

Appendix C: Monte Carlo simulation for feature selection

To find the most relevant features for each research question composite scores were constructed using principal component analysis (PCA). PCA tries to identify the space in which the data points approximately lie (Jolliffe, 2011). It computes new variables called principle components which are obtained from linear combinations of the original features. By doing so, the goal of the PCA is to extract the most important features (Abdi & Williams, 2010). To find how many principal components should be computed a subset of the training data, which included the sliding windows and additional features for consumer sentiment and the value of Y_t , was used to compute the proportion of variance explained.

The principal components with the highest weights were then used in the Monte Carlo simulation. Monte Carlo is a simulation method that relies on repeated random sampling. The algorithm creates subsets of randomly chosen features and divides the objects in each subset in train and test sets (Komorowski, 2015). For each combination of features 10-fold cross validation was performed and the Mean Squared Errors (MSE) were computed on the test set. The combination of features with the lowest test MSE score were the features considered most relevant to each research question.

C1. MSE per feature combination

Experiment	Target value	Features	MSE
1 & 3.1	$\text{change}_{bpt+3;bpt+2}$	$CS_{max}, CS_{min}, CS_{median}, CSCQD$	1.228 E-4
2	rs_{t+3}	$CS_{max}, CS_{min}, CSCQD, CS_{t+1}$	8.811 E-2
3.2	$\text{change}_{cit+3;cit+2}$	$CS_{max}, CS_{min}, CSCR, ci_t$	4.255 E-2
4.1	$\text{change}_{cst+3;cst+2}$	$bp_{min}, bp_{CR}, bp_{CQD}, cs_t$	17.577
4.2	$\text{change}_{cst+3;cst+2}$	rs_{max}, rs_{min}, rs_t	17.637
4.3	$\text{change}_{cst+3;cst+2}$	$ci_{\tilde{x}}, ci_{\sigma^2}, ci_{t+2}, cs_t$	17.456

C2. Predictions with feature selection

Experiment 1

Part	Model	MSE train	MSE test	Parameters
I	Baseline	2.721	8.675	-
	Elastic Net	1.230	3.754	$\alpha = 0.2121425$; $\lambda = 0.001205047$
	SVM	1.227	3.770	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; support vectors: 2591
	Random Forest	0.993	3.440	$ntree = 5000$; $importance = TRUE$
II	Baseline	2.135	5.826	-
	Elastic Net	1.021	2.892	$\alpha = 0.006356115$; $\lambda = 0.006691759$
	SVM	0.983	2.830	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; support vectors: 316
	Random Forest	0.809	2.680	$ntree = 5000$; $importance = TRUE$

Experiment 2

Part	Model	Acc. train	Acc. test	F1 train	F1 test	Parameters
I	Baseline	0.985	0.985	0.991	0.991	-
	SVM	0.902	0.895	0.944	0.940	$method = C\text{-}classification$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; support vectors: 1302
	PART	0.940	0.935	0.966	0.963	-
	Bagging	0.941	0.937	0.966	0.964	-
	RandomForest	0.941	0.938	0.966	0.964	$ntree = 5000$; $importance = TRUE$
	k-NN	0.940	0.938	0.965	0.964	$method = knn$; $trControl = cv$ (number: 5); $k = 5$
II	Baseline	0.894	0.901	0.0217	-	-
	SVM	0.946	0.951	-	-	$method = C\text{-}classification$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; support vectors: 105
	PART	0.955	0.947	0.345	0.286	-
	Bagging	0.957	0.951	0.400	0.364	-
	RandomForest	0.957	0.951	0.400	0.364	$ntree = 5000$; $importance = TRUE$
	k-NN	0.953	0.947	0.286	0.211	$method = knn$; $trControl = cv$ (number: 5); $k = 7$

Experiment 3.1

Cl.	Model	MSE train	MSE test	Parameters
1	Baseline	3.034	52.600	-
	Elastic Net	1.469	25.782	$\alpha = 0.06905604$; $\lambda = 0.00229073$
	SVM	1.476	26.220	method = <i>eps-regression</i> ; kernel = <i>radial</i> ; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; support vectors: 616
	Random Forest	1.202	23.097	<i>ntree</i> = 5000; <i>importance</i> = <i>TRUE</i>
2	Baseline	7.705	15.539	-
	Elastic Net	3.722	5.899	$\alpha = 0.2426044$; $\lambda = 6.790757$
	SVM	3.688	5.794	method = <i>eps-regression</i> ; kernel = <i>radial</i> ; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; support vectors: 253
	Random Forest	2.391	6.544	<i>ntree</i> = 5000; <i>importance</i> = <i>TRUE</i>
3	Baseline	0.967	0.977	-
	Elastic Net	0.444	0.437	$\alpha = 0.1274343$; $\lambda = 0.001274972$
	SVM	0.453	0.455	method = <i>eps-regression</i> ; kernel = <i>radial</i> ; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; support vectors: 1285
	Random Forest	0.226	0.307	<i>ntree</i> = 5000; <i>importance</i> = <i>TRUE</i>
4	Baseline	3.354	0.345	-
	Elastic Net	1.251	0.152	$\alpha = 0.2827089$; $\lambda = 0.002055782$
	SVM	1.236	0.149	method = <i>eps-regression</i> ; kernel = <i>radial</i> ; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; support vectors: 532
	Random Forest	0.953	0.185	<i>ntree</i> = 5000; <i>importance</i> = <i>TRUE</i>

Experiment 3.2

Cl.	Model	MSE train	MSE test	Parameters
1	Baseline	0.126	0.070	-
	Elastic Net	0.042	0.024	$\alpha = 0.3073374$; $\lambda = 0.00926526$
	SVM	0.041	0.023	$method = eps-regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; $support\ vectors: 1357$
	Random Forest	0.023	0.023	$ntree = 5000$; $importance = TRUE$
2	Baseline	0.144	0.134	-
	Elastic Net	0.057	0.046	$\alpha = 0.8686318$; $\lambda = 0.008117249$
	SVM	0.055	0.045	$method = eps-regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; $support\ vectors: 541$
	Random Forest	0.023	0.049	$ntree = 5000$; $importance = TRUE$
3	Baseline	0.124	0.187	-
	Elastic Net	0.046	0.070	$\alpha = 0.4247356$; $\lambda = 0.002565703$
	SVM	0.043	0.070	$method = eps-regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; $support\ vectors: 2188$
	Random Forest	0.025	0.072	$ntree = 5000$; $importance = TRUE$
4	Baseline	0.088	0.122	-
	Elastic Net	0.029	0.042	$\alpha = 0.5303174$; $\lambda = 0.007506053$
	SVM	0.029	0.042	$method = eps-regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; $support\ vectors: 1098$
	Random Forest	0.014	0.044	$ntree = 5000$; $importance = TRUE$

Experiment 4

Prt.	Model	MSE train	MSE test	Parameters
1	Baseline	35.284	35.291	-
	Elastic Net	17.567	17.614	$\alpha = 0.1561852$; $\lambda = 0.1073471$
	SVM	17.620	17.919	$method = eps-regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; $support\ vectors: 5185$
	Random Forest	4.578	10.578	$ntree = 5000$; $importance = TRUE$
2	Baseline	35.284	35.291	-
	Elastic Net	17.623	17.743	$\alpha = 0.09788889$; $\lambda = 0.005984826$
	SVM	17.660	17.795	$method = eps-regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; $support\ vectors: 5329$
	Random Forest	17.661	17.711	$ntree = 5000$; $importance = TRUE$
3	Baseline	35.284	35.291	-
	Elastic Net	17.432	17.526	$\alpha = 0.2203477$; $\lambda = 0.003436149$
	SVM	16.919	17.433	$method = eps-regression$; $kernel = radial$; $C = 1$; $\gamma = 0.25$; $\epsilon = 0.1$; $support\ vectors: 5235$
	Random Forest	2.742	11.486	$ntree = 5000$; $importance = TRUE$

Appendix D: States in state clusters

Cluster	Train set	Test set
1. Financial cluster	Connecticut, Maine, Maryland, Massachusetts, New Hampshire, New Jersey, New York, Rhode Island, Vermont, Virginia	California
2. Oil cluster	Louisiana, North Dakota, Oklahoma, Texas	Alaska, Wyoming, New Mexico
3. Manufacturing cluster	Alabama, Illinois, Indiana, Iowa, Kansas, Kentucky, Michigan, Minnesota, Mississippi, Missouri, Ohio, Pennsylvania, South Carolina, Tennessee, West Virginia, Wisconsin	Washington, Montana
4. Mixed economy cluster	Arkansas, Delaware, Florida, Georgia, Hawaii, Nebraska, North Carolina, South Dakota	Oregon, Idaho, Colorado, Nevada, Arizona, Utah

Appendix E: Multiple Imputation

Variable	Imputation method
sixmonthsout	Logistic regression
Oil price	Bayesian linear regression
Oil state	PMM
Agriculture	PMM
Mining	PMM
Construction	PMM
Manifacutring	PMM
Durable goods	PMM
Nondurable goods	PMM
Current coincident index	PMM

Appendix F: Results of experiment 1

Experiment 1.1

RQ1.1		RQ1.1		RQ1.1	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	0.00230	CS_t	7.460	CS_t	71.211
CS_t	0.00018	CS_{t+1}	2.219	CS_{t+1}	81.072
CS_{t+1}	0.00006	CS_{t+2}	1.492	CS_{t+2}	79.080
CS_{t+2}	0.00004	CS_{max}	2.403	CS_{max}	65.682
CS_{min}	0.00006	CS_{min}	-	CS_{min}	67.426
CS_{σ^2}	0.00001	CS_{σ^2}	40.009	CS_{σ^2}	98.415
$CS_{\bar{x}}$	0.00092	$CS_{\bar{x}}$	4.208	$CS_{\bar{x}}$	73.329
$CS_{\bar{x}}$	0.00011	CS_{median}	9.682	CS_{median}	73.616
CS_{median}	0.00023	CS_{CR}	7.670	CS_{CR}	85.855
CS_{CR}	-0.00019	CS_{CQD}	12.276	CS_{CQD}	89.923
CS_{CQD}	-0.00029	bp_t	100.000	bp_t	70.350
bp_t	0.00229	<i>Elastic Net feature importance</i>		<i>Random Forest feature importance</i>	
<i>Elastic Net coefficients</i>		RQ1.1		RQ1.1	

Experiment 1.2

RQ1.2		RQ1.2		RQ1.2	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	-0.00012	CS_t	-	CS_t	30.655
CS_t	-	CS_{t+1}	-	CS_{t+1}	20.624
CS_{t+1}	-	CS_{t+2}	-	CS_{t+2}	46.361
CS_{t+2}	-	CS_{max}	-	CS_{max}	21.741
CS_{max}	-	CS_{min}	-	CS_{min}	31.887
CS_{min}	-	CS_{σ^2}	-	CS_{σ^2}	28.235
CS_{σ^2}	-	$CS_{\bar{x}}$	-	$CS_{\bar{x}}$	22.810
$CS_{\bar{x}}$	-	CS_{median}	-	CS_{median}	23.275
CS_{median}	-	CS_{CR}	-	CS_{CR}	25.958
CS_{CR}	-	CS_{CQD}	-	CS_{CQD}	28.758
CS_{CQD}	-	bp_t	-	bp_t	-6.333
bp_t	-	<i>Elastic Net feature importance</i>		<i>Random Forest feature importance</i>	
<i>Elastic Net coefficients</i>		RQ1.2		RQ1.2	

Appendix G: Results of experiment 2

Experiment 2.1

RQ2.1		RQ2.1	
Feature	Importance	Feature	Importance
CS_t	0	CS_t	14.733
CS_{t+1}	0	CS_{t+1}	17.830
CS_{t+2}	0	CS_{t+2}	17.781
CS_{max}	0	CS_{max}	547.502
CS_{min}	1	CS_{min}	571.022
CS_{σ^2}	0	CS_{σ^2}	17.582
$CS_{\bar{x}}$	0	$CS_{\bar{x}}$	532.179
CS_{median}	1	CS_{median}	476.344
CS_{CR}	1	CS_{CR}	18.150
CS_{CQD}	0	CS_{CQD}	22.460
rst	1	rst	1277.657
<i>582PART feature importance RQ2.1</i>		<i>Bagging feature importance RQ2.1</i>	

RQ2.1		RQ2.1	
Feature	Importance	Feature	Importance
CS_t	28.899	CS_t	56.60
CS_{t+1}	29.911	CS_{t+1}	59.05
CS_{t+2}	28.133	CS_{t+2}	60.53
CS_{max}	107.108	CS_{max}	61.21
CS_{min}	138.206	CS_{min}	61.89
CS_{σ^2}	18.001	CS_{σ^2}	-
$CS_{\bar{x}}$	88.650	$CS_{\bar{x}}$	62.54
CS_{median}	59.538	CS_{median}	62.13
CS_{CR}	20.517	CS_{CR}	27.07
CS_{CQD}	19.236	CS_{CQD}	27.43
rst	773.681	rst	100.00
<i>Random Forest feature importance RQ2.1</i>		<i>k-NN feature importance RQ2.1</i>	

Experiment 2.2

RQ2.2

Feature	Importance
CS_t	0
CS_{t+1}	0
CS_{t+2}	0
CS_{max}	0
CS_{min}	1
CS_{σ^2}	0
$CS_{\bar{x}}$	0
CS_{median}	1
CS_{CR}	1
CS_{CQD}	0
rst	0

PART feature importance RQ2.2

RQ2.2

Feature	Importance
CS_t	11.020
CS_{t+1}	12.405
CS_{t+2}	9.641
CS_{max}	16.998
CS_{min}	16.407
CS_{σ^2}	15.325
$CS_{\bar{x}}$	7.106
CS_{median}	5.312
CS_{CR}	18.763
CS_{CQD}	17.881
rst	-

Bagging feature importance RQ2.2

RQ2.2

Feature	Importance
CS_t	2.389
CS_{t+1}	2.677
CS_{t+2}	2.320
CS_{max}	2.548
CS_{min}	2.948
CS_{σ^2}	5.193
$CS_{\bar{x}}$	2.647
CS_{median}	2.839
CS_{CR}	5.472
CS_{CQD}	5.569
rst	-

Random Forest feature importance RQ2.2

RQ2.2

Feature	Importance
CS_t	82.26
CS_{t+1}	78.36
CS_{t+2}	80.73
CS_{max}	85.33
CS_{min}	93.34
CS_{σ^2}	79.34
$CS_{\bar{x}}$	87.90
CS_{median}	85.19
CS_{CR}	99.08
CS_{CQD}	100.00
rst	-

k-NN feature importance RQ2.2

Appendix H: Results of experiment 3

Experiment 3.1

RQ3.1		RQ3.1		RQ3.1	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	0.00248	CS_t	-	CS_t	39.455
CS_t	-	CS_{t+1}	-	CS_{t+1}	51.794
CS_{t+1}	-	CS_{t+2}	16.475	CS_{t+2}	53.928
CS_{t+2}	0.00042	CS_{max}	-	CS_{max}	41.509
CS_{max}	-	CS_{min}	-	CS_{min}	39.952
CS_{min}	-	CS_{σ^2}	7.922	CS_{σ^2}	44.923
CS_{σ^2}	0.00020	$CS_{\bar{x}}$	-	$CS_{\bar{x}}$	44.720
$CS_{\bar{x}}$	-	CS_{median}	-	CS_{median}	43.813
CS_{median}	-	CS_{CR}	-	CS_{CR}	42.749
CS_{CR}	-	CS_{CQD}	-	CS_{CQD}	45.261
CS_{CQD}	-	bp_t	100.000	bp_t	52.540
bp_t	0.00256	<i>Elastic Net feature importance</i>		<i>Random Forest feature importance</i>	
<i>Elastic Net coefficients</i>		<i>RQ3.1 - Cluster 1</i>		<i>RQ3.1 - Cluster 1</i>	
<i>RQ3.1 - Cluster 1</i>					
RQ3.1		RQ3.1		RQ3.1	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	0.00388	CS_t	7.463	CS_t	36.917
CS_t	0.00033	CS_{t+1}	6.301	CS_{t+1}	32.903
CS_{t+1}	0.00028	CS_{t+2}	-	CS_{t+2}	36.041
CS_{t+2}	-	CS_{max}	5.215	CS_{max}	36.177
CS_{max}	0.00023	CS_{min}	-	CS_{min}	34.714
CS_{min}	-	CS_{σ^2}	52.475	CS_{σ^2}	34.773
CS_{σ^2}	0.00232	$CS_{\bar{x}}$	3.374	$CS_{\bar{x}}$	41.640
$CS_{\bar{x}}$	0.00015	CS_{median}	8.107	CS_{median}	34.401
CS_{median}	0.00036	CS_{CR}	5.114	CS_{CR}	35.380
CS_{CR}	-0.00022	CS_{CQD}	8.248	CS_{CQD}	36.010
CS_{CQD}	-0.00037	bp_t	100.000	bp_t	3.209
bp_t	0.00443	<i>Elastic Net feature importance</i>		<i>Random Forest feature importance</i>	
<i>Elastic Net coefficients</i>		<i>RQ3.1 - Cluster 2</i>		<i>RQ3.1 - Cluster 2</i>	
<i>RQ3.1 - Cluster 2</i>					

RQ3.1

Feature	Coefficient
<i>Intercept</i>	0.00201
CS_t	0.00014
CS_{t+1}	0.00009
CS_{t+2}	-
CS_{max}	0.00008
CS_{min}	0.00005
CS_{σ^2}	0.00004
$CS_{\bar{x}}$	0.00008
CS_{median}	0.00010
CS_{CR}	-
CS_{CQD}	-
bp_t	0.00056

Elastic Net coefficients
RQ3.1 - Cluster 3

RQ3.1

Feature	Importance
CS_t	24.026
CS_{t+1}	16.636
CS_{t+2}	-
CS_{max}	14.143
CS_{min}	9.507
CS_{σ^2}	6.811
$CS_{\bar{x}}$	14.405
CS_{median}	18.528
CS_{CR}	-
CS_{CQD}	-
bp_t	100.000

Elastic Net feature importance
RQ3.1 - Cluster 3

RQ3.1

Feature	Importance
CS_t	89.817
CS_{t+1}	86.980
CS_{t+2}	88.329
CS_{max}	72.722
CS_{min}	80.380
CS_{σ^2}	120.125
$CS_{\bar{x}}$	83.692
CS_{median}	80.356
CS_{CR}	113.053
CS_{CQD}	117.660
bp_t	117.701

Random Forest feature importance
RQ3.1 - Cluster 3

RQ3.1

Feature	Coefficient
<i>Intercept</i>	0.00187
CS_t	0.00016
CS_{t+1}	0.00019
CS_{t+2}	0.00003
CS_{max}	0.00015
CS_{min}	0.00002
CS_{σ^2}	0.00059
$CS_{\bar{x}}$	0.00014
CS_{median}	0.00027
CS_{CR}	-
CS_{CQD}	-
bp_t	0.00147

Elastic Net coefficients
RQ3.1 - Cluster 4

RQ3.1

Feature	Importance
CS_t	10.913
CS_{t+1}	13.026
CS_{t+2}	2.117
CS_{max}	9.991
CS_{min}	1.079
CS_{σ^2}	40.204
$CS_{\bar{x}}$	9.674
CS_{median}	18.041
CS_{CR}	-
CS_{CQD}	-
bp_t	100.000

Elastic Net feature importance
RQ3.1 - Cluster 4

RQ3.1

Feature	Importance
CS_t	25.177
CS_{t+1}	32.803
CS_{t+2}	30.940
CS_{max}	22.138
CS_{min}	28.151
CS_{σ^2}	36.063
$CS_{\bar{x}}$	22.662
CS_{median}	27.743
CS_{CR}	30.797
CS_{CQD}	33.887
bp_t	9.663

Random Forest feature importance
RQ3.1 - Cluster 4

Experiment 3.2

RQ3.2		RQ3.2		RQ3.2	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	0.00126	CS_t	-	CS_t	39.896
CS_t	-	CS_{t+1}	-	CS_{t+1}	36.362
CS_{t+1}	-	CS_{t+2}	-	CS_{t+2}	46.558
CS_{t+2}	-	CS_{max}	-	CS_{max}	36.385
CS_{min}	-	CS_{min}	-	CS_{min}	37.466
CS_{σ^2}	-	CS_{σ^2}	-	CS_{σ^2}	37.892
$CS_{\bar{x}}$	-	$CS_{\bar{x}}$	-	$CS_{\bar{x}}$	40.229
CS_{median}	-	CS_{median}	-	CS_{median}	39.030
CS_{CR}	-	CS_{CR}	-	CS_{CR}	36.579
CS_{CQD}	-	CS_{CQD}	-	CS_{CQD}	34.459
ci_t	-0.01594	ci_t	100.000	ci_t	58.357
<i>Elastic Net coefficients</i>		<i>Elastic Net feature importance</i>		<i>Random Forest feature importance</i>	
<i>RQ3.2 - Cluster 1</i>		<i>RQ3.2 - Cluster 1</i>		<i>RQ3.2 - Cluster 1</i>	
RQ3.2		RQ3.2		RQ3.2	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	-0.00041	CS_t	-	CS_t	24.080
CS_t	-	CS_{t+1}	59.145	CS_{t+1}	23.418
CS_{t+1}	-0.04367	CS_{t+2}	51.377	CS_{t+2}	21.541
CS_{t+2}	0.03794	CS_{max}	2.594	CS_{max}	19.196
CS_{max}	0.00192	CS_{min}	87.059	CS_{min}	18.977
CS_{min}	0.06428	CS_{σ^2}	79.630	CS_{σ^2}	22.545
CS_{σ^2}	0.05880	$CS_{\bar{x}}$	-	$CS_{\bar{x}}$	22.346
$CS_{\bar{x}}$	-	CS_{median}	100.000	CS_{median}	22.986
CS_{median}	-0.07384	CS_{CR}	66.944	CS_{CR}	22.543
CS_{CR}	-0.04943	CS_{CQD}	-	CS_{CQD}	23.462
CS_{CQD}	-	ci_t	46.740	ci_t	19.543
ci_t	-0.03451	<i>Elastic Net feature importance</i>		<i>Random Forest feature importance</i>	
<i>Elastic Net coefficients</i>		<i>RQ3.2 - Cluster 2</i>		<i>RQ3.2 - Cluster 2</i>	
<i>RQ3.2 - Cluster 2</i>					

RQ3.2

Feature	Coefficient
<i>Intercept</i>	0.00018
CS_t	-0.00203
CS_{t+1}	-0.00104
CS_{t+2}	-
CS_{max}	-
CS_{min}	-
CS_{σ^2}	0.05051
$CS_{\bar{x}}$	-
CS_{median}	-
CS_{CR}	-
CS_{CQD}	-0.05214
ci_t	-0.04133

Elastic Net coefficients
RQ3.2 - Cluster 3

RQ3.2

Feature	Importance
CS_t	3.895
CS_{t+1}	1.994
CS_{t+2}	-
CS_{max}	-
CS_{min}	-
CS_{σ^2}	96.871
$CS_{\bar{x}}$	-
CS_{median}	-
CS_{CR}	-
CS_{CQD}	100.000
ci_t	79.270

Elastic Net feature importance
RQ3.2 - Cluster 3

RQ3.2

Feature	Importance
CS_t	62.331
CS_{t+1}	53.597
CS_{t+2}	61.540
CS_{max}	62.584
CS_{min}	58.320
CS_{σ^2}	42.867
$CS_{\bar{x}}$	63.918
CS_{median}	60.370
CS_{CR}	52.421
CS_{CQD}	52.225
ci_t	131.339

Random Forest feature importance
RQ3.2 - Cluster 3

RQ3.2

Feature	Coefficient
<i>Intercept</i>	0.00060
CS_t	-
CS_{t+1}	0.00265
CS_{t+2}	-
CS_{max}	-
CS_{min}	-
CS_{σ^2}	-
$CS_{\bar{x}}$	-
CS_{median}	-
CS_{CR}	-
CS_{CQD}	-
ci_t	-0.01978

Elastic Net coefficients
RQ3.2 - Cluster 4

RQ3.2

Feature	Importance
CS_t	-
CS_{t+1}	-
CS_{t+2}	13.37
CS_{max}	-
CS_{min}	-
CS_{σ^2}	-
$CS_{\bar{x}}$	-
CS_{median}	-
CS_{CR}	-
CS_{CQD}	-
ci_t	100.000

Elastic Net feature importance
RQ3.2 - Cluster 4

RQ3.2

Feature	Importance
CS_t	55.299
CS_{t+1}	57.078
CS_{t+2}	46.606
CS_{max}	49.063
CS_{min}	52.805
CS_{σ^2}	50.079
$CS_{\bar{x}}$	52.304
CS_{median}	56.769
CS_{CR}	48.915
CS_{CQD}	48.120
ci_t	53.226

Random Forest feature importance
RQ3.2 - Cluster 4

Appendix I: Experiment 3.1 with 70/30 partitioning

Experiment 3.1 (10^{-4})

Cl.	Model	MSE train		MSE test		Parameters
1.	Baseline	6.382	-	8.053	-	-
	Elastic Net	2.820	(55.81%)	4.382	(45.56%)	$\alpha = 0.2954246$; $\lambda = 0.001006681$
	SVM	3.226	(49.45%)	4.572	(43.23%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 468$
	Random Forest	0.890	(86.05%)	0.433	(94.62%)	$ntree = 5000$; $importance = TRUE$
2.	Baseline	15.766	-	4.126	-	-
	Elastic Net	5.470	(65.31%)	1.928	(53.27%)	$\alpha = 0.1503563$; $\lambda = 0.001694307$
	SVM	5.524	(64.96%)	2.065	(49.95%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 233$
	Random Forest	2.472	(84.32%)	2.915	(29.35%)	$ntree = 5000$; $importance = TRUE$
3.	Baseline	0.963	-	0.846	-	-
	Elastic Net	0.433	(55.04%)	0.405	(52.13%)	$\alpha = 0.02349696$; $\lambda = 0.001108925$
	SVM	0.456	(52.65%)	0.431	(49.05%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 1001$
	Random Forest	0.112	(88.37%)	0.201	(76.24%)	$ntree = 5000$; $importance = TRUE$
4.	Baseline	2.843	-	0.696	-	-
	Elastic Net	0.920	(67.64%)	0.320	(54.02%)	$\alpha = 0.1480629$; $\lambda = 0.001153624$
	SVM	0.928	(67.36%)	0.329	(52.73%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 731$
	Random Forest	0.479	(83.15%)	0.331	(52.44%)	$ntree = 5000$; $importance = TRUE$

Appendix J: Experiment 3.2 with 70/30 partitioning

Experiment 3.2

Cl.	Model	MSE train		MSE test		Parameters
1.	Baseline	0.113	-	0.095	-	-
	Elastic Net	0.041	(63.72%)	0.040	(57.89%)	$\alpha = 0.03792504$; $\lambda = 0.009532534$
	SVM	0.040	(64.60%)	0.040	(57.89%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 1063$
	Random Forest	0.021	(81.41%)	0.043	(54.74%)	$ntree = 5000$; $importance = TRUE$
2.	Baseline	0.119	-	0.159	-	-
	Elastic Net	0.046	(61.34%)	0.069	(56.60%)	$\alpha = 0.8567382$; $\lambda = 0.008085317$
	SVM	0.044	(63.03%)	0.070	(55.97%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 694$
	Random Forest	0.020	(83.19%)	0.074	(53.46%)	$ntree = 5000$; $importance = TRUE$
3.	Baseline	0.124	-	0.095	-	-
	Elastic Net	0.050	(59.68%)	0.044	(53.68%)	$\alpha = 0.07239164$; $\lambda = 0.003337746$
	SVM	0.047	(62.10%)	0.043	(54.74%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 1684$
	Random Forest	0.026	(79.03%)	0.044	(53.68%)	$ntree = 5000$; $importance = TRUE$
4.	Baseline	0.090	-	0.076	-	-
	Elastic Net	0.034	(62.22%)	0.035	(53.95%)	$\alpha = 0.01827431$; $\lambda = 0.006731816$
	SVM	0.033	(63.33%)	0.035	(53.95%)	$method = eps\text{-}regression$; $kernel = radial$; $C = 1$; $\gamma = 0.09090909$; $\epsilon = 0.1$; $support\ vectors: 1306$
	Random Forest	0.019	(78.89%)	0.037	(51.32%)	$ntree = 5000$; $importance = TRUE$

Appendix K: Results of experiment 4

Experiment 4.1

RQ4.1		RQ4.1		RQ4.1	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	0.03949	bp_t	-	bp_t	93.033
bp_t	-	bp_{t+1}	0.948	bp_{t+1}	93.779
bp_{t+1}	0.00289	bp_{t+2}	0.741	bp_{t+2}	90.071
bp_{t+2}	0.00226	bp_{max}	-	bp_{max}	87.340
bp_{max}	-	bp_{min}	-	bp_{min}	87.703
bp_{min}	-	bp_{σ^2}	-	bp_{σ^2}	142.421
bp_{σ^2}	-	$bp_{\bar{x}}$	-	$bp_{\bar{x}}$	93.767
$bp_{\bar{x}}$	-	bp_{median}	-	bp_{median}	94.672
bp_{median}	-	bp_{CR}	19.050	bp_{CR}	102.711
bp_{CR}	-0.05817	bp_{CQD}	2.268	bp_{CQD}	109.283
bp_{CQD}	0.00692	cs_t	100.000	cs_t	258.137
cs_t	-0.30534	<i>Elastic Net feature importance RQ4.1</i>		<i>Random Forest feature importance RQ4.1</i>	
<i>Elastic Net coefficients RQ4.1</i>					

Experiment 4.2

RQ4.2		RQ4.2		RQ4.2	
Feature	Coefficient	Feature	Importance	Feature	Importance
<i>Intercept</i>	0.03949	<i>rs_t</i>	65.032	<i>rs_t</i>	35.366
<i>rs_t</i>	0.35703	<i>rs_{t+1}</i>	0.452	<i>rs_{t+1}</i>	14.968
<i>rs_{t+1}</i>	0.00248	<i>rs_{t+2}</i>	100.000	<i>rs_{t+2}</i>	39.025
<i>rs_{t+2}</i>	-0.54901	<i>rs_{max}</i>	-	<i>rs_{max}</i>	25.026
<i>rs_{max}</i>	-	<i>rs_{min}</i>	-	<i>rs_{min}</i>	18.867
<i>rs_{min}</i>	-	<i>rs_{σ²}</i>	18.699	<i>rs_{σ²}</i>	34.862
<i>rs_{σ²}</i>	-0.10267	<i>rs_{̄x}</i>	-	<i>rs_{̄x}</i>	28.787
<i>rs_{̄x}</i>	-	<i>rs_{median}</i>	2.973	<i>rs_{median}</i>	14.901
<i>rs_{median}</i>	0.01632	<i>rs_{SCR}</i>	11.952	<i>rs_{SCR}</i>	34.796
<i>rs_{SCR}</i>	-0.06562	<i>rs_{CQD}</i>	-	<i>rs_{CQD}</i>	24.016
<i>rs_{CQD}</i>	-	<i>cs_t</i>	82.639	<i>cs_t</i>	77.292
<i>cs_t</i>	-0.45370	<i>Elastic Net feature importance RQ4.2</i>		<i>Random Forest feature importance RQ4.2</i>	
<i>Elastic Net coefficients RQ4.2</i>					

Experiment 4.3

RQ4.3

Feature	Coefficient
<i>Intercept</i>	0.03949
ci_t	-0.33595
ci_{t+1}	-0.16706
ci_{t+2}	0.58840
ci_{max}	-0.00005
ci_{min}	0.01761
ci_{σ^2}	0.13447
$ci_{\bar{x}}$	-
ci_{median}	-0.01800
ci_{CR}	-0.02495
ci_{CQD}	0.01279
cs_t	-0.38059

Elastic Net coefficients
RQ4.3

RQ4.3

Feature	Importance
ci_t	57.096
ci_{t+1}	28.393
ci_{t+2}	100.000
ci_{max}	0.0084
ci_{min}	2.992
ci_{σ^2}	22.854
$ci_{\bar{x}}$	-
ci_{median}	3.059
ci_{CR}	4.241
ci_{CQD}	2.174
cs_t	64.682

Elastic Net feature
importance RQ4.3

RQ4.3

Feature	Importance
ci_t	116.425
ci_{t+1}	107.359
ci_{t+2}	115.332
ci_{max}	99.967
ci_{min}	111.285
ci_{σ^2}	108.662
$ci_{\bar{x}}$	100.335
ci_{median}	107.319
ci_{CR}	105.841
ci_{CQD}	103.137
cs_t	220.702

Random Forest feature importance
RQ4.3

Appendix L: Sliding window approach

	Window 1	Window 2	Window 3	Window 4	Window 5
Year	2005 to 2018	2005 to 2018	2005 to 2018	2005 to 2017	2005 to 2017
Month 1	January	February	March	April	May
Month 2	February	March	April	May	June
Month 3	March	April	May	June	July
	Window 6	Window 7	Window 8	Window 9	Window 10
Year	2005 to 2017	2005 to 2017	2005 to 2017	2005 to 2017	2005 to 2017
Month 1	June	July	August	September	October
Month 2	July	August	September	October	November
Month 3	August	September	October	November	December

Appendix M – Software and packages

This appendix provides a global overview of the packages that were used in the experimental procedure. All analyses and experiments were implemented using R Studio.

mice. The “mice” package is used to perform multiple imputation. The *mice::quickpred()* function is used to quick select predictors from the data. The *mincor* parameter that specifies the minimum threshold is set to 0.25. The *mice::mice* is used to replace the missing values. The parameter of the number of imputations *m* is set to 1 with the number of iterations *maxit* set to 1 too. The seed is set to ‘314159’. *Mice::complete* extracts the subset of complete cases. **TSPred.** “TSPred” is used for the sliding window method. *TSPred::slidingWindows* extracts all possible subsequences of a time series. The parameter *swSize* is set to 3. **zoo.** The “zoo” package is used for the extraction of features from the sliding window data. With *zoo::rollapply* the functions for the construction of the features is applied to rolling margins of the data. The parameter *width* is set to 3. **stats.** The “stats” package is used to perform PCA with the use of *stats::prcomp*. This function performs a principal components analysis on the data and returns the weights of the components. **glmnet.** “glmnet” is used to create an OLS model for the Monte Carlo simulation. The parameter *intercept* is set to TRUE, the parameters *alpha* and *lambda* to 0 and *standardize* to FALSE. **e1071.** The package “e1071” is used for training SVM. The parameters of *e1071::svm* are presented in the results section. **RWeka.** *RWeka::PART* is used for the PART algorithm. **ipred.** *ipred::bagging* is used to implement the bagging classification model. **randomForest.** The “randomForest” package is used for the implementation of the Random Forest algorithm. The parameters of the function *randomForest::randomForest* are listed in the results section. **caret.** “caret” is used to fit Elastic Net and k-NN to the data. *caret::confusionMatrix* is used for calculating cross-tabulations of the observed and predicted classes. *caret::createDataPartition()* is used to partition the data for experiment 3. **ggplot2, tidyr.** Packages used for creating visualizations of the data.