



# LINEAR ALGEBRA AND ITS APPLICATIONS

## UE19MA251

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## Unit 3. Linear Transformations and Orthogonality

### *Transformations Represented by Matrices*

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#### *Rotation Matrices $Q$ :*

The matrix that rotates ( left ) every point in  $\mathbb{R}^2$  about origin through  $\theta$  is given by

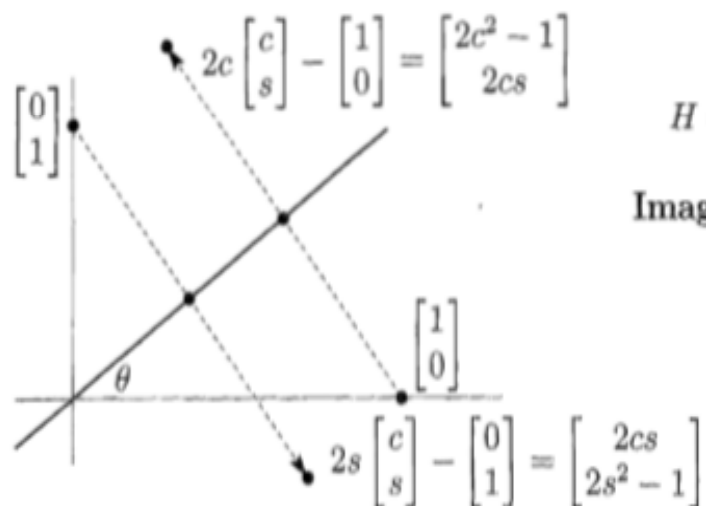
$$Q_{\theta} = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$$

This transformation is invertible since the matrix has an inverse.

A rotation through  $-\theta$  brings back the original.

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$$H = 2P - I = \begin{bmatrix} 2c^2 - 1 & 2cs \\ 2cs & 2s^2 - 1 \end{bmatrix}$$

Image + original =  $2 \times$  projection

$$Hx + x = 2Px$$

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#### *To conclude....*

Product of two transformations is another transformation by itself. Matrix multiplication is so defined that product of matrices corresponds to the product of the transformations that they represent.





THANK YOU

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