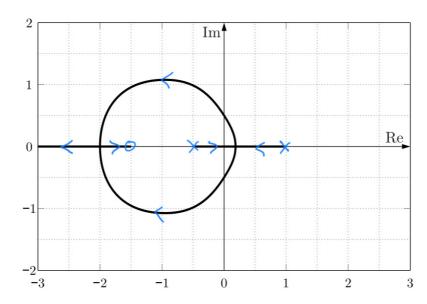
## Exam 02-Control Engineering

Monday, 10. February 2020 15:45

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a



b From figure,
$$8N_{1} = -1.5$$

$$2P_{1} = -0.5$$

$$8P_{2} = 1$$
Now,
$$(N_{0}(2) = 1 \cdot (2 + 1.5) \cdot (2 - 1)$$

$$= \frac{1}{2} \left\{ \frac{28 + 3}{(8 + 0.5)} \cdot (8 - 1) \right\}$$

$$= \frac{1}{2} \left\{ \frac{(2 + 0.5) + (2 - 1) + 3.5}{(8 + 0.5)} \cdot (8 - 1) \right\}$$

$$= \frac{1}{2} \left\{ \frac{1}{8 - 1} + \frac{1}{8 + 0.5} \cdot (8 + 0.5) \cdot (8 - 1) \right\}$$

$$= \frac{1}{2} \left\{ \frac{-1}{1 - 2} + \frac{2}{1 + 22} + \frac{-7}{3} \cdot (e^{-1} - e^{-1}) \right\}$$

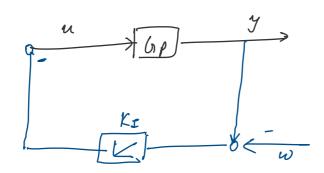
$$= \frac{1}{2} \left\{ \frac{1}{1 - 2} + \frac{2}{1 + 22} + \frac{-7}{3} \cdot (e^{-1} - e^{-1}) \right\}$$

$$= \frac{1}{2} \left\{ e^{-1} \cdot (\frac{10}{3}) + e^{-\frac{1}{2}} \cdot (-\frac{1}{3}) \right\}$$

$$= \frac{1}{2} \left\{ e^{-1} \cdot (\frac{10}{3}) + e^{-\frac{1}{2}} \cdot (-\frac{1}{3}) \right\}$$

$$g(t) = \frac{5}{3}e^{-\frac{3}{2}}e^{-\frac{3}{2}}$$





behaviour. . . It is preferable for stationary accuracy

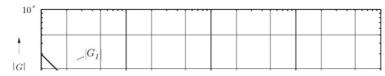
From Bode plot:  $\alpha_{PD} > \alpha_{I}$ ..  $G_{PD}(jw)$  is preferable w.r.t phase margin

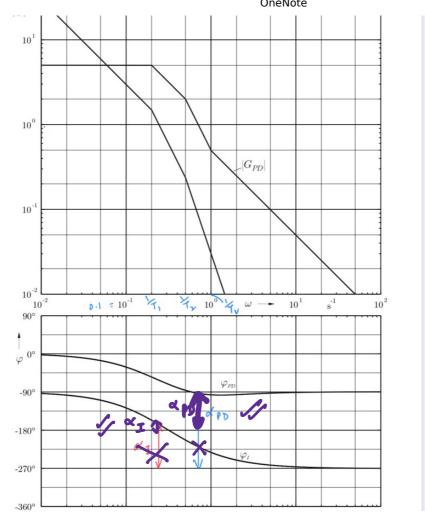
ic) : Greneral form of 
$$G_p = \frac{1}{T_1 T_2 \ell^2 + (T_2 + T_1) \ell^2 + 1}$$

with slope changes of -1 at  $\frac{1}{T_1}$  and  $\frac{1}{T_2}$ 

From BODE Plot and company it w/ given  $(r_0(j\omega))$   $\frac{1}{T_1} = 0.2 \text{ see}^{-1} > T_1 = 5 \text{ see}$   $\frac{1}{T_2} = 0.5 \text{ see}^{-1} > T_2 = 2 \text{ see}$ 

a, = 
$$(T_1 + T_2) = 7$$
 see





 $G(S) = \frac{G_2 G_3}{1 + G_2 G_3}$ 

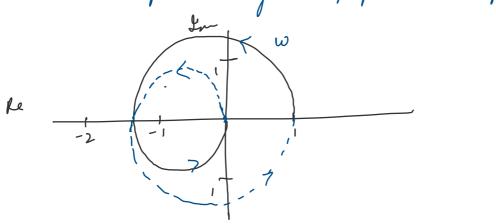
hou, Gols)=G2 G3.

Now,

. On and One both have one pole in

suight half plane.

Total pol in suight half plane = 2 = p



. 2 rocends anti-clockwise about -1 ... m = -2, no of sevolutions of L'associated -1 (opposite mathematically five direction i.e. clockwill)

Now,  $m = n - \rho$   $n = m + \rho = -2 + 2 = 0$ 

:. there are 0 7lms in N(s) inside C ( gright & halfplane)

On 0 no. of poles of  $G_{12}(S)$  in right 8 half plane.

On  $G_{2}(S)$  is stable if  $n \rightarrow 0$ 

in our case (n(s) is stable

4)

18 I-A1 =0

For characteristic eq

$$|3+1| > | = 0$$

$$|-1| 3-3|$$

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b) 
$$s_1 = -1 + j$$
  $s_2 = -1 - j$ 

Characterdie eq<sup>n</sup>

$$(8^{-8},) (8^{-8}z) = 0$$

$$\{8 - (-1+j)\} \{8 + 1+j\} = 0$$

$$\{8 + 1 - j\} \{8 + 1 + j\} = 0$$

$$(8+1) - j^{2} = 0$$

$$5^{2} + 1 + 28 + 1 = 0$$

$$5^{2} + 28 + 2 = 0$$

$$0$$

Now, For given value of 
$$V = -k \times X$$

$$\begin{array}{cccc}
\dot{X} &= & A \times & + & B - k \times X \\
&= & (A - B k) \times X \\
&= & \left\{ \begin{pmatrix} -1 & -5 \\ 1 & 3 \end{pmatrix} - \begin{pmatrix} k, & k_2 \\ 0 & 0 \end{pmatrix} \right\} \times \\
&= & \left\{ \begin{pmatrix} -1 - k_1 & -5 - k_2 \\ 1 & 3 \end{pmatrix} - \begin{pmatrix} k & k_2 \\ 0 & 0 \end{pmatrix} \right\} \times \\
&= & \left\{ \begin{pmatrix} -1 - k_1 & -5 - k_2 \\ 1 & 3 \end{pmatrix} - \begin{pmatrix} k & k_2 \\ 0 & 0 \end{pmatrix} \right\} \times \\
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&= & \begin{pmatrix} -1 - k_1 & -5 \\ 1 & 3 \end{pmatrix} \times \\
&= & \begin{pmatrix} -1 - k_1 & -5 \\ 1 & 3$$

Now, Charactuste eg "
$$\begin{vmatrix} s & J - A_k | = 0 \\ s + 1 + k, + 5 + k_2 \\ -1 & s - 3 \end{vmatrix} = 0$$

$$s^{2} + s(1+k_{1}) - 3s - 3(1+k_{1}) + (5+k_{2}) = 0$$
  
 $s^{2} + s(k_{1} - 2) + (2 - 3k_{1} + k_{2}) = 0$ 

Composing eq (1) and (2)
$$2 = k_1 - 2$$

$$4 = k_1$$

$$2 - 3 \cdot 4 + k_2 = 2$$

$$k_2 = 12$$