# Package 'tensorMam'

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<b>Description</b> A tensor Estimation approach to multivariate additive models. The B-splines are used to approximate unknown function. The number of predictors can be diverged as sample size increases, in which the penalty LASSO, MCP or SCAD can be used.	
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tensorMam-package	A tensor estimation approach to multivariate additive models

### **Description**

For a high-dimensional multivariate additive model (MAM) using B-splines, with or without aparsity assumptions, treating the coefficients as a third-order tensor and borrowing Tucker decomposition to reduce the number of parameters. The multivariate sparse group lasso (mcp or scad) and the coordinate descent algorithm are used to estimate functions for sparsity situation.

### **Details**

This section should provide a more detailed overview of how to use the package, including the most important functions.

### Author(s)

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### References

A tensor estimation approach to multivariate additive models.

generateData	Generate data from MAM model.	

### Description

Generate data for a high-dimensional multivariate additive model, with or without aparsity assumptions.

### Usage

```
generateData(n, q, p, s, D2, sigma2=NULL)
```

### Arguments

n	Sample size.
q	The number of responses.
р	The number of covariates.
S	The true covariates associating to response.
D2	The mode of unfolding $D_{(2)}$ .
sigma2	err variance. Default is 0.1.

### **Details**

This function gives pq functional coefficients' estimators of MAM. The singular value matrix of tensor is a  $r_1 \times r_2 \times r_3$ -tensor. We choose  $r_1$ ,  $r_2$  and  $r_3$  by BIC or CV.

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#### Value

Υ	Response, a $n \times q$ -matrix.
Χ	Design matrix, a $n \times p$ -matrix.
f0	True functions.

### References

A tensor estimation approach to multivariate additive models.

#### See Also

mam\_sparse

### **Examples**

```
# Example 1
D2 <- matrix(runif(30, 0.7, 1), 2, 15)
mydata <- generateData(200, 3, 5, 5, D2)</pre>
Y <- mydata$Y
X \leftarrow mydata$X
# Example 2
n <- 500
p <- 10
q <- 10
s <- 10
K <- 6
s0 <- s
r10=r20=r30=2
S3 \leftarrow matrix(runif(r10*r20*r30,3,7),nrow = r30)
T1 <- matrix(rnorm(s0*r10), nrow = s0)
U1 <- qr.Q(qr(T1))
T1 <- matrix(rnorm(K*r20),nrow = K)
U2 \leftarrow qr.Q(qr(T1))
T1 <- matrix(rnorm(q*r30), nrow = q)
U3 \leftarrow qr.Q(qr(T1))
D3 <- U3%*%S3%*%t(kronecker(U2,U1))
D2 <- TransferModalUnfoldings(D3,3,2,s0,K,q)
mydata <- generateData(n,q,p,s0,D2)</pre>
```

mam

Fit MAM without sparsity assumption and with fixed ranks.

### **Description**

Fit a low-dimensional multivariate additive model using B-splines, without aparsity assumptions, and given ranks given ranks  $r_1, r_2, r_3$ .

### Usage

```
mam(y, x, K = 7, r1 = NULL, r2 = NULL, r3 = NULL, SABC = NULL, degr = 3, eps = 1e-4, max_step = 20)
```

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### **Arguments**

У	A $n \times q$ numeric matrix of responses.
x	A $n \times p$ numeric design matrix for the model.
K	The number of B-spline base function, that is the plus of both degrees of base function and the number of knots. Default is 6.
degr	the number of knots of B-spline base function. Default is 3.
r1	The first dimension of single value matrix of the tensor. Default is 2.
r2	The second dimension of single value matrix of the tensor. Default is 2.
r3	The third dimension of single value matrix of the tensor. Default is 2.
SABC	A user-specified list of initial coefficient matrix of $S,A,B,C.$ By default, initial matrices are provided by random.
eps	Convergence threshhold. The algorithm iterates until the relative change in any coefficient is less than eps. Default is 1e-4.
max_step	Maximum number of iterations. Default is 20.

### **Details**

This function gives pq functional coefficients' estimators of MAM. The singular value matrix of tensor is a  $r_1 \times r_2 \times r_3$ -tensor. We choose  $r_1$ ,  $r_2$  and  $r_3$  by BIC or CV.

### Value

Dnew	Estimator of $D_{(3)}$ .
rss	Residual sum of squares (RSS).
Υ	Response $Y$ .
X	Design matrix $X$ .
Z	Design matrix of Bspline approximation.

### References

A tensor estimation approach to multivariate additive models.

### See Also

mam\_sparse

### **Examples**

```
D2 <- matrix(runif(50, 0.7, 1), 2, 25)
mydata <- generateData(200, 5, 5, 5, D2)
fit <- mam(mydata$Y, mydata$X)
Coeff <- fit$Dnew
```

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	mam_dr	Fit MAM without sparsity assumption, and with ranks selected by BIC or CV.
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### Description

Fit a low-dimensional multivariate additive model using B-splines, without aparsity assumptions, and with ranks  $r_1, r_2, r_3$  selected by BIC or CV.

### Usage

### **Arguments**

У	A $n \times q$ numeric matrix of responses.
x	A $n \times p$ numeric design matrix for the model.
method	The method to be applied to select parameters. Either "BIC" (the default), or "CV".
ncv	The number of cross-validation folds. Default is 10. If method is "BIC", ncv is useless.
K_index	A user-specified sequence of K values, where K is he number of B-spline base function. Default is $k\_index=6$ .
r1_index	A user-specified sequence of $r_1$ values, where $r_1$ is the first dimension of single value matrix of the tensor. Default is $r1\_index = 1, \cdots, \min(\log(n)\rceil, p)$ .
r2_index	A user-specified sequence of $r_2$ values, where $r_2$ is the second dimension of single value matrix of the tensor. Default is $r2\_index = 1, \cdots, \max K_index$ .
r3_index	A user-specified sequence of $r_3$ values, where $r_3$ is the third dimension of single value matrix of the tensor. Default is $r3\_index = 1, \cdots, \min(\log(n)\rceil, q)$ .
SABC	A user-specified list of initial coefficient matrix of $S$ , $A$ , $B$ , $C$ , which is a list with values $S$ , $A$ , $B$ , $C$ . By default, initial matrices are provided by random.
degr	the number of knots of B-spline base function. Default is 3.
eps	Convergence threshhold. The algorithm iterates until the relative change in any coefficient is less than eps. Default is 1e-4.
max_step	Maximum number of iterations. Default is 20.

### **Details**

This function gives pq functional coefficients' estimators of MAM. The singular value matrix of tensor is a  $r_1 \times r_2 \times r_3$ -tensor. We choose  $r_1, r_2$  and  $r_3$  by BIC or CV.

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#### Value

Dnew	Estimator of $D_{(3)}$ .
rss	Residual sum of squares (RSS).
rk_opt	The optimal parametres that slected by BIC or CV
selected	Which $\lambda$ is selection.
Υ	Response $Y$ .
Χ	Design matrix $X$ .
Z	Design matrix of Bspline approximation.

#### References

"A tensor estimation approach to multivariate additive models".

#### See Also

```
mam and mam_sparse_dr
```

### **Examples**

```
D2 <- matrix(runif(50, 0.7, 1), 2, 25)
mydata <- generateData(200, 5, 5, 5, D2)

fit <- mam_dr(mydata$Y, mydata$X)
opt <- fit$rk_opt</pre>
```

mam\_sparse

Fit MAM with sparsity assumption and fixed ranks.

### **Description**

Fit a high-dimensional multivariate additive model using B-splines, with or without aparsity assumptions, and given ranks given ranks  $r_1, r_2, r_3$ . The multivariate sparse group lasso (mcp or scad) and the coordinate descent algorithm are used to estimate functions for sparsity situation.

#### Usage

#### **Arguments**

у	A $n \times q$ numeric matrix of responses.
x	A $n \times q$ numeric design matrix for the model.
K	The number of B-spline base function, that is the plus of both degrees of base function and the number of knots. Default is 7.
degr	The number of knots of B-spline base function. Default is 3.

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r1 The first dimension of single value matrix of the tensor. Default is 2.
r2 The second dimension of single value matrix of the tensor. Default is 2.
r3 The third dimension of single value matrix of the tensor. Default is 2.

penalty The penalty to be applied to the model. Either "LASSO" (the default), "SCAD",

or "MCP".

lambda A user-specified sequence of lambda values. By default, a sequence of values of

length nlam is computed, equally spaced on the log scale.

SABC A user-specified list of initial coefficient matrix of S, A, B, C. By default, initial

matrices are provided by random.

nlam The number of lambda values. Default is 20.

lam\_min The smallest value for lambda, as a fraction of lambda.max. Default is 1e-3.

eps1 Convergence threshold. The algorithm iterates until the relative change in any

coefficient is less than eps1. Default is 1e-4.

maxstep1 Maximum number of iterations. Default is 20.

eps2 Convergence threshhold. The Coordinate descent method algorithm iterates un-

til the relative change in any coefficient is less than eps2. Default is 1e-4.

maxstep2 The maximum iterates number of coordinate descent method. Default is 20.

gamma The tuning parameter of the MCP/SCAD penalty (see details).

dfmax Upper bound for the number of nonzero coefficients. Default is no upper bound.

However, for large data sets, computational burden may be heavy for models

with a large number of nonzero coefficients.

alpha Tuning parameter for the Mnet estimator which controls the relative contri-

butions from the LASSO, MCP/SCAD penalty and the ridge, or L2 penalty. alpha=1 is equivalent to LASSO, MCP/SCAD penalty, while alpha=0 would be equivalent to ridge regression. However, alpha=0 is not supported; alpha

may be arbitrarily small, but not exactly 0.

#### Details

This function gives pq functional coefficients' estimators of MAM. The singular value matrix of tensor is a  $r_1 \times r_2 \times r_3$ -tensor. We choose  $r_1$ ,  $r_2$  and  $r_3$  by BIC or CV.

#### Value

betapath Solution path of  $\beta$ .

rss Residual sum of squares (RSS).

df Degrees of freedom.

lambda The sequence of regularization parameter values in the path.

lambda\_opt The value of lambda with the minimum BIC value.
selectedID The index of lambda corresponding to lambda\_opt.

activeA The active set. 
Dnew Estimator of  $D_{(3)}$ . 
Y Response Y. 
X Design matrix X.

Z Design matrix of Bspline approximation  $\lambda$ .

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#### References

A tensor estimation approach to multivariate additive models.

#### See Also

```
mam, mam_sparse_dr
```

#### **Examples**

```
D2 <- matrix(runif(50, 0.7, 1), 2, 25)
mydata <- generateData(200, 5, 10, 5, D2)

fit <- mam_sparse(mydata$Y, mydata$X)
Coeff <- fit$Dnew
```

mam\_sparse\_dr

Fit MAM with sparsity assumption and ranks selected by BIC or CV.

#### **Description**

Fit a high-dimensional multivariate additive model using B-splines, with or with aparsity assumptions and ranks selected by BIC or CV. The multivariate sparse group lasso (mcp or scad) and the coordinate descent algorithm are used to estimate functions for sparsity situation. The tuning parameter is selected by BIC or CV, which matchs the method of rank selection.

### Usage

### **Arguments**

у	A $n \times q$ numeric matrix of responses.
x	A $n \times q$ numeric design matrix for the model.
method	The method to be applied to select parameters. Either "BIC" (the default), or "CV".
ncv	The number of cross-validation folds. Default is $10$ . If method is "BIC", now is useless.
penalty	The penalty to be applied to the model. Either "LASSO" (the default), "SCAD", or "MCP".
K_index	A user-specified sequence of K values, where K is he number of B-spline base function. Default is $k\_index=6$ .
r1_index	A user-specified sequence of $r_1$ values, where $r_1$ is the first dimension of single value matrix of the tensor. Default is $r1\_index = 1, \cdots, min(\lceil log(n) \rceil, p)$ .
r2_index	A user-specified sequence of $r_2$ values, where $r_2$ is the second dimension of single value matrix of the tensor. Default is $r_2$ index = $1, \dots, \max_i K_i n d e x$ .

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r3\_index A user-specified sequence of  $r_3$  values, where  $r_3$  is the third dimension of single

value matrix of the tensor. Default is r3\_index=  $1, \dots, \min(\lceil \log(n) \rceil, q)$ .

lambda A user-specified sequence of lambda values. By default, a sequence of values of

length nlam is computed, equally spaced on the log scale.

SABC A user-specified list of initial coefficient matrix of S, A, B, C. By default, initial

matrices are provided by random.

nlam The number of lambda values. Default is 50.

degr The number of knots of B-spline base function. Default is degr = 3.

lam\_min The smallest value for lambda, as a fraction of lambda.max. Default is 1e-2.

eps1 Convergence threshhold. The algorithm iterates until the relative change in any

coefficient is less than eps1. Default is 1e-4.

maxstep1 Maximum number of iterations. Default is 20.

eps2 Convergence threshhold. The Coordinate descent method algorithm iterates un-

til the relative change in any coefficient is less than eps2. Default is 1e-4.

maxstep2 The maximum iterates number of coordinate descent method. Default is 20.

gamma The tuning parameter of the MCP/SCAD penalty (see details).

dfmax Upper bound for the number of nonzero coefficients. Default is no upper bound.

However, for large data sets, computational burden may be heavy for models

with a large number of nonzero coefficients.

alpha Tuning parameter for the Mnet estimator which controls the relative contri-

butions from the LASSO, MCP/SCAD penalty and the ridge, or L2 penalty. alpha=1 is equivalent to LASSO, MCP/SCAD penalty, while alpha=0 would be equivalent to ridge regression. However, alpha=0 is not supported; alpha

may be arbitrarily small, but not exactly 0.

#### **Details**

This function gives pq functional coefficients' estimators of MAM. The singular value matrix of tensor is a  $r_1 \times r_2 \times r_3$ -tensor. We choose  $r_1$ ,  $r_2$  and  $r_3$  by BIC or CV.

#### Value

Dnew Estimator of  $D_{(3)}$ .

rss Residual sum of squares (RSS).

df Degrees of freedom.

activeA The active set.

lambda The sequence of regularization parameter values in the path.

selectedID The index of lambda corresponding to lambda\_opt.

lambda\_opt The value of lambda with the minimum BIC or CV value.

RSS The values of BIC or CV, which is a vector.

rk\_opt The optimal parametres that slected by BIC or CV.

Y Response Y.

X Design matrix X.

Z Design matrix of Bspline approximation.

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#### References

A tensor estimation approach to multivariate additive models.

#### See Also

```
mam_dr, mam_sparse
```

### **Examples**

```
D2 <- matrix(runif(50, 0.7, 1), 2, 25)
mydata <- generateData(200, 5, 10, 5, D2)
fit <- mam_sparse_dr(mydata$Y, mydata$X)
opt <- fit$rk_opt</pre>
```

plotfuns

Plot the estimated curves from \codestensorMam.

#### **Description**

Plot the curves fit by mam, mam\_dr, mam\_sparse, and mam\_sparse\_dr

### Usage

```
plotfuns(fit,funTrueID)
```

### **Arguments**

fit ??????mam or mam\_sparse object. funTrueID Which function be plotted.

### Details

This function gives pq functional coefficients' estimators of MAM. The singular value matrix of tensor is a  $r_1 \times r_2 \times r_3$ -tensor. We choose  $r_1$ ,  $r_2$  and  $r_3$  by BIC or CV.

### References

A tensor estimation approach to multivariate additive models.

### See Also

mam

### **Examples**

```
## Not run:
    D2 <- matrix(runif(50, 0.7, 1), 2, 25)
    mydata <- generateData(200, 5, 5, 5, D2)
    fit <- mam(mydata$Y, mydata$X)
    plotfuns(fit, c(1,1))
## End(Not run)</pre>
```

### TransferModalUnfoldings

Transfer a tensor's modal unfoldings to another.

### Description

Transfer a tensor's modal unfoldings to another.

### Usage

```
tensorTransModeUnfold(T, d1, d2 , r1, r2, r3)
```

### Arguments

T An	node-d1-unfolding of a tensor with size $r_1 \times r_2 \times r_3$ , input unfolding
d1 An	integer, the mode of unfolding $T_{(d_1)}$
d2 An	integer, the mode of output unfolding $T_{(d_2)}$
r1 The	fist dimension of tensor
r2 The	second dimension of tensor
r3 The	third dimension of tensor

### **Details**

This function transfers an input mode-d1-unfolding  $T_{(d_1)}$  to mode-d2-unfolding  $T_{(d_2)}$ 

### Value

```
D the output mode-d2-unfolding, T_{(d_2)}
```

#### References

A tensor estimation approach to multivariate additive models.

### **Examples**

```
T <- matrix(1:24,nrow = 4)
TransferModalUnfoldings(T,1,2,4,3,2)
```

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