

$$1) f(x, y, z) = \sum m(1, 3, 7)$$

	x	y	z	s
0	0	0	0	0
1	0	0	1	1
2	0	1	0	0
3	0	1	1	1
4	1	0	0	0
5	1	0	1	0
6	1	1	0	0
7	1	1	1	1

$$\bar{x}\bar{y}z + \bar{x}yz + x\bar{y}z$$

xy \ z	0	1
00		1
01		1
11		1
10		

$$\bar{x}z + yz$$

$$b) f(x, y, z) = \sum m(0, 4, 6)$$

	x	y	z	s
0	0	0	0	1
1	0	0	1	0
2	0	1	0	0
3	0	1	1	0
4	1	0	0	1
5	1	0	1	0
6	1	1	0	1
7	1	1	1	0

$$\bar{x}\bar{y}\bar{z} + x\bar{y}\bar{z} + x\bar{y}z$$

xy \ z	0	1
00	1	
01		
11	1	
10	1	

$$x\bar{z} + \bar{y}\bar{z}$$

c)  $f(x, y, z) = \sum m(0, 1, 3, 5)$

x	y	z	s
0	0	0	1
1	0	1	1
2	0	1	0
3	0	1	1
4	1	0	0
5	1	0	1
6	1	1	0
7	1	1	1

$$\bar{x}\bar{y}\bar{z} + \bar{x}\bar{y}z + \bar{x}yz + x\bar{y}z$$

z 0 1

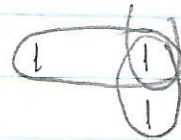
xy

00

01

11

10



$$\bar{x}\bar{y} + \bar{x}z + \bar{y}z$$

d)  $f(x, y, z) = \sum m(2, 3, 6, 7)$

x	y	z	s
0	0	0	0
1	0	1	0
2	0	1	1
3	0	1	1
4	1	0	0
5	1	0	1
6	1	1	1
7	1	1	1

$$\bar{x}y\bar{z} + \bar{x}yz + x\bar{y}\bar{z} + xyz$$

z 0 1

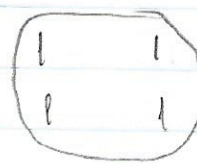
xy

00

01

11

10



$$s = y$$

$$e) f(x, y, z) = \sum m(0, 3, 4, 5)$$

	x	y	z	s
0	0	0	0	1
1	0	0	1	0
2	0	1	0	0
3	0	1	1	1
4	1	0	0	1
5	1	0	1	1
6	1	1	0	0
7	1	1	1	0

$$\bar{x}\bar{y}\bar{z} + \bar{x}yz + x\bar{y}\bar{z} + x\bar{y}z$$

$$z \quad 0 \quad 1$$

$$xy \quad 00 \quad 1$$

$$01 \quad 1$$

$$11$$

$$10$$

$$11$$

$$\bar{y}\bar{z} + x\bar{y} + \bar{x}yz$$

2)

$$F(x, y, z) = \prod M(1, 3, 7)$$

	x	y	z	s
0	0	0	0	1
1	0	0	1	0
2	0	1	0	1
3	0	1	1	0
4	1	0	0	1
5	1	0	1	1
6	1	1	0	1
7	1	1	1	0

$$\bar{x}\bar{y}\bar{z}$$

$$(x+y+\bar{z}) \cdot (x+\bar{y}+\bar{z}) \cdot (\bar{x}+\bar{y}+\bar{z})$$

$$z \quad 1 \quad 0$$

$$xy$$

$$00$$

$$01$$

$$11$$

$$10$$

$$00$$

$$01$$

$$11$$

$$(x+\bar{z}) \cdot (\bar{y}+\bar{z})$$

b)  $F(x, y, z) = \prod M(3, 5, 7)$

	x	y	z	s	
0	0	0	0	1	$(x\bar{y} + \bar{z}) \cdot (\bar{x} + y + \bar{z}) \cdot (\bar{x} + \bar{y} + \bar{z})$
1	0	0	1	1	
2	0	1	0	1	z 0 1
3	0	1	1	0	xy
4	1	0	0	1	00
5	1	0	1	0	01
6	1	1	0	1	11
7	1	1	1	0	00



$(\bar{y} + \bar{z}) \cdot (\bar{x} + \bar{z})$

c)  $F(x, y, z) = \prod M(1, 2, 3, 5)$

	x	y	z	s	
0	0	0	0	1	
1	0	0	1	0	$(x + y + \bar{z}) \cdot (x + \bar{y} + z) \cdot (x + \bar{y} + \bar{z})$
2	0	1	0	0	$(\bar{x} + y + \bar{z})$
3	0	1	1	0	z 0 1
4	0	0	0	1	xy
5	1	0	1	0	00
6	1	0	0	1	01
7	1	1	1	1	11



$(x + \bar{y}) \cdot (\bar{x} + \bar{z}) \cdot (\bar{y} + \bar{z})$



$$d) F(x, y, z) = \prod M(0, 2, 3, 7)$$

	x	y	z	s	
0	0	0	0	0	$(x+y+z) \cdot (x+\bar{y}+z) \cdot$
1	0	0	1	1	$(x+\bar{y}+\bar{z}) \cdot (\bar{x}+\bar{y}+\bar{z})$
2	0	1	0	0	
3	0	1	1	0	z
4	1	0	0	1	xy 0 1
5	1	0	1	1	00 (0)
6	1	1	0	1	01 (0) (0)
7	1	1	1	0	11 (0)
					10

$$(x+z) \cdot (\bar{y} \cdot \bar{z})$$

$$e) F(x, y, z) = \prod M(2, 3, 5, 7)$$

	x	y	z	s	
0	0	0	0	0	$(x+\bar{y}+z) \cdot (x+\bar{y}+\bar{z}) \cdot (\bar{x}+y+\bar{z}) \cdot$
1	0	0	1	1	$(\bar{x}+\bar{y}+\bar{z})$
2	0	1	0	0	
3	0	1	1	0	z 0 1
4	1	0	0	1	xy 1 0
5	1	0	1	0	00
6	1	1	0	1	01 (0) (0)
7	1	1	1	0	11 (0)
					10

$$(x+\bar{y}) \cdot (\bar{x}+\bar{z})$$

3)

a)  $f(x, y, w, z) = \sum m(1, 2, 3, 7, 13, 15)$

	x	y	w	z	s	
0	0	0	0	0	0	
1	0	0	0	1	1	-
2	0	0	1	0	1	-
3	0	0	1	1	1	-
4	0	1	0	0	0	
5	0	1	0	1	0	
6	0	1	1	0	0	
7	0	1	1	1	1	
8	1	0	0	0	0	
9	1	0	0	1	0	
10	1	0	1	0	0	
11	1	0	1	1	0	
12	1	1	0	0	0	
13	1	1	0	1	1	
14	1	1	1	0	0	
15	1	1	1	1	1	

wz

xy	00	01	11	10
00		1	1	
01		1		
10			1	
11				

$\bar{x}\bar{y}z + \bar{x}wz + ywz + x\bar{y}z + \bar{x}yz + x\bar{y}z$

$$b) f(x, y, w, z) = \sum m(0, 4, 3, 5, 6, 7)$$

	x	y	w	z	s
0	0	0	0	0	1
1	0	0	0	1	0
2	0	0	1	0	0
3	0	0	1	1	1
4	0	1	0	0	1
5	0	1	0	1	1
6	0	1	1	0	1
7	0	1	1	1	1
8	1	0	0	0	0
9	1	0	0	1	0
10	1	0	1	0	0
11	1	0	1	1	0
12	1	1	0	0	0
13	1	1	0	1	0
14	1	1	1	0	0
15	1	1	1	1	0

xy \ wz	00	01	11	10
00	1	0	1	0
01	1	1	1	1
11				
10				

$$\bar{x}\bar{w}\bar{z} + \bar{x}y\bar{w} + \bar{x}wz + \bar{x}yw$$

c)  $f(x, y, w, z) = \sum m(0, 1, 2, 3, 5, 8, 9, 13)$

	x	y	w	z	s
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	1
3	0	0	1	1	1
4	0	1	0	0	0
5	0	1	0	1	1
6	0	1	1	0	0
7	0	1	1	1	0
8	1	0	0	0	1
9	1	0	0	1	1
10	1	0	1	0	0
11	1	0	1	1	0
12	1	1	0	0	0
13	1	1	0	1	1
14	1	1	1	0	0
15	1	1	1	1	0

xy \ wz	00	01	11	10
00	1	1	1	1
01		1		
11		1		
10	1	1		

$$\bar{x}\bar{y} + y\bar{w}z + x\bar{y}\bar{w}$$

~~$\bar{x}\bar{y} + y\bar{w}z$~~



$$d) f(x, y, w, z) = \sum m(2, 4, 6, 10, 12, 14)$$

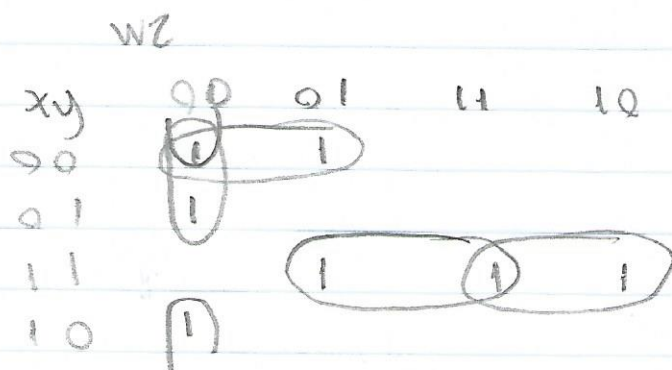
	wz		
xy	00	01	11
00			1
01	1		
11	1		
10			

1
1
1
1

	x	y	w	z	s	$w\bar{z} + y\bar{w}\bar{z}$
0	0	0	0	0	0	
1	0	0	0	1	0	
2	0	0	1	0	1	-
3	0	0	1	1	0	
4	0	1	0	0	1	-
5	0	1	1	1	0	
6	0	1	1	0	1	-
7	0	1	1	1	0	
8	1	0	0	0	0	
9	1	0	0	1	0	
10	1	0	1	0	1	-
11	1	0	1	1	0	
12	1	1	0	0	1	-
13	1	1	0	1	0	
14	1	1	1	0	1	
15	1	1	1	1	0	

$$e) f(x, y, w, z) = \sum m(0, 1, 4, 8, 13, 14, 15)$$

	x	y	w	z	S
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	0
3	0	0	1	1	0
4	0	1	0	0	1
5	0	1	0	1	0
6	0	1	1	0	0
7	0	1	1	1	0
8	1	0	0	0	1
9	1	0	0	1	0
10	1	0	1	0	0
11	1	0	1	1	0
12	1	1	0	0	0
13	1	1	0	1	1
14	1	1	1	0	1
15	1	1	1	1	1



$$\bar{x}\bar{w}\bar{z} + \bar{y}\bar{w}\bar{z} + x\bar{y}\bar{w} + xyz + xyw$$

4)  $F(x, y, w, z) = \sum m(2, 6, 8, 13)$

	x	y	w	z	S
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	0
3	0	0	1	1	1
4	0	1	0	0	1
5	0	1	0	1	1
6	0	1	0	1	0
7	0	1	1	1	1
8	1	0	0	0	0
9	1	0	0	1	1
10	1	0	1	0	1
11	1	0	1	1	1
12	1	1	0	0	1
13	1	1	0	1	0
14	1	1	1	0	1
15	1	1	1	1	1

	wz	00	01	11	10
xy	00	00	01	11	10
00					0
01			0		
11			0		
10		0			

~~$ywz + ywz + ywz$~~   $(\bar{y} + w + \bar{z}) \cdot (y + w + z) \cdot (x + y + z)$

b)  $f(x, y, w, z) = \prod M(4, 9, 11, 12)$

	x	y	w	z	s
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	1
3	0	0	1	1	1
4	0	1	0	0	0
5	0	1	0	1	1
6	0	1	1	0	1
7	0	1	1	1	1
8	1	0	0	0	1
9	1	0	0	1	0
10	1	0	1	0	1
11	1	0	1	1	0
12	1	1	0	0	0
13	1	1	0	1	1
14	1	1	1	0	1
15	1	1	1	1	1

xy	00	01	11	10
00				
01	0			
11	0			
10		0	0	

$(\bar{y} + w + z) \cdot (\bar{x} + y + z)$

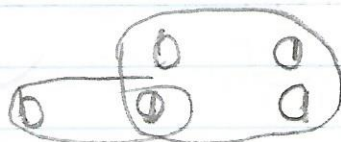


$$c) f(x, y, w, z) = \Pi M(8, 9, 11, 13, 15)$$

	x	y	w	z	s
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	1
3	0	0	1	1	1
4	0	1	0	0	1
5	0	1	0	1	1
6	0	1	1	0	1
7	0	1	1	1	1
8	1	0	0	0	0-
9	1	0	0	1	0-
10	1	0	1	0	1
11	1	0	1	1	0-
12	1	1	0	0	1
13	1	1	0	1	0-
14	1	1	1	0	1
15	1	1	1	1	0

wz

xy	00	01	11	10
00				
01				
11				
10				



$$(\bar{x} + \bar{z}) \cdot (x + y + z)$$

d)  $f(x, y, w, z) = \prod M(1, 3, 5, 6, 13, 14)$

	x	y	w	z	s
0	0	0	0	0	1
1	0	0	0	1	0
2	0	0	1	0	1
3	0	0	1	1	0
4	0	1	0	0	1
5	0	1	0	1	0
6	0	1	1	0	0
7	0	1	1	1	1
8	1	0	0	0	1
9	1	0	0	1	1
10	1	0	1	0	1
11	1	0	1	1	1
12	1	1	0	0	1
13	1	1	0	1	0
14	1	1	1	0	0
15	1	1	1	1	1

	xy	00	01	11	10
wz	00	0	0		
	01	0	0		0
	11				0
	10				

$$(x + y + \bar{z}) \cdot (\bar{y} + w + \bar{z}) \cdot (\bar{y} + \bar{w} + z)$$

e)  $f(x, y, w, z) = \prod M(4, 6, 7, 8, 12)$

	x	y	w	z	S
0	0	0	0	0	1
1	0	0	0	1	1
2	0	0	1	0	1
3	0	0	1	1	1
4	0	1	0	0	0
5	0	1	0	1	1
6	0	1	1	0	0
7	0	1	1	1	0
8	1	0	0	0	0
9	1	0	0	1	1
10	1	0	1	0	0
11	1	0	1	1	1
12	1	1	0	0	0
13	1	1	0	1	1
14	1	1	1	0	1
15	1	1	1	1	1

xy	wz	10	11
00			
01	1		1
11			1
10	1		1

$$(x + \bar{y} + z) \cdot (\bar{x} + y + z) \cdot (x + \bar{y} + \bar{w}) \cdot (\bar{x} + \bar{w} + z)$$

4)

$$a) (\overline{x+y}) \cdot (\overline{x \cdot y}) + (\overline{yz+x})$$

	x	y	z	s
0	0	0	0	0
1	0	0	1	0
2	0	1	0	0
3	0	1	1	0
4	1	0	0	1
5	1	0	1	1
6	1	1	0	1
7	1	1	1	0

z 0 1

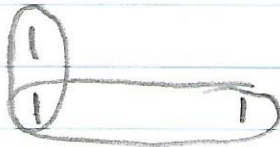
xy

00

01

11

10

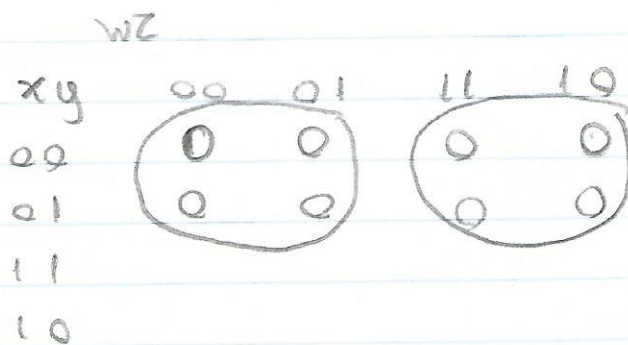


$$(x \cdot \bar{z}) + (x \bar{y})$$



5)

	x	y	w	z	s
0	0	0	0	0	0
1	0	0	0	1	0
2	0	0	1	0	0
3	0	0	1	1	0
4	0	1	0	0	0
5	0	1	0	1	0
6	0	1	1	0	0
7	0	1	1	1	0
8	1	0	0	0	1
9	1	0	0	1	1
10	1	0	1	0	1
11	1	0	1	1	1
12	1	1	0	0	1
13	1	1	0	1	1
14	1	1	1	0	1
15	1	1	1	1	0



$$(x + w) \cdot (x + \bar{w})$$