# SeleDiff Manual

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# Contents

1	Intr	roduction	1					
	1.1	1 Basic Model						
	1.2	Correction for Admixed Populations	1					
		1.2.1 Estimate Admixed Proportion	2					
		1.2.2 Estimate Allele Frequencies in Missing Parental Populations	2					
2	Usa	nges	3					
	2.1	Environment Setting	3					
	2.2	Input Files	5					
		2.2.1 EIGENSTRAT	5					
		2.2.2 Oxford GEN/SAMPLE	6					
		2.2.3 HAPS/SAMPLE	7					
		2.2.4 Ancestral Allele File	7					
		2.2.5 Divergence Time File	7					
		2.2.6 Admixed Population File	8					
		2.2.7 Haplotype File	8					
	2.3	Output File	8					
3	Exa	amples	9					
	3.1	Estimate Selection Coefficient Differences in SNPs	9					
	3.2	Estimate Selection Coefficient Differences in Haplotypes	10					
4	Dep	pendencies	10					
5	Ref	erences	10					

# 1 Introduction

SeleDiff is implemented with a probabilistic method for testing and estimating selection coefficient differences between populations<sup>1</sup>.

#### 1.1 Basic Model

Let  $\Phi$  denote the difference of selection between population A and B, i.e.,  $\Phi = s_A - s_B$ , then

$$\hat{\Phi} = E(s_A - s_B) = \frac{\log(\text{Odds})}{t}$$

where  $s_A$  and  $s_B$  are the selection coefficients in population A and B respectively, t is the divergence time between A and B, and  $Odds = \frac{C_{A,m}C_{B,m}}{C_{A,w}C_{B,m}}$  (For more details, please see [1]),  $C_{A,m}$  denotes the count of derived allele in population A,  $C_{A,w}$  denotes the count of ancestral allele in population A,  $C_{B,m}$  denotes the count of derived allele in population B,  $C_{B,w}$  denotes the count of ancestral allele in population B.

The variance of  $\Phi$  could be calculated as

$$\mathrm{Var}(\Phi) = \frac{\mathrm{Var}[\log(\mathrm{Odds})]}{t^2} + \mathrm{Var}(\Omega)$$

where  $\Omega$  is the general effect of genetic drift between population A and B.

Therefore, when a sample has n neutral loci and n is large, the variance of  $\Omega$  can be estimated as

$$\hat{\mathrm{Var}}(\Omega) = \mathrm{median}\left(\frac{\hat{\Phi}^2(i)}{0.455} - \frac{\mathrm{Var}[\log(\mathrm{Odds}_i)]}{t^2}\right), n \ge i \ge 1$$

where the variance of log-odds ratio could be effectively approximated as

$$Var[log(Odds)] = \frac{1}{C_{A,m}} + \frac{1}{C_{A,w}} + \frac{1}{C_{B,m}} + \frac{1}{C_{B,w}}$$

When C < 5, we do corrections as C' = C + 0.5.

The statistic for natural selection of a candidate locus is

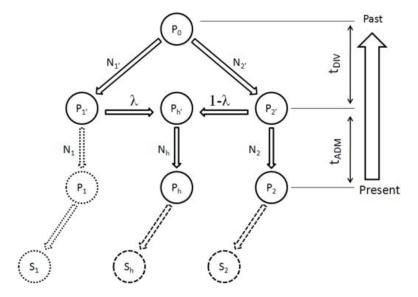
$$\delta = \frac{\hat{\Phi}^2}{\operatorname{Var}(\hat{\Phi})}$$

Under the null hypothesis that differences in natural selection are absent, the statitics  $\delta$  follows a central chi-square distribution with a degree of freedom = 1. Under the alternative hypothesis with a selection difference the statistic  $\delta$  has a noncentral chi-square distribution with non-centrality parameter  $\hat{\Phi}^2$  and a degree of freedom = 1.

### 1.2 Correction for Admixed Populations

In the basic model, we assume no gene flow in population A and B. When at least one population is admixed, we have to estimate the admixture proportion and use its parental populations instead.

We assume an admixture model as shown in the figure in below. An ancestral population  $P_0$  is split into two parental populations,  $P_{1'}$  and  $P_{2'}$  (with effective sizes  $N_{1'}$  and  $N_{2'}$ , respectively), which evolve independently for  $t_{\text{DIV}}$  generations before they contribute genes of proportion  $\lambda$  and  $1 - \lambda$  to form the hybrid population,  $P_{h'}$  with effective sizes  $N_1$ ,  $N_2$  and  $N_h$ , respectively, and evolve independently for  $t_{\text{ADM}}$  generations before a sample  $(S_i, j = 2, h)$  is taken from each of them.<sup>2</sup>



#### 1.2.1 Estimate Admixed Proportion

We estimate admixed proportion for neutral locus i in the admixed population  $P_h$  with n loci as

$$\lambda_i = \frac{f_{ih} - f_{i2}}{f_{i1} - f_{i2}}$$

where  $f_{ij}(j = 1, 2, h)$  is the allele frequency of locus i in population j.

The overall admixed proportion from population  $P_1$  is estimated as

$$\hat{\lambda} = \text{mean}(\lambda_i)$$

#### 1.2.2 Estimate Allele Frequencies in Missing Parental Populations

When population  $P_1$  is missing, we estimated allele frequency of each SNP in admixed population using an maximum likelihood method. Given a genetic contribution  $\lambda$  and current observation  $C_{j2}$  and  $C_{jh}$  on locus j for population  $P_2$  and  $P_h$ , allele frequency  $f_{j1'}$  in the missing ancestral population  $P_{1'}$  could be estimated when the recent effective population sizes  $(N_h$  and  $N_2)$  are large and the admixture event is relatively young.<sup>3</sup>

Given the current observation  $C_j(C_{j2}, C_{jh})$  and sample size  $S(S_2, S_h)$ , we have the probability of observation

$$P(C_{j2}, C_{jh}|f_{j2}, f_{jh}, S_2, S_h) \approx \binom{S_h}{C_{jh}} f_{jh'}(1 - f_{jh'}) \binom{S_2}{C_{j2}} f_{j2'}(1 - f_{j2'})$$

Maximize the probability  $P(C_{j2}, C_{jh}|f_{j2}, f_{jh}, S_2, S_h)$ , we have estimation for the allele frequency in missing parental population  $f_{j1}$  by

$$\hat{f_{j1}} = \max\left(0, \min\left(\frac{C_{jh}/S_h - (1-\lambda)C_{j2}/S_2}{\lambda}, 1\right)\right)$$

Suppose we want to compare population  $P_1$  with another population  $P_3$  that is without admixture. Then

$$Var[log(Odds)] = Var \left[ log \left( \frac{f_{j1}}{1 - f_{j1}} \right) \right] + Var \left[ log \left( \frac{f_{j3}}{1 - f_{j3}} \right) \right]$$

Use  $\Delta$ -method<sup>4</sup>,

$$\begin{aligned} \operatorname{Var}\left[\log\left(\frac{f_{j1}}{1-f_{j1}}\right)\right] &\approx \operatorname{Var}\left(\frac{f_{j1}}{1-f_{j1}}\right) \left[1/\operatorname{E}\left(\frac{f_{j1}}{1-f_{j1}}\right)\right]^{2} \\ &\approx \frac{\operatorname{E}^{2}(f_{j1})}{\operatorname{E}^{2}(1-f_{j1})} \left[\frac{\operatorname{Var}(f_{j1})}{\operatorname{E}^{2}(1-f_{j1})} - 2\frac{\operatorname{Cov}(f_{j1},1-f_{j1})}{\operatorname{E}(f_{j1})\operatorname{E}(1-f_{j1})} + \frac{\operatorname{Var}(1-f_{j1})}{\operatorname{E}^{2}(1-f_{j1})}\right] \left[1/\operatorname{E}\left(\frac{f_{j1}}{1-f_{j1}}\right)\right]^{2} \\ &= \left(\frac{1}{\operatorname{E}(f_{j1})} + \frac{1}{\operatorname{E}(1-f_{j1})}\right)^{2} \operatorname{Var}(f_{j1}) \\ &= \frac{\operatorname{Var}(f_{j1})}{\operatorname{E}^{2}(f_{j1})\operatorname{E}^{2}(1-f_{j1})} \end{aligned}$$

where

$$\operatorname{E}(f_{j1}) = \hat{f}_{j1}$$

$$\operatorname{Var}(f_{j1}) = \frac{1}{\lambda^2} \left[ \frac{C_{jh}(S_h - C_{jh})}{S_h^3} + (1 - \lambda)^2 \frac{C_{j2}(S_2 - C_{j2})}{S_2^3} \right]$$

While

$$\operatorname{Var}\left[\log\left(\frac{f_{j3}}{1 - f_{j3}}\right)\right] = \frac{1}{C_{j3}} + \frac{1}{S_3 - C_{j3}}$$

where  $C_{i3}$  is the observation in population  $P_3$  and  $S_3$  is the sample size of  $P_3$ .

# 2 Usages

#### 2.1 Environment Setting

To use SeleDiff, you should install Java SE Runtime Environment 8 first.

After the installation, you can check Java version in the command line (command starts by ">" prompt).

```
> java -version
java version "1.8.0_25"
Java(TM) SE Runtime Environment (build 1.8.0_25-b17)
Java HotSpot(TM) 64-Bit Server VM (build 25.25-b02, mixed mode)
```

Once you have installed Java SE Runtime Environment 8, you can run SeleDiff without any parameter in the command line to look at help information.

```
> java -jar SeleDiff.jar
Usage: SeleDiff [options]
  Options:
    --admixed-population
       A file specifies admixed population.
    --all-gen
       A Oxford GEN file contains all the sample SNPs' information and genotype
       data.
    --all-gen-threshold
       A threshold specifes the confidence of genotype in all the sample data,
       if Oxford GEN/SAMPLE format is used.
       Default: 0.9
    --all-geno
       A EIGENSTRAT GENO file contains all the sample genotype data.
    --all-haps
       A HAPS file contains all the sample SNPs' information and genotype data.
    --all-ind
       A EIGENSTRAT IND file contains all the sample individuals' information.
    --all-sample
       A Oxford SAMPLE file contains all the sample individuals' information.
   --all-snp
       A EIGENSTRAT SNP file contains all the sample SNPs' information.
  * --ancestral-allele
       A file specifies ancestral alleles.
    --candidate-gen
       A Oxford GEN file contains the candidate SNPs' information and genotype
       data.
    --candidate-gen-threshold
       A threshold specifies the confidence of genotypes in the candidate data,
       if Oxford GEN/SAMPLE format is used.
       Default: 0.9
   --candidate-geno
       A EIGENSTRAT GENO file contains the candidate genotype data.
    --candidate-haps
       A HAPS file contains the candidate SNPs' information and genotype data.
   --candidate-ind
       A EIGENSTRAT IND file contains the candidate individuals' information.
    --candidate-sample
       A Oxford SAMPLE file contains the candidate individuals' information.
    --candidate-snp
       A EIGENSTRAT SNP file contains the candidate SNPs' information.
  * --divergence-time
       A file specifies divergence time.
   --haplotype
       A file specifies haplotypes.
    --help
       Show SeleDiff's usage.
       Default: false
    --log
       Redirect log into a file.
  * --output
       The output file.
```

\* indicates required options.

# 2.2 Input Files

SeleDiff accepts 3 kinds of file formats of genetic data as inputs. They are EIGENSTRAT format, Oxford GEN/SAMPLE format and HAPS/SAMPLE format.

In order to describe each format, consider an example dataset containing 3 unrelated individuals (Ind1, Ind2 & Ind3) from 3 populations (Pop1, Pop2 & Pop3) that were typed on 3 SNPs (SNP1, SNP2 & SNP3):

```
SNP1 SNP2 SNP3
Ind1 T/T A/T T/T
Ind2 C/G C/G C/G
Ind3 C/C A/A ?/?
```

#### 2.2.1 EIGENSTRAT

For EIGENSTRAT format, there are 3 files: SNP file, IND file and GENO file.

The SNP file describes the information of each SNP. The SNP file corresponding to the example dataset is:

```
SNP1 1 0.1 100 A T
SNP2 1 0.2 101 C G
SNP3 1 0.3 103 C A
```

Each row corresponds to a SNP. The 6 columns are:

- 1. SNP ID
- 2. Chromosome number
- 3. SNP genetic position
- 4. SNP physical position
- 5. Reference allele
- 6. Alternative allele

The IND file describes the information of each individual. The IND file corresponding to the example dataset is:

```
Ind1 M pop1
Ind2 F pop2
Ind3 U pop3
```

Each row corresponds to an individual. The 3 columns are:

- 1. Individual ID
- 2. Sex: M for male, F for female and U for unknown
- 3. Population ID

The **GENO** file contains genetic data. The GENO file corresponding to the example dataset is:

010 111

209

Each row corresponds to a SNP, and each column corresponds to an individual. The characters, 0, 1, 2, 9, correspond to an individual's genotype:

- 0 means zero copies of reference allele.
- 1 means one copy of reference allele.
- 2 means two copies of reference allele.
- 9 means missing data.

### 2.2.2 Oxford GEN/SAMPLE

For Oxford GEN/SAMPLE format, there are 2 files: GEN file and SAMPLE file.

The **GEN** file describes the information of each SNPs and its genotypes. The GEN file corresponding to the example dataset is:

```
1 SNP1 100 A T 0 0 1 0 1 0 0 0 1
1 SNP2 101 C G 0 1 0 0 1 0 0 1 0
1 SNP3 103 C A 1 0 0 0 0 1 0 0
```

Each row corresponds to a SNP. The first 5 columns are:

- 1. Chromosome number
- 2. SNP ID
- 3. SNP physical position
- 4. Reference allele
- 5. Alternative allele

From the 6th column, every 3 columns correspond to 3 three probabilities of an individual's genotype (AA, AB, BB). If the largest of the probabilities is over the threshold specified by --all-gen-threshold or --candidate-gen-threshold, then the genotype corresponding to the largest probability is used for SeleDiff.

The **SAMPLE** file describes the information of each individuals. The SAMPLE file corresponding to the example dataset is:

```
ID_1 ID_2 missing sex phenotype
0 0 0 D P
Pop1 Ind1 0 M -9
Pop2 Ind2 0 F -9
Pop3 Ind3 0.33 U -9
```

The 1st and 2nd rows are headers. From the 3rd row, each row corresponds to an individual. The 5 columns are:

- 1. Population ID
- 2. Individual ID
- 3. Missing data rate
- 4. Sex
- 5. Phenotype

#### 2.2.3 HAPS/SAMPLE

For HAPS/SAMPLE format, there are 2 files: HAPS file and SAMPLE file.

The **HAPS** file describes the information of each SNPs and its genotypes. The HAPS file corresponding to the example dataset is:

```
1 SNP1 100 A T 1 1 0 1 1 1 1 SNP2 101 C G 0 1 0 1 0 1 1 1 SNP3 103 C A 0 0 1 1 9 9
```

Each row corresponds to a SNP. The first 5 columns are the same as those in Oxford GEN file.

From the 6th column, every two columns correspond to an individual's genotype. The characters, 0, 1, 9, correspond to alleles of a SNP:

- 0 means reference allele
- 1 means alternative allele
- 9 means missing data

The **SAMPLE** file is the same as the Oxford SAMPLE file.

#### 2.2.4 Ancestral Allele File

SeleDiff uses --ancestral-allele option (required) to accept a *TAB* delimited file that specifies the ancestral allele of each SNP in the data. The content of the file looks like:

```
rsID Ancestral Allele rs001 A rs002 G ....
```

The first line is a header which will be skipped by SeleDiff.

#### 2.2.5 Divergence Time File

SeleDiff uses --divergence-time option (required) to accept a TAB delimited file that specifies divergence time between two populations.

```
Population1 Population2 Time(generations)
EastAfrica WesAfrica 2000
EastAfrica EastSouthasia(EastAsia) 3600
...
```

The first line is a header which will be skipped by SeleDiff. Here, EastSouthasia is a admixed population. We estimate and use its missing parental population in East Asia instead.

#### 2.2.6 Admixed Population File

SeleDiff uses --admixed-population option to accept a TAB delimited file that specifies admixed populations in the data. The content of the file looks like:

```
Population1 Population2 Desc
EastAsia Europe EastSouthasia
EastAsia Europe CentralAsia
```

The first line is a header which will be skipped by SeleDiff. The first two columns (e.g., EastAsia and Europe) are the parental populations we can sample in the present time. The third column (e.g. CentralAsia) is the admixed population. You can find admixture proportions in the log generated by SeleDiff.

#### 2.2.7 Haplotype File

SeleDiff uses --haplotype option to accept a TAB delimited file that specifies haplotypes in the data. The content of the file looks like:

```
rs001 rs002
rs001 rs003 rs004
```

Each row represents a haplotype.

# 2.3 Output File

The output file from SeleDiff is TAB delimited. The first row is a header that describes the meaning of each column.

Column	Column Name	Description
1	SNP ID/Haplotype ID	The name of a SNP/haplotype
2	Ancestral Allele	The ancestral allele of a SNP/haplotype
3	Derived Allele	The derived allele of a SNP/haplotype
4	Population1	The first population's ID
5	Ancestral Allele Count	The count of the ancestral allele in the first population
6	Derived Allele Count	The count of the derived allele in the first population
7	Population2	The second population's ID
8	Ancestral Allele Count	The count of the ancestral allele in the second population
9	Derived Allele Count	The count of the derived allele in the second population
10	Selection Coefficient Difference	The selection coefficient difference between the first
	(Population1 - Population2)	and second populations
11	Std	The standard deviation of the selection coefficient difference
12	95% Confidence Interval	95% confidence interval of the selection coefficient difference
13	Divergence Time	The divergence time between the first and second populations
14	log(Odds Ratio)	The logarithm of Odds Ratio
15	Var(log(Odds Ratio))	The variance of the logarithm of Odds Ratio
16	Population Variance	The drift strength $\hat{\text{Var}}(\Omega)$ between the first and second
		populations without dividing the square of divergence time
17	Delta	The $\delta$ statistic for selection difference
18	p-value	The p-value of the $\delta$ statistic

Note: For a admixed population, the allele counts of its missing parental populations are estimated by their estimated allele frequecies multiply by 1000 (See Introduction section for estimating allele frequencies in missing parental populations).

# 3 Examples

Here is an example to show how SeleDiff tests and estimates selection coefficient differences between populations. 5 populations (YRI, CEU, CHB, CHD, ASW) from HapMap3 (release3) were extracted. CHB and CHD were merged into one population called CHS. Correlated individuals and SNPs which major allele frequencies are less than 0.05 were removed by PLINK 1.07(--geno 0.01 --maf 0.05). SNPs in strong linkage disequilibrium were removed, applying a window of 50 SNPs advanced by 5 SNPs and r<sup>2</sup> threshold of 0.01 (--indep-pairwise 50 5 0.01) in PLINK. All the genetic data are stored in EIGENSTRAT format.

#### 3.1 Estimate Selection Coefficient Differences in SNPs

The SNP rs12913832 in gene *HERC2* is associated with blue/non-blue eyes. Its ancestral allele is A and its derived allele is G. The SNP rs1800407 in gene *OCA2* is also associated with blue/non-blue eyes. Its ancestral allele is C and its derived allele is T. The ancestral allele information is stored in examples/ancestral\_alleles.tsv.

The counts of alleles in our example data were summarized in below.

SNP ID	Population	Ancestral Allele Count	Derived Allele Count
rs12913832	YRI	294	0
rs12913832	CEU	47	177
rs12913832	CHS	491	1
rs1800407	YRI	290	0
rs1800407	CEU	207	17
rs1800407	CHS	486	4

We assume the divergence time of YRI-CEU and YRI-CHS are both 3600 generations, while the divergence time of CEU-CHS is 2000 generations. This information is stored in examples/divergence\_times.tsv.

To estimate selection coefficient differences, in the command line, we type

```
> java -jar SeleDiff.jar --all-geno example.geno --all-ind example.ind --all-snp example.snp \
    --candidate-geno example.candidate.geno --candidate-ind example.candidate.ind \
    --candidate-snp example.candidate.snp --ancestral-allele ancestral_alleles.tsv \
    --divergence-time divergence_times.tsv --output example.result.tsv
```

The result is stored in examples/example.result.tsv. The main result is in below.

SNP ID	Population1	Population2	Selection Coefficient Difference	Std	delta	p-value
rs12913832	YRI	CEU	-0.00214	3.96E-4	16.57374	4.7E-5
rs12913832	YRI	CHS	-1.63E-4	$4.54\mathrm{E}\text{-}4$	0.079586	0.777859
rs12913832	CEU	CHS	0.003558	4.17E-4	30.083597	0.0
rs1800407	YRI	CEU	-0.001073	3.99E-4	4.127239	0.042198
rs1800407	YRI	CHS	-4.67E-4	4.15E-4	0.730705	0.392655
rs1800407	CEU	CHS	0.001091	2.68E-4	3.733448	0.053333

From the result, we can see the selection coefficient of rs12913832 in CEU is significantly higher than that in YRI or CHS, which indicates rs12913832 is under positive selection in CEU. While the selection coefficient of rs1800407 in CEU is marginal significantly higher than that in YRI or CHS.

When estimating selection coefficient differences in admixed populations, we have to correct for its admixed proportions from parental populations. In our example, ASW is an admixed population. We assume its parental populations are YRI and CEU. This information is stored in examples/admixed\_populations.tsv.

To estimate selection coefficient differences, we have to use --admixed-population to specify the information of admixed populations. In the command line, we type

```
> java -jar SeleDiff.jar --all-geno example.geno --all-ind example.ind --all-snp example.snp \
    --candidate-geno example.candidate.geno --candidate-ind example.candidate.ind \
    --candidate-snp example.candidate.snp --ancestral-allele ancestral_alleles.tsv \
    --divergence-time admixed_divergence_times.tsv --admixed-population admixed_populations.tsv \
    --output example.admixed.result.tsv
```

From the log information generated by SeleDiff, we can see the admixed proportion of ASW from YRI is approximately equal to 0.8. The result is stored in examples/example.admixed.result.tsv.

# 3.2 Estimate Selection Coefficient Differences in Haplotypes

It was reported that the derived allele of rs1800407 increased the penetrance of the blue eye phenotype associated with the derived allele of rs12913832. We used IMPUTE2 to phase chromosome 15 (-phase -int 24e6 27e6 -Ne 10000 -m genetic\_map\_chr15\_combined\_b36.txt) in our example data and stored the phased data in examples/example.candidate.chr15.phased.haps and examples/example.candidate.chr15.phased.sample. The genetic map is downloaded from IMPUTE2. We specified the haplotype by the haplotype list file, which is stored in examples/haplotype.list.

To estimate selection coefficient differences, we have to store candidate data in HAPS/SAMPLE format and use --haplotype to specify the information of haplotypes. In the command line, we type

```
> java -jar SeleDiff.jar --all-geno example.geno --all-ind example.ind --all-snp example.snp \
    --candidate-geno example.candidate.geno --candidate-ind example.candidate.ind \
    --candidate-snp example.candidate.snp --ancestral-allele ancestral_alleles.tsv \
    --divergence-time divergence_times.tsv --haplotype haplotypes.list --output example.result
```

The result is stored in examples/example.hap.result.tsv. As the result indicates, the derived haplotypes have signature of positive selection in CEU population.

# 4 Dependencies

- Java 1.8
- Apache Commons Math 3.5
- JCommander 1.48

## 5 References

1 Yungang He, Minxian Wang, Xin Huang, Ran Li, Hongyang Xu, Shuhua Xu and Li Jin. A Probabilistic Method for Testing and Estimating Selection Differences Between Populations. *Genome Research*, 25:1903-1909, 2015.

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