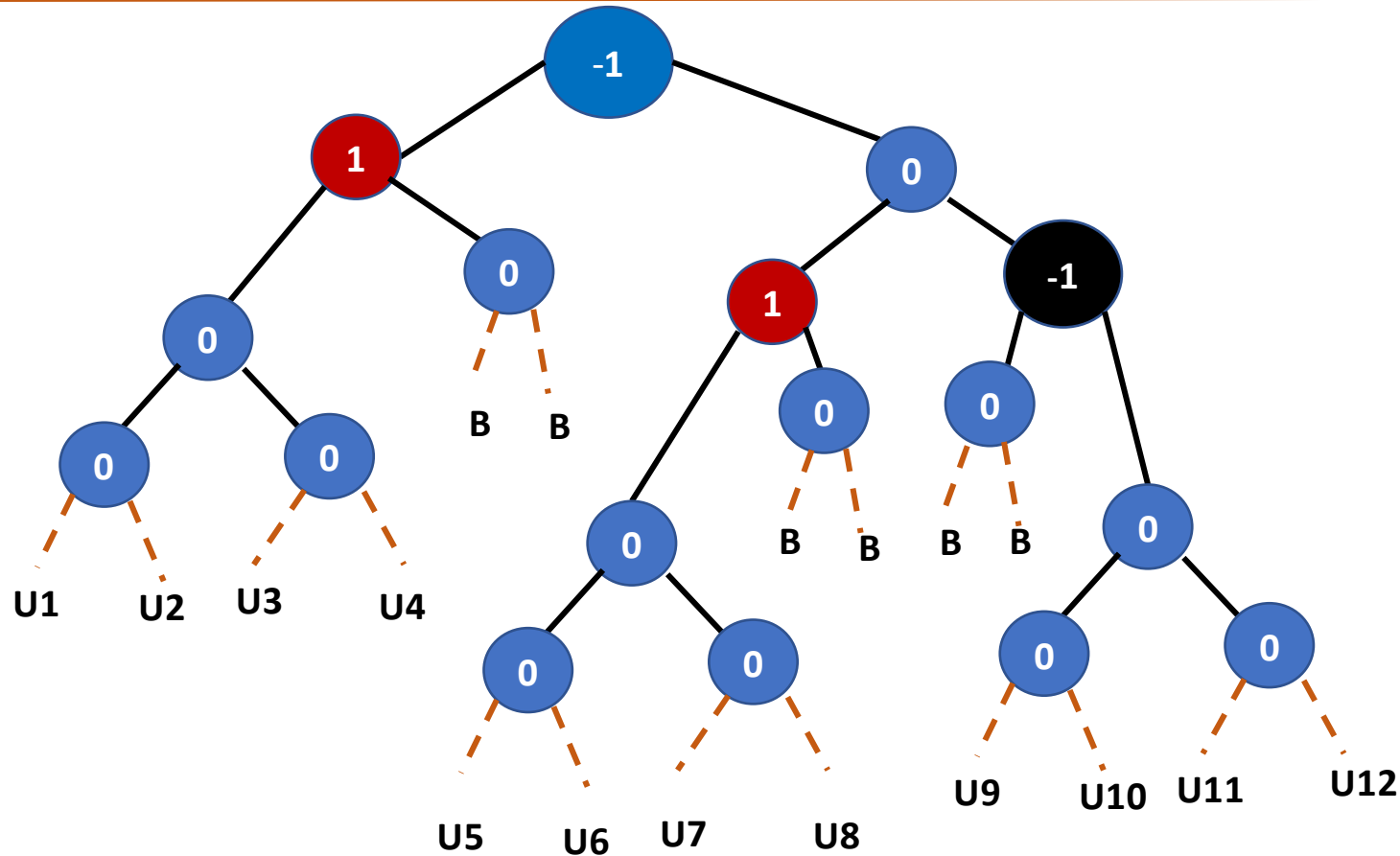
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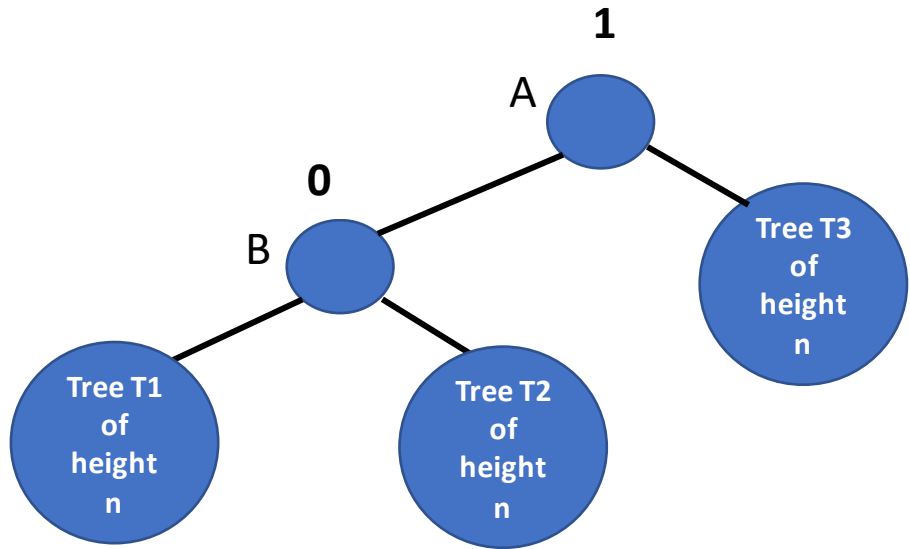
Possible insertion into AVL tree



- Unbalanced insertions are indicated by **U**
- Balanced insertions are indicated by **B**

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Unbalanced Tree after inserting a node to left subtree



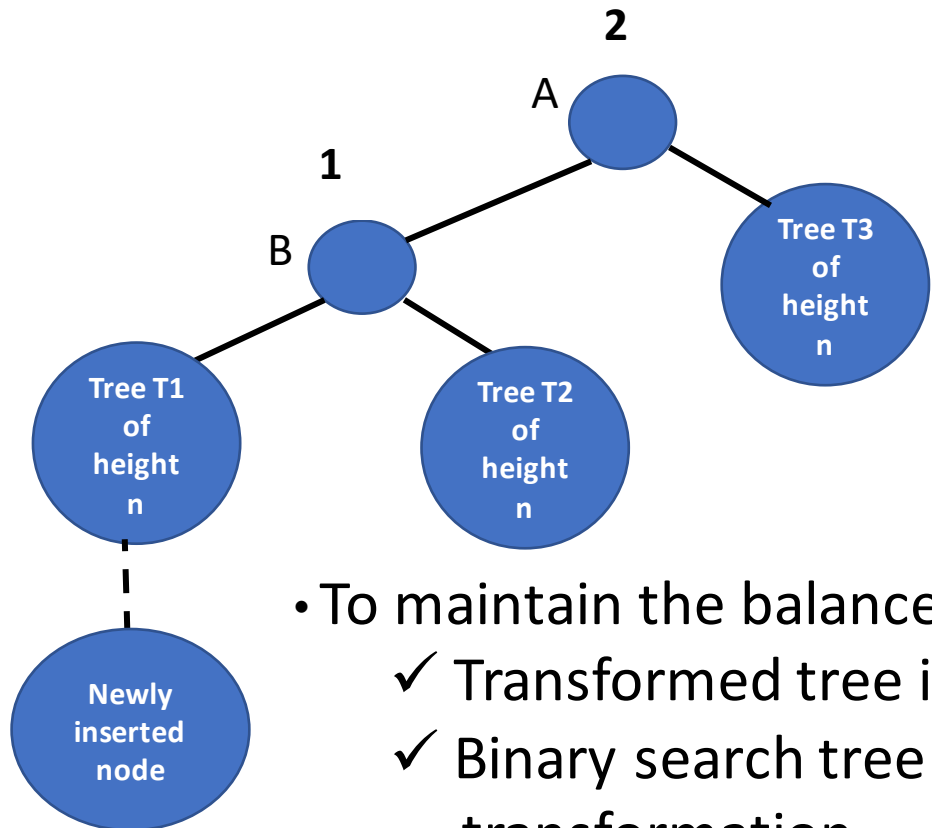
$$\text{Balance factor}(A) = (n+1) - n = 1$$
$$\text{Balance factor}(B) = n - n = 0$$

- Let us consider A is the youngest ancestor which becomes unbalanced
- Balance factor of A should 1 before insertion
- A should have a left child B with the balance factor of 0

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Unbalanced Tree after inserting a node to left subtree

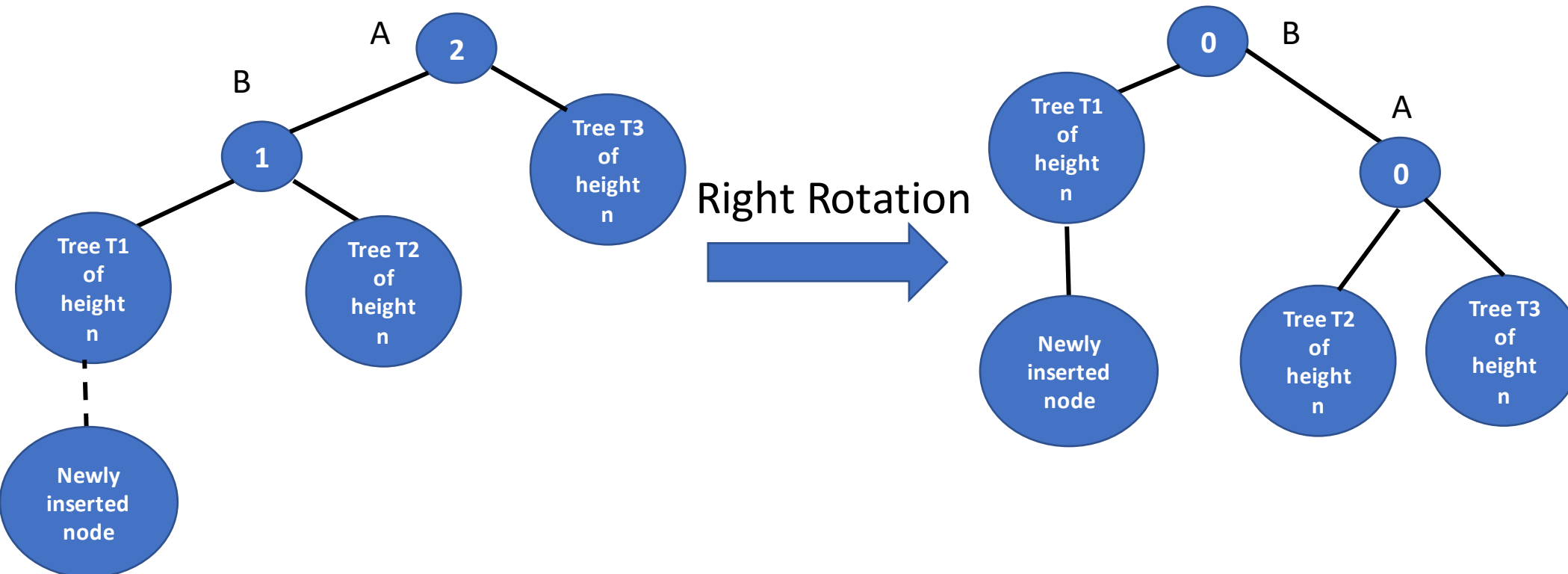
- Newly created node is inserted into left subtree of node B
- Changing the balance **B to 1** and **A to 2**
- A is the youngest ancestor of the new node to become unbalanced



- To maintain the balance : Tree needs to be transformed
 - ✓ Transformed tree is balanced
 - ✓ Binary search tree property is maintained after transformation

Transformed Balanced Tree after Rotations

- To maintain a balance we need to rotate sub tree B rooted at node A



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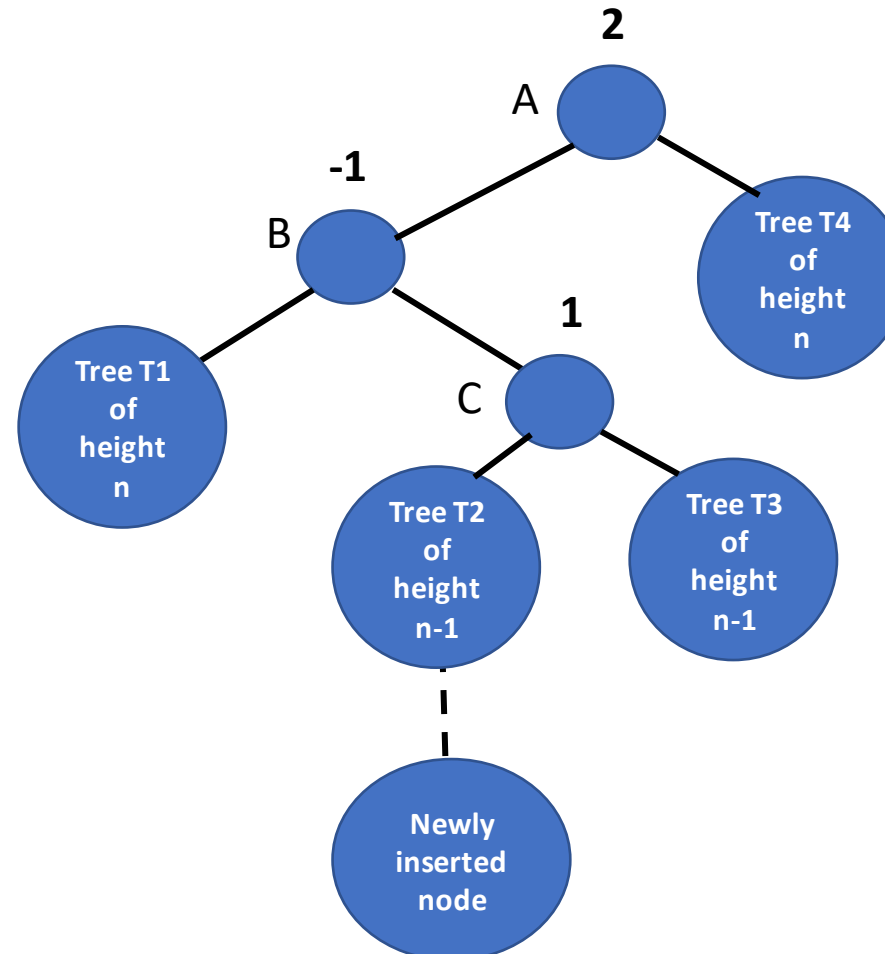
Unbalanced Tree after inserting a node to right subtree

- Newly created node is inserted into right subtree changing the balance:

Balance factor(C) = $n - (n - 1) = 1$

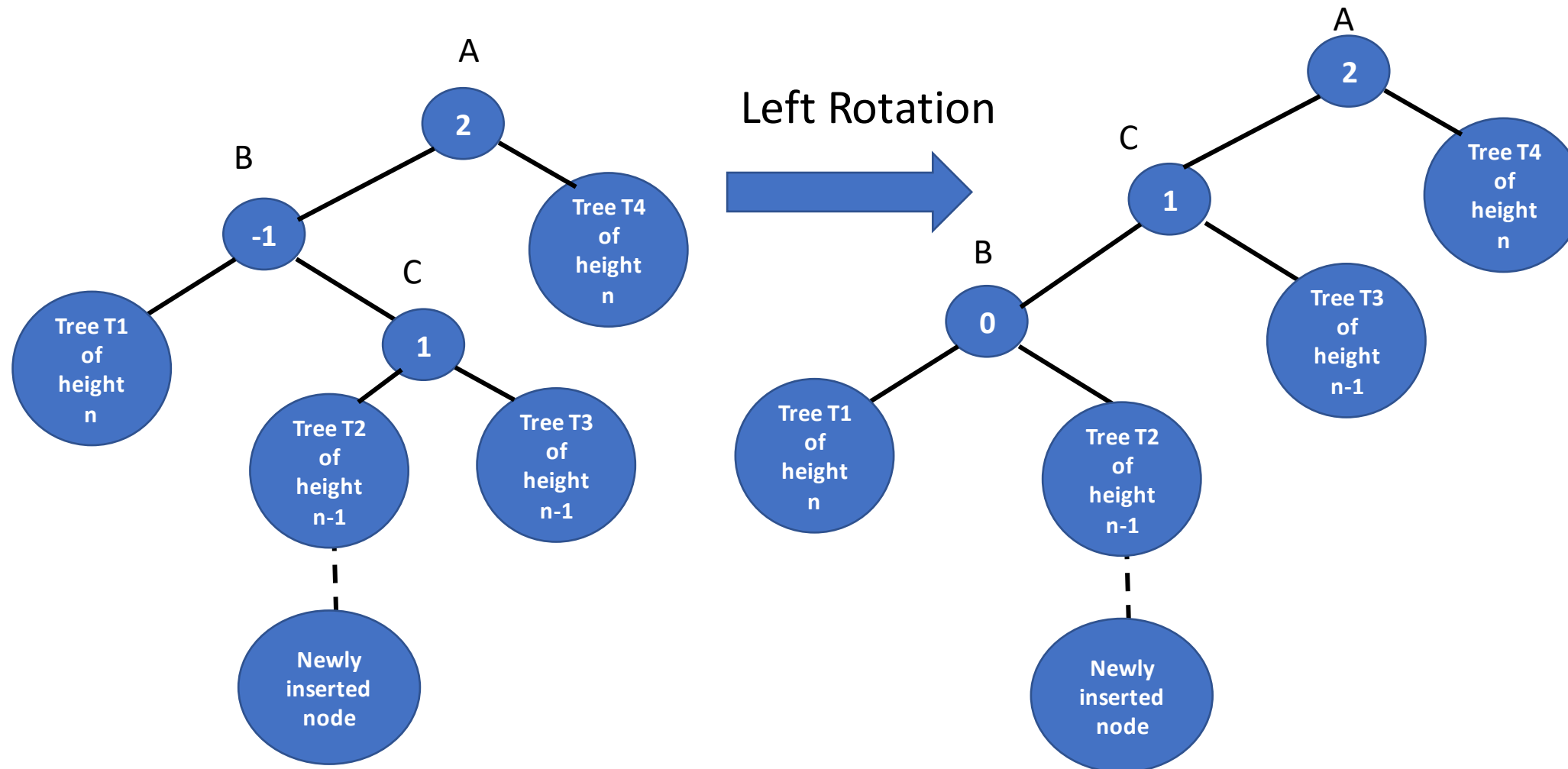
Balance factor(B) = $n - (n + 1) = -1$

Balance factor(A) = $n + 2 - n = 2$



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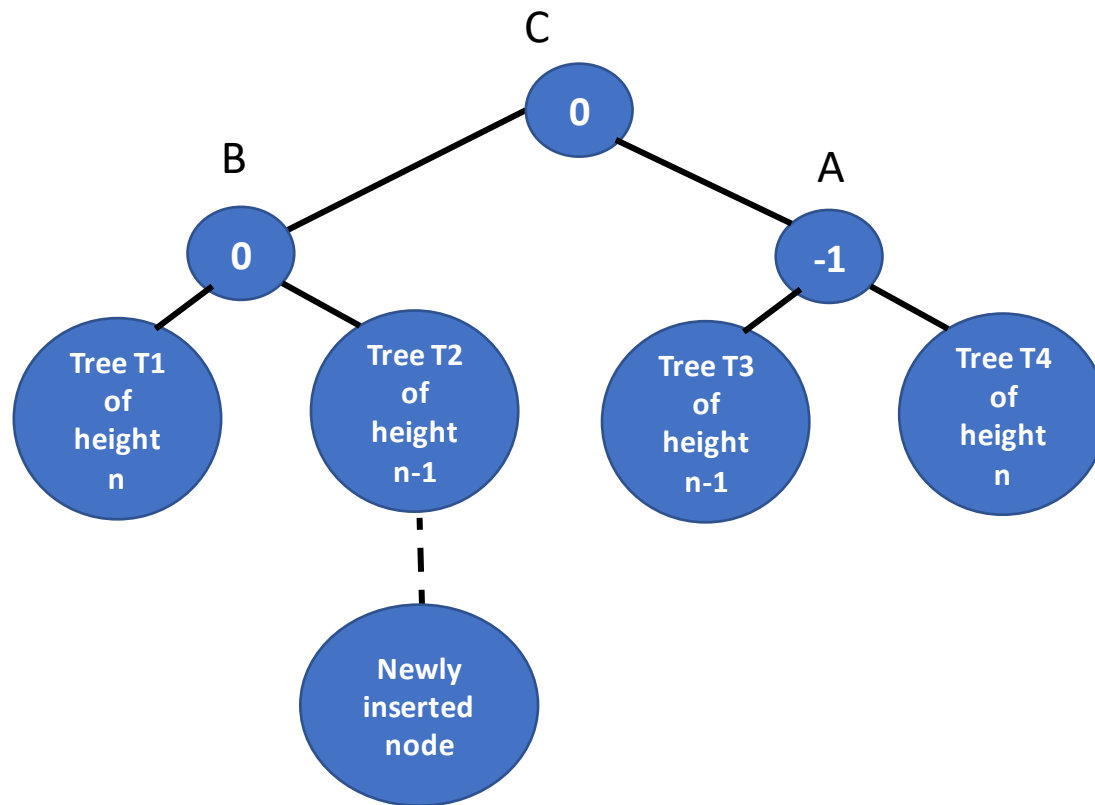
Transformed Balanced tree after Rotations



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Transformed Balanced tree after Rotations

Right Rotation



- Insertion in AVL tree is performed using standard BST Insertion
- If tree becomes unbalanced, we rebalance the tree using left or right rotation
- If node X is inserted into BST
- we need to find the youngest ancestor which becomes unbalanced

Four cases:

- Balance factor of node is greater than 1 – unbalanced node(U)
 - ✓ Left-Left case
 - if newly inserted key is less than the key in the left subtree' root
 - ✓ Left-Right case
 - if newly inserted key is greater than the key in the left subtree's root

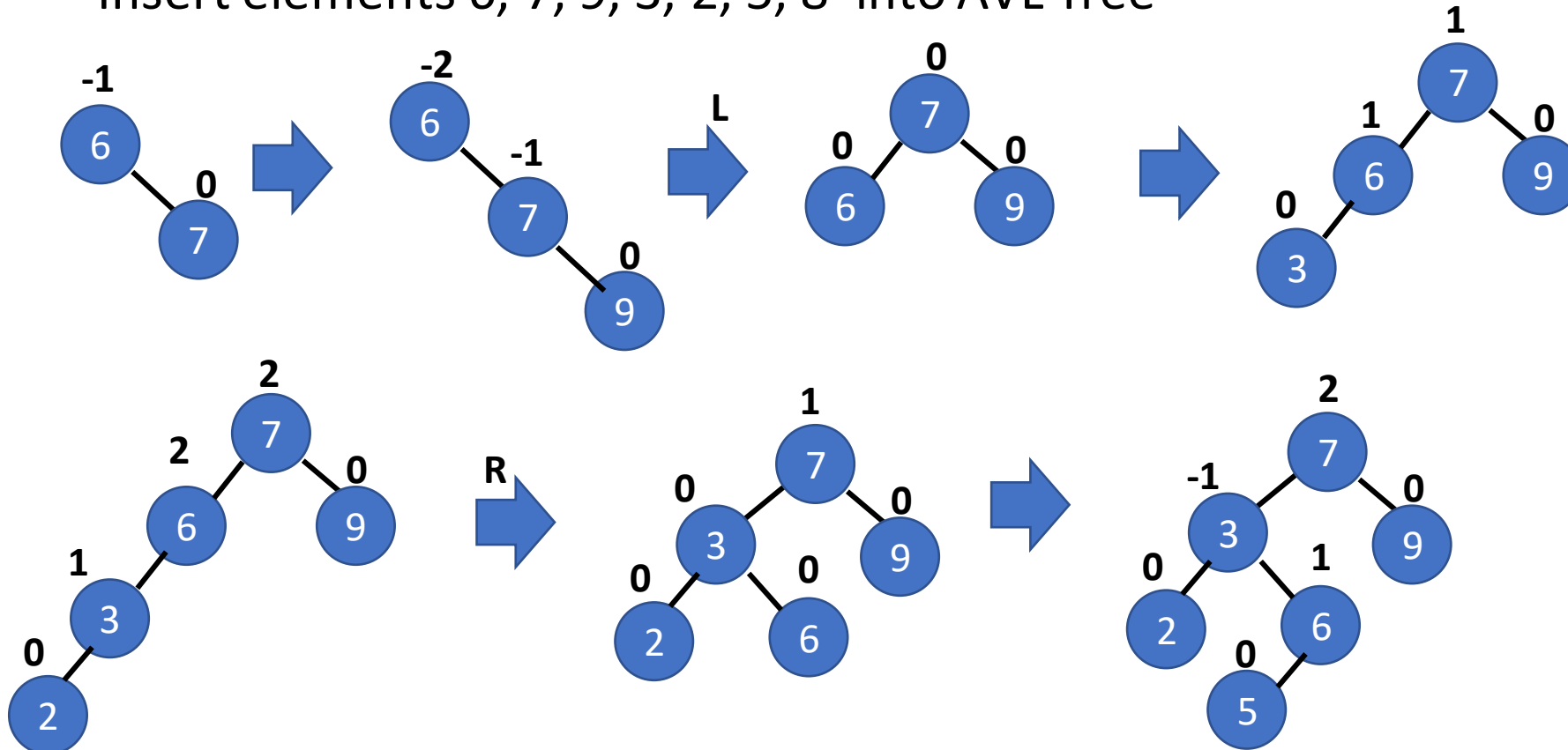
Four cases:

- Balance factor of node is lesser than -1 – unbalanced node(U)
 - ✓ Right-Right case
 - if newly inserted key is greater than the key in the right subtree' root.
 - ✓ Right-Left case
 - if newly inserted key is lesser than the key in the right subtree's root.

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Examples – AVL Tree Insertions

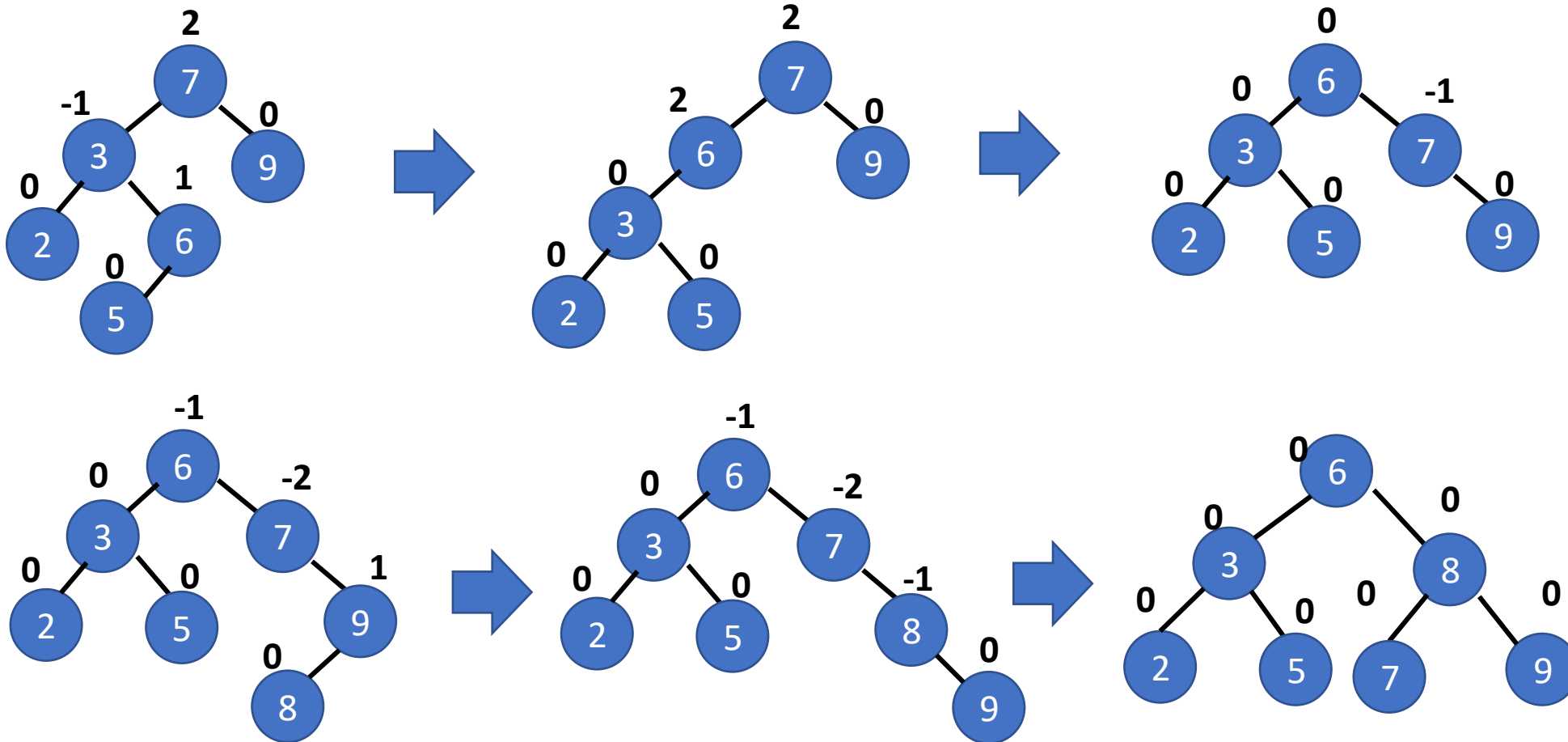
- Insert elements 6, 7, 9, 3, 2, 5, 8 into AVL Tree



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Example – AVL Tree Insertions

- Insert elements 6, 7, 9, 3, 2, 5, 8 into AVL Tree



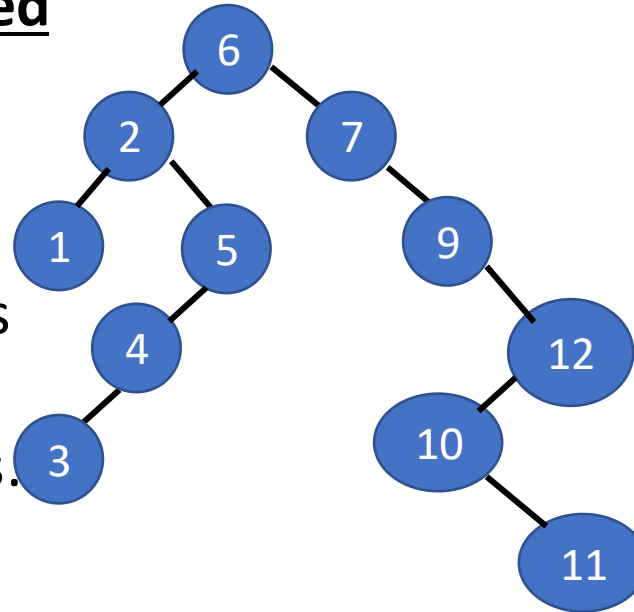
- Deletion in AVL tree is performed using standard BST Deletion
- If tree becomes unbalanced, we rebalance the tree using left or right rotation

BST Deletion: 3- case: Node to be deleted

Case 1: Does not have any children

Case 2: has either left or right subtrees

Case 3: has both left and right subtrees.



- If node X is deleted from the BST
- we need to find the youngest ancestor which becomes unbalanced

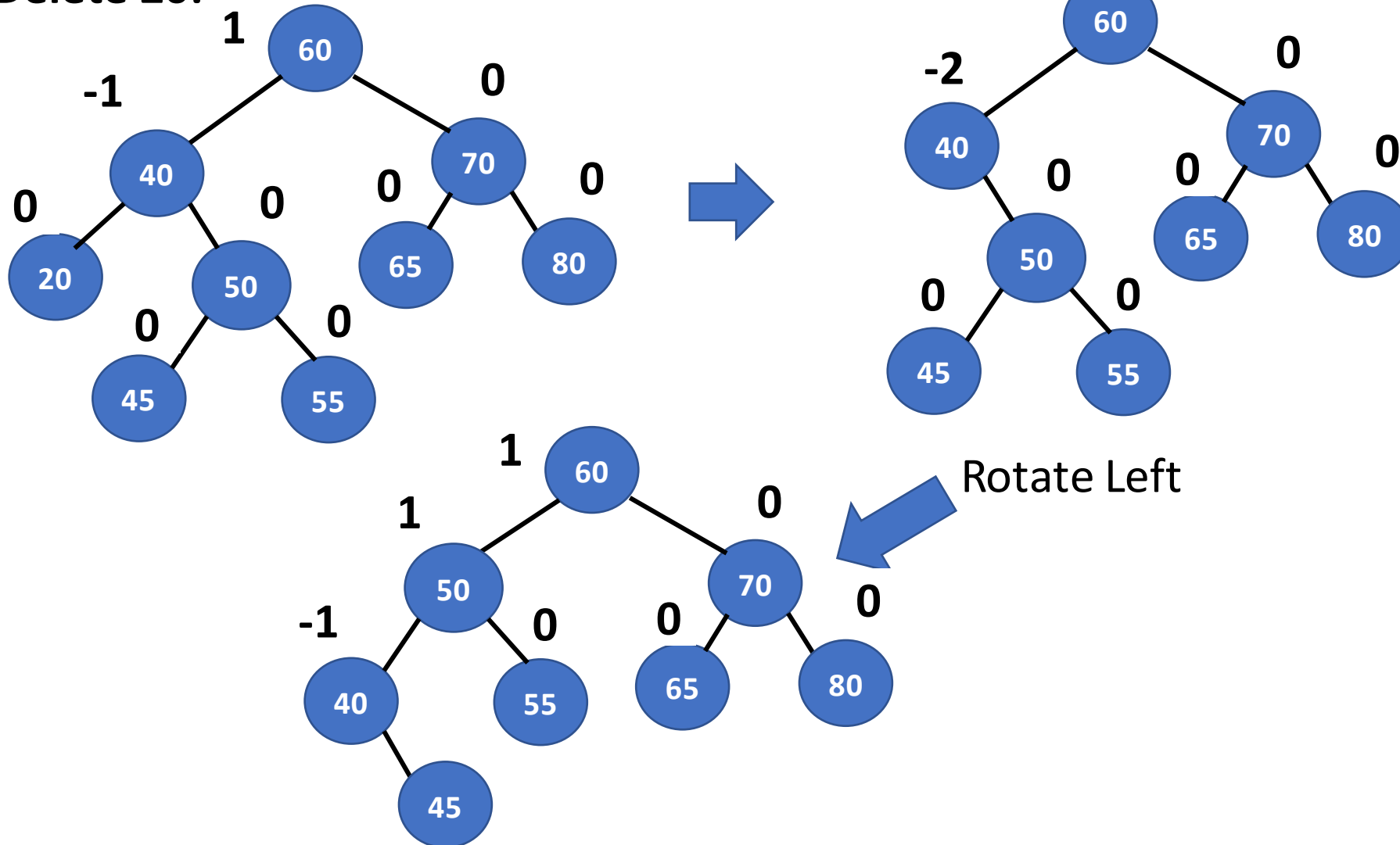
Four cases:

- Balance factor of a node is greater than 1 – unbalanced node(U)
 - ✓ Left-Left case
 - Balance factor of left subtree's root is greater than or equal to 0
 - ✓ Left-Right case
 - Balance factor of left subtree's root is less than 0
- Balance factor of unbalanced node is less than -1
 - ✓ Right-Right case
 - Balance factor of Right subtree's root is less than or equal to 0
 - ✓ Right-Left case
 - Balance factor of sub tree is greater than 0

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Example – Deletions in AVL tree

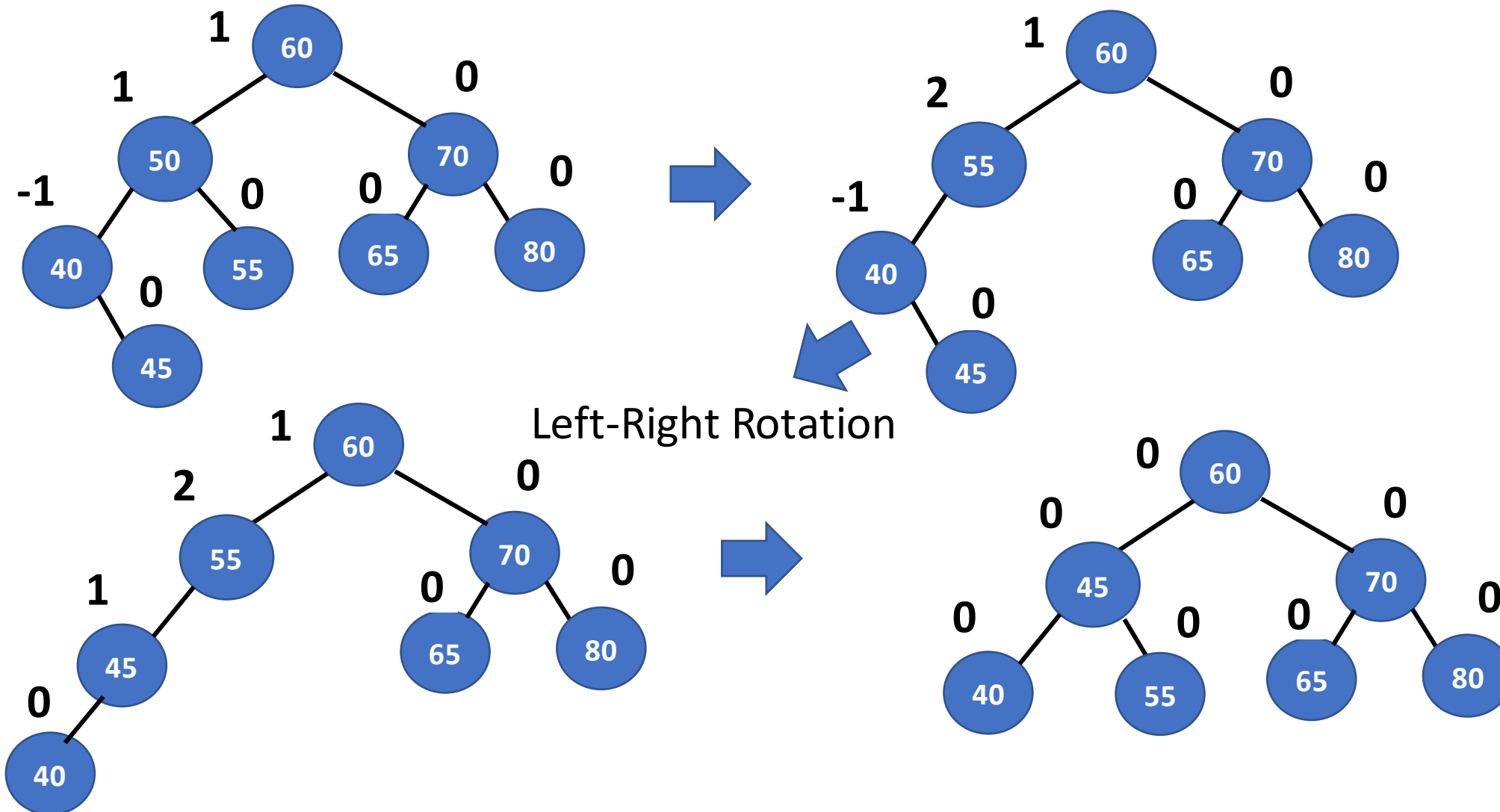
Delete 20:



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Example – Deletions in AVL tree

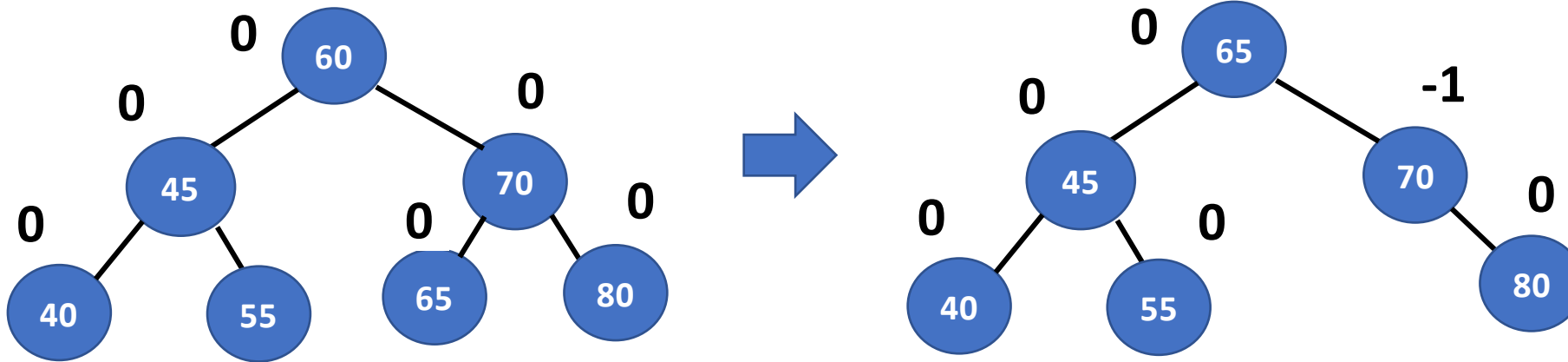
Delete 50:



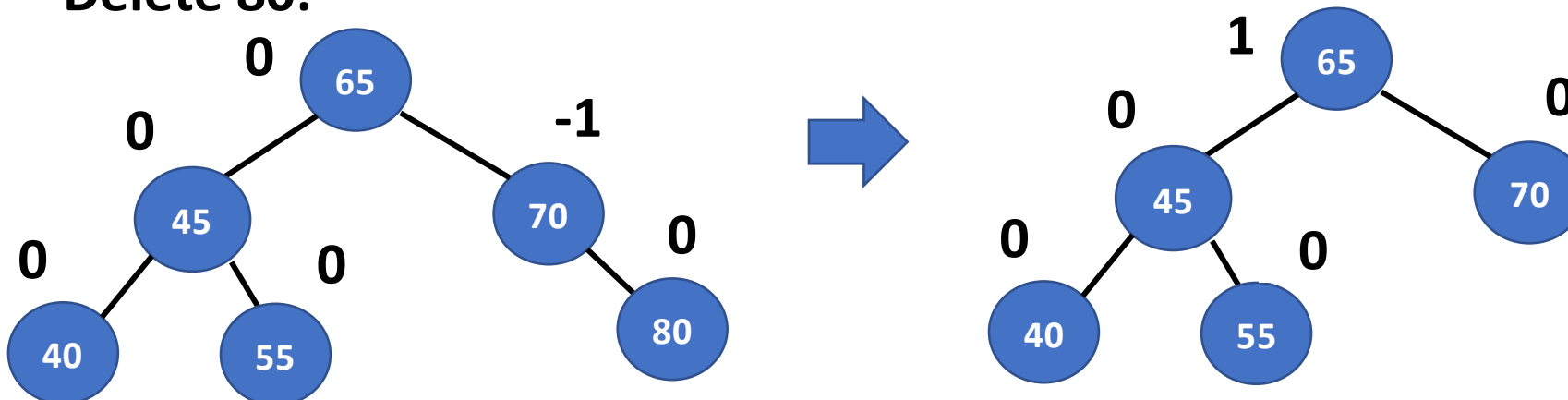
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Example – Deletions in AVL tree

Delete 60:



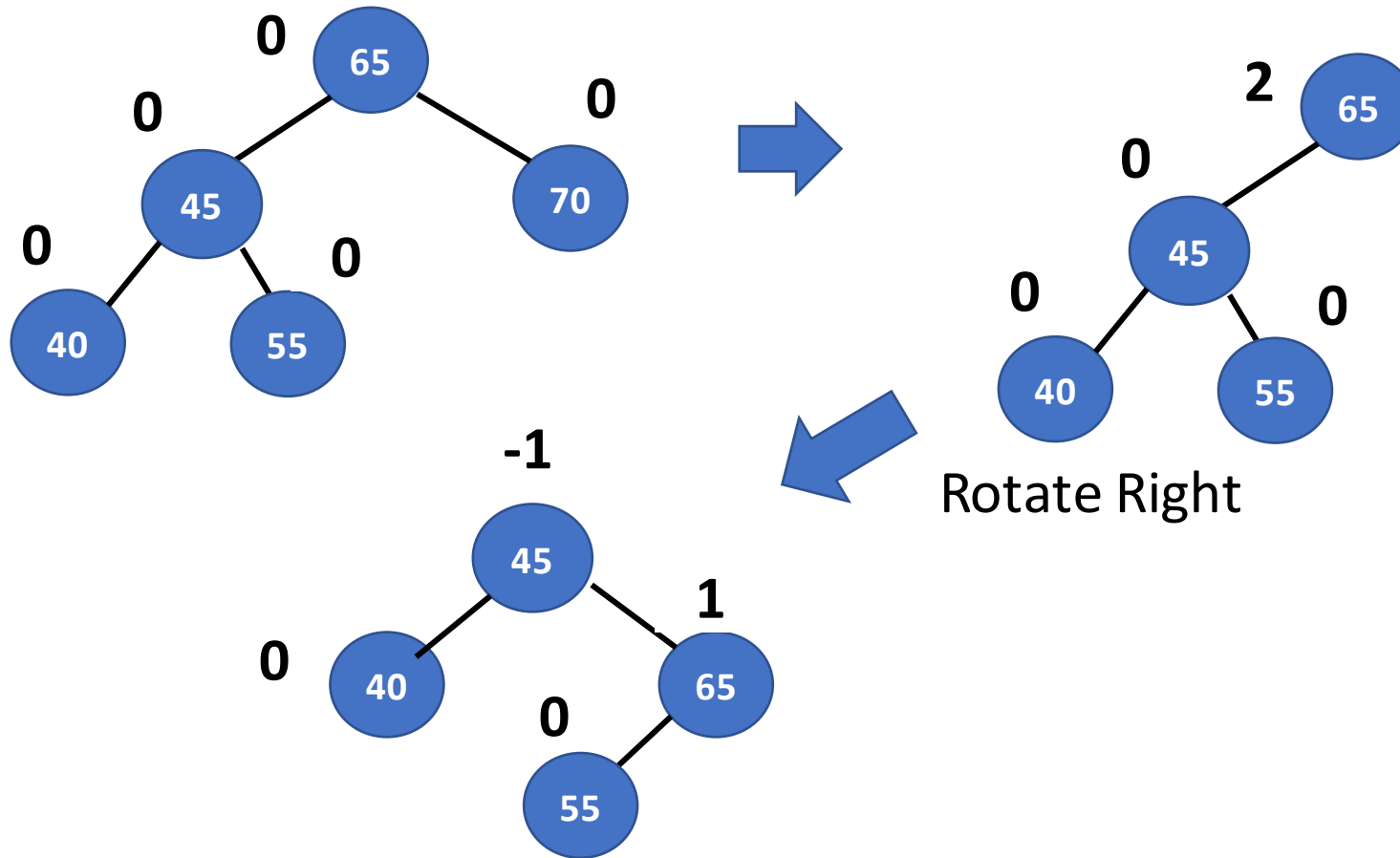
Delete 80:



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Example – Deletions in AVL tree

Delete 70:

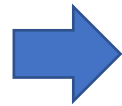
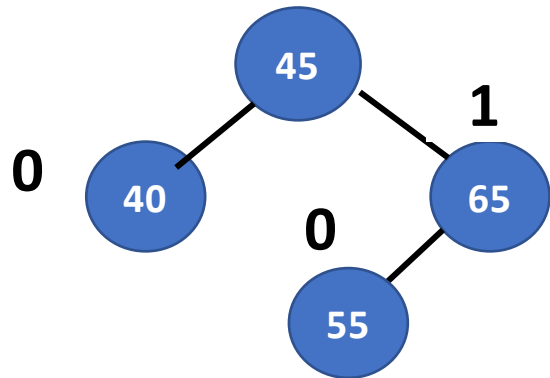


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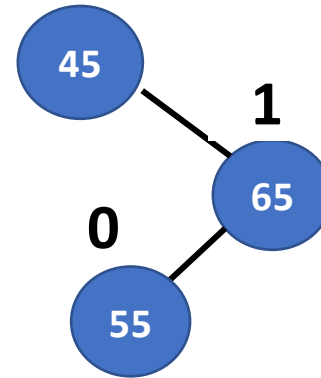
Example – Deletions in AVL tree

Delete 40:

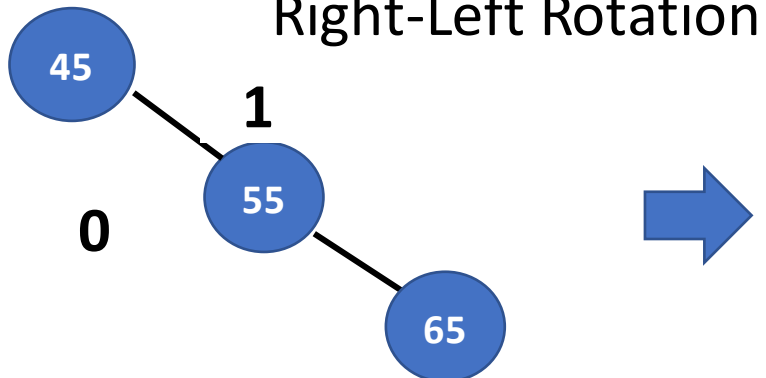
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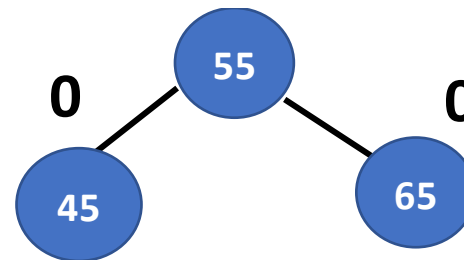
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THANK YOU

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