

# Compilers

## Semantic Analysis

LEIC

FEUP-FCUP

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# This lecture

Semantic analysis

Scopes

Symbol table

Type Systems

Type Checking

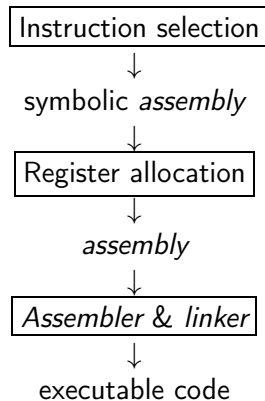
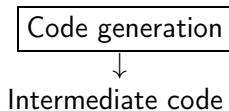
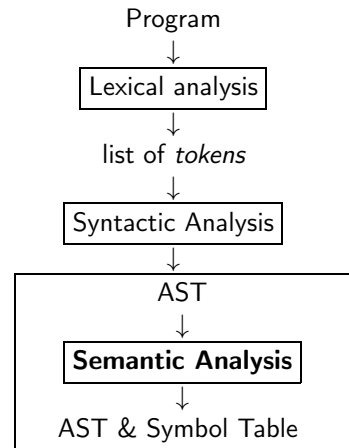
- Expressions

- Type Declarations

- Type Checking for Functions

Extras

# Compiler



# This lecture

## Semantic analysis

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Context dependent static verifications.

Examples:

- ▶ undeclared variables
- ▶ type checking
- ▶ type inference

## Semantics analysis (cont.)

- ▶ This can be done while parsing takes place
- ▶ Usually it is done after parsing - AST is the input of semantic analysis
- ▶ Needs information about **identifiers** (variables, function names, etc.) stored in a **symbol table**
- ▶ The symbol table is also used later for code generation

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- ▶ Variable declarations have a **limited scope**
  - ▶ e.g. we may declare a local variable with the same name as a global variable



# Example

Scopes.

```
int i, j;  
int f(int size)  
{ char i, temp;  
  ...  
  { double j;  
    ...  
  }  
  ...  
  { char * j;  
    ...  
  }  
}
```

# Example

Scopes.

```
int i, j;           // global: i, j
int f(int size)     // global: f
{ char i, temp;
  ...
  { double j;
    ...
  }
  ...
  { char * j;
    ...
  }
}
```

# Example

Scopes.

```
int i, j;           // global: i, j
int f(int size)     // global: f
{ char i, temp;     // function: size, i, temp
  ...              // new declaration for i
  { double j;
    ...
  }
  ...
  { char * j;
    ...
  }
}
```

# Example

Scopes.

```
int i, j;           // global: i, j
int f(int size)     // global: f
{ char i, temp;     // function: size, i, temp
  ...              // new declaration for i
  { double j;       // block 1: j hides the global declaration
    ...
  }
  ...
  { char * j;
    ...
  }
}
```

# Example

Scopes.

```
int i, j;           // global: i, j
int f(int size)     // global: f
{ char i, temp;     // function: size, i, temp
  ...               // new declaration for i
  { double j;       // block 1: j hides the global declaration
    ...
  }
  ...
  { char * j;       // block 2: j hides the global declaration
    ...
  }
}
```

**Lexical scope** (also known as *static scope*) each use of a variable corresponds to the **closest declaration** in the AST

- ▶ Used in Pascal, C, C++, Java, Haskell, SML, etc.
- ▶ Dynamic scope: first versions of LISP

# Function scopes

- ▶ Functions may be used in any scope:
  - ▶ Pascal, Modula e Ada,...
  - ▶ Scheme, ML, Haskell,...
  - ▶ JavaScript, Ruby, Python,...
- ▶ C and Java limit the scope for functions to the global scope (C) or classes (C++/Java)

## Function scopes (cont.)

```
// Pascal
function E(x: real): real;
    function F(y: real): real;
    begin
        F := x + y
    end;
begin
    E := F(3) + F(4)
end;
```

```
-- Haskell
e :: Float -> Float
e x = f 3 + f 4
    where f y = x + y
```

```
// GNU C (not standard C)
float e(float x) {
    float f(float y) {
        return x + y;
    }
    return f(3) + f(4);
}
```



## Function scopes (cont.)

GCC (extention to the *standard*):

```
float E(float x)
{
    float F(float y)
    {
        return x + y;
    }
    return F(3) + F(4);
}
```

## Function scopes (cont.)

### Advantages of functions inside functions

- ▶ local auxiliary functions
- ▶ simplifies the control flow
- ▶ enable the use of local auxiliary functions instead of cycles

## Function scopes (cont.)

Example: test primes (C vs. Haskell).

```
int is_prime(int n) {  
    int d = 2;  
    if(n<=1)  
        return FALSE;  
    while(d*d <= n) {  
        if (n%d == 0)  
            return FALSE;  
        d++;  
    }  
    return TRUE;  
}
```

```
isPrime :: Int -> Bool  
isPrime n = n>1 && checkDivs 2  
    where checkDivs d  
            | n`mod`d==0 = False  
            | d*d <= n    = checkDivs (d+1)  
            | otherwise  = True
```

## Function scopes (cont.)

Non-standard C extension:

```
int is_prime(int n) {  
    int checkDivs() {  
        int d = 2;  
        while(d*d <= n) {  
            if(n%d == 0)  
                return FALSE;  
        }  
        return TRUE;  
    }  
    return n>1 && checkDivs();  
}
```

# This lecture

Semantic analysis

Scopes

Symbol table

Type Systems

Type Checking

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# Symbol table

- ▶ Relates **identifiers** with semantic information **informação**; some examples:
  - ▶ *values* of variables (interpreters);
  - ▶ *types*;
  - ▶ *location* (registers or memory during code generation)

# Name spaces

- ▶ Multiple name spaces
  - ▶ e.g. in Haskell we may have the same name for a *type* and a *constructor*

```
data Expr = Int Int | Add Expr Expr
```

- ▶ **modules** or *packages* usually have different name spaces
- ▶ We may use **different symbol tables** for different name spaces
- ▶ Or: use a global symbol table and **prefixes**

```
Prelude.lookup
```

```
Data.Map.lookup
```

# Symbol table

Functions:

`initialize` an *empty table*;

`insert` a pair *identifier e information*;

`lookup` given an *identifier* returns the *information*

Use *tables* built-in in your programming language. Examples:

- ▶ Map in Java
- ▶ Data.Map in Haskell
- ▶ dict in Python
- ▶ `std::map` in C++



## Symbol table (cont.)

New operations to deal with scopes:

`open` a new scope (i.e. in the beginning of a function/method)

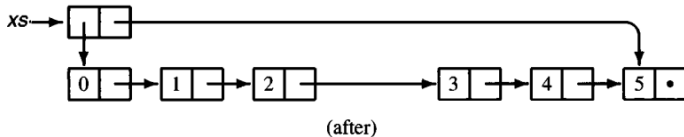
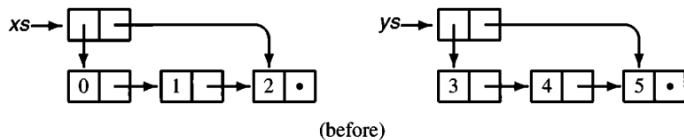
`close` finishes the actual scope

Note: **it is not sufficient to delete information** when closing the scope (we need to reconstruct the table as it was before).

# Implementation

C, Java, etc.

```
xs = new List(0,1,2);  
ys = new List(3,4,5);  
xs.append(ys);
```



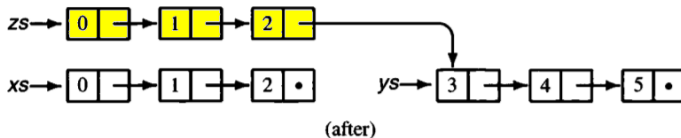
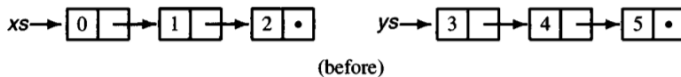
# Implementation (cont.)

Haskell, SML, etc.

`xs = [0,1,2]`

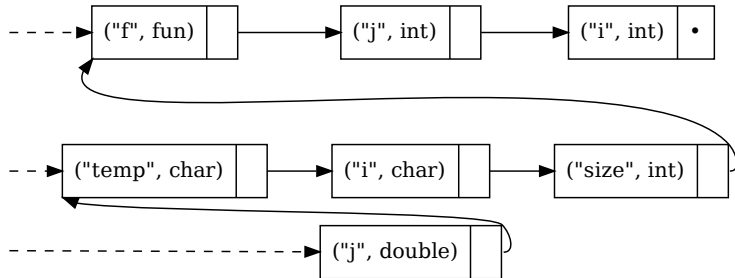
`ys = [3,4,5]`

`zs = xs ++ ys`



## Types (with lists)

```
int i, j;  
int f(int size)  
{ char i, temp;  
  ...  
  { double j;  
    ...
```



## Types (with a stack)

Opera de forma similar às listas funcionais.

`init` an empty stack;

`insert` push (*name,info*)

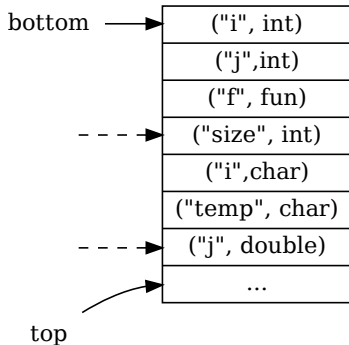
`lookup` pop;

`open scope` store the top of the stack;

`close scope` load the previous top of the stack.

## Types (with a stack) (cont.)

```
int i, j;  
int f(int size)  
{ char i, temp;  
  ...  
  { double j;  
    ...
```



- ▶ Lists and stacks use **sequential search**:  $O(n)$  for a table with  $n$  elements
- ▶ Not efficient!
- ▶ Alternatives: **search trees** or **hash tables**

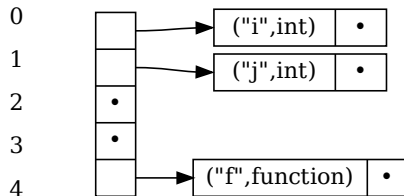
- ▶ Based on a **total order on keys** ( $>$ ,  $<$ ,  $==$ )
- ▶ AVL or Red-Black trees are  $O(\log n)$  in the worse case



# Hash tables

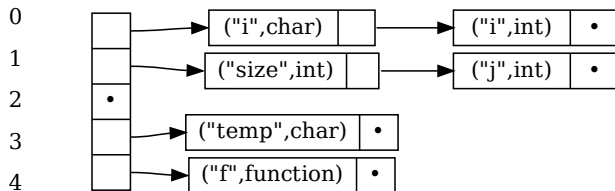
Exemplo:

- ▶ Hash table with  $N = 5$  *buckets* and 3 entries (i,j,f)
- ▶ Suppose that  $h(i) = 0$ ,  $h(j) = 1$  e  $h(f) = 4$
- ▶ No collisions: each *bucket* has one entry



## Hash tables (cont.)

- ▶ Insert new entries for `i`, `size` and `temp`
- ▶ **Collisions** for (`i`) and suppose that:  $h(\text{size}) = h(j) = 1$
- ▶ We solve collisions putting the new entries at the beginning:



- ▶ Search from the beginning of each list
- ▶ Closing the scope removes the entries

How to choose a good *hash function*?

$$x = x_0x_1 \dots x_{k-1}$$

- ▶ There are lots of different heuristics depending on the *trade-offs* (speed / collisions)
- ▶ One simple solution: sum the character codes multiplied by powers of  $\alpha$

$$h(x) = (x_0\alpha^{k-1} + x_1\alpha^{k-2} + \dots + x_{k-1}\alpha^0) \bmod N$$

Choose an  $\alpha$  with a 2 exponent: multiplications may be implemented by *shifts*

## Hash tables (cont.)

Example ( $\alpha = 2^4 = 16$ ).

```
#define N ...
```

```
unsigned hash(char *ptr) {  
    unsigned h = 0;  
    while(*ptr) {  
        h = (h<<4) + (unsigned)(*ptr++);  
    }  
    return (h % N);  
}
```

# Symbol Table - Example

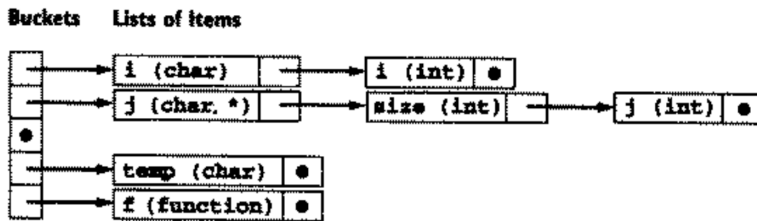
Consider the following C code fragment illustrating nested scopes:

```
int i,j;

inf f(int size)
{ char i, temp;
  ...
  { double j;
    ...
  }
  ...
  { char *j;
    ...
  }
}
```

# Symbol Table - Example

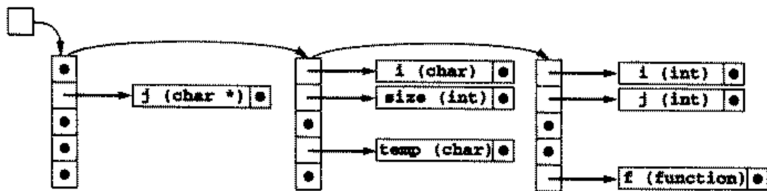
Symbol table contents:



After processing the declaration of the second nested compound statement within the body of f

# Separate Symbol Tables

Symbol table structure:



Using separate tables for each scope - corresponding to the same example)

# This lecture

Semantic analysis

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**Type Systems**

Type Checking

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**Type System** A set of **logical rules** which programs must respect.

Exemples:

- ▶  $+$ ,  $-$ ,  $*$ ,  $/$  are only applied to numbers
- ▶ the condition in an `if` command must be a *boolean*
- ▶ On an assignment `var = expr` the *variable* `var` must have the same type as the *expression* `expr`

# Type Systems

Classification of type Systems:

**Static** type checking is done at **compile time**

vs.

**Dinamic** type checking is done at **run-time**

**Strong** type errors are **not allowed**

vs.

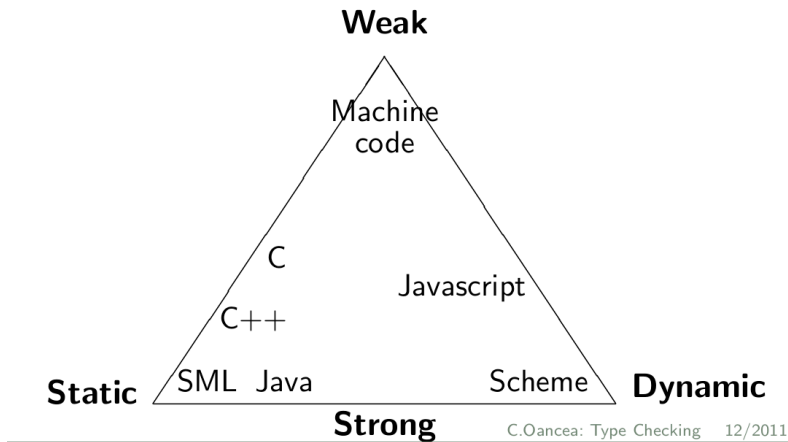
**Weak** some type errors **may be allowed**

# Type Systems (cont.)

Examples:

- ▶ Haskell, SML, Java: **static and strong** typing
- ▶ Python, Scheme: **dynamic and strong** typing
- ▶ C: **static and weak** typing
- ▶ Note that these classifications are gradual and not mandatory  
e.g. o Java type system is stronger than for C and weaker than Haskell

## Type Systems (cont.)



(Image: *Introduction to Compiler Design*, Torben Mogensen.)

# Why do we need types?

- ▶ avoids type errors at run-time
- ▶ helps the compiler to generate more efficient code
- ▶ helps the programmer to detect bugs (a first program verification technique)

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# Attribute Grammars

- ▶ Type checking may be made by traversing the AST (one or more times) and may make several passes over this
- ▶ Each pass is a recursive walk over the AST gathering information or using information gathered in previous passes: such information is called *attributes* of the AST
- ▶ The compiler builds **node attributes**; examples:
  - ▶ Types;
  - ▶ Symbol Table (**context**);
  - ▶ Values of expressions;
  - ▶ Target code
- ▶ **Synthesized attributes**: bottom-up from the leaves up to the root
- ▶ **Inherited attributes**: top-down, passed downwards the AST
- ▶ Attributes maybe synthesized and inherited  
(e.g. the symbol table is synthesized on the variable declarations and inherited on expressions)

# Expressions

- ▶ A language with *variables*, *arithmetic expressions* and *boolean expressions*
- ▶ Types: `int` (integer numbers) e `bool` (boolean values)

Examples:

$1+2*3$

$(1+2)<3$

$1+x*3$       (*valid if  $x$  has type `int`*)

$(1+x)<y$       (*valid if  $x$  and  $y$  have type `int`*)

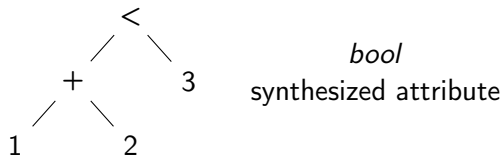
A **type error**:

$1+(2<3)$

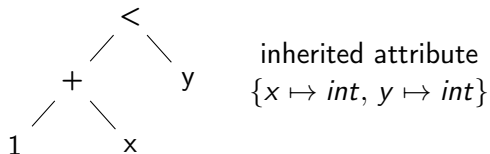


# Inherited and Synthesized Attributes

We calculate the type of an expression from the type of its sub-expressions (**synthesized attribute**).



We use a symbol table with the types of variables (**inherited attribute**).



# Type Checking

Grammar Rule	Semantic Rules
$decl \rightarrow type\ var\text{-}list$	
$type \rightarrow \mathbf{int}$	$dtype = integer$
$type \rightarrow \mathbf{float}$	$dtype = real$
$var\text{-}list_1 \rightarrow \mathbf{id}, var\text{-}list_2$	$insert(\mathbf{id}.name, dtype)$
$var\text{-}list \rightarrow \mathbf{id}$	$insert(\mathbf{id}.name, dtype)$

(Attribute Grammar for Type Declarations)

# Type Checking

Grammar Rule	Semantic Rules
$\text{var-decl} \rightarrow \text{id} : \text{type-exp}$	$\text{insert}(\text{id.name}, \text{type-exp.type})$
$\text{type-exp} \rightarrow \text{int}$	$\text{type-exp.type} := \text{integer}$
$\text{type-exp} \rightarrow \text{bool}$	$\text{type-exp.type} := \text{boolean}$
$\text{type-exp}_1 \rightarrow \text{array} \quad [\text{num}] \text{ of type-exp}_2$	$\text{type-exp}_1.\text{type} :=$ $\text{makeTypeNode}(\text{array}, \text{num.size}, \text{type-exp}_2.\text{type})$
$\text{stmt} \rightarrow \text{if exp then stmt}$	<b>if not</b> $\text{typeEqual}(\text{exp.type}, \text{boolean})$ <b>then</b> $\text{type-error}(\text{stmt})$
$\text{stmt} \rightarrow \text{id} := \text{exp}$	<b>if not</b> $\text{typeEqual}(\text{lookup}(\text{id.name}), \text{exp.type})$ <b>then</b> $\text{type-error}(\text{stmt})$
$\text{exp}_1 \rightarrow \text{exp}_2 + \text{exp}_3$	<b>if not</b> ( $\text{typeEqual}(\text{exp}_2.\text{type}, \text{integer})$ <b>and</b> $\text{typeEqual}(\text{exp}_3.\text{type}, \text{integer})$ ) <b>then</b> $\text{type-error}(\text{exp}_1)$ ; $\text{exp}_1.\text{type} := \text{integer}$

(Attribute Grammar for Types)

# Type Checking

$exp_1 \rightarrow exp_2 \text{ or } exp_3$	<b>if not</b> ( $typeEqual(exp_2.type, boolean)$ <b>and</b> $typeEqual(exp_3.type, boolean)$ ) <b>then</b> $type-error(exp_1)$ ; $exp_1.type := boolean$
$exp_1 \rightarrow exp_2 [ exp_3 ]$	<b>if</b> $isArrayType(exp_2.type)$ <b>and</b> $typeEqual(exp_3.type, integer)$ <b>then</b> $exp_1.type := exp_2.type.child1$ <b>else</b> $type-error(exp_1)$
$exp \rightarrow num$	$exp.type := integer$
$exp \rightarrow true$	$exp.type := boolean$
$exp \rightarrow false$	$exp.type := boolean$
$exp \rightarrow id$	$exp.type := lookup(id.name)$

(Attribute Grammar for Types)

# Implementation (two phases)

1. Fill the symbol table with type declarations (visitor which builds the symbol table)
  - 1.1 variables bound with their types
  - 1.2 method names bound to their parameters, result type and local variables
  - 1.3 class names bound to their variable and method declarations
2. Type check expressions and statements (visitor which type checks)

## Implementation (example)

```
// PlusExp e1,e2;

public Type visit(Plus n) {
    if (! (n.e1.accept(this) instanceof IntegerType) )
        error.complain("Left side of Plus must be of type integer");
    if (! (n.e2.accept(this) instanceof IntegerType) )
        error.complain("Right side of Plus must be of type integer");
    return new IntegerType();
}
```

# Type Declarations

- ▶ Type declarations add new information to the symbol table: (Identifier i, Type t)

```
public void visit(VarDecl n) {
    Type t = n.t.accept(this);
    String id = n.i.toString();

    if (currMethod == null) {
        if (!currClass.addVar(id,t))
            error.complain(id + "is already defined in " + currClass.getId());
        } else if (!currMethod.addVar(id,t))
            error.complain(id + "is already defined in "
                + currClass.getId() + "." + currMethod.getId());
    }
}
```

## Type Declarations (cont.)

```
class ErrorMsg {  
    boolean anyErrors;  
    void complain(String msg) {  
        anyErrors = true;  
        System.out.println(msg);  
    }  
}
```



# Type Checking for Commands

**Assignment** ( $var := expr$ ) is well-typed if the type declaration for  $var$  is the type of  $expr$

**Conditional** ( $if\ cond\ then\ e1\ else\ e2$ ) is well-typed if:

1.  $cond$  must have type `bool`
2.  $e1$  and  $e2$  must have the same type

**Conditional** ( $if\ cond\ then\ expr$ ) is well-typed if:

1.  $cond$  must have type `bool`
2.  $expr$  must be well-typed

**While** ( $while\ cond\ expr$ ) is well-typed if::

1.  $cond$  must have type `bool`
2.  $expr$  must be well-typed

**Sequence** ( $e1; e2$ ) is well-typed if  $e_1$  and  $e_2$  are well-typed

# Type Checking for Functions

- ▶ Let us extend the language with **function definitions and function calls**
- ▶ Functional types:

$$(t_1, t_2, \dots, t_n) \rightarrow r$$

(they can be trivially reconstructed by the type declarations for arguments and return values)

- ▶  $t_1, t_2, \dots, t_n$  are the types of **function arguments**
- ▶  $r$  is the **type of the result value**

# Function calls

To type check a function call  $f(e_1, \dots, e_n)$

1. lookup for  $f$  in the symbol table and get a functional type  $(t_1, \dots, t_n) \rightarrow r$
2. type check  $e_1, \dots, e_n$
3. if the types are equal to types  $t_1, \dots, t_n$  return type  $(r)$ ; otherwise return a type error

# Function Definition

To type check  $f(x_1 : t_1, \dots, x_n : t_n) : r = e$

1. Add the new binding  $\{x_1 \mapsto t_1, \dots, x_n \mapsto t_n\}$  to the symbol table
2. Using this new symbol table type check  $e$
3. If the type of  $e$  is equal to  $r$  return a new symbol table with

$$\{f \mapsto (t_1, \dots, t_n) \rightarrow r\}$$

Otherwise return a type error.

(Note: the symbol table in this case is an *inherited* and *synthesized* attribute)

# Recursive Functions

- ▶ This type checking algorithm does not work with *recursive calls*
- ▶ The solution to this problem is simple: add an entry for  $f$  to the symbol table used to type check the body of the function.

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# Overloading and coercion

**Overloading** Use the *same operator* applied to different types (e.g. + for integers and reals)

```
1 + 2      -- int
1.0 + 2.5  -- float
```

**Coercion** Type conversion

```
int x = ...;
(float)x + 2.5  -- explicit coercion
x + 2.5         -- implicit coercion
```

## Overloading and coercion (cont.)

- ▶ Type checking is trivial for built-in operators (e.g. C, Pascal)
- ▶ More (much more!) complex if the programmer may define operators for new types (e.g. C++, Haskell, ...)



# Polymorfism

*polymorphic: something which has several forms.*

In programming languages: the possibility of writing programs which **work for different types**

**Parametric Polymorphism** SML/Haskell or “generics” in Java/C#

```
reverse :: [t] -> [t]           -- em Haskell  
void reverse(List<T> list);     // em Java
```

**Ad-hoc Polymorphism** *overloading*, interfaces, inheritance in OO languages...

# Type Inference

- ▶ For some type systems it is possible to automatically **infer the types** instead of just doing **type checking**
- ▶ Strongly typed functional languages (Haskell, ML) have type inference (*Damas-Milner* type inference algorithm)