



# Automata Formal Languages & Logic

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## Unit 3

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### Example 1:

Parse the string abba using CYK algorithm ,

Grammar:

$S \rightarrow aSb \mid bSa \mid SS \mid \lambda$

### Solution :

Conversion to CNF

$S \rightarrow AB \mid BA \mid AC \mid BD \mid SS \mid \lambda$

$A \rightarrow a$

$B \rightarrow b$

$C \rightarrow SB$

$D \rightarrow SA$

Example 1:

Parse the string abba using CYK algorithm

Grammar:

$S \rightarrow aSb \mid bSa \mid SS \mid \lambda$

Solution :

4	S			
3	C	$\emptyset$		
2	S	$\emptyset$	S	
1	A	B	B	A
	a	b	b	a

1) Strings of the length 1 can be generated by

$A \rightarrow a$

$B \rightarrow b$

2) Strings of the length 2 can be generated by

For AB

$S \rightarrow AB$

For BA

$S \rightarrow BA$

For BB it is  $\emptyset$

3) Strings of the length 3 can be generated by

a)  $A.\emptyset \cup S.B = \emptyset.SB$  (SB is generated by C)

$C \rightarrow SB$

b)  $B.S \cup \emptyset.A$

BS is not generated by any rule

4) Strings of the length 4 can be generated by

$A.\emptyset \cup SS \cup CA$

$S \rightarrow SS$

The given string belongs to the grammar

Example 1:

Parse the string aabba using CYK algorithm ,

Grammar:

$S \rightarrow AB$

$A \rightarrow BB \mid a$

$B \rightarrow AB \mid b$

Solution :

5	$\emptyset$				
4	A	$\emptyset$			
3	S,B	A	$\emptyset$		
2	$\emptyset$	S,B	A	$\emptyset$	
1	A	A	B	B	A
	a	a	b	b	a

Length 3:

- 1)  $A(S,B) \cup \emptyset.B \quad (S \rightarrow AB, B \rightarrow AB)$   
 $AS, AB, \emptyset$
- 2)  $AA \cup (S,B)(B) \quad (A \rightarrow BB)$   
 $AA \cup SB, BB$
- 3)  $A.\emptyset$   
 $\emptyset$

Length 4:

- 1)  $AA \cup \emptyset.A \cup (S,B)(B)$   
 $AA \cup \emptyset \cup SB \cup BB$   
 $(A \rightarrow BB)$
- 2)  $A.\emptyset \cup (S,B)\emptyset \cup AA$   
 $\emptyset \cup \emptyset \cup AA$   
 $=\emptyset$

Length 5:

- $A\emptyset \cup \emptyset.\emptyset \cup (S,B)\emptyset \cup AA$   
 $=\emptyset$

The string does not belong to grammar



Example 1:

Parse the string baaa using CYK algorithm ,

Grammar:

$S \rightarrow AA \mid BC$

$A \rightarrow BA \mid a$

$B \rightarrow CC \mid b$

$C \rightarrow AB \mid a$

Solution :

4	S,A,C			
3	∅	S,A,C		
2	A,S	B	B	
1	B	A,C	A,C	A,C
	b	a	a	a

Length 3:

- 1)  $BB \cup \{A, S\}\{A,C\}$   
 $BB \cup AA \cup AC \cup SA \cup SC$   
 $= \emptyset$
- 2)  $(A,C)(B) \cup B(A,C)$   
 $AB \cup CB \cup BA \cup BC$   
 $S \rightarrow AB \mid BC \quad A \rightarrow BA$   
 $C \rightarrow AB$

Length 4:

$B(S,A,C) \cup (A,S)B \cup \emptyset(A,C)$   
 $= BS \cup BA \cup BC \cup AB,SB$   
 $A \rightarrow BA$   
 $S \rightarrow BC$   
 $S \rightarrow AB$   
 $C \rightarrow AB$

The string baaa belongs to the grammar



# THANK YOU

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