

Dear learners,

You are required to:

Write equation no 3 and 4 as illustrated in class

Add a YouTube link to your markdown file

Then remember to submit your work for review.

Thank you

3. (a) (i) Define what it means to say that a square matrix with real entries is **diagonalisable** over  $\mathbb{R}$

(ii) Show that if  $A$  is a square matrix with real entries and  $\mathbf{u}$  and  $\mathbf{v}$  are eigen values of  $A$  corresponding to different eigenvalues, then  $\mathbf{u}$  and  $\mathbf{v}$  are linearly independent.

(b) (i) Consider  $2 \times 2$  real square matrix

$$A = \begin{pmatrix} a & a \\ b & d \end{pmatrix}$$

Show tha  $A$  has atleast one real eigenvalue,, and that if  $a \neq d$  or  $b \neq 0$ , then it has two sitinct real eigen values. Deduce that  $A$  is diagonalisable.

(ii) Determine the values of  $\alpha$  and  $\beta$  for which the real matrix

$$A = \begin{pmatrix} 1 & \alpha \\ \beta & 1 \end{pmatrix}$$

is diagonalisable.

(iii) Determine the values of  $\alpha$  and  $\beta$  for which the real matrix

$$A = \begin{pmatrix} a & b \\ c & a \end{pmatrix}$$

is diagonalisable.

4. Let  $\mathbf{u}$  and  $\mathbf{w}$  be vectors in  $\mathbb{R}^3$

(a) (7 points) (i) Prove that  $\mathbf{u}$ ,  $\mathbf{v}$  and  $\mathbf{w}$  are linearly independent if and only if  $\mathbf{u} \cdot (\mathbf{v} \wedge \mathbf{v}) \neq 0$ .

✓ 1s completed at 9:29 AM



(C)(6 points) Suppose that  $\mathbf{u}$ ,  $\mathbf{v}$  and  $\mathbf{w}$  are linearly independent and that

$$\mathbf{r} = \alpha \mathbf{u} + \beta \mathbf{v} + \gamma \mathbf{w}.$$

Find the coefficients  $\alpha$ ,  $\beta$  and  $\gamma$  such that

$$\mathbf{r} = \alpha \mathbf{v} \wedge \mathbf{w} + \beta \mathbf{w} \wedge \mathbf{u} + \gamma \mathbf{u} \wedge \mathbf{v}.$$

[Youtube link](#)