

Answer

The formula is an action whose meaning is a Boolean-valued mapping on pairs of states. It is true iff its meaning maps all pairs of states to TRUE. Its meaning is computed as follows:

$$\begin{aligned} & \llbracket (A \equiv B) \Rightarrow ((\text{ENABLED } A) \equiv (\text{ENABLED } B)) \rrbracket (\langle s, t \rangle) \\ & \equiv (\llbracket A \rrbracket (\langle s, t \rangle) \equiv \llbracket B \rrbracket (\langle s, t \rangle)) \Rightarrow \\ & \quad (\llbracket \text{ENABLED } A \rrbracket (\langle s, t \rangle) \equiv \llbracket \text{ENABLED } B \rrbracket (\langle s, t \rangle)) \\ & \equiv (\llbracket A \rrbracket (\langle s, t \rangle) \equiv \llbracket B \rrbracket (\langle s, t \rangle)) \Rightarrow \\ & \quad ((\exists t : \llbracket A \rrbracket (\langle s, t \rangle)) \equiv (\exists t : \llbracket B \rrbracket (\langle s, t \rangle))) \end{aligned}$$

Note that in the last formula, the left-hand side depends on t but the right-hand side doesn't. Let A be the action FALSE and find an action B and states s and t such that $\llbracket B \rrbracket (\langle s, t \rangle)$ equals FALSE and $\exists t : \llbracket B \rrbracket (\langle s, t \rangle)$ equals TRUE.

To show that the rule isn't valid, you need to need to remember what it means for state predicates and actions to be true on a behavior and use the definition of \models .