

Date :- September 10, 2020

AFLC

Last class :-

Equivalence of RE and FA

- 1)  $RE \rightarrow FA$  (Thompson construction method)
- 2)  $FA \rightarrow RE$  (State Elimination method)

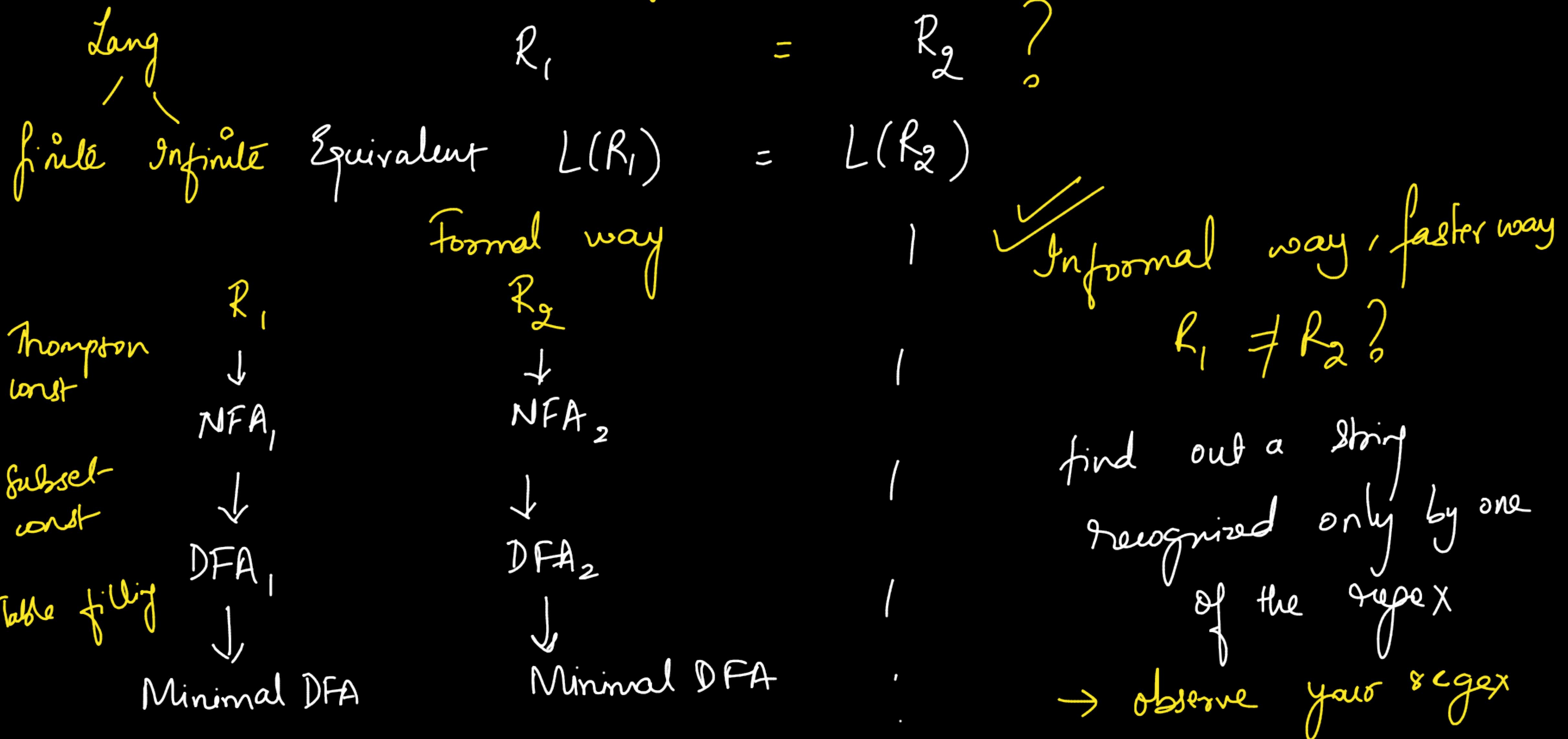


Today's class :-

- ✓ 1) Solve one more question on  $FA \rightarrow RE$
- ✓ 2) Equivalence of two RE
- ✓ 3) Regular Grammar
  - ✓ 3.1) Construction
  - 3.2) Equivalence of RG and FA

$FA \rightarrow RG$ ,  
 $RG \rightarrow FA$  is pending

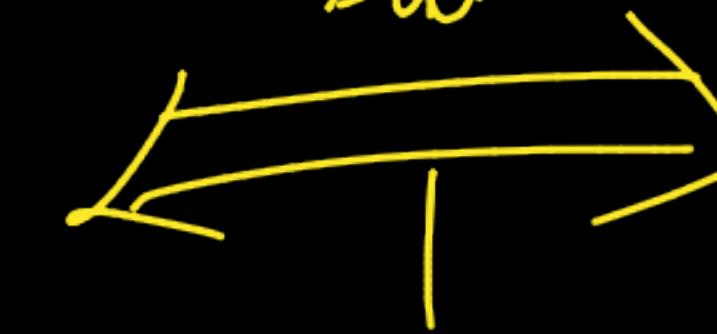
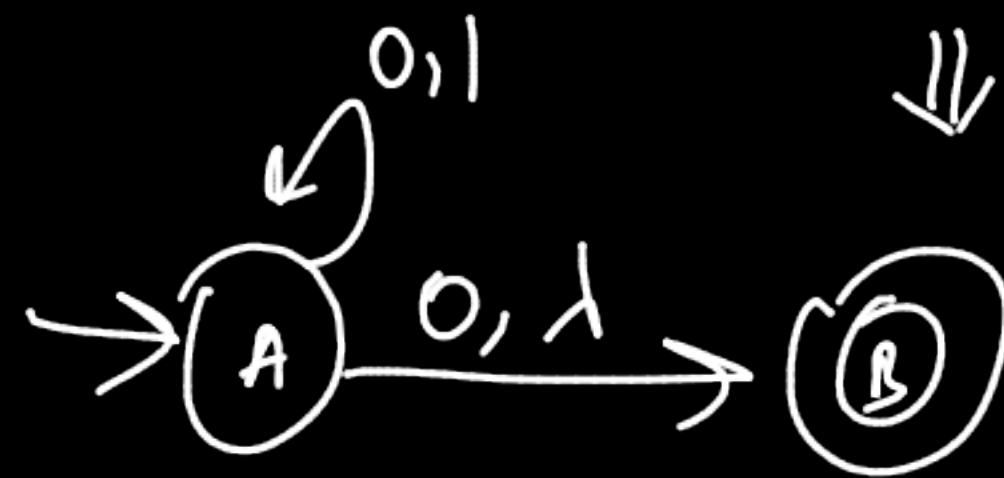
## Equivalence of two Regex



Example :- formal way

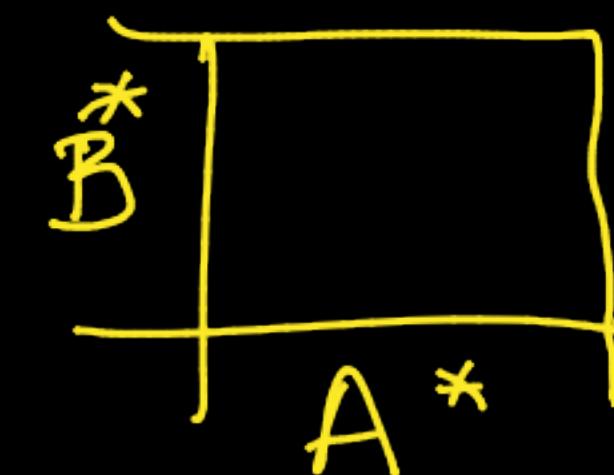
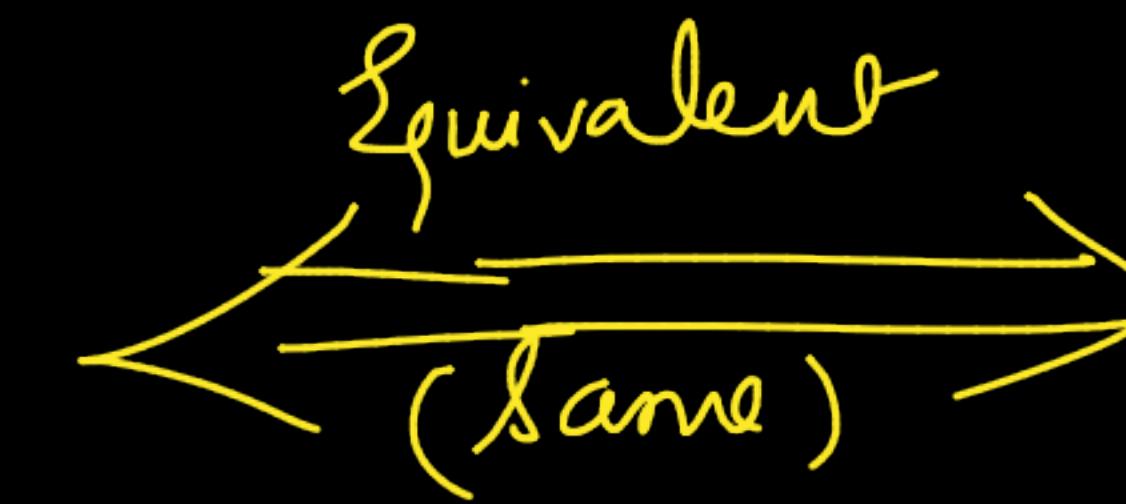
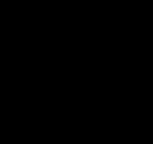
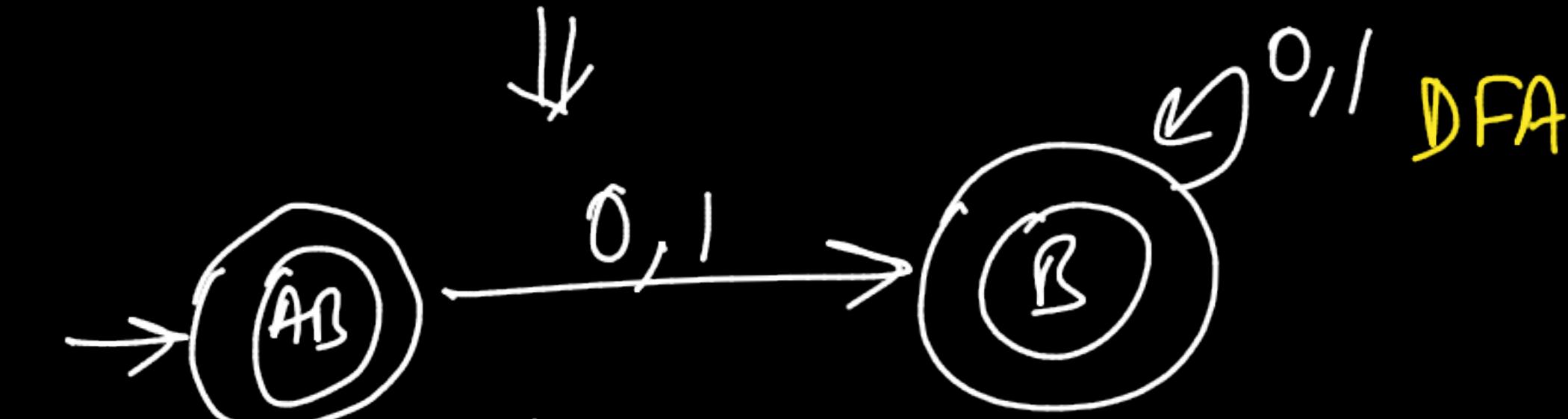
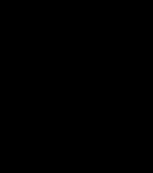
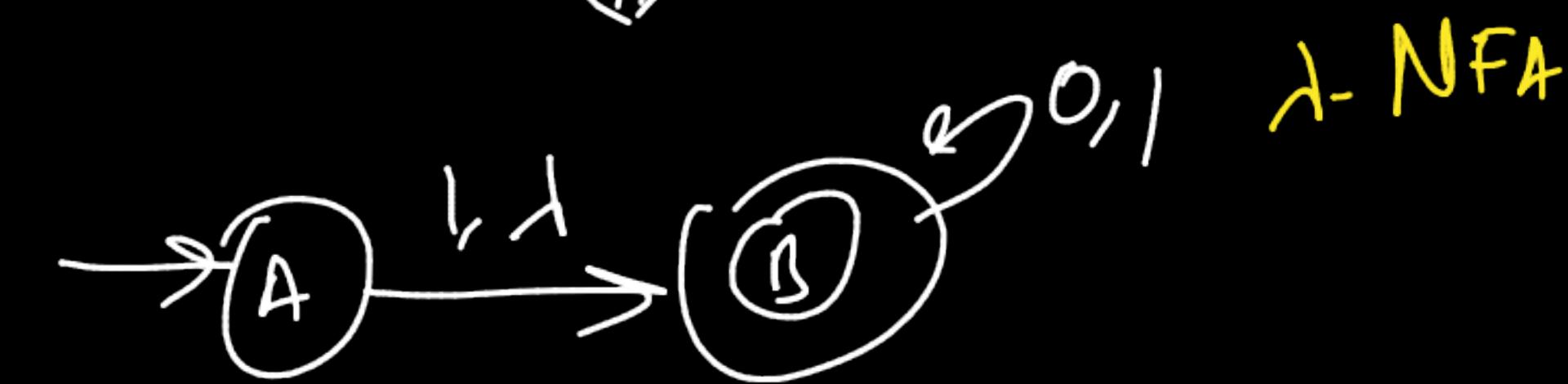
$$R_1 = (0+1)^* (0+\lambda)$$

$$(0+1)^*$$



$$R_2 = (1+\lambda) (1+0)^*$$

$$(0+1)^*$$



Example :

$$R_1 = (0+\lambda) (11^* 0)^* (1+\lambda)$$

$R_2 =$

$$(1+\lambda) \boxed{(01)^*} (0+\lambda)$$

Not equivalent

$$110 \rightarrow R_1$$

$$\rightarrow X R_2$$

$$011 \begin{matrix} \nearrow X R_1 \\ \searrow R_2 \end{matrix}$$

Minimal strings

$R_1$

$\{\lambda\}$

Minimal strings

$R_2$

$\{01\}$

## Regular Grammar

Grammar - captures syntax

Basis of all the Programming lang

=, \*, +

$\Rightarrow \text{if } (a \geq b) \{ a = 0 \}$

$\Rightarrow S \rightarrow \boxed{\text{if}} \quad (\text{Cond}) \{ S \}^{\text{PL's}}$

Cond  $\rightarrow \dots \dots$

Keyword

(terminal)

(Input symbols in your  $\Sigma$ )

Formal Definition

Grammar is a 4 tuple

$$G = (V, T, P, S)$$

$V = \text{Set of Variables (Non-Terminals expanded)}$

$$S \in V$$

$T = \text{Terminals } (\Sigma)$

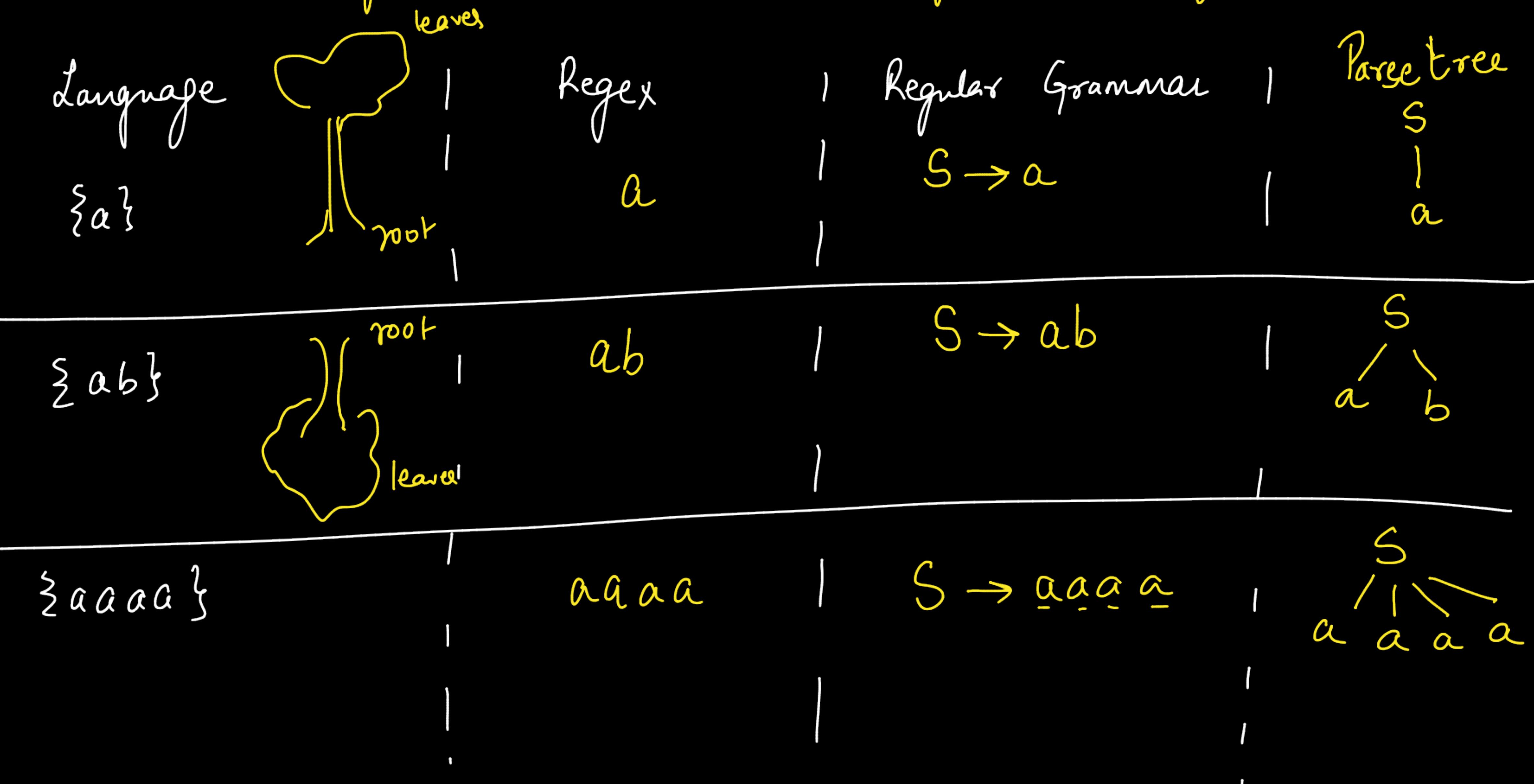
$P = \text{Set of production rules } \alpha \rightarrow \beta$

$\alpha, \beta \in (VUT)^*$

Regular grammar  $V \rightarrow \beta$

$S = \text{Start symbol / Variable of your } G$

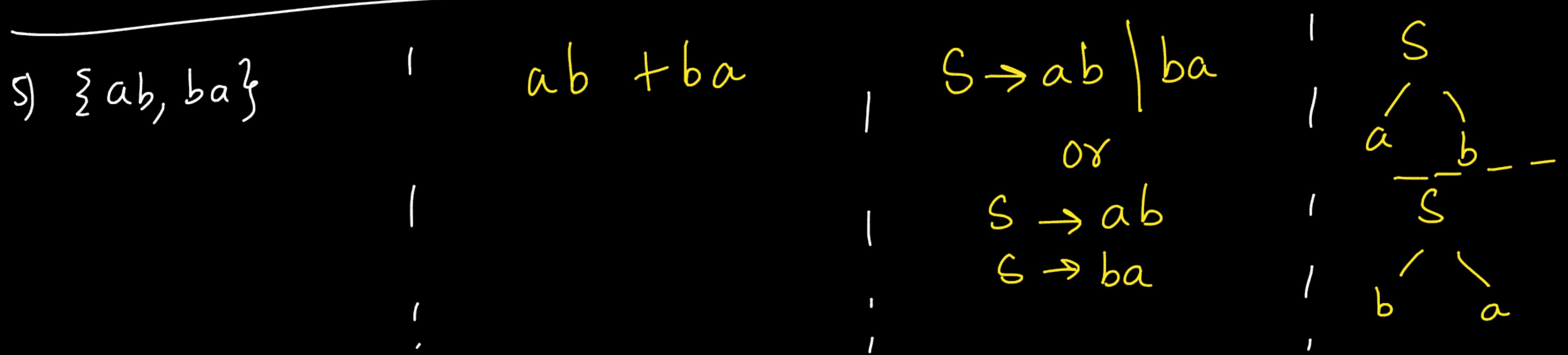
Construct Regular Grammar for the given language Descriptions:



Construct regular grammar for the given language descriptions

Parse tree

Language	Regex	Regular Grammar	Parse tree
4) $\{a, b\}$	$a + b$	$S \rightarrow a$ $S \rightarrow b$ or $S \rightarrow a \mid b$	$S$   $b$   Non-rewriting grammar
5) $\{ab, ba\}$	$ab + ba$	$S \rightarrow ab \mid ba$ or $S \rightarrow ab$ $S \rightarrow ba$	$S$   $a \overline{b} - -$   $b \overline{a} - -$



Construct Regular Grammar for the given language descriptions: yield of

Language

6)  $\{\lambda, a, aa, aaa \dots\}$

Regex

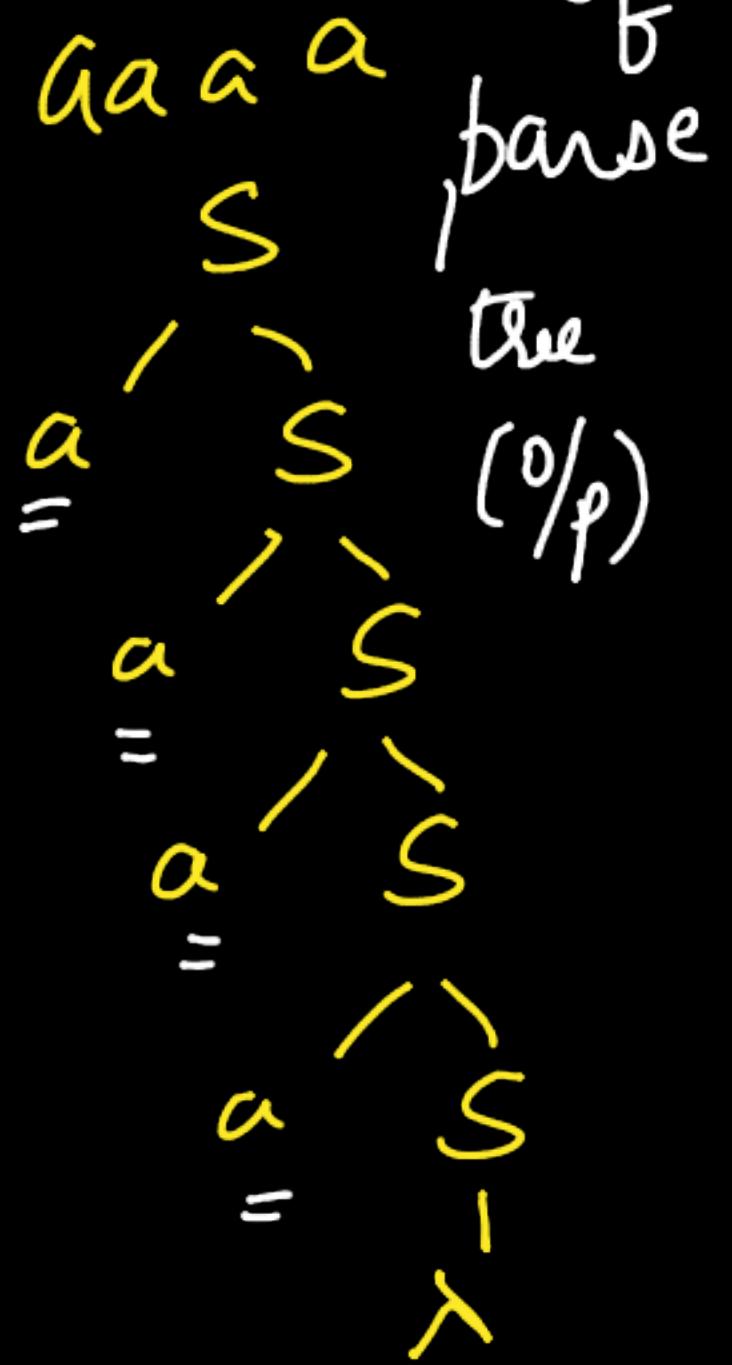
$a^*$

Regular Grammar

$S \rightarrow aS \mid \lambda$  or  $S \rightarrow \lambda$

or

$S \rightarrow Sa \mid \lambda$



7)  $\{\lambda, ab, abab, ababab, \dots\}$

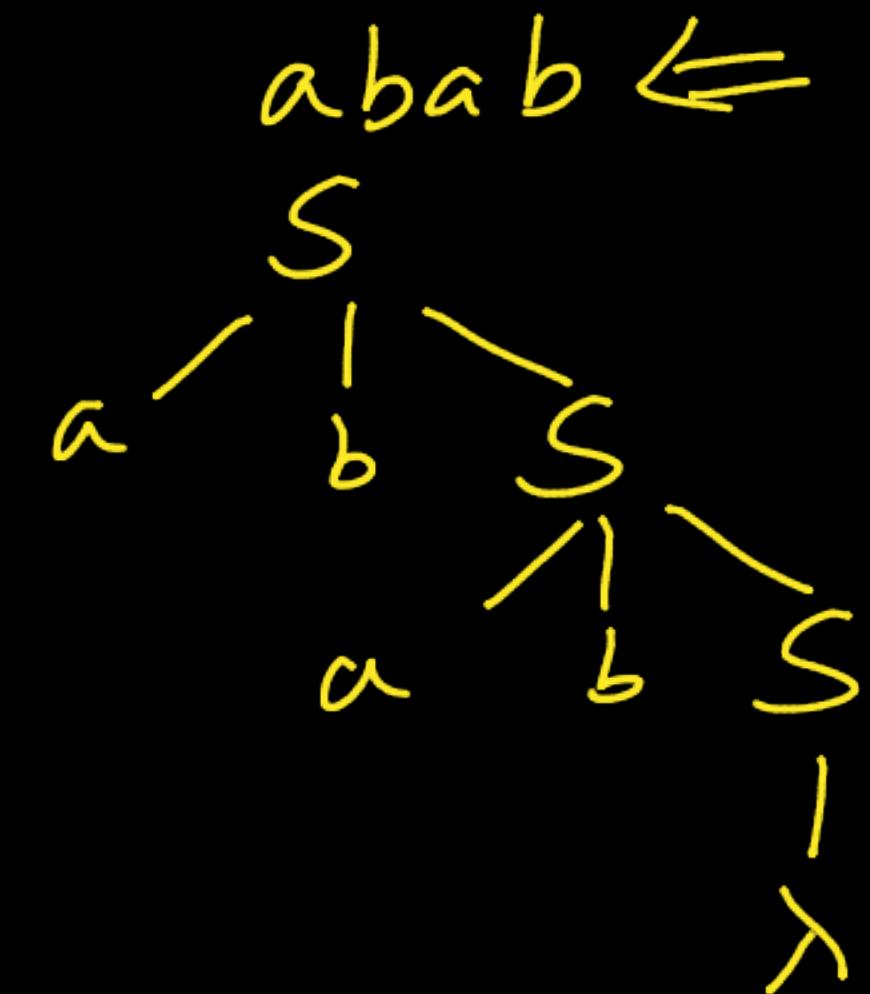
$(ab)^*$

Regular Grammar

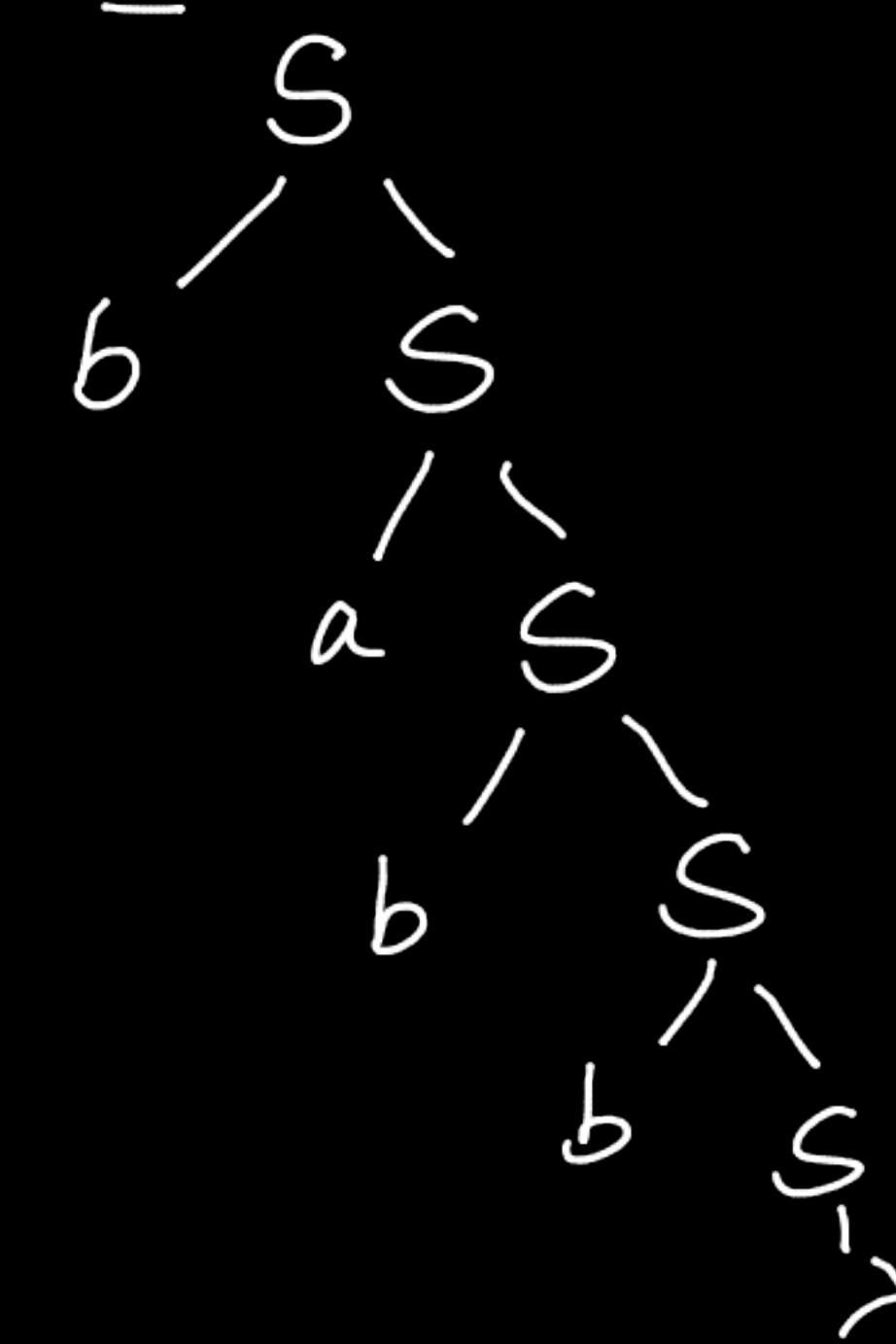
$S \rightarrow abS \mid \lambda$

or

$S \rightarrow Sab \mid \lambda$



Construct Regular Grammar for the given language descriptions:

Language	Regex	Regular Grammar
8) $\{ w, w \in \{a, b\}^*\}$	$(a+b)^*$	$S \rightarrow aS \mid bS \mid \lambda$ ✓ $=ba\underline{a}\underline{b} = \in L(G)$  <p>All rules Left linear form</p> <p>or</p> $S \rightarrow Sa \mid Sb \mid \lambda$

$$S \rightarrow aS \mid Sb \mid \lambda$$

All  
rules

LLG

You cannot have a  
mix

RG

/

\

All  
rules

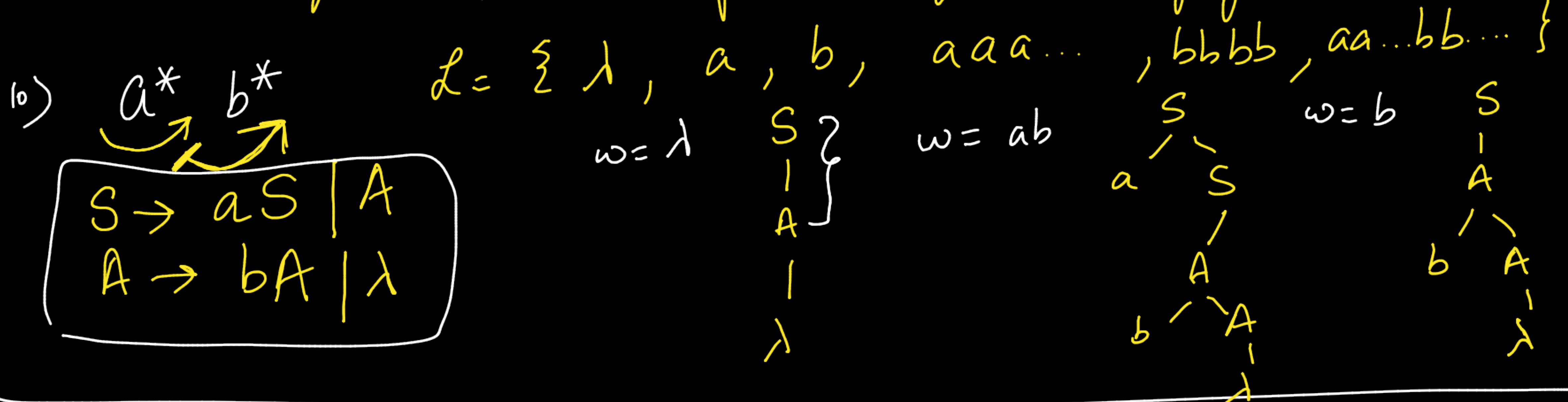
RLG

Not the  
right way

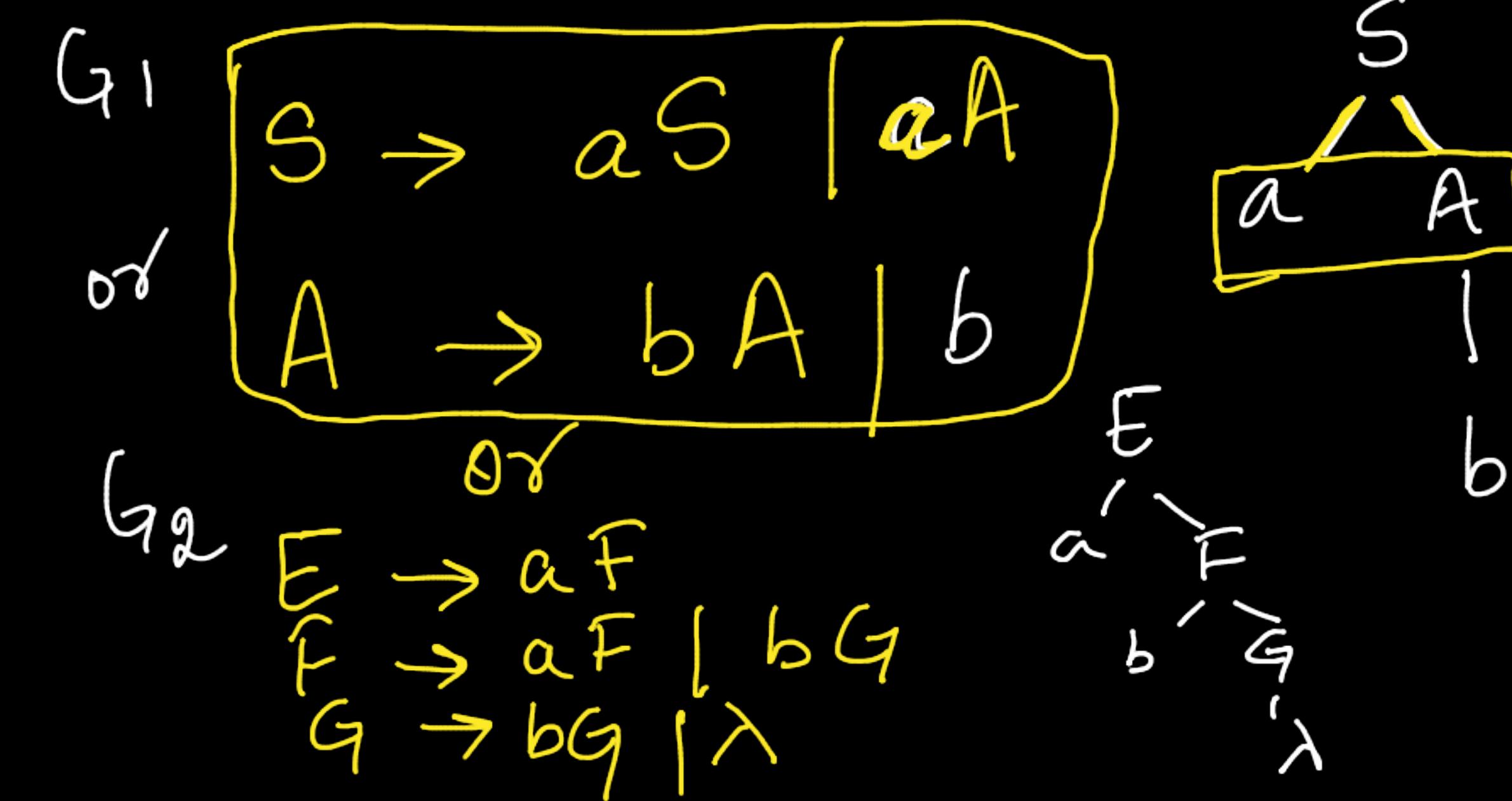
Construct regular grammar for the given language :-

Language	Regex	Regular Grammar
q) $\{ w, w \in \{ab, ba\}^*\}$	$(ab + ba)^*$	$S \rightarrow abS \mid baS \mid \lambda$

Construct regular grammar for the given language



11)  $a^n b^m, n, m \geq 1$   
minimal string  
 $\{ab, a\dots b\dots\}$



Construct regular grammar for the following language:

Language over  $\{a, b\}^*$  where the string must contain all final states at least one 'a'.

$$\overbrace{b^*}^{\text{RE}} \overbrace{a}^{\text{RE}} \overbrace{(a+b)^*}^{\text{RE}}$$

RG

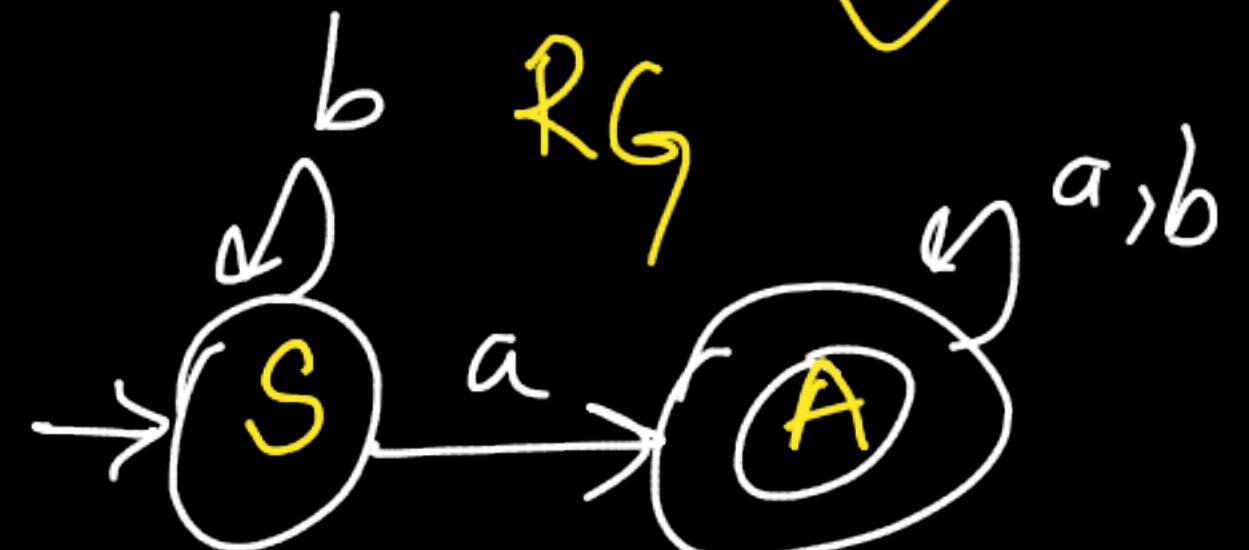
$$S \rightarrow bS \mid aA$$

$$S \mid a \mid A$$

$$A \rightarrow aA \mid bA \mid \lambda$$

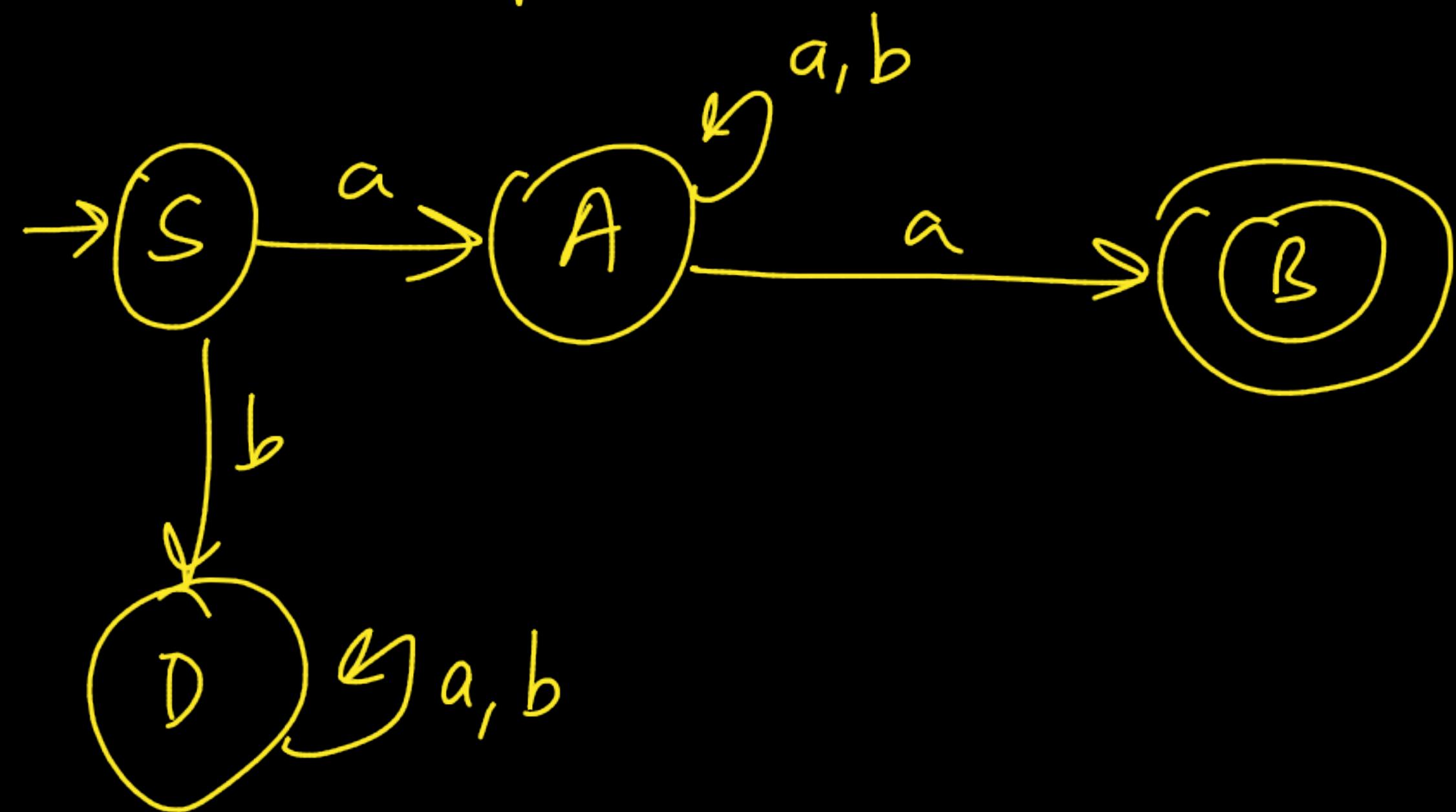
$\lambda$

FA  
↓  
all final states generate  $\lambda$



$$S \rightarrow bS \mid aA$$
$$A \rightarrow aA \mid bA \mid \lambda$$

Convert given Finite automata to Regular Grammar :-



Ignore the Dead State !

Although it's reachable from S but it doesn't generate anything  
(end)

$$\begin{aligned} S &\rightarrow aA \quad \cancel{| bD} \\ A &\rightarrow aA \mid bA \mid aB \\ B &\rightarrow \lambda \\ D &\rightarrow \cancel{aD} \mid \cancel{bD} \end{aligned}$$

S  
|  
b D  
|  
a D  
|  
b D  
|  
a D  
|  
b D  
|  
D